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# Analytical Investigation of the Heat-Transfer Limits of a Novel Solar Loop-Heat Pipe Employing a Mini-Channel Evaporator

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**Abstract:** This paper presents an analytical investigation of heat-transfer limits of a novel solar loop-heat pipe developed for space heating and domestic hot water use. In the loop-heat pipe, the condensate liquid returns to the evaporator via small specially designed holes, using a mini-channel evaporator. The study considered the commonly known heat-transfer limits of loop-heat pipes, namely, the viscous, sonic, entrainment, boiling and heat-transfer limits due to the two-phase pressure drop in the loop. The analysis considered the main factors that affect the limits in the mini-channel evaporator: the operating temperature, mini-channel aspect ratio, evaporator length, evaporator inclination angle, evaporator-to-condenser height difference and the dimension of the holes. It was found that the entrainment is the main governing limit of the system operation. With the specified loop design and operational conditions, the solar loop-heat pipe can achieve a heat-transport capacity of 725 W. The analytical model presented in this study can be used to optimise the heat-transfer capacity of the novel solar loop-heat pipe.

**Keywords:** solar loop-heat pipe; mini-channel evaporator; solar collector; heat transfer; limit

## 1. Introduction

Loop-heat pipes (LHPs) are two-phase heat-transfer (evaporation/condensation) devices that are able to transfer large amounts of heat over long distances due to a capillary or gravitational structure [1,2]. The major advantages of LHPs compared to heat pipes (HPs) are an ability to operate against gravity and a higher maximum heat-transport capacity [1]. The maximum heat-transport capacity for an LHP system is governed by different limits, including the viscous, sonic, entrainment, boiling and capillary limits [3]. The minimum value of these limits represents the maximum heat-transport capacity of the LHP system, which is the maximum amount of heat the LHP system could transfer. This maximum heat-transfer capacity represents the most significant performance characteristic of an LHP [3]. Due to the above advantages, LHPs are ideally suitable for use in solar collection systems for hot water and space heating use, which allow heat to be collected by an evaporator outside a building, and transfer it to water flowing across the heat exchanger. Therefore, in recent years, some numerical and experimental studies have been performed to study the heat-transfer limit and thermal performance of conventional LHPs applied to solar collectors [4–7]. Existing solar LHPs are not technically mature; there are still opportunities to enhance their maximum heat-transport capacity and thermal performance [3]. An efficient way to enhance the thermal performance of solar LHPs could be the use of mini-channel heat pipes (MCHPs) in the evaporator.

MCHPs are characterised by a hydraulic diameter range of 0.5 to 5 mm [8]. To our knowledge, this way to improve the thermal performance of solar LHPs has not yet been investigated and reported. However, the use of mini-channels in solar heat pipe collectors has been numerically and experimentally investigated because of their higher thermal performance compared to conventional HPs [9–12]. In order to improve the performance of solar LHP systems, in this study a novel solar LHP system employing a mini-channel heat pipe evaporator is proposed. However, before a thermal performance characterisation of the novel LHP system is conducted, there is a need to assess its maximum heat-transport capacity. Few studies have been performed upon the heat-transfer limits of solar LHPs for the determination of their heat-transfer governing limit and maximum heat-transport capacity [13,14]. The available studies concern solar LHPs that employ conventional wicked evaporator channels with a hydraulic diameter greater than 4 mm. Wang and Zhao [13] showed that, for their solar LHP system (with heat pipe diameter ranges from 4 to 10 mm), the capillary limit was the governing heat-transfer limit for heat pipe diameters above 5.6 mm, while the entrainment limit was the governing limit for diameters below 5.6 mm. Zhang et al. [14] showed that the capillary limit was the main governing limit of their LHP system (with heat pipe diameter ranges from 14 to 22 mm).

In this paper, an analytical investigation of the heat-transfer limits for a novel solar LHP, employing a wickless mini-channel heat pipe evaporator, is realised. Firstly, the novel solar LHP operation and design characteristics are presented. Particularly, a special design for the condensate return path to the mini-channel evaporator is proposed. Secondly, the paper presents a computer model developed to estimate the heat-transfer limits (viscous, sonic, entrainment, boiling and pressure-drop limits) of the LHP system and then its heat-transport capacity. Finally, the paper presents a parametric analysis of the main factors of the mini-channel heat pipe evaporator that can affect the heat-transfer capacity system.

## 2. Methods

### *LHP System Description and Operation*

The loop-heat pipe studied is described in Figure 1. The system is filled with the refrigerant R134a instead of water, which is chemically incompatible with the aluminium mini-channel. In fact, the water interaction with the aluminium can lead to a corrosion reaction without natural inhibition. This corrosion can generate non-condensable gas and then causes the breakage of the internal vacuum, which causes the non-functioning of the heat pipe [15]. The system is composed of the following main elements (Figure 1): the evaporator mini-channel, the condenser (shell and tube heat exchanger), the vapour transportation line (vtl), the liquid transportation line (ltl), the vapour header (vh), the liquid header (lh) and the liquid collector at the bottom of the evaporator. The fluid evaporated in the mini-channel is collected by the vapour header and transferred towards the heat exchanger via the vapour transportation line. After condensation at the heat exchanger, the liquid returns to the water header and enters the evaporator through small holes (Figures 1 and 2). The natural fluid circulation in the loop-heat pipe system is governed by the pressure head between the condenser and the bottom of the evaporator. The solar collector is composed of 20 mini-channel heat pipes. Each mini-channel is composed of 10 ports (Figure 2). The condensed liquid enters into each port via four small holes with 0.75 mm diameter. The holes were placed on one side of each mini-channel port (Figure 2). They do not exist at the opposite side of the wall to avoid blocking the vapour flow because of a higher gravitational effect when the evaporator is inclined.

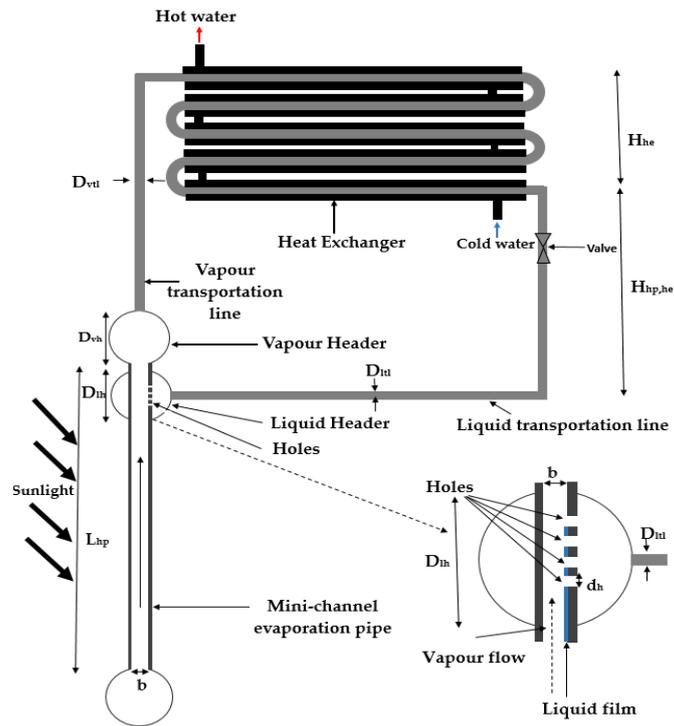


Figure 1. Schematic of the novel solar loop-heat pipe.

