



Article A Method for Assessing the Impact of Changes in Demand for Coal on the Structure of Coal Grades Produced by Mines

Dariusz Fuksa 回



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Abstract: Due to the withdrawal of coal from power generation in the EU, mining companies in Poland are forced to adapt their production to the decreasing demand. Forecasting the volume of demand plays an important role in planning the volume of the mine's output. The demand for coal is constantly changing, with a downward trend. This article presents a method that allows to assess the impact of the variable demand on mine profits and on the volumes of sales of individual coal grades. The proposed method is based on the Monte Carlo simulation and on a solution consisting of the optimization of the production and sales of coal by the mining company (the SIMPLEX algorithm). By using the Monte Carlo simulation to forecast the demand, unlike other commonly used methods, a sufficiently large set of real situations that may occur in the future can be obtained. The results allow us to conclude the extent of desirable adjustment of the structure of the mine's production to the requirements of its consumers, as well as to predict in which direction these changes will proceed and with what probability. The usefulness of the developed method has been verified on the example of an existing hard coal mine.

Keywords: algorithm simplex; Monte Carlo simulation

1. Introduction

The most important external conditions determining the effectiveness of the operation and development of mines and companies exploiting resource companies include the level of demand for coal from domestic and foreign consumers. The method presented in this article, which allows to assess the impact of the variability of demand on the grade structure of the production, is presented on the example of an existing hard coal mine. However, it can be applied to any enterprise which needs to adjust its output to the quantitative and qualitative requirements of its consumers. Every activity is based on planning, and for most companies, the most important thing is to plan the volume of their production. Different approaches are used for this. However, due to its great importance for the operation of the coal company, the determination of the size of the expected demand must be based on multi-factor analyses.

In general, coal is treated as an energy medium, which is why the demand for it is determined primarily by the requirements of the power industry. In the literature you can find numerous studies on forecasts of energy demand, and related demand for coal, in various cross-sections: by country, region, economy sector or enterprise. This approach is most appropriate in relation to the planning of the energy policy of a country but, in the case considered in this publication, the forecasting of the volume of coal production for the next year is considered from the point of view of one of the coal companies competing with other groups of mines.

Forecasting demand is a difficult task, burdened with uncertainty and determined by a large number of external factors. In addition, we are dealing with seasonality (daily, weekly and annual).

Predictive models and methods can generally be divided into two groups of techniques based on artificial intelligence and on conventional (statistical) models. The first group

includes expert systems, fuzzy neural models, fuzzy inference, and neural networks. They flourished in the 1990s. Interestingly, opinions can be found in some studies and textbooks, e.g., [1,2], that there is little evidence that neural networks can excel standard prognostic methods.

The other group (statistical methods) differs from the first one by the fact that the forecast of the value of an analyzed variable is a strict mathematical combination of the previous values of this variable and of possible other values of external variables. The most commonly used are the autoregression (AR) models, linear regression models, dynamic linear and nonlinear models, ARMAX models, ARIMA models, Threshold AR models, methods based on the Kalman filter, optimization techniques and curve adjustment procedures. The interest in the statistical models stems from the fact that it is relatively easy to interpret their individual components. Another important aspect is that they have a relatively high accuracy [3–6].

The issues of coal demand forecasting can be found in the abundant scientific and educational literature. The simplest approach (forecast model) is to assume for the calculation for the planned period (next year) the same size and structure of demand as those valid for the current year (the "zero" forecast) [7]. This is a major simplification, although this forecast seems to be the most appropriate, at least in the first period of the planning of the demand (the beginning of the activity). In practice, this model is adopted when we are dealing with a slow-changing phenomenon [8].

In the area of coal demand forecasting two approaches can be distinguished in the literature: the analysis of factors determining the demand for coal and the forecasting itself. The authors of publication [9] investigated the relationship between coal consumption, gross domestic product, electric power production and population based on a vector autoregressive model and on the modified Granger causality test. Manuscript [10] analyzes the factors influencing the increase in the coal consumption in China using the Logarithmic Mean Divisia Index (LMDI) method. It was noted that the improving energy efficiency of coal-fired power generation and of the final combustion of coal was the main factor reducing the coal consumption. The authors of paper [11], analyzing the discrepancy between the increase in the demand for coal in China and the economic growth, are of a similar opinion: technological progress, change in the quality of coal, adaptation of the energy structure, change in the structure of industry, environmental management and coal dioxide emission considerations are important reasons for the change in the demand for coal.

Of the analyzed publications on the forecasting methods, paper [12] deserves attention. Its authors carried out a short-range modeling and forecasting of the aggregate monthly coal production in the USA. As a result of their research, the authors have found that the simplicity of the ARIMA and intervention models, the reality of their forecasts and the ease of updating them, make them very attractive compared to large-scale econometric models—for use in the short-term forecasting of coal output. In contrast, paper [13] determined the projected demand for coal in China using the Granger causality test. Publication [14] predicted the coal consumption in seven major Chinese coal industries based on the exponential smoothing and on the Holt–Winters model. Manuscript [15] is concerned with the forecasting of coal consumption in various sectors (transport, energy and others) in India. The authors developed a prediction model based on artificial neural networks (one-and multi-dimensional) and compared it to regression models. The conclusion is that, in most cases, the artificial neural network model gives better results.

However, the authors of publication [16], using the X-12-ARIMA procedure, predicted the demand for hard coal in Poland within a 12-month cycle.

The occurrence of seasonality in the mining industry suggests that this aspect should be taken into account in demand planning. However, due to the fact that planning the coal output of Polish mines requires annual planning, seasonality is not important in this case. Fluctuations (seasonality) in demand are included in the total annual production, and any surplus of coal, occurring in summer, is stored in dumps. In accordance with this policy, an optimization model has been developed, also based on the annual planning of coal production and sales, for the selected coal company. The necessary demand for next year was determined using the regression method. Based on time series, the trend that matched the retrospective data being analyzed was determined, and then it was extrapolated to next year.

This method was successfully verified by me on the example of this existing coal company. Of course, one can strive for the most accurate estimation of demand, if the results differ significantly from the real ones. Secondly, it would make sense to resort to advanced forecasting techniques if just one specific solution were to be developed on their basis: in this case an optimal production plan for the next year. A forecast is just a forecast, not a certainty. Even in this case, its optimistic and pessimistic (or "conservative") variants are given. However, the author's opinion, three variants—optimal, optimistic and pessimistic—are not enough. Therefore, the best solution is to include a random factor in the forecasts, on a wider scale, and to generate a fairly large set of possible demand scenarios. The proposed method generates 1000 possible plans for the production and sales of coal for the company. The number of these plans can be arbitrary, but it allows one to get reliable results. Such a large set of solutions makes it possible to estimate with what probability the mine will have consumers for its individual coal grades (and their quantities) and allows for the forecasting of which coal grades may not find consumers (and turn into an excess stock). To generate the solutions, I used the algorithm described in Section 2.2, based on the Monte Carlo simulation [17–22]. The Monte Carlo simulation turns out to be extremely useful in practical applications because it allows one to solve even very complex probabilistic problems. In addition, it reflects with high probability the events that can happen, and the large number of draws affects the quality of the estimate (certainty of the results). In addition, the advantage of the Monte Carlo method, unlike other methods, is its ability to draw a large number of demand variants at once.

