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Numerical Investigation of Flow and Heat Transfer in a Rotor-Stator Cavity with Centripetal Carbon Dioxide Through-Flow

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Abstract: A centrifugal carbon dioxide compressor is a kind of general machine with extensive applications. The geometry of the side chambers of the compressors can be determined by studying the rotor-stator cavity with centripetal through-flow. In this paper, numerical simulations were conducted to predict the characteristics of flow and heat transfer. Three different speeds of rotation and two axial gap widths were considered. The correlations of the core swirl ratios were determined by fitting the results for two axial gap widths. The amounts of the moment coefficients of the disk were predicted. In order to better analyze the temperature field, the radial distributions of the local heat transfer coefficient were numerically investigated. According to the simulation results, the average Nusselt number was found to be dominated by the turbulent flow parameter. It also seemed to be proportional to the moment coefficient at a fixed circumferential Reynolds number.

Keywords: rotor-stator cavity; centripetal; carbon dioxide; flow; moment coefficient; heat transfer

1. Background

The main application fields of centrifugal carbon dioxide compressors are at oil exploitation sites as the supplies of injection gas or at carbon capture and storage power plants for carbon dioxide compression [1]. To transport more fluid and to lower the energy consumption, the rotational speed of the impeller (whose outer radius is 0.4 m) in a large centrifugal carbon dioxide compressor already reaches up to 5000 rpm, whose circumferential Reynolds number Re , defined in Equation (1), is up to 2.09×10^7 . There are two main methods used to improve the compressor efficiencies. The first method, which is extensively studied, is to optimize the geometry of the impeller. The other method is to conduct the geometry optimization of the side chambers (both the front chamber and the back chamber in Figure 1), which is not sufficiently researched. The unreasonable geometry of the side chamber may result in excessive axial thrust, severe mechanical vibration, large disk frictional loss, low service life, etc. Compared with air, carbon dioxide is a kind of fluid with low kinematic viscosity. The design of the side chambers in such a centrifugal compressor is therefore becoming one of the focuses of study. In Figure 1a, a meridional sketch of a centrifugal carbon dioxide compressor stage is depicted. The side chambers include the front chamber (marked blue) and the back chamber (marked green). The simplified model of either side chamber is the rotor-stator cavity with centripetal through-flow, shown in Figure 1b. In order to design the geometry rationally, it is of great significance to investigate the characteristics of the flow and the heat transfer within the cavity.

$$Re = \frac{\Omega \cdot b^2}{\nu} \quad (1)$$

where Ω is the angular velocity of the disk, b is the outer radius of the disk, and ν is the kinematic viscosity.

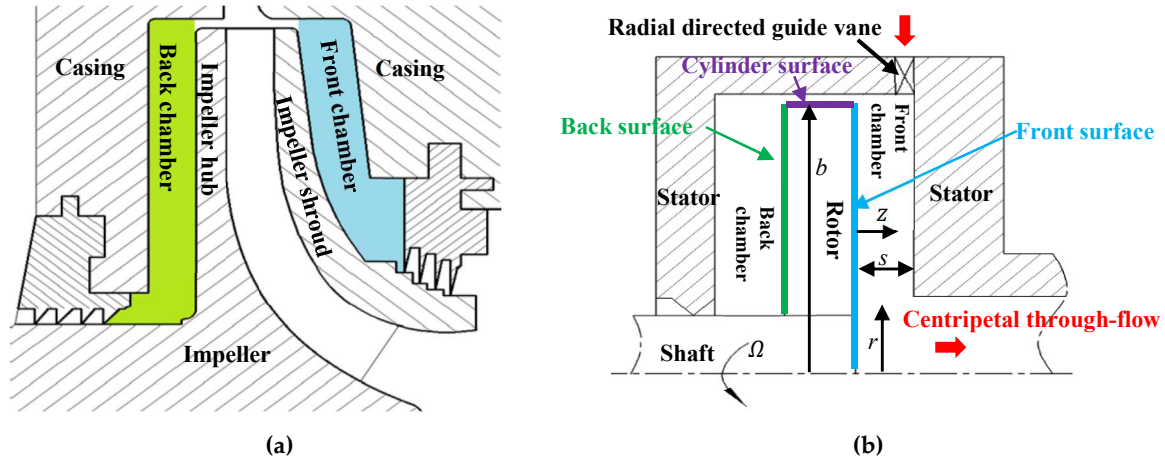


Figure 1. Meridional sketch: (a) a centrifugal compressor stage and (b) the simplified rotor-stator cavity model for a side chamber. z : axial coordinate; r : radial coordinate; s : axial gap width of the front chamber.

1.1. Turbulent Flow Type

In a rotor-stator cavity, the dynamic behaviors and the energy losses differ depending on the turbulent flow types. In a side chamber, the turbulent flow is classified into two types [2,3], namely the Batchelor type and the Couette type. The difference is that the Batchelor-type flow has a viscous core region (the gradient of the tangential velocity V_t is close to zero) between the disk boundary layer and the wall boundary layer, while the Couette-type flow has merged boundary layers. Owen et al. [4–6] distinguished the Batchelor type flow based on the turbulent flow parameter λ_t , defined in Equation (2). The parameter λ_t weighs the relative strength of the viscous and the inertial force of the through-flow. Ewa et al. [7,8] found that the Couette-type flow may change to the Batchelor-type flow with the increase of the non-dimensional axial gap G (defined in Equation (2)) or with the increase of Re . Hu et al. [9] investigated the effects of G and through-flow on the flow types when the flow changes from the Batchelor type to the Couette type based on numerical simulations. With a third axis of the through-flow coefficient C_w , they extended part of the 2D Daily and Nece diagram into 3D. The boundaries distinguishing the Batchelor-type flow and the Couette-type flow are valid for the parameter ranges $|C_w| \leq 5050$ and $Re \leq 3.17 \times 10^6$.

$$\lambda_t = \frac{C_w}{Re^{0.8}}; \quad C_w = \frac{\dot{m}}{\mu \cdot b}; \quad G = \frac{s}{b} \quad (2)$$

where λ_t is the turbulent flow parameter, C_w is the through-flow coefficient, $\dot{m}$ is the mass flow rate, and μ is the dynamic viscosity.