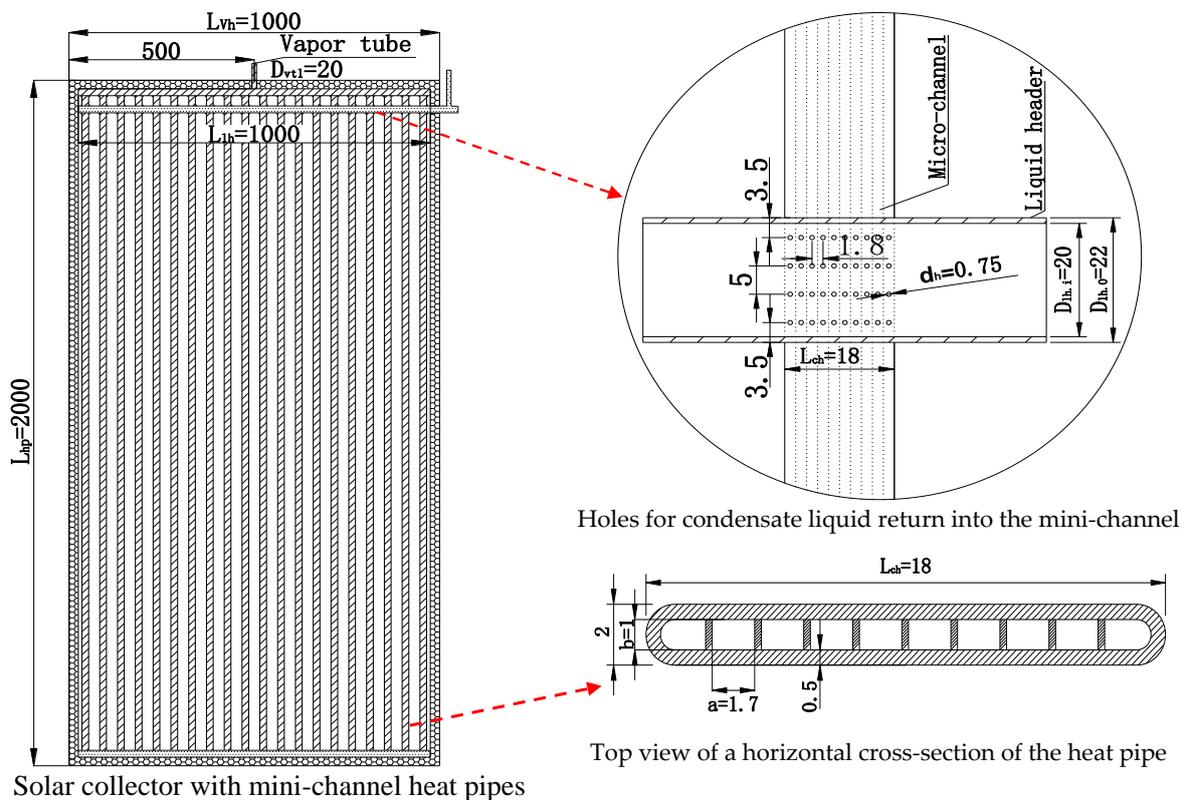


Figure 2. Solar collector with mini-channel heat pipes and condensate liquid pathway (units in mm).

Table 1 summarises the first set of the LHP system components. These values will be used to experimentally study the thermal performance of the system.

**Table 1.** Design parameters of the LHP operation and heat exchanger.

Parameters	Nomenclature	Value	Unit
Mini-channel port width	a	0.0017	m
Mini-channel port height	b	0.001	m
Evaporator length	$L_{hp}$	1.9	m
Number of mini-channel heat pipes	$N_{hp}$	20	-
Number of mini-channel ports	$N_p$	10	-
Total number of mini-channel ports	$N_{ch}$	200	-
Operating temperature range	$t_v$	20–60	°C
Evaporator-to-condenser height difference	$H_{hp-he}$	0.6	m
Transportation line outer diameter	$D_{tl,o}/D_{vtl,o}$	0.015	m
Transportation line inner diameter	$D_{tl,i}/D_{vtl,i}$	0.0174	m
Liquid head length	$L_{lh}$	1	m
Liquid head diameter	$D_{lh}$	0.022	m
Vapour header length	$L_{vh}$	1	m
Hole diameter	$d_h$	0.00075	m
Transportation line length	$L_{tl}/L_{vtl}$	1/1	m
Heat exchanger central tube total length	$L_{he}$	5	m

### 3. Mathematical Equations for Heat-Transfer Limits

Five main heat-transfer limits that affect the system operation are considered, namely, the viscous limit  $Q_{VL}$ , sonic limit  $Q_{SL}$ , entrainment limit  $Q_{EL}$ , boiling limit  $Q_{BL}$  and pressure-drop limit  $Q_{PL}$ . These limits depend on the working fluid, the heat pipe dimensions, and the heat pipe operating temperature  $t_v$ . The minimum value of these limits determines the maximum heat-transfer capacity of the LHP system. These limits are defined as following:

#### 3.1. Viscous Limit $Q_{VL}$

The viscous limit occurs at low operating temperatures, when the viscous forces are larger than the pressure gradients [1]. This results in an insufficient pressure available to drive the vapour, and leads to the evaporator dry-out. The viscous limit at the evaporator can be expressed [16,17]:

$$Q_{VL,e} = \frac{N_{ch} A_v r_v h_{fg} \rho_v P_v}{12 \mu_v L_{hp}}. \quad (1)$$