In the scenario-based method, three variants are determined: optimistic, pessimistic (conservative) and the most likely (realistic). The inefficiency of this method is due to the very low probability that all the analyzed values will take the best (optimistic variant) or worst (pessimistic variant) values, and due to the limitation to just three scenarios. On the other hand, the assessment of the impact of changes in the demand for coal on the performance of a multi-company mining group or an individual mine should be analyzed for a sufficiently large set of scenarios.

When examining the sensitivity of mine production plans [23–25], it was noticed that they are very susceptible to random changes in the demand. The results obtained in the form of profit histograms revealed a lack of adjustment of the quantitative and qualitative structure of the output of some mines to the needs of the market. Therefore, the research on this issue was undertaken and the Monte Carlo method was used for this analysis.

The analyzed demand scenarios reflect real situations that may occur; hence, the results of the analysis can be helpful when planning annual production volumes for mines.

In view of the above considerations, it makes sense to use the method in this paper in the planning of the output of individual mines as well as multi-company mining organizations.

2. Materials and Methods

2.1. The Model and Method of Optimization

The starting point of the proposed method is the SIMPLEX table obtained as a result of optimizing the coal production and sales plan for a specific mathematical optimization model, using the SIMPLEX method [26–34]. The formal record of the general mathematical model of the optimization of the coal production and sales, determined by a set of limiting conditions and the assumed form of the objective function, is as follows [35]:

Objective function:

$$F = \sum_{j=1}^{p} \sum_{i=1}^{r_j} \sum_{k=1}^{m_{ij}} (c_{ijk} - kz_{ijk}) \cdot x_{ijk} - \sum_{j=1}^{p} Ks_j \to \max$$
(1)

Sales restrictions:

$$\sum_{i=1}^{r_j} \sum_{j=1}^p \sum_{k=1}^{m_{ij}} x_{ijk_n} \le Z_k \text{ for all } k,$$
(2)

$$\sum_{i=1}^{r_j} \sum_{n=1}^{m_{ij}} x_{ijk_n} \cdot b_{ijk_n} \le Qs_j \text{ for all } j, \tag{3}$$

$$\sum_{i=1}^{r_j} \beta_{ij} = 1 \text{ for all j,}$$
(4)

$$x_{iik} \ge 0,$$
 (5)

where:

 c_{iik} —the price of *ij* type of coal accepted by consumers in group *k* (PLN/Mg);

 kjz_{iik} —the variable cost of *i* type of coal for mine *j* (PLN/Mg);

 Ks_i —the fixed cost for mine *j* (PLN);

 x_{ijk} —the net amount of extracted coal of *ij* type accepted by consumers in group kn (Mg);

 Z_k —the consumer demand for group k (Mg);

 Qs_j —the total gross extraction for mine *j* (Mg);

i—the index of coal type, i = 1, 2, ..., rj;

j—the index of mine; j = 1, 2, ..., p;

 k_n —the index of consumer groups; $k = 1, 2, ..., m_{ij}$, where m_{ij} marks numerousness miscellany k_n for coal of ij type;

 b_{ii} —conversion gross/net;

 β_{ii} —the share of extracted coal of certain type against the total gross coal extracted.

As a result of the optimization, we have an optimal (from the point of view of the adopted criterion) annual plan for the production and sales of coal for a multi-mine company, broken up into the individual component mines. The software package used for the optimization maximizes the aggregate profit of the mines (Equation (1)), taking into account the quality requirements of coal users.

The developed plan for the production and sales of coal often precedes the moment when a decision will be made on its basis. It may turn out that the mathematical model with which we have described a given issue does not fully correspond to the real decisionmaking situation. In other words, the optimal solution obtained based on a mathematical model does not have to actually be the best in specific conditions (at a given moment of decision-making). The taking of more variables and limiting conditions into account boils down to developing a complex model. In general, it is a non-linear model, for which it may be practically impossible to obtain a solution. Therefore, in practice, the desired adaptation of solutions to specific conditions in which decisions will be made can be achieved by modifying optimal solutions obtained based on simplified linear models. We are talking about the use of the author's proprietary post-optimization methods. However, they are not the subject of this publication.

On the other hand, the development of the model itself and the resulting single solution are insufficient for making informed production decisions. The solution deserves, or even requires, an assessment in terms of the impact of a random factor such as, in the case of the coal mining, the variable level of demand for extracted coal. The method proposed by the author, described in Section 2.2, provides this possibility.

2.2. The Algorithm for Estimating the Impact of Random Fluctuations in Demand on the Company's Performance

The proposed method consists of reiterated determination of the optimal program for coal production and sales for different demand scenarios. The implementation of this process begins with the drawing of a demand vector (the Monte Carlo simulation) constituting a sub-vector of the right sides of the equation of the optimization model (Equation (2)). Demand sub-vectors will be a random variable with normal distribution, with the expected (nominal) value equal to the planned demand for a given period. The most likely error of the model was taken as the dispersion (standard deviation).

The author's assumption of the normal distribution of the random variable (coal demand) is due to several reasons. The normal distribution plays an important role in the statistical description of natural, industrial and other processes. Authors studying phenomena of a technical or economic nature in the broadly defined mining industry state that the phenomena are characterized by a distribution which is normal or similar to normal [36–38]. The drawing of the variants of the demand for coal is carried out using a Gaussian number generator.

The optimal solution is obtained using the SIMPLEX algorithm for each variant of a sufficiently large set of clusters of random demand. In this way, a set of production tasks and corresponding financial results for a single mine or a multi-mine company is obtained. Furthermore, additional information is obtained, such as: unused production capacity of the mine(s), the demand volumes of individual consumers (for each of the variants), the possible volume of imported coal, etc. The results are presented in the form of histograms of random fluctuations of the analyzed quantities (in this case, the demand for a specific coal grade of a specific mine). The results obtained by means of this analysis make it possible to assess the adjustment of the quantitative and qualitative structure of the mine's production to the size of the variable demand, as well as to analyze what will be the demand for a specific grade and with what probability. The feasibility of the obtained solutions is ensured by allowing the possibility of storing coal.

The algorithm of the proposed method runs in two steps (Figure 1). In the first step, the randomly selected demand vector is transferred to the original solution, thus modifying relevant attenuating variables. The smallest attenuating variable with negative value (the most unacceptable) is selected. It is then reduced to zero so as not to reduce other negative attenuating constraints. The above procedure always leads to an acceptable solution (thanks to the possibility of storing coal).

