

Article

Multi-Disciplinary Optimization Design of Axial-Flow Pump Impellers Based on the Approximation Model

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Abstract: This study adopts a multi-disciplinary optimization design method based on an approximation model to improve the comprehensive performance of axial-flow pump impellers and fully consider the interaction and mutual influences of the hydraulic and structural designs. The lightweight research on axial-flow pump impellers takes the blade mass and efficiency of the design condition as the objective functions and the head, efficiency, maximum stress value, and maximum deformation value under small flow condition as constraints. In the optimization process, the head of the design condition remains unchanged or varies in a small range. Results show that the mass of a single blade was reduced from 0.947 to 0.848 kg, reaching a decrease of 10.47%, and the efficiency of the design condition increased from 93.91% to 94.49%, with an increase rate of 0.61%. Accordingly, the optimization effect was evident. In addition, the error between the approximate model results and calculation results of each response was within 0.5%, except for the maximum stress value. This outcome shows that the accuracy of the approximate model was high, and the analysis result is reliable. The results provide guidance for the optimal design of axial-flow pump impellers.

Keywords: axial-flow pump; impeller; approximation model; optimization design; multi-disciplinary

1. Introduction

A multi-disciplinary optimization (MDO) design, which is among the latest and most active fields in the current research on complex system optimization design, is mainly used in specializations such as aerospace and torpedo missile design. The research on MDO in fluid machinery is mainly focused on the optimization design of turbine and wind turbine blades. However, pumps are classified as general machinery with varied applications [1–5]. The axial-flow pump impeller is the core and most important flow component of a pump device. The result of the design directly determines the comprehensive effects of the pump device and the entire pumping station. In recent years, approximately half of the axial-flow pump impellers produced annually have been used to replace scrapped products caused by blade problems [6]. To improve the comprehensive performance of axial-flow pump impellers, a multi-disciplinary optimization design of an axial-flow pump impeller should be implemented.

MDO is mainly used in some large-scale systems engineering. Sun et al. [7] used the MDO platform to focus on integral solid propellant ramjet supersonic cruise vehicles and constructed two MDO frameworks through discipline codes. Thus, the optimization of the detailed parameters and high fidelity were achieved. Chen X et al. [8] adopted MDO by introducing the multi-disciplinary feasible architecture and gradient-based optimization algorithm, which further improved the efficiency of gradient calculation. The optimized design was more energy-saving than the initial design. Xu HW et al. [9] dealt with time-varying uncertainty by proposing a multi-disciplinary robust

design optimization method based on time-varying sensitivity analysis through a multi-disciplinary optimization design. MDO provides a good solution in the fields of launch vehicle design optimization, hard rock tunnel boring machine performance design optimization, and all-electric GEO satellite design optimization [10–14]. The MOD technology has incomparable advantages in solving the optimization design problem of large-scale complex systems engineering.

The optimal design of a pump is based on the design theory and method of pumps, which uses optimal design theory to achieve superior comprehensive performance [15]. At present, optimization methods for pumps mainly include those based on simplified model prediction and accurate model analysis. To improve the efficiency of a centrifugal pump, Wang WJ et al. [16] and Pei J et al. [17] optimized the impeller and guide vane, thereby obtaining a highly efficient hydraulic model. Miao F et al. [18] proposed a multi-objective optimization of the impeller shape of an axial-flow pump based on the modified particle swarm optimization (MPSO) algorithm. This novel algorithm was successfully applied for the optimization of axial-flow pump impeller shape designs by comparing the results of the MPSO and Computational Fluid Dynamics (CFD) simulation results. Yun JE [19] studied the impact loss at the inlet of rotor blades and obtained the optimal design of a blade shape by numerical analysis and optimization. Some studies [20,21] have adopted optimization design methods to achieve improved cavitation and good hydraulic performance of axial-flow pumps. Numerous studies have shown that the numerical simulation method has become the most important research method in the field of pumps. However, the majority of these studies have used a single subject optimization method to obtain the design result of pumps, in which the hydraulic performance and structural strength were optimized separately.

Only a few studies have been conducted on the fluid–structure coupling of pumps. These studies used the fluid–structure coupling analysis method based on the MDO platform to optimize the blades of pumps [22,23]. Tong YF et al. [24] implemented a multi-disciplinary energy-saving optimization design of bridge cranes and adopted the finite element analysis and multi-disciplinary optimization technology to reduce the total quality and energy-saving design of cranes. However, these studies have yet to achieve the degree of coordinated design optimization of hydraulic performance and structural strength.

The current study draws on the relevant research methods in the aforementioned fields to adopt an MDO design method for large axial-flow pump blades. At present, the rapid development of computational fluid and structural mechanics has resulted in numerous and successful research in the field of hydraulic performance and structural performance of axial-flow pump impellers. However, the traditional single-discipline optimization analysis method disregards the interaction and mutually affects between the hydraulic and structural designs. The method also fails to achieve a real coordinated design, which does not consider the reliability and accuracy of the optimized design results. To further improve the overall performance of pumps in axial-flow pump impeller optimization designs, the theory and method of multi-disciplinary design optimization of axial-flow pumps were applied in this research. This study focuses on the two disciplines of hydraulics and structure. Therefore, the MDO problem in this research can be presented as follows: considering the blade quality and efficiency of the design condition as objective functions; using the head of small flow (i.e., flow under the highest operating head), efficiency of small flow, maximum stress value, and maximum deformation value of small flow as constraints; and ensuring that the blade head of the design conditions remains unchanged or varies in a small range.

2. Numerical Calculation

2.1. Governing Equations

The solution of the fluid–structure interaction problem should consider the flow and structure fields and the data transfer between them. To considerably study this interaction, the current research used the calculation method of unidirectional fluid–solid coupling based on the system coupling module of the Ansys Workbench platform. First, the calculation of the fluid domain is performed. Second, information on the fluid domain is transmitted to the structural field by the fluid–solid coupling interface. Lastly, finite element structure analysis is performed.

In the flow field calculation, three-dimensional (3D) Reynolds-averaged N–S equations are used to solve the turbulent flow in the impeller of the axial-flow pump. By solving the equation, the fluid information of the discretized time and space flow field is obtained. The performance shows that the parameters can obtain the flow field flow characteristics. The basic control equations are as follows:

$$\frac{\partial v_j}{\partial x_j} = 0 \quad (1)$$

$$\frac{\partial(\rho v_i)}{\partial t} + \frac{\partial(\rho v_i v_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \mu \frac{\partial v_i}{\partial x_i \partial x_j} \quad (2)$$

where v is the inflow velocity, p is the flow field pressure, ρ is the fluid density, μ is the fluid dynamic viscosity, and the subscripts i and j are the x- and y-coordinates, respectively.

The numerical simulation adopted the renormalization group(RNG) k - ε turbulence model. When water flows through the blade passage of the axial-flow pump impeller, it will produce a higher strain rate and larger bending streamline. The RNG k - ε model adopts a statistical technique called renormalization grouping to correct the turbulence viscosity by considering the condition of rotation and swirl. The RNG k - ε turbulence model has better analysis ability than other turbulence models in the internal flow field calculation process of axial-flow pumps. The governing equations are as follows:

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j}(\alpha_k \mu_{eff} \frac{\partial k}{\partial x_j}) + G_k - \rho \varepsilon \quad (3)$$

$$\frac{\partial}{\partial t}(\rho \varepsilon) + \frac{\partial}{\partial x_i}(\rho \varepsilon u_i) = \frac{\partial}{\partial x_j}(\alpha_\varepsilon \mu_{eff} \frac{\partial \varepsilon}{\partial x_j}) + \frac{C_{1\varepsilon} \varepsilon}{k} G_k - C_{2\varepsilon} \rho \frac{\varepsilon^2}{k} \quad (4)$$

where G_k represents the generation of turbulence kinetic energy caused by the mean velocity gradients. The quantities α_k and α_ε are the inverse effective Prandtl numbers for k and ε . $C_{1\varepsilon} = 1.42$, $C_{2\varepsilon} = 1.68$. μ_{eff} is the effective viscosity accounting for turbulence. k is turbulence energy. ε is dissipation rate of turbulent kinetic energy.

