Review

A Survey on FOPID Controllers for LFO Damping in Power Systems Using Synchronous Generators, FACTS Devices and Inverter-Based Power Plants

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Abstract: In recent decades, various types of control techniques have been proposed for use in power systems. Among them, the use of a proportional–integral–derivative (PID) controller is widely recognized as an effective technique. The generalized type of this controller is the fractional-order PID (FOPID) controller. This type of controller provides a wider range of stability area due to the fractional orders of integrals and derivatives. These types of controllers have been significantly considered as a new approach in power engineering that can enhance the operation and stability of power systems. This paper represents a comprehensive overview of the FOPID controller and its applications in modern power systems for enhancing low-frequency oscillation (LFO) damping. In addition, the performance of this type of controller has been evaluated in a benchmark test system. It can be a driver for the development of FOPID controller applications in modern power systems. Investigation of different pieces of research shows that FOPID controllers, as robust controllers, can play an efficient role in modern power systems.

Keywords: fractional-order proportional–integral–derivative (FOPID) controller; FACTS; inverter-based power plant (IBPP); low-frequency oscillation (LFO); power oscillation damping controller (PODC); synchronous generator (SG)

1. Introduction

With the development of power systems in the world, as well as the existence of new types of applications, the concept of power system stability is becoming very important. Accordingly, one of the most important issues is the robustness of power systems against uncertainties [1,2]. A robust controller is a controller that has a wide stability area and where the system uncertainties do not affect its performance significantly. So, in recent years, many studies on robust controllers have been conducted by researchers around the world [3]. On the other hand, one of the important problems of power grids is the risk of low-frequency oscillation (LFO) [4]. LFO is an electro-mechanical phenomenon that occurs in power systems due to the lack of damping torque [1–4]. The common technique for damping LFOs is to use an auxiliary controller called a power system stabilizer (PSS) in an

automatic voltage regulator (AVR) of a synchronous generator (SG) [1–4]. Conventional PSSs are the lead–lag compensators (LLCs) that are easy to design [5]. The operating mechanism of these types of controllers is based on the injection of an additional voltage signal into the excitation system of an SG. The input of these controllers can be the deviation of the frequency, power or variation of the generator rotor angle [1,2,6].

Recently, many studies have been conducted on LFO damping by power system devices, such as flexible AC transmission system (FACTS) devices, [5] and [7–10], and inverter-based power plants (IBPPs) [11–18]. Studies have been performed with various types of control strategies and electrical controllers. In the studies, the proposed controllers have been used as power oscillation damping controllers (PODCs). One of these types of controllers is the fractional-order proportional–integral–derivative (FOPID) controller [19–25]. Conventional PODCs, although easy to set up and install, with industrial applications, have many problems and challenges. For example, LLCs [15] and proportional–integral–derivative (PID) controllers [18] have a small stability area. Another important issue is the robustness of the PODCs against power system uncertainties. Therefore, it is necessary that a PODC, in addition to the abilities of easy tuning and being applicable for industrialization, has a wide range of stability as well as sufficient robustness against power system uncertainties.

Due to the robustness and wide stability area of the FOPID controller, its application in power systems has been widely discussed in many studies. Most of the studies of FOPID controller applications in power systems have been related to load frequency control (LFC) [26–29] and automatic generation control (AGC) [30–34]. Additionally, in [35] the FOPID controller was used to improve the power quality. In many studies, the FOPID controller has been investigated as a PODC to mitigate LFOs by SGs [36–44], FACTS devices [45,46], and IBPPs [47–49]. Given the advantages of the FOPID controller, it is expected that these types of controllers will be used extensively for LFO damping in modern power systems.

The aim of this paper is to introduce FOPID controllers and investigate the advantages and challenges of their application for LFO damping in modern power systems. For this purpose, an overview of the power system stability has been done with a focus on LFO. The fractional-order calculus is then presented in order to provide the model of the FOPID controller that can be used for LFO damping in modern power systems. Furthermore, this paper represents the optimization techniques used to tune the FOPID controller parameters in order to achieve better performance for LFO damping. In addition, a comparison has been made between the performance of FOPID controllers and other proposed controllers to damp LFOs in power systems. For this purpose, a benchmark test system has been used and the necessary simulations have been performed in different operating conditions. Additionally, this study highlights the opportunities and challenges of using FOPID controllers with the aim of introducing future research topics.

The rest of the paper is organized as follows. Section 2 provides an overview of the LFOs. An overview of fractional-order calculus, the role of FOPID controller to increase the stability area, and the structure of FOPID controller are introduced in Section 3. Then, Section 4 describes the tuning methods of FOPID controllers. The applications of FOPID controllers for LFO damping are presented in Section 5. Moreover, the PODC performance evaluation and comparative simulations are presented in Section 6. Then, opportunities and challenges are provided in Section 7. Section 8 provides the discussion, while Section 9 concludes.

2. Concept of LFOs

LFOs are one of the most important factors in destroying power system stability. The system's ability to maintain the acceptable point of operation during and after disturbances is called power system stability [1,2,50]. This concept is classified into main categories as shown in Figure 1 [50–52]. One of the categories is rotor angle stability, which is defined as the capability of SGs to maintain or restore the balance between mechanical torque

and electromagnetic torque [2]. Based on the power system events, rotor angle stability is classified into two different categories as follows:

- Small-signal stability;
- Transient stability.