1.2. Core Swirl Ratio

The core swirl ratio K is defined in Equation (3). It is the ratio of the angular velocity of the fluid Ω_f at a position half of the axial gap width to that of the disk, namely Ω . The radial distributions of K can be used to estimate the pressure distributions along the rotor. After that, the axial thrust can be predicted. Poncet et al. [2,3], Hu et al. [9] and Debuchy et al. [10] investigated the velocity profiles for both the Batchelor-type and the Couette-type flow. Hu et al. [11] investigated the effects of G and centrifugal through-flow on K . Nguyen et al. [12] studied the velocity profiles in a rotor-stator system by PIV (Particle Image Velocimetry) measurements. Lock et al. [13] investigated the distributions of K in a rotor-stator cavity with pre-swirl nozzles, which deliver the cooling air to the turbine blade.

Kurokawa et al. [14,15], Coren et al. [16] and Will et al. [17,18] conducted either numerical or the experimental investigations on K .

$$K = \frac{\Omega_f}{\Omega} \text{ at } \zeta = 0.5; \quad \zeta = \frac{z}{s} \quad (3)$$

where Ω_f is the angular velocity of the fluid, and ζ is the non-dimensional axial coordinate.

1.3. Disk Frictional Loss

Reducing the disk frictional losses is always the hotspot of the research into rotor-stator cavities. With the models of enclosed rotor-stator cavities, Daily and Nece [19] found that the moment coefficient C_M , defined in Equation (4), on a single surface can be predicted according to the flow regimes. Kurokawa et al. [20] illustrated the impacts of C_w on C_M . Dibelius et al. [21] carried out the torque measurements in a shrouded rotor-stator system. Gartner [22,23] used an analytical approach to predict the frictional torque in a rotor-stator system with both radial outflow and cylindrical shroud. Coren et al. [16] determined a correlation giving the amounts of C_M in terms of Re and C_w . Dorfman [24] theoretically studied the effects of disk roughness on C_M . By pasting sand papers, Daily and Nece [25], Kurokawa et al. [20] and Hu et al. [26] experimentally investigated the roughness effects on C_M .

$$C_M = \frac{2 \cdot |M|}{\rho \cdot \Omega^2 \cdot b^5} \quad (4)$$

where M is the frictional torque on a single surface, ρ is the density of the fluid.

1.4. Heat Transfer

The design of a side chamber requires insight into the characteristics of the heat transfer. Metzger et al. [27] calculated the average convective heat transfer coefficient h_{ave} , computed with Equation (5), on the rotor with the help of remote infrared sensors.

$$h_{ave} = \frac{\int_{r_c}^b 2hrdr}{b^2 - r_c^2} \quad (5)$$

where h is transfer coefficient and r_c is the inner radius where the measurements of h start.

Owen's research group [4–6], Metzger's research group [28–30] and Luo et al. [31] used the transient TLC technique to measure the radial distribution of the local convective heat transfer coefficient h , computed as

$$h = \frac{-q}{(T_{aw} - T_w)}; \quad T_{aw} = T_\infty + r_{rec} \cdot \frac{u_\infty^2}{2 \cdot l}; \quad r_{rec} \approx Pr^{0.5}; \quad Pr = \frac{\mu \cdot l}{k} \quad (6)$$

where q is the heat flux, T_{aw} is the adiabatic wall temperature, T_w is the surface temperature, T_∞ is the temperature of the mainstream at $\zeta = 0.5$, r_{rec} is the recovery factor, u_∞ is the velocity of the mainstream at $\zeta = 0.5$, l is the specific heat at constant pressure, Pr is the Prandtl number and, k is the thermal conductivity.

Luo et al. [31] found that the heat transfer behaviors of the rotor are quite different in the viscous, the co-determined and the inertial sections, which are identified by the amounts of the flow pattern parameters. Poncet et al. [32] performed a numerical investigation on the flow and the heat transfer inside a rotor-stator cavity. Tuliscka-Sznitko et al. [33] and Majchrowski et al. [34] performed the large-eddy simulation for the distributions of the local Nusselt numbers Nu , written in Equation (7). Tuliscka-Sznitko et al. [35] conducted the numerical investigations on the flow and the heat transfer in a rotating cavity. In the literature, however, most of the investigations concerning the characteristics of the heat transfer are conducted using the rotor-stator cavity model with centrifugal through-flow instead of centripetal through-flow.

$$Nu = \frac{h \cdot r}{k}; \quad Nu_{ave} = \frac{\int_{r_c}^b \frac{2hr^2 dr}{k}}{(b^2 - r_c^2)} \quad (7)$$

The parameter k is mainly affected by the temperature. By fitting the results in [36], the heat conductivity k of carbon dioxide is estimated with Equation (8). The variation of k versus T_∞ is plotted in Figure 2.

$$k = 8 \times 10^{-5} \cdot T_\infty - 0.0069 \quad (8)$$

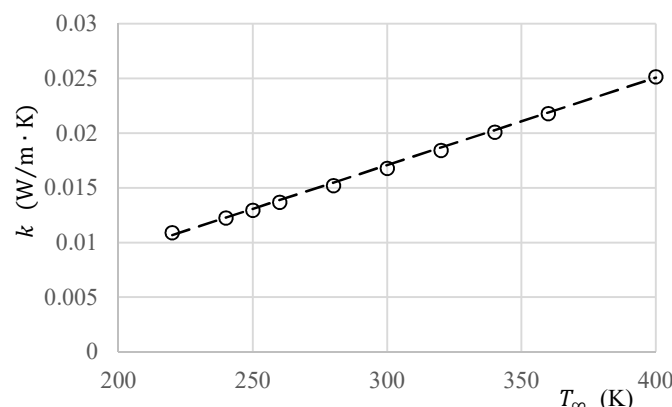


Figure 2. Variation of k versus T_∞ for the carbon dioxide. Hollow points: results in [36]; Dashed line: results from Equation (8).

Currently, most of the investigations concerning rotor-stator cavities are performed for $Re \leq 3.17 \times 10^6$. The experimental medium is primarily water or air. The available results of the velocity and the moment coefficient, however, are not fully applicable to the design of the side chambers in centrifugal carbon dioxide compressors with the numbers of Re up to 2.09×10^7 . In order to extend the service life, the characteristic of the heat transfer should also be studied. Hence, this paper aimed to conduct the numerical simulations of the flow and the heat transfer in a rotor-stator cavity with centripetal carbon dioxide through-flow. To verify the correctness of the simulation set-ups, some measurements of the tangential velocity, the temperature and the disk frictional torque were performed by the rotor-stator cavity group at the chair of turbomachinery, University of Duisburg-Essen. The results were used to verify the correctness of the set-ups of numerical simulations. According to the results from numerical simulations, the distributions of K , C_M , h and the average Nusselt number Nu_{ave} were predicted for two cavity models: $G = 0.0125$ and $G = 0.0375$. The results in this paper can help the designers to better design high-speed centrifugal carbon dioxide compressors.

2. Rotor-Stator Cavity Test Rig

A rotor-stator cavity test rig with carbon dioxide was designed and built-up to investigate the cavity flow at the University of Duisburg-Essen. A sketch of the main region is shown in Figure 3 [1]. The main parameters of the test zone are listed in Table 1. The front chamber (FC) is the test section. The test rig mainly includes four parts, namely the air supply system, the pipelines, the test zone and the data acquisition system. A centrifugal compressor is used to supply the desired carbon dioxide flow. The carbon dioxide enters the test section via the pipeline and a mesh heater. The temperature of the carbon dioxide at the inlet of the test rig (see Figure 3) is around 350 K, which is measured by a thermocouple. The pressure at the inlet is around 2 bar (absolute pressure). The front cover has a special designed geometry so that the axial gap width of the front cavity can be changed. A radial directed guide vane is installed (see Figure 1) at the inlet, ensuring that the flow has no angular momentum when pumped into the cavity. The shaft of the test rig is driven by a high-speed motor (up to 5000 rpm). The disk frictional torque is measured by a torquemeter. The front cover of the test rig is produced with 13 holes at different radial coordinates for the implementation of hot-wire anemometry (5 positions) and the measurements of pressure or temperature (8 positions), given in Table 2. The probes of both the hot-wire and the thermocouple measure the data at the position $\zeta = 0.5$. The errors of the measurements are listed in Table 3.

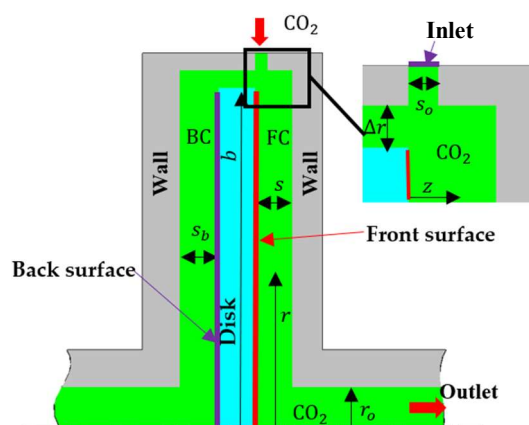


Figure 3. A sketch of the main region of the test rig (not to scale). r_o : radius of the outlet pipe; s_b : axial gap width of the back chamber (BC), Δr : radial gap; s_o : axial width of the inlet.

Table 1. Main parameters of the test zone in this study.

b (m)	r_o (m)	s (mm)	s_b (mm)	Δr (mm)	s_o (mm)	n (rpm)
0.4	0.07	5, 15	15	2	2	≤ 5000

Table 2. Positions of the measurements in the test rig.

Parameters	Non-Dimensional Radial Coordinate $x (= \frac{r}{b})$							
Temperature or pressure	0.42	0.5	0.58	0.67	0.74	0.82	0.87	0.955
Hot-wire anemometry	0.51		0.67		0.74		0.87	0.955

Table 3. Error of the measurements.

Hot-Wire Anemometry		Pressure	Temperature	Torque
Displacement	Rotation			
± 0.05 m	$\pm 0.5^\circ$	1% (FS)	0.02 K	0.1 % FS

3. Numerical Simulation

3.1. Numerical Simulation Set-Ups

Numerical simulations are carried out using the ANSYS CFX 13.0 code. Considering the axial symmetry of the problem, two segments (each 5 degree) of the two domains ($G = 0.0125$ and $G = 0.0375$) are modeled and meshed. A rotational periodic boundary condition is applied. Due to the good thermal conductivity of the aluminum disk and the cooling system in the stationary wall, the temperature on the front surface, the back surface of the disk and the stationary wall (see Figure 3) are set as 300 K (environment temperature). The surface roughness on all the surfaces in contact with carbon dioxide are $R_z = 1 \mu\text{m}$. The boundary conditions at the inlet and the outlet are the pressure inlet and mass flow outlet. The values of pressure at the inlet are set as 2 bar (absolute pressure), which is obtained by the pressure measurements at the cavity inlet. At the outlet, the values of the mass flow rate are set according to the correlation $\dot{m} = \frac{1}{72} \cdot \mu \cdot b \cdot C_w$. The simulation type is set as steady state. The convergence criteria for all the numerical simulations are set as 10^{-5} in RMS type. The heat transfer model is set as total energy. The values of the temperature at the centripetal inlet and the cavity outlet are set as 350 K and 300 K. The fluid for numerical simulations is carbon dioxide at STP. The turbulent numeric is set as second-order upwind. The mesh independence analyses are performed, and the suitable numbers of elements are 1.23 million ($G = 0.0125$) and 1.47 million ($G = 0.0375$), respectively. The maximum value of y^+ in the two simulation models is 3.4. The SST $k - \omega$ turbulence model in combination with the scalable wall functions is selected [1]. The values of C_w and Re investigated in this paper are given in Table 4. The values of Q_t , C_w and C_{qr} are defined as negative for centripetal through-flow.

Table 4. Computing conditions.

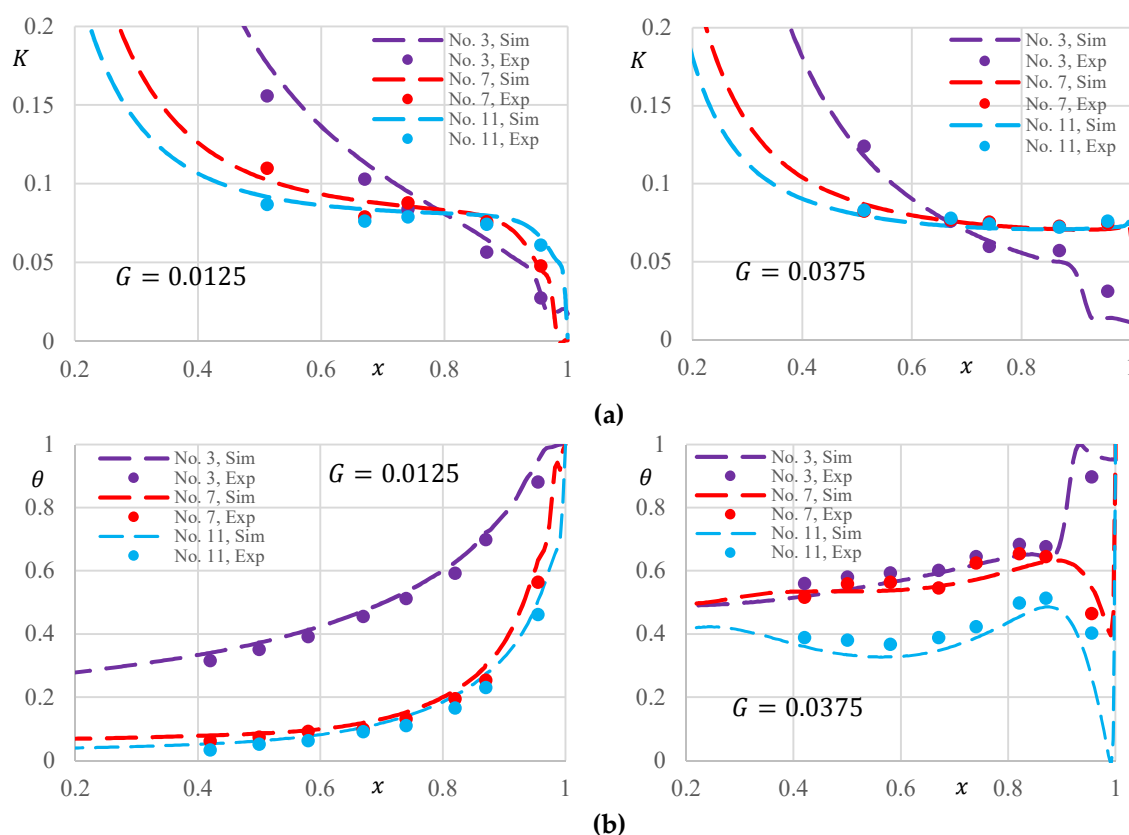
1	−1262	3.87×10^6	7	−3787	1.28×10^7
2	−2525		8	−5050	
3	−3787		9	−1262	
4	−5050	1.28×10^7	10	−2525	2.09×10^7
5	−1262		11	−3787	
6	−2525		12	−5050	

3.2. Verifications of the Numerical Simulation Set-Ups

The experiments are conducted to verify the correctness of the numerical simulation set-ups. The values of K and θ , related by Equation (9), from numerical simulations and by measurements are compared in Figure 4a and Figure 4b. The distributions of K from numerical simulations are in relatively good accordance with those obtained by measurements. At a small axial gap width of $G = 0.0125$, the differences of K are relatively large. It is speculated that the geometry of the hot-wire probe has a relatively large impact on the local velocity distribution for $G = 0.0125$. The amounts of θ from numerical simulations follow the same trends as those by measurements. The errors are primarily attributed to the assumption that the temperatures on the surfaces of both the rotor and the stator are fixed values while there are certain temperature gradients during the experiments.

$$\theta = \frac{T_{\infty} - T_{min}}{T_{max} - T_{min}} \text{ at } \zeta = 0.5 \quad (9)$$

where T_{max} is the maximum temperature and T_{min} is the minimum temperature.



No.	C_w	Re	No.	C_w	Re	No.	C_w	Re
3	−3787	3.87×10^6	7	−3787	1.28×10^7	11	−3787	2.09×10^7

Figure 4. Verification of the numerical simulation set-ups: (a) distribution of K and (b) distribution of θ . Sim: from numerical simulations; Exp: by measurements.

4. Results and Discussions

4.1. Core swirl Ratio K

According to Poncet et al. [2,3], the radial pressure distribution can be estimated with Equation (10):

$$\frac{\partial p}{\partial r} = \rho \cdot K^2 \cdot \Omega^2 \cdot r \quad (10)$$

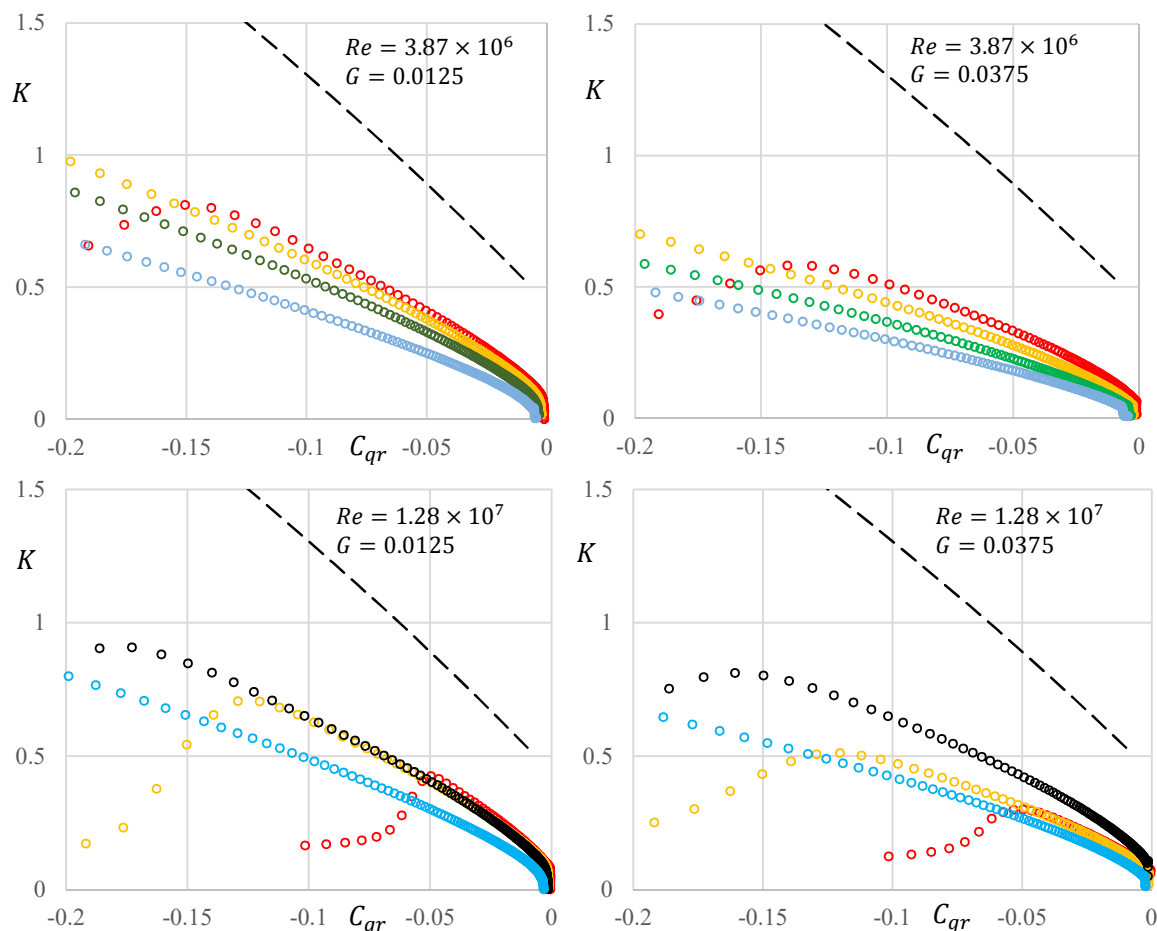
where v_t is the tangential velocity, v_r is the radial velocity, and Q_t is the volumetric through-flow rate per second.