By considering the liquid thickness in the micro-channel port, the vapour area  $A_v$  can be expressed as the following:

$$A_v = a \times (b - \delta_{lf}), \quad (2)$$

where 'a' is the mini-channel port width, 'b' is the mini-channel port height and  $\delta_{lf}$  is the liquid film thickness. This liquid film is formed by the condensate liquid from the four holes in the mini-channel (Figure 2). According to Imura et al. [18], the average film thickness with a current flow may be approximated to that without one because the average film thickness becomes a little larger. The liquid film thickness  $\delta_{lf}$  can be approximated as follows:

$$\delta_{lf} = \left( \frac{3\mu_l^2}{\rho_l^2 g} \right)^{1/3} Re^{1/3} \text{ for } Re \leq 400, \quad (3)$$

and

$$\delta_{lf} = 0.369 \left( \frac{3\mu_l^2}{\rho_l^2 g} \right)^{1/2} Re^{1/2} \text{ for } Re > 400, \quad (4)$$

where  $Re$  is the Reynolds number,  $\mu_l$  the liquid dynamic viscosity,  $g$  the gravitational acceleration. The Reynolds number is given by:

$$Re = \frac{\rho_l U_1 \delta_{lf}}{\mu_l} \quad (5)$$

$U_1$  is the superficial velocity of the liquid film. Since the liquid flow through the holes of the microchannel depends of the driving force of the LHP, which is the pressure head, it is suitable to link it with the superficial flow. To consider this effect, the superficial velocity is linked to the pressure head by the following equation (it is simply expressed as the liquid flow throughout a hole caused by the pressure head):

$$U_1 = A_h \frac{\left(2g H_{hp-he}\right)^{\frac{1}{2}}}{A_l \left(1 - Cd^2 \left(\frac{d_h}{D_{lh}}\right)\right)}, \quad (6)$$

where  $A_h$  is the hole's section,  $H_{hp-he}$  is the pressure head (height difference between the top of the evaporator and the heat exchanger),  $d_h$  is the hole's diameter and  $D_{lh}$  is the diameter of liquid header. The mass velocity  $U_1$  is assumed the same for the four holes, and then the film thickness is assumed the same along the adjacent wall.  $A_l$  is the liquid film section expressed as following:

$$A_l = a \times \delta_{lf}, \quad (7)$$

where 'a' is the mini-channel port width.  $Cd$  [-], the discharge coefficient of the flow from the liquid head to the hole, is expressed as following [19]:

$$C_d = 0.611 \left[ 87 \left( \frac{\mu_l}{\rho_l d_h \sqrt{g H_{hp,he}}} \right)^{1.43} + \left( 1 + \frac{4.5 \mu_l}{\rho_l D_H \sqrt{g H_{hp,he}}} \right)^{-1.26} \right]^{-0.7}. \quad (8)$$

The liquid thickness is calculated iteratively by assuming that the liquid mass flow from the liquid header is equal to the mass flow of the liquid film. Equation (1) can be applied to the other components of the loop, for example, the vapour transportation line  $Q_{v, vtl}$ , the vapour header  $Q_{v, vh}$  and the heat exchanger  $Q_{v, he}$ . Thus, the minimum among these items would be the viscous limit of the system.

$$Q_{VL} = \min(Q_{VL, vtl}, Q_{VL, vh}, Q_{VL, he}, Q_{VL, e}) \quad (9)$$

### 3.2. Sonic Limit $Q_{SL}$

The sonic limit is due to the fact that at low vapour densities the corresponding vapour flow rate in the heat pipe may result in very high vapour speed, and a choked vapour flow can occur in the vapour passage [1,16]. The sonic limit at the evaporator can be expressed as:

$$Q_{SL,e} = N_{ch} A_v \rho_v h_{fg} \left[ \frac{(\gamma_v R_v T_v)}{2(\gamma_v + 1)} \right]^{\frac{1}{2}}. \quad (10)$$

Equation (10) can be applied to the other components of the loop, for example, the vapour transportation line  $Q_{SL, vtl}$ , the vapour header  $Q_{SL, vh}$  and the heat exchanger  $Q_{SL, he}$ . Thus, the minimum among these items would be the sonic limit of the system.

$$Q_{SL} = \min(Q_{SL, vtl}, Q_{SL, vh}, Q_{SL, he}, Q_{SL, e}) \quad (11)$$

### 3.3. Entrainment Limit $Q_{EL}$

The entrainment limit refers to the case of high shear forces that are developed when the vapour passes over the liquid in the counter-flow direction, and liquid droplets may be entrained with

the vapour towards the condenser. The entrainment limit exists in two parts of the system, in the evaporator and in the condenser. The entrainment limit for a wickless heat pipe can be expressed as follows [17]:

$$Q_{EL, hp} = N_{ch} f_1 f_2 f_3 (A_v) h_{fg} \rho_v^{\frac{1}{2}} [(g(\rho_l - \rho_v)\sigma)]^{\frac{1}{2}}, \quad (12)$$

where  $f_1$  (Figure A1),  $f_2$  and  $f_3$  (Figure A2) are variables given in [16] and presented in Appendix A.

For the heat exchanger, the entrainment limit is given by:

$$Q_{EL, he} = \pi \left( \frac{D_{he,i} - 2\delta_w}{2} \right)^2 h_{fg} \left( \frac{\sigma \rho_v}{D_w} \right)^{0.5}, \quad (13)$$

where  $D_{he,i}$  is the heat-exchanger's internal diameter,  $\delta_w$  is the liquid thickness (Appendix C (A11)) and  $D_w$  is the condensed liquid hydraulic diameter. The smaller of  $Q_{EL, hp}$  and  $Q_{EL, he}$  represents the entrainment limit of the system, as shown:

$$Q_{EL} = \min(Q_{EL, hp}, Q_{EL, he}). \quad (14)$$

### 3.4. Boiling Limit $Q_{BL}$

The boiling limit occurs when the applied evaporator heat flux is sufficient to cause nucleate boiling. This creates vapour bubbles that partially block the liquid return and can lead to evaporator dry-out. The boiling limit can occur at the evaporator and the condenser. The boiling limit for the evaporator can be expressed as follows [20]:

$$Q_{BL, hp} = N_{ch} Ku h_{fg} \rho_v^{\frac{1}{2}} ((g(\rho_l - \rho_v)\sigma))^{\frac{1}{4}}, \quad (15)$$

where

$$Ku = 0.14 \left( 1 - \frac{T_v}{T_c} \right)^{1/5} \left( \rho_l g \frac{b^2}{\sigma} \right)^{\frac{1}{2}} \left( \frac{b}{L_c} \right)^{0.9} \left( 1 + \left( \frac{\rho_v}{\rho_l} \right)^{\frac{1}{4}} \right)^{-2} \times \left( 1 + \left( -0.0125 \frac{T_v}{T_c} + 1.01 \right) \beta \right)^{-2}. \quad (16)$$

The boiling limit for the heat exchanger can be expressed as follows [13,14]:

$$Q_{BL, he} = \frac{2 \pi L_{hx} \lambda_w T_v \left( \frac{2\sigma}{r_b} \right)}{h_{fg} \rho_v \log \left( \frac{D_{he,i}}{D_{he,i} - 2\delta_w} \right)}, \quad (17)$$

where  $\lambda_w$  is the thermal conductivity of the water and  $r_b$  is the critical radius of bubble generation and is assumed to be  $2.54 \times 10^{-7}$  m [14].

