

Article

Solar-Based DG Allocation Using Harris Hawks Optimization While Considering Practical Aspects

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Abstract: The restructuring of power systems and the ever-increasing demand for electricity have given rise to congestion in power networks. The use of distributed generators (DGs) may play a significant role in tackling such issues. DGs may be integrated with electrical power networks to regulate the drift of power in the transmission lines, thereby increasing the power transfer capabilities of lines and improving the overall performance of electrical networks. In this article, an effective method based on the Harris hawks optimization (HHO) algorithm is used to select the optimum capacity, number, and site of solar-based DGs to reduce real power losses and voltage deviation. The proposed HHO has been tested with a complex benchmark function then applied to the IEEE 33 and IEEE 69 bus radial distribution systems. The single and multiple solar-based DGs are optimized for the optimum size and site with a unity power factor. It is observed that the overall performance of the systems is enhanced when additional DGs are installed. Moreover, considering the stochastic and sporadic nature of solar irradiance, the practical size of DG has been suggested based on analysis that may be adopted while designing the actual photovoltaic (PV) plant for usage. The obtained simulation outcomes are compared with the latest state-of-the-art literature and suggest that the proposed HHO is capable of processing complex high dimensional benchmark functions and has capability to handle problems pertaining to electrical distribution in an effective manner.

Keywords: RDS; Harris hawks; optimal power flow; optimization; solar PV; transmission loss



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1. Introduction

Installing distributed generation (DG) sources in the distribution network system has been standard practice in recent years to minimize overall power losses and enhance the power quality [1,2]. The optimum sizing and positioning of DGs in power system networks are essential to maximize the benefits from those installations. The incorrect allocation and unreasonable sizing of DG units in the power system networks may increase voltage sags, voltage flickering, harmonic distortion, fault current, and power losses. With the application of DG units, the power system losses may be reduced by 13% [3,4]. In the functioning of power systems, economic damage and voltage collapse may be avoided through the reduction in power loss and voltage stability enhancement, respectively [5]. Thus, the investigation in optimal location selection and sizing of DG units in the distribution network is a step towards a profitable electricity supply [6,7]. Among all DG systems, solar photovoltaic DG systems seek attention worldwide for their abundant availability, easy installation, maintenance, and environment-friendly features.

The major goals of most techniques to determine the best location and size of DG units are to reduce power loss and improve voltage profile. The various techniques such as analytical methods, ant bee colony (ABC), genetic algorithm (GA), tabu search (TS), particle swarm optimization (PSO), fuzzy system, evolutionary programming, dynamic programming, etc., have been utilized to achieve the aforesaid objectives in a distribution network through the proper allocation and sizing of DG units. In the literature, GA is used to estimate the placement and size of DG units to improve the voltage profile and reduce power loss. Once DG units are appropriately placed in the distribution system network, voltage stability and loss reduction are improved significantly. The GA is utilized as the most applied optimization technique in resolving the problem of DGs allocation and sizing [8,9]. The multiobjective genetic optimization method is used in radial distribution systems to determine the best position and size for renewable-based DG units [10]. For site determination of DGs planning and performance index-based size, a GA-based multiobjective optimization is utilized to minimize the actual power loss in distribution systems with constant power, current, and impedance models [11]. Almabsout et al. [12] suggest an improved GA to determine the best placement and capacity of the simultaneous allocation of DGs/SCs in radial systems by combining the benefits of genetic algorithms and local search [12]. To minimize system losses, a mix of analytical and genetic algorithm approaches is utilized to optimize the allocation of numerous DGs in a distribution network [13].

To reduce real power losses and improve the voltage profile, Madhusudhan et al. [14] proposed the GA to identify the optimum location, as well as the size of the distribution network's DG units. Ayodele et al. [15] used GA to find the best DG technology for optimal power system functioning, as well as the best position and size of the DG to reduce network power loss. GA is applied to reduce the cost of system expansion and improves system stability [16,17]. However, GA convergence time is high, especially, when applied in the solution of complex problems, and may suggest inaccurate solutions. When compared to GA and TS techniques, Hassan et al. and Fan et al. [18,19] employed simulated annealing (SA) to find and specify the capacity of DGs while lowering computation time. However, the SA method has disadvantages such as termination at a local minimum, significant computational time, no information regarding the divergence of the local minimum from the global minimum, and no upper constraint for the calculation time. Using the TS approach, Liu et al. and Azam et al. [20,21] concentrated on DG optimum planning with the goal of minimizing both losses and line loadings. The TS technique, on the other hand, has the drawback of requiring a large number of iterations and parameter calculations. PSO was used to determine the best scale and distribution of DG units in the power system, together with its benefits [22].

One of the most effective and widely used optimization strategies is the PSO [23–25]. Barik et al. [26] presented a multiobjective PSO method for determining the best location and size of DG units while taking economic and technical factors into account. The advanced versions of PSO methods, such as improved PSO [27], binary PSO [28], social learning PSO [29], PSO with inertia weight, and PSO with constriction factor [30], are also applied in the DG allocation and sizing problems. However, the PSO technique has some disadvantages, such as difficulty in initializing the design parameters and inapplicability to scattering problems. Tolabi et al. and Oloulade et al. [31,32] introduced the ant colony optimization (ACO) technique to tackle the allocation and size problem of renewable energy source-based DGs in radial distribution networks with the goal of minimizing overall system losses. Their analysis showed that ACO gives a better solution, and computational time is less than GA. However, ACO takes more time to converge due to the complex nature of the problem but is still shorter than analytical methods. The major disadvantage of the ACO technique lies with its uncertainty in time to convergence. Das et al. [33] and Seker and Hocaoglu [34] used the artificial bee colony (ABC) method to compare results to the PSO technique and discovered that ABC provides a higher-quality solution with a faster convergence rate. The cuckoo search algorithm was used by Yuvaraj and Ravi [35]

to improve the voltage profile and reduce power losses in biomass and solar–thermal DG units. To optimize the system voltage profile and decrease line losses, Arya and Koshti [36] used a shuffled frog leaping algorithm.

Rajaram et al. [37] used a plant growth simulation algorithm with objectives such as decreasing the losses and improving the voltage profile. To reduce energy losses in a distribution network system, Othman et al. [38] used the big bang–big crunch approach to find appropriate DG units. The bat algorithm was suggested by Sudabattula and Kowsalya [39] for the efficient allocation of solar-based DGs in the distribution network. To decrease power losses while preserving voltage profile, Duong et al. [40] developed an efficient biogeography-based optimization for optimal location and size of solar photovoltaic distributed generating units.

Harris hawks optimization (HHO) is a new metaheuristic optimization algorithm used in various applications, as tabulated in Table 1.

After a thorough search in credible academic publications, as shown in Table 1, to-date, the efficient newly invented HHO method has not been utilized to optimal solar-based DG allocation in a radial distribution system. As a result, this study compares and contrasts the suggested work with well-known optimization techniques. Suitable DG unit placement may bring significant benefits, including cost saving through a reduction in power loss and increasing the purchasing power capacity.

Table 1. Application of HHO in different literatures.

Year	Area of Application	Research Objectives	Research Findings	Reference No.
2021	Design of truss structures	The use of HHO to solve planar and spatial trusses with discrete design variables was investigated in this paper. Five benchmark structural issues were used to assess HHO's performance, and the resultant designs were compared to 10 state-of-the-art algorithms.	The statistical results demonstrate that HHO is quite consistent and reliable when related to truss structure optimization.	[41]
2021	Prediction of slope stability	The study's major goal is to develop a new metaheuristic optimization approach HHO for improving the accuracy of the traditional multilayer perceptron technique in estimating the factor of safety in the presence of inflexible foundations. Four slope stability conditioning elements are taken into account in this method: slope angle, rigid foundation position, soil strength, and applied surcharge.	The findings revealed that employing the HHO improves the ANN's prediction accuracy while analyzing slopes with unknown circumstances.	[42]
2021	Power flow controller	To reduce oscillations in single and multimachine power systems, a HHO tuned dual interval type-2 fuzzy lead–lag (Dual-IT2FLL)-based universal power flow controller (UPFC) is suggested. The suggested damping controller uses speed deviation, a distant input signal for stability enhancement, to coordinate between the modulation index (MI) and phase angle of series and shunt converters of UPFC at the same time.	Different performance indicators (PIs) such as mean, standard deviation, overshoots, and settling time are used to demonstrate that the proposed HHO-tuned dual-IT2FLL-based UPFC outperforms others under various operating circumstances.	[43]

Table 1. Cont.

Year	Area of Application	Research Objectives	Research Findings	Reference No.
2021	Shear strength estimation of reinforced concrete walls	The authors suggested three novel models for estimating peak shear strength using a mix of support vector regression and metaheuristic optimization techniques including teaching–learning-based optimization (TLBO), PSO, and HHO. The authors compiled a huge database with 228 RC shear wall experimental data and eight input parameters.	The suggested models may be used to estimate the shear strength of RC shear walls, potentially improving the accuracy of forecasting the structure’s behavior and lowering construction costs.	[44]
2021	Screening of COVID-19 CT-scans	For the identification of COVID-19 from CT scan images, they suggested a two-stage pipeline consisting of feature extraction followed by feature selection (FS). A state-of-the-art convolutional neural network (CNN) model based on the DenseNet architecture was used for feature extraction. The HHO method was used in conjunction with SA and Chaotic initialization to remove noninformative and redundant features. The SARS-COV-2 CT-Scan dataset, which contains 2482 CT-scans, was used to test the suggested method.	The technique has an accuracy of about 98.42% without the chaotic initialization and the SA, which improves to 98.85% when the two are included, and therefore outperforms several state-of-the-art methods including other metaheuristic-based feature selection (FS) algorithms. The suggested approach reduces the number of characteristics chosen by around 75%, which is significantly better than most existing algorithms.	[45]
2021	Drug design and discovery	The authors presented a modified Henry gas solubility optimization (HGSO) based on heavy-tailed distributions (HTDs) utilizing improved HHO. A dynamical exchange between five HTDs were employed in this work to increase the HHO, which alters the exploitation phase in HGSO.	According to the values of accuracy, fitness value, and the number of selected characteristics, the results show that dynamic modified HGSO based on improved HHO has a high quality.	[46]
2021	Prediction of meteorological drought	In this study, the SVR (support vector regression) model was combined with two distinct optimization methods, PSO and HHO, to forecast the effective drought index (EDI) one month in advance in various sites across Uttarakhand, India.	The SVR-HHO model beat the SVR-PSO model in forecasting EDI, according to the results. SVR-HHO performed better than SVR-PSO in recreating the median, interquartile range, dispersion, and pattern of the EDI calculated from observed rainfall, according to visual assessment of model.	[47]
2021	Wireless sensor networks	The authors applied the HHO method to sensor node localization and compared their findings to other well-known optimization techniques that had just become available.	The suggested work’s simulation results revealed that it outperforms existing computational intelligence methods in terms of average localization error, number of localized sensor nodes, and computational cost.	[48]

Table 1. Cont.

Year	Area of Application	Research Objectives	Research Findings	Reference No.
2021	Groundwater	The HHO method was used to minimize the sum of absolute deviation between observed and simulated water-table levels in order to optimize hydraulic conductivity and specific yield parameters of a modular three-dimensional finite-difference (MODFLOW) groundwater model.	According to the findings, the Pareto parameter sets gave appropriate results when the maximum and minimum aquifer drawdown were defined in the range of -40 to $+40$ cm/year.	[49]
2020	Parameter optimization of support vector regression	The goal of this research is to look at the SVR approach that is optimized using HHO, also known as HHO-SVR. To establish the performance of the HHO-SVR, five benchmark datasets were used to assess it. The HHO method is also compared to various metaheuristic algorithms and kernel types.	The findings revealed that the HHO-SVR has almost the same performance as other techniques, but is less time efficient.	[50]
2020	MPPT control	This study offers a new MPPT controller based on HHO that successfully tracks maximum power in all weather situations.	The suggested HHO outperforms the competition in terms of maximum power point tracking (MPPT) and convergence at the global maximum power point. The HHO-based MPPT approach provides faster maximum power point (MPP) tracking, decreased computing burden, and increased efficiency.	[51]
2020	Data dissemination for the Internet of Things	This study offers reliable data dissemination for the Internet of Things using HHO technique, which is a safe data diffusion mechanism for wireless sensor networks (WSN)-based IoT that accoutered a fuzzy hierarchical network model.	Simulation results show that RDDI delivers a more dependable approach and a better result than the other three disposals.	[52]
2020	Image segmentation	The HHO algorithm and the lowest cross-entropy as a fitness function are used to provide an efficient approach for multilevel segmentation in this work.	This HHO-based method outperforms other segmentation methods currently in use in the literature.	[53]
2020	Modeling of rainfall–runoff	To simulate the rainfall–runoff connection, data-driven approaches such as a multilayer perceptron (MLP) neural network and least squares support vector machine (LSSVM) are combined with a sophisticated nature-inspired optimizer, namely HHO.	All of the enhanced models with HHO outperformed other integrated models with PSO in predicting runoff changes, according to the findings. Furthermore, when HHO was combined with LSSVM, a high degree of accuracy in forecasting runoff levels was attained.	[54]
2020	Image segmentation	The HHO technique is used in this study to find reduced pulse coupled neural network settings.	The results of the experiments show that the HHO method is superior in image segmentation.	[55]

Table 1. Cont.

Year	Area of Application	Research Objectives	Research Findings	Reference No.
2020	Prediction of scour depth downstream of the ski-jump spillway	To forecast scour depth (SD) downstream of the ski-jump spillway, an alternative to standard techniques was used in this study. To improve the performance of an artificial neural network (ANN) to predict the SD, a novel optimization technique HHO was suggested.	The ANN-HHO model beat other existing models during the testing period, according to the findings. Furthermore, graphical evaluation reveals that the ANN-HHO model is more accurate than other models in predicting SD near the ski-jump spillway.	[56]
2020	Optimal power flow	By addressing single and multiobjective Optimal Power Flow (OPF) problems, this study provides a unique nature-inspired and population-based HHO approach for reducing emissions from thermal producing sources.	The findings are compared to artificial intelligence (AI), whale optimization algorithm (WOA), salp swarm algorithm (SSA), moth flame (MF), and glow warm optimization (GWO). Furthermore, according to the study on DG deployment, system losses and emissions are decreased by 9.83% percent and 26.2%, respectively.	[57]
2020	Water distribution network	A model based on the HHO was created to optimize the water distribution network for a one-month period, in Homashahr, Iran.	The findings showed that the HHO algorithm performed effectively in the challenge of optimal water supply network design. This method was equivalent to approximately 12% of the optimization in the end.	[58]
2020	Design of load frequency control	The best settings of the proportional-integral (PI) controller modeling load frequency control (LFC) in a multi-interconnected system with renewable energy sources are evaluated using a reliable technique-based HHO.	The collected findings proved the validity and superiority of the suggested HHO-based strategy for developing LFC for the systems under consideration.	[59]
2019	Design of microchannel heat sinks	For the reduction of entropy production, a unique Harris hawks optimization technique is used to microchannel heat sinks. The slip velocity and temperature jump boundary conditions were taken into account when creating the microchannel heat transfer model.	The Harris hawks method outperforms the other algorithms in terms of reducing microchannel entropy production.	[60]

Motivation and Contributions

The primary motivation behind this work is to design a novel technique for appropriate allocation and sizing of solar photovoltaic DGs to reduce power losses and enhance the voltage profile. Worldwide sustainable development is possible through the generation of electricity from renewable energy resources. The Indian government has taken a number of steps to stimulate the use of renewable energy (RE) resources, including setting state-specific RE objectives in the form of solar purchase obligations (SPO) and renewable purchase obligations (RPO). Every state has set a goal to fulfill a significant part of its overall energy demand from renewable resources under the provisions of RPO and SPO. The solar photovoltaic DGs (PV DG) considered in this paper are among all the renewable energy resources; solar energy has received major importance due to its abundant availability worldwide. Although researchers have previously used a variety of

approaches to tackle the problem of DG allocation and size in the power system network, the authors have not considered the actual field installation capacity of PV DG; instead, they have considered only the actual power to be injected. Whereas the output of the solar PV DG is a meteorological parameter and PV module parameter-dependent system, thus, it is imperative to calculate the actual size of the PV DG to be installed to inject the targeted power into the grid. The contribution of this work is presented below:

- The proposed HHO has been tested with complex benchmark functions;
- Assign a novel approach for appropriate allocation and sizing of PV DGs in IEEE 33 bus and IEEE 69 bus power system network using HHO to minimize the power losses and improve the voltage profile;
- Compare the simulation outcomes of the proposed technique together with the recently available methods such as the teaching–learning–based optimization (TLBO), genetic algorithm (GA), particle swarm optimization (PSO), quasi-oppositional TLBO (QOTLBO), comprehensive teaching learning-based optimization (CTLBO), CTLBO ϵ -method, improved multiobjective elephant herding optimization (IMOEHO), improved decomposition-based evolutionary algorithm (I-DBEA), bat algorithm (BA), simulated annealing (SA), invasive weed optimization (IWO), bacterial foraging optimization algorithm (BFOA), and moth–flame optimization (MFO) to determine the effectiveness of the proposed algorithm over the exciting ones;
- Calculate the actual/practical size of the solar PV DG units to be installed to inject the targeted power into the power system grid.

The remainder of this article is structured in the following order. The mathematical formulation of the problem with various constraints is detailed in Section 2. The detail of the proposed HHO and the solution approach for the considered problem is presented in Section 3. In Section 4, the problem is tested with a benchmark function and with standard test systems. Section 5 deals with the practical calculation of solar PV DG. Section 6 concludes with some final observations together the breadth of future development.

2. Formulation of the Mathematical Problem

2.1. Loss Minimization

The objective of the present work is to relax the congestion in power lines along with determining the proper size and optimal location of DGs while keeping the losses (202.67 kW and 224.9 kW for IEEE 33 and IEEE 69 bus RDS, respectively) to the minimum. The major objective function (OF) is framed in the form of total system losses. Therefore, the OF may be stated by Equation (1).

$$OF = \text{Minimize}(P_{Loss}) \quad (1)$$

where

$$P_{Loss} = \sum_{k=1}^n g_k \left(V_i^2 + V_j^2 - 2V_i \times V_j \times \cos(\delta_i - \delta_j) \right) \quad (2)$$

The various constraints of the proposed optimization problem are as stated in Equations (3)–(7).

$$V_i^{min} \leq V_i \leq V_i^{max} \quad (3)$$

$$P_{DG}^{min} \leq P_{DG} \leq P_{DG}^{max} \quad (4)$$

$$Q_{DG}^{min} \leq Q_{DG} \leq Q_{DG}^{max} \quad (5)$$

$$Q_{G_i}^{min} \leq Q_{G_i} \leq Q_{G_i}^{max} \quad (6)$$

$$P_{G_i}^{min} \leq P_{G_i} \leq P_{G_i}^{max} \quad (7)$$

where g_k is the conductance of branch k ; V_i and V_j are the magnitude of voltages at sending and receiving bus, respectively; P_{DG} and Q_{DG} represent active and reactive power

generation by DG; δ_i is the phase angle at i th and j th bus, respectively; and P_{G_i} represents active power generation at i th bus.

In Equations (3)–(7), the superscripts max and min represent the upper and the lower limits of the respective variables. The major objective here is to reduce congestion in lines and minimize losses.

2.2. Practical Sizing of PV DG

The power output of the PV module depends on meteorological parameters (such as ambient temperature and solar irradiance at the particular location) and on the parameters of the PV modules. To address the dependence on solar irradiation, the beta probability density function was used to model the uncertain nature of solar irradiance. The distribution of solar irradiance may be written as Equation (8) [61].

$$f_b(s) = \begin{cases} \frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} s^{(\alpha-1)} (1-s)^{(\beta-1)} & 0 \leq s \leq 1 \text{ \& } \alpha, \beta \geq 0 \\ 0 & \end{cases} \quad (8)$$

$$\beta = (1-\mu) \left(\frac{\mu(1-\mu)}{\sigma^2} - 1 \right) \quad (9)$$

$$\alpha = \frac{\mu\beta}{(1-\mu)} \quad (10)$$

where $\Gamma(\cdot)$ is defined as the gamma function, s is defined as the random variable of solar irradiance, $f_b(s)$ is defined as the beta distribution function of s , α and β are defined as the parameters of the beta distribution function, μ and σ are defined as the mean and standard deviation of s .

Equations (11)–(13) have been used to address the effect of ambient temperature on the output of the PV module. The temperature of the PV module is influenced by the nominal operating module temperature (NOMT), solar irradiance, and ambient temperature, as shown by Equation (11) [62].

$$T_M = T_A + s \left(\frac{\text{NOMT} - 20}{0.8} \right) \quad (11)$$

The output current of the PV module is a function of the solar irradiance, short-circuit current, temperature coefficient of current, and temperature of PV module, shown by Equation (12) [63].

$$I_M = s[I_{SC} + \varepsilon_i(T_M - 25)] \quad (12)$$

The voltage of the PV module is a function of the open-circuit voltage, voltage temperature coefficient of the module, and its temperature, as shown by Equation (13).

$$V_M = [V_{OC} - \varepsilon_v(T_M - 25)] \quad (13)$$

$$FF_M = \frac{I_{mpp} \times V_{mpp}}{I_{SC} \times V_{OC}} \quad (14)$$

Considering aforesaid environmental and PV module parameters correction factors, Equation (14) will be modified to Equation (15).

$$FF_M = \frac{I_{mpp} \times V_{mpp}}{I_M \times V_M} \quad (15)$$

The output power of PV module, operating at maximum power point at solar irradiance s , may be estimated using Equation (16).

$$P_o(s) = I_{mpp} \times V_{mpp} = FF_M \times I_M \times V_M \quad (16)$$

The output power of the PV plant, operating at maximum power point at solar irradiance s may be estimated using Equation (17) [64].

$$P_o(s) = N_M \times FF_M \times I_M \times V_M \quad (17)$$

The power output from the PV module considering maximum power point may be obtained by Equations (14) and (15). The variables used are defined as follows: T_M is the temperature of the PV module; T_A is the ambient temperature; NOMT is the nominal operating module temperature; I_M is the current of the PV module; V_M is the voltage of the PV module; I_{SC} is the short-circuit current of PV module; V_{OC} is the open-circuit voltage of PV module; ε_i is the temperature coefficient of current; ε_v is the temperature coefficient of voltage; I_{mpp} is the current at maximum power point at standard test condition (STC); V_{mpp} is the voltage at maximum power point at STC; FF_M is defined as the fill factor; N_M denotes the number of PV modules used in the PV plant; and $P_o(s)$ is the power output from the PV module ($N_M = 1$)/plant at solar irradiance s .

The expected output power from the PV module considering the effect of solar irradiance s and ambient temperature T_A may be calculated using Equation (18), and the expected total output power for a specific time period may be calculated using Equation (19) [64].

$$EOP(s) = P_o(s) \times f_b(s) \quad (18)$$

$$ETOP = \int_0^1 EOP(s) ds \quad (19)$$

Monocrystalline silicon PERC PV module of the following specifications as presented in Table 2, was used for calculation [65].

$$\varepsilon_i = T_i \times I_{mpp} \quad (20)$$

$$\varepsilon_v = T_v \times V_{mpp} \quad (21)$$

Table 2. PV module parameters.

Parameter	Specification
Nominal power— P_{mpp} (Wp)	350
V_{mpp} (V)	38.9
I_{mpp} (A)	9.0
V_{OC} (V)	46.7
I_{SC} (A)	9.72
T_v (Temperature coefficient of voltage)	−0.30 %/°C
T_i (Temperature coefficient of current)	0.066 %/°C
NOMT	44.6 °C
Area	2.01 m ²

To convert the temperature coefficient of voltage and current from %/°C (T_i and T_v) to A/°C (ε_i) and V/°C (ε_v), Equations (20) and (21) are used, respectively. Impact of NOMT and irradiance on the temperature, voltage, and current of the PV module are depicted in Figure 1.

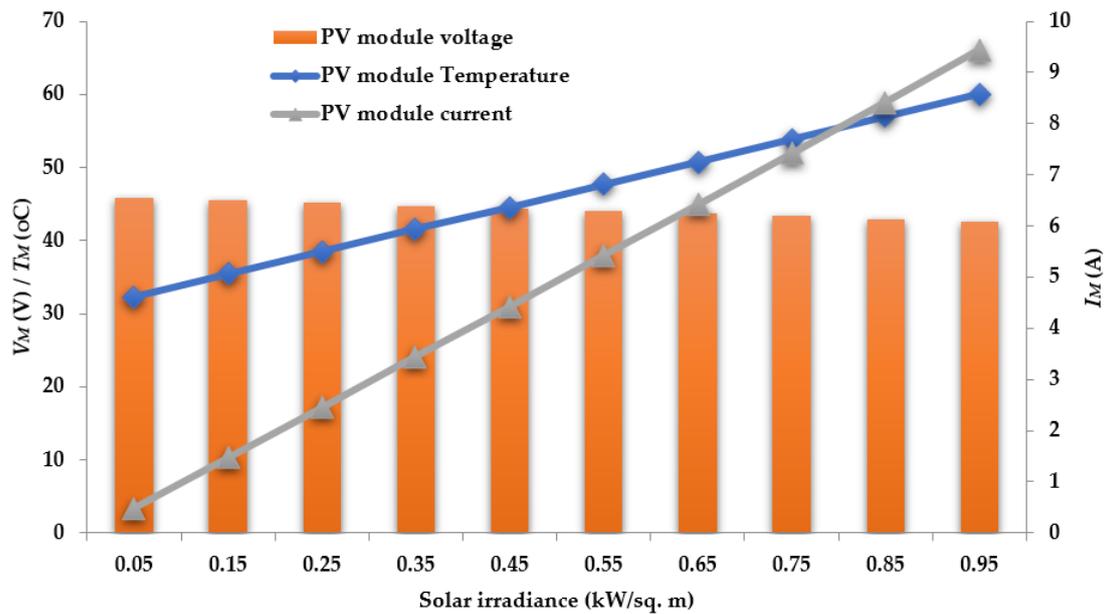


Figure 1. Different PV module parameters considering the NOMT and solar irradiance.

Considering the parameters effecting the output of PV module, it is observed that the voltage and the current of the PV module varies from 45.85 to 42.62 V and 0.49 to 9.43 A, respectively, with the variation of solar irradiance. The temperature of the PV module varies from 32.3 to 60 °C as irradiance changes, as shown in Figure 1.

The ambient temperature, mean, and standard derivation of solar irradiance during a specified time period are considered as 30.76°, 0.52 kW/m², and 0.21 kW/m², respectively [61]. The expected output power from the PV module considering the effect of solar irradiance and ambient temperature, associated environmental parameters, PV module parameters and modeling parameters are tabulated in Table 3.

Table 3. The expected output power from the PV module considering correction factors.

Environmental Parameters		PV Module Parameters Considering Correction Factors		Modeling Parameters		Output	
<i>s</i>	<i>T_A</i>	<i>I_M</i>	<i>V_M</i>	<i>f_b(s)</i>	<i>β</i>	<i>P_o(s)</i>	<i>EOP(s)</i>
0.05	30.76	0.49	45.85	2.16	0.14	17.26	2.38
0.15	30.76	1.47	45.49	2.16	0.56	51.48	28.66
0.25	30.76	2.45	45.13	2.16	0.98	85.28	83.44
0.35	30.76	3.44	44.77	2.16	1.32	118.66	156.88
0.45	30.76	4.43	44.41	2.16	1.54	151.62	234.05
0.55	30.76	5.42	44.05	2.16	1.62	184.16	297.55
0.65	30.76	6.42	43.70	2.16	1.52	216.27	329.15
0.75	30.76	7.42	43.34	2.16	1.26	247.95	311.49
0.85	30.76	8.42	42.98	2.16	0.83	279.20	230.65
0.95	30.76	9.43	42.62	2.16	0.27	310.02	83.51
						Average	175.78

The power output from the PV module *P_o(s)* and *f_b(s)* with respect to solar irradiance *s* is presented in Figure 2.

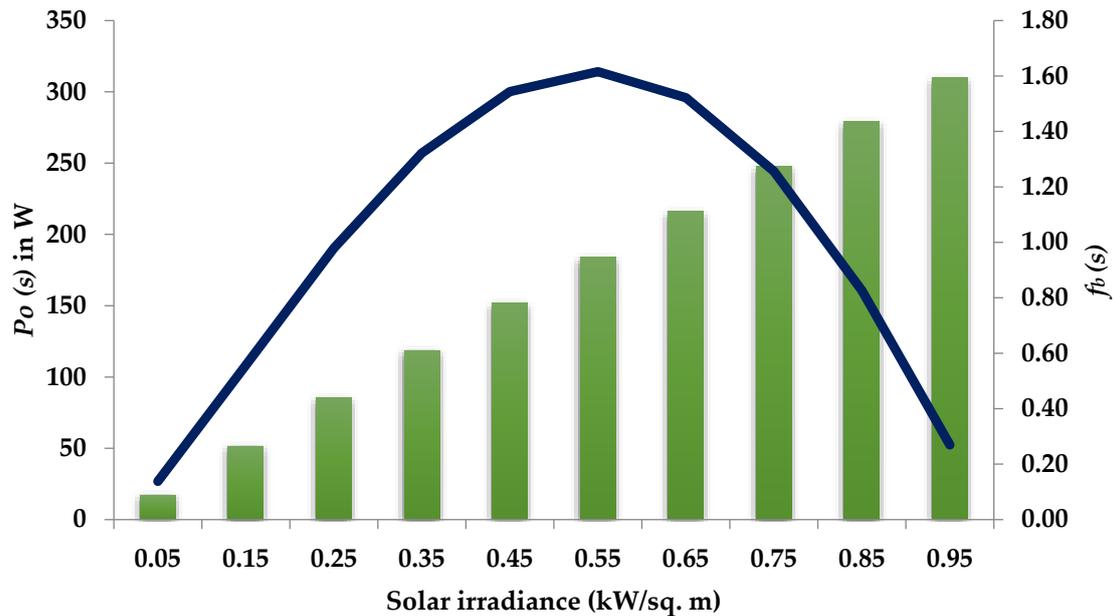


Figure 2. Output power from the PV module at different solar irradiance s .

The expected total power obtained from a single PV module is the average of $EOP(s)$, which is shown in Table 3 and depicted in Figure 3, i.e., 175.78 W.

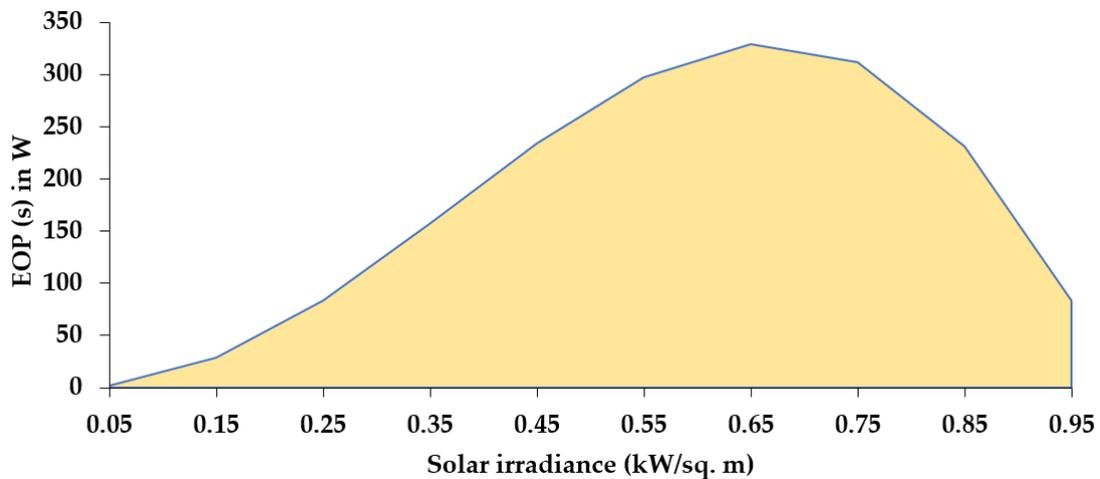


Figure 3. Expected output power from the PV module.

3. Proposed HHO and Solution Approach

3.1. HHO: Features

The Harris hawks is a recent population-based and gradient-free metaheuristic [66], hence, equally applicable to all optimization models or problems. The different phases of Harris hawks formulation are described in the next subsections.

3.2. Exploration Phase

In this phase, Harris hawks randomly search on locations and adopt a wait and watch strategy to catch the prey, as per Equation (22) [66].

$$X(t+1) = \begin{cases} X_{rand}(t) - r_1 |X_{rand}(t) - 2r_2 X(t)| & q \geq 0.5 \\ (X_{rabit}(t) - X_m(t)) - r_3(LB + r_4(UB - LB)) & q < 0.5 \end{cases} \quad (22)$$

where X_{rabbit} is the rabbit position and $X(t+1)$ is the hawks' position for next iteration; $x(t)$ shows the current position of the hawks. The LB and UB are maximum and minimum of decision variables. $X_{rand}(t)$ is a randomly selected hawk from the current position. The random number in the range (0,1) is shown by the $r_{(1-4)}$.

$$X_m(t) = \frac{1}{N} \sum_{i=1}^N X_i(t) \quad (23)$$

where X_m is the mean of the current population of hawks while N indicates the hawks' total population.

Assuming the energy of the rabbit is given by

$$E = 2E_o \left(1 - \frac{t}{T}\right) \quad (24)$$

E , E_o , and T represent the escaping energy of prey, primary energy, and the maximum number of iterations taken, respectively.

3.3. Exploitation Phase

3.3.1. Soft Besiege

This behavior is demonstrated by Equation (25) [66].

$$X(t+1) = \Delta X(t) - E|JX_{rabbit}(t) - X(t)| \quad (25)$$

$$\Delta X(t) = X_{rabbit}(t) - X(t) \quad (26)$$

where $X(t)$ and J represent the difference between the position vector of the rabbit and the current location in iteration and the random jump strength of the rabbit, respectively.

3.3.2. Hard Besiege

This behavior is showcased by (27).

$$(t+1) = X_{rabbit}(t) - E|\Delta X(t)| \quad (27)$$

3.3.3. Soft Besiege along with Rapid Drives

In this behavior, it is assumed that hawks may choose their next step provided by the rule given in Equation (28) [66].

$$Y = X_{rabbit}(t) - E|JX_{rabbit}(t) - X(t)| \quad (28)$$

$$Z = Y + S \times LF(D) \quad (29)$$

D , S , and LF are problem dimensions, a random number of order $(1 \times D)$, and levy flight function, respectively. In addition, u and v are random numbers (0 to 1 range), while β is the default constant value (assuming 1.5).

$$LF(x) = 0.01 \times \frac{U \times \sigma}{|\theta|^{\frac{1}{\beta}}}, \quad \sigma = \left(\frac{\Gamma(1+\beta) \times \sin\left(\frac{\pi\beta}{2}\right)}{\Gamma\left(\frac{1+\beta}{2}\right) \times \beta \times 2^{\left(\frac{\beta-1}{2}\right)}} \right)^{\frac{1}{\beta}} \quad (30)$$

Soft besiege updates the position of the hawks by

$$X(t+1) = \begin{cases} Y, & \text{if } F(Y) < F(X(t)) \\ Z, & \text{if } F(Z) < F(X(t)) \end{cases} \quad (31)$$

3.3.4. Hard Besiege along with Rapid Drives

Hard besiege condition given by the following rule:

$$X(t+1) = \begin{cases} Y, & \text{if } F(Y) < F(X(t)) \\ Z, & \text{if } F(Z) < F(X(t)) \end{cases} \quad (32)$$

$$Y = X_{rabit}(t) - E|JX_{rabit}(t) - X_m(t)| \quad (33)$$

$$Z = Y + S \times LF(D) \quad (34)$$

The step-by-step procedure of HHO is summarized to the pseudocode, as shown in Figure 4 [66].

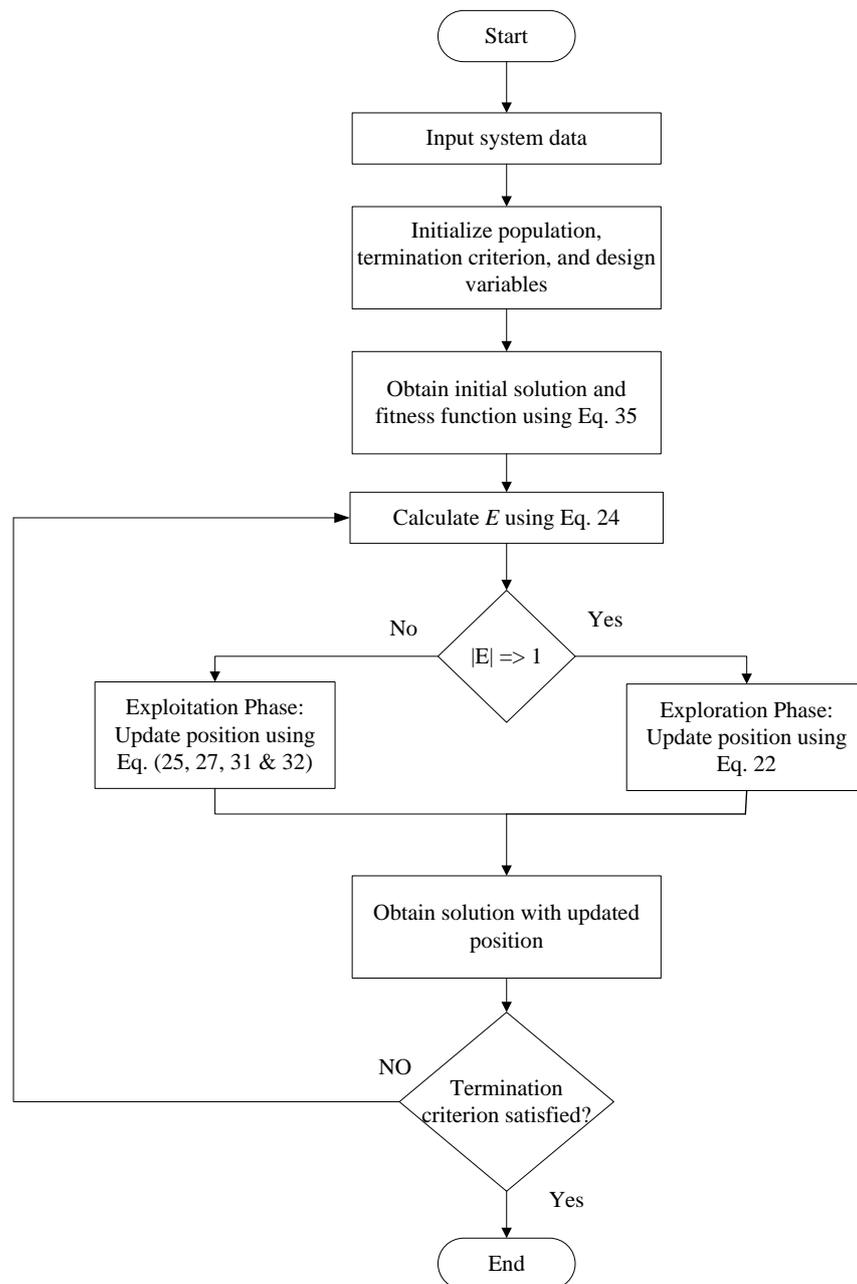


Figure 4. Flow chart of HHO. Reproduced from [66], Elsevier: 2019.

3.4. Solution Approach

3.4.1. HHO for PV DG Placement and Location

The major goal of this research is to determine the best placement and size for numerous PV DGs with the least amount of network power loss and a better voltage profile. In this work, the inequality constraints are converted to the penalty functions (PFs), and these PFs are added to the OF to construct the fitness function (FF) defined in Equation (35).

$$\text{Minimum FF} = \text{OF} + \text{PF} \times \sum_{j=1}^{VB} (\Delta V_j)^2 \quad (35)$$

Here, FF is essential to be minimized in order to get minimum loss value, VB represents the set of overloaded lines and voltage violated load buses, and PF represents the penalty factor. The violation in inequality constraints such as load bus voltage and line power flows was handled using the penalty function approach. PF that represents penalty factor was taken as 10,000 throughout the simulation process.

3.4.2. Computational Practice of HHO for DG Location and Values

Step 1 Read the input data of the system, such as the maximum number of iterations, number of PV DG units, and population size.

Step 2 Generate the value of the size of PV DG within their upper (DG_{max}) and lower limits (DG_{min}). The same is shown in Equation (36).

$$DG_i = DG_i^{min} + rand \times (DG_i^{max} - DG_i^{min}) \quad (36)$$

Here, DG_i represents the size of i th DG unit. Now, constitute a vector X_j , that contains the possible locations (LOC) and size of DGs as mentioned in Equation (37).

$$X_j = [DG_{j,1}, DG_{j,2}, \dots, DG_{j,n}, LOC_{j,1}, LOC_{j,2}, \dots, LOC_{j,n}] \quad (37)$$

The LOC is generated randomly. Initial solution set X is then formulated as shown in Equation (38).

$$X = [X_1, X_2, \dots, X_N] \quad (38)$$

Step 3 Evaluation of the fitness function is processed using Equation (35) for individual Harris hawks, and the best hawk location is acknowledged.

Step 4 Calculate E using Equation (24).

Step 5 Exploration phase: Update the location of Harris hawks using Equation (22).

Step 6 Exploitation phase: Update the position using Equation (25), (27), (31), and (32).

Step 7 Once the number of iterations reaches the maximum value, then terminate. Else, go back to Step 3.

4. Simulation Results and Discussions

4.1. Testing Strategies

The simulations were run on a MATLAB 9.9 computer with an Intel i3 CPU running at 2.4 GHz and 4 GB of RAM. The software utilized is MATPOWER 7.2, which is a well-known power modeling tool.

4.2. Case 1

In order to establish an algorithm, the proposed HHO was tested with selected extremely complex benchmark functions taken from CEC-2014 (see Table 4). The results obtained are tabulated in Table 5. The HHO seems to provide very competitive results as compared to other recent metaheuristic optimization techniques.

Table 4. Summary of the CEC-2014 benchmark functions considered.

Type	ID	Functions	Fi = Fi(x)
Unimodal	F1	Rotated High Conditioned Elliptic	100
	F2	Rotated Bent Cigar	200
Simple Multimodal	F3	Shifted and Rotated Rastrigin's	900
	F4	Shifted Schwefel's	1000
Hybrid	F5	Hybrid Function 3 (N = 4)	1900
	F6	Hybrid Function 4 (N = 4)	2000
Composition	F7	Composition Function 8 (N = 3)	3000

Table 5. Comparative experimental outcomes on selected benchmark functions.

ID	Parameters	PSO	TLBO	CS	GSA	SFS	HHO
F1	max	4.56×10^8	8.93×10^8	5.51×10^8	5.31×10^7	1.17×10^6	3.01×10^5
	min	2.47×10^8	4.39×10^7	1.18×10^8	4.56×10^6	1.54×10^5	1.43×10^4
	median	3.31×10^8	3.42×10^8	3.10×10^8	8.37×10^6	6.16×10^5	1.52×10^5
	std	7.92×10^7	3.42×10^8	1.05×10^8	1.32×10^7	2.35×10^5	1.23×10^5
F2	max	3.63×10^{10}	4.06×10^4	2.42×10^4	1.61×10^4	2.00×10^2	2.00×10^2
	min	6.00×10^7	6.00×10^3	3.09×10^2	3.47×10^3	2.00×10^2	2.00×10^2
	median	1.55×10^{10}	1.52×10^4	8.08×10^3	8.38×10^3	2.00×10^2	2.00×10^2
	std	1.43×10^{10}	8.65×10^3	6.00×10^3	2.90×10^3	7.89×10^{-9}	0.00
F3	max	1.24×10^3	1.12×10^3	1.34×10^3	1.10×10^3	9.84×10^2	9.03×10^2
	min	1.13×10^3	1.06×10^3	1.15×10^3	1.02×10^3	9.35×10^2	9.20×10^2
	median	1.18×10^3	1.09×10^3	1.25×10^3	1.06×10^3	9.61×10^2	9.19×10^2
	std	4.33×10	0.25×10^2	4.41×10	1.74×10	1.11×10	1.017×10
F4	max	7.90×10^3	5.92×10^3	3.21×10^3	5.25×10^3	2.71×10^3	1.05×10^3
	min	6.26×10^3	4.14×10^3	1.36×10^3	3.45×10^3	1.02×10^3	1.00×10^3
	median	7.18×10^3	5.06×10^3	2.17×10^3	4.37×10^3	1.49×10^3	1.01×10^3
	std	5.98×10^2	7.89×10^2	4.33×10^2	3.61×10^2	3.62×10^2	1.45×10
F5	max	2.10×10^3	1.91×10^3	2.04×10^3	2.00×10^3	1.91×10^3	1.92×10^3
	min	1.91×10^3	1.90×10^3	1.91×10^3	1.91×10^3	1.90×10^3	1.90×10^3
	median	1.97×10^3	1.91×10^3	1.92×10^3	2.00×10^3	1.91×10^3	1.91×10^3
	std	7.07×10	1.65	3.30×10	3.43×10	1.47	1.46
F6	max	4.37×10^3	5.34×10^3	6.02×10^4	6.82×10^4	2.10×10^3	2.75×10^3
	min	2.55×10^3	2.30×10^3	2.22×10^4	2.32×10^3	2.02×10^3	2.00×10^3
	median	3.00×10^3	2.74×10^3	3.68×10^4	1.77×10^4	2.06×10^3	2.26×10^3
	std	5.32×10^2	7.00×10^2	8.42×10^4	1.39×10^4	2.60×10	2.06×10^2
F7	max	9.70×10^5	1.56×10^6	5.08×10^5	1.14×10^5	7.66×10^3	5.62×10^3
	min	6.90×10^4	2.08×10^4	6.26×10^4	1.22×10^4	4.25×10^3	3.56×10^3
	median	3.35×10^5	6.56×10^5	1.77×10^5	1.46×10^4	5.63×10^3	4.71×10^3
	std	3.63×10^5	5.64×10^5	9.11×10^4	1.84×10^4	7.38×10^2	1.30×10^3

4.3. Case 2

The proposed HHO-based approach is applied to find the suitable location and capacity of the DGs in the IEEE 33-bus RDS test system where the network and load data may be obtained from [67]. The single line diagram of the IEEE 33-bus RDS is shown in Figure 5. IEEE 33-bus RDS has a total of 33 buses, among which 32 are load buses and 1 is a generator bus. It can be visualized from Figure 5 that at bus no. 1 generator is connected; the other buses may have any type of load connected, as per the requirement. The total active power demand is 3.72 MW while reactive is 2.3 MVAR. Total power loss of the system is 202.67 kW.

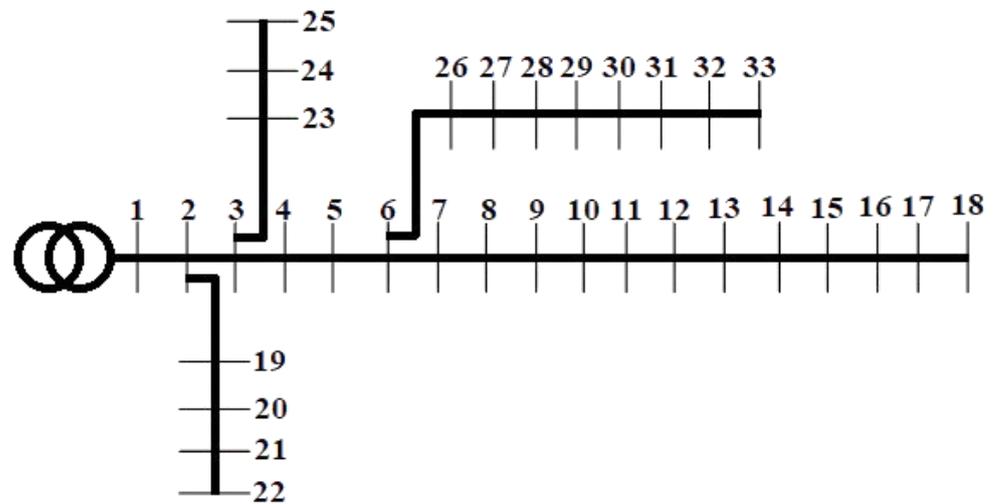


Figure 5. Single line diagram of IEEE 33-bus RDS.

In order to find candidate buses for locating a PV DG using this approach for each individual bus, it is assumed that there is a PV DG at that bus at a time. For optimal sizing of a PV DG at this stage, it is assumed that the PV DG may produce electric power in all possible ranges (e.g., 0–1 MW). The proposed HHO algorithm is applied for the minimization of overall loss as the objective function of the problem. First, only one PV DG is used to relax the congestion in lines, and the results obtained are tabulated in Table 6. With the application of proposed HHO on distribution problem, the losses are reduced to 129.2 from 202.67 kW with only one DG in installation of size 0.95 MW.

Table 6. Variation in power loss with change in an optimal allocation of PV DGs.

Test System	Buses Count	Array Location	P_{loss} (kW)	Loss Reduction (%)
33 bus system	1	30	129.20	38.76
	2	12, 30	86.90	58.81
	3	13, 24, 30	72.10	64.42

For further improvement, the problem is tested by installing two and three PV DGs in the power network. The results obtained are presented in Table 6. The overall active power losses decreased to 86.9 and 72.10 kW with the application of two and three PV DGs, respectively, using HHO. The comparative results are portrayed in Table 7 in terms of the best location and size of PV DGs. The locations suggested by HHO to install PV plants in IEEE 33 bus are depicted in Figure 6.

Table 7. Comparative results for optimal location and values of PV DGs corresponding to case 2.

Optimization Method	Bus Count	Array Location	DG Size (MW)	Total DG Size (MW)	P_{loss} (kW)	Loss Reduction (%)
Base case	-	-	-	-	202.67	0.00
TLBO [68]	3	12	1.1826	3.560	124.70	38.47
		28	1.1913			
		30	1.1863			
GA [69]	3	11	1.5000	2.994	106.30	47.55
		29	0.4230			
		30	1.0710			
PSO [69]	3	8	1.1770	2.989	105.30	48.04
		13	0.9820			
		32	0.8300			

Table 7. Cont.

Optimization Method	Bus Count	Array Location	DG Size (MW)	Total DG Size (MW)	P_{loss} (kW)	Loss Reduction (%)
GA/PSO [69]	3	11	0.9250	2.998	103.40	48.98
		16	0.8630			
		32	1.2000			
QOTLBO [68]	3	13	1.0834	3.470	103.40	48.98
		26	1.1876			
		30	1.1992			
CTLBO ϵ -method [70]	3	13	1.1926	3.693	96.17	52.55
		25	0.8706			
		30	1.6296			
IMOEOHO [71]	3	14	1.0570	3.852	95.00	53.13
		24	1.0540			
		30	1.7410			
I-DBEA [72]	3	13	1.0980	3.913	94.85	53.20
		24	1.0970			
		30	1.7150			
CTLBO [70]	3	13	1.0364	3.721	85.96	57.59
		24	1.1630			
		30	1.5217			
BA [39]	3	15	0.81630	2.721	75.05	62.97
		25	0.95235			
		30	0.95235			
HHO [Proposed]	3	13	0.8311	2.731	72.10	64.42
		24	0.9500			
		30	0.9500			

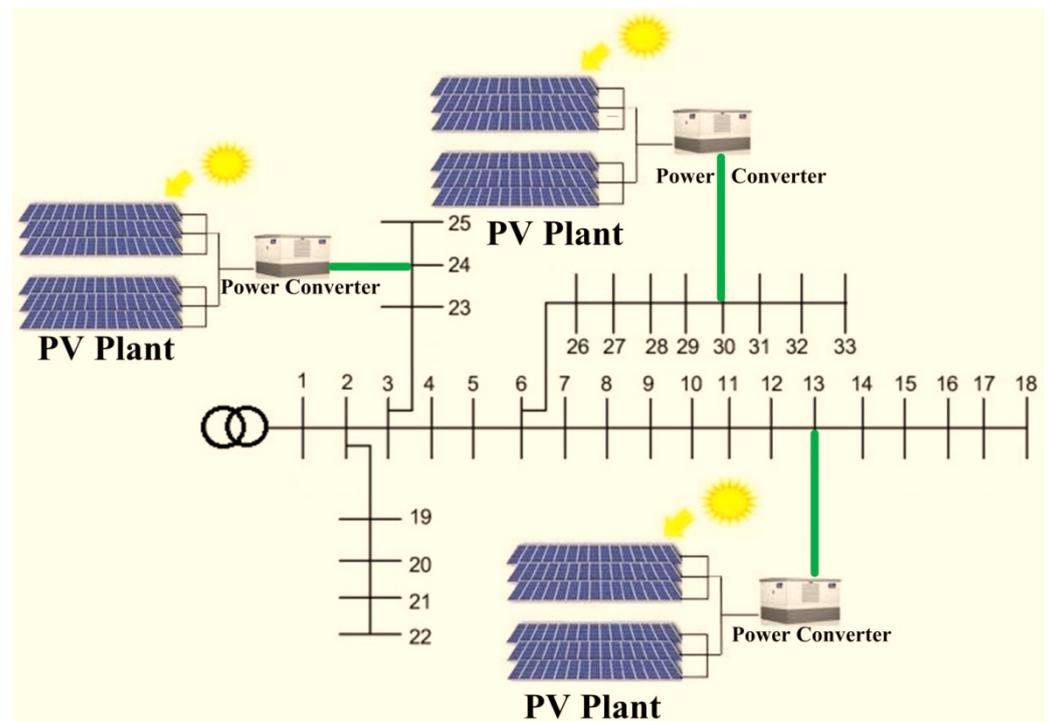


Figure 6. IEEE 33 bus line diagram with PV plants at locations suggested by HHO.

The size and location suggested by HHO (refer to Table 7) provide maximum reduction in losses as compared to TLBO [68], GA [69], PSO [69], GA/PSO [69], QOTLBO [68], CTLBO ϵ -method [70], IMOEOHO [71], I-DBEA [72], CTLBO [70], and BA [39]. In addition, the voltage graph of all the buses obtained after utilization of PV DGs is showcased in Figure 7.

The bus voltages are obtained from the load flow analysis. The bus voltage profile improves significantly under the application of three PV DGs at their respective optimal locations. The variation of fitness function against the number of iterations for installation with three PV DGs using HHO is showcased in Figure 8. The iterative graph shows that the HHO converges to an optimal solution value with very few iterations.

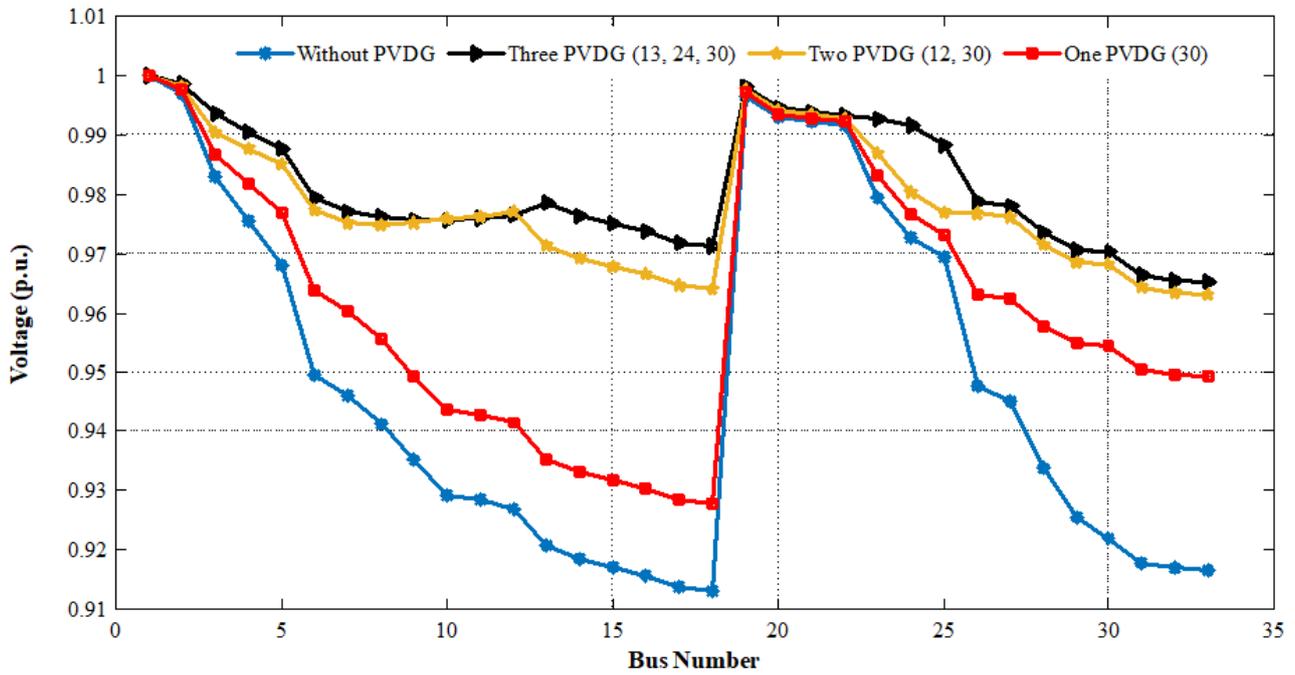


Figure 7. Voltage graph for IEEE 33 bus system without and with PV DGs.

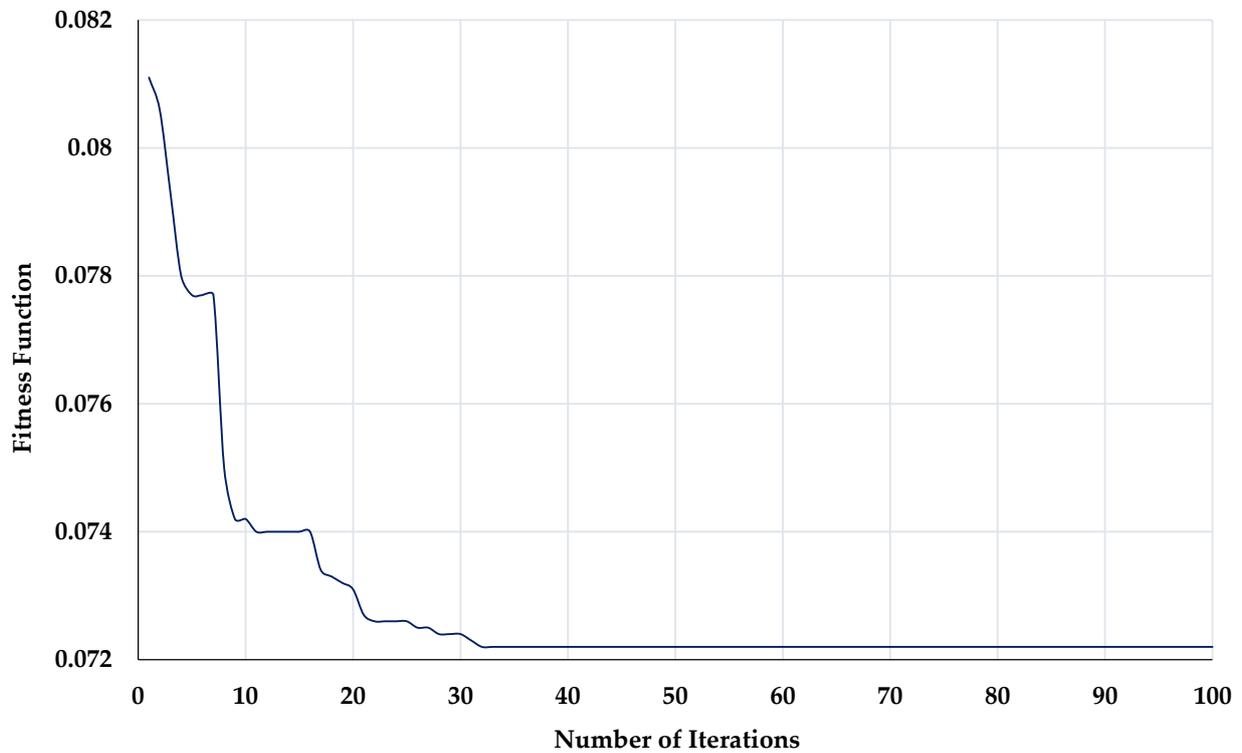


Figure 8. Convergence characteristics of fitness function pertaining to case 2 (with three PV DG).

4.4. Case 3

To test the effectiveness of the HHO on a larger system, the proposed approach is tested to find the suitable location and capacity (size) of the DGs in the IEEE 69 bus RDS test system where the load and branch data values may be obtained from [73]. The single line diagram of the IEEE 69-bus RDS is shown in Figure 9. IEEE 69-bus RDS consists of 69 buses, including 68 load buses and 1 generator bus. The generator is connected at bus no. 1 and a load of the required amount can be connected to the other buses. The total active power demand is 3.80 MW while reactive is 2.69 MVAR. Total power loss of the system is 224.9 kW.

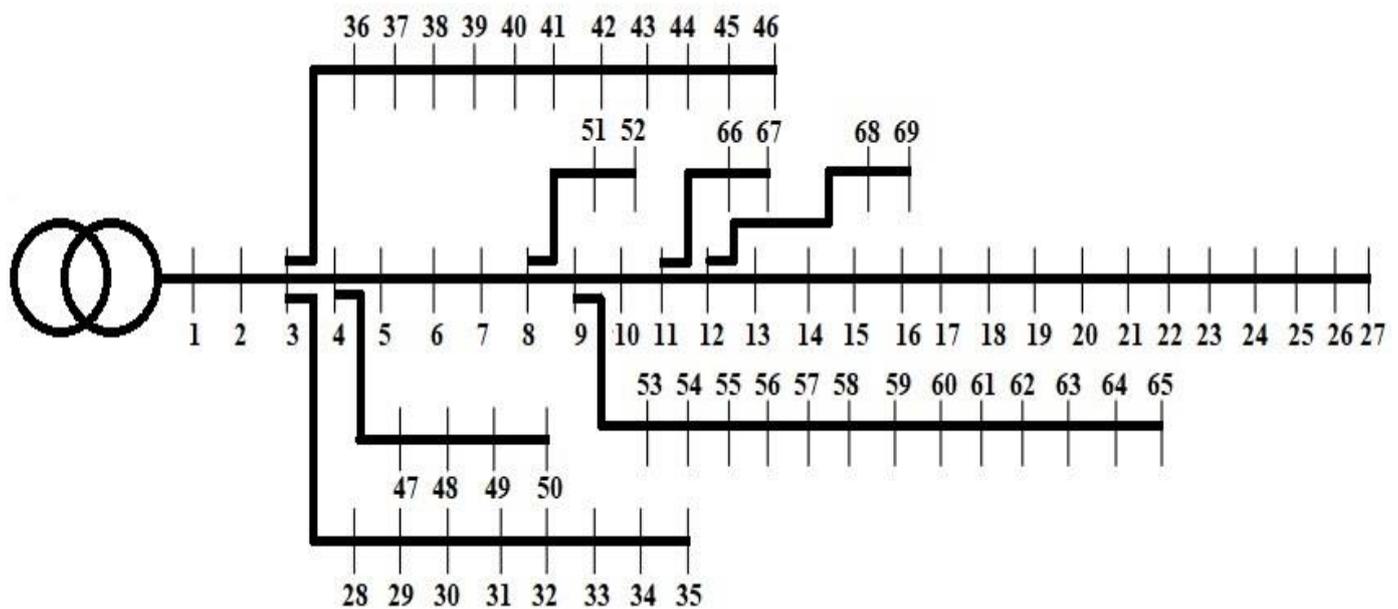


Figure 9. Single line diagram of IEEE 69-bus RDS.

For addressing the most suitable candidate buses for locating a PV DG using this approach for each individual bus, it is assumed that there is a PV DG at that bus at a time. For optimal sizing of a PV DG at this stage, it is assumed that the PV DG may produce electric power in all possible ranges (e.g., 0–1 MW). The proposed HHO algorithm is applied for the reduction/minimization of overall loss as the objective function of the problem. First, only one PV DG is used to relax the congestion and reduce losses in lines, and the results obtained are tabulated in Table 8. The installation of one optimum PV DG the line losses reduced by 48.86% with DG size of 0.95 MW.

Table 8. Variation in power loss with change in an optimal allocation of PV DGs.

Test System	Bus Count	Array Location	DG Size (MW)	P_{loss} (kW)	Loss Reduction (%)
69 bus system	1	61	0.95	115	48.866
	2	61, 62	0.95, 0.9118	83.4	62.916
	3	17, 61, 62	0.5329, 0.95, 0.822	71.8	68.074

For further improvement, the problem is tested by installing two and three PV DGs in the power network. The results obtained are presented in Table 8. The overall active power losses decreased to 71.80 kW with the application of three PV DGs using HHO. The comparative results are portrayed in Table 9 in terms of the best location and size of PV DGs. The locations suggested by HHO to install PV plants in the IEEE 69 bus are depicted in Figure 10.

Table 9. Comparative results for optimal location and values of PV DGs corresponding to case 3.

Optimization Method	Bus Count	Array Location	DG Size (MW)	Total DG Size (MW)	P_{loss} (kW)	Loss Reduction (%)
Base case	-	-	-	-	224.9	0.00
GA [69]	3	21	0.9297	2.9897	89	60.43
		62	1.0752			
PSO [69]	3	64	0.9848	2.9879	83.2	60.43
		61	1.1998			
		63	0.7956			
TLBO [68]	3	17	0.9925	3.1636	82.172	63.46
		13	1.0134			
		61	0.9901			
GA/PSO [69]	3	62	1.1601	2.988	81.1	63.94
		63	0.8849			
		61	1.1926			
QOTLBO [68]	3	21	0.9105	2.9606	80.585	64.17
		15	0.8114			
		61	1.1470			
CTLBO ϵ -method [70]	3	63	1.0022	3.3301	79.66	64.58
		12	0.9658			
		25	0.2307			
I-DBEA [72]	3	61	2.1336	3.32	78.347	65.16
		61	2.1487			
		19	0.4717			
SA [74]	3	11	0.7126	2.1813	77.09	65.72
		18	0.4204			
		60	1.3311			
CTLBO [70]	3	65	0.4298	3.1411	76.372	66.04
		11	0.5603			
		18	0.4274			
IWO [75]	3	61	2.1534	1.9981	76.12	66.15
		27	0.2381			
		65	0.4334			
BFOA [76]	3	61	1.3266	2.0881	75.21	66.56
		27	0.2954			
		65	0.4476			
MFO [77]	3	61	1.3451	2.9625	72.37	67.82
		61	2.0000			
		18	0.3803			
HHO [Proposed]	3	11	0.5822	2.3049	71.8	68.07
		17	0.5329			
		61	0.9500			
		62	0.8220			

The size and location suggested by HHO (refer to Table 9) provides maximum reduction in losses as compared to GA [69], PSO [69], TLBO [68], GA/PSO [69], QOTLBO [68], CTLBO ϵ -method [70], I-DBEA [72], SA [74], CTLBO [70], IWO [75], BFOA [76], and MFO [77]. In addition, the voltage graph of all the buses obtained after utilization of PV DGs is showcased in Figure 11. The bus voltages are obtained from the load flow analysis. The bus voltage profile improves significantly under the application of three PV DGs at their respective optimal locations. The variation of fitness function against the number of iterations for installation with three PV DGs using HHO is showcased in Figure 12. The iterative graph shows that the HHO converges to an optimal solution value with very few iterations.

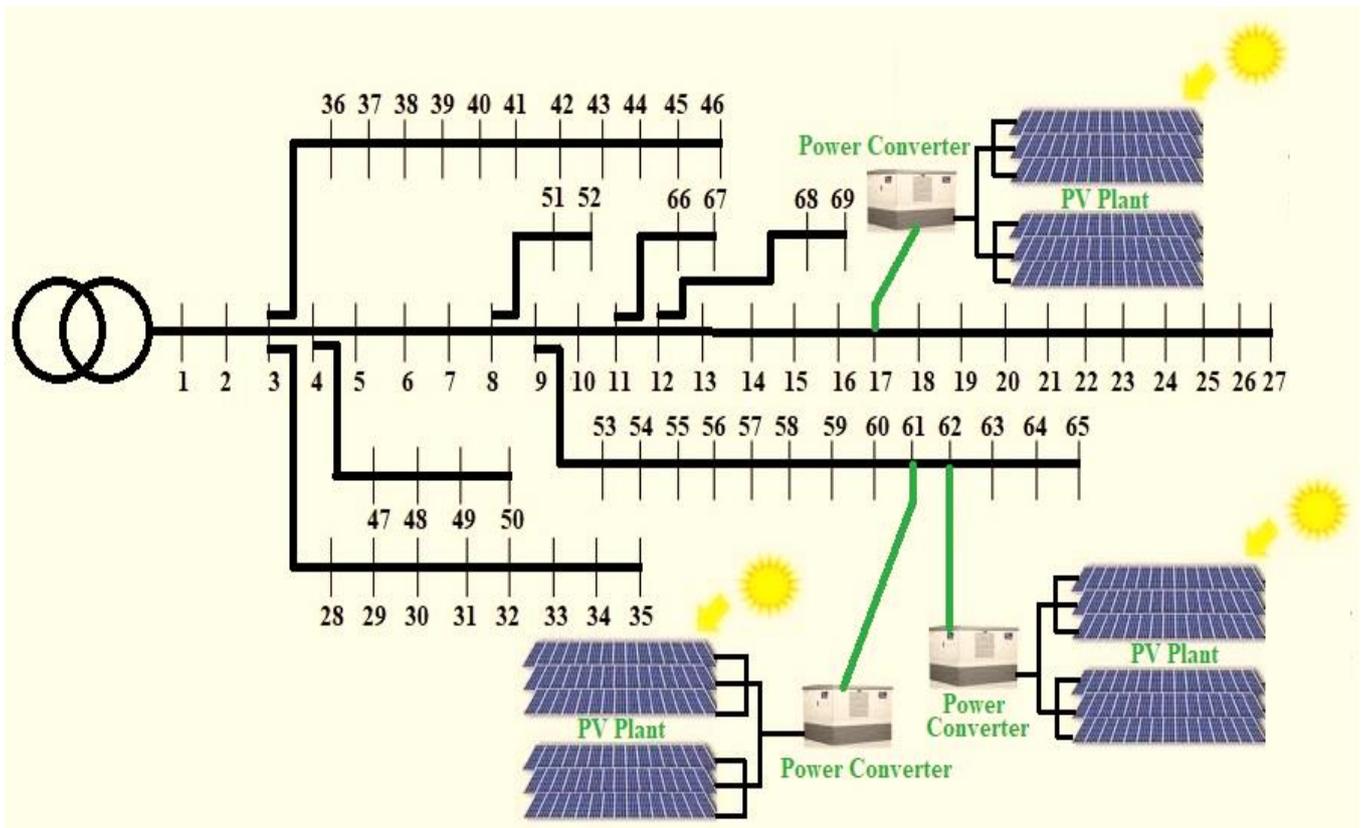


Figure 10. IEEE 69 bus line diagram with PV plants at locations suggested by HHO.

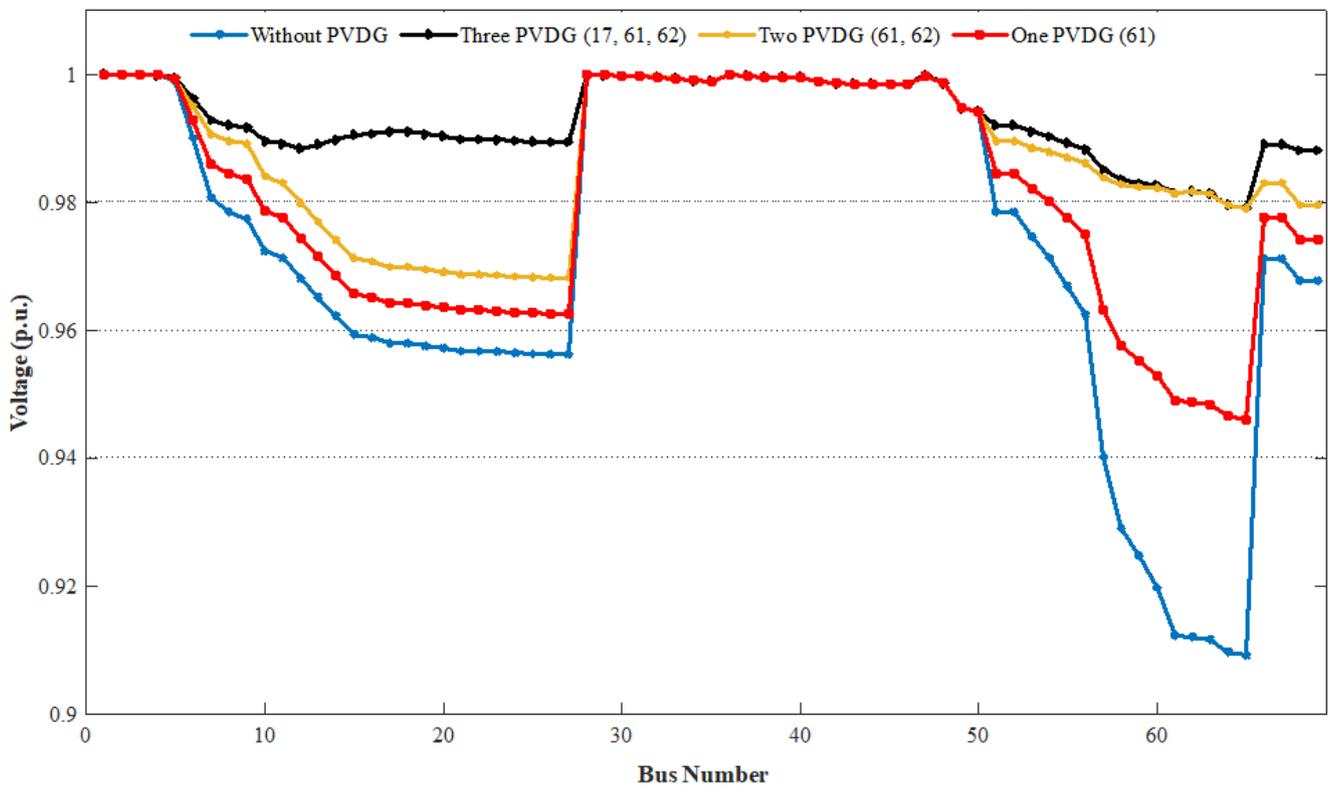


Figure 11. Voltage graph for IEEE 69 bus system without and with PV DGs.

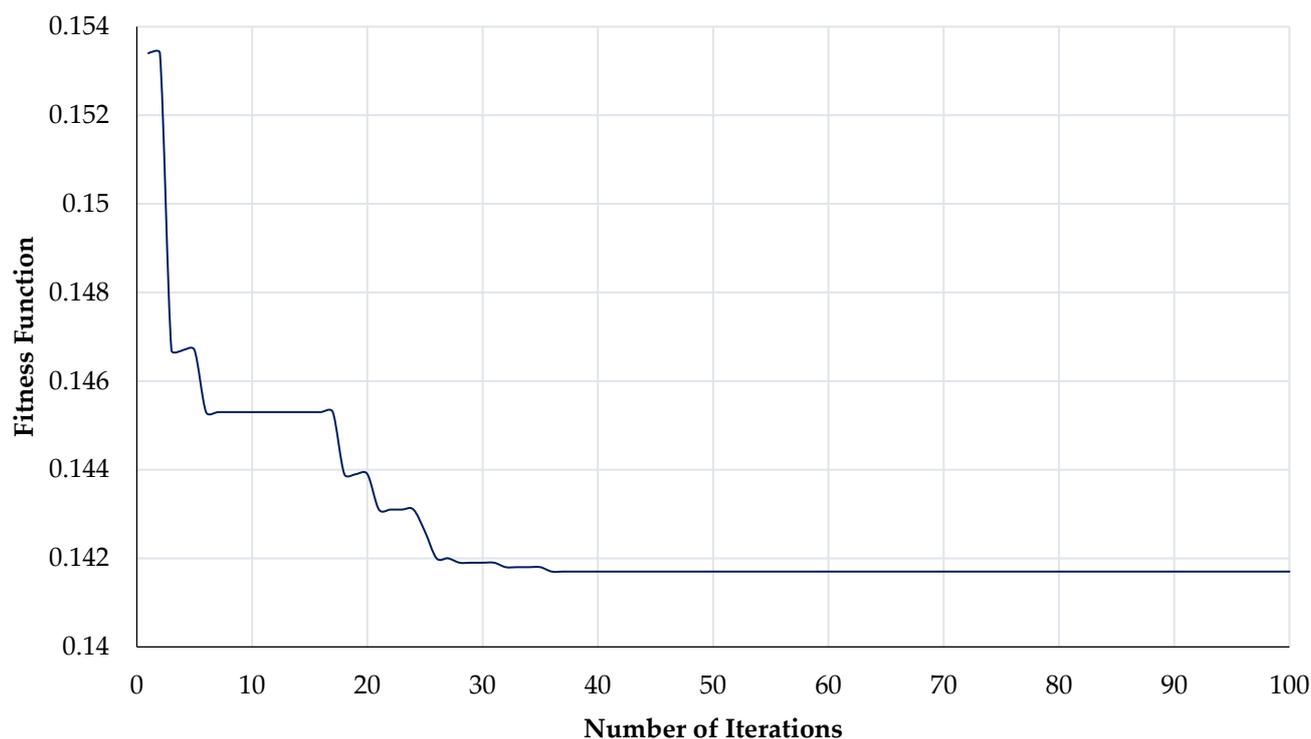


Figure 12. Convergence characteristics of fitness function pertaining to case 3 (with three PV DGs).

5. Practical PV DG Size Analysis

The optimum allocation of PV DGs using HHO indicates (refer to Table 7) that PV DGs need to be installed at bus number 13, 24, and 30 in case 2 and at bus number 17, 61 and 62 in case 3 (refer to Table 9) for optimum results. The analysis based on calculation from Section 2.2 suggests that in case 2, power to be injected at bus number 13, 24, and 30 are 831, 950, and 950 kW, respectively. In case 3, power to be injected at bus number 17, 61, and 62 are 532.9, 950, and 822 kW, respectively. Practically, to inject the targeted power as calculated through HHO, DC overload needs to be considered as described in Section 2.2. The actual field size of the PV DG plant and the number of PV modules required for case 2 and case 3 are tabulated in Table 10.

Table 10. Size of practical PV DG corresponding to case 2 and case 3 (with three PV DGs).

Case No.	Bus No.	Targeted Power to Be Injected (kW)	Actual Size of PV DG (kW)	DC Overload (kW)	Number of PV Modules
Case 2	13	831.0	1655.00	824.00	4728
	24	950.0	1891.00	941.00	5404
	30	950.0	1891.00	941.00	5404
Case 3	17	532.9	1061.08	528.18	3032
	61	950.0	1891.59	941.59	5405
	62	822.0	1636.73	814.73	4676

In case 2, the number of PV modules used in bus number 13 is 4728 to form a PV array of capacity 1.655 MW_P. The PV array of capacity 1.891 MW_P is proposed to be installed at bus number 24 and 30 using 5404 numbers of PV modules at each bus. In case 3, the practical size of the PV plant to be installed at bus number 17, 61, and 62 are of size 1.061, 1.892, and 1.637 MW_P, respectively. The analysis shows that in practical conditions, approximately 50% DC overload exists on PV DGs installation. The allocation of PV DGs in-network without considering the practical size of the PV DG may lead to underperformance.

6. Conclusions

The proposed HHO-based approach is significantly effective in finding the optimum number, optimal locations, and optimal sizes of DGs. On conventional IEEE 33 and IEEE 69 bus test systems, the efficacy of the suggested technique is evaluated. With the employment of optimally sized DGs at their optimum location, voltage profiles of load buses are improved and the losses reduced noticeably. When more PV DGs are installed, the system's performance improves. The comparison with the TLBO, GA, PSO, QOTLBO, CTLBO, CTLBO ϵ -method, IMOEHO, I-DBEA, SA, IWO, BFOA, MFO, and BA methods shows that the proposed method performs comparatively better among all. The active power loss is reduced by 64.42% and 68.07% using this approach with the installation of three PV DGs in IEEE 33 and IEEE 69 bus RDS, respectively. The collected findings demonstrate that the proposed technique reduces power loss by a greater proportion with a smaller DG size when compared to other algorithms, and it offers better convergence properties. According to the analysis, there is roughly a 50% DC overload on PV DGs installations under real-world situations. The in-network allocation of PV DGs without consideration of the PV DG's realistic size may result in underperformance.

The HHO is established as a reliable optimization technique for tackling the congestion problem of power systems with the application of DGs. The proposed method provides an alternative way for both system operators and energy producers to tackle complex problems such as voltage instability, transmission congestion, and huge system losses in an impressive way. In addition, current work suggests the practical size of PV DGs that may be employed for producing effective outcomes.

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