The structural calculation used the finite element method to analyze the structural field of the axial-flow pump blade. The dynamic equation of the axial-flow pump blade under hydrodynamic action is defined as follows:

$$[M](\ddot{x}) + [C](\dot{x}) + [K](x) = \{F\} \quad (5)$$

where $[M]$ is the structural mass matrix, $[C]$ is the structural damping matrix, $[K]$ is the structural stiffness matrix, (x) is the structural displacement, (\dot{x}) is the structural velocity, (\ddot{x}) is the structural acceleration, and $\{F\}$ represents the flow field force of the structure under a fluid–solid coupling.

When the static calculation of axial-flow pumps blade is performed through fluid–solid coupling, the fluid and solid systems are included in such a calculation. On the coupling surface, the velocity and stress continuous equations should be satisfied. The water pressure on the blade surface under a certain

operating condition of pumps can be approximated and is constant with time. That is, the time-related quantity is disregarded. Thus, the relationship can be simplified as follows:

$$[K](x) = \{F\} \quad (6)$$

where $K = \sum_V \iiint B^T C B dV$ and $[B]$ is the strain matrix.

The stress requirement for the MDO design of axial-flow pumps is the most important. The stress distribution of blades under the design conditions is unnecessary because the general pumping station project focuses on the highest head. The most important aspect in terms of hydraulic performance is the efficiency of the design conditions. The highest operating head conditions focus on safe operations. The practical application requirements of pump stations and the corresponding flow given under the highest operation head of these stations indicate the calculation of stress distribution by using the head as a constraint under this flow. In energy saving and emission-reduction environments, blade quality is regarded as the goal of structural optimization design. Therefore, the MDO problem in this research can be presented as follows: considering the blade quality and efficiency of the design condition as objective functions; using the head of small flow (i.e., flow under the highest operating head), efficiency of small flow, and maximum stress and maximum deformation values of small flow as constraints; and ensuring that the blade head of the design conditions remains unchanged or varies in a small range. Under these conditions, the impeller of the axial-flow pump undergoes multi-constraint, multi-objective, multi-modality, and multi-disciplinary optimization.

2.2. Parameterized Model

A blade modeling program written in MATLAB based on the Zhukovsky airfoil can generate blade curve files for Turbo-Grid and UG. In this manner, the 3D model of the fluid and 3D model of the blade structure can be established conveniently. The flow–solid coupling calculation analysis of axial-flow pumps is only for the impeller. Thus, the analysis only involves the calculation of the single channel flow field to save calculation time and improve calculation efficiency in the flow field analysis. Structural calculations consider the single blade in the corresponding coordinate quadrant. The majority of the axial-flow pumps in actual pumping stations are fully regulated vane pumps. To fit the actual situation, a 3D modeling of the model impeller round shank is performed instead of a 3D hub shape, with the inner surface of the round shank being a fixed end. The 3D model of the blade structure is shown in Figure 1.

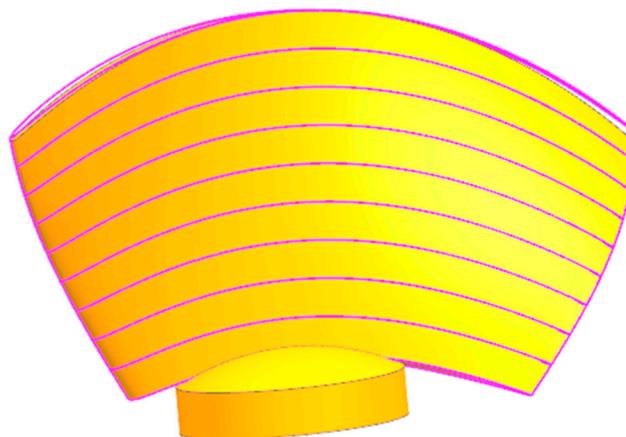


Figure 1. Three-dimensional shape of blade.

2.3. Grid and Load

The fluid domain calculation model is mainly for the impeller of axial-flow pumps. In this study, the nominal specific speed of the axial-flow impeller n_s is 750, design flow Q is 360 L/s, design head H is 7.0 m, rotating speed n is 1450 r/min, and the blade tip unilateral gap is 0.15 mm. The diameter of the impeller is 300 mm. The number of impeller blades is four. The impeller is modeled by using Turbo-Grid according to the 3D coordinate data points. The axial-flow pump impeller is the computational domain. The inlet and outlet of the computational domain are respectively set as the total pressure inlet and the flow outlet. No-slip conditions are used for all the walls.

The structural grid of the axial-flow impeller is meshed by the software of Turbo-Grid. The quality of the grid is good and can meet orthogonal requirement. The grid of the impeller is shown in Figure 2.

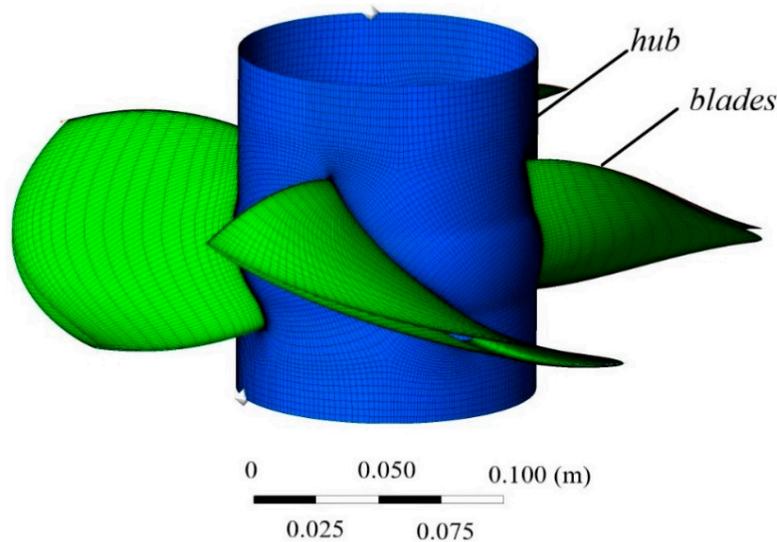


Figure 2. Fluid grid of the impeller.

In the mesh elements ranging from 8.0×10^4 to 1.6×10^5 , six sets of single channel grids of the impeller are used to do the grid independence analysis. Numerical calculation results of the head and efficiency of the impeller reveal a small difference when the grid elements are up to 1.21×10^5 (Figure 3). Therefore, 121,527 is selected as the number of single channel computational mesh elements for numerical simulation in this study.

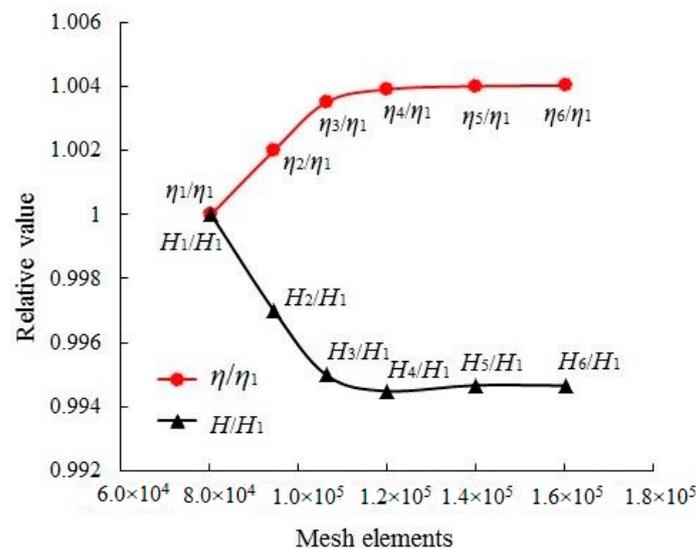


Figure 3. Mesh independence of the impeller.

Bernoulli energy equations were adopted to calculate the head of axial-flow pump. The head of the pump is shown as follows:

$$H_{net} = \frac{\int_{s_2} P_2 u_{t2} ds}{\rho Q g} + H_2 + \frac{\int_{s_2} u_2^2 u_{t2} ds}{2 Q g} - \left(\frac{\int_{s_1} P_1 u_{t1} ds}{\rho Q g} + H_1 + \frac{\int_{s_1} u_1^2 u_{t1} ds}{2 Q g} \right) \quad (7)$$

where H_1 is the inlet water level, H_2 is the outlet water level (m), s_1 is the inlet section area, s_2 is the outlet section area (m^2), u_1 is flow velocity of inlet section, u_2 is flow velocity of outlet section (m/s), u_{t1} is the normal component velocity of inlet section, u_{t2} is the normal component velocity of outlet section (m/s), P_1 is static pressure of inlet section, and P_2 is static pressure of outlet section (Pa).