The smaller of  $Q_{BL, hp}$  and  $Q_{BL, he}$  represents the boiling limit of the heat pipe system, as shown:

$$Q_{BL} = \min(Q_{BL, hp}, Q_{BL, he}). \quad (18)$$

### 3.5. Pressure-Drop Limit $Q_{PL}$

The heat-transfer limit due to the pressure-drop limit  $Q_{PL}$  is reached when the condensate return level reaches the end of the condenser, and then any further increase of the heat-transfer rate causes the condensate to block part of the condenser, increasing the overall thermal resistance of the heat pipe [21]. The balance of the pressure drop is crucial for the loop operation; the total pressure head  $\Delta P_g$  must be superior to the total pressure drop  $\Delta P_t$  in the loop:

$$\Delta P_g \geq \Delta P_t, \quad (19)$$

where  $\Delta P_t = \Delta P_{vt, v} + \Delta P_{ft, l} + \Delta P_{vh, v} + \Delta P_{lh, l} + \Delta P_e + \Delta P_{cond}$ .

$\Delta P_{vtl,v}$  is the vapour pressure drop in the vapour transportation line and  $\Delta P_{lhl,l}$  is the liquid pressure drop in the liquid transportation lines.  $\Delta P_{vh,v}$  is the pressure drop in the vapour header,  $\Delta P_{lh,l}$  is the pressure drop in the liquid header,  $\Delta P_e$  is the two phase pressure drop in the evaporator and  $\Delta P_{cond}$  (Pa) is the two-phase pressure drop in the condenser. By solving Equation (19), the heat-transfer limit due to the pressure drop  $Q_{PL}$  can be obtained. The items in Equation (19) can be addressed as follows.

*The gravitational pressure  $\Delta P_g$ :*  $\Delta P_g$  is the gravitational pressure caused by the height difference between the top of the heat exchanger and the bottom of the mini-channel evaporator, and can be expressed as [13,14]:

$$\Delta P_g = \rho_l g \left( H_{he}/2 + H_{he,hp} + L_{hp} \sin(\beta) \right), \quad (20)$$

where  $H_{he}$  is the height of the heat exchanger and  $H_{he,hp}$  is the height difference between the outlet of the heat exchanger and the top of the evaporator.  $L_{hp}$  is the evaporator length and  $\beta$  is the evaporator inclination.

*The pressure drop in the evaporator  $\Delta P_e$ :* The two-phase pressure drop in the mini-channel evaporator is expressed as follows [22]:

$$\Delta P_e = \Delta P_{tp,F} + \Delta P_{tp,G} + \Delta P_{tp,A}, \quad (21)$$

where  $\Delta P_{tp,F}$  is the frictional pressure drop,  $\Delta P_{tp,G}$  (Pa) is the gravitational and  $\Delta P_{tp,A}$  (Pa) accelerational pressure drops as given in Appendix B.

*The pressure drops in the vapour transportation line  $\Delta P_{vtl,v}$  and the vapour header  $\Delta P_{vh,v}$ :* The vapour pressure drop in the vapour transportation line and the vapour header could be expressed as [23,24]:

$$\Delta P_{vtl,v} = \left( \frac{C_{vtl}(f_{vtl,v} Re_{vtl,v}) \mu_v}{2\pi(D_{vtl}/2)^4 \rho_v h_{fg}} \right) L_{vtl} Q_{PL}, \quad (22)$$

where  $Q_{PL}$  is the pressure-drop limit, estimated at  $\sim 3.6$ .  $f_{vtl,v}$ , and  $C_{vtl}$  are given in Appendix C (A10).

The vapour pressure drops in the vapour header  $\Delta P_{vh,v}$  can be expressed by Equation (22) similarly.

*Two-phase pressure drop in the condenser  $\Delta P_{cond}$ :* The Muller-Steinhagen and Heck correlation [25] is used to estimate the two-phase pressure drop in the condenser. The correlation is given as:

$$\frac{dP}{dz} = \Lambda (1-x)^{1/3} + \left( \frac{dP}{dz} \right)_{LO} x^3, \quad (23)$$

where  $\Lambda$  and  $\left( \frac{dP}{dz} \right)_{LO}$  are given in Appendix D.

*Total vapour pressure drop  $\Delta P_v$ :* Total vapour pressure drop could be written as follows:

$$\Delta P_v = \Delta P_{e,v} + \Delta P_{vtl,v} + \Delta P_{vh,v} + \Delta P_{he,v}. \quad (24)$$

*Liquid pressure drop in the liquid header  $\Delta P_{lh}$ :* The liquid pressure drop in liquid header can be expressed by the following equation:

$$\Delta P_{lh} = \left( \frac{8 \mu_l}{\pi((D_{lf})/2)^4 \rho_l h_{fg}} \right) L_{lh} Q_{PL}. \quad (25)$$

Liquid pressure drop in the liquid transportation line  $\Delta P_{lhl,l}$  can be expressed by the same form as Equation (25).

### 3.6. Algorithm for the Computer Model

The modelling approach used to calculate the heat-transfer limits of the LHP has been validated experimentally for a mini-channel heat pipe [26], and the mini-channel evaporator model used has

been validated by much experimental data in the literature [22]. The algorithm used to compute the five heat-transfer limits is described as follows. Figure 3 presents the chart of the computer model.

- i. Given the geometry of the solar LHP, technical parameters are presented in Table 1.
- ii. Given a certain operating temperature, the thermodynamic properties of the refrigerant are estimated.
- iii. Calculating the viscous limits at an appropriate region in the operation, and taking the minimum value as the viscous limit by Equations (1) and (9).
- iv. Calculating the sonic limit at an appropriate region in the operation, and taking the minimum value as the sonic limit by Equations (10) and (11).
- v. Calculating the entrainment limits at an appropriate region in the operation, and taking the minimum value as the entrainment limit by Equations (12)–(14).
- vi. Calculating the boiling limits at an appropriate region in the operation, and taking the minimum value as the boiling limit by Equations (15), (17) and (18).
- vii. Running a numerical iteration to calculate the pressure-drop limit.
  - (a) Given the initial value of  $Q_{PL}$ .
  - (b) Gravity pressure is estimated  $\Delta P_g$  by Equation (20).
  - (c) Total pressure drop in the loop is estimated  $\Delta P_t$  by Equation (19).
  - (d) If  $[(\Delta P_g - \Delta P_t)/\Delta P_g] < -0.5\%$  (error allowance), then decrease  $Q_{PL}$  by 10.
  - (e) If  $[(\Delta P_g - \Delta P_t)/\Delta P_g] > 0.5\%$  (error allowance), then increase  $Q_{PL}$  by 10.
  - (f) If  $-0.5\% \leq [(\Delta P_g - \Delta P_t)/\Delta P_g] \leq 0.5\%$  (error allowance), heat balance is achieved and real value of  $Q_{PL}$  can be obtained.
- viii. Taking the minimum value, the five limits as the governing limit of the system operation.
- ix. Program stops.

