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Continuous-Input Continuous-Output Current Buck-Boost DC/DC Converters for Renewable Energy Applications: Modelling and Performance Assessment

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Received: 21 April 2019; Accepted: 27 May 2019; Published: 10 June 2019

Abstract: Stand-alone/grid connected renewable energy systems (RESs) require direct current (DC)/DC converters with continuous-input continuous-output current capabilities as maximum power point tracking (MPPT) converters. The continuous-input current feature minimizes the extracted power ripples while the continuous-output current offers non-pulsating power to the storage batteries/DC-link. CUK, D1 and D2 DC/DC converters are highly competitive candidates for this task especially because they share similar low-component count and functionality. Although these converters are of high resemblance, their performance assessment has not been previously compared. In this paper, a detailed comparison between the previously mentioned converters is carried out as several aspects should be addressed, mainly the converter tracking efficiency, conversion efficiency, inductor loss, system modelling, transient and steady-state performance. First, average model and dynamic analysis of the three converters are derived. Then, D1 and D2 small signal analysis in voltage-fed-mode is originated and compared to that of CUK in order to address the nature of converters' response to small system changes. Finally, the effect of converters' inductance variation on their performance is studied using rigorous simulation and experimental implementation under varying operating conditions. The assessment finally revels that D1 converter achieves the best overall efficiency with minimal inductor value.

Keywords: continuous-input current; continuous-output current; buck-boost; DC/DC converters; renewable energy system; photovoltaic; MPPT; dynamic modelling; and small-signal analysis

1. Introduction

The world's increasing energy consumption, depleting fossil fuels, global warming concerns and environmental problems have greatly increased the interest in clean renewable energy sources recently [1]. Wind energy forms one of the best candidates due to its high power penetration capabilities [2]. Photovoltaic (PV) solar energy has become a promising renewable/alternate energy source due to several advantages such as absence of noise or mechanical moving parts, low operation cost, no emission of CO₂ or other harmful gases, flexibility in size, and its convenience in arid areas [1–3].

The non-linear behavior and dependency of almost all renewable energy sources on the atmospheric conditions create one of the main challenges facing the renewable energy sector's penetration of the energy market [4–5]. To minimize these drawbacks, renewable energy systems

(RESs) operation at the maximum power point is a necessity. Consequently, a switched-mode power electronic converter, called a "maximum power point tracker", must be placed between the RES terminals and the load [6]. Various maximum power point tracking (MPPT) techniques have been developed to maximize the RES extracted power efficiently [7–9]. These converters can be placed in standalone or two-stage grid tied configurations [8–11].

Buck-boost direct current (DC)/DC converters are commonly applied as RES MPPT converters. However, the basic buck-boost converters suffer from discontinuous input current [12,13] resulting in discontinuous RES current, thus deteriorating the MPPT process. To overcome the latter, a large electrolytic capacitor filter buffer is applied at the converter input yet at the penalty of added extra cost, weight, electrical resonance issues and less system reliability [14]. Fortunately, these shortcomings can be eliminated if the conversion input stage draws continuous and controllable input current that allows the RES's maximum power point to be closely tracked, with minimal current/voltage ripple (i.e., power ripple) [15].

A number of continuous-input-current buck-boost DC-DC converters have been developed [15–22] as shown in Table 1. These converters can be extensively used for maximum utilization of RES as wind and PV systems. Quadratic buck-boost converters have the merit of high quadratic gain expanding system voltage levels; however, at the cost of high component count [21,22]. Boost-cascaded and Boost-interleaved buck-boost converters show low switch and diode stress but again at the cost of high component count increasing switching losses and converter cost [15, 16, and 19]. CUK and SEPIC serve as promising buck-boost converters with the merits of continuous-input-current at the least component count [13,15,17,18]. However, SEPIC shows pulsating output current that can be smoothed out using additional output filter which increases system size and losses [20]. Hence, from the non-pulsating input and output current with the least component count perspective, CUK is a good candidate for versatile standalone/grid integrated RES applications with different voltage levels and various loads nature. With similar merits as CUK including component count, D1 and D2 buck-boost converters are introduced in [23], and tested with fixed input DC sources. These DC/DC converters behave as current-sourced converters, which are topological duals of the buck-boost voltage-sourced converters [24].

Converter	V_o/V_i	Component Count				Switches and		
Topology		Switch	Diode	L	С	Diodes Voltage Stress	Merits	Limitations
Quadratic converter [22]	$\left(\frac{D}{1-D}\right)^2$ Positive V_o $D_1 = D_2 =$ D	2	2	2	2	S1: $\frac{1}{1-D}V_i$, S2: $\frac{D}{(1-D)^2}V_i$ d1: $\frac{1}{1-D}V_i$, d2: $\frac{D}{(1-D)^2}V_i$	* High quadratic gain * Positive output voltage	High component count
Single switch Quadratic converter [21]	$\left(\frac{D}{1-D}\right)^2$ Negative V_o	1	5	3	3	S: $\frac{1}{(1-D)^2} V_i$, d1 = d4: $\frac{1}{1-D} V_i$ d2 = d5: $\frac{D}{(1-D)^2} V_i$, d3: $\frac{1}{(1-D)^2} V_i$	* Quadratic gain	* High component count * Inverted voltage
Boost Cascaded converter [15,16,19]	$ \frac{D_2}{1 - D_1} $ Positive $ V_o $	2	2	2	2	S1: V_i , S2: V_i d1: $V_o = \frac{D_2}{1 - D_1} V_i$, d2: V_i	* Less stress on switches and diodes * Positive output voltage	High component count
Boost interleaved converter [16]	$ \begin{array}{c} D_2 \\ + \frac{D_1}{1 - D_1} \\ Positive \\ V_o \end{array} $	2	2	2	2	S1: V_i , S2: V_i d1: V_o , d2: V_i	* Less stress on switches and diodes * Positive output voltage	High component count

 Table 1. Comparison between most recent continuous-input-current buck-boost direct current (DC)/DC converters.

SEPIC converter [15,18]	$\frac{D}{1-D}$ Positive V_o	1	1	2	2	S: $V_i + V_o =$ $\frac{1}{1-D}V_i$ d: $V_i + V_o =$ $\frac{1}{1-D}V_i$	* Low component count * Positive output voltage	Pulsating discontinuous output current
CUK converter [13,15,17]	$\frac{D}{1-D}$ Negative V_o	1	1	2	2	S: $V_i + V_o =$ $\frac{1}{1-D}V_i$ d: $V_i + V_o =$ $\frac{1}{1-D}V_i$	Continuous input/output current at Least component count	Inverted output voltage
D1 converter	$\frac{D}{1-D}$ Negative V_o	1	1	2	2	S: $V_i + V_o =$ $\frac{1}{1-D}V_i$ d: $V_i + V_o =$ $\frac{1}{1-D}V_i$	Continuous input/output current at Least component count	Inverted output voltage
D2 converter	$\frac{D}{1-D}$ Negative V_o	1	1	2	2	S: $V_i + V_o =$ $\frac{1}{1-D}V_i$ d: $V_i + V_o =$ $\frac{1}{1-D}V_i$	Continuous input/output current at Least component count	Inverted output voltage

Although the three converters (CUK, D1 and D2) resemble each other in many aspects (defined in Table 1), they can show differences especially when being applied with RES as maximum power point trackers (MPPTs). Besides experiencing different power conversion efficiencies, they also differ in tracking efficiency. Hereby, not only the converter losses affect the converter overall efficiency but the input current ripples play an important role [25]. The latter affects the tracked RES power ripples, which impact the converter power tracking efficiency. Moreover, system small changes and ripples can affect converters' output voltage; hence it is a point that should be addressed. Finally, the converters' tolerance to inductances variation has significant impact on their performance and should be taken into account. Increasing converter inductances minimizes converter input-current-ripples, thus improving its tracking efficiency, but meanwhile increases converter inductor losses, which downgrades its conversion efficiency.

In order to build a fair comparison among the three converters regarding the previously discussed aspects, this paper originates a detailed modelling and performance analysis of the newly introduced D1 and D2 converters, versus that of CUK, when being applied as RES MPPT converters. Average modelling and dynamic analysis of the three converters are originated to derive a formula for each converter inductor copper losses, mirroring its conversion efficiency and another formula for each converter input current ripples, mirroring its tracking efficiency. Then, small signal analysis is originated for each converter when operated in voltage-fed-mode in order to address each converter response to small system changes. Finally, a sensitivity analysis is carried out to study the effect of converter inductance variation on converter efficiency. The latter is realized by simulation and practical implementation of each converter in a stand-alone PV system, as a RES example, undergoing step-changes in power and repeated for different values of converters' inductances. Results are analyzed to assess conversion efficiency and tracking efficiency of each converter separately then decide the converter with the highest overall efficiency among all cases.