On the basis of theoretical derivation, Poncet et al. [2,3] determined the basic form of the correlation for K in a rotor-stator cavity with air, written as Equation (11). The values of a and a_1 are determined by LDA (Laser Doppler Anemometry) measurements. This is valid in a rotor-stator cavity with air for $Re \leq 4.15 \times 10^6$, $G = 0.012$ and $G = 0.036$.

$$K = 2 \cdot (a \cdot C_{qr} + a_1)^{\frac{5}{7}} - 1 ; C_{qr} = \frac{Q_t \cdot Re_\phi^{0.2}}{2 \cdot \pi \cdot \Omega \cdot r^3} ; a = -5.9 ; a_1 = 0.63 \quad (11)$$

where C_{qr} is the local flow rate coefficient and Re_ϕ is the local circumferential Reynolds number.

According to the results from numerical simulations, the radial distributions of K are plotted in Figure 5. The results are much smaller than those from Equation (11). The amounts of a change obviously with Re and C_w . With the decrease of C_{qr} , the amounts of K increase in general. Under some computing conditions, the values of K drop after reaching their maximum values with the decrease of C_{qr} . These results are not discussed because this phenomenon occurs at a small radius ($x \leq 0.21$, in the impeller instead of the side chamber).



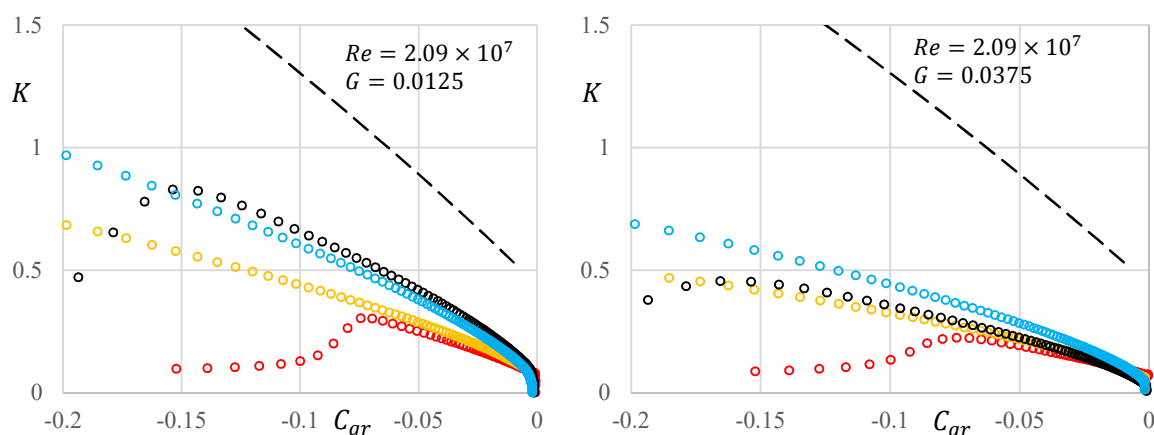


Figure 5. Variations of K versus C_{qr} for various Re and G from numerical simulations. Color of hollow points: red: $C_w = -1262$; orange: $C_w = -2525$; black: $C_w = -3787$; blue: $C_w = -5050$; dashed lines: results from Equation (11).

By fitting the results, the values of a and a_1 are found and are listed in Table 5. Compared with the constants in Equation (11), the amounts of a are found to be much smaller than 5.9. The values of a_1 are also smaller than 0.63. The variable a is expressed by λ_t with Equation (12) and Equation (13) for the two axial gap widths. The results are compared in Figure 6. Since the values of a_1 do not change greatly, the two average values of a_1 for the various computing conditions are used ($a_1 = 0.442$ for $G = 0.0125$ and $a_1 = 0.427$ for $G = 0.0375$).

$$a = 50.4 \cdot \lambda_t + 3.317; \quad a_1 = 0.442; \quad G = 0.0125 \quad (12)$$

$$a = 36 \cdot \lambda_t + 2.496; \quad a_1 = 0.426; \quad G = 0.0375 \quad (13)$$

Table 5. Amounts of a and a_1 by fitting the results.

G	No.	1	2	3	4	5	6	7	8	9	10	11	12
0.0125	a	3.1	2.8	2.4	1.8	3.4	3.1	3.1	2.4	2.6	2.5	3.1	3.1
	a_1	0.45	0.45	0.44	0.43	0.45	0.45	0.45	0.42	0.43	0.44	0.46	0.43
0.0375	a	2.4	2.1	1.8	1.5	2.5	2.3	2.5	1.9	2.4	2.2	1.9	2
	a_1	0.42	0.42	0.45	0.43	0.44	0.42	0.42	0.43	0.44	0.43	0.42	0.4

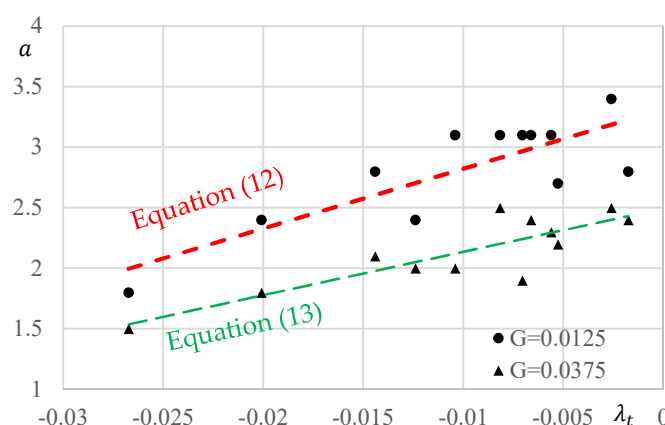


Figure 6. Variations of a versus λ_t for $G = 0.0125$ and $G = 0.0375$.

4.2. Moment Coefficient

The values of C_M from numerical simulations and the experimental results are plotted in Figure 7. The amounts of C_M keep a decreasing trend with increasing λ_t although there is some volatility.

Currently, the maximum difference between the simulation results and the experimental data is 28.51%. Two reasons appear to account for the large errors. Each value of M on the front surface (see Figure 1) is obtained by reducing the torque on the back surface and on the cylinder surface M_{cyl} (related by Equation (14) [11]). It is noted that the torques on the back surface are obtained when there is no through-flow and the axial gap widths of the two side chambers are equal at three speeds of rotation. The maximum error of 28.51% includes at least the errors on both the front and the back surfaces. The second reason is that the friction in the bearing may increase due to the vibration of the disk and the shaft for a smaller axial gap width of $G = 0.0125$.

$$M_{cyl} = \frac{0.042 \cdot \pi \cdot t \cdot \rho \cdot \Omega^2 \cdot b^5}{b \cdot \left(\lg \frac{\Omega \cdot b^2}{\nu}\right)^{1.5152}} \quad (14)$$

where t is the thickness of the disk (20 mm).

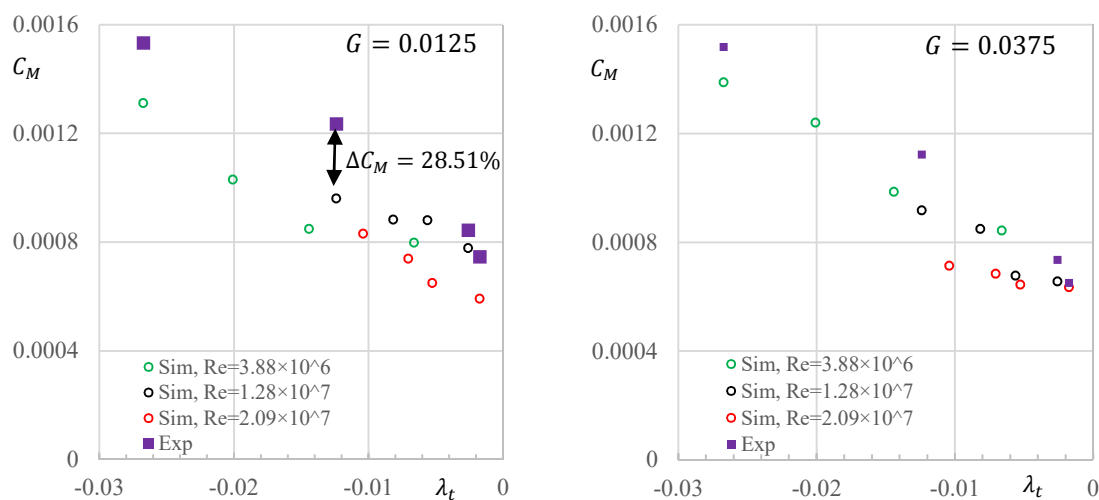


Figure 7. Variations of C_M versus λ_t for $G = 0.0125$ and $G = 0.0375$. Sim: from numerical simulations; Exp: by measurements.

4.3. Distribution of h along the Radius

According to the results from numerical simulations, the radial distributions of h are plotted in Figure 8. With the decrease of C_w , the amounts of h increase in general at each radial coordinate. For wider axial gap widths, the $h - x$ curves are flatter and the values of h are smaller. Near the centripetal inlet ($x \geq 0.85$), the parameter h is irregularly distributed versus x . The values of h are volatile for $G = 0.0375$. The explanation for this phenomenon is that there is a jet flow near the centripetal inlet. The flow begins to separate when pumped into the front chamber, which significantly impacts the local heat transfer capacity. The values of h drop as x decreases from 0.85 to 0.4. It is believed that when the flow enters the cavity, it is accelerated by the disk resulting in the increase of u_∞ . The increment of u_∞ becomes smaller when x decreases from 0.85 to 0.4, resulting in the flatter $h - x$ curves (see Equation (6)). At the low radius $x < 0.4$ region, when the amounts of K exceed 1, the flow rotates faster than the disk and is decelerated. The values of u_∞ then drop with decreasing x . This appears to result in the increase of h with decreasing x ($x < 0.4$) in most of the results from numerical simulations.

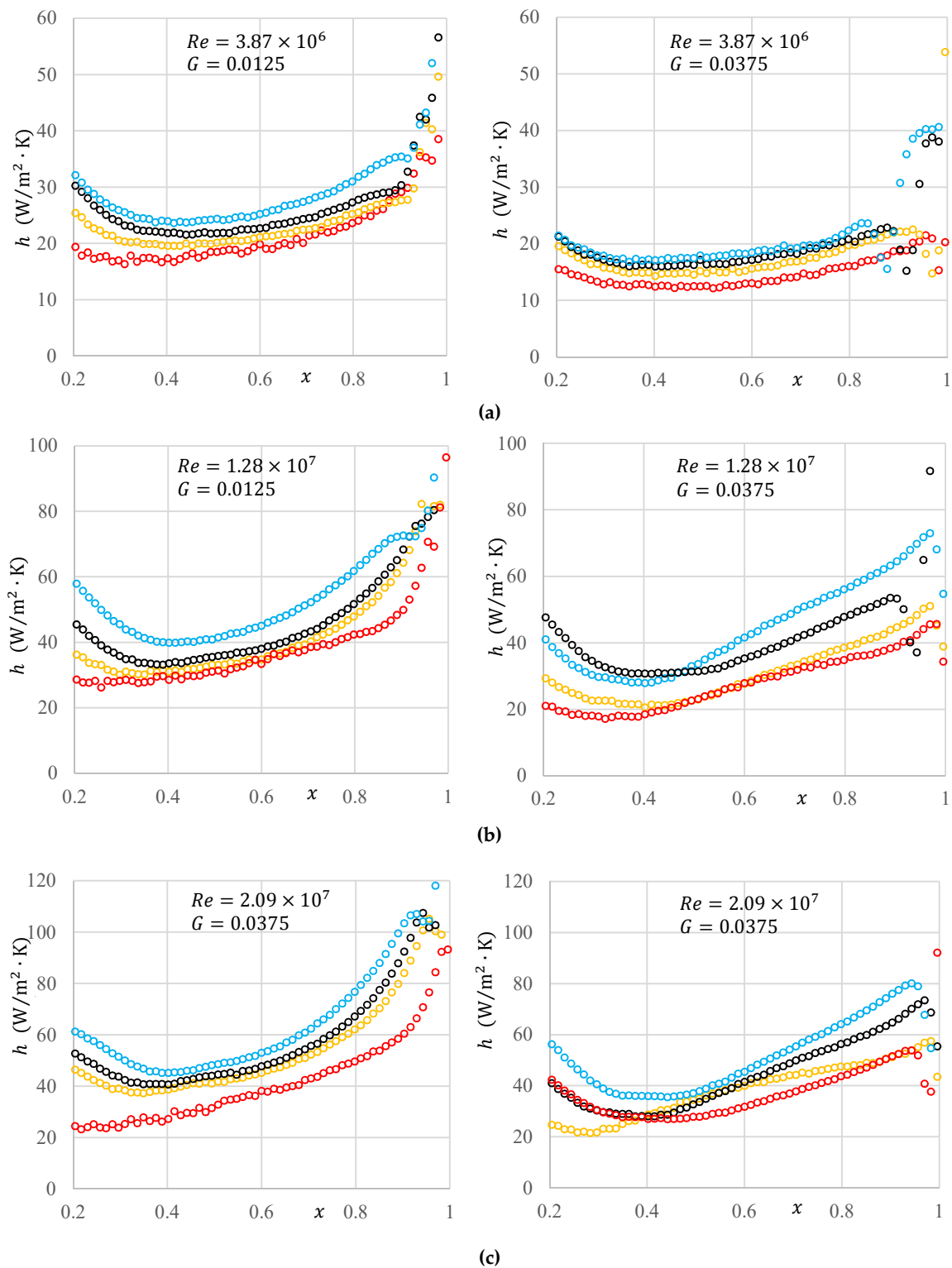


Figure 8. Radial distribution of h from numerical simulations for (a) $Re = 3.87 \times 10^6$; (b) $Re = 1.28 \times 10^7$ and (c) $Re = 2.09 \times 10^7$. x : non-dimensional radial coordinated, $x = \frac{r}{b}$. Color of symbols: red: $C_w = -1262$; orange: $C_w = -2525$; black: $C_w = -3787$; blue: $C_w = -5050$;

4.4. Average Nusselt Number

The parameter λ_t mainly determined the flow pattern inside the cavity, and then the general heat transfer capacities [6]. The values of Nu_{ave} , computed with Equation (7), are plotted versus λ_t in Figure 9a. During the calculation, the parameter k (from Equation (8)) is considered as a fixed value every 1 mm along the radius. The amounts of Nu_{ave} increase with the increase of Re while they drop with increasing λ_t . For smaller axial gap widths, the values of Nu_{ave} are larger. When

$|\lambda_t|$ is not large enough, the parameter $\frac{Nu_{ave}}{Re^{0.8}}$ is mainly affected by λ_t in a rotor-stator system [6,31]. In [31], the values of $|\lambda_t|$ range from 0 to 1.6. In this study, however, the values of $|\lambda_t|$ do not exceed 0.03. The parameter $\frac{Nu_{ave}}{Re^{0.8}}$ is therefore analyzed according to λ_t . It is noted that the exponent value of 0.8 is typical for turbulent boundary layers, as put forward by Schlichting [37]. Aus der Wiesche [38] pointed out that small deviations exist with regard to the exact value of that value in the literature. However, it should be remarked that these deviations are typically of minor importance in comparison with the experimental uncertainty levels occurring in actual systems. As shown in Figure 9b, the values of $\frac{Nu_{ave}}{Re^{0.8}}$ are almost in linear relationships with λ_t for the three values of Re and two values of G . The parameter Re has quite small impacts on $\frac{Nu_{ave}}{Re^{0.8}}$ at a fixed λ_t value. The finding is in accordance with the conclusion by Owen and Rogers [6]. Similar trends can also be found in a rotor-stator cavity with centrifugal through-flow [31]. In Figure 9c, the variations of $\frac{Nu_{ave}}{Re^{0.8}}$ are plotted versus C_M . With the increase of C_M , the values of $\frac{Nu_{ave}}{Re^{0.8}}$ increase in general at a fixed Re value. The results are considered reasonable because the values of Nu_{ave} can be indirectly estimated with the values of C_M [6].

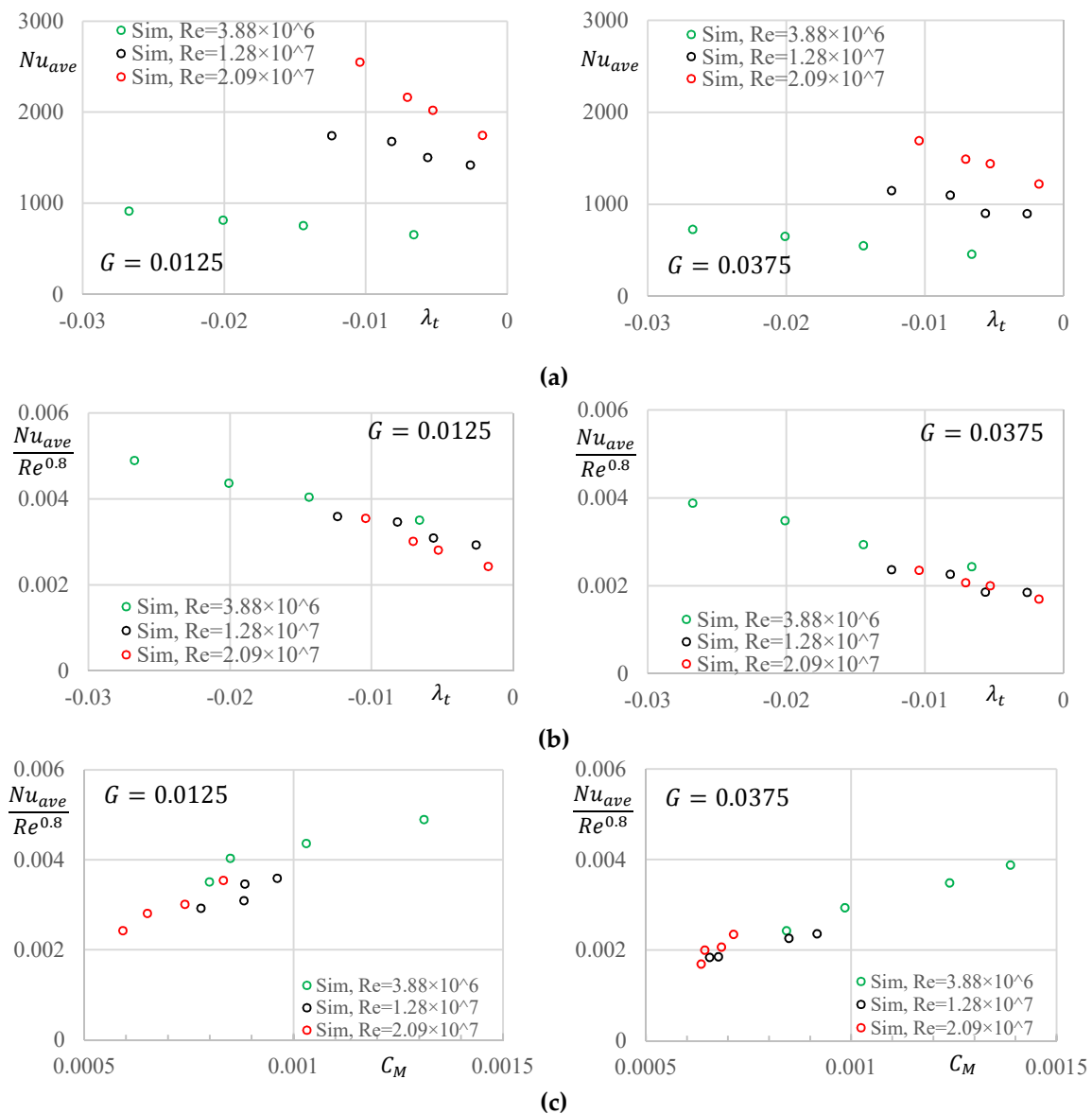


Figure 9. Simulation results of heat transfer capacities: (a) Nu_{ave} versus λ_t ; (b) $\frac{Nu_{ave}}{Re^{0.8}}$ versus λ_t and (c) $\frac{Nu_{ave}}{Re^{0.8}}$ versus C_M .

5. Conclusions

In this paper, the characteristics of flow and heat transfer in a rotor-stator cavity with centripetal carbon dioxide through-flow are investigated using ANSYS CFX 13.0 code. The radial distribution of K and θ are in good agreement with the experimental data, which proves that the numerical simulation set-ups are reasonable. The conclusions are as follows:

Two empirical correlations of K are determined for the two axial gap widths and centripetal carbon dioxide through-flow. The constants in the correlations are obtained by fitting the results from numerical simulations.

The amounts of C_M maintain a decreasing trend with increasing λ_t in general.

The $h-x$ curves are flatter and the values of h are smaller in general for a wider axial gap width of $G = 0.0375$. When x decreases from 0.85 to 0.2, the capacity of local convective heat transfer firstly decreases and then increases under most of the computing conditions. The variations of u_∞ appear to result in this trend.

The amounts of Nu_{ave} increase with the increase of Re while they drop with increasing λ_t . For a smaller axial gap width of $G = 0.0125$, the capacities of average convective heat transfer are much stronger.

The values of $\frac{Nu_{ave}}{Re^{0.8}}$ are almost in linear relationships with λ_t for the three speeds of rotation and two axial gap widths. With the increase of C_M , the values of $\frac{Nu_{ave}}{Re^{0.8}}$ increase in general at a fixed Re value.

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Nomenclature

Latin Symbols

a, a_1	Variable	—
b	Outer radius of the disk	m
C_M	Moment coefficient	$\frac{2 \cdot M }{\rho \cdot \Omega^2 \cdot b^5}$ —
C_{qr}	Local flow rate coefficient	$\frac{Q_t \cdot Re_\phi^{0.2}}{2 \cdot \pi \cdot \Omega \cdot r^3}$ —
C_w	Through-flow coefficient	$\frac{\dot{m}}{\mu \cdot b}$ —
G	Non-dimensional axial gap	$\frac{s}{b}$ —
h	Heat transfer coefficient	$h = \frac{-q}{(T_{aw} - T_w)}$ W/(m ² · K)
h_{ave}	Average heat transfer coefficient	$\frac{\int_{r_c}^b 2hrdr}{b^2 - r_c^2}$ W/(m ² · K)
K	Core swirl ratio	$\frac{\Omega_f}{\Omega}$ —
k	Thermal conductivity	W/(m · K)
l	Specific heat at constant pressure	J/(kg · K)
M	Frictional torque on a single surface	Nm
$\dot{m}$	Mass flow rate	$\rho \cdot Q_t$ kg/s

Nu	Local Nusselt number	$\frac{h \cdot r}{k}$	—
Nu_{ave}	Average Nusselt number	$\frac{\int_{r_c}^b \frac{2hr^2 dr}{k}}{(b^2 - r_c^2)}$	—
n	Speed of rotation		rpm
p	Pressure		Pa
Q_t	Volumetric through-flow rate per second		m ³ /s
q	Wall heat flux		W/m ²
Re	Global circumferential Reynolds number	$\frac{\Omega \cdot b^2}{\nu}$	—
Re_ϕ	Local circumferential Reynolds number	$\frac{\Omega \cdot r^2}{\nu}$	—
r	Radial coordinate		m
r_c	Inner radius where the measurements of h start		m
r_{rec}	Recovery factor		—
r_o	Radius of the outlet pipe		m
Δr	Radial clearance		mm
s	Axial gap of the front chamber		mm
s_b	Axial gap of the back chamber		mm
s_o	Axial width of the inlet		mm
T_∞	Temperature in the main stream at $\zeta = 0.5$		K
T_w	Temperature on the wall		K
t	Thickness of the disk		mm
u_∞	Velocity of the mainstream at $\zeta = 0.5$		m/s
V_t	Non-dimensional tangential velocity	$\frac{v_t}{\Omega \cdot r}$	—
v_t	Tangential velocity		m/s
x	Non-dimensional radial coordinate	$\frac{r}{b}$	—
Greek Symbols			
θ	Non-dimensional temperature	$\frac{T - T_{min}}{T_{max} - T_{min}}$	—
λ_t	Turbulent flow parameter	$\frac{C_w}{Re^{0.8}}$	—
μ	Dynamic viscosity		N · s/m ²
ν	Kinematic viscosity		m ² /s
ρ	Density		kg/m ³
Ω	Angular velocity of the disk		rad/s
Ω_f	Angular velocity of the fluid		rad/s

Abbreviations

FS	Full scale
HWA	Hot-wire anemometry
rpm	Revolution per minute
RMS	Root mean square
SST	Shear stress transport
TLC	Thermochromic liquid crystal

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