Figure 1. Power system stability classification.

The small-signal stability analysis is classified into two various categories: an oscillatory condition due to lack of damping torque and a non-oscillatory condition due to lack of synchronizing torque [4]. In oscillatory conditions, oscillation with a frequency between 0.1 Hz to 2 Hz is called LFO [2,3], which is divided into two general categories as follows [2,3]:

- Oscillation with a frequency between 0.1 Hz to 1 Hz, due to the oscillation in a group of SGs or power plants in an area relative to SGs or power plants in another area, called inter-area oscillation [2,3];
- Oscillation with a frequency between 1 Hz to 2 Hz, due to the oscillation in an SG or a power plant relative to an SG or power plant in the same area, called local oscillation [2,3].

In conventional power systems, LFOs are usually damped by the PSS of SGs. It should be noted that although LFOs are the most important section of oscillatory states, control modes and torsional modes are also in the category of oscillatory states.

3. Review of the FOPID Controller

The mathematical model of this type of controller is based on fractional-order calculus [53–56]. This type of calculus is the general form of integer-order calculus. Although fractional-order calculus is very old, its use in the design of controllers is limited to recent years [53–56].

3.1. Concept of Fractional-Order Calculus

Fractional-order calculus is a basic concept in mathematics that actually expands the conventional integer-order calculus to the desired orders. The history of this concept dates back to about 300 years ago. However, due to the complexities of this concept, its implementation has been studied in recent decades. This is while there is still no physical and tangible understanding of fractional-order calculus [19].

The fundamental form of the fractional-order differentiator, which can be represented by a general operator as a general form of differential and integral operators, is defined as follows, extracted from [19] and [53–55]:

$${}_a D_t^q = \begin{cases} \frac{d^q}{dt^q}, q > 0 \\ 1, q = 0 \\ \int_a^t (d\tau)^{-q}, q < 0 \end{cases} \quad (1)$$

where, q , a , and t denote the fractional-order and lower as well as upper limits of the operator D , respectively. Generally, there are three different definitions for the fractional-order differentiator [53–55]:

- The Grunwald–Letnikov (GL) definition;
- The Riemann–Liouville (RL) definition;
- The Caputo definition.

The GL definition is as follows:

$${}_a D_t^q f(t) = \lim_{h \rightarrow 0} \frac{1}{h^q} \sum_{j=0}^{[(t-a)/h]} (-1)^j \binom{n}{j} f(t - jh) \quad (2)$$

$$\binom{n}{j} = \frac{\Gamma(n+1)}{\Gamma(j+1)\Gamma(n-j+1)}. \quad (3)$$

where n is the integer value that satisfies the condition and $n-1 < q < n$. Furthermore, operator $[\]$ in (2) indicates a floor function [53–55]. Moreover, Γ function notes Euler's gamma function as follows [53–55]:

$$\Gamma(x) = \int_0^\infty t^{(x-1)} e^{-t} dt \quad (4)$$

In addition, the RL definition is as follows [53–55]:

$${}_a D_t^q f(t) = \frac{1}{\Gamma(n-q)} \frac{d^n}{dt^n} \int_a^t \frac{f(\tau)}{(t-\tau)^{q-n+1}} d\tau \quad (5)$$

Additionally, the Caputo definition is as follows [53–55]:

$${}_a D_t^q f(t) = \frac{1}{\Gamma(n-q)} \int_a^t \frac{f^n(\tau)}{(t-\tau)^{q-n+1}} d\tau \quad (6)$$

3.2. Stability of Fractional-Order System

Execution of the fractional-order controller in a power system changes the mathematical model of the system from integer-order to fractional-order. Fractional-order linear time-invariant (FOLTI) dynamic systems are modeled by a differential equation as follows [19,53]:

$$a_n D^{q_n} y(t) + a_{n-1} D^{q_{n-1}} y(t) + \dots + a_0 D^{q_0} y(t) = b_m D^{r_m} y(t) + b_{m-1} D^{r_{m-1}} y(t) + \dots + b_0 D^{r_0} y(t) \quad (7)$$

where $D^x \equiv {}_0 D_t^x$ defines the RL derivative, a_k , b_l for $k = 0, \dots, n$ and $l = 0, \dots, m$ are constants, and q_k , r_l for $k = 0, \dots, n$ and $l = 0, \dots, m$ are arbitrary real numbers. Moreover,

$q_n > q_{n-1} > \dots > q_0$ and $r_n > r_{n-1} > \dots > r_0$. The transfer function of a FOLTI system with incommensurate orders is as follows [19,53]:

$$C(s) = \frac{b_m s^{r_m} + b_{m-1} s^{r_{m-1}} + \dots + b_0 s^{r_0}}{a_n s^{q_n} + a_{n-1} s^{q_{n-1}} + \dots + a_0 s^{q_0}} = \frac{Y(s^{r_k})}{R(s^{q_k})} \quad (8)$$

Additionally, for a fractional-order system with commensurate-order q , it holds that $q_k = qk$, $r_k = qk$, ($0 < q < 1$) $\forall k \in \mathbb{Z}$. This system is as follows [19,53]:

$$C(s) = K_0 \frac{\sum_{k=0}^M b_k (s^q)^k}{\sum_{k=0}^N a_k (s^q)^k} = K_0 \frac{Y(s^q)}{R(s^q)} \quad (9)$$

The stability condition for this system is presented as below [19,53]:

Matignon's Stability Theorem. A fractional-order system with commensurate-order q , explained by a rational transfer function shown in (9) is stable if and only if, $|\arg(\lambda_i)| > q(\pi/2)$ for all i , where λ_i is the i th root of $R(s^q)$.

The state-space model of FOLTI systems is stated as below [19,53]:

$${}_0 D_h^q x(t) = Ax(t) + Bu(t) \quad (10)$$

$$y(t) = Cx(t) \quad (11)$$

where $x \in \mathbb{R}^n$, $u \in \mathbb{R}^m$, and $y \in \mathbb{R}^p$ are the state vector, vector of system inputs, and vector of system outputs. For an n th-order system with m inputs and p outputs, $A \in \mathbb{R}^{n \times n}$, $B \in \mathbb{R}^{n \times m}$, and $C \in \mathbb{R}^{p \times n}$ are the system matrix, input matrix, and output matrix. Moreover, $q = [q_1, q_2, \dots, q_n]^T$ is the fractional-order vector. The fractional-order system in (10) and (11) is stable if and only if:

$$|\arg(\text{eig}(A))| > (q\pi)/2 \quad (12)$$

where $\text{eig}(A)$ denotes the eigenvalue of the system matrix. As shown in Figure 2, the fractional-order system's stability range depends on the value of fractional-order q . Therefore, changing the value of q can increase or decrease the stability range [19,53]. As shown in this figure, the maximum stability range of the fractional-order system is in the case where the q is between 0 and 1.

Figure 2. Stability area of the fractional-order system for the various values of q : (A) $0 < q < 1$; (B) $1 < q < 2$.

3.3. FOPID Controller

The FOPID controller is actually an extended form of the PID controller. Since the PID controller has derivative and integral operators, the FOPID controller has a fractional order between 0 and 1 for each operator. According to the contents of the previous section, it can be concluded that the FOPID controller has a higher range of stability compared to the PID controller due to extra degrees of freedom resulting from the order of fractional integral λ and the order of fractional derivative δ , extracted from [19] and [53–56].

High flexibility in design and robustness against system uncertainties, especially in non-linear systems, are the most important advantages of the FOPID controller [19,53,56]. The fractional differential equation of this type of controller is as follows [20–27]:

$$U(t) = K_P E(t) + K_I D_t^{-\lambda} E(t) + K_D D_t^{\delta} E(t) \quad (13)$$

Additionally, to model this type of controller, it is necessary to obtain its transfer function in the Laplace domain. The transfer function $C(s)$ in the Laplace domain is expressed as follows:

$$C(s) = \frac{U(s)}{E(s)} = K_P + K_I s^{-\lambda} + K_D s^{\delta} \quad (14)$$

where $E(s)$, $U(s)$, K_P , K_I , and K_D present the system input, system output, proportional gain, integral gain, and derivative gain of the FOPID controller, respectively. Moreover, λ and δ display the fractional orders of integrals and derivatives. The block diagram of the FOPID controller has been shown in Figure 3A [20–27]. As depicted in Figure 3B, the FOPID controller extends the PID controller from a point to a plane [20].

Figure 3. The FOPID controller: (A) structure in a control loop; (B) graphical presentation in δ – λ plane.

4. Tuning Methods of FOPID Controllers

Although the controller is very flexible in design, it is not easy to design and it is challenging. The FOPID controller design determines three gains and two fractional orders. The fractional-order parameters in the differential equation of the FOPID controller and the large number of parameters makes it impossible to use popular methods for controller design [56]. According to [20,55], design methods can be classified into three various categories, as follows:

- Rule-based techniques;
- Numerical techniques;
- Analytical techniques.

Two techniques have been applied for FOPID controller design in various studies for power system applications. The rule-based technique is based on approximation [42,56,57], and the numerical technique is based on optimization [58,59]. The first technique is based

on the approximation of the fractional-order function to an integer-order function [43,57]. Additionally, the numerical technique is to use optimization algorithms to determine the optimal values of the parameters [39–45,58,59]. This technique has been used in the literature for the application of the FOPID controller as a PODC, so this will be stated in detail in the next section.

It should be noted that the analytical techniques are based on the specified optimal behavior of the system, so the aim is to minimize the steady-state error. The analytical techniques are based on the Nyquist method. However, other methods may also be used to design fractional-order controllers in the future. Although FOPID controller design with different methods has many complexities and challenges, however, controller design using optimization methods is simpler than rule-based and analytical methods and has a wide variety of optimization algorithms. Moreover, the analytical method is very complex and has so far been used less in power system applications. However, analytical methods are very accurate in controller design and are widely used in theoretical studies of control systems.

Optimization Methods Technique

In this technique, the parameters of the FOPID controller are determined by solving an optimization problem subjected to technical constraints [20,59–61]. As indicated in Figure 3 and based on Equation (14), the closed-loop transfer function is as follows [19]:

$$\frac{Y(s)}{Y_r(s)} = \frac{C(s)G(s)}{1 + C(s)G(s)} \quad (15)$$

where $Y(s)$ and $Y_r(s)$ are the input and output of the closed-loop system. Therefore, the steady-state error of the closed-loop system is [19]:

$$E(s) = Y(s) - Y_r(s) = \frac{C(s)G(s)}{1 + C(s)G(s)} Y_r(s) - Y_r(s) \quad (16)$$

where there are five unknown parameters in the FOPID controller. Therefore, the objective function J is defined as follows [20,60]:

$$J(K_P, K_I, K_D, \lambda, \delta) \quad (17)$$

As shown in Equation (17), there are many parameters for optimal adjustment of the FOPID controller; therefore, the controller tuning is a challenging task [39–49]. The optimization process has been depicted in Figure 4.

Figure 4. Optimization process for FOPID controller design.

The optimization process is to determine the optimal values of controller parameters based on a specific objective; therefore, it is necessary to define a proper objective function. Many popular objective functions have been defined and used based on $E(s)$ minimization, such as follows [39–44]:

$$J_1 = \int_0^{\infty} (e(t))^2 dt \quad (18)$$

$$J_2 = \int_0^{\infty} t (e(t))^2 dt \quad (19)$$

$$J_3 = \int_0^{\infty} |e(t)| dt \quad (20)$$

$$J_4 = \int_0^{\infty} t |e(t)| dt \quad (21)$$

where $e(t)$ is the steady-state error. Furthermore, J_1 , J_2 , J_3 , and J_4 demonstrate the integral squared error (ISE), integral of the time-weighted squared error (ITSE), integral absolute error (IAE), and integral time-weighted absolute error (ITAE) indices, respectively [40–42,60,62]. In [47–49], the ITAE index has been used as a non-linear objective function for time-domain simulation. Likewise, the ITSE index has been used as an objective function in [45]. Table 1 shows the optimization algorithms used to tune the FOPID controller in power systems.

Table 1. Literature of FOPID controller design using optimization algorithms for power system applications.

Reference	Optimization Algorithm	Power System Application
[32]	Teaching–learning-based optimization (TLBO)	AGC
[36]	Particle swarm optimization (PSO)	PODC
[37,38]	Chaotic non-dominated sorting genetic algorithm-II (chaotic NSGA-II)	PODC
[39]	Genetic algorithm (GA), ant colony optimization (ACO)	PODC
[40]	Bat algorithm (BA)	PODC
[41]	Cuckoo search (CS)	PODC
[42]	Sine–cosine algorithm (SCA)	PODC
[43]	Hybrid firefly algorithm-PSO (FAPSO)	PODC
[44]	Chaotic yellow saddle goatfish algorithm	PODC
[45]	Improved PSO (IPSO)	PODC
[46]	Dolphin echolocation optimization (DEO)	PODC
[47]	PSO	PODC
[48]	PSO, GA	PODC
[49]	TLBO, PSO, GA	PODC
[63]	SCA	AGC
[64]	Chaotic multi-objective optimization	LFC
[65]	Atom search optimization (ASO)	LFC
[66]	Chaotic ASO (ChASO)	Controller of DC motor
[67]	Bacterial foraging optimization algorithm (BFOA), hybrid firefly algorithm-pattern search (hFA-PS), grey wolf optimization (GWO), GA	AGC
[68]	Group search optimization (GSO)	LFC
[69]	GA	AGC

5. FOPID Controller for LFO Damping in Power Systems

As mentioned, many studies have focused on the LLC, PID, linear quadratic Gaussian (LQG), FOPID, and other controllers for damping the LFOs in power systems. In this section, the FOPID controllers implemented in power system equipment to damp LFOs are reviewed and discussed.

5.1. FOID-PODC of SG

A PSS is an auxiliary controller connected to the exciter of an SG to damp LFOs. Research on new advanced control methods to improve PSS performance is a very interesting topic in electrical engineering. For this purpose, many types of control methods, including

adaptive control [70–72], gain-scheduling fuzzy control [73], robust control [74], and sliding mode control [75] have been carried out in the last two decades to improve the performance of PSSs. A robust and flexible control approach whose potential is now being examined in various engineering applications is based on FOPID controllers [19–21]. Usually, the PSS of an SG is the conventional LLC [2]. The first idea to use the FOPID controller as a PODC was to use it instead of PSS in the exciter of an SG, as depicted in Figure 5 [36].

Figure 5. The simple structure of the SG control system with the FOPID controller.

In [36–44], the FOPID controller has been proposed as a PODC of the AVR system. The results of the studies indicated the better performance of the FOPID controller than the PID controller and conventional LLC for LFO damping and dynamic stability improvement due to its flatness in the phase margin contribution with a wider bandwidth. Furthermore, simulation results indicated that the FOPID controller provides better robustness performance than the PID and conventional LLC under power system uncertainties and disturbance conditions [36–45].

In [36], the usage of the FOPID controller in an AVR has been studied. In the paper, the PSO algorithm has been used for FOPID controller tuning. In the study, a new objective function, considered to facilitate the control mode over both the time-domain and the frequency-domain specifications, was examined. The simulation results showed that the FOPID controller can highly improve the system robustness with respect to model uncertainties. In other studies in 2012 [37] and 2013 [38], the FOPID controller was designed as a PODC for an AVR system. In the studies, an improved evolutionary NSGA, expanded with a chaotic map, has been used for controller tuning. Additionally, the multi-objective function has been defined for optimization.

In [38], the controller tuning has been done in the frequency domain, so stability and robustness have been automatically guaranteed, unlike the other time-domain optimization-based tuning techniques. Additionally, another study in 2016 [39] proposed a FOPID controller for implementation in the excitation system of an SG. The study used the GA and ACO optimizations for controller tuning.

In 2017 [40], the FOPID controller tuning was done using a meta-heuristic optimization, BA. This optimization algorithm is based on the echolocation behavior for power system stability improvement. Furthermore, the problem of FOPID controller tuning has been solved based on the optimization method using performance indices, including IAE, ISE, ITAE, and ITSE. The simulation results illustrated that the FOPID controller provides better performance than conventional PID controller and LLC. In another study in 2018 [41], a robust FOPID controller was proposed for the excitation system of an SG as a PODC. In the study, the FOPID controller has been tuned using the CS algorithm. Then, the system performance was evaluated. The simulation results showed the better performance of the

CS-based FOPID controller than the PSO-based FOPID controller and the PID controller. Additionally, in [42] the FOPID controller was suggested as a PODC and adjusted by an advanced SCA optimization method. Moreover, the time-domain objective function has been considered for optimization. The results of the research indicated the proper performance of the FOPID controller in terms of frequency responses, reference tracking, and LFO damping. In 2019 [43], the implementation of a hybrid FAPSO algorithm for optimizing the parameters of a FOPID controller was suggested. In the research, the FOPID controller was designed by considering speed deviation and acceleration as input signals. The results demonstrated that the FOPID controller provides better performance in terms of LFO damping compared to the conventional PSSs. Additionally, the results showed the better performance of the hybrid FAPSO algorithm than other optimization algorithms such as PSO, hybrid GA, and bacterial foraging optimization in terms of optimal tuning of the FOPID controller. Furthermore, in other study in 2020 [44], the FOPID controller was proposed for an AVR system as a PSS application. In the study, the SCA and chaotic yellow saddle goatfish algorithm were used for controller designs.

5.2. FOPID-PODC of FACTS Devices

Due to the development of FACTS devices application in power systems, applying the FACTS-based PODCs is an efficient method to damp the LFOs [3]. One of the important types of these devices is the thyristor-controlled series capacitor (TCSC). This device has been proposed in many studies as a series compensator [76–78]. The internal structure of a TCSC is illustrated in Figure 6.

Figure 6. Schematic of a TCSC with the FOPID controller.

In the TCSC the capacitive impedance, X_C , is constant and the amount of reactance, $X_L(\alpha)$, is adjusted by the firing angle of the thyristors. Accordingly, the impedance of the TCSC is as follows [10,79]:

$$X_{TCSC}(\alpha) = \frac{X_C X_L(\alpha)}{X_L(\alpha) - X_C} \quad (22)$$

As shown in (22), the TCSC impedance is a function of the thyristors' firing angle. In [45], the FOPID controller has been used as a PODC in the TCSC for LFO damping and improve the rotor angle stability. Additionally, the FOPID-PODC has been coordinated with an AGC loop. The TCSC dynamic model with the FOPID controller has been shown in Figure 7.

Parameters of the FOPID controller and AGC loop have been optimally tuned using an IPSO algorithm. Furthermore, the ITSE index has been used as an objective function. The simulation results showed the better dynamic performance of the FOPID controller than conventional PODCs in terms of reducing the risk of LFOs. Moreover, the investigation of the results showed that with the addition of the fractional-order controller, the power system is strongly robust to the system uncertainties and severe disturbances.

Figure 7. Dynamic model of a TCSC with the FOPID controller.

Additionally, in another study in 2018 [46], the FOPID controller was proposed to mitigate the LFOs and stabilize the dynamic behavior of the power system using a static synchronous compensator (STATCOM). In the paper, the DEO algorithm was used and its superiority compared to other optimization algorithms for FOPID controller tuning was shown.

5.3. FOPID-PODC of IBPPs

Climate change and the tendency to use clean energy have increased the influence of IBPPs in the world. Due to the fact that these types of power plants don't have rotating components, their high penetration level reduces the power system's inertia [80,81]. Accordingly, many studies have raised the subject of LFO damping by these types of power plants [11–17]. This is done by considering the various control strategies or designing different controllers, such as conventional LLCs [12,14], PID controllers [17], and LQG controllers [11].

In 2020 [47] the use of the FOPID controller in the dynamic model of an IBPP as a PODC was suggested. In the research, an LPF was considered as a case study. In addition, the controller was tuned using PSO. Furthermore, in the research, the objective function has been considered based on the ITAE index. The results indicated the better performance of the FOPID controller for LFO damping than the PID controller, LQG controller, and conventional LLCs. It should be noted that, as depicted in Figure 8, the generic dynamic model of IBPP includes three sub-models as below [82]:

- The renewable energy generator/converter (REGC);
- The renewable energy electrical control (REEC);
- The renewable energy plant control (REPC).

Figure 8. General structure of the dynamic model of an LPF with the FOPID controller.

The proposed FOPID controller in the study has been connected to the REPC.

In 2021 [48], a method was suggested for coordinated tuning of the FOPID controller of an LPF and PSSs of SGs in order to damp the LFOs. Recently, in a study [49], a phasor measurement unit (PMU)-based FOPID controller was proposed to mitigate LFOs via

a large-scale hybrid wind-PV farm (LWPF). In the study, the performance of the LWPF for LFO damping by the FOPID controller was evaluated. The robustness of the FOPID controller against some uncertainties of the power system was also investigated. As shown in Figure 9, the papers suggested two different positions for the PODC in the REPC. The results of the studies show the proper performance and robustness of the FOPID controller compared to the popular controllers in a wide range of disturbances and uncertainties.

Figure 9. Block diagram of an REPC_B module of an LPF dynamic model with the FOPID controller.

The results of the studies show that the FOPID controller is suitably capable of being used as a PODC. Table 2 summarizes the literature.

Table 2. Summary of the FOPID controller for LFO mitigation in power systems.

Reference	Device	Tuning Method	Comparison with Other Controllers	Time-Domain Analysis	Frequency-Domain Analysis
[36]	SG	Optimization by PSO	No	Yes	No
[37,38]	SG	Optimization by chaotic NSGA-II	No	Yes	No
[39]	SG	Optimization by ACO	Yes	Yes	No
[40]	SG	Optimization by BA	Yes	Yes	No
[41]	SG	Optimization by CS	Yes	Yes	No
[42]	SG	Optimization by SCA	Yes	Yes	No
[43]	SG	Optimization by FAPSO	No	Yes	Yes
[44]	SG	Optimization by chaotic yellow saddle goatfish algorithm	No	Yes	No
[45]	FACTS (TCSC)	Optimization by IPSO	Yes	Yes	Yes
[46]	FACTS (STATCOM)	Optimization by DEO	No	Yes	No
[47]	IBPP (LPF)	Optimization by PSO	Yes	Yes	No
[48]	IBPP (LPF)	Optimization by PSO	Yes	Yes	No
[49]	IBPP (LWPF)	Optimization by TLBO	Yes	Yes	No

6. Performance Evaluation and Comparative Simulation

The performance of the FOPID-PODC in comparison to other proposed PODCs has been examined in this section. Therefore, a modified two-area system has been used in this paper [2,83]. For this purpose, three different scenarios are considered as shown in Table 3. These scenarios include different applications of the FOPID controller to mitigate the LFOs in the benchmark test system.

Table 3. Three scenarios for the FOPID controller in a power system as a PODC, based on the literature.

Scenario	Application
1	Supplementary controller for excitation system of an SG as a PSS
2	Auxiliary controller of TCSC as a PODC
3	Supplementary controller of LPF controller as a PODC

The modified system according to the scenarios is shown in Figure 10. Moreover, the specifications of the system are listed in Table 4. It should be noted that other data is in accordance with [2]. The benchmark test system is a smart grid under a wide-area measurement system (WAMS). In this system, the required signals are measured by PMUs and sent to the phasor data concentrator (PDC) for data processing. Furthermore, command signals are sent to the desired devices. Note that signal transmission has a time delay that should be applied in research and simulations. Although the time delay is a random value, in this study the signal transmission time delay between PMUs, PDCs, and PODCs is considered as a constant time delay, T_m , which is 100 ms as shown in Table 4 [47–49].

Table 4. Characteristics of the benchmark system.

Item	Description/Value
Dynamic model of SGs	Sixth-order model
Exciters model	IEEE-ST1A
PSSs model	STAB1
Loads	Constant power load
Constant time delay of signal transmission	100 ms [84,85]

Simulation is required for assessing the performance of the suggested PODCs in the reviewed applications. Therefore, four states are considered as follows:

- State 1: A three-phase fault at bus 8 at $t = 1$ s for 170 ms.
- State 2: Disconnection of line $L12$ at $t = 1$ s for 67 ms.
- State 3: Disconnection of generator $G1$ at $t = 1$ s for 67 ms.
- State 4: Disconnection of load 2 at $t = 1$ s for 67 ms.

It should be noted that the values of the FOPID-PODC parameters, K_P , K_I , K_D , λ , δ , in the three scenarios are obtained using the PSO algorithm. Furthermore, the ITAE index has been used as an objective function. In addition, the error function was defined as follows [62,86]:

$$|e(t)| = \sum_{G=1}^{n_G} |\Delta\omega_G(t)| \quad (23)$$

where n_G and $\Delta\omega_G$ denote the number of SGs and speed deviation of generator G , respectively. In order to obtain the value of the ITAE, it is necessary to consider a severe disturbance in the test system. In this study, a three-phase short circuit at bus 8 for 100 ms is considered as a severe disturbance. For this purpose, (21) must be minimized subject to parameter constraints. The constraints of the FOPID-PODC parameters are indicated in Table 5 [86].

Figure 10. Benchmark test system for three scenarios.

Table 5. Constraints of the FOPID-PODC parameters.

Item	K_P	K_I	K_D	λ	δ
Upper range	100	100	100	1	1
Lower range	0	0	0	0	0

6.1. Scenario 1

In this scenario, the excitation system of generator G2 is equipped with a FOPID-PODC as depicted in Figure 10. Additionally, other generators were equipped with conventional PSSs. It should be noted that, other system specifications are in accordance with [2]. The optimal values of the PODC parameters are available in Table 6.

Table 6. Optimal values of the FOPID-PODC parameters for scenario 1.

Item	Value
K_P	32.752
K_I	64.958
K_D	82.003
λ	0.4910
δ	0.5360

Note that the FOPID controller with the optimal set of parameters can mitigate both inter-area and local oscillations. This is exactly the same as the PSS mechanism. In fact, all types of PODCs can damp both types of oscillations. Of course, the most effective is the use of a multi-band PODC.

The simulation results performed in four states are presented in Figures 11 and 12. It should be noted that the simulation is based on a comparison between the performance of the FOPID controller and other proposed PODCs in the literature [87–98].

Figure 11. Rotor angle of generator G1 for scenario 1: (A) state 1, (B) state 2, (C) state 3, and (D) state 4.

Based on the simulation results, the FOPID-PODC performs well compared to the literature. Based on (21), the ITAE index has been used to compare the performance of the FOPID-PODC with the literature. As indicated in Figure 13, the value of the ITAE index for the FOPID-PODC is lower than the other controllers in the four scenarios. This indicates the proper performance of the FOPID-PODC in terms of LFO damping.

Figure 12. Power system frequency at bus 6 for scenario 1: (A) state 1, (B) state 2, (C) state 3, and (D) state 4.

Figure 13. ITAE index for scenario 1.

6.2. Scenario 2

In this section, the compensation scenario of transmission line L11, which is actually the main line between the two areas in the test system, is presented as depicted in Figure 10. The specifications of the benchmark test system are in accordance with [2], except that the TCSC has been added to line L11. Moreover, only generators G2 and G4 have the PSSs as shown in Figure 11. The TCSC is equipped with the FOPID controller as a PODC. The values of the TCSC parameters for simulation are listed in Table 7 [85].

Table 7. TCSC parameters.

Parameter	Value
Time constant of TCSC (T_f) (s)	0.05
Series capacitor of TCSC (X_c) (Ohm)	20
X_{L-Min} (minimum reactance) (Ohm)	25
X_{L-Max} (maximum reactance) (Ohm)	50
X_{Min} (Ohm)	11.1
X_{Max} (Ohm)	14.3

Based on Equations (21) and (22), the optimal values of the FOPID-PODC parameters are defined by the PSO algorithm. The results are shown in Table 8.

Table 8. Optimal values of the FOPID-PODC parameters for Scenario 2.

Item	Value
K_P	86.423
K_I	61.622
K_D	73.355
λ	0.687
δ	0.337

For performance evaluation of the proposed PODC, it is necessary to compare the controller with the literature [5,9,99–104]. Therefore, the necessary simulations are performed for four types of controllers: the FOPID controller, LLCs, the PID controller, and the LQG controller. The simulation results are illustrated in Figures 14 and 15. Furthermore, the ITAE index for each controller is obtained in four states as shown in Figure 16.

Figure 14. Rotor angle of generator G1 for scenario 2: (A) state 1, (B) state 2, (C) state 3, and (D) state 4.

Figure 15. Voltage magnitude at bus 6 for scenario 2: (A) state 1, (B) state 2, (C) state 3, and (D) state 4.

Figure 16. ITAE index for scenario 2.

6.3. Scenario 3

In this scenario, a 600 MVA LPF as an IBPP is connected to bus 6. In addition, the rating of generator G_2 has been changed from 900 MVA to 300 MVA. Furthermore, only generators G_2 and G_4 have the PSS. As shown in Figure 10, the LPF is equipped with a FOPID controller as a PODC. Based on Equations (21) and (22), the optimal values of the FOPID-PODC parameters are specified using the PSO algorithm, as listed in Table 9. In addition, the voltage control at plant level has been considered as the LPF control strategy [105–107]. Therefore, position 1 in Figure 9 is intended for the FOPID-PODC. So, bus 6 is considered as a PV bus [47]. For performance evaluation of the FOPID-PODC,

this section compares the PODC performance with the literature, including LLCs [14,17], PID controllers [18], LQG controllers [11], and multiple-model adaptive control (MMAC) strategy [13]. The simulation results are shown in Figures 17 and 18. Moreover, the ITAE index is shown in Figure 19. The simulation results confirm the accuracy of the literature results.

Table 9. Optimal values of the FOPID-PODC parameters for scenario 3.

Item	Value
K_P	26.874
K_I	32.821
K_D	85.233
λ	0.266
δ	0.219

Figure 17. Rotor angle of generator $G1$ for scenario 3: (A) state 1, (B) state 2, (C) state 3, and (D) state 4.

It should be noted that the lower value of the ITAE index is due to the increase in the damping ratio, the decrease in the settling time as well as the decrease in the overshoot of the system response using the FOPID controller. Each of these three factors alone or together can change the ITAE index and affect the system response.

The simulation results show that the application of FOPID controllers has a great effect on reducing the risk of LFOs and increasing the power system stability. However, the use of this type of controller to mitigate the LFOs has not yet been applied or is very limited. The main reason is the obstacles and challenges that exist to expanding its applications.

Figure 18. Power system frequency at bus 6 for scenario 3: (A) state 1, (B) state 2, (C) state 3, and (D) state 4.

Figure 19. ITAE index for scenario 3.

7. Opportunities and Challenges

Power systems are moving to modern power systems to overcome environmental problems and fossil fuel shortages. Next-generation systems have a high penetration level of renewable energy power plants, most of which are IBPPs. Therefore, the high penetration level of IBPP greatly reduces the power system inertia, which affects the stability. On the other hand, due to the nature of renewable energy power plants, their production has high uncertainty and fluctuates. Such fluctuations lead to an increase in LFOs, which is one of the main problems in power systems. A common method for LFO damping is to use an auxiliary controller as a PODC. Today, the focus of research is on the main topics:

1. Using robust controllers with a higher range of stability area in accordance with the requirements of next-generation systems;

2. Damping the LFOs using new devices in power systems, such as IBPPs and FACTS devices.

In recent years, the FOPID controller has been proposed as a PODC for LFO mitigation. The results of studies show that the FOPID-PODC performs better than conventional PODCs. The most important opportunities and benefits of using FOPID controllers in the power systems for LFO damping are listed in Table 10.

Table 10. Opportunities and benefits of the FOPID controller for LFO mitigation in power systems.

Opportunity	Description
Wide range of stability area	Due to the nature of the FOPID controller, this type of controller provides a large range of stability area.
Robustness	Due to the natural properties of the FOPID controller, which is due to the fractional orders of derivative and integral operators, this type of controller has a high robustness against system uncertainties.
Flexibility in design	It seems that the most important opportunity created by fractional-order calculus is its high flexibility to propose new types of robust PODCs in power systems by researchers.

However, there seem to be challenges and research gaps that need to be addressed in future studies. The main challenges and research gaps are addressed in Table 11.

Table 11. Research gaps and challenges of the FOPID controller for LFO mitigation in power systems.

Opportunity	Description
Auto-tuning	Although FOPID controllers have better performance in terms of LFO damping than conventional controllers, their tuning is difficult and time consuming compared to conventional controllers. Given the need for auto-tuning in modern power systems and smart grids, this is one of the most fundamental challenges of these types of controllers. It seems that the industrial use of FOPID controllers can be developed by creating and developing auto-tuning techniques.
Multi-band FOPID-PODC	One of the major research gaps in this subject is the design of multi-band FOPID-PODCs. Multi-band PODCs have the ability to mitigate oscillations at different frequencies. Although, in recent years, some studies have designed PSS-based multi-band controllers [108–110] and fractional-order LLC-based multi-band controller [111], no study has been done on multi-band FOPID controllers.
Commercialization and industrialization	One of the important research gaps of these types of controllers for PODC application in power systems is the examination of the capabilities for commercialization and industrialization. Conventional LLCs and PID controllers are easily and cheaply available for PODC applications. Today, conventional PSSs are based on LLCs that are very affordable and easy to design.
Fractional-order-based software packages	Given that the power system modeling in many software packages of electrical engineering is based on integer-order calculus, it is not possible to model the FOPID controllers. On the other hand, in many software packages where it is possible to model FOPID controllers, there is a limitation that the fractional orders cannot be variable. Therefore, it is impossible to tune the FOPID controller using these software packages.
Practical justification	The most important challenge with fractional-order calculus is that there is currently no practical justification for a fractional-order integral or derivative, e.g., the integral of a function means the area under its curve, but there is still no practical justification for fractional-order integrals.

8. Discussion

The FOPID controllers have several technical advantages over integer-order controllers. However, for the industrial application of these types of controllers, it is necessary to overcome the limitations mentioned in Section 7. The use of FOPID controllers should be properly justified by superior performance or at least the same efficiency as the conventional PODCs. A Technology Readiness Level (TRL) may have to be established for an industry-implementation-ready FOPID controller [112,113]. Sometimes, the variation in

FOPID controller parameters may result in instability, and hence the sensitivity of this type of controller to variations in the controller parameters should be studied.

As mentioned in Section 4, one of the main challenges of the FOPID controller is its tuning. The use of metaheuristic optimization techniques reduces the complexity of the design of fractional controllers. With the advances in artificial intelligence and fuzzy logic, better optimization methods can be used to tune the FOPID controllers. Such methods, with the inherent robustness of the FOPID controllers, can be used to obtain the desired system response.

The results obtained in Section 6 showed that the FOPID-PODC has a better performance than conventional PODCs in terms of LFO damping. Given that FOPID controllers are the extension form of the conventional PID controllers, which are the dominant controllers used by the industry, it can be expected that it will be easier to incorporate FOPID controllers soon into power systems.

9. Conclusions

In this paper, the applications of FOPID controllers in power systems for LFO damping were investigated. The most important feature of FOPID controllers that distinguishes them from other controllers is their wide stability range, which is due to the nature of these types of controllers. In this study, the difference between this type of controller and other controllers discussed in the literature in terms of mathematics was convincingly shown. Furthermore, the advantages of FOPID controllers were clearly identified in the simulations. The results of this review show that:

- Superior performance of the FOPID-PODC than conventional PODCs in terms of LFO mitigation;
- Superior performance of the FOPID-PODC than conventional PODCs in terms of robustness to some power system uncertainties.

This study also investigated the problems and challenges as well as opportunities in developing the applications of FOPID controllers. Although this type of controller has many advantages, considering the challenges mentioned, it has not been developed much in terms of application. Obviously, in the near future, with the development of mathematics and its applications in control engineering and industrialization of this type of controller, we can see the increasing development of FOPID controller applications in power systems to damp the LFOs.

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