2. Average Circuit Modelling for the Considered Buck-Boost Converters

Modelling of the three considered buck-boost choppers in the inductor continuous current mode (CCM) is presented using the average model as shown in Figure 1. Voltage and current gains are derived for each converter along with dynamic analysis of each converter as follows:



Figure 1. Circuit topology for: (a) CUK; (b) D1; (c) D2 converters.

2.1. CUK Converter

For the CUK converter shown in Figure 1a, the following analysis is carried out; The average capacitor current $I_c = 0$,

$$\therefore -I_{Lo}(DT) + I_{Li}(1-D)T = 0$$

$$\therefore \frac{I_{Li}}{I_{Lo}} = \frac{D}{(1-D)}$$
(1)

2.1.1. Voltage Transfer Function Calculation

The average input current $I_i = I_{L_i}$, while the average output current $I_o = I_{L_o}$, hence;

$$\frac{I_i}{I_o} = \frac{D}{(1-D)} \tag{2}$$

Note that I₀ has an opposite direction.

Average input power P_i = Average output power P_{o_i}

$$\begin{array}{c} \therefore V_i I_i = V_o I_o \\ \vdots \quad \frac{V_o}{V_i} = \frac{I_i}{I_o} = \frac{D}{(1-D)} \end{array} \right\}$$
(3)

Note that V^{*o*} *has an opposite polarity.*

2.1.2. Inductors' Ripple Currents Calculation

When the switch *S* is closed;

$$\begin{aligned} v_{Li} &= L_i \frac{\Delta i_{Li}}{\Delta t} = L_i \frac{\Delta i_{Li}}{DT} = \boldsymbol{V}_i \\ &\therefore \Delta i_{Li} = \frac{\boldsymbol{V}_i \boldsymbol{D} T}{L_i} = \frac{\boldsymbol{V}_i \boldsymbol{D}}{\boldsymbol{f}_{sw} L_i} \end{aligned}$$

$$(4)$$

$$v_{Lo} = v_C - V_o = V_C \pm \Delta v_C - V_o \tag{5}$$

Since, average of inductor voltages = 0

$$\therefore V_C - V_o = V_i \tag{6}$$

Substitute (6) in (5)

$$\therefore v_{Lo} = V_i \pm \Delta v_c \quad , \Delta v_c \ll V_i$$

$$\therefore v_{Lo} = L_o \frac{\Delta i_{Lo}}{\Delta t} = L_o \frac{\Delta i_{Lo}}{DT} \approx V_i$$

$$\therefore \Delta i_{Lo} = \frac{V_i DT}{L_o} = \frac{V_i D}{f_{sw} L_o}$$

$$(7)$$

2.1.3. Input/Output Ripple Currents Calculation

$$\Delta i_{i} = \Delta i_{Li} = \frac{V_{i}DT}{L_{i}}$$

$$\Delta i_{o} = \Delta i_{Lo} = \frac{V_{i}DT}{L_{o}}$$
(8)

2.2. D1 Converter

For D1 converter shown in Figure 1b, the following analysis is carried out; The average capacitor current $I_c = 0$,

$$\therefore \left(I_{Li} - I_{Lo} \right) (DT) + I_{Li} (1 - D)T = 0$$

$$\therefore \left. \frac{I_{Li}}{(I_{Lo} - I_{Li})} = \frac{D}{(1 - D)} \right\}$$

$$(9)$$

2.2.1. Voltage Transfer Function Calculation

The average input current $I_i = I_{Li}$ while the average output current $I_o = I_{Lo} - I_{Li}$, hence

$$\frac{I_i}{I_o} = \frac{D}{(1-D)} \tag{10}$$

Note that *I*⁰ has an opposite direction.

Average input power P_i = Average output power P_{o_i} hence

$$\stackrel{\stackrel{\cdot}{\sim}}{} \frac{V_{i}I_{i}}{V_{i}} = \frac{V_{o}I_{o}}{I_{o}} = \frac{D}{(1-D)}$$

$$(11)$$

Note that V_o has an opposite polarity.

2.2.2. Inductors' Ripple Currents Calculation

When the switch S is closed;

$$v_{Li} = V_i + V_o - v_c = V_i + V_o - (V_c \pm \Delta v_c)$$
(12)

Since average of inductor voltages =0

$$\therefore V_i + V_o - V_c = 0 \tag{13}$$

Substitute (13) in (12)

$$\begin{array}{l} \therefore v_{Li} = \mp \Delta v_{c} \\ \therefore v_{Li} = L_{i} \frac{\Delta i_{Li}}{\Delta t} = L_{i} \frac{\Delta i_{Li}}{DT} = \mp \Delta v_{c} \\ \therefore \Delta i_{Li} = \frac{\mp \Delta v_{c} DT}{L_{i}} = \frac{\mp \Delta v_{c} D}{f_{sw}L_{i}} \end{array}$$

$$(14)$$

Regarding voltage ripples of the output inductor

$$v_{Lo} = \boldsymbol{V}_{\boldsymbol{i}} - v_{Li} \tag{15}$$

From (14);

$$\begin{aligned} v_{Lo} &= \mathbf{V}_{i} \pm \Delta \mathbf{v}_{c} \quad , \Delta \mathbf{v}_{c} \ll \ll \mathbf{V}_{i} \\ \therefore v_{Lo} &= L_{o} \frac{\Delta i_{Lo}}{\Delta t} = L_{o} \frac{\Delta i_{Lo}}{DT} \approx \mathbf{V}_{i} \\ \therefore \Delta i_{Lo} &= \frac{\mathbf{V}_{i} D T}{L_{o}} = \frac{\mathbf{V}_{i} D}{f_{sw} L_{o}} \end{aligned}$$

$$(16)$$

2.2.3. Input/Output Ripple Currents Calculation

$$\Delta i_{i} = \Delta i_{Li} = \frac{\overline{\mp} \Delta v_{c} DT}{L_{i}}$$

$$\Delta i_{o} = \Delta i_{Lo} - \Delta i_{Li} = \frac{V_{i}DT}{L_{o}} - \left(\overline{\mp} \frac{\Delta v_{c} DT}{L_{i}}\right)$$
(17)

2.3. D2 Converter

For the D2 converter shown in Figure 1c, the following analysis is carried out; The average capacitor current $I_c = 0$,

$$\therefore -I_{Lo}(DT) + (I_{LI} - I_{Lo})(1 - D)T = 0 \\ \therefore \frac{I_{Li} - I_{Lo}}{I_{Lo}} = \frac{D}{(1 - D)}$$
(18)

2.3.1. Voltage Transfer Function Calculation

The average input current $I_i = I_{Li} - I_{Lo}$ while the average output current $I_o = I_{Lo}$, hence

$$\frac{I_i}{I_o} = \frac{D}{(1-D)} \tag{19}$$

Note that I₀ has an opposite direction.

Average input power P_i = Average output power P_o , hence

$$\begin{array}{c} \therefore V_i I_i = V_o I_o \\ \gamma_i = \frac{I_i}{I_o} = \frac{D}{(1-D)} \end{array}$$

$$(20)$$

Note that V₀ has an opposite direction.