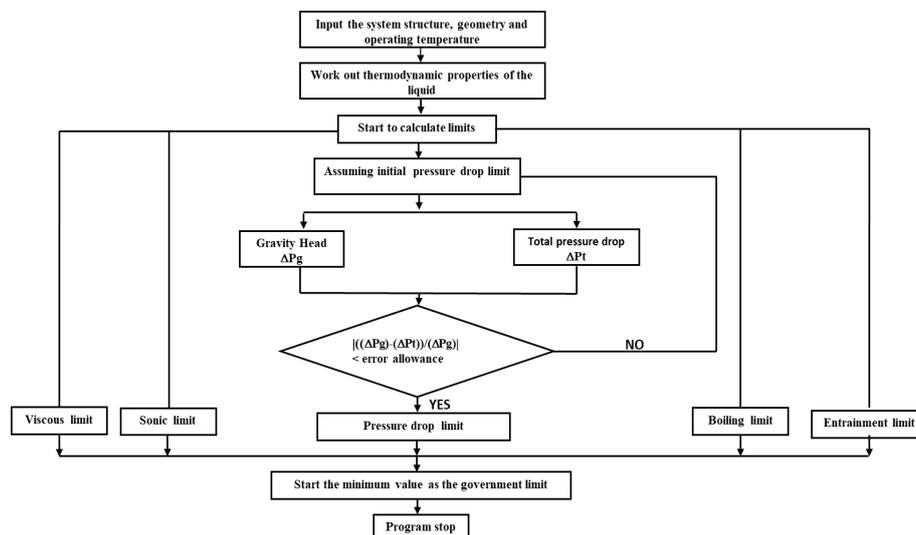


Figure 3. Computer model flow chart.

## 4. Results and Discussion

### 4.1. The Impact of the Operating Temperature of the Mini-Channel Evaporator

By using the computer model, the influence of the operating temperature on the different heat-transfer limits was investigated. Table 2 presents the variation of the five heat-transfer limits

(viscous, sonic, entrainment, boiling and pressure). For each given operating temperature, the governing heat-transfer limit (in bold in the table) is the minimum value of the five heat-transfer limits. At a given operating temperature, this minimum value represents the maximum heat-transport capacity of the system.

**Table 2.** Impact of the operating temperature.

Operating Temperature $t_v$ (°C)	Viscous Limit $Q_{VL}$ (kW)	Sonic Limit $Q_{SL}$ (kW)	Entrainment Limit $Q_{EL}$ (kW)	Boiling Limit $Q_{BL}$ (kW)	Pressure-Drop Limit $Q_{PL}$ (kW)
25	183.00	81.80	0.888	2.89	24.40
30	233.00	91.90	0.885	2.88	22.70
40	350.00	102.00	0.801	2.72	19.70
45	409.00	107.00	0.767	2.62	18.30
50	465.00	110.00	0.725	2.50	17.01
55	515.00	111.00	0.677	2.36	15.01
60	555.00	111.05	0.623	2.19	14.46

Table 2 shows that the viscous and sonic limits ( $Q_{VL}$  and  $Q_{SL}$ ) increase with the operating temperature  $t_v$ ; however, the entrainment limit, the boiling limit and the pressure-drop limit decrease when the temperature is increased. For each operating temperature, the governing heat-transfer limit is the entrainment limit. The viscous limit  $Q_{VL}$  occurs in the vapour transportation line. The viscous limit reflects the difficulty of the vapour flow because of higher viscous forces, and is related to the Reynolds number. When the temperature increases, the Reynolds number, which is related to the working fluid thermodynamic properties, rises. Therefore, the vapour pressure difference becomes larger to overcome the viscous forces, and thus facilitates the vapour flow, and consequently the viscous limit increases. The sonic limit  $Q_{SL}$  also appears in the evaporator. The sonic limit increases with the vapour flow rate. Increasing the operating temperature would cause a smaller vapour density and a higher vapour flow rate. Therefore, the sonic limit of the system would be higher. The sonic limit increases and tends to a limit where any increase in temperature does not affect the vapor speed and tends to be constant. Otherwise, the increased vapour flow, because of the temperature rise, increases the possibility to entrain droplets from the evaporator towards the vapour transportation line, and thus the entrainment limit  $Q_{EL}$  that occurs in the mini-channel evaporator becomes lower. As with the entrainment limit, the boiling limit decreases when there is an increase in the operating temperature, because of the increase of the evaporation rate that can lead to the dry-out. This increased operating temperature increases the total pressure drop in the loop  $\Delta P_t$  because of higher flow velocity, and as a result, the heat-transfer limit  $Q_{PL}$  due to the pressure drop decreases.

#### 4.2. The Impact of the Heat Pipe Aspect Ratio

Table 3 presents the effect of the aspect ratio on heat-transfer limits when the operating temperature  $t_v$  is held at 50 °C and the height from the top of the absorber to the bottom of the condenser  $H_{hp,he}$  is 0.6 m. The aspect ratio ( $b/a$ ) is the ratio of the mini-channel port height 'b' by its width 'a'. Table 3 shows that all the heat-transfer limits increase with the aspect ratio. The increase of the aspect ratio by increasing 'b' on one hand creates higher vapour transporting space  $A_v$  and thus higher evaporation rate, and on the other hand, leads to higher Bond number  $Bo$  (gravitational forces become more important compared to tension forces); as a result, the entrainment of the liquid droplets decreases and consequently the entrainment limit  $Q_{EL}$  increases. Low aspect ratios lead to decreased entrainment limits because the higher vapour flow, the small vapour space and the lower importance of gravitational forces (lower Bond number  $Bo$ ) favour the entrainment of liquid droplets towards the condenser. As the aspect ratio increases, the vapour transportation space and the importance of gravitational forces (higher Bond number  $Bo$ ) increase, enabling more liquid to return along the heat pipe, which causes higher boiling limitation  $Q_{BL}$ . As the vapour space increases, the shear forces decrease and the entrainment decreases slightly, tending to a constant value. Increasing the heat pipe ratio leads to a higher Reynolds number and thus lower viscous forces, and therefore, the LHP viscous

limit  $Q_{VL}$  increases. The increase of the aspect ratio causes lower vapour speed, and as a result, the sonic limit increases. The sonic limit  $Q_{SL}$  first appears at the evaporator; as the vapour spaces increase, the sonic limit appears in the vapour transportation line and becomes constant. The fact that the aspect ratio increases allows more space for the vapour flow and a lower pressure drop, meaning that there is a higher heat-transfer limit  $Q_{PL}$  due to the pressure drop.