The second step is the optimization of the acceptable solution by the SIMPLEX method. The general mathematical model for optimizing the production and sales of coal (Equations (1)–(5)), after being reduced to the canonical form, is as follows:

$$A \cdot X = b \tag{6}$$

$$\max_{x} J = c^{T} \cdot X \tag{7}$$

$$X \ge 0 \tag{8}$$

where:

A—constraint matrix (simplex tableau), $A = [a_{ij}]$, (I = 1, ..., m; j = 1, ..., n);

X—vector of decision variable values together with inequality constraint slack variables;

-vector of the right-hand sides of the equation; b-

c-vector of objective function coefficients and zero coefficients for slack variables; *J*—objective function (quality coefficient).

If we have a base solution x^{B} , then the x^{B} components can be divided into two groups and written as follows [34]:

$$x^{B} = \begin{bmatrix} x_{B}^{B} \\ x_{N}^{B} \end{bmatrix}$$

$$\tag{9}$$

where:

 x_B^B —base variables ($x_B^B \ge 0$); x_N^B —non-base variables ($x_N^B = 0$).

The matrix of the limiting condition coefficients can be written as follows:

$$A = \begin{bmatrix} B N \end{bmatrix} \tag{10}$$

where:

B, *N*—sub-matrices of matrix *A*.

The base solution x^B relative to the base variables (after the substitutions and at $x^N = 0$) will take this form:

$$x^B = [B]^{-1} \cdot b \tag{11}$$

$$J = c^{BT} \cdot [B]^{-1} \cdot b \tag{12}$$



Figure 1. The flowchart of the algorithm of the proposed method.

The algorithm for bringing the acceptable solution to optimality (while maximizing the objective function) is as follows (Figure 2) [34]:

1. An assessment of the optimality of the current solution.

To check whether the acceptable solution is optimal, the so-called "optimality indicators" should be calculated. They are calculated for all the non-base variables in the SIMPLEX array (for the base variables they always equal zero). The formula for their determination is as follows:

$$z_j^B - c_j < 0 \tag{13}$$

where:

$$z_j^B = c^{BT} a_j^B \tag{14}$$

Based on the values of Equation (13), calculated for all the problem variables with a given base solution x^{B} , it is possible to determine whether or not it is the optimal solution.

In the case of maximizing the objective function, if all optimality indicators are greater than, or equal to, zero, the solution is optimal:

$$\forall \sum_{j=1,2,\dots,n} z_j^B - c_j \ge 0 \text{ gdy } f(x) \to \max$$
 (15)

2. The selection of the vector entering the base.

If the current base solution does not meet the optimality condition (Equation (15)), it becomes necessary to replace the base vectors. Finding the optimal solution consists of moving from one base to another. The selection of a new, neighboring, solution is performed by selecting a vector (accompanying the appropriate non-base variable, e.g., xk), which will be in the future database. The number, k, of the variable is determined using this Equation (16):

$$z_k^B - c_k = \min\left\langle z_j^B - c_j \middle| z_j^B - c_j < 0 \right\rangle$$
(16)

The formula is called the "entry criterion". When maximizing the objective function, we select the variable for which the optimality index has turned out to be the lowest.

3. The selection of the vector leaving the base.

Because the base is made up of more than one base variable, one needs to decide which one will not be retained in the new database. For the vector selected in the previous step, we calculate the so-called "exit quotients". It should be noted here that the method of their calculation is independent of the direction of the criterion. We remove from the base the *l*-th vector such that:

$$\min\left\langle \frac{x_i^B}{a_{ik}^B} \middle| a_{ik}^B > 0 \right\rangle = \frac{x_r^B}{a_{rk}^B}$$
(17)

If there were to be a zero or a negative value in the denominator, the exit quotients are not counted. If the result is several identical minimum exit quotients, it is best to choose the one with the largest divider.

4. The exchange of vectors in the base and the determination of the SIMPLEX array elements.



Figure 2. The SIMPLEX algorithm flowchart with the maximization of the objective function.

It is more convenient to start the determination of the elements of the SIMPLEX array from the row associated with the new base variable xk, and then proceed to the calculation of the remaining elements of the array. The principle of determination by rows

using the Jordan-Gaussian elimination method was adopted for the calculation of the remaining elements:

$$\begin{cases} a_{kj}^{B'} = \frac{a_{lj}^B}{a_{lk}^B} \\ a_{ij}^{B'} = a_{ij}^B - a_{ik}^B \cdot a_{kj}^{B'} (i \neq k) \end{cases} \quad (j = 1, 2, ..., n)$$
(18)

 w_i denotes the row of the old SIMPLEX array associated with the x_i variable and w_i' denotes the corresponding line in the new array. The second part of Equation (18) shows that the numerical process of building the array in rows can be schematically written in the form of Equation (19):

$$w_i' = w_i - a_{ik}^B \cdot w_k' \tag{19}$$

Once the new optimal solution has been obtained, the procedure starts from the beginning. Thanks to this, we get a sufficiently large set of solutions (mine production plans). The size of this set is determined by the decision-maker, by assuming the right number of draws.

Based on the algorithm described above, a software package was created. It consists of the main program, Smprand.exe, the Problem.txt file and the MPS (SIMPLEX array) file. The optimal solution of the production and sales program, namely the SIMPLEX array (MPS), is the starting point to conducting an analysis of the impact of the variable demand of coal on the efficiency of the operation of a multi-mine company.

In the Problem.txt file the name of the output file is defined, in which the set of optimal solutions, the number of the set of optimal solutions, the values of demand forecasts for all consumers and their dispersions are saved. Smprand.exe is the executable program that retrieves data from the Problem.txt file and from the MPS file.

2.3. The Algorithm for Determining the Planned Demand

The planning the coal demand for a given future period is carried out by the regression method [39]. For a sufficiently large set of retrospective data, the least squares method is used to adjust the best model for each of the groups of coal recipients. Then, according to the selected trend model, the volume of the demand from the consumers for the planned period is forecast (the author has adopted the annual planning regime). To put it simply, a trend is determined that matches the analyzed data, and then it is extrapolated to future years. The formulas of the trends proposed to extrapolate the magnitude of future demand inter alia [40,41]:

- The linear model:
- $Z = a + b \cdot t$ (20)

(21)

- The exponential model: $Z = a \cdot b^t$
 - The hyperbolic model:

$$Z = a + \frac{b}{t} \tag{22}$$

The power model:

$$Z = a \cdot t^b \tag{23}$$

The logarithmic model:

$$Z = a + b \cdot \log t \tag{24}$$

where:

- Z—demand volume (Mg/year);
- *t*—consecutive years of the analyzed period, (t = 1, 2, ..., n);
- *a*, *b*—regression coefficients.

The regression coefficients for the linear model are calculated with Equation (25):

$$b = \frac{\sum \left[\left(t_i - \overline{t} \right) \cdot \left(Z_i - \overline{Z} \right) \right]}{\sum \left(Z_i - \overline{Z} \right)^2}$$
(25)

$$a = \overline{Z} - b \cdot \overline{t} \tag{26}$$

where:

 Z_i —demand in the *i*-th year (Mg/year);

 \overline{Z} —average demand in the analyzed period (Mg/year).