2.3.2. Inductors' Ripple Currents Calculation

When the switch S is closed;

$$\begin{aligned} v_{Li} &= L_i \frac{\Delta i_{Li}}{\Delta t} = L_i \frac{\Delta i_{Li}}{DT} = \boldsymbol{V}_i \\ &\therefore \Delta i_{Li} = \frac{\boldsymbol{V}_i \boldsymbol{D} T}{L_i} = \frac{\boldsymbol{V}_i \boldsymbol{D}}{\boldsymbol{f}_{sw} L_i} \end{aligned}$$

$$(21)$$

$$v_{Lo} = v_{\mathcal{C}} - V_o - V_i = V_{\mathcal{C}} \pm \Delta v_{\mathcal{C}} - V_o - V_i$$
(22)

Since average of inductor voltages = 0

$$\therefore V_C - V_o - V_i = 0 \tag{23}$$

Substitute (23) in (22)

$$\therefore v_{Lo} = \pm \Delta v_{C}$$

$$\therefore v_{Lo} = L_{o} \frac{\Delta i_{Lo}}{\Delta t} = L_{o} \frac{\Delta i_{Lo}}{DT} = \pm \Delta v_{C}$$

$$\therefore \Delta i_{Lo} = \frac{\pm \Delta v_{C} DT}{L_{o}} = \frac{\pm \Delta v_{C} DT}{f_{sw} L_{o}}$$

$$(24)$$

2.3.3. Input/output Ripple Currents Calculation

$$\Delta i_{i} = \Delta i_{Li} - \Delta i_{Lo} = \frac{V_{i}DT}{L_{i}} - \left(\pm \frac{\Delta v_{c}DT}{L_{o}}\right)$$

$$\Delta i_{o} = \Delta i_{Lo} = \frac{\pm \Delta v_{c}DT}{L_{o}}$$
(25)

In all cases, when S is closed; $i_c = -i_o$

$$\therefore \Delta \nu_{c} = \frac{1}{C} \int_{0}^{DT} -i_{o} dt \approx \frac{-I_{o} DT}{C}$$
(26)

D1, D2 and CUK are common in many aspects, as shown in Table 1, however they differ in efficiency. DC/DC power converter conversion efficiency ($\zeta_{conv.} = \frac{Output power to load}{Input DC power}$) is a dominant aspect to evaluate converter performance. However, for the converters under consideration, the input is commonly a RES in which the converter input voltage and current are controlled to track the maximum power. This results in RES current and voltage ripples and, in turn, extracted power oscillations which affect the converter MPPT performance. Hence, another efficiency aspect rises which can even show more importance than the converter power conversion efficiency. This is the converter tracking efficiency.

Hence, the converter overall efficiency includes both MPPT tracking efficiency and power conversion efficiency. The former $(\zeta_{MPT}-\frac{RES\ tracked\ power}{Available\ maximum\ RES\ power\ at\ same\ conditions})$ decreases with the increase in the extracted RES power oscillations and input converter current ripple, forcing the converter to extract less power. On the other hand, the converter power conversion efficiency ($\zeta_{conv.}=\frac{Output\ power\ to\ load}{RES\ tracked\ power}$) is a measure of the converter ability to transfer the RES tracked power to the load. This efficiency decreases with the increase in converter losses especially in case of large inductances with high copper losses.

Table 2 summarizes the considered converters' performances, derived in this section, regarding efficiency. The input current ripples affect the extracted RES power value which reflects directly in the converter tracking efficiency. While inductor copper losses affect converters' losses which mirror converter power conversion efficiency. Referring to Table 2, CUK shows highest conversion efficiency since it experiences the least inductors' copper losses while D1 shows highest tracking efficiency than CUK

converter **D1** converter

D2

but poorer tracking efficiency than D1. To find out the optimal converter to use, converters' performances will be compared, in simulation and practically, regarding their overall efficiencies;

$$\zeta_{\text{total}} = \underbrace{\text{Output power to load}}_{\text{Available maximum RES power at same conditions}} = \zeta_{\text{MPPT}}, \zeta_{\text{conv}}$$
(27)

Table 2. Aspects considered for converter efficiency assessment. Inductor Losses Indicator $(I_{L_{1}}^{2} + I_{L_{2}}^{2})/I_{1}^{2}$ Input Ripple Current Δi_i [23] $\Delta i_{Li} = \frac{V_i DT}{L_i}$ $\Delta i_{Li} = \frac{\mp \Delta v_c \ DT}{L_i}$ $\frac{1 + \frac{(1-D)^2}{D^2}}{1 + \frac{1}{D^2}} = \frac{1}{D^2}$ CUK

	converter	D^{2} +	D^2	$\frac{\frac{1}{L_i}}{L_i} - \left[\pm \frac{\frac{1}{L_o}}{L_o}\right]$
C 11 C		the Cours	1 1 D	

 $1 (1-D)^2$

3. Small Signal Model for the Considered Buck-Boost Converters in Continuous Current Mode (CCM)

The small signal model of CUK in inductor CCM is derived in using the circuit averaging technique [26,27]. Accordingly, small signal models for D1 and D2 in CCM are originally derived in this paper and their relative control-to-output voltage and input-to-output voltage transfer functions are then computed and compared in voltage-fed-mode as follows.

In order to obtain converters' small signal model, small signal ac terms should be included as follows;

$$D_{tot} = D + \widehat{D}, \ v_i = V_i + \widehat{v}_i, \ v_o = V_o + \widehat{v}_o, \\ i_{Li} = I_{Li} + \widehat{\iota}_{Li}, \ i_{Lo} = I_{Lo} + \widehat{\iota}_{Lo}$$
(28)

 $\Delta i_{Li} - \Delta i_{Lo} =$

V.DT

3.1. CUK Converter

The average diode current (*I*_{*d*}) and the average MOSFET voltage (*V*_{*s*}) are given by:

$$I_{d} = \frac{1}{T} \int_{DT}^{T} (I_{Li} + I_{Lo}) dt = (I_{Li} + I_{Lo})(1 - D)$$

$$V_{S} = \frac{1}{T} \int_{DT}^{T} V_{C} dt = \frac{1}{T} \int_{DT}^{T} (V_{i} + V_{o}) dt = (V_{i} + V_{o})(1 - D)$$

$$(29)$$

To obtain CUK converter small signal model, substitute (28) in (29) and letting D' = 1 - D;

$$\begin{array}{l} I_{d} + \hat{\iota_{d}} = (1 - D_{tot})(i_{Li} + i_{Lo}) \\ = (D' - \hat{d})(I_{Li} + \hat{\iota_{Li}} + I_{Lo} + \hat{\iota_{Lo}}) \\ V_{S} + \hat{v_{S}} = (1 - D_{tot})(v_{i} + v_{o}) \\ = (D' - \hat{d})(V_{i} + \hat{v_{i}} + V_{o} + \hat{v_{o}}) \end{array}$$
(30)

Using the facts that $\frac{V_o}{V_i} = \frac{I_i}{I_o} = \frac{D}{D'}$ and that in CUK $I_{Li} = I_i$ and $I_{Lo} = I_o$, then after manipulations, (31) results;

$$I_{d} + \widehat{\iota_{d}} = I_{Lo} - \frac{I_{Lo}}{D'} \hat{d} + D' \widehat{\iota_{Li}} + D' \widehat{\iota_{Lo}} - \hat{d} \widehat{\iota_{Li}} - \hat{d} \widehat{\iota_{Lo}}$$

$$V_{S} + \widehat{v_{S}} = V_{i} - \frac{V_{i}}{D'} \hat{d} + D' \widehat{v_{i}} + D' \widehat{v_{o}} - \hat{d} \widehat{v_{i}} - \hat{d} \widehat{v_{o}}$$

$$(31)$$

Considering small signal model, only small signal ac components are extracted (average quantities are excluded). Furthermore, high order non-linear ac terms are neglected since $d \ll$

 $D, \hat{v}_i \ll V_i, \hat{\tau}_{Li} \ll I_{Li}, \hat{\tau}_{Lo} \ll I_{Lo}$. Hence, (32) can be obtained and CUK small signal model in CCM is demonstrated in Figure 2a, where $Z_{Li} = R_{Li} + sL_i, Z_{Lo} = R_{Lo} + sL_o, Z_C = \frac{1}{sC}, Z_o = R_o \parallel \frac{1}{sC_o}$



Figure 2. Converters' small signal models in continuous current mode (CCM): (**a**) CUK model; (**b**) D1 model; (**c**) D2 model; (**d**) Bode plot of control-to-output and (**d**) input-to-output transfer functions for the three investigated converters.

$$\widehat{\iota_{d}} = D' \widehat{\iota_{Li}} + D' \widehat{\iota_{Lo}} - \frac{I_{Lo}}{D'} \widehat{d}$$

$$\widehat{v_{S}} = D' \widehat{v_{i}} + D' \widehat{v_{o}} - \frac{V_{i}}{D'} \widehat{d}$$

$$(32)$$

3.1.1. To Get Control-to-Output Transfer Function

Set $\hat{v}_i = 0$, small signal voltage and current of Z_{Li} are given by:

$$\begin{aligned} \widehat{v_{Li}} &= \frac{V_i}{D'} \hat{d} - D' \widehat{v_o} \\ \widehat{\iota_{Li}} &= \frac{\widehat{v_{Li}}}{Z_{Li}} = \frac{V_i}{Z_{Li}D'} \hat{d} - \frac{D'}{Z_{Li}} \widehat{v_o} \end{aligned}$$
(33)

Small signal voltage and current of Z_{Lo} are given by:

$$\begin{aligned}
\widehat{\iota_{Lo}} &= \widehat{\iota_o} = \frac{\widehat{v_o}}{Z_o} \\
\widehat{v_{Lo}} &= Z_{Lo} \widehat{\iota_{Lo}} = \frac{Z_{Lo}}{Z_o} \widehat{v_o}
\end{aligned}$$
(34)

Small signal voltage and current of Z_c are given by:

$$\widehat{\iota_{C}} = \widehat{\iota_{d}} - \widehat{\iota_{Lo}} = D'\widehat{\iota_{Li}} + D'\widehat{\iota_{Lo}} - \frac{I_{Lo}}{D'}\widehat{d} - \widehat{\iota_{Lo}}
= D'\widehat{\iota_{Li}} - D\widehat{\iota_{Lo}} - \frac{I_{o}}{D'}\widehat{d}
\widehat{\upsilon_{C}} = Z_{C}\widehat{\iota_{C}} = Z_{C}D'\widehat{\iota_{Li}} - Z_{C}D\widehat{\iota_{Lo}} - \frac{Z_{C}I_{o}}{D'}\widehat{d}$$
(35)

Applying K.V.L;

$$\widehat{v_C} + \frac{V_i}{D'}\hat{d} - \widehat{v_o} - D'\,\widehat{v_o} - \,\widehat{v_{Lo}} = 0 \tag{36}$$

Substituting (33–35) in (36) and using the facts that $\frac{V_o}{V_i} = \frac{I_i}{I_o} = \frac{D}{D'}$ and $I_o = \frac{V_o}{R_o} = \frac{DV_i}{D'R_o}$, control-to-output transfer function results after some manipulations as shown in (37),

$$\frac{\widehat{v_o}(s)}{\widehat{d}(s)} = \frac{Z_{Li}Z_oV_i(1 + \frac{D'Z_C}{Z_{Li}} - \frac{DZ_C}{D'R_o})}{D'(D'Z_{Li}Z_o + Z_{Li}Z_o + Z_{Li}Z_{Lo} + D'^2Z_CZ_o + DZ_{Li}Z_C)}$$
(37)

3.1.2. To Get Input-to-Output Transfer Function

Set $\hat{d} = 0$, small signal voltage and current of Z_{Li} are given by:

$$\left. \begin{array}{l} \widehat{v_{Li}} = \widehat{v_l} - D' \widehat{v_l} - D' \widehat{v_o} \\ = D \widehat{v_l} - D' \widehat{v_o} \\ \widehat{\iota_{Li}} = \frac{\widehat{v_{Li}}}{Z_{Li}} = \frac{D}{Z_{Li}} \widehat{v_l} - \frac{D'}{Z_{Li}} \widehat{v_o} \end{array} \right\}$$
(38)

Small signal voltage and current of Z_{Lo} are given by:

$$\begin{aligned}
\widehat{\iota_{Lo}} &= \widehat{\iota_o} = \frac{\widehat{v_o}}{Z_o} \\
\widehat{v_{Lo}} &= Z_{Lo} \widehat{\iota_{Lo}} = \frac{Z_{Lo}}{Z_o} \widehat{v_o}
\end{aligned}$$
(39)

Small signal voltage and current of Z_c are given by:

$$\begin{aligned}
\widehat{\iota_{C}} &= \widehat{\iota_{d}} - \widehat{\iota_{Lo}} = D'\widehat{\iota_{Li}} + D'\widehat{\iota_{Lo}} - \widehat{\iota_{Lo}} \\
&= D'\widehat{\iota_{Li}} - D\widehat{\iota_{Lo}} \\
\widehat{\upsilon_{C}} &= Z_{C}\widehat{\iota_{C}} = Z_{C}D'\widehat{\iota_{Li}} - Z_{C}D\widehat{\iota_{Lo}}
\end{aligned}$$
(40)

Applying K.V.L;

$$\widehat{v_c} - D' \, \widehat{v_i} - D' \, \widehat{v_o} - \, \widehat{v_o} - \, \widehat{v_{Lo}} = 0 \tag{41}$$

Substituting (38–40) in (41) and after some manipulations, input-to-output transfer function results as shown in (42);

$$\frac{\widehat{v_o}(s)}{\widehat{v}_l(s)} = \frac{DD'Z_C Z_o - D'Z_{Li} Z_o}{D'Z_{Li} Z_o + Z_{Li} Z_o + Z_{Li} Z_{Lo} + D'^2 Z_C Z_o + DZ_{Li} Z_C}$$
(42)

3.2. D1 Converter

The average diode current (*I*_d) and the average MOSFET voltage (*V*_S) are given by:

$$I_{d} = \frac{1}{T} \int_{DT}^{T} I_{Lo} dt = I_{Lo} (1 - D)$$

$$V_{S} = \frac{1}{T} \int_{DT}^{T} V_{C} dt = \frac{1}{T} \int_{DT}^{T} (V_{i} + V_{o}) dt = (V_{i} + V_{o})(1 - D)$$

$$(43)$$

To obtain D1 converter small signal model, substitute (28) in (43) and letting D' = 1 - D;

$$I_{d} + \widehat{\iota}_{d} = (D' - \widehat{d})(I_{Lo} + \widehat{\iota}_{Lo})$$

$$V_{S} + \widehat{v}_{S} = (D' - \widehat{d})(V_{i} + \widehat{v}_{i} + V_{o} + \widehat{v}_{o})$$

$$(44)$$

Using the facts that $\frac{V_o}{V_i} = \frac{I_i}{I_o} = \frac{D}{D'}$ and after some manipulations, (45) results;

$$I_{d} + \widehat{\iota}_{d} = D'I_{Lo} + D'\widehat{\iota}_{Lo} - I_{Lo}\widehat{d} - \widehat{d}\widehat{\iota}_{Lo}$$

$$V_{S} + \widehat{v}_{S} = V_{i} - \frac{V_{i}}{D'}\widehat{d} + D'\widehat{v}_{i} + D'\widehat{v}_{o} - \widehat{d}\widehat{v}_{i} - \widehat{d}\widehat{v}_{o}$$

$$(45)$$

Considering small signal model, only small signal ac components are extracted (average quantities are excluded). Furthermore, high order nonlinear ac terms are neglected. Hence, (46) can be obtained and D1 small signal model in CCM is demonstrated in Figure 2b:

$$\begin{aligned}
\widehat{\iota_d} &= D' \widehat{\iota_{Lo}} - I_{Lo} d \\
\widehat{v_s} &= D' \widehat{v_i} + D' \ \widehat{v_o} - \frac{V_i}{D'} d
\end{aligned}$$
(46)

3.2.1. To Get Control-to-Output Transfer Function

Set $\hat{v}_i = 0$, small signal voltage and current of Z_{Lo} are given by:

$$\begin{aligned}
\widehat{\iota_{Lo}} &= \widehat{\iota_{Ll}} + \widehat{\iota_o} = \widehat{\iota_{Ll}} + \frac{v_o}{Z_o} \\
\widehat{v_{Lo}} &= Z_{Lo}\widehat{\iota_{Lo}} = Z_{Lo}\widehat{\iota_{Ll}} + \frac{Z_{Lo}}{Z_o}\widehat{v_o}
\end{aligned}$$
(47)

Small signal voltage and current of Z_{Li} are given by:

$$\begin{aligned}
\widehat{v_{Li}} &= \frac{V_i}{D'} \hat{d} - D' \widehat{v_o} - \widehat{v_{Lo}} \\
\widehat{\iota_{Li}} &= \frac{V_i}{Z_{Li}} = \frac{V_i}{Z_{Li}D'} \hat{d} - \frac{D'}{Z_{Li}} \widehat{v_o} - \frac{Z_{Lo}}{Z_{Li}} \widehat{\iota_{Li}} - \frac{Z_{Lo}}{Z_{Li}Z_o} \widehat{v_o} \\
\therefore \ \widehat{\iota_{Li}} &= \frac{V_i}{D'(Z_{Li} + Z_{Lo})} \hat{d} - \frac{(D'Z_o + Z_{Lo})}{Z_o(Z_{Li} + Z_{Lo})} \widehat{v_o}
\end{aligned}$$
(48)

Small signal voltage and current of Z_c are given by:

$$\begin{aligned}
\widehat{\iota}_{C} &= \widehat{\iota}_{d} - \widehat{\iota}_{o} = D' \widehat{\iota}_{Lo} - I_{Lo} \hat{d} - \widehat{\iota}_{o} \\
&= D' (\widehat{\iota}_{Li} + \widehat{\iota}_{o}) - (I_{i} + I_{o}) \hat{d} - \widehat{\iota}_{o} \\
&= D' \widehat{\iota}_{Li} - D \widehat{\iota}_{o} - \frac{I_{o}}{D'} \hat{d} \\
\widehat{\nu}_{C} &= Z_{C} \widehat{\iota}_{C} = Z_{C} D' \widehat{\iota}_{Li} - Z_{C} D \widehat{\iota}_{o} - \frac{Z_{C} I_{o}}{D'} \hat{d}
\end{aligned}$$
(49)

Applying K.V.L;

$$\widehat{v_C} + \frac{V_i}{D'}\hat{d} - \widehat{v_o} - D'\,\widehat{v_o} - \,\widehat{v_{Lo}} = 0 \tag{50}$$

Substituting (47–49) in (50) and using the facts that $\frac{V_o}{V_i} = \frac{I_i}{I_o} = \frac{D}{D'}$ and $I_o = \frac{V_o}{R_o} = \frac{DV_i}{D'R_o}$, control-to-output transfer function results after some manipulations as shown in (51),

$$\frac{\widehat{v_o}(s)}{\widehat{d}(s)} = \frac{V_i Z_o(D' Z_C - Z_{Lo}) - \frac{D V_i Z_C Z_o(Z_{Li} + Z_{Lo})}{D' R_o} + V_i Z_o(Z_{Li} + Z_{Lo})}{D' Z_o(1 + D')(Z_{Li} + Z_{Lo}) + D'(D Z_C + Z_{Lo})(Z_{Li} + Z_{Lo}) + D'(D' Z_C - Z_{Lo})(D' Z_o + Z_{Lo})}$$
(51)

3.2.2. To Get Input-to-Output Transfer Function

Set $\hat{d} = 0$, small signal voltage and current of Z_{Lo} are given by:

$$\widehat{\iota_{Lo}} = \widehat{\iota_{Ll}} + \widehat{\iota_o} = \widehat{\iota_{Ll}} + \frac{\widehat{\nu_o}}{Z_o}
\widehat{\nu_{Lo}} = Z_{Lo}\widehat{\iota_{Lo}} = Z_{Lo}\widehat{\iota_{Ll}} + \frac{Z_{Lo}}{Z_o}\widehat{\nu_o}$$
(52)

Small signal voltage and current of Z_{Li} are given by

$$\begin{aligned}
\widehat{v}_{Li} &= \widehat{v}_{l} - D' \widehat{v}_{l} - D' \widehat{v}_{o} - \widehat{v}_{Lo} \\
&= D \widehat{v}_{l} - D' \widehat{v}_{o} - \widehat{v}_{Lo} \\
\widehat{v}_{Li} &= \frac{D}{Z_{Li}} \widehat{v}_{l} - \frac{D'}{Z_{Li}} \widehat{v}_{o} - \frac{Z_{Lo}}{Z_{Li}} \widehat{v}_{li} - \frac{Z_{Lo}}{Z_{Li}Z_{o}} \widehat{v}_{o} \\
&\therefore \widehat{v}_{Li} &= \frac{D \widehat{v}_{l} - D' \widehat{v}_{o} - \frac{Z_{Lo}}{Z_{o}} \widehat{v}_{o} \\
&\therefore \widehat{v}_{Li} &= \frac{D \widehat{v}_{l} - D' \widehat{v}_{o} - \frac{Z_{Lo}}{Z_{o}} \widehat{v}_{o} \\
&(53)
\end{aligned}$$

Small signal voltage and current of Z_c are given by:

$$\begin{array}{l}
\left\{ \widehat{i}_{C} = \widehat{i}_{d} - \widehat{i}_{o} = D' \widehat{i}_{Lo} - \widehat{i}_{o} \\
= D' \widehat{i}_{Li} + D' \widehat{i}_{o} - \widehat{i}_{o} \\
= D' \widehat{i}_{Li} - D \widehat{i}_{o} \\
\widehat{v}_{C} = Z_{C} \widehat{i}_{C} = Z_{C} D' \widehat{i}_{Li} - Z_{C} D \widehat{i}_{o} \\
\end{array} \right\}$$
(54)

Applying K.V.L;

$$\widehat{v_c} - D' \, \widehat{v_i} - D' \, \widehat{v_o} - \, \widehat{v_o} - \, \widehat{v_{Lo}} = 0 \tag{55}$$

Substituting (52–54) in (55) and after some manipulations, input-to-output transfer function results as shown in (56);

$$\frac{\widehat{\nu_o}(s)}{\widehat{\nu}_l(s)} = \frac{DZ_o(D'Z_C - Z_{Lo}) - D'Z_o(Z_{Li} + Z_{Lo})}{Z_o(1 + D')(Z_{Li} + Z_{Lo}) + (DZ_C + Z_{Lo})(Z_{Li} + Z_{Lo}) + (D'Z_C - Z_{Lo})(D'Z_o + Z_{Lo})}$$
(56)

3.3. D2 Converter

The average diode current (*I*_d) and the average MOSFET voltage (*V*_S) are given by:

$$I_{d} = \frac{1}{T} \int_{DT}^{I} I_{Li} dt = I_{Li}(1 - D)$$

$$V_{S} = \frac{1}{T} \int_{DT}^{T} V_{C} dt = \frac{1}{T} \int_{DT}^{T} (V_{i} + V_{o}) dt = (V_{i} + V_{o})(1 - D)$$
(57)

To obtain D2 converter small signal model, substitute (28) in (57) and letting D'=1-D;

$$I_d + \hat{\iota}_d = (D' - \hat{d})(I_{Li} + \hat{\iota}_{Li})$$

$$V_S + \hat{\nu}_S = (D' - \hat{d})(V_i + \hat{\nu}_i + V_o + \hat{\nu}_o)$$
(58)

Using the facts that $\frac{V_o}{V_i} = \frac{I_i}{I_o} = \frac{D}{D'}$ and after some manipulations, (59) results;

$$I_{d} + \widehat{\iota_{d}} = D'I_{Li} + D'\widehat{\iota_{Li}} - \hat{d}I_{Li} - \hat{d}\widehat{\iota_{Li}}$$

$$V_{S} + \widehat{v_{S}} = V_{i} - \frac{V_{i}}{D'}\hat{d} + D'\widehat{v_{i}} + D'\,\widehat{v_{o}} - \hat{d}\widehat{v_{i}} - \hat{d}\widehat{v_{o}}$$

$$(59)$$

Considering small signal model, only small signal ac components are extracted (average quantities are excluded). Furthermore, high order nonlinear ac terms are neglected. Hence, (60) results and D2 small signal model in CCM is demonstrated in Figure 2c:

$$\left. \begin{aligned} \widehat{\iota_d} &= D' \widehat{\iota_{Li}} - I_{Li} \widehat{d} \\ \widehat{v_S} &= D' \widehat{v_i} + D' \widehat{v_o} - \frac{V_i}{D'} \widehat{d} \end{aligned} \right\}$$
(60)

3.3.1. To Get Control-to-output Transfer Function

Set $\hat{v}_i = 0$, small signal voltage and current of Z_{Li} are given by:

$$\left. \begin{aligned} \widehat{v_{Li}} &= \frac{V_i}{D'} \hat{d} - D' \widehat{v_o} \\ \widehat{\iota_{Li}} &= \frac{\widehat{v_{Li}}}{Z_{Li}} = \frac{V_i}{Z_{Li}D'} \hat{d} - \frac{D'}{Z_{Li}} \widehat{v_o} \end{aligned} \right\}$$
(61)

Small signal voltage and current of Z_{Lo} are given by:

$$\begin{aligned}
\widehat{\iota_{Lo}} &= \widehat{\iota_o} = \frac{\widehat{v_o}}{Z_o} \\
\widehat{v_{Lo}} &= Z_{Lo} \widehat{\iota_{Lo}} = \frac{Z_{Lo}}{Z_o} \widehat{v_o}
\end{aligned}$$
(62)