**Table 3.** Impact of the aspect ratio.

Aspect Ratio	b (mm)/a (mm)	Viscous Limit $Q_{VL}$ (kW)	Sonic Limit $Q_{SL}$ (kW)	Entrainment Limit $Q_{EL}$ (kW)	Boiling Limit $Q_{BL}$ (kW)	Pressure-Drop Limit $Q_{PL}$ (kW)
0.29	(0.0005/0.0017)	3.52	21.70	0.126	1.16	4.01
0.58	(0.001/0.0017)	465.00	110.00	0.725	2.50	17.01
0.86	(0.0015/0.0017)	2730.00	122.00	1.455	3.88	20.20
1.15	(0.002/0.0017)	8230.00	122.50	2.290	5.29	30.50
1.44	(0.0025/0.0017)	18,400.00	122.50	2.370	6.71	54.40
1.73	(0.003/0.0017)	38,800.00	122.50	2.371	8.14	98.19

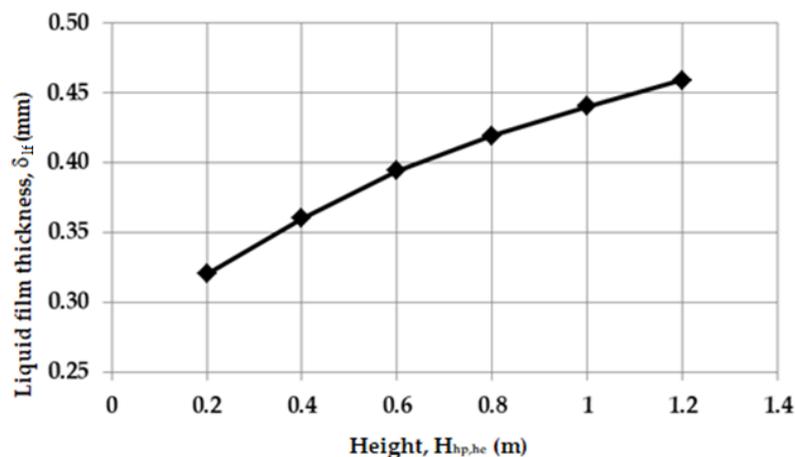
#### 4.3. The Impact of the Condenser-to-Absorber Height Difference

Table 4 presents the effect of condenser-to-absorber height difference  $H_{hp,he}$  (Figure 1) on heat-transfer limits when the operating temperature  $t_v$  is held at 50 °C and the aspect ratio at 0.58 (0.001/0.0017). It shows that the entrainment is the governing heat-transfer limit and it increases with an increase of the condenser-to-absorber height difference. The viscosity and sonic limits decrease with the height difference because of the reduction of the vapour space due the increase of the liquid film thickness  $\delta_{if}$ . Figure 4 presents the evolution of the liquid thickness in function of the height  $H_{hp,he}$ .

The pressure limit remained unchanged because the impact height variation on the pressure drop was not considered.

**Table 4.** Impact of the condenser-to-absorber height difference.

Height $H_{hp,he}$ (m)	Viscous Limit $Q_{VL}$ (kW)	Sonic Limit $Q_{SL}$ (kW)	Entrainment Limit $Q_{EL}$ (kW)	Boiling Limit $Q_{BL}$ (kW)	Pressure-Drop Limit $Q_{PL}$ (kW)
0.20	699.00	122.00	0.831	2.50	17.01
0.40	551.00	117.00	0.768	2.50	17.01
0.60	465.00	110.00	0.725	2.50	17.01
0.80	404.00	105.00	0.692	2.50	17.01
1.00	359.00	101.00	0.665	2.50	17.01
1.20	322.00	97.80	0.642	2.50	17.01



**Figure 4.** Impact of the height  $H_{hp,he}$  on the liquid film thickness  $\delta_{if}$ .

An approximate linear relation is found and the increase of the height difference leads to an increase of the maximum heat-transfer capacity (Figure 5). This effect can be explained by the influence

of gravity. A greater height difference leads to a higher gravitational force, which increases the liquid film thickness  $\delta_{lf}$  in the mini-channel evaporator.

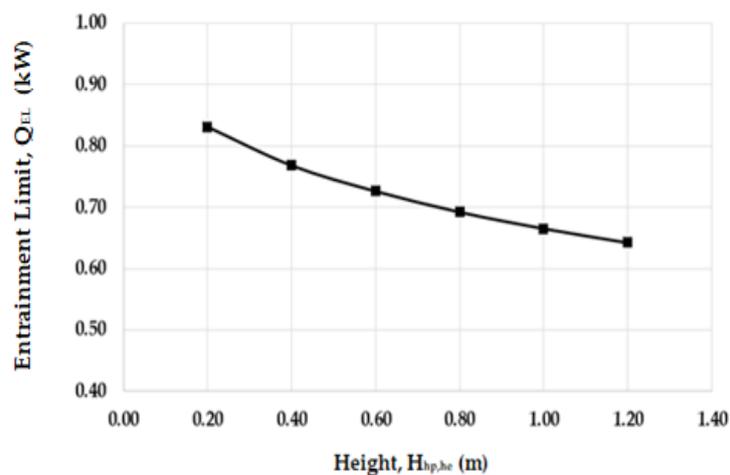


Figure 5. Impact of the height  $H_{hp,he}$  on the entrainment limit.

#### 4.4. Impact of the Individual Hole's Dimension

For the loop-pipe system pipe with a 0.58 aspect ratio, an evaporator-to-condenser height difference  $H_{hp,he}$  of 0.6 m and the operating temperature of 50 °C, the impact of the individual hole's diameter on the heat-transfer limits was investigated. As shown in Table 5, the hole diameter (Figure 2) has an influence on viscous limit, sonic limit and the entrainment limit. Increasing the hole's diameter increases the liquid film thickness in the micro-channel and increased the possibility to entrain the liquid towards the condenser, and so the entrainment limit becomes lower. This increase of liquid film thickness decreases the vapour space and then causes the decrease of the sonic and viscous limits.

Table 5. Impact of the condenser-to-absorber height difference.

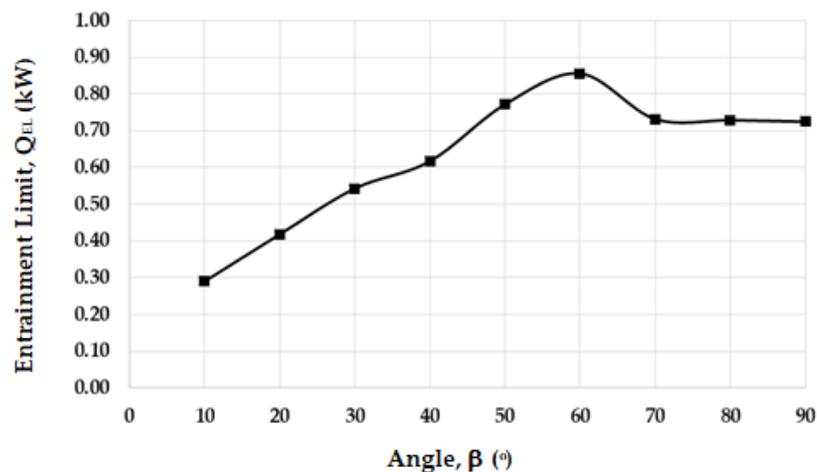
Hole Diameter $d_h$ (mm)	Viscous Limit $Q_{VL}$ (kW)	Sonic Limit $Q_{SL}$ (kW)	Entrainment Limit $Q_{EL}$ (kW)	Boiling Limit $Q_{BL}$ (kW)	Pressure-Drop Limit $Q_{PL}$ (kW)
0.30	1090.00	122.50	0.96	2.50	17.01
0.50	689.00	122.00	0.83	2.50	17.01
0.75	465.00	110.00	0.73	2.50	17.01
1.00	141.00	74.20	0.49	2.50	17.01