The efficiency of the axial-flow pump is shown as follows:

$$\eta = \frac{\rho g Q H_{net}}{T_p \omega} \quad (8)$$

where T_p is torque of the blade (N·m), and ω is the angular velocity of the impeller (rad/s).

According to the actual situation of the blade structure, the 3D solid model is imported into the Design Modeler module of the Workbench platform to set the properties of the model material to structural steel.

The material property parameters of the axial-flow pump blade are as follows: modulus of elasticity $E = 2.0 \times 10^{11}$ Pa, Poisson's ratio $\mu = 0.3$, and density $\rho = 7850$ kg/m³. The diameter and thickness of the round shank are 60 mm and 12.5 mm, respectively. The solid grid model is divided in the mesh module of a model that uses unstructured grids. The number of grids of a single blade is around approximately 120,000. The grid model is shown in Figure 4.

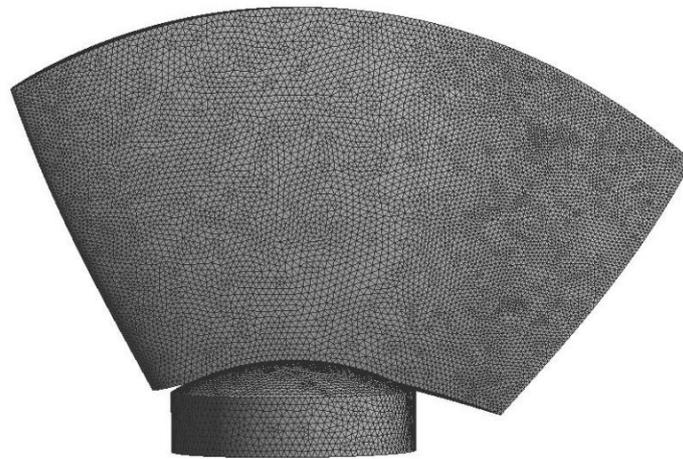


Figure 4. Solid grid model.

This study calculated the stress distribution of a pump blade under inertial and pressure loads. Inertial load is the centrifugal force received by the pump. The pump's rate of speed is $n = 1450$ r/min. The pressure load is the water pressure. In the structural analysis, the influence of bearing load and bolt load on the stress distribution is disregarded for convenience of calculation.

2.4. Model Test Verification

A field performance test of the initial scheme was carried out on an axial-flow pump model test bench in China. The impeller of the axial-flow pump was machined with copper material according to design results of the initial scheme. The rotating speed of the impeller was 1450 r/min, and the diameter of the impeller was 300 mm. The number of the blades was four. The impeller of the axial-flow pump is shown in Figure 5a. According to the hydraulic industry standard of the pump model test of China, the model test of the axial-flow pump section includes impeller, guide vane, inlet pipe and outlet pipe, etc. The guide vane adopts the matching design guide vane. The pump installation is shown in Figure 5b. The comparison of numerical simulation and model test is shown in Figure 6. The predicted performance curve of numerical simulation is consistent with the experimental curve. The curves have a good agreement, and the error of each point is less than 3%. The results show that the numerical simulation of the axial-flow pump is accurate and reliable.

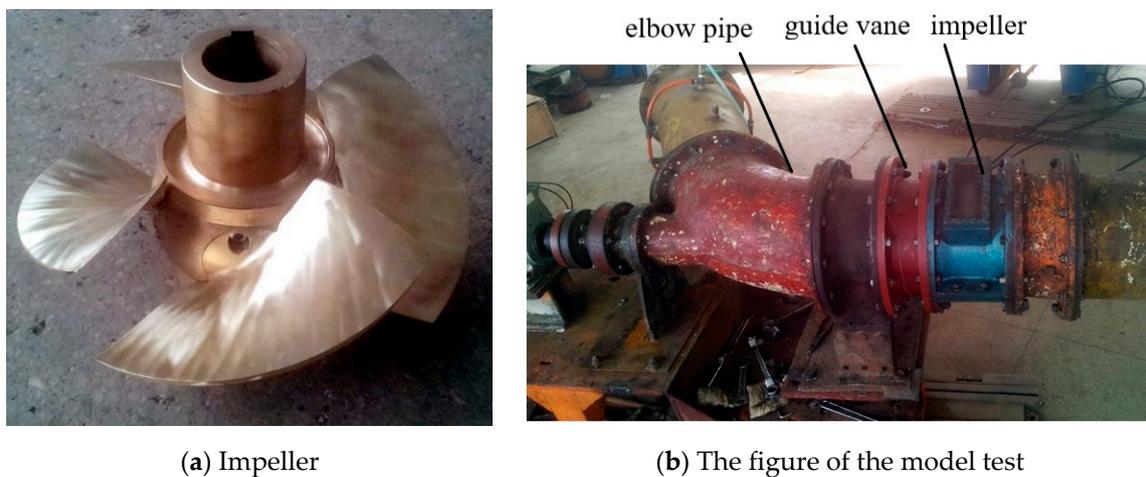


Figure 5. Model test physical map.

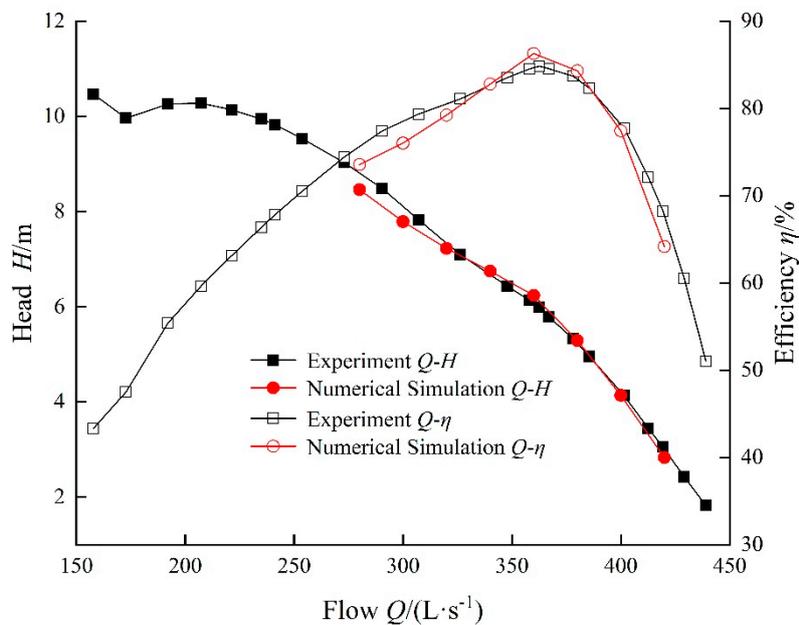


Figure 6. Comparison of numerical simulation and model test.

3. Analysis of Design of Experiment

The optimal Latin hypercube method was selected for the calculation of the sample points in the flow–solid coupling calculation of the axial-flow pump. This method allows many more points and more combinations to be studied for each factor. Experiment points are spread evenly, allowing higher order effects to be captured. The engineer has total freedom in selecting the number of designs to run as long as it is greater than the number of factors. The optimal Latin hypercube method is based on the random Latin hypercube method to improve the uniformity. The level selection of the factors is regulated by the corresponding algorithm, so that the selected sample points have better space filling and more uniform distribution in the whole design space.