Small signal voltage and current of Z_c are given by:

$$\begin{aligned}
\widehat{\iota_{C}} &= \widehat{\iota_{d}} - \widehat{\iota_{Lo}} = D'\widehat{\iota_{Li}} - I_{Li}\hat{d} - \widehat{\iota_{Lo}} \\
&= D'\widehat{\iota_{Li}} - (I_{i} + I_{o})\hat{d} - \widehat{\iota_{Lo}} \\
&= D'\widehat{\iota_{Li}} - \widehat{\iota_{Lo}} - \frac{I_{o}}{D'}\hat{d} \\
\widehat{\upsilon_{C}} &= Z_{C}\widehat{\iota_{C}} = Z_{C}D'\widehat{\iota_{Li}} - Z_{C}\widehat{\iota_{Lo}} - \frac{Z_{C}I_{o}}{D'}\hat{d}
\end{aligned}$$
(63)

Applying K.V.L;

$$\widehat{v_c} - \widehat{v_o} - \widehat{v_{Lo}} = 0 \tag{64}$$

Substituting (61–63) in (64) and using the facts that $\frac{V_o}{V_i} = \frac{I_i}{I_o} = \frac{D}{D'}$ and $I_o = \frac{V_o}{R_o} = \frac{DV_i}{D'R_o}$, control-to-output transfer function results after some manipulations as shown in (65);

$$\frac{\widehat{v_o}(s)}{\widehat{d}(s)} = \frac{V_i Z_c Z_o (1 - \frac{D Z_{Li}}{D'^2 R_o})}{Z_{Li} (Z_c + Z_{Lo} + Z_o) + D'^2 Z_c Z_o}$$
(65)

3.3.2. To Get Input-to-Output Transfer Function

Set $\hat{d} = 0$, small signal voltage and current of Z_{Li} are given by:

$$\left. \begin{array}{l} \widehat{v_{Li}} = \widehat{v_i} - D' \widehat{v_i} - D' \widehat{v_o} \\ = D \widehat{v_i} - D' \widehat{v_o} \\ \widehat{v_{Li}} = \frac{\widehat{v_{Li}}}{Z_{Li}} = \frac{D}{Z_{Li}} \widehat{v_i} - \frac{D'}{Z_{Li}} \widehat{v_o} \end{array} \right\}$$
(66)

Small signal voltage and current of Z_{Lo} are given by:

$$\widehat{\iota_{Lo}} = \widehat{\iota_o} = \frac{\widehat{v_o}}{Z_o} \\
\widehat{v_{Lo}} = Z_{Lo} \widehat{\iota_{Lo}} = \frac{Z_{Lo}}{Z_o} \widehat{v_o}$$
(67)

Small signal voltage and current of Z_c are given by:

$$\begin{aligned}
\widehat{\iota}_{C} &= \widehat{\iota}_{d} - \widehat{\iota}_{Lo} = D' \widehat{\iota}_{Li} - \widehat{\iota}_{Lo} \\
\widehat{\nu}_{C} &= Z_{C} \widehat{\iota}_{C} = Z_{C} D' \widehat{\iota}_{Li} - Z_{C} \widehat{\iota}_{Lo}
\end{aligned}$$
(68)

Applying K.V.L;

$$\widehat{v_C} - \widehat{v_l} - \widehat{v_o} - \widehat{v_{Lo}} = 0 \tag{69}$$

Substituting (66–68) in (69) and after some manipulations, input-to-output transfer function results as shown in (70)

$$\frac{\widehat{v_o}(s)}{\widehat{v}_l(s)} = \frac{DD'Z_C Z_o - Z_{Li} Z_o}{Z_{Li}(Z_C + Z_{Lo} + Z_o) + {D'}^2 Z_C Z_o}$$
(70)

For voltage-fed-mode, Bode plots of converters' $\frac{\widehat{v}_0(s)}{\hat{d}(s)}$ and $\frac{\widehat{v}_0(s)}{\widehat{v}_l(s)}$ are shown in Figure 2d.

Regarding the $\frac{\hat{v}_0(s)}{\hat{d}(s)}$ Bode plot, high identical DC gain (50 dB) is achieved for the three converters which proves the capability of all converters to minimize the steady-state error during open-loop operation. Almost identical crossover frequency (frequency at 0 db gain) in both D1 and D2 converters at ω_{cl} , while CUK converter showed slightly higher frequency at ω_{c2} . This indicates the CUK converter's capability of using a controller with higher bandwidth but meanwhile D1 and D2 converters show higher rejection capability to high frequency disturbances. Moreover, the latter showed that the CUK converter has to be operated at switching frequency higher than that of D1 and D2 converters since the converter switching frequency should be at least five times its crossover frequency [28]. A comprehensive view indicates that the choice of 15 KHz switching frequency is sufficient and convenient for all converters. A deep look into each converter phase margin which reflects the level of damping coefficient inherited in the converter [28], the highest phase margin present in D2 converter leads to least oscillations and overshoot peaks in output voltage at operation startup yet at the slowest response. On the other hand, the D1 converter has a moderate phase margin leading to a compromise between output voltage oscillations and rate of response. Finally, the CUK converter shows the smallest phase margin leading to fastest response yet with the highest oscillations.

Regarding $\frac{\hat{v}_0(s)}{\hat{v}_l(s)}$ Bode plot, during low order frequencies, all converters have the same gain value, thus responding similarly to input voltage low frequency ripples and transferring them with the same amplification value to the output voltage in open loop-operation. However, during high frequencies, CUK converter shows slightly narrower bandwidth thus having slightly higher rejection capability to high frequency disturbances in input voltage.

In view of the investigated converters' small signal models in voltage-fed-mode, the converters show identical output voltage response due to system low-order frequency changes and close response due to high-frequency changes. On the other hand, the average model indicated that although the converters resemble in voltage and current gains, they differ in inductor losses and input current ripples. Hence, these are considered the main dominant differences among the investigated converters and have the greatest impact on converters' overall efficiency. Therefore, in the following sections (simulation and practical implementation), the load is considered a constant voltage battery load, to solely focus on the effect of these two factors (RES extracted power ripples and inductances losses) on the investigated converters' efficiency and performance, when being applied as MPPT converters for different inductances values and varying irradiance conditions.

4. Simulation Results

This section investigates the comparison between the considered DC/DC converters' tracking and conversion efficiency using simulation analysis. Hence, the investigated converters must operated as RES MPPT converters. The PV standalone system is considered as an example. The performances of the three considered buck-boost converters are assessed for varying converter inductances' values and varying irradiances as well. Each converter is implemented in a PV stand-alone system supplying a battery load (of 36 V) as shown in Figure 3a. A KD135SX_UPU PV module with the *P-V* and *I-V* curves, shown in Figure 3b, is utilized. A comprehensive current-source based PV model is utilized with a modified incremental conductance MPPT technique applied for its high accuracy and simple implementation [9] with the flowchart shown in Figure 3c.



Figure 3. Considered system for simulation: (**a**) block diagram; (**b**) *I-V* and *P-V* curves of the simulated photovoltaic (PV) panel under different irradiance levels; (**c**) flowchart of the applied modified Inc. Cond. algorithm [9].

Converters are tested when PV undergoes two step-changes in irradiance from 1000 W/m² to 400 W/m² at 0.2 s and from 400 W/m² to 700 W/m² at 0.4 s. This is repeated for three different values of input and output inductances (L_i and L_o) of each converter as follows:

First case; $L_i = L_o = 0.5$ mH for $\Delta i_i = 20\%$ and $\Delta i_o = 40\%$.

Second case; $L_i = L_o = 1$ mH for $\Delta i_i = 10\%$ and $\Delta i_o = 20\%$.

Third case; $L_i = L_o = 5$ mH for $\Delta i_i = 2\%$ and $\Delta i_o = 4\%$.

These inductances are designed according to CUK converter ripple current equation which differs in other converters as they show less ripple input current. Inductance losses are emulated by resistance connected in series to inductor and its value increases with the increase in inductance value. Switches and diodes are considered ideal. For a fair comparison, the three converters are tested for the three inductance cases with link capacitance (*C*) of 25 uF for Δv_c = 12% and switching frequency of 15 kHz.

Simulation results are shown in Figures 4–6 for CUK, D1, and D2 converters respectively. These results are analyzed, as shown in Table 3, for three different values of each converter input and output inductances (L_i and L_o). It is clear that all the converters can successfully track the PV maximum power and transfer it to the load yet with different efficiencies. Increasing the input converter inductances decreases the PV power ripple which increases the average extracted PV power. Meanwhile, the inductance copper losses increase, thus decreasing the power transferred to the load. For CUK converter, its highest overall efficiency is achieved in case of 1 mH inductances. For D2, again its best overall efficiency is achieved at 1 mH while occurs at 0.5 mH in case of D1.

Table 3. Simulation results summary.

