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A Frequency Locking Method for ICPT System Based on LCC/S Compensation Topology

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Abstract: Aiming to maximize the transmission efficiency of inductively coupled power transmission (ICPT) system with the designed output power, a frequency locking method for an ICPT system based on LCC/S compensation topology is proposed in this paper. Firstly, the relationship between compensation component L_{f1} and output power was deduced by the lossless model, and the initial value of L_{f1} was obtained. Then, considering the system loss, the designed output power and frequency were input into the frequency locking program, and L_{f1} and other compensation parameters were dynamically tracked. At the same time, the transmission efficiency of the system was calculated, and the frequency that achieved maximum efficiency was automatically locked when the system met the requirements of the designed output power. Finally, based on the method, the output characteristics of the system were verified by experiments.

Keywords: wireless power transfer; compensation topology; loosely coupled transformer; power transmission system; transmission efficiency

1. Introduction

Inductively coupled power transmission technology uses the alternating magnetic field generated by the transmitting coils to couple the energy to the receiving coils so as to realize the wireless power transmission. Its non-contact power transmission characteristics make it convenient, safe, adaptable, so it is widely used in various fields such as biomedicine, electric vehicles and so on [1–3].

Compensation topology is an important aspect in ICPT systems because it can increase the power transfer ability, minimize the reactive power rating of the power source, and help achieve soft switching of the power in electronics devices [4]. There are four basic topologies depending on how the compensation capacitors are added to the primary and secondary coils, namely, series-series (SS), series-parallel (SP), parallel-series (PS), and parallel-parallel (PP) topologies [5,6]. In these four compensation topologies, the power transfer ability of ICPT system cannot be used to increase the transmission power when the load resistance is fixed because of the effect of the parameters of the loosely coupled transformer. More advantageous topologies have been forward to solve this problem by increasing the order of equivalent circuit in References [7,8]. LCC third-order topology is an outstanding method since the resonant frequency is independent of the parameters of loosely coupled transformer [8]. The doubled-side LCC compensation topology has been studied in depth by many scholars [9–14]. The double-sided LCC compensation is less sensitive to the variations of self-inductances caused by the change in the relative position of the primary and secondary coils [9]. The LCC compensation network has the least consumption of reactive power than CLC and four-coil structure [10]. A close-cycle transfer control strategy has been investigated to realize transmission from CC (constant current) mode to CV (constant voltage) mode for IPT EV (electric vehicle) charging system [11]. However, the use of multiple reactive devices makes its transmission efficiency limited and increases the system cost and volume [12]. The literature [13,14] discusses the power loss model

of the WPT system with doubled-side LCC compensation topology, expounding the necessity of considering loss. The literature [15] has designed a value for the compensation component L_{f1} and resonant frequency respectively and then calculates the parameters of other compensation components. However, the model does not consider the loss, and the resonant frequency value that the literature choose is lack of reasons. There is no locking process of the resonant frequency.

Aiming to maximize the transmission efficiency of the ICPT system with designed output power, a frequency locking method for ICPT system based on LCC/S compensation topology is proposed in the paper. Firstly, the expression of output power was deduced by establishing a lossless model to get the initial value of L_{f1} . Then, considering the loss, the output power was calculated by establishing a loss model to adjust L_{f1} until the output power reaches the design value. The equivalent parameters and magnetic flux density distribution of the loosely coupled transformer were obtained by finite element simulation analysis. When the output power was fixed, different frequencies correspond to different L_{f1} values. By comparing the transmission efficiency of different combinations of frequency and L_{f1} , the optimal combination was obtained, which maximized the transmission efficiency of the system with the designed output power, completing frequency locking and parameter design of LCC/S compensation structure.

2. Analysis of LCC/S Compensation

2.1. The Lossless Model of LCC/S Compensation

The proposed LCC/S compensation topology is shown in Figure 1. L_{f1} , C_{f1} and C_1 are the primary-side compensation inductor and capacitors, respectively. C_2 is the secondary-side compensation capacitor. L_1 and L_2 are the self-inductances of the primary coils and secondary coils, respectively. M is the mutual inductance between the primary and secondary coils. $-j\omega M I_2$ and $j\omega M I_1$ are reflected voltages from secondary and primary. I_{Lf1} , I_1 and I_2 are the currents on L_{f1} , L_1 and L_2 , respectively. U_S is the input voltage applied to the compensated coil.