The choice of the model that most faithfully reflects the development of the demand over time is made based on the correlation coefficient determined by this formula:

$$r = \frac{\sum \left[\left(t_i - \overline{t} \right) \cdot \left(Z_i - \overline{Z} \right) \right]}{\sum \left(Z_i - \overline{Z} \right)^2 \cdot \sum \left(t_i - \overline{t} \right)^2}$$
(27)

In order to obtain more accurate results, the most likely (standard) error of the forecast was taken as the dispersion. In order to estimate the forecast error, the following is performed in each instance:

- 1. Estimation of the parameters of the stochastic structure (distribution of the random component), which allow to conclude the fit of the model to the empirical data held, by determining [17,18,42–44]:
- Variance (estimator) of the residual component:

$$\sigma_r^2 = \frac{\sum_{n=1}^{N} (y_n - y_{\text{mod}})^2}{N - K}$$
(28)

where:

 y_n —actual value of endogenous factor;

 y_{mod} —model-based value of endogenous factor;

N—number of observations;

K—number of estimating parameters for model structure.

• Variance and covariance matrices:

$$K = \left[X^T \cdot X\right]^{-1} \cdot \sigma_r^2 \tag{29}$$

and

$$X = \begin{bmatrix} 1 & x_1 \\ 1 & x_2 \\ 1 & x_3 \\ -- & -- \\ 1 & x_N \end{bmatrix}$$
(30)

$$X^{T}X = \begin{bmatrix} N & \sum x_{n} \\ \sum x_{n} & \sum x_{n}^{2} \end{bmatrix}$$
(31)

2. Estimation of the variance of forecasts:

$$\sigma_{\widehat{\nu}}^2 = u \cdot K \cdot u^T \tag{32}$$

and

$$u = \begin{bmatrix} 1 & x_{n+1} \end{bmatrix}$$
(33)

where:

$$x_{n+1}$$
—time, during which prognosis is prepared.

3. Average forecast error, taking into account (6.1) and (6.4), according to the following formula:

$$\sigma_{yprog} = \sqrt{\sigma_r^2 + \sigma_{\widehat{y}}^2} \tag{34}$$

Following the proposed algorithm, for the assumed number of draws, the results presented in the form of histograms are obtained.

3. Results

The calculations were carried out for the existing coal company consisting of seven mines with different production characteristics. The breadth of this subject does not allow for its full presentation, therefore only the results obtained for one of the mines, mine "F", are presented. The production capacity of the mines with their technical and economic parameters are shown in Table 1, while their coal grades and quality parameters are provided in Table 2. Tables 3–5 characterizes the consumers of the studied company, divided into aggregated groups. To the values given in PLN their equivalent in EUR was added according to the average exchange rate of 16 September 2021 (1 EUR = 4.57 PLN).

Table 1. Technical and economic coefficients for mines.

Mines	Average Extraction	Max. Extraction	Unit Cost	Fixed Cost
WINCS	(Mg/day)	(Mg/year)	(PLN/Mg)	(%)
Mine A	5500	1,454,750	131.20 (EUR 27.71)	69.51
Mine B	3000	793,500	139.40 (EUR 30.50)	72.22
Mine C	4200	966,000	132.68 (EUR 29.03)	68.95
Mine D	12,000	2,760,000	136.50 (EUR 29.86)	73.40
Mine E	11,300	2,599,000	137.20 (EUR 30.02)	71.31
Mine F	12,800	3,385,600	138.30 (EUR 30.26)	69.37
Mine G	11,500	2,645,000	134.40 (EUR 29.41)	69.38

Table 2. Types and quality parameters of coal offered by mines.

Mines	Coal Size Crade	Coal Type Name	Share in Extraction	Calorific Value
whites	Coal Size Glade	cour type tunie	(%)	(kJ/kg)
	cobble	33	11.0	24,892
	nut coal	33	1.5	25,650
	fine coal I	33	18.2	25,904
Mine A	fine coal IIA	32.1	46.4	20,089
	fine coal II	32.1	21.8	22,056
	slurry	32.1	1.1	13,516
Min a D	fine coal II	32.1	31.0	22,142
Mine B	coking coal	34.1	69.0	28,789

Mines	Coal Size Grade	Coal Type Name	Share in Extraction	Calorific Value
WIIICS	Coar Size Grade		(%)	(kJ/kg)
Mine C	coking coal	34.1	100.0	31,552
	cobble	33	2.2	29,504
	nut coal	33	0.5	26,988
Mine D	fine coal IIA	33	40.74	22,233
	fine coal II	34.2	1.1	29,924
	coking coal	34.2	55.46	28,884
	cobble	33	7.2	31,189
	nut coal	33	1.3	29,520
	fine coal I	32.2	6.9	25,600
Mine E	fine coal IIA	32.1	51.7	20,788
	fine coal II	32.1	28.9	24,533
	slurry	-	2.9	15,722
	coking coal	34.2	1.1	28,936
	cobble	33	7.19	30,238
	nut coal	33	1.8	29,268
	fine coal I	32.2	7.19	28,780
Mine F	fine coal IIA	32.1	0.7	20,667
	fine coal II	32.1	65.04	22,813
	slurry	-	2.2	16,487
	coking coal	34.2	15.88	28,455
	cobble	33	3.49	30,283
	nut coal	33	0.5	29,934
	fine coal I	33	0.39	28,746
Mine G	fine coal IIA	33	52.9	22,720
	fine coal II	32.1	6.7	23,255
	slurry	-	1.1	18,305
	coking coal	34.2	34.92	28,941

Table 2. Cont.

 Table 3. The characteristics of the company's aggregated consumer groups.

Name of Concumer Crown		Accepted Types of Coal ¹															
Name of Consumer Group		2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
Export 1					x												
Export 2						х											
Export 3							х										
Export 4									х	х							
Export 5		х	х	х	х												
Export 6		х	х	х	х												
Export 7		х	х	х	х												
Indv. consumers 1		х	х	х	х												
Indv. consumers 2		х	х	х	х												
Cokerys 1						х	х										
Cokerys 2					х	х	х										
Cokerys 3								х	х	х	х	х					
Dust kettles		х	х	х	х	х	х	х									
Grates 1	х		х	х	х												
Grates 2	x	х	х	х	х	х	х	х	х	x	х	х	х	х	х	х	х
Chamber grates 1	х		х	х	х												
Chamber grates 2						x	x	x									

¹ see Table 5.

Name of Consumer Group			Acce	pted Ass	ortmen	t Name	2			Demand	Maximum Calorific Value	Minimum Calorific Value
	1	2	3	4	5	6	7	8	9	(Mg/year)	(kJ/kg)	(kJ/kg)
Export 1									х	24,920	29,308	25,960
Export 2									x	328,082	41,868	25,960
Export 3									x	239,015	41,868	23,027
Export 4									x	133,944	41,868	23,027
Export 5	х									243,955	29,307	25,958
Export 6		х	х							92,959	26,795	25,120
Export 7					х	х	x			1,235,013	25,120	23,027
Indv. consumers 1	х	х	х							336,714	29,307	20,934
Indv. consumers 2					х	х	x			1,368,046	25,120	20,934
Cokerys 1									x	676,323	41,868	24,900
Cokerys 2									x	81,284	41,868	24,900
Cokerys 3									x	900,676	41,868	24,900
Dust kettles					х	х	x			5,907,550	23,027	12,979
Grates 1						х	x			126,789	18,840	14,653
Grates 2						х	x	х		65,724	18,840	14,653
Chamber grates 1					х	х	x			49,299	21,771	19,259
Chamber grates 2					х	х	х			38,286	18,840	14,653

Table 4. The characteristics of the company's aggregated consumer groups.

 1 see Table 5.

Table 5. List of numbers and names of coal types.

Coal Type/Assortment Number	Coal Type Name	Assortment Name
1	31.1	cobble
2	31.2	nut coal
3	32.1	fine coal I
4	32.2	fine coal II
5	33	fine coal IIA
6	34.1	slurry
7	34.2	coking coal
8	35.1	
9	35.2A	
10	35.2B	
11	36	
12	37.1	
13	37.2	
14	38	
15	41	
16	42	
17	43	

The Appendix A contains data on the demand in the years 2010–2020 (Tables A1–A3). The demand from each aggregated consumer group (for the year 2021) was calculated based on the algorithm presented in Section 2.3 (Equations (20)–(27)). For each forecasted demand of the group of consumers, the most probable forecast error was calculated according to Equation (34). The results are summarized in Table 6.

Name of Consumer Group	Nominal Prognosis Values	Dispersion $\sigma_{\rm yprog}$
······	(Mg)	(Mg)
Export 1	24,920	1,675.30
Export 2	328,082	22,056.13
Export 3	239,015	16,068.36
Export 4	133,944	9004.69
Export 5	243,955	16,400.50
Export 6	92,959	6249.39
Export 7	1,235,013	83,026.78
Indv. consumers 1	336,714	18,924.03
Indv. consumers 2	1,368,046	81,045.96
Cokerys 1	676,323	35,788.92
Cokerys 2	81,284	4301.29
Cokerys 3	900,676	47,660.97
Dust kettles	5,907,550	312,609.30
Grates 1	126,789	6709.27
Grates 2	65,724	3477.92
Chamber grates 1	49,299	2608.74
Chamber grates 2	38,286	2025.96

Table 6. A summary of the nominal values of the forecast of the demand from the consumer groups and of the dispersion $\sigma_{yprog.}$

For example, the calculations for the "Indv. consumers 1", "Export 1" and "Export 7" groups are presented. Figure 3 illustrates the demand in the years 2010–2020 along with the trend line and the forecast value for the "Indv. consumers 1". However, these results are in Figure 4 for the Export 1, and in Figure 5 for the Export 7.



Figure 3. Demand of the "Indv. consumers 1" group in the years 2010–2020 with the forecast for 2021.



Figure 4. Demand of the "Export 1" group in the years 2014–2020 with the forecast for 2021.





The linear model with the -0.939 correlation coefficient has turned out to be the best model. The sales volume estimated on its basis, which, in effect, represents the volume of the demand from the "Indv. consumers 1" group of consumers in 2021, amounted to 336,714 Mg per year. Table 7 shows the results for the other models. However, in Tables 8 and 9 are the models that forecast the demand for "Export 1" and "Export 7", respectively.

Table 7. A summary of the regression analysis results for the domestic coal sales ("Indv. consumers 1").

Model	The Model form of the Function	Correlation Coefficient
linear	Z = -13,035.91t + 493,145.06	-0.939
exponential	$Z = 500,842.61 \times 0.968t$	-0.930
hyperbolic	$Z = 382,551.32 \times 117,938.95/t$	0.691
power	$Z = 506,073.86 \times t^{-0.13}$	-0.830
logarithmic	Z = 498,617.53 - 121,108.83logt	-0.851

Table 8. A summary of the regression analysis results for the domestic coal sales ("Export 1").

Model	The Model form of the Function	Correlation Coefficient
linear	Z = -1935.06t + 40,400.33	-0.9631
exponential	$Z = 41,160.05 \times 0.94t$	-0.9629
hyperbolic	$Z = 28,284.87 \times 11,811.94/t$	0.8249
power	$Z = 40,290.10 \times t^{-0.18}$	-0.9129
logarithmic	Z = 39,792.53 - 13,484.91logt	-0.9240

Model	The Model form of the Function	Correlation Coefficient
linear	Z = -104,292.09t + 2,047,921.34	-0.978
exponential	$Z = 2,093,621.65 \times 0.94t$	-0.975
hyperbolic	$Z = 1,403,079.82 \times 614,654.82/t$	0.809
power	$Z = 2,041,275.94 \times t^{-0.19}$	-0.916
logarithmic	Z = 2,011,000.32 - 718,914.59logt	-0.928

Table 9. A summary of the regression analysis results for the domestic coal sales ("Export 7").

Based on the production capacity of the "A–G" mines (Tables 1 and 2) and the estimated demand volumes from individual groups of consumers in terms of coal quantity and quality (Tables 3–6), the production and sales of coal was optimized using the SIMPLEX algorithm (Equations (1)–(5)). The solution is an optimal plan for the production and sales of coal for a given year from the point of view of the adopted criterion (Equation (1)) and the adopted restrictions (Equations (2)–(5)). A fragment of this plan, the annual optimal production plan for mine "F", is presented in Table 10. It provides information relevant from the decision-maker's point of view about the volume of sales (across the population of consumers), the stock of coal at hand, unused production capacity and the profit achieved by the mine. The optimal production and sales plans for the remaining mines ("A"–"E" and "G") are included in Appendix A (Tables A4–A9).

Table 10. The optimal production and sales plan for mine "F" for 2021.

Name of	Coal Size Grade	Sales Quantity	Total Sales	Profit:	Mine Reserves
Consumer Group	Cour Size Grade	(Mg)	(Mg)	(PLN)	(Mg)
Export 5	cobble	225,012	3,069,123	395,060,748	0
Cokerys 2	coking coal	78,136		(EUR 86,446,553)	
Export 6	nut coal	46,885			
Indv. consumers 1	cobble	18,507			
Cokerys 1	coking coal	231,563			
Dust kettles	fine coal I	243,520			
Dust kettles	fine coal IIA	23,675			
Dust kettles	fine coal II	2,201,825			
Dumping coal	coking coal	228,073			
Dumping coal	nut coal	13,995			
Dumping coal	slurry	74,409			

As can be seen, the mine has 6 out of the 17 potential consumers of the company as a whole. To achieve the planned sales, the mine should extract the amount of coal consistent with its production capacity of 3,385,600 Mg (Table 1). This is due to the longwall exploitation system (about 15–20% of the extraction is made up of thick assortments, and the rest are fine coal). As a result, the unsold, excess coal will be stored on site.

The optimal plan for the production and sale of coal (Tables 10 and A4, Tables A5–A9) is one of the possible solutions. In order to assess the impact of the randomness of the consumer demand on the possibility of selling coal, it is necessary to analyze a sufficiently large set of realistic variants of the future demand. Following the algorithm described in Section 2.2, demand volumes for all the groups of consumers were drawn (in the Monte Carlo simulation). Each of the selected demand sub-vectors is a random variable with normal distribution, with an expected (nominal) value equal to the planned volume of demand (sales) in 2021 (Table 6). For the analysis, a number of taken draws was equal to 1000, which allowed to obtain a sufficient set of production tasks and corresponding financial results, as a result of which was obtained a good quality of estimation of the resulting probability distribution. Each time a new optimal production plan is obtained for the selected demand vector—for the whole company and for each of its mines. In this case, it is 1000 optimal production plans for the company. Such a large set of optimal production plans

makes it possible to assess sensitivity of the company and its mines to fluctuations in the planned demand. The nominal values and dispersions of the demand are summarized in Table 6. The results for mine "F" are summarized in Tables 11 and 12, and in Figures 6–9. For the remaining mines, the results are included in Appendix A (Tables A10–A15 and Figures A1–A28).

Table 11. A summary of the expected gross profit with the probability of achieving them at σ_{yprog} for mine "F".

Nominal Profit	Minimum Profit	Maximum Profit	Probability of Achieving					
i toininui i ioint	Willing in 1 lone		Nominal Profit	Minimum Profit	Maximum Profit			
(PLN)	(PLN)	(PLN)	(-)	(-)	(-)			
99,053,000 (EUR 21,674,617)	46,437,497 (EUR 10,161,378)	149,825,520 (EUR 32,784,577)	0.482	1	0.181			

Table 12. A summary of the volumes of sales of the individual coal grades with the probability of their achievement at σ_{yprog} for mine "F".

Coal Size	Quantity According to	Minimum Ouantity	Maximum Ouantity	Probability of Achieving the Quantity		
Grade	Plan	~	~	According to the Plan	min	max
	(Mg)	(Mg)	(Mg)	(-)	(-)	(-)
cobble	243,519	228,456	243,519	0.998	1	0.998
nut coal	46,885	24,853	60,880	0.586	1	0.071
fine coal I	243,519	243,519	243,519	1	1	1
fine coal IIA	23,675	23,675	23,675	1	1	1
fine coal II	2,201,825	2,201,825	2,201,825	1	1	1
coking coal	251,240	0	537,772	0.532	0.676	0.352



Figure 6. Histogram showing frequencies of achieving given profits for mine "F" with dispersion $\sigma_{yprog.}$ * The black vertical line illustrates the nominal value quantity (according to the optimal plan from Table 10).



Figure 7. Histogram showing frequencies of achieving given quantity of sales of cobble for mine "F" with $\sigma_{yprog.}$



Figure 8. Histogram showing frequencies of achieving given quantity of sales of coal for mine "F" with $\sigma_{yprog.}$

Table 11 shows, for comparative purposes, the probability that mine "F" will obtain the profit shown in the optimal plan, as well as its minimum and maximum values. It was performed the same for the specific coal grades (Table 12). In addition, the probabilities of their sale were counted in the minimum and maximum quantities, which were found in the 1000 random plans.

In order to facilitate the interpretation of the results, the black vertical line was added to the Figures to illustrate the nominal value of a given quantity (according to the optimal plan from Table 10).





4. Discussion

The analysis of the histogram of the profit achievable for mine "F" has revealed distortions of the histogram resulting from the mismatch of the production structure to the demand (Figure 4). The histogram shows that the probability of achieving the nominal gross profit (shown in the optimal annual production plan, see Table 10) is only 0.482 (Table 11). The mine is most likely to achieve a profit of PLN 46,437,000 (EUR 10,161,378). In 181 cases out of the 1000, the mine could achieve a profit of PLN 149,825,000 (EUR 32,784,577). Such large fluctuations in the mine's profit are caused by the quantity and quality of individual coal grades accepted by the consumers, and so in the case of:

- The "cobble" grade—the probability that the mine will sell the amount shown in the optimal plan (Table 10) is practically 1. In two cases, sales per the 1000 were lower by 15,063 Mg (Table 12, Figure 5).
- The "nut coal" grade—the probability that the mine will sell the amount that was shown in the optimal plan (Table 10) is 0.586. Selling a larger quantity is unlikely: the probability of selling, for example, 60,880 Mg (the maximum quantity) of this grade is 0.071 (Table 12, Figure 6). However, a quantity of 24,853 Mg will always be sold.
- The "coking coal" grade—the chance of maintaining the sales at the level as shown in the optimal plan is only 50% (probability 0.532) (Table 12). The probability of selling more coking coal is small: 0.352. The most likely situation is that the mine will not find buyers for this coal. The probability of such situation is 0.676 (Table 12, Figure 7).

Regarding the sales of other grades to the consumer group concerned, the mine has no problems and will always find buyers for any volume (Table 12).

5. Conclusions

Changes in the volume of consumers' demand for coal have a significant impact on the volume of mining production and, thus, on the economic performance of mines and mine groups. The results of the above analysis make it possible to formulate certain strategies for future operations, mainly in terms of decisions regarding feasible volumes of coal extraction and sales. They also provide a basis for taking measures aimed at adapting the production structure to the requirements of the consumers both in terms of quantity and quality.

With the company concerned, coal from one mine accepted in one of the solutions by a specific consumer may be rejected by the same consumer in the next variant of the solution, in favor of a "more attractive" offer from another mine. This is revealed by the results described, e.g., in paper [23–25], for the multivariate changes in the demand.

The results enable direct identification of coal grades to be accepted by consumers, and with what probability, and the extraction of those grades is unprofitable due to the lack of market demand.

Maintaining a mining structure that is not accepted by consumers involves costs. Unfortunately, the production structure of a mine is dependent on its mining technology (e.g., the longwall system). On the other hand, such a supply–demand mismatch calls for a restructuring. In the case of managing a group of mines, it is possible to control the extraction and sale of coal. Sometimes, this has to be done at the expense of changes in the optimal production and sales plan. We are departing from the optimal solution, but it becomes a rational plan [23–25].

The results obtained as a result of the research undertaken by the author have shown that the proposed method can be useful, in particular with regard to the economic performance of mines (in the environment of variable demand) [24,25]. Only the combination of the method of rationalization of production decisions presented in paper [35] with the method of assessing the impact of the variability of demand on the performance of a multi-mine company provides a comprehensive and useful decision-making tool for the management of a multi-mine company.

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Appendix A

Table A1. The historical volumes of coal demand from the "Export" consumers in the years 2014–2020, (Mg).

Years		Name of Consumer Group								
Icuis	Export 1	Export 2	Export 3	Export 4	Export 5	Export 6	Export 7			
2014	38,707	509 <i>,</i> 597	371,252	208,049	378,926	144,389	1,918,295			
2015	35,126	462,456	336,809	180,803	353,873	135,032	1,840,840			
2016	35,790	471,187	343,269	192,868	350,365	133,506	1,773,707			
2017	34,076	443,624	326,832	183,156	333,588	127,113	1,688,772			
2018	29,274	385,412	280,781	157,349	286,585	109,203	1,450,821			
2019	28,234	371,708	270,797	151,754	276,394	105,320	1,389,234			
2020	27,414	360,914	262,933	147,348	268,368	102,261	1,353,602			

		Name of Consumer Group								
Years [–]	Indv. Consumers 1	Indv. Consumers 2	Cokerys 1	Cokerys 2	Cokerys 3	Dust Kettles				
2010	473,581	1,924,126	951,233	114,324	1,266,780	8,308,837				
2011	469,230	1,906,447	942,493	113,273	1,255,141	8,232,494				
2012	439,106	1,784,055	881,986	106,001	1,174,562	7,703,977				
2013	436,654	1,774,092	877,061	105,409	1,168,003	7,860,956				
2014	423,062	1,718,873	859,762	102,129	1,131,648	7,422,504				
2015	427,639	1,737,466	858,954	103,233	1,143,890	7,502,796				
2016	434,257	1,774,354	872,247	104,831	1,161,592	7,618,905				
2017	411,055	1,670,086	825,643	99 <i>,</i> 230	1,079,529	7,211,832				
2018	365,582	1,485,336	734,308	88,253	977,895	6,414,035				
2019	348,864	1,417,410	700,727	89,217	933,175	6,120,715				
2020	335,198	1,361,885	673,277	80,918	896,620	5,880,946				

Table A2. The historical volumes of coal demand from the domestic consumers in the years 2010–2020, (Mg).

Table A3. The historical volumes of coal demand from the domestic consumers in the years 2010–2020, (Mg).

		Name of Con	sumer Group	
Years	Grates 1	Grates 2	Chamber Grates 1	Chamber Grates 2
2010	178,326	92,439	69,338	53,848
2011	176,687	91,590	68,701	53,353
2012	165,344	85,710	64,290	49,928
2013	164,421	83,232	63,931	49,649
2014	159,303	82,579	61,941	48,104
2015	161,026	83,472	62,611	48,624
2016	169,518	84,764	63,580	49,377
2017	154,782	80,235	60,183	46,788
2018	137,659	71,359	53,526	41,568
2019	131,364	68,096	51,078	39,667
2020	126,218	65,428	49,077	38,113

Table A4. The optimal production and sales plan for mine "A" for 2021.

Name of Consumer Group	Coal Size Grade	Sales Quantity	Total Sales	Profit:	Mine Reserves
r	Giude	(Mg)	(Mg)	(PLN)	(Mg)
Dust kettles	fine coal I	264,765	597,902	4,843,299	0
Dust kettles	fine coal II	317,136		(€1,059,803)	
Grates 2	slurry	16,003			
Dumping coal	cobble	160,023			
Dumping coal	nut coal	21,821			
Dumping coal	fine coal IIA	675,004			

Table A5. The optimal production and sales plan for mine "B" for 2021.

Name of Consumer	Coal Size Grade	Sales Quantity	Total Sales	Profit:	Mine Reserves
Group	Giude	(Mg)	(Mg)	(PLN)	(Mg)
Grates 1 Dumping coal	fine coal II coking coal	113,486 252,598	113,486	-4,880,293 (€-1,067,898)	427,416

Name of Consumer	Coal Size Grade	Sales Quantity	Total Sales	Profit:	Mine Reserves
Group		(Mg)	(Mg)	(PLN)	(Mg)
Export 5 Cokerys 3	coking coal coking coal	123,542 865,806	989,348	49,931,963 (€10,926,031)	121,552

 Table A6. The optimal production and sales plan for mine "C" for 2021.

Table A7. The optimal production and sales plan for mine "D" for 2021.

Name of Consumer Group	Coal Size Grade	Sales Quantity	Total Sales	Profit:	Mine Reserves
	Giude	(Mg)	(Mg)	(PLN)	(Mg)
Export 2	coking coal	292,713	1,662,027	77,472,349	1,493,506
Export 3	coking coal	220,455		(€16,952,374)	
Indv. consumers 1	cobble	36,934			
Indv. consumers 2	fine coal IIA	637,566			
Grates 1	fine coal II	8394			
Chamber grates 1	fine coal IIA	47,390			
Cokerys 1	coking coal	418,575			
Dumping coal	fine coal I	18,467			

Table A8. The optimal production and sales plan for mine "E" for 2021.

Name of Consumer Group	Coal Size Grade	Sales Quantity	Total Sales	Profit:	Mine Reserves
r	Giude	(Mg)	(Mg)	(PLN)	(Mg)
Export 1	coking coal	22,984	2,952,728	76,118,502	0
Export 2	coking coal	9893		(€16,656,127)	
Export 6	nut coal	38,855			
Indv. consumers 1	cobble	215,197			
Dust kettles	fine coal I	206,231			
Dust kettles	fine coal IIA	1,545,236			
Dust kettles	fine coal II	863,778			
Grates 2	slurry	13,752			
Chamber grates 2	slurry	36,803			
Dumping coal	slurry	36,122			

Table A9. The optimal production and sales plan for mine "G" for 2021.

Name of Consumer Group	Coal Size Grade	Sales Quantity	Total Sales	Profit:	Mine Reserves
r	Giude	(Mg)	(Mg)	(PLN)	(Mg)
Indv. consumers 1	cobble	53,039	1,915,771	34,031,639	0
Export 7	fine coal IIA	932,482		(€7,446,748)	
Export 7	fine coal II	206,632			
Indv. consumers 2	fine coal IIA	677,516			
Dust kettles	fine coal IIA	521			
Dust kettles	fine coal II	12,155			
Grates 2	slurry	33,426			
Dumping coal	cobble	53,315			
Dumping coal	nut coal	15,194			
Dumping coal	coking coal	1,057,470			

	Quantity	Minimum	Maximum	Probability of Achieving the Quantity			
Coal Size Grade	According to Plan	Quantity	Quantity	According to the Plan	min	max	
	(Mg)	(Mg)	(Mg)	(-)	(-)	(-)	
fine coal I	264,765	0	264,765	0.008	0.881	0.881	
fine coal II	317,136	0	317,136	0.008	0.881	0.881	
slurry	16,003	0	16,003	0.008	0.881	0.881	

Table A10. A summary of the volumes of sales of the individual coal grades with the probability of their achievement at σ_{yprog} for mine "A".

Table A11. A summary of the volumes of sales of the individual coal grades with the probability of their achievement at σ_{yprog} for mine "B".

	Quantity	Minimum	Maximum	Probability of Achieving the Quantity		
Coal Size Grade	According to Plan	Quantity	Quantity	According to the Plan	min	max
	(Mg)	(Mg)	(Mg)	(-)	(-)	(-)
coking coal	113,486	81,002	142,488	0.001	0.001	0.496

Table A12. A summary of the volumes of sales of the individual coal grades with the probability of their achievement at σ_{yprog} for mine "C".

Coal Size Grade	Quantity According to Plan	Minimum Quantity	Maximum _ Quantity	Probability of Achieving the Quantity		
				According to the Plan	min	max
	(Mg)	(Mg)	(Mg)	(-)	(-)	(-)
coking coal coking coal	123,542 865,806	92,798 658,213	152,237 1,001,054	1 1	0.004 0.011	0.506 0.565

Table A13. A summary of the volumes of sales of the individual coal grades with the probability of their achievement at σ_{yprog} for mine "D".

	Quantity	Minimum	Maximum	Probability of Achieving the Quantity		
Coal Size Grade	According to Plan	Quantity	Quantity	According to the Plan	min	max
	(Mg)	(Mg)	(Mg)	(-)	(-)	(-)
cobble	36,934	0	69,758	0.005	0.071	0.505
fine coal II	8394	0	15,854	0.003	0.106	0.526
fine coal IIA	637,566	0	1,293,697	0.003	0.038	0.529
fine coal IIA	47,390	0	57,314	0.277	0.006	0.442
coking coal	292,713	0	371 <i>,</i> 593	0.277	0.002	0.335
coking coal	220,455	0	270,714	0.003	0.006	0.376
coking coal	418,575	0	788,355	0.217	0.005	0.562

	Quantity	Minimum	Maximum	Probability of Achieving the Quantity		
Coal Size Grade	According to Plan	Quantity	Quantity	According to the Plan	min	max
	(Mg)	(Mg)	(Mg)	(-)	(-)	(-)
cobble	215,197	0	215,197	0.018	0.949	0.949
nut coal	38,855	24,684	38,855	0.001	0.994	0.994
fine coal I	206,231	0	206,231	0.111	0.852	0.852
fine coal IIA	1,545,236	1,545,236	1,545,236	1	1	1
fine coal IIA	863,778	0	863,778	0.096	0.836	0.836
slurry	13,752	0	68,867	0.001	0.725	0.725
slurry	36,803	0	44,779	0.043	0.007	0.444
coking coal	22,984	0	26,172	0.780	0.007	0.063
coking coal	9893	0	32,877	0.661	0.193	0.197

Table A14. A summary of the volumes of sales of the individual coal grades with the probability of their achievement at σ_{yprog} for mine "E".

Table A15. A summary of the volumes of sales of the individual coal grades with the probability of their achievement at σ_{yprog} for mine "G".

Coal Size Grade	Quantity According to Plan	Minimum Quantity	Maximum. Quantity	Probability of Achieving the Quantity		
				According to the Plan	min	max
	(Mg)	(Mg)	(Mg)	(-)	(-)	(-)
cobble	53,039	0	106,355	0.515	0.039	0.267
fine coal II	12,155	0	12,155	0.339	0.657	0.657
fine coal IIA	932,482	0	1,313,094	0.646	0.001	0.146
fine coal IIA	677 <i>,</i> 516	0	1,310,936	0.475	0.01	0.221
fine coal IIA	521	0	1,610,518	0.145	0.433	0.855
fine coal II	206,632	0	206,632	0.024	0.840	0.840
slurry	33,426	0	33,426	0.227	0.731	0.731



Figure A1. Histogram showing frequencies of achieving given quantity of sales fine coal I for mine "A" with $\sigma_{yprog.}$



Figure A2. Histogram showing frequencies of achieving given quantity of sales fine coal II for mine "A" with $\sigma_{yprog.}$



Figure A3. Histogram showing frequencies of achieving given quantity of sales slurry for mine "A" with $\sigma_{yprog.}$



Figure A4. Histogram showing frequencies of achieving given quantity of sales of coking coal for mine "B" with $\sigma_{yprog.}$







Figure A6. Histogram showing frequencies of achieving given quantity of sales of coking coal ("Cokerys 3") for mine "C" with $\sigma_{yprog.}$



Figure A7. Histogram showing frequencies of achieving given quantity of sales of cobble for mine "D" with $\sigma_{yprog.}$



Figure A8. Histogram showing frequencies of achieving given quantity of sales of fine coal II for mine "D" with $\sigma_{yprog.}$



Figure A9. Histogram showing frequencies of achieving given quantity of sales of fine coal IIA ("Indv. Consumers 2") for mine "D" with σ_{yprog} .



Figure A10. Histogram showing frequencies of achieving given quantity of sales of fine coal IIA ("Chamber grates 1") for mine "D" with σ_{yprog} .



Figure A11. Histogram showing frequencies of achieving given quantity of sales of coking coal ("Export 2") for mine "D" with $\sigma_{yprog.}$



Figure A12. Histogram showing frequencies of achieving given quantity of sales of coking coal ("Export 3") for mine "D" with $\sigma_{yprog.}$



Figure A13. Histogram showing frequencies of achieving given quantity of sales of coking coal ("Cokerys 1") for mine "D" with σ_{yprog} .



Figure A14. Histogram showing frequencies of achieving given quantity of sales of cobble for mine "E" with $\sigma_{yprog.}$



Figure A15. Histogram showing frequencies of achieving given quantity of sales of nut coal for mine "E" with $\sigma_{yprog.}$



Figure A16. Histogram showing frequencies of achieving given quantity of sales of fine coal I for mine "E" with $\sigma_{yprog.}$



Figure A17. Histogram showing frequencies of achieving given quantity of sales of fine coal II for mine "E" with $\sigma_{yprog.}$



Figure A18. Histogram showing frequencies of achieving given quantity of sales of slurry ("Grates 2") for mine "E" with $\sigma_{yprog.}$



Figure A19. Histogram showing frequencies of achieving given quantity of sales of slurry ("Chamber grates 2") for mine "E" with $\sigma_{yprog.}$



Figure A20. Histogram showing frequencies of achieving given quantity of sales of coking coal ("Export 1") for mine "E" with $\sigma_{yprog.}$



Figure A21. Histogram showing frequencies of achieving given quantity of sales of coking coal ("Export 2") for mine "E" with $\sigma_{yprog.}$



Figure A22. Histogram showing frequencies of achieving given quantity of sales of cobble for mine "G" with $\sigma_{uprog.}$







Figure A24. Histogram showing frequencies of achieving given quantity of sales of fine coal IIA ("Export 9") for mine "G" with σ_{yprog} .



Figure A25. Histogram showing frequencies of achieving given quantity of sales of fine coal IIA ("Indv. consumers 2") for mine "G" with $\sigma_{yprog.}$







Figure A27. Histogram showing frequencies of achieving given quantity of sales of fine coal II ("Export 7") for mine "G" with $\sigma_{yprog.}$



Figure A28. Histogram showing frequencies of achieving given quantity of sales of slurry for mine "G" with $\sigma_{yprog.}$

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