			CUK			D1			D2	
L_i	= Lo	1000	400	700	1000	400	700	1000	400	700
		W/m ²	W/m^2	W/m ²	W/m^2	W/m ²				
	Δ <i>I</i> _{PV} (A)	±1	±0.75	±0.9	±0.3	±0.2	±0.4	±1	± 0.75	± 0.85
	Р _{РV} (W)	120.5	40.4	80.5	131.4	47.85	89.85	126.3	41.8	85.5
0.5	ζмррт	89.3%	80.8%	87.3%	97.3%	95.7%	97.45%	93.56%	83.6%	92.7%
mH	Pload (W)	116.5	38.8	77.5	121.2	45.4	84.4	118.85	39.8	81.43
	ζconver	96.7%	96%	96.3%	92.23%	94.87%	93.9%	94.1%	95.2%	95.2%
	ζtotal	86.3%	77.6%	84%	90%	91%	91.5%	88%	79.6%	88.3%
	Δ <i>I</i> _{PV} (A)	±0.75	±0.5	± 0.7	±0.175	±0.15	±0.2	± 0.7	± 0.45	± 0.5
	<i>Р</i> _{РV} (W)	126.5	45	86.2	133.9	49.4	92.3	132	47.87	90.4
1	ζмррт	93.7%	90%	93.5%	99.2%	98.8%	100%	97.8%	95.7%	97.9%
mH	Pload(W)	118.7	43	82	118	45.7	82.6	118.2	44.9	83
	ζconver	93.8%	94.9%	95.1%	88.1%	92.5%	89.5%	89.5%	93.8%	91.8%
	ζtotal	87.9%	85.4%	88.9%	87.5%	91.4%	89.6%	87.5%	89.8%	89.9%
	Δ <i>I</i> _{PV} (A)	±0.5	±0.15	±0.4	±0.6	±0.2	±0.3	± 0.7	±0.2	±0.35
- 5 - mH	Р _{РV} (W)	128	50.3	84.7	122.5	49.2	88	124	50.2	92.1
	ζмррт	94.8%	100%	91.9%	90.7%	98.4%	95.4%	91.85%	100%	99.8%
	Pload(W)	94.3	44.3	67.5	53.5	36.5	51	74	40.4	64.7
	ζconver	73.7%	88.6%	79.7%	43.67%	74.2%	5795	59.7%	80.47%	70.2%
	ζtotal	69.8%	88.6%	73.2%	39.6%	73%	55.3%	54.8%	80.47%	70.1%

As explained before since the input source experiences PV current and power ripples, the converters' conversion efficiency is not the sole aspect to compare between their performance. This is vivid when comparing CUK converter performance to others at low inductances (0.5 and 1 mH). Although CUK converter shows better conversion efficiency, it transfers less power to load since it experiences higher PV power ripples (i.e., less tracking efficiency). Hence, a dominant aspect in evaluating the converters' efficiency is the converter tracking capability to extract maximum PV power with low ripples. Thus a D1 converter with least input PV current ripples shows better overall efficiency and can transfer the highest power to load at least inductance value. However, D1 and D2 performances degrade in the case of high inductances (5 mH) due to their high copper losses. The latter decreases the load power and, meanwhile, affects the converter gain, which is directly related to the converter tracking capability resulting in low tracked PV power.



Figure 4. CUK PV power and average load power for: (a) 0.5 mH; (b) 1 mH; (c) 5 mH.



Figure 5. D1 PV power and average load power for: (a) 0.5 mH; (b) 1 mH; (c) 5 mH.



Figure 6. D2 PV power and average load power for: (a) 0.5 mH; (b) 1 mH; (c) 5 mH.

(c)

In conclusion, when comparing overall efficiencies of all converters in all cases, the highest one is achieved by D1 topology applying smallest input and output inductances (0.5 mH each) which additionally, decreases system size, weight, cost and fastens system response during transients.

For deeper analysis on the converters' efficiencies, Figure 7a focuses on the effect of converters' inductances on tracking, conversion and overall efficiencies at a certain irradiance level (1000 W/m²). It is clear that the tracking efficiency of D1 converter is the highest among all till 1 mH then a considerable drop occurs at 5 mH due to the high inductance losses affecting the D1 converter tracking process. However, CUK converter shows highest conversion efficiency. When combining both efficiencies, it is noticeable that the overall efficiency is greatly affected by the tracking efficiency pattern till 1 mH then it is affected by the conversion efficiency pattern. D1 converter shows highest overall efficiency at 0.5 mH while it is achieved by CUK at 5 mH. At 1 mH almost similar overall efficiency is acquired by all converters. Figure 7b shows the converters' three efficiencies for different irradiances and in turn different power levels at the optimal inductance value (0.5 mH). It is clear that D1 converter shows the highest tracking efficiency while CUK converter acquires the highest conversion efficiency for all power levels. However, differences in conversion efficiency among the three converters are relatively very small when compared to converters' differences in tracking efficiency. Hence, at 0.5 mH, the converters' tracking efficiencies

pattern has dominant effect resulting in converters' overall efficiencies with the same pattern where the D1 converter shows the highest overall efficiency for all power levels.



Figure 7. Tracking, conversion and overall efficiencies of the three investigated converters for: $(\mathbf{a}-\mathbf{c})$ different inductance values at 1000 W/m²; $(\mathbf{d}-\mathbf{f})$ variable irradiance levels at 0.5 mH.

To sum up simulation results, Figure 8 illustrates the load power achieved by the three investigated converters under three irradiance levels and for three inductances values. It is clear that at 1 mH inductances, the three converters achieve almost the same results. However, at 5 mH inductances, the highest load power is achieved by CUK, while at 0.5 mH, it is achieved by D1. Finally, among all cases, highest load power is achieved at 0.5 mH by D1 converter for the three considered irradiances levels.



Figure 8. Converters' load power under different cases.

5. Experimental Results

In order to compare the performance of the considered three converters under sudden changes, a step change in irradiance is created. It is impossible to ensure similar conditions for all the investigated converters with roof-mounted PV panels, as their surrounding environmental conditions are uncontrollable. Thus, a PV module simulator can replace the actual PV panel simulating *I*-*V* and *P*-*V* curves.

A simplified PV simulating circuit is employed, as shown in Figure 9a [9,29]. This circuit emulates the PV source when exposed to sudden step-change in irradiance. It consists of a DC power supply with constant voltage of 30 V and two parallel resistances of 6.667 Ω each to represent *R*_{ss}. When the switch S is on, the two resistances are in parallel and *R*_{ss} is about 3.5 Ω and

this gives a *P*-*V* curve of almost 64.3 W peak power. When S is opened, R_{ss} becomes 6.667 Ω resulting in a step decrease in the current *I* producing a different *P*-*V* curve with reduced peak power level (33.75 W) as shown in Figure 9b. Figure 9c shows the test rig photograph of the considered system.



Figure 9. Experimental setup: (**a**) schematic diagram; (**b**) test rig photography, (**c**) PV emulator *P-V*, *I-V* curves.

Each of the three considered buck-boost converters is implemented and its performance is tested at 15 kHz switching frequency and under step change in power level (from 33.75 W to 64.3 W). This is repeated for three values of converters' input and output inductances (0.7, 1.4, and 2.8 mH).

Li=Lo		CUK	C (C3)	Ε	01	D2		
		Low Power	High Power	Low Power	High Power	Low Power	High Power	
0.7 mH	ζ_{total}	73.8%	82.3%	83.5%	82.9%	78%	79.2%	
1.4 mH	ζ_{total}	75.6%	81.5%	80 %	77%	76.7%	77.4%	
2.8 mH	ζtotal	54.2 %	57.4%	37.3%	37.6%	42.4%	45.7%	

Table 4. Experimental converters' overall efficiencies.

Experimental results of the considered converters are analyzed in all cases, and their tracked PV power and average load power values are computed and compared in Figure 10 while the converters' overall efficiencies are computed in Table 4.

It is clear from Figure 10 that the three converters can successfully track the PV power during sudden changes, and reasonably transfer the tracked power to the load yet with different levels of accuracy and efficiency. A noticeable decrease in load power occurs at 2.8 mH for all converters due to high inductance losses, yet CUK converter shows higher load power in this case for its higher conversion efficiency.



Figure 10. Experimental results analysis: (a) PV power; (b) average load power.

However, among all cases of converters' inductance values, the D1 converter shows the highest PV tracked power and highest load power, during various power levels, at the lowest inductance value (0.7 mH) and in-turn highest overall efficiency, as shown in Table 4. This is related to the D1 converter's inherited feature of minimal PV power ripples and highest tracking efficiency, as shown in Figure 11a, resulting in highest tracked PV power and in turn highest load power as clarified in Figure 11b.

Hence, experimental results verify those of the simulation confirming that the converter tracking efficiency has a dominant effect on the converter's overall efficiency, thus the D1 converter shows highest load power at low size input and output inductances.



Figure 11. Experimental results of CUK, D1 and D2 converters at 0.7 mH: (**a**) PV power; (**b**) average load power.

6. Discussion

In this subsection, three critical issues need to be clarified to avoid readers' confusion.

6.1. Why are the Inductance Values Used in the Simulation Different than those Used in the Experimental *Verification*?

Utilizing the PV emulator is unavoidable and cannot be replaced by a PV panel to ensure consistency of the environmental operating conditions as the main article concern is the performance evaluation of three DC/DC converters.

From the authors' point of view, the experimental setup should in these circumstances specifically utilizes parameters differ than that of the simulation for the following reasons:

- 1. The different range of examined PV power, input and output DC voltage at the converter terminals, input and output current across the examined converter, percentage acceptable ripples in the system currents, etc... are all aspects characterizing the fact that both the simulation and experimental analysis are different and hence mandate the utilization of different converter inductances in the experimental setup in order to ensure the CCM and preserve the same acceptable power and current oscillation level. This is in order to achieve fair counterpart DC/DC converters performance assessment as the main factor in selecting the inductor values to ensure CCM is the percentage current ripples which is not the same as in simulation due to the difference in system aspects as mentioned above. The inductance values are selected just above the minimum value that ensure the CCM operation to avoid the added conduction loss that may be exerted when higher values of inductances are selected as their parasitic resistance is proportional to the inductance values.
- 2. Comparative analysis between counterparts can be enhanced by using system parameters in the simulation that differ from that in the experimental assessment. The simulation assessment examines the investigated converters using certain inductance values and operating condition where a conclusion is deducted from this assessment. The authors perform the experimental analysis with different system parameters to emphasise that the conclusions obtained from the

simulation results are still valid even if the system power, voltage/current level, oscillation percentage change. Consequently, the final conclusions are mainly converters' trend and irrelevant to the selected inductance values. From the authors' point of view, this way of assessment adds elaborated generalization of the obtained results emphasizing on their uniqueness irrespective from the designer selection of the converter inductances.

6.2. Why are the Investigated Converters Examined at 15 kHz, a Relatively Low Switching Frequency?

The authors prefer to perform the converters assessment at this low switching frequency as this reflects the worst case scenario where the converter loss is comparable with the power loss due to the divergence in the tracking efficiency. Hence, from the authors' point of view this range of operations is the most confusing to designer selection as the converters' performance might appear similar if only the conversion efficiency is considered. Hence, adequate assessment incorporating the tracking efficiency is unavoidable.

Technically, the majority of the installed PV systems adopt either central or string converter configuration featuring medium to high power scale converters. These converters by nature utilize low-order switching frequencies (several kHz range) to minimize the massive switching loss that evolve rapidly when the converter switching frequency increases. Hence, the paper focuses its research towards this range of widespread PV converters. The high switching frequency is adopted by low power (up to 300 W) PV converters named AC modules/micro-inverters that acquire a small share in the PV converters' commercial market, hence being less important to address at this stage.

6.3. Does the Photovoltaic (PV) Generator Affect the Interfacing Converter Dynamics?

Voltage-type sources have dominated as an input source for power electronics converters for a long type. The existence of duality implies that there are also current-type sources. The growing application of renewable energy sources such as wind and solar energy has evidently shown that the current-type input sources exist in reality such as a PV generator or the feedback technique used in controlling the power electronics converters in the renewable energy systems changes the power electronic converters to behaving in this way. Recent research on renewable energy systems has indicated that the current-type input sources are very challenging input sources affecting the dynamics of the interfacing converters profoundly. The dual nature of the PV generator (i.e., the constant-current region (CCR) at the voltage less than the maximum-power-point (MPP) voltage, and the constant-voltage region (CVR) at the voltages higher than the MPP voltage) [12] may imply that the PV non-linear nature heavily influence the interfacing converter dynamics as it cannot be considered as a simple DC voltage source.

The PV generator is a highly non-linear input source with two distinct source regions as discussed above. Its low-frequency dynamic output impedance (i.e., incremental resistance) behaves as is characteristic to the named sources as well. At the MPPs, the PV-generator dynamic (i.e., rpv) and static (i.e., Rpv = Vpv/Ipv) resistances are equal [29-31]. The dynamic changes in the PV-generator-interfacing converter are caused by the operating-point-dependent dynamic resistance, which is very high in the CCR, equal to static resistance at the MPP, and rather small in the CVR. The typical dynamic changes are the appearance of extra right-half-plane (RHP) zero in the output control dynamics, when the converter operates in the CCR [32,33], change of damping in resonant circuit along the changes in the operating point [34], and the change of sign of the control-to-output transfer function, when the operating point travels through the MPP [35]. In some cases, the RHP zero can be removed by the design of the converter power stage as explained in [36], but usually the RHP zero will effectively limit the output-side feedback-loop control bandwidth to rather low frequencies [37].

Consequently, a detailed analysis is unavoidable considering the dynamic PV generator model when a closed loop control system is to be designed. This issue needs more attention especially if the utilized converter will be used in two stage grid feeding/grid forming conversion system. The stability aspect mandates deep analysis of the source-converter dynamic modelling to avoid/manipulate RHP zero creation. The authors clarify that the RES–converter interface, specially when the RES exhibits non-linear nature, must be carefully analyzed. The utilization of the PV system in this paper was for illustration purpose only for the newly addresses aspect, the tracking efficiency. Hence, a converter interfacing an RES was unavoidable. But, the stability and controller design aspects related to the interface of PV non-linear model on the converter dynamics is out of scope of the present manuscript.

7. Conclusions

The paper presents a detailed comparison for three continuous-input/continuous-output current DC/DC converters. Dynamic modeling and small signal analysis of two continuous-input continuous-output current buck-boost converters (D1 and D2) are derived and compared to those of a CUK converter when operated in voltage-fed-mode. Although the CUK converter has the least converter losses, D1 converter was found to have the least input current ripples. The latter greatly affects the converter overall efficiency when if applied as RES interfacing converter as it enhances the MPPT process and maximizes the extracted output power. The converters' performances are assessed, using simulation and experimental results, when being applied to a PV stand-alone system, as an example, under varying irradiance for three different values of converters' inductances. Among all cases, the D1 converter transfers the highest power to the load and achieves the most enhanced total efficiency at small size inductances which in turn decreases system weight and cost.

Author Contributions: Conceptualization, Ahmed K. Abdelsalam; Formal analysis, Nahla E. Zakzouk and Ahmed khamis Hassan; Investigation, Nahla E. Zakzouk; Methodology, Nahla E. Zakzouk and Ahmed K. Abdelsalam; Project administration, Barry W. Williams; Supervision, Barry W. Williams; Validation, Ahmed khamis Hassan; Writing – original draft, Nahla E. Zakzouk; Writing – review & editing, Ahmed K. Abdelsalam.

Funding: This research receives no external funding

Conflicts of Interest: The authors declare no conflict of interest



Appendix A



List of Symbols

- Co Converter output capacitor
- *D* Switch duty ratio
- *D'* 1- D
- *f*_{sw} Converter switching frequency
- *ic* Capacitor current
- *ia* Diode current
- *i*^{*i*} Converter input current
- *i*^o Converter input current
- *i*Li Current of converter input inductor
- *iLo* Current of converter output inductor
- *Li* Converter input inductance
- *Lo* Converter output inductance
- Pload Load power
- **P**_{PV} Tracked PV power
- *M* Converter conversion ratio
- *R*^o Converter load resistance

- *RLi* Resistance of converter intput inductor
- **R**_{Lo} Resistance of converter output inductor
- T Converter switching period
- *v*^{*i*} Converter input voltage
- *v*^o Converter output voltage
- vs Switch voltage
- *v*_c Capacitor voltage
- *vLi* Voltage of converter input inductor
- *vLo* Voltage of converter output inductor
- Zc Impedance of converter link capacitor
- ZLi Impedance of converter input inductor
- ZLo Impedance of converter output inductor
- Z_o Converter output impedance
- *X* Average value of the specified quantity
- Δx Ripples of the specified quantity
- \hat{x} Small signal term of the specified quantity

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