Figure 1. Inductively coupled power transmission system with LCC/S compensation topology.

According to LCC compensation topology [8], the resonant frequency ω_0 should be

$$\omega_0 = \frac{1}{\sqrt{L_{f1}C_{f1}}} = \frac{1}{\sqrt{(L_1 - L_{f1})C_1}} = \frac{1}{\sqrt{L_2C_2}} \tag{1}$$

When the system is in resonance, the secondary-side impedance Z_{sec} , the reflected impedance Z_{ref} , and the input impedance Z_{in} can be simplified as follows:

$$Z_{sec} = j\omega_0 L_2 + \frac{1}{j\omega_0 C_2} + R_L = R_L \tag{2}$$

$$Z_{ref} = \frac{-j\omega_0 M I_2}{I_1} = \frac{\omega_0^2 M^2}{R_L}$$
(3)

$$Z_{in} = j\omega_0 L_{f1} + \frac{1}{j\omega_0 C_{f1}} \parallel (j\omega_0 L_1 + \frac{1}{j\omega_0 C_1} + Z_{ref}) = \frac{L_{f1}^2 R_L}{M^2}$$
(4)

According to Equation (4), the input current of this compensation topology is

$$I_{in} = \frac{U_S}{Z_{in}} = \frac{U_S M^2}{L_{f1}^2 R_L}$$
(5)

From Equation (5), it is obvious that I_{in} is in phase with U_S , zero phase angle is achieved and no reactive power is needed from the power source.

In the lossless model, the system is considered to have no power loss. So the input power equals to the output power, and the transmission power of this system is given by

$$P_{out} = P_{in} = \frac{U_S^2}{Z_{in}} = \frac{U_S^2 M^2}{L_{f1}^2 R_L}.$$
(6)

It can be seen that the output power is proportional to the square of the input voltage U_S and the square of the mutual inductance M. The output power is inversely proportional to the load R_L and the square of the compensation inductance L_{f1} . When the loosely coupled transformer parameters are fixed, the transmission power can be adjusted by adjusting the value of the compensation inductance L_{f1} .

It is known that P_{out} can be obtained in Equation (6) when not considering the power loss. In addition, we have $P_{out} = \frac{U_{out}^2}{R_L}$. Therefore, the output voltage and output current are given by

$$U_{out} = \sqrt{P_{out}R_L} = \frac{U_SM}{L_{f1}}$$
(7)

$$I_{out} = \frac{U_{out}}{R_L} = \frac{U_S M}{R_L L_{f1}}.$$
(8)

From Equations (7) and (8), it is obvious that the output voltage and output current are in phase. The unit power factor for the output rectifier is also achieved. Moreover, the output voltage does not rely on the load R_L , ICPT system with LCC/S compensation has constant voltage output characteristics.

2.2. The Loss Model of LCC/S Compensation

According to Equation (6), once the input voltage, the mutual inductance, the compensation inductance and the load are determined, the system power value is fixed. Moreover, if the resonance frequency is changed, the matching network will also change to reflect this frequency change. The system is required to achieve the highest efficiency at the desired output power and the compensated inductance values can be optimized at that point.

When the transmission power of the ICPT system is fixed, the transmission efficiency of the system will depend on the power loss, which will be closely related to the equivalent series resistances (ESRs) of each component in the LCC/S compensation topology. The ESRs of inductances are closely related to the quality factors of the inductances, the inductances values, and the operating frequency. The ESRs of capacitances are closely related to the dissipation factors of the capacitance values, and the operating frequency. The expressions of ESRs are given by

$$R_{Lf1} = \frac{\omega L_{f1}}{Q_{f1}} \tag{9}$$

$$R_{Cf1} = \frac{DF}{\omega C_{f1}} R_{C1} = \frac{DF}{\omega C_1} R_{C2} = \frac{DF}{\omega C_2}$$
(10)

where Q_{f1} stand for the quality factors of L_{f1} , which can be approximated at 200 based on their inductance values. *DF* is the dissipation factor of the capacitors, which can be approximated at 0.05% [13,14]. R_{L1} and R_{L2} are the AC resistances of the primary coils and secondary coils, respectively.

Figure 2 shows the equivalent circuit with ESRs. The efficiency analysis can be done separately. The total efficiency η_{LCCS} is the product of η_1 , η_2 , η_3 , η_4 . As shown in Figure 2, η_1 stands for the efficiency of Block 1, which is the ratio of real power obtained by the load over the real power entering into Block 1. η_2 stands for the efficiency of Block 2, which is the ratio of real power entering into Block 3, which is the ratio of real power entering into Block 4, which is the ratio of real power entering into Block 2 over the real power absorbed by Block 3 over the real power absorbed by Block 4. The expressions of η_1 , η_2 , η_3 , η_4 are shown below respectively.



Figure 2. The equivalent circuit with ESRs.

$$\eta_1 = \frac{R_L}{R_L + R_{C2} + R_{L2}} \tag{11}$$

$$\eta_2 = \frac{R_{ref}}{R_{ref} + R_{C1} + R_{L1}}$$
(12)

$$\eta_{3} = \frac{\left|R_{Cf1} + \frac{1}{j\omega C_{f1}}\right|^{2} (R_{C1} + R_{L1} + R_{ref})}{\left|R_{Cf1} + \frac{1}{j\omega C_{f1}}\right|^{2} (R_{C1} + R_{L1} + R_{ref}) + \left|R_{C1} + R_{L1} + Z_{ref} + \frac{1}{j\omega C_{1}} + j\omega L_{1}\right|^{2} R_{Cf1}}$$
(13)

$$\eta_4 = \frac{\operatorname{Re}(Z_{block3})}{R_{Lf1} + \operatorname{Re}(Z_{block3})} \tag{14}$$

where Z_{block3} , Z_{ref} are respectively the impedances of Block 3 and the reflected impedance to the primary side. R_{ref} is the reflected resistance to the primary side.

Therefore, the total efficiency of the system can be gain by the product of Equations (11), (12), (13) and (14), providing a theoretical basis for calculating transmission efficiency in the frequency locking method. However, the parameters of the loosely coupled transformer in the above formulas are still unknown. In order to obtain the primary and secondary inductances, AC resistances and mutual inductances of the transformer, the finite element simulation of the loosely coupled transformer is needed to carry out, as shown below.

3. Analysis of Finite Element Simulation

The finite element simulation software COMSOL was used in this paper to construct LCC/S compensation network based on the axial loosely coupled transformer. Axial loosely coupled transformer model was first established, and the primary and secondary inductances and mutual inductances of the transformer were determined through the no-load and short-circuit experiments inside the COMSOL. Then, the component parameters of the compensation structure were calculated according to the obtained transformer structural parameters, and then the entire ICPT system including the compensation structure was completed.

Figure 3 is the schematic diagram of the axial loosely coupled transformer and the model in the finite element simulation software COMSOL. It is mainly composed of primary and secondary cores and primary and secondary coils, the inner core and the inner coils are the primary parts, and the

outer core and the outer coils are the secondary parts. The geometric parameters of the axial loosely coupling transformer are shown in Table 1.



Figure 3. Axial loosely coupled transformer. (a) Two-dimensional axisymmetric model;(b) three-dimensional model.

Geometric Parameter	Value	
The inner diameter of the primary core/mm	83	
The outer diameter of the primary core/mm	103	
The inner diameter of secondary core/mm	137	
The outer diameter of secondary core /mm	157	
Height/mm	50	
Turns of coil	46/46	

Table 1. Geometric parameters of the axial loosely coupling transformer.

According to the structure diagram shown in Figure 4, an ICPT simulation platform was built. The entire system included five parts: high-frequency power supply, primary compensation, loosely coupled transformer, secondary compensation and load. The primary and secondary compensations were achieved through the 'coils' in COMSOL to realize the real-time coupling of the compensation circuits and the loosely coupled transformer.



Figure 4. Structure diagram of the ICPT system simulation.

Figure 5 shows the distribution of magnetic flux density. Figure 5a shows the distribution of the magnetic flux density of the three-dimensional model, and Figure 5b shows the distribution of the magnetic flux density of the two-dimensional axisymmetric model.

In the COMSOL simulation, L_1 and R_{L1} can be estimated by opening the secondary side and applying the rated voltage to the primary side. L_2 and R_{L2} can be measured by opening the primary side and applying the rated voltage to the secondary side. Mutual inductance M can be measured by a short circuit on the secondary side and applying rated current to the primary side. The results of the primary and secondary inductances, AC resistances and mutual inductances of the transformer were: $L_1 = 0.84$ mH; $L_2 = 0.76$ mH; M = 0.67 mH; $R_{L1} = 0.27 \Omega$; $R_{L2} = 0.31 \Omega$. The coupling coefficient between the primary and secondary sides was 0.839.



Figure 5. The distribution of magnetic flux density. (**a**) Three-dimensional model; (**b**) two-dimensional axisymmetric model.

4. Frequency Locking Method

From Equation (6), the output power is related to L_{f1} , while L_{f1} is related to the resonant frequency, so the output power is indirectly related to the resonant frequency. When the transmission capacity is determined, the loss of the system can be reduced by changing the resonant frequency, thus the transmission efficiency will be improved.

When the required power is set, the inductance L_{f1} can be determined by Equation (6). However, the output power will be less than the set value (P_{set}) when taking the loss of the system into account, so the inductance L_{f1} must be adjusted. The design procedures can be summarized in the flowchart as shown in Figure 6.



Figure 6. Flowchart of compensation parameters design.

Substituting the initial L_{f1} into Equations (1), (9) and (10), C_1 , C_{f1} , C_2 , R_{Lf1} , R_{Cf1} , R_{C1} and R_{C2} can be calculated. The values of each compensation component and its equivalent series resistance were substituted into the Figure 2, the output power (P_{out}) of the whole ICPT system can be calculated. If the absolute value of the difference between P_{out} and P_{set} is greater than the setting tolerance (1%)

was set in this paper), the value of L_{f1} will be decreased to re-enter the loop. Otherwise, the loop will be terminated.

The output power and efficiency of the ICPT system can be obtained by applying Equations (9), (10), (11), (12), (13) and (14) in the MATLAB. For our case, the desired output power was 1 kW and the load is 100 Ω . Figure 7 shows the output powers with the compensation inductance L_{f1} and resonant frequency. Figure 8 shows the efficiencies with the compensation inductance and resonant frequency. Output power decreases with the increase of compensation inductance and resonant frequency. When the resonant frequency was within 5 kHz to 100 kHz, the efficiency of the entire ICPT system varied within 0.919–0.978. Therefore, there must be a combination of compensation inductance and resonant frequency, which can maximize the transmission efficiency while allowing the ICPT system to transmit 1 kW.



Figure 7. Output powers with the compensation inductance L_{f1} and resonant frequency.



Figure 8. Efficiencies with the compensation inductance L_{f1} and resonant frequency.

Figure 9 shows the curve of the compensation inductance L_{f1} with the resonant frequency when the output power was 1 kW. From the picture, the value of compensation inductance L_{f1} decreased as the frequency increased. Figure 10 shows the curve of the efficiency with resonant frequency at the output power of 1 kW, where the compensation inductance is the value in Figure 9. From Figure 10, the transmission efficiency increases first and then decreases with the increase of the resonant frequency. The peak value of the transmission efficiency curve is the highest efficiency that the ICPT system can achieve, which was 97.8%. The value of the resonant frequency at this point is the optimal frequency value, which was 15 kHz.



Figure 9. Curve of the compensation inductance with different resonant frequency when the output power is 1 kW.



Figure 10. Curve of the efficiency with a different resonant frequency.

Figure 11 shows the relationships between the output voltage and load resistance when the resonant frequency was 15 kHz, considering loss and not considering loss respectively. As can be seen from the figure, when the loss is considered, the output voltage is smaller and the output voltage change rate is larger. Therefore, the influence of loss is necessary to be considered when discussing LCC/S compensation. When considering the loss, the output voltage change rate was less than 0.7% in the load resistance range of 80–200 Ω , showing that the system had good output voltage stability.



Figure 11. Curves of the output voltage with different load.

5. Experimental Verification

Based on the previous simulation analysis, the constant voltage, large capacity and high-efficiency transmission characteristics of LCC/S compensation were experimentally verified. The results before and after compensation were compared.

5.1. Construction of ICPT System Experimental Platform

Figure 12 is the ICPT experimental platform with LCC/S compensation structure. The instruments needed for the experiment are: (1) a high-frequency power supply that ranges from 3 kHz to 120 kHz in frequency and from 0 V to 120 V in voltage; (2) an axial loosely coupled transformer; (3) high-frequency and high-voltage compensation elements L_{f1} , C_{f1} , C_1 , C_2 , which are resonant with loosely coupled transformer parameters; (4) oscilloscope; (5) resistance. Setting the frequency of the high-frequency power supply at 15 kHz and the voltage at 100 V.



Figure 12. ICPT experimental platform with LCC/S compensation structure.

5.2. Verification of Constant Voltage Output Characteristic of LCC/S Compensation

The output voltage before and after compensation varied with load resistance is shown in Table 2 (due to the limitation of power supply capacity, only 100–140 Ω load resistance experiments have been carried out). We can know that when the load resistance was 100 Ω , the output voltage was 72.6 V before compensation, but it increased considerably to 294.2 V after LCC/S compensation. When the load resistance varied in the range of 100 to 140 Ω , the maximum voltage variation rate was 6.17% before compensation, but it decreased obviously to 1.87% after LCC/S compensation. Therefore, by LCC/S compensation, not only the output voltage of the system can be increased, but also the voltage variation rate can be smaller.

Load/Ω	100	110	120	130	140
Voltage before compensation/V	72.6	73.1	73.9	74.9	76.1
Voltage variation rate before compensation/%	0	0.69	1.79	6.17	4.82
Voltage after compensation/V	294.2	295.6	296.8	298.1	299.7
Voltage variation rate after compensation/%	0	0.48	0.88	1.33	1.87

Table 2. The output voltage before and after compensation.

5.3. Verification of Large-capacity and High-efficiency Transmission Characteristic of LCC/S Compensation

As shown in Table 3, when the load resistance varied in the range of 100 to 140 Ω and the system frequency was at 15 kHz, the output power before and after compensation was compared (due to the limitation of power supply capacity, only 100–140 Ω load resistance experiments have been carried out). It can be known that after LCC/S compensation, the output power of the ICPT system was significantly greater than that before compensation, and the transmission efficiency was up to 92.16% when the load was 100 Ω . With the increase of load resistance, the transmission power and efficiency of the compensated ICPT system decreased, which is in agreement with Equation (6). Therefore, the experiment shows that LCC/S compensation can greatly improve the transmission power of the ICPT system and get a high level of transmission efficiency.

Table 3. Power and efficiency after compensation.

Load/Ω	100	110	120	130	140
Output power before compensation/W	52.71	48.58	44.96	43.15	41.37
Output power after compensation/W	865.54	794.36	734.09	683.57	641.57
Input power after compensation/W	939.19	877.66	836.48	813.10	802.26
Efficiency after compensation/%	92.16	90.51	87.76	84.07	79.97

6. Conclusions

The paper proposes a frequency locking method for ICPT system based on LCC/S compensation topology. The relationships between the parameters of each compensation component in LCC/S compensation are given. Based on this, the output characteristics were derived and the calculation method of the efficiency of the ICPT system is given. In order to achieve efficient operation of the ICPT system, the optimal frequency locking method under constant output power is proposed through the synergy between resonant frequency and compensation inductance. A 1 kW ICPT system was designed and built using the method proposed in this paper. The efficiency of the simulated system was up to 97.8%. At last, the ICPT experiments show that by LCC/S compensation and optimal frequency locking, the system can get a nearly constant output voltage and greatly larger transmission power.

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