#### 4.5. Impact of the Evaporator Inclination Angle

While maintaining an aspect ratio ( $b/a$ ) of 0.58, an operational temperature  $t_v$  of 50 °C, an evaporator length  $L_{hp}$  of 1.9 m, an evaporator-to-condenser height difference  $H_{hp,he}$  at 0.6 m and keeping the other LHP parameters the same, a change of the evaporator inclination angle  $\beta$  would influence the heat-transfer limits of the LHP. Table 6 shows that the entrainment limit is the governing limit, and increases with the evaporator inclination angle, while the other three limits all remain the same except for the boiling limit, which increases and attains a maximum at 60° and then decreases. The entrainment limit increases between 0° to 60°, attains a maximum at 60° and afterwards decreases between 60–90° (Figure 6). The behaviour of this curve reflects the evolution of different parameters  $f_1$  and  $f_3$  of Equation (12) with the Bond number (Appendix A). Equation (12), used to estimate the entrainment limit of the wickless heat pipe (thermosyphon), is empirical, and many experimental studies show that the maximal heat-transport capacity occurs when the wickless heat pipe is at 60–80° to the horizontal, not vertical [17].

**Table 6.** Impact of the evaporator inclination angle.

Angle $\beta$ ( $^{\circ}$ )	Viscous Limit $Q_{VL}$ (kW)	Sonic Limit $Q_{SL}$ (kW)	Entrainment Limit $Q_{EL}$ (kW)	Boiling Limit $Q_{BL}$ (kW)	Pressure-Drop Limit $Q_{PL}$ (kW)
10	465.00	110.00	0.290	146.000	17.01
20	465.00	110.00	0.418	146.000	17.01
30	465.00	110.00	0.543	145.600	17.01
40	465.00	110.00	0.617	127.300	17.01
50	465.00	110.00	0.772	102.400	17.01
60	465.00	110.00	0.856	77.400	17.01
70	465.00	110.00	0.732	52.400	17.01
80	465.00	110.00	0.729	27.400	17.01
90	465.00	110.00	0.725	2.500	17.01

**Figure 6.** Impact of the evaporator inclination angle on the entrainment limit.

A higher inclination angle led to higher hydrostatic force, which improved the system capability in transporting the condensed liquid film flow, and thus led to increased heat flux while the other limits remained constant.

#### 4.6. Impact of the Evaporator Length

While keeping the operational temperature, evaporator diameter, evaporator inclination angle, evaporator-to-condenser height difference and other LHP parameters constant, a change in the evaporator length can influence the heat-transfer limits of the LHP. Table 7 shows that by increasing the evaporator length, the viscous limit decreases while the boiling limit varies in the opposite trend. The viscous limit trend can be explained by the fact that the increase of the heat-pipe length increases the vapour distance, which could reduce the vapour volume flow rate and lead to a lower viscous limit. The sonic limit remains constant while the pressure limit increases slightly with evaporator length because of the pressure-drop decrease. The entrainment limit was found to be the main governing heat-transfer limit. The entrainment limit is constant because there is no interrelation (Equation (12)) between the entrainment limit and the heat-pipe length. Otherwise, the boiling limit became larger as the increased evaporator length led to an increased vapour space in the LHP, evaporation rate of the fluid and operating temperature.

**Table 7.** Impact of the evaporator length.

Evaporator Length $L_{hp}$ (m)	Viscous Limit $Q_{VL}$ (kW)	Sonic Limit $Q_{SL}$ (kW)	Entrainment Limit $Q_{EL}$ (kW)	Boiling Limit $Q_{BL}$ (kW)	Pressure-Drop Limit $Q_{PL}$ (kW)
0.50	1310.00	100.00	0.66	2.19	16.79
1.00	657.00	100.00	0.66	2.34	16.94
1.50	488.00	100.00	0.66	2.44	16.98
1.90	465.00	100.00	0.66	2.50	17.01

## 5. Conclusions

This paper presented a numerical investigation of the heat-transfer limits for a novel solar LHP system using a mini-channel heat-pipe evaporator. Six main limits of the LHP, namely, the entrainment, viscous, boiling, sonic and pressure limits, were considered. The influence of the main mini-channel evaporator parameters (aspect ratio, length, inclination angle), the LHP operating temperature and the condenser-to-absorber height difference on the limits were assessed. The study showed that, for all varied parameters, the entrainment limit was the main governing heat-transfer limit of the novel solar LHP because of higher vapour flow and shear forces in the mini-channel evaporator. With the considered design of the LHP system and operational conditions, the system can achieve a heat-transfer limit of 725 W. Operation of the system with higher operating temperature enables higher heat-transfer capacity of the system. Similarly, the aspect ratio should be relatively larger and the condenser-to-absorber height difference should be low to avoid a higher liquid film thickness that could decrease the maximum heat-transport capacity of the system. The inclination of the mini-channel evaporator should enhance the maximum heat-transfer capacity of the system. The increase of the mini-channel length would lead an increased maximum heat-transfer capacity of the system. Finally, the computer model presented in this study can be used to optimise the heat-transfer capacity of the novel solar LHP.

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**Author Contributions:** Xudong Zhao conceived and proposed the research; Thierno M. O. Diallo, Min Yu, Jinzhi Zhou and Xudong Zhao participated to the novel Solar LHP system conception and design; Thierno M. O. Diallo, Min Yu, Jinzhi Zhou, Xudong Zhao and Jie Ji, conducted the numerical model development, simulations analysis and participated to write the paper; David hardy participated to the system analysis and the paper writing.

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## Nomenclature

A	cross-section	$[m^2]$
a	mini-channel width	$[m]$
b	mini-channel height	$[m]$
Bo	Bond number	$[-]$
Cd	discharge coefficient	$[-]$
D	diameter	$[m]$
$D_h$	hydraulic diameter	$[m]$
f	Fanning friction factor	$[-]$
$f_1$	factor 1	$[-]$
$f_2$	factor 2	$[-]$
$f_3$	factor 3	$[-]$

g	gravitational acceleration	9.81 [m/s <sup>2</sup> ]
G	mass velocity	[kg/m <sup>2</sup> /s]
H	height	[m]
h <sub>fg</sub>	latent heat of vaporisation	[J/kg]
L	length	[m]
M	Mach number	[-]
N	number	[-]
N <sub>ch</sub>	number channel ports	[-]
P	pressure	[Pa]
ΔP	pressure drop	[Pa]
Q	heat-transfer limit	[W]
r <sub>b</sub>	critical radius of bubble generation	[m]
R	specific gas constant	[J/(kg K)]
Re	Reynolds number	[-]
t/T	temperature	[°C/°K]
U	superficial velocity	[m/s]
v	velocity	[m/s]
x	vapour quality	[-]

### Subscripts

A	accelerational
BL	boiling limit
ch	channel
cond	condenser
F	frictional
e	evaporator
EL	entrainment limit
f	fluid
F	frictional
fg	fluid gas
g	gravity
G	gravitational
h	hole
he	heat exchanger
hp	heat pipe
hp-he	heat-pipe-to-heat-exchanger
i	inner
k	liquid or vapour
lf	liquid film
lh	liquid header
LO	liquid only
l <sub>tl</sub>	liquid transportation line
l	liquid
o	outer
p	ports
PL	pressure limit
SL	sonic limit
t	total

tp	two-phase
v	vapour
vh	vapour header
VL	viscosity limit
VO	vapour only
vtl	vapour transportation line
w	water

### Greek Symbols

$\alpha$	void fraction	
$\beta$	inclination angle	[°]
$\Delta$	difference	
$\gamma$	ratio of specific heat	
$\lambda$	thermal conductivity	[W/(m·K)]
$\mu$	dynamic viscosity	[Pa·s]
$\rho$	density	[kg/m <sup>3</sup> ]
$\delta$	liquid film thickness	[m]
$\sigma$	surface tension	[N/m]
$v$	specific volume	[m <sup>3</sup> /kg]

### Appendix A

The factor  $f_1$  depends on the Bond number and can be obtained by the following curve:

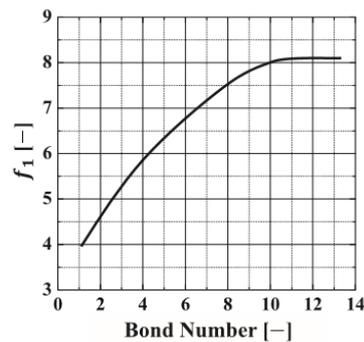


Figure A1. Variation of factor  $f_1$  with the Bond number [27,28].

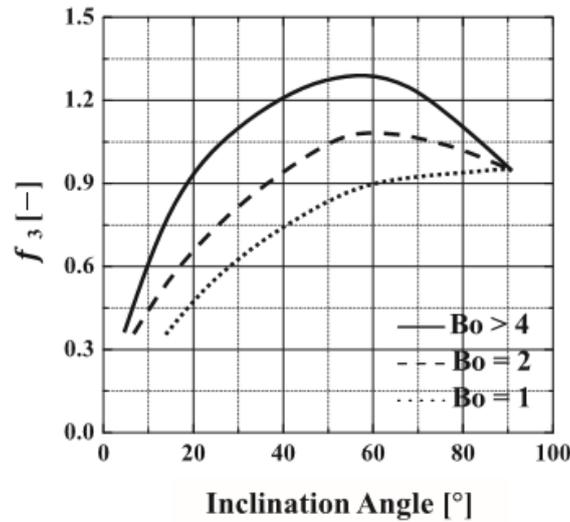
The factor  $f_2$  is function of the dimensionless parameter  $K_p$  obtained with the following equation [16]:

$$f_2 = K_p^{-0.17} \text{ when } K_p \leq 4 \times 10^4 \text{ and } f_2 = K_p^{-0.17} \text{ when } K_p > 4 \times 10^4, \quad (\text{A1})$$

where

$$K_p = \frac{P_v}{g (\rho_l - \rho_v) \sigma^{0.5}}. \quad (\text{A2})$$

The factor  $f_3$  is a function of the inclination angle of the wickless heat pipe and the Bond number:



**Figure A2.** Variation of factor  $f_3$  with the inclination angle  $\beta$  and the Bond number [27,28].

The Bond number for the mini-channel port can be expressed as follows:

$$Bo = \frac{g (\rho_l - \rho_v) b^2}{\sigma}. \quad (A3)$$

## Appendix B

The accelerational pressure gradient is expressed as follows:

$$-\left(\frac{dP}{dz}\right)_A = G^2 \frac{d}{dz} \left[ \frac{v_v x^2}{\alpha} + \frac{v_l (1-x)^2}{(1-\alpha)} \right], \quad (A4)$$

where:  $\alpha$  (-) is the void fraction,  $v_v$  is the vapour specific volume,  $v_l$  is the liquid specific volume,  $x$  [-] vapour quality,  $G$  is the mass velocity, and

$$\alpha = \left[ 1 + \left( \frac{1-x}{x} \right) \left( \frac{\rho_v}{\rho_l} \right) \right]^{-1}. \quad (A5)$$

The gravitational pressure gradient:

$$-\left(\frac{dP}{dz}\right)_G = [\alpha \rho_v + (1-\alpha) \rho_l] g \sin(\beta), \quad (A6)$$

where  $\beta$  is the channel inclination angle,  $\rho_g$  is the gas density,  $\rho_l$  is the liquid density. The frictional pressure gradient is given by:

$$-\left(\frac{dP}{dz}\right)_F = \frac{2f_{tp} v_l G^2}{D_h} \left( 1 + x \frac{v_{fg}}{v_l} \right), \quad (A7)$$

where  $f_{tp}$  is the two-phase frictional coefficient,  $f_{tp} = 16 \text{Re}_{tp}^{-1}$  for  $\text{Re}_{tp} < 2000$ ;  $f_{tp} = 0.079 \text{Re}_{tp}^{-0.25}$  for  $2000 \leq \text{Re}_{tp} < 20,000$ ;  $f_{tp} = 0.046 \text{Re}_{tp}^{-0.2}$  for  $\text{Re}_{tp} \geq 20,000$ .  $\text{Re}_{tp}$  is the two-phase Reynolds number. The two-phase pressure drop is given by:

$$\Delta P_e = \int_0^{L_e} \left[ -\left(\frac{dP}{dz}\right)_F - \left(\frac{dP}{dz}\right)_G - \left(\frac{dP}{dz}\right)_A \right] dz. \quad (A8)$$

## Appendix C

$$\text{Re}_{v,vtl} = \frac{4 Q_{PL}}{\pi \mu_v h_{fg} D_{v,vtl}} M_{v,vtl} = \frac{4 Q_{PL}}{\pi D_{v,vtl}^2 \rho_v h_{fg} (R_v t_v \gamma_v)^{0.5}} \quad (A9)$$

$C_{v,vtl}$  and  $f_{v,vtl}$  with different conditions as follows:

If  $\text{Re}_{v,vtl} \leq 2300$  and  $M_{v,vtl} \leq 0.2$ ,  $(f_{v,vtl} \text{Re}_{v,vtl}) = 16$ ,  $C_{v,vtl} = 1$ .

If  $Re_{v,vtl} \leq 2300$  and  $M_{v,vtl} > 0.2$ ,  $(f_{v,vtl} Re_{v,vtl}) = 0.038$ ,  $C_{v,vtl} = \left(1 + \left(\frac{\gamma_v - 1}{2}\right) M_{vtl,v}^2\right)^{-0.5}$ .  
 If  $Re_{v,vtl} > 2300$  and  $M_{v,vtl} \leq 0.2$ ,  $(f_{v,vtl} Re_{v,vtl}) = 0.038$ ,  $C_{v,vtl} = Re_{vