

Article



A Multi-Stage Fault Diagnosis Method for Proton Exchange Membrane Fuel Cell Based on Support Vector Machine with Binary Tree

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Abstract: The reliability and durability of the proton exchange membrane (PEM) fuel cells are vital factors restricting their applications. Therefore, establishing an online fault diagnosis system is of great significance. In this paper, a multi-stage fault diagnosis method for the PEM fuel cell is proposed. First, the tests of electrochemical impedance spectroscopy under various fault conditions are conducted. Specifically, prone recoverable faults, such as flooding, membrane drying, and air starvation, are included, and different fault degrees from minor, moderate to severe, are covered. Based on this, an equivalent circuit model (ECM) is selected to fit impedance spectroscopy by the hybrid genetic particle swarm optimization algorithm, and then fault features are determined by the analysis of each model parameter under different fault conditions. Furthermore, a multi-stage fault diagnosis model is constructed with the support vector machine with the binary tree, in which fault features obtained from the ECM are used as the characteristic inputs to realize the fault classification (including fault type and fault degree) online. The results show that the accuracy of the basic fault test and subdivided fault test can reach 100% and 98.3%, respectively, which indicates that the proposed diagnosis method can effectively identify flooding, drying, and air starvation of PEM fuel cells.

Keywords: fuel cell; fault diagnosis; support vector machine; equivalent circuit model

1. Introduction

The energy shortage and environmental pollution problems caused by using fossil fuels are becoming increasingly severe, which means new and clean alternative energy sources are gradually becoming the key research direction of various countries [1]. The proton exchange membrane (PEM) fuel cell has become one of the ideal power sources for new energy transportation due to the advantages of high efficiency, fast start-up speed, environmental protection, and lower operating temperature [2]. However, the promotion and large-scale commercial application of PEM fuel cells are restricted by their service life and reliability [3]. Under vehicular conditions, improper internal states management can lead to adverse phenomena, such as reactant starvation, membrane drying, and flooding, finally affecting output performance and service life. Material and structural optimization and design, as well as manufacturing methods for internal components, including membrane [4], catalyst layer [5], gas diffusion layer [6], and bipolar plate [7], can fundamentally alleviate these failures. On the other hand, advanced system control and management to ensure that the fuel cell works under the right conditions are also important, where the online fault diagnosis system can detect the early stage of the fault in time so that the operating conditions can be adjusted in time to prevent further deterioration, which is of great significance to improving the reliability and lifetime of PEM fuel cells [8].

For an online fault diagnosis system, two major elements, namely, the information acquisition module and diagnosis module, are included. In terms of critical information



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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). extraction, techniques are mainly divided into two main categories: physicochemical tests, such as pressure drop measurement, neutron imaging, and magnetic resonance imaging; electrochemical methods: such as polarization curve, current pulse injection, and electrochemical impedance spectroscopy (EIS) [9]. The gas pressure drop between channel inlet and outlet is an effective signal for the determination of gas transfer resistance, which is closely associated with flooding failure, but it seems that drying information cannot be obtained [10]. Neutron imaging and magnetic resonance imaging can realize internal in situ measurement but are not suitable for on-board applications due to limitations of measurement and price [11]. The polarization curve or voltage under specific current density is the most direct indicator to judge output performance and is easy to obtain by cell voltage monitor, while it is not accessible to distinguish fault type since all failures are ultimately a drop in voltage [12]. Current pulse injection mainly reflects ohmic resistance, which is primarily related to membrane water content, thus flooding or starvation cannot be accurately located [13]. On the other hand, the electrochemical impedance spectroscopy analyzing internal dynamics of PEM fuel cells at different time scales from the perspective of the frequency domain has been widely applied in performance assessment [14,15]. Legros et al. [16] found that PEM fuel cell flooding mainly affected the mass transfer impedance and cathode Warburg impedance by EIS measurement under fault experiment and further proved the feasibility of using EIS to diagnose flooding fault. Similarly, Debenjak et al. [17] measured the EIS of an 80-piece PEM fuel cell stack and found that the impedance at 30 Hz, 100 Hz, and 300 Hz had more significant differences under flooding and drying, so they concluded that the impedance at these frequency points could be used for fault diagnosis. Considering that the faster impedance acquisition with quick calculation techniques had been already proposed for low-cost online application [18], by this, the EIS-based feature acquisition is applied in this paper.

Fault diagnosis is an essential prerequisite for fault-tolerant control and fault elimination, and Gao et al. [19] presented a comprehensive review of the real-time fault diagnosis method from model-based and signal-based perspectives. As for PEM fuel cells, fault diagnosis methods can mainly be divided into the model-based method, data-driven method, and hybrid method [20–22]. The model-based approach, where the mechanism model or empirical model that can predict the system performance is needed, detects typical faults by a residual evaluation based on the variance between the predefined model and measured signal. In detail, the mechanism model shows satisfactory accuracy, but it is not suitable for online applications due to its high computation. In contrast, the empirical model with a simpler expression and fewer parameters, such as the equivalent circuit model (ECM), is more popularly used in fault diagnosis of PEM fuel cells. For example, Fouquet et al. [23] improved the traditional Randles ECM by replacing the double-layer capacitor with a constant phase element (CPE) and provided a qualitative explanation for the variation of the model parameters under flooding and drying. Rubio et al. [24] proposed two kinds of ECM and established the correlation between the parameters of ECM and internal states within the PEM fuel cell to diagnose flooding and drying fault. For another, the data-driven diagnosis method that considers the PEM fuel cell as a black box detects fault via artificial intelligence method, statistical method, and signal processing method based on analyzing a large amount of historical data [25,26]. Li et al. [27] applied Fisher discriminant analysis to extract characteristic parameters from voltage and used the support vector machine to classify faults of fuel cells, which achieved good results both offline and online. Benouioua et al. [28] analyzed the singularities of the output voltage signal of PEM fuel cell via wavelet transform and further classified the flooding fault of fuel cell accurately by using the k-nearest neighbor method. Riascos et al. [29] used Bayesian networks classification for the PEM fuel cell fault diagnosis. Note that the data-driven diagnosis method is essentially the analysis of data, and the accuracy of its diagnosis results depends on the training of data, which means that high precision requires a particular scale of data. However, the acquisition and storage of large amounts of data are often not easy, which requires many prior experiments and has high requirements on hardware

resources. Recently, several researchers have used EIS as the information acquisition to diagnose fuel cell faults in combination with a data-driven approach. Zhang et al. [30] proposed a diagnosis method based on fuzzy clustering by extracting graphic features from the EIS of PEM fuel cell as indicators to complete the fault diagnosis of different degrees of flooding and drying. Lu et al. [31] designed an online fault diagnosis system via online EIS calculation, and the parameters of the ECM identified by the least square method were input into the model on the basis of a machine-learning algorithm to complete the diagnosis. Their proposed system successfully diagnosed the flooding and drying faults of the PEM fuel cell with an accuracy of 90.9%. Inspired by the characteristics of the model-based method and data-driven method, these two methods can be combined, namely the hybrid method [22]. Recently, Djeziri et al. [32] proposed a hybrid method that combines a prior physical model and data-driven updated kernel for fuel cell failure diagnostics, where the updated kernel is enabled when the estimation error between the predicted and measured values of stack voltage surpasses a predefined threshold. Similarly, Pan et al. [33] combined a model-based adaptive Kalman filter and data-driven NARX neural network to realize fuel cell failure diagnostics. From another perspective, the fault diagnosis of the PEM fuel cell based on external signals is inseparable from the sensor measurement. The accuracy of measurement data is the premise of subsequent diagnostic applications. In the actual application of fuel cell vehicles, sensors may encounter significant measurement errors and complete failure. In general, the underlying software of the fuel cell system control unit may determine whether there is a complete failure through analog detection. As for measurement errors, an example is given by Won et al. [34], where the air flow meter fault caused by reduced measurement sensitivity was detected by an artificial neural network classifier and a residual-based diagnosis model. In comparison, this paper assumes that all sensors, including impedance measurement equipment, can work normally. The failure of the PEM fuel cell itself is the focus of research.

Although the above methods have made a significant effect on the fault diagnosis study of PEM fuel cells, there are still some challenges. Firstly, respecting fault features extraction based on EIS with a predefined ECM, the least-squares or directly software fitting is usually used for EIS fitting thanks to their fast convergence speed, but the initial value of various components of ECM needs to be set in advance artificially, which is not conducive to the online application of diagnosis. What is more, the vehicular fuel cell system operating under dynamic conditions has been facing a wide variety of situations with different fault types/degrees. It seems that incorrect fault degree detection may lead the controller to take drastic measures, even fault type is correctly identified, which may result in the fault aggravation or occurrence of other faults. Therefore, fault degree detection is also essential, and a case of the detection and identification of air stoichiometry fault with different degrees was given by Pahon et al. [35], where the fault diagnosis tool was established by wavelet transform technology. Zheng et al. [36] also proposed a data-driven fault detection tool on the basis of reservoir computing to study faults under four degrading operating conditions. However, multi-degree fault diagnoses of membrane drying, flooding, and air starvation are often overlooked. Considering these research gaps, it is strongly incentivized to design an innovative multi-stage online impedance-based fault diagnosis method for improving fuel cell management robustness. In this study, first, a comprehensive fuel cell fault experimental procedure is carried out, in which flooding, membrane drying, and air starvation, covering from minor to moderate and severe, are included. Accordingly, a fuel cell failure data set is established. Second, an improved Randles ECM is introduced to fit EIS by the hybrid genetic particle swarm optimization algorithm, in which the initial values of ECM components are replaced by parameter ranges, avoiding the accurate initial parameter selection. Then, a support vector machine with the binary tree (BT-SVM) is introduced for the detection of fault types, where part of the fitted ECM parameters is selected as characteristic inputs to realize the fault type classification, which can further distinguish the fault degree on the basis of fault types.

2. Experimental Setups

2.1. Experimental Platform

The PEM fuel cell tested here is a single cell with an active area of 50 cm² commercial membrane electrode assembly (MEA) produced by Shanghai Fuel cell Vehicle Powertrain Co. LTD. The flow field structure within the anode/anode graphite bipolar plate is a three-channel snake flow field, and the flow field of coolant is parallel straight structure. The general connection structure of the experimental test system is shown in Figure 1. The fuel cell test bench (G60, Greenlight, Vancouver, BC, Canada) is used to monitor the external state and control the operating parameters, such as gas stoichiometry, inlet humidity, pressure, and cell temperature. The electrochemical workstation (Reference 3000AE with 30k Booster, Gamry Instruments, Warminster, PA, USA) is applied to measure the EIS, and a booster is added to amplify the disturbance signal in the workstation (the original equipment is not suitable for EIS testing at high current density). Consider that a minor voltage disturbance can lead to a considerable change in current, the EIS experiment is conducted under galvanostatic mode by sweeping frequencies covering the range of 5 kHz to 0.1 Hz with 10 points per decade (when the low frequency is as low as 0.01 Hz and 0.001 Hz, the measurement time will increase to about 1 h and 10 h, which is not conducive to stable measurement). Furthermore, in order to ensure that the system approximately meets the linear condition during impedance measurement, the amplitude of the disturbance signal should be as small as possible. On the other hand, respecting the interference of noise and the measurable precision, the amplitude of the disturbance signal should not be too small. For this, the amplitude of the current disturbance selected is 8% of the DC load to ensure a significant trade-off between system linearization conditions and signal-to-noise ratio. Moreover, before each EIS measurement under corresponding fault test conditions, the PEM fuel cell should be sufficiently stable until cell voltage does not change obviously to ensure measurement accuracy.



Figure 1. Connection structure of PEM fuel cell experimental system.

2.2. Experiment Procedures

This paper aims to propose a multi-stage fault diagnosis method and validate its performance under flooding, membrane drying, and starvation conditions. First of all, a standard operating condition referred to typical vehicle working conditions is established prior to fault impedance testing, and specific information is displayed in Table 1. Based on previous papers, Table 2 presents primary causes of flooding, drying, and starvation by external operating conditions and internal effects [31,37]. It seems that changing operating conditions is convenient and the most direct way to create anticipant faults by directly influencing internal transfer and reaction process. Hence, fault conditions are adjusted based on the standard operating condition. On the other hand, according to polarization curves and sensitivity analysis of polarization loss against different operating conditions in our previous works [38], it can be noted that cell temperature has a significant influence on the ohmic resistance and proton transfer resistance. A higher cell temperature can lead to a lower cell voltage at a smaller current density because this condition easily causes lower water activity. In contrast, the PEM fuel cell presents a poor performance at a lower cell temperature since water vapor condenses easily. Moreover, the convection on the cathode side is conducive to the discharge of liquid water, if the air stoichiometry is reduced, the convection effect will be weakened, and the fuel cell is extremely prone to flooding. At the same time, higher inlet gas humidity and higher current density are also recommended in the flooding experiment. Membrane drying is usually the opposite of flooding fault, and its occurrence can adjust operating conditions in the reverse direction of flooding experiments. As for the vehicular fuel cell system, air starvation is more likely to occur than hydrogen starvation in the process of dynamic load change since the mixture air is more viscous, and the response hysteresis of the air compressor is more severe than that of the proportional valve [39,40]. Hence, the air starvation fault experiment is designed here, and air stoichiometry is the main regulating parameter.

Table 1. Fuel cell standard operating condition.

Name	Symbol	Unit	Value
Current density	Ι	A/cm ²	1
Inlet pressure ¹	$P_{\rm c}/P_{\rm a}$	kPa	150/160
Cell temperature	T	°C	75
Gas stoichiometry	$\lambda_{\rm c}/\lambda_{\rm a}$	-	2.5/1.5
Inlet humidity	$RH_{\rm c}/RH_{\rm a}$	%	50/60

¹ The operating pressure is relative pressure.

Table 2. Fault cases of external operating conditions and internal effect.

Fault Type	Causes by Operating Conditions	Internal Effect
Flooding	 Excessive humidity in the inlet gases High working current Lower cell temperature Lower water discharging rate 	 Liquid water accumulates Porous media and gas flow channel are blocked Hydrophobic materials degradation
Drying	 Insufficient humidification Higher gas stoichiometry Excessive cell temperature 	 Membrane dehydration Membrane crack Proton transport path is cut off Coolant loop blocked
Starvation	 Higher current density Inappropriate operating pressure Lower gas stoichiometry Flooding is a factor 	 Carbon in porous media dissolve, in turn, leading to porosity reduction Gas supply pipeline is blocked Insufficient reactant concentration at catalyst layer

The basic fault experiments designed based on the standard operating condition are shown in Table 3. The experimental steps of the basic fault are as follows: (1) Adjust the test bench to make the fuel cell run stably for 20 min under the standard operating condition; (2) Set the minor flooding condition according to Table 3, and run steadily for 30 min and

then measure EIS 20 times, and stabilize for 10 min between each two EIS measurements; (3) Change the condition to moderate flooding and severe flooded conditions, repeat step 3 to complete the EIS measurement of medium and severe flooding; (4) Repeat steps 1, 2, and 3 to complete the basic fault EIS measurements of minor, moderate, and severe degrees of drying and air starvation.

 Table 3. Fuel cell basic fault operating condition adjusted based on standard operating condition 1.

Fault	Level	Degree	$\Delta I(A/cm^2)$	$\Delta T(^{\circ}C)$	$\Delta\lambda_c$	$\Delta RH_c / \Delta RH_a$
	Minor	1	0.5	-10	-0.3	20%/20%
Flooding	Moderate	4	0.7	-15	-0.5	30%/30%
	Severe	7	0.7	-20	-0.8	40%/40%
	Minor	1	-0.5	-	-	-30%/-10%
Drying	Moderate	4	-0.6	5	0.2	-40%/-10%
	Severe	7	-0.7	10	0.5	-50%/-10%
	Minor	1	-	-	-0.8	-
Starvation	Moderate	4	-	-	-1.0	-
	Severe	7	-	-	-1.2	-

 \overline{A} A positive value means increasement, and a negative value stands for decrement. As for the degree information, the higher the number, the more serious the fault.

Again, four subdivided fault degree experiments of fuel cells are defined, on account of the above basic fault (degree: 1, 4, 7) tested procedures. The subdivided fault degrees are labeled as 2, 3, 5, and 6, respectively, in which degree 2 corresponds to the minor level of the fault, degrees 3 and 5 represent the moderate level, and degree 6 to the severe level. The specific subdivided fault conditions are listed in Table 4, and each test sequence is tested 5 times.

Fault	Level	Degree (Basis)	$\Delta I(A/cm^2)$	$\Delta T(^{\circ}C)$	$\Delta \lambda_c$	$\Delta RH_c / \Delta RH_a$
	Minor	2(1)	0.05	-	-	5%/5%
Flooding	Moderate	3(4)	-0.05	-	-	-5%/-5%
		5(4)	0.05	-	-	5%/5%
	Severe	6(7)	-0.05	-	-	-5%/-5%
	Minor	2(1)	-	-	0.1	-5%/0%
Durving		3(4)	-	-	-0.1	5%/0%
Drying	Moderate	5(4)	-	-	0.1	-5%/0%
	Severe	6(7)	-	-	-0.1	5%/0%
	Minor	2(1)	-	-	-0.05	-
Starvation	Moderate	3(4)	-	-	0.05	-
		5(4)	-	-	-0.05	-
	Severe	6(7)	-	-	0.05	-

Table 4. Fuel cell subdivided fault operating condition adjusted based on standard operating condition ¹.

¹ A positive value means increasement, and a negative value stands for decrement. As for the degree information, the higher the number, the more serious the fault.

2.3. Data Set

So far, a total of 200 basic fault experiments and 60 subdivided fault experiments have been conducted. First, 150 measured samples extracted from basic fault experimental data were selected as the training data set for diagnosis model training. The remaining 50 samples from basic fault date set and 60 samples in subdivided fault data set were utilized for model accuracy detection. The data usage instructions are shown in Figure 2.



Figure 2. Instructions for the use of experimental data set.

3. Equivalent Circuit Model and Parameters Identification

3.1. Equivalent Circuit Model

The equivalent circuit model composed of several simple equivalent components, separating from the complex internal mechanism process, is an effective means to analyze the impedance spectroscopy of the PEM fuel cell in real-time and quantitatively calculate each polarization loss. A typical EIS of the PEM fuel cell and its relation to internal dynamics are given in Figure 3a, and anode polarization processes are not included because they show negligible effects on the overall performance loss of the PEM fuel cell [41]. The ohmic impedance, equaling to the intercept of the spectroscopy and the real axis, mainly refers to the loss of the proton passing through the membrane and the electron passing through the electrode material. Furthermore, the impedance from high-frequency to low-frequency is mainly dominated by proton transfer within the cathode ionomer, charge transfer attributed to oxygen reduction, and oxygen transfer in the cathode, respectively. The high-frequency inductive phenomenon is mainly related to equipment disturbance [42]. For another, there is the same variation trend between the ohmic loss and cathode proton transfer loss, so the fault characteristic involving proton transport loss in the cathode catalyst layer is ignored to reduce the calculation of ECM. The traditional Randles model with Warburg element is shown in Figure 3b, where R_m is the ohmic resistance, and R_{ct} is the charge transfer resistance, and C_{dl} stands for the double-layer capacitor attributed to the capacitance effect between the anode and cathode. Warburg element Z_w reflects the oxygen mass transfer, and its impedance expression is given as:

$$Z_{\rm w} = R_{\rm w} \frac{\tanh(T_{\rm w}j\omega)^{P_{\rm w}}}{(T_{\rm w}j\omega)^{P_{\rm w}}}$$
(1)

where R_w represents the mass transfer resistance; T_w is the time constant; ω is the angular frequency; and *j* is the imaginary part. Give that the capacitor with distributed parameters rather than lumped parameters can better describe real non-uniform structure in porous electrode, the constant phase element (CPE) can be used to replace the standard double-layer capacitor, and its impedance Z_{CPE} is expressed as:

$$Z_{\rm CPE} = \frac{1}{T_{\rm dl} \cdot (jw)^{P_{\rm dl}}} \tag{2}$$

where T_{dl} is the time constant; P_{dl} is an exponent of the electrode distribution parameters, and the CPE is a standard capacitor. Based on this, the total impedance of Randles model with Warburg element and CPE (see Figure 3c) can be calculated as follows:

$$Z = R_{\rm m} + \frac{(T_{\rm w}j\omega)^{P_{\rm w}} \cdot R_{\rm ct} + R_{\rm w} \cdot \tanh(T_{\rm w}j\omega)^{P_{\rm w}}}{(T_{\rm w}j\omega)^{P_{\rm w}} + T_{\rm dl}(j\omega)^{P_{\rm dl}} \cdot R_{\rm w} \cdot \tanh(T_{\rm w}j\omega)^{P_{\rm w}} + (T_{\rm w}j\omega)^{P_{\rm w}} \cdot T_{\rm dl}(j\omega)^{P_{\rm dl}} \cdot R_{\rm ct}}$$
(3)

in which R_m , R_{ct} , R_w , T_w , P_w , T_{dl} , and P_{dl} are the parameters to be identified. The second-order RQ (R-CPE) model evolved from the Randles model with CPE, as shown in Figure 3d, is also frequently used for impedance analysis.



Figure 3. (a) Critical internal dynamics within the PEM fuel cell, (b) traditional Randles model with Warburg element, (c) Randles model with Warburg element and CPE, and (d) two-order RQ model.

To select an appropriate ECM for fault feature identification and extraction, the impedance carried out in the standard operating condition given in Table 1 is chosen to test the fitting effect of three ECMs mentioned above by Zview software. The Chi-square is often used to evaluate the fitting accuracy of ECM, which represents the deviation between the actual value and the fitted value of the model, and its expression is as follows:

$$\chi^2 = \sum \frac{(Z_0 - Z_e)^2}{Z_e}$$
(4)

where Z_0 is the measured impedance; Z_e is the estimated impedance of the ECM. The fitting results are shown in Figure 4 and Table 5. In particular, the initial parameters of each component are obtained by separate fitting of data in different frequency bands. It can be observed that traditional Randles model with Warburg element is more deviated in the middle frequency range because of the characteristics of the standard double-layer capacitor, while the improved Randles model with CPE and the second-order RQ model have higher impedance fitting accuracy in the whole frequency range, and the former has a lower Chi-square value. To this end, the Randles model with Warburg element and CPE is finally selected for fault diagnosis study.



Figure 4. Fitting results of different ECMs by Zview software.

Fable 5. Chi-square values of fitting re	esults by different ECMs.
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ECM	Chi-Square Value
Randles model with Warburg element	2.67
Randles model with Warburg element and CPE	0.86
Second-order RQ model	1.30

3.2. Hybrid Genetic Particle Swarm Optimization Algorithm

To avoid initial parameter determination, intelligent optimization algorithms are more appropriate for online identification. The genetic algorithm (GA) is an evolutionary algorithm that imitates the evolution of a population, which mainly includes coding, fitness calculation, selection, crossover, and mutation steps [43]. The algorithm first needs to encode the target parameters and initialize individuals to construct the initial population, then combine the target problem to calculate fitness calculation of the corresponding chromosomal individuals, and on this basis, select the outstanding individuals with high fitness to complete the genetics operations such as crossover and mutation. After each process, better populations will be produced, repeatedly subjected to fitness calculation and genetics operations until the target population is obtained. The particle swarm optimization (PSO) algorithm is a global search algorithm based on the habits of the foraging behavior of a flock of birds, which is modified by using the velocity and position model, and the adaptation calculation is completed through the continuous iteration of particle velocity and position to find the optimal solution [44]. First, PSO assumes that there exists a particle population ($\mathbf{X} = \left\{ x_1^{(t)}, x_2^{(t)}, x_3^{(t)}, \cdots, x_n^{(t)} \right\}$) in a n-dimensional search space, and the position vector of the kth particle in the space at moment *t* is $\mathbf{X}_{k}^{(t)} = \left\{ x_{k1}^{(t)}, x_{k2}^{(t)}, x_{k3}^{(t)}, \cdots, x_{kn}^{(t)} \right\}, k = 1, 2, \cdots, n$. The position of each particle is a potential feasible solution in the search space, and the velocity vector corresponding to the particle at moment *t* is $\mathbf{V}_{k}^{(t)} = \left\{ v_{k1}^{(t)}, v_{k2}^{(t)}, v_{k3}^{(t)}, \cdots, v_{kn}^{(t)} \right\}$. If the best position searched by the *k*th particle in the current space is $\mathbf{P}_{k}^{(t)} = \left\{ p_{k1}^{(t)}, p_{k2}^{(t)}, p_{k3}^{(t)}, \cdots, p_{kn}^{(t)} \right\}$, and the best position of the whole target population is $\mathbf{P}_{g}^{(t)} = \left\{ p_{g1}^{(t)}, p_{g2}^{(t)}, p_{g3}^{(t)}, \cdots, p_{gn}^{(t)} \right\}$. The iterative formulas of particle velocity and position can be expressed as:

$$v_k^{(t+1)} = \omega \cdot v_k^{(t)} + c_1 r_1 \left(p_k^{(t)} - x_k^{(t)} \right) + c_2 r_2 \left(p_g^{(t)} - x_k^{(t)} \right)$$
(5)

$$x_k^{(t+1)} = x_k^{(t)} + v_k^{(t+1)}$$
(6)

where ω is the inertia factor; c_1 and c_2 are learning factor; and r_1 and r_2 are random numbers within in [0, 1]. A comprehensive review of parameter identification techniques for the PEM fuel cell is given by Priya et al [45], and more detailed information about GA and PSO can be found in it.

Both GA and PSO belong to the bionic algorithm, and the evolution process of both is similar. The information is shared among individuals in GA with the population going through genetics operations so that the whole population can evolve uniformly toward the optimal solution, making GA obtain high precision. However, the computation of GA is considerable because of its chromosomes encoding and decoding, which results in a long convergence time. In contrast, the PSO has fewer parameters with a more straightforward structure, making it easy to implement and converge quickly. Still, it is easy to fall into the local optimum and reach a poor result due to the insufficient information interaction between particles. By this, we combine the advantages of GA and PSO to construct a hybrid genetic particle swarm optimization algorithm (HGAPSO) for parameter identification of ECM in the application of PEM fuel cells. The general framework of the HGAPSO is shown in Figure 5. The selection and mutation are further added on particles at each iteration to reduce the uncertainties of being trapped into local optima [46].



Figure 5. Schematic of the hybrid genetic particle swarm optimization algorithm.

3.3. Parameters Identification

In general, the sum of the error squares of the actual measured values and calculated values will be adopted as the fitness function of the algorithm, which can be expressed as:

$$F = \sum_{j=1}^{n} \left(Z'_{j} - z'_{j} \right)^{2} + \sum_{j=1}^{n} \left(Z''_{j} - z''_{j} \right)^{2}$$
(7)

where *n* is the total frequency points of EIS; Z' and Z'' are the real and imaginary parts of the single-frequency impedance measured by the electrochemical workstation, respectively; and z' and z'' are the real and imaginary parts of the impedance fitted by ECM.

The goal of the HGAPSO algorithm is to minimize the fitness function. However, the fitness function does not distinguish the impedance at the high and low frequencies based on Equation (7), which will lead to obvious error of fitting in high frequency. To improve the fitting accuracy, a frequency weighting factor W_j consisting of the inverse of the impedance modulus is introduced, as expressed in Equation (8). W_j can be adaptively adjusted according to the frequency, thus reducing the volatility of the fitness function.

$$W_j = \frac{1}{\left(Z'_j\right)^2 + \left(Z''_j\right)^2}$$
 (8)

According to Equations (7) and (8), the final fitness function of HGAPSO can be expressed as:

$$F = \sum_{j=1}^{n} W_j \left(Z'_j - z'_j \right)^2 + \sum_{j=1}^{n} W_j \left(Z''_j - z''_j \right)^2$$
(9)

The parameter range is adjusted on account of experimental data and can cover the extreme conditions of fuel cells, which ensures the stability of the algorithm and make the online application possible, which is shown in Table 6.

Symbol	Unit	Range	
	$m\Omega \cdot cm^2$	10~200	
$R_{\rm ct}$	$m\Omega \cdot cm^2$	10~1500	
$R_{ m w}$	$m\Omega \cdot cm^2$	10~1500	
$T_{\mathbf{w}}$	${ m s}^{ m P_w}/{ m m}\Omega\cdot{ m cm}^2$	0.1~1	
$P_{\mathbf{w}}$	-	0.5~1	
T_{dl}	${ m s}^{ m P_{dl}}/{ m m}\Omega\cdot { m cm}^2$	$1 imes 10^{-5} \sim 1 imes 10^{-4}$	
P _{dl}	-	0.5~1	

Table 6. Parameter range of critical components of the ECM.

Four different conditions (normal/flooding/drying/air starvation) test whether the HGAPSO algorithm could keep high identification accuracy under extreme conditions. The maximum number of iterations of the HGAPSO is set to 200, and the termination condition is that the minimum value of the fitness function is less than 1×10^{-5} . Figure 6 presents the convergence curves of the fitness function of HGAPSO under the four working conditions. It is seen that the adaptation curves are relatively smooth in the convergence process, and the algorithm converges to the same fitness value at a lower number of iterations for 10 consecutive identifications in all four conditions, proving that the HGAPSO algorithm has good stability and convergence speed in the parameter identification.

Figure 7 shows the EIS fitting results for the above four conditions with the HGAPSO algorithm and Zview, and the relative deviation between the HGAPSO and the Zview is less than 3%, which also indicates that the HGAPSO algorithm has sufficient accuracy.



Figure 6. Convergence curve of the fitness function under four conditions.



Figure 7. Fitting results of the HGAPSO algorithm and Zview under four fault conditions: (**a**) normal; (**b**) flooding; (**c**) drying; (**d**) air starvation.

4. Multi-Stage Fault Diagnosis Based on BT-SVM Algorithm

4.1. Support Vector Machine Algorithm with Binary Tree

Support vector machine (SVM) is a machine learning method based on statistical learning theory. As shown in Figure 8, the basic SVM is designed to solve the binary classification problem, and its principle is to find an optimal hyperplane L in the data set [47]. Hence, the separation distance between the two types of data and the hyperplane L is the largest, that is, with the L parallel sample boundary l_1 and l_2 have the largest interval, and the sample point on the maximum interval sample boundary is the support vector.

The set of sample data should be set as $D_i = \{x_i, y_i \mid x_i \in \mathbb{R}^m, y_i \in \{-1, 1\}\}^n$, where x_i is the sample vector, and y_i is the sample label, such that the classification function is:

$$g(\mathbf{x}) = \mathbf{w} \cdot \mathbf{x}_i + b \tag{10}$$

Then the classification interval is:

$$\gamma_i = y_i (\boldsymbol{w} \cdot \boldsymbol{x}_i + \boldsymbol{b}) \tag{11}$$

Normalize Equation (11) and one can obtain:

$$\gamma_i = \frac{|g(\mathbf{x}_i)|}{\parallel \mathbf{w} \parallel} \tag{12}$$

where *w* is the normal vector to the optimal plane; *b* is the bias of the hyperplane to the origin. To maximize the classification interval distance γ_i , $\|w\|$ should be minimized, which is equivalent to minimizing $\|w\|^2$ /2. Therefore, the objective function minimization problem can be transformed into a plane programming problem with constraints [48]:

$$\begin{cases} f(\mathbf{x}) = sgn[\sum \alpha_i^* y_i(\mathbf{x} \cdot \mathbf{x}_i) + b^*] \\ \text{s.t. } \alpha_i^*[y_i(\mathbf{w}^* \cdot \mathbf{x}_i + b^*) - 1] = 0 \end{cases}$$
(13)

where the optimal Lagrange factor α_i^* can be obtained by solving the following convex optimization problem:

$$\begin{cases} \max_{a} \sum_{i=1}^{n} \alpha_{i} - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_{i} \alpha_{j} y_{i} y_{j} (\mathbf{x}_{i} \cdot \mathbf{x}_{j}) \\ \text{s.t. } 0 \leq \alpha_{i} \leq C, \ i = 1, 2 \cdots, n \\ \sum_{i=1}^{n} \alpha_{i} y_{i} = 0 \end{cases}$$
(14)

in which *C* is a penalty factor to constrain the error degree of the algorithm. When the sample data of the system are not linearly separable, a nonlinear mapping, i.e., a kernel function needs to be introduced to map the sample data into higher dimensions and transform it into a linear problem for further processing. The kernel function chosen in this study is a Gaussian kernel function, as shown in the following equation:

$$K(\boldsymbol{x}, \boldsymbol{x}_i) = \exp\left(-\frac{\|\boldsymbol{x} - \boldsymbol{x}_i\|^2}{2\sigma^2}\right)$$
(15)

Then the final classification decision function can be shown in the following Equation (16):

$$f(\mathbf{x}) = \operatorname{sgn}\left[\sum \alpha_i^* y_i K(\mathbf{x} \cdot \mathbf{x}_i) + b^*\right]$$
(16)

Nevertheless, the traditional SVM algorithm is a binary classifier that cannot meet the multiple fault type classification. Therefore, it is necessary to improve the traditional SVM algorithm by extending its binary classification capability into multi-classification. Currently, there are two primary forms of SVM-based multiclassification improvement: one-to-one and one-to-many. In details, one-to-one refers to designing classifiers for the data set two-by-two, and it is necessary to train N(N - 1)/2 classifiers for the *N*-class problem. In contrast, only *N* classifiers need to be trained in one-to-many, which have higher efficiency for issues with a more significant number of classes. Recognizing that the fault of the PEM fuel cell contains three types, the one-to-many SVM is applied to transform the fault diagnosis of fuel cells into a multiclassification problem in the form of the binary tree. The whole structure of the designed fuel cell fault diagnosis tool is manifested in Figure 9. Specially, the backbone of the fault classifier consists of a pre-classifier and three fault-type classifiers. The pre-classifier is placed first to determine whether the PEM fuel cell has faults, and terminate if there is no fault to improve the diagnosis efficiency, which is consistent with the actual situation that the PEM fuel cell is in the normal status most of the time during operating. The fault type classifier is designed in the order of flooding, drying, and air starvation, which is arranged according to the probability of fault occurrence in the empirical data statistics [49]. Such a design sequence can save computing resources and improve computing efficiency to a certain extent, which is conducive to the online application of the diagnostic algorithm. When the PEM fuel cell is diagnosed to be in specific fault status (flooding, drying, and air starvation), it will continue to enter three fault degree classifiers to analyze the fault degree further, thus improving the diagnostic accuracy and providing a more accurate guide for the controller regulation.



Figure 8. Linear classification principle of the support vector machine.



Figure 9. Structure of BT-SVM-based fuel cell fault classifier: (a) fault type; (b) fault degree.

4.2. Fault Feature Extraction and Selection

Figure 10 shows the average EIS under each fault degree of flooding, drying, and air starvation conditions, respectively, where 0 represents the normal status (standard

conditions), 1, 4, and 7 labeled by solid line illustrate the three fault levels of minor, moderate, and severe under the basic fault degree, respectively. At the same time, 2, 3, 5, and 6 labeled by discrete form correspond to the average EIS under the subdivided fault degree. As expected, there are apparent differences between the EIS curve under the basic fault degree, while the EIS under the subdivided fault degree is close to the corresponding basic fault levels. Therefore, the experiments of subdivided fault can further test the validity of fault degree diagnosis between adjacent basic fault levels.



Figure 10. Measured average EIS under different fault degrees: (a) flooding; (b) drying; (c) air starvation.

Figure 11 shows the ECM parameters under different operating conditions identified by HGAPSO algorithm. As can be seen, with the fault degree increasing, R_m , R_w , T_w , and P_{dl} have no obvious intersection of the curves under three fault conditions, possessing high differentiation and good fault type differentiation capability. R_{ct} also increases with the growth of fault degree after the interpolation of low fault degree. On the other hand, P_w and T_{dl} cross over each other as the fault degree growth, and there is no linear relationship between different fault degrees. In this regard, it can be considered that P_w and T_{dl} are not suitable for fault diagnosis so that R_m , R_w , R_{ct} , T_w , and P_{dl} are selected as fault feature inputs.

4.3. Results and Discusion

4.3.1. Fault Diagnosis Results

Once the fault features were extracted and filtered, as mentioned in Section 2.3, 150 samples from the basic fault experiments were selected as training data to complete the offline training of the diagnostic model, and the remaining 50 samples of basic fault data and 60 samples from the subdivided fault experiments were used as online test data for the diagnostic model. The diagnostic results are shown in Figure 12, where N represents the normal status, F, D, and S stand for the fuel cell faults of flooding, drying and air starvation, respectively. Additionally, the subscript notation "min", "mod", and "sev" represent the three levels of minor, moderate, and severe level, respectively. The number marked indicates the severity of the fault (five samples in a group). As shown in Figure 12a, it is seen that the diagnostic model can recognize fault type/degree with 100% accuracy under the basic fault experiment, and this is because both training and test data are extracted from impedance parameters under the basic fault conditions. Moreover, among the 60 samples in the subdivided fault experiment, the diagnostic model only misdiagnosed 1 sample, and the overall diagnostic accuracy is 98.3%. The misdiagnosis occurred in the 47nd sample, in which the fault is moderate air starvation in real, but diagnosed as minor level. The fault type was diagnosed correctly, confirming that the model has a high diagnostic ability for the fault type. The diagnostic error of the fault degree may be caused by the slight measurement error of EIS during the experiment. In summary, the fault diagnosis method proposed in this paper cannot only accurately diagnose flooding, drying, and air starvation

fault types of the fuel cell based on the EIS, but also has good differentiation performance in terms of fault degree, which can effectively ensure the controller for fuel cell internal status regulation, so as to improve the reliability and service life of the PEM fuel cell.



Figure 11. Fitted results of the ECM under different fault types and degrees.

4.3.2. Algorithm Related Parameters Analysis

It is well known that the amount of training data has a significant influence on the accuracy or learning ability of diagnostic models. Therefore, in addition to 150 samples for training, 50 samples and 100 samples were respectively applied for model training, and the same test set was used to test their accuracy, as shown in Figure 13. It can be seen that a lower number of training samples can also achieve 100% basic fault diagnosis. As for subdivided fault conditions, the detection accuracy based on the training of 50 samples and 100 samples is 90% and 96.7%, respectively, meaning that increasing the number of samples can improve the detection accuracy in a particular range. Still, the detection result of 200 samples after training was the same as that of 150 samples (not plotted here), which may be related to the fact that the training samples are all basic fault data.



Figure 12. Diagnosis results under (a) basic fault conditions and (b) subdivided fault conditions.



Figure 13. Diagnosis results with different training samples under (**a**) basic fault conditions and (**b**) subdivided fault conditions.

Another critical parameter setting in support vector machines is kernel function selection. Here, three different kernel functions, including linear, polynomial, and Gaussian, are compared. The linear kernel is usually used for linearly separable cases, suitable for the number of features up to about the number of samples. Both polynomials and Gaussian kernels can map a sample to a higher-dimensional feature space, but higher-order polynomials have more parameters. Theoretically speaking, when selecting the kernel function, if we have specific prior knowledge of our data, the kernel function can be chosen based on the data distribution. If there is no previous information, cross-validation is usually used to try different kernels, and the kernel with the lowest error is the best effect. Figure 14 shows the diagnosis results based on different kernels. Observing that all configurations can achieve a satisfactory diagnostic result under basic fault conditions, but for subdivided fault, the Gaussian kernel has the best effect, while the accuracy of linear and polynomial are 70% and 96.7%, respectively.



Figure 14. Diagnosis results with kernel function configuration under (**a**) basic fault conditions and (**b**) subdivided fault conditions.

5. Conclusions and Future Research Orientations

In this paper, a multi-stage fault diagnosis method based on BT-SVM was proposed to diagnose the fault type and fault degree of the PEM fuel cell. Firstly, a fault data set was established, including different fault types and fault degrees. Then, a Randles model with Warburg element and CPE was selected to extract fault features from the measured EIS. To realize the online parameter identification of ECM, a parameter identification method based on HGAPSO was proposed, where the initial values of ECM components were replaced by parameter ranges, avoiding the initial parameter selection. The relative error of parameters identified by the HGAPSO algorithm and the software Zview is less than 3% under four working conditions of normal, flooding, drying, and air starvation. Based on this, a diagnosis model in conjunction with BT-SVM was constructed and trained by 150 samples from basic fault experiment data set, where five identified ECM parameters were selected

as valuable features to be input into the diagnostic model. The remaining 50 samples from the basic fault data set and 65 samples from the subdivided fault data set were applied to complete the online fault diagnosis. The results show that the diagnostic model demonstrates satisfactory performance for both basic fault and subdivided fault with the accuracy of 100% and 98.3%, respectively, which proves that the proposed diagnosis method is capable of improving the reliability and durability of the fuel cell system. Furthermore, the multi-stage fault diagnosis method with different training samples and kernel function configuration were analyzed.

There are still many improvements in the future:

- (1) Impedance online acquisition is the premise of impedance diagnosis. However, current laboratory impedance measurements are primarily based on expensive test equipment, which is challenging to use in a real vehicle environment. At present, the signal processing method based on wavelet variation can calculate the impedance spectrum covering a wide frequency range quickly online, but it requires an additional square wave excitation source, and the existing controller resources are challenging to meet its calculation requirements. Hence, it is necessary to develop a more efficient and fast online impedance calculation method to meet the needs of real-time fault diagnosis.
- (2) In this paper, although varying degrees of failure is produced by changing the external operating conditions, it seems that the complex working conditions of the vehicle fuel cell system are still not satisfied. In the future, it will be necessary to simulate fuel cell failure scenarios in extreme environments, such as high temperature, high humidity, cold, and plateau, based on the environment chamber, and then to implement diagnostic algorithm validation.
- (3) At present, the experimental object is a single cell (MEA level), so it is necessary to carry out fault experiment and diagnosis for a high-power fuel cell stack. Meanwhile, except for the overall performance of the stack, failures of the single cell in the stack also need to be considered.

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Nomenclature

BT	Binary tree
CPE	Constant phase element
ECM	Equivalent circuit model
EIS	Electrochemical impedance spectroscopy
HGAPSO	Hybrid genetic particle swarm optimization algorithm
MEA	Membrane electrode assembly
PEM	Polymer electrolyte membrane
RQ	Resistance-CPE
SVM	Support vector machine
b	Bias of the hyperplane
С	Learning factor

C_{dl}	Double-layer capacitor
D	Sample data
F	Fitness function
8	Classification function
Ĩ	Current density
j	Imaginary part
K	Kernel function
Р	Position vector
Р	Inlet pressure
R	Resistance
RH	Inlet humidity
r	random number
Т	Cell temperature or time constant
υ	Particle velocity
V	Velocity vector
W	Weighting factor
w	normal vector
x	Particle position
Х	Particle population
Z_0	Measured impedance
Ze	Estimated impedance
Z'	Real part of impedance
Z'	Imaginary part of impedance
λ	Gas stoichiometry
ω	Angular frequency or inertia factor
χ	Chi-square
γ_i	Interval distance
α_i^*	Lagrange factor

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