The design variables included four design parameters: cascade density, airfoil placement angle, airfoil arch ratio, and airfoil thickness ratio. Airfoil selects the Zhukovsky airfoil structure used in the flushing angle research. All parametric modeling works were implemented in MATLAB. The 3D coordinate data of the blade section were generated using MATLAB, while the 3D solid models were built in Turbo-Grid and UG. To save calculation time and improve efficiency, the 3D shape of the entire blade was controlled using the minimum design variables. By using the equal strength design method, the cascade density of 10 sections can be controlled by two design variables: cascade density multiple of the blade tip and cascade density multiple of the blade root. The third-order B-spline curve control can reduce the airfoil angle data of 10 sections to only three variables: airfoil angle of the hub, rim, and middle section. The maximum camber and maximum thickness of the 10 sections are linear from hub to rim. Therefore, each parameter is only controlled by two variables of the hub and the rim, which successfully reduces 40 design variables to nine design variables. The initial value and range of the nine design variables are as follows:

$$\text{Design variables} \left\{ \begin{array}{l} x_1 = 0.8 \in [0.7, 0.9] \\ x_2 = 1.2 \in [1.15, 1.45] \\ x_3 = 15.6 \in [13.6, 17.6] \\ x_4 = 32 \in [30, 34] \\ x_5 = 48 \in [46, 50] \\ x_6 = 4.2 \in [3.5, 4.9] \\ x_7 = 6.2 \in [5.5, 6.9] \\ x_8 = 6 \in [5, 7] \\ x_9 = 12 \in [10, 14] \end{array} \right. \quad (9)$$

where x_1 is the cascade density of the blade tips, x_2 is the cascade density multiple of the blade root, x_3 is the airfoil angle of the hub ($^\circ$), x_4 is the airfoil angle of the rim ($^\circ$), x_5 is the airfoil angle of the middle section ($^\circ$), x_6 is the maximum camber of the hub (mm), x_7 is the maximum camber of the rim (mm), x_8 is the maximum thickness of the hub (mm), and x_9 is the maximum thickness of the rim (mm).

Within the range of the design variables, 80 sample points were generated using an optimized Latin hypercube method. A complete fluid–solid coupling calculation is required for each set of sample points. Each fluid–solid coupling calculation requires a complete set of processes including 3D modeling of fluid and structure, mesh division, and flow field and finite element calculation. Each flow–solid coupling calculation process is shown in Figure 7.

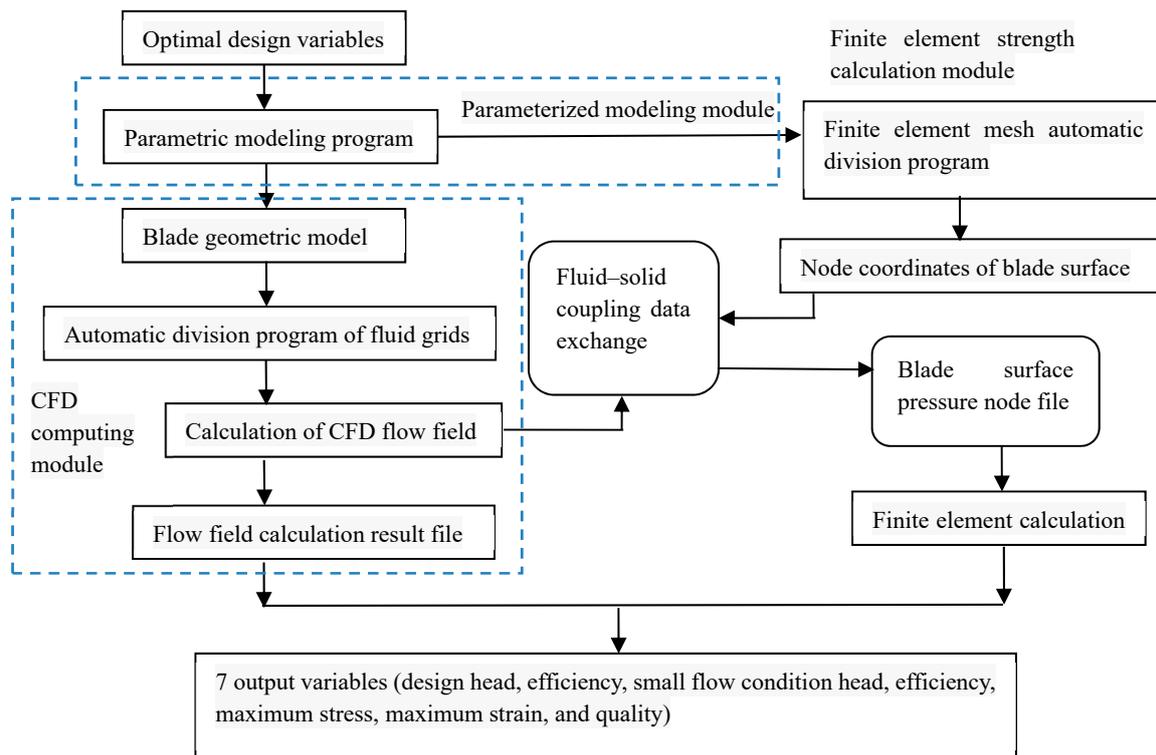


Figure 7. Flow chart of the fluid–solid coupling calculation.

According to the optimization requirements, the structural parameters, including mass, maximum stress, and maximum strain, should be calculated. Hydraulic parameters include the head and the efficiency under design conditions and small flow conditions. The design and small flow conditions are 360 L/s and 240 L/s, respectively. Table 1 shows the calculation results of the 80 sample points.

Table 1. Calculation results of the sample points. y_1 is the head of the small flow condition (m), y_2 is the efficiency of small flow condition (%), y_3 is the maximum deformation value of small flow condition (m), y_4 is the maximum stress value of small flow condition (Pa), y_5 is the mass of blade (kg), y_6 is the head of design condition (m), y_7 is the efficiency of design condition (%).

Serial Number	y_1	y_2	y_3	y_4	y_5	y_6	y_7
Initial value	11.44	90.2147	0.00017979	103,620,000	0.94769	6.95309	93.9141
1	11.7532	90.1304	0.00018335	107,910,000	0.93693	6.71377	93.6598
2	10.9753	91.8065	0.00017092	89,098,000	0.90572	5.96531	93.3522
3	11.6557	91.557	0.00016117	71,270,000	0.99557	6.50123	93.5828
4	12.8308	89.2097	0.00017691	92,624,000	0.9928	7.85457	94.291
5	11.9646	90.8667	0.00015263	92,273,000	0.95464	7.40514	94.233
6	12.4638	90.1697	0.00015064	76,457,000	1.0196	7.57474	94.0972
7	10.7539	90.9872	0.00016243	79,116,000	0.86208	6.48433	93.861
8	11.4467	89.449	0.00016261	71,086,000	0.86371	7.30957	94.0902
9	10.9185	90.9655	0.00012786	65,613,000	0.89861	6.58435	93.679
10	10.5674	91.0425	0.00013858	72,479,000	0.87519	6.00038	93.4396
...
71	11.6549	88.9273	0.00025333	111,840,000	0.81188	7.55323	94.1173
72	11.3588	90.6635	0.00014668	81,217,000	0.85662	7.2884	94.2028
73	11.6204	91.7638	0.00012582	66,575,000	0.95936	6.81371	94.0114
74	12.3619	89.0101	0.00017739	89,281,000	0.90464	7.85347	94.1984
75	11.1076	91.171	0.0002191	109,260,000	0.87431	6.60246	93.8747
76	12.0918	89.3128	0.00014278	76,217,000	0.951	7.51066	94.0422
77	11.1648	90.4989	0.00020433	107,720,000	0.86179	6.84219	93.794
78	11.0768	90.8673	0.00013344	74,040,000	0.94497	6.37273	93.4434
79	11.707	90.0439	0.00021392	120,720,000	0.92188	6.89957	93.7827
80	11.3428	89.1842	0.00019157	90,251,000	0.82919	7.34594	94.1117

The calculation results of hydraulic performance and structural performance of the axial-flow pump were obtained according to 80 different blade design schemes. In the calculation results of 80 groups of samples, the minimum value of the head was 10.38 m and the maximum value was 12.83 m under the small flow condition (Figure 8a). The lowest value of the pump efficiency was 87.41%, and the highest value was 92.36% under the small flow condition (Figure 8b). Under the small flow condition, the maximum deformation of the pump blade was in the range of 0.126~0.287 mm (Figure 8c). Under the small flow condition, the maximum stress of the pump blade was in the range of 65.6~152.9 MPa (Figure 8d). When the axial-flow pump was operated under small flow conditions, the pump head was relatively high, and the blades in this operating area were most vulnerable to structural damage. Therefore, it is necessary to consider structural deformation and structural stress under small flow condition when doing structural optimization design. The minimum mass value of the single axial-flow pump blade under different design schemes was 0.79 kg, and the maximum value was 1.04 kg (Figure 8e). Under the design condition, the minimum value of the head was 5.60 m, and the maximum value was 8.19 m (Figure 8f). Under design condition, the minimum value of the pump efficiency was 92.97%, and the highest value was 94.43% (Figure 8g). The head and efficiency of the axial-flow pump under design condition are very important evaluation parameters for the design of the axial-flow pump. In order to ensure that the specific speed of the pump is constant, the head under the design condition should be kept basically unchanged, and at the same time, the efficiency is expected to be higher. The difference between the calculation results of the different sample points is relatively large, particularly the structural performance (Figure 8). The maximum calculation results of the maximum stress and deformation value were more than twice the minimum value. This result shows that the change of the design parameters has immense influence on the structural performance of pump.

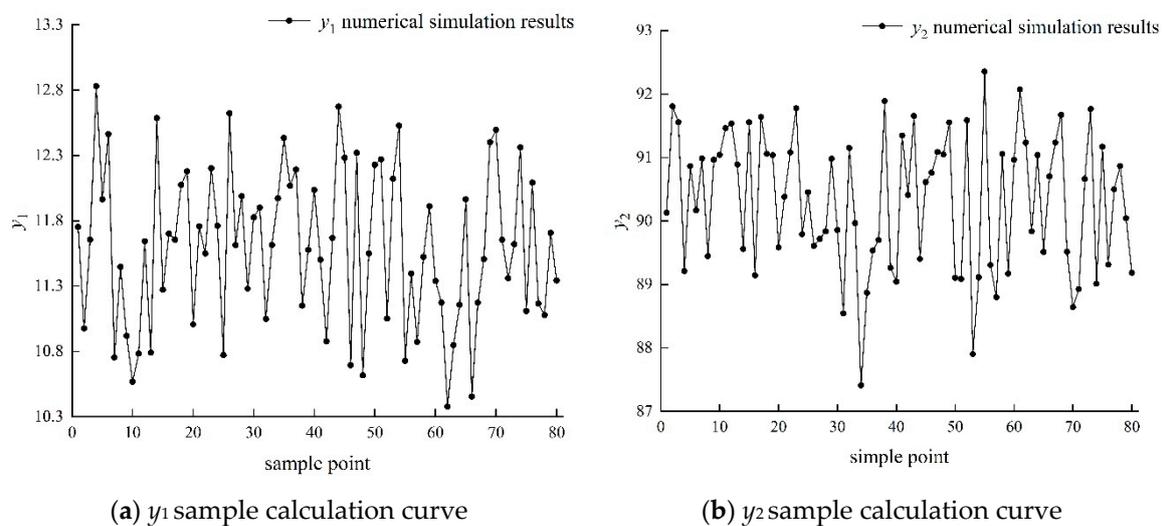
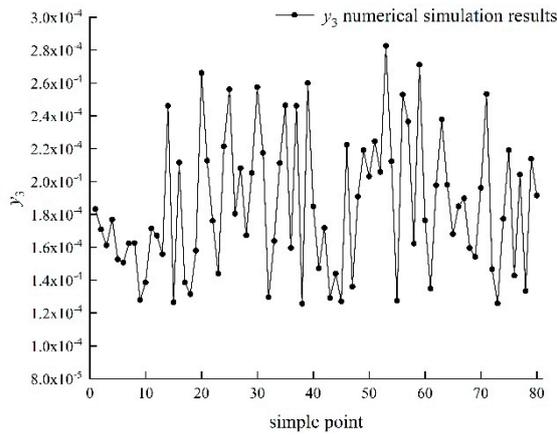
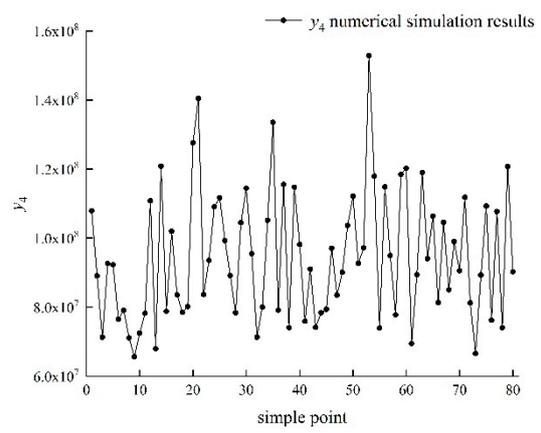


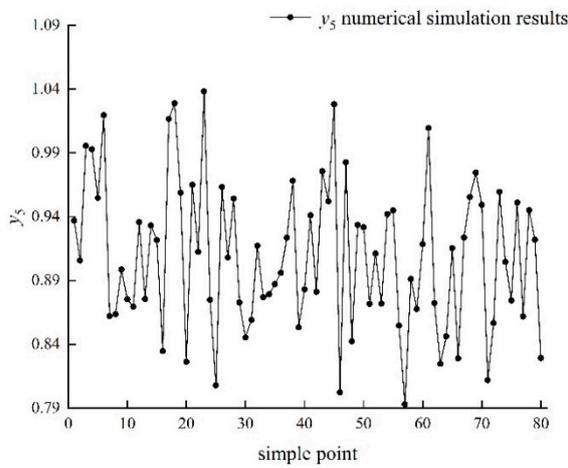
Figure 8. Cont.



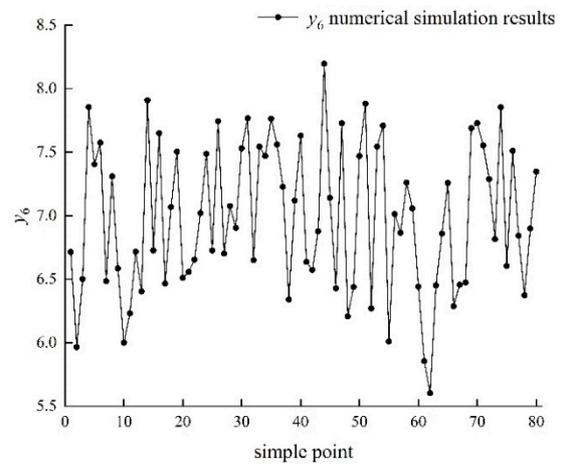
(c) y_3 sample calculation curve



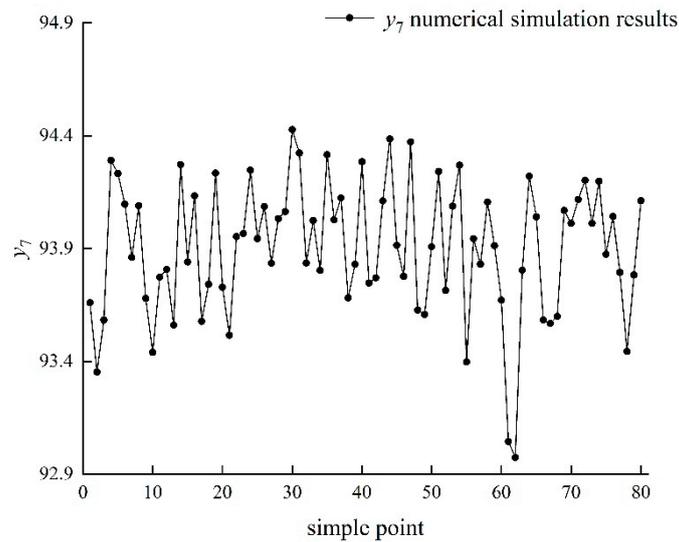
(d) y_4 sample calculation curve



(e) y_5 sample calculation curve



(f) y_6 sample calculation curve



(g) y_7 sample calculation curve

Figure 8. Calculation results of the sample points.

The three typical conditions of stress and strain distribution are shown in Figures 9 and 10.

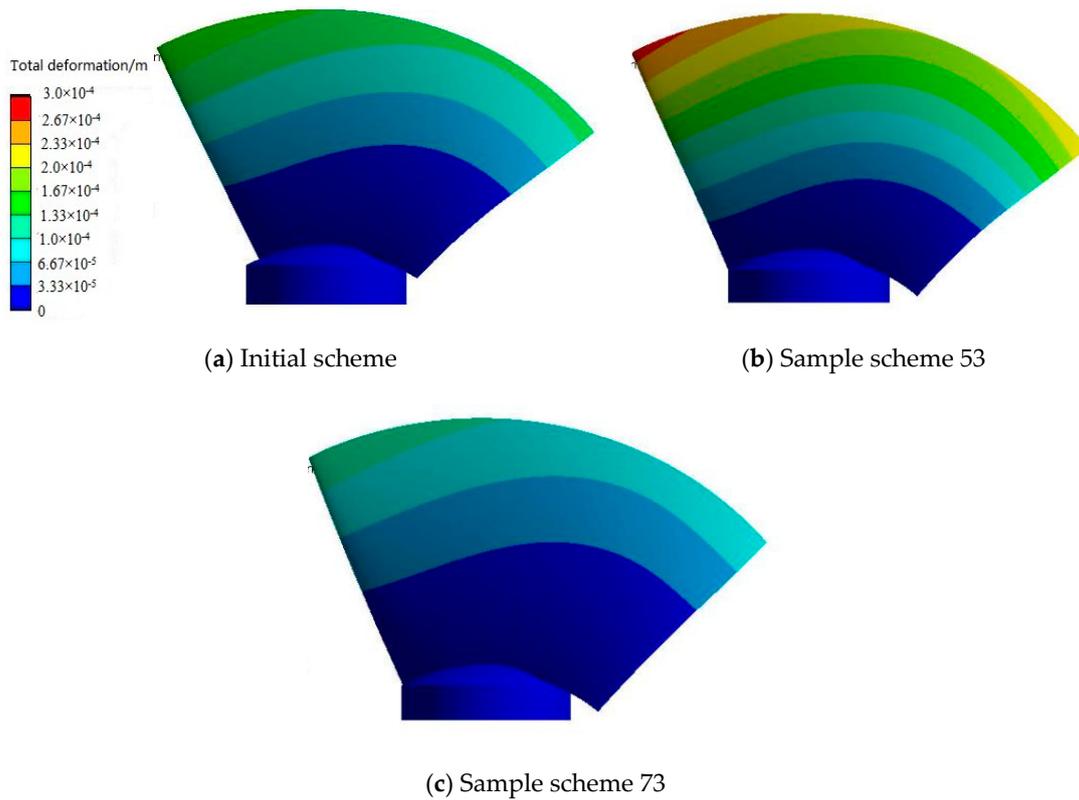


Figure 9. The deformation distribution ($Q = 240 \text{ L/s}$).

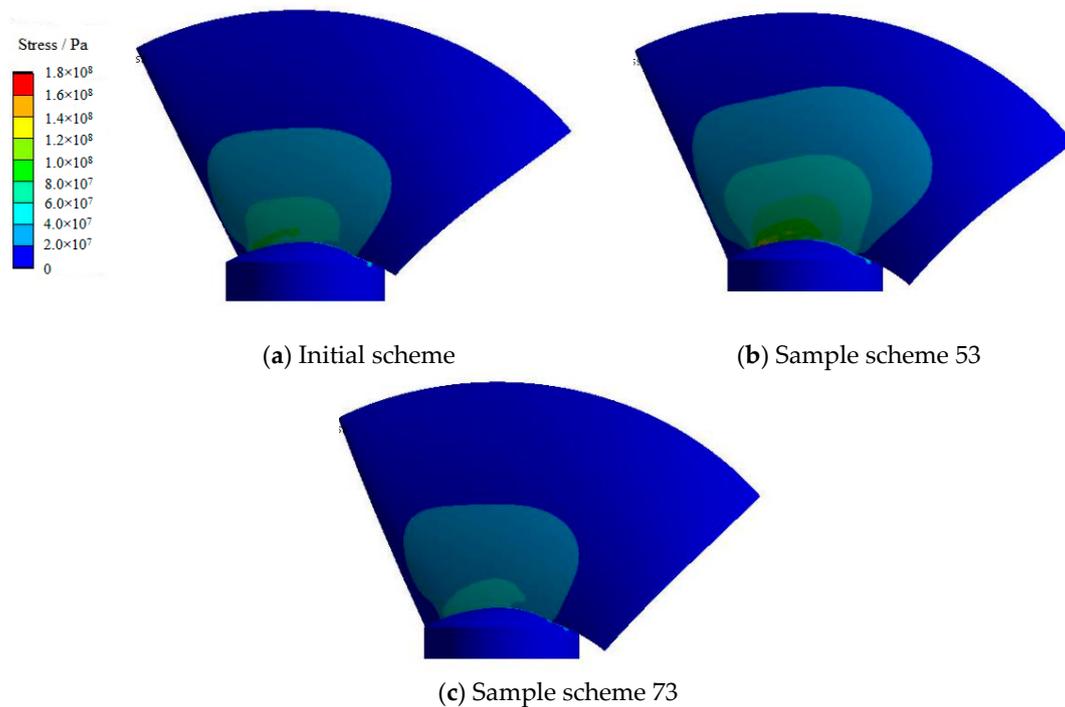


Figure 10. Stress distribution ($Q = 240 \text{ L/s}$).

The structural performance calculation results of sample points 73 and 53 were taken out to analyze their structural characteristics because the structural performance of sample points 73 and 53 were the maximum and minimum values respectively in the whole sample. Evidently, the maximum deformation position of the blade of the axial-flow pump was near the edge of the blade inlet section. The maximum stress position was near the hub of the blade. The maximum stress and maximum

deformation position and distribution trend corresponding to the different design parameters were consistent. However, the maximum deformation and maximum stress values differed substantially. The solid line in the graph indicates the position of the blade when it was not subjected to external stress. The cloud image shows the position after deformation. The deformation direction of the blade was the same. The deformation was found toward the inlet direction of the impeller; the closer the rim, the more substantial the deformation was.

4. Approximation Models

Approximation models are methods of approximating a set of input variables (i.e., independent variables) and output variables (i.e., response variables) through a mathematical model. The approximate model uses the following equation to describe the relationship between the input variable and output response:

$$y(x) = \tilde{y}(x) + \varepsilon, \quad (10)$$

where $y(x)$ is the response to the actual value, which is an unknown function; $\tilde{y}(x)$ is a response to the approximation, which is a known polynomial; and ε is the random error between the approximation and actual value, which typically follows the standard normal distribution of $(0, \sigma^2)$.

An approximate model structure was constructed and aimed at the 80 sample points of the axial-flow pump multi-disciplinary optimization design. R^2 is a regression coefficient that characterizes the correlation between the predicted and actual values. When R^2 is equal to 1, the predicted value of each sample point is the best fit with the actual value; the closer the R^2 coefficient of the approximate model to 1, the closer the approximate model to the real solution. The R^2 coefficients of the different approximation models are listed as follows.

R-squared can be used to analyze the degree of consistency between the approximate model and the sample points. An R-squared value of 1.00 indicates that the approximate model has high reliability. The credibility is low when the value of R-squared is less than the set acceptance level of 0.8. The approximate models were established by means of RSM method, neural network method, and Kriging method. The R-squared value of Table 2 displayed in red is closest to 1. It shows that the approximate model displayed in red is the most ideal scheme, and it has high reliability. Table 2 shows that the Kriging model cannot fit the approximate model data of the two responses—the largest deformation and maximum stress values and the effect is not good when fitting other responses. Hence, the Kriging model was not used in this study. When using neural network models to construct approximate models, the radial and elliptical basis models have minimal effect on the fitting results. These models only have a good fitting effect on part of the responses. The response surface model has a superior fitting effect. Table 2 shows that the more complex the response of the maximum stress value, the higher the order and the better the fitting effect, which was not the case in the other responses, particularly in the quality response. The fitting quality of the fourth-order response surface model decreases substantially. This study used the second-order response surface method to construct an approximate model of the small flow rate efficiency and quality, in accordance with the comparative results of the fitting effect. The third-order response surface method was used to construct an approximate model of the small flow head and the design condition head. The fourth-order response surface method was used to construct an approximate model of the small flow maximum deformation, maximum stress, and design efficiency.

Table 2. Analysis of the R^2 correlation coefficient of different approximate models.

Evaluation Index	Response	RSM				Neural Network		Kriging
		First Order	Second Order	Third Order	Fourth Order	RBF	EBF	
R^2	y_1	0.94685	0.99669	0.99693	0.98667	0.99343	0.99282	0.96766
	y_2	0.88756	0.98814	0.98739	0.98634	0.97069	0.9654	0.95398
	y_3	0.96856	0.99898	0.99293	0.99949	0.98135	0.99294	0
	y_4	0.70425	0.8275	0.87918	0.88162	0.67383	0.68307	0
	y_5	0.99692	0.99991	0.99869	0.8498	0.9984	0.99933	0.95499
	y_6	0.96582	0.99926	0.99929	0.9915	0.99727	0.99651	0.95914
	y_7	0.8369	0.99039	0.99135	0.99155	0.9524	0.96781	0.90637

5. Optimal Design

5.1. The Optimization Model

The multi-disciplinary optimization design of the axial-flow pump blades adopted a discipline analysis method to construct an approximate model, reduce calculation time, and save on calculation cost. Optimization aimed to make the axial-flow pump blades meet the operational requirements of the highest head of the pump station under the small flow condition. Within the constraints of a few changes in the head of the design conditions, and satisfying the condition that the maximum blade stress was lower than the yield strength of the material, the highest efficiency and lightest quality or design conditions of the highest efficiency and minimum deformation optimization goals under axial-flow pump blade design conditions were achieved.

The optimization model is as follows:

Objective function:

$$\text{Max}y_7 \text{ and } \text{min}y_5 \quad (11)$$

$$\text{Constraints : } \begin{cases} y_1 \geq 11.5 \\ y_2 \geq 90 \\ y_3 \leq 3.0 \times 10^{-4} \\ y_4 \leq 1.1 \times 10^8 \\ 6.8 \leq y_6 \leq 7.2 \end{cases} \quad (12)$$

The relevant literature has indicated that the yield strength of steel is $\sigma > 207$ MPa, and the maximum stress of the blade in the sample point was 150 MPa, which is considerably below the yield strength of the material. Given that the head of the low-flow condition in this research did not reach the maximum operational head that the pump can run, the maximum stress should have a higher margin to ensure that the pump station operates under the high head. Therefore, the maximum stress constraints ≤ 110 MPa were combined with the maximum stress analysis of the sample points. Given that the deformation was relatively small, the constraint range can be relaxed in the optimization process. The head of the design condition point is an important design parameter of the pump station operation. Moreover, the requirements are high. To ensure that the specific speed of the optimized impeller does not change substantially, the head of the design condition must be constrained to change within a small range.

5.2. Optimization Results and Analysis

In the optimization process, three multi-objective optimization methods can be realized because of the approximate model method, short optimization time, low computational cost, and minimally complex optimization objectives. This study selected the AMGA optimization algorithm. According to the optimization algorithm and approximation model, 15,000 iterations were carried out using the Isight 5.8 software. The optimization model and all Pareto solution sets of feasibility are shown in Figures 11 and 12, respectively.

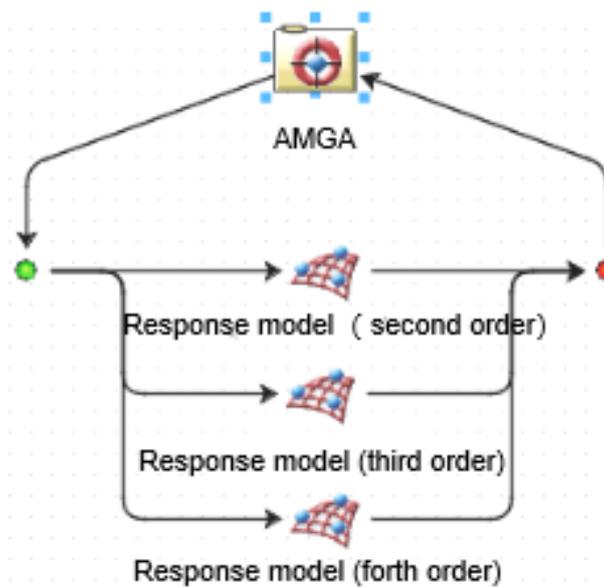


Figure 11. Optimization model.

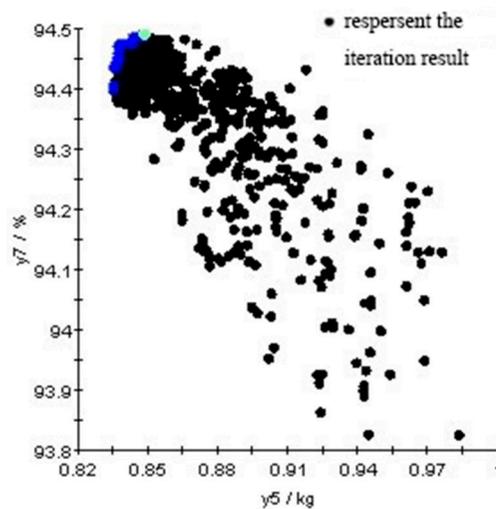


Figure 12. Pareto solution set.

All points in the graph are feasible solutions. The combination of the color points is the Pareto frontier, and the optimal solution can be selected flexibly according to different weight values. The green solution is the final result in this study. The optimized results were compared with the initial results. Table 3 shows the comparison of the design variables before and after optimization. Table 4 presents the comparison of the response values before and after optimization. The comparison of the model before and after optimization is shown in Figure 13. The cloud chart of the maximum stress and deformation distribution is shown in Figure 14.

Table 3. Comparison of the design variables before and after optimization.

Design Variables	x_1	x_2	x_3	x_4	x_5	x_6	x_7	x_8	x_9
Initial value	0.8	1.2	15.6	32	48	4.2	6.2	6	12
Optimal value	0.745	1.448	17.408	31.269	49.803	4.538	5.984	5.057	11.360

Table 4. Comparison of the response values before and after optimization.

Response	y_1	y_2	y_3	y_4	y_5	y_6	y_7
Initial value	11.44	90.2147	0.00017979	103,620,000	0.94769	6.95309	93.9141
Optimal value	11.5174	90.2637	0.00021611	98,923,000	0.84843	7.1999	94.4913
Effect	0.67%	0.054%	20.20%	−4.53%	−10.47%	3.54%	0.61%
Computation value	11.5564	90.2068	0.00021412	102,600,000	0.84704	7.22086	94.4188
Error	0.33%	0.063%	0.92%	3.71%	0.16%	0.29%	0.076%

Note: Minus sign represents a decrease.

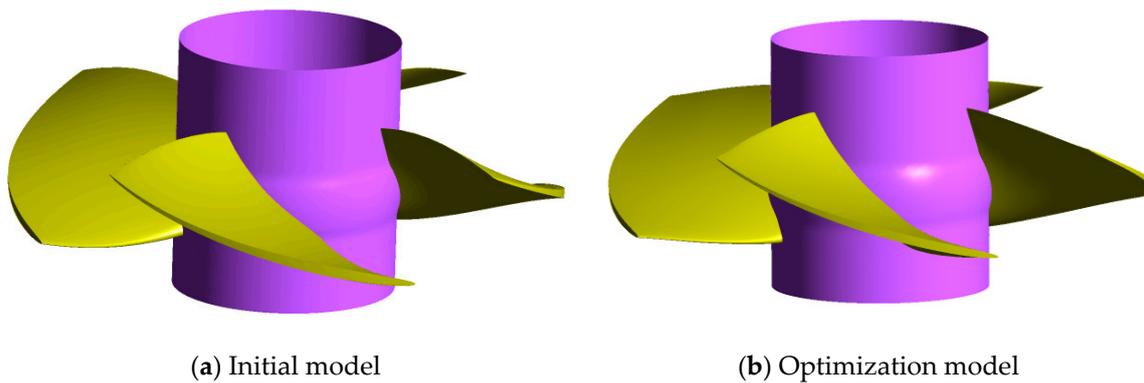


Figure 13. Comparison of the model before and after optimization.

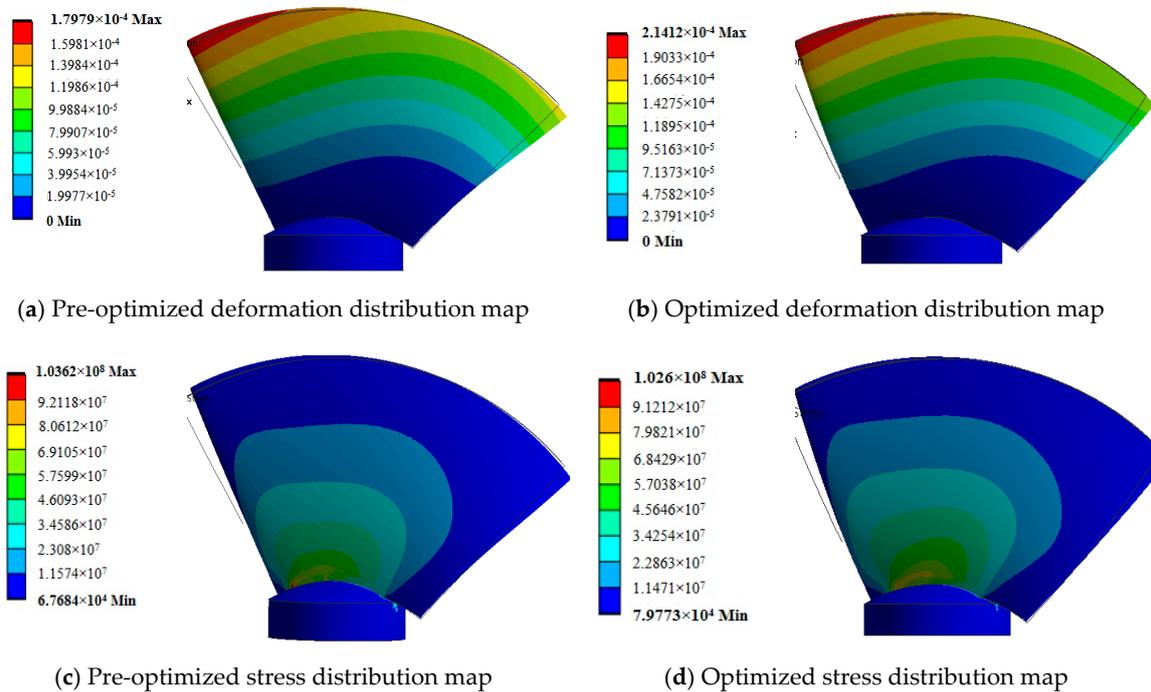


Figure 14. Cloud chart of the maximum stress and deformation distribution.

Table 3 and the Figure 13 show that the cascade density of the blade tip decreased after optimization, whereas the cascade density of the blade root increased. x_1 is the cascade density of blade tip, and x_2 is the cascade density multiple of blade root. The most direct effect of the change of the cascade density is the change of the shape and the mass of the blade. At the same time, it can reduce the length difference between the hub and rim airfoils and increase the efficiency of the axial-flow pump when reducing the cascade density of the blade tip and the cascade density of the blade hub. From the change trend of design parameters of x_3 , x_4 , and x_5 in Table 3, it can be found that the airfoil angle of

the rim and hub were increased. Hence, the attack angle of the blade was increased. Consequently, the airfoil work ability was improved, and the airfoil angle of the middle section was reduced, thereby making the distribution regular considerably reasonable. From the change trend of design parameters of x_6 and x_7 in Table 3, the camber of the airfoil on the flange side increased, while that on the hub side decreased. That means it can reduce the distortion of the blade and increase the work capacity of the blade. The airfoil thickness decreased from the change trend of the design parameter of x_8 and x_9 in Table 3. The reduction of the airfoil thickness had little effect on the hydraulic performance of axial-flow pump, but it can affect the mass of the axial-flow pump blade. The 3D blade models were obtained as shown in Figure 13 according to the design parameters before and after optimization in Table 3.

Table 4 shows that all constraints of the optimization result meet the requirements. The 'optimal value' in Table 4 is the theoretical calculation result by the approximation model, which is corresponding to the highlighted scheme in Figure 10. The 'computation value' in Table 4 is the numerical calculation result by the CFD software. The 'error' in Table 4 is the difference between numerical simulation results and theoretical calculation results. From the value of the error, it can be found that the numerical simulation results by CFD verify the theoretical calculation results by the approximation model well.

From Table 4, the head of the small flow condition point was above 11.5 m. Accordingly, the efficiency increased, but the increase was small. The constraint conditions were satisfied. From the optimization target, the quality decreased from 0.947 to 0.848 kg, the decline reached 10.47%, and design efficiency increased from 93.91% to 94.49%. Given an increase of 0.61%, the optimization effect is evident. Apart from the maximum deformation, other responses were optimized. According to the optimized design variables, the results can be obtained using a fluid–structure interaction calculation. Compared with the approximate model optimization results, the errors of other responses were below 0.5%, except for the maximum stress value error. The 3.71% error is acceptable because maximum stress varies widely, and the constraint value is less than half of the yield strength of the material. According to Figure 14, the maximum stress and maximum deformation distribution trends were consistent before and after optimization. The maximum stress and maximum deformation position remained the same, but the maximum value changed. The maximum deformation of the initial scheme was 0.18 mm, and the maximum deformation of the optimized scheme was 0.21 mm (Figure 14a,b), but all of them were within 0.3 mm of the constraint condition, which was caused by the increase of the working capacity and the decrease of the thickness of the blades. The maximum stress of the initial scheme was 103.6 MPa, and the maximum stress of the optimized scheme was 102.6 MPa (Figure 14c,d). After optimization, the structural strength increased due to the shorter blade length.

6. Conclusions

This study applied the theory and method of multi-disciplinary design optimization of the axial-flow pump to further improve the overall performance of the axial-flow pump impeller optimization design in this research. The MDO problem in this research was addressed can be concluded as follows: considering the blade quality and efficiency of design condition as an objective function; using the head of the small flow, efficiency of the small flow, maximum stress value, and maximum deformation value of the small flow as constraints; and ensuring that the blade head of the design conditions remains unchanged or varies in a small range. According to the range of the design variables, 80 sample points were generated using an optimized Latin hypercube method. Thereafter, the response surface method was used to build the approximate model according to the sample points. Lastly, the optimal design of axial-flow pump impeller was carried out by the approximate model, and the impeller satisfying the constraint conditions was obtained. The following results were obtained through calculation and analysis.

- (1) From the 80 sample points, the difference between the calculation results of the different sample points was relatively large, particularly for the structural performance. The maximum calculation results of the maximum stress and deformation value were over twice the minimum value,

which shows that the change of design parameters had a substantial influence on the structural performance of the pump. The response surface model had a superior fitting effect. This study used the second-order response surface method to construct the approximate model of the small flow rate efficiency and quality, in accordance with the comparative results of the fitting effect. The third-order response surface method was used to construct the approximate model of the small flow and design condition head. The fourth-order response surface method was used to construct the approximate model of the small flow maximum deformation, maximum stress, and design efficiency.

- (2) For the construction of the approximate model of the MDO design, the fitting effect of the response surface approximate model was better than that of the other approximate models. The results of the MDO design of the impeller are as follows: the quality decreased from 0.947 kg to 0.848 kg; the decline reached 10.47%, whereas the design efficiency increased from 93.91% to 94.49%; the increase was 0.61%; and the optimization effect was obvious. In addition, the errors of the other responses were below 0.5%, except for the maximum stress value error. The approximate model has high accuracy and the analysis results are reliable.

As we all know, the impeller of the axial-flow pump is the core and most important flow part in the pump station. The design quality of the impeller directly determines the overall efficiency of the pump device and even the pumping station. With the increasingly complex operational requirements, the pump design has to meet higher design requirements [25–27]. A multi-disciplinary design optimization [28] method can combine hydraulic design and structural design, so that it can get the optimized impeller to match the complex operating conditions. This present study solved some key technical problems in the MDO process of the axial-flow impeller. However, in addition to the mass of the blade, how to combine vibration characteristics, hydraulic noise, and materials to carry out multi-disciplinary optimization design is the main content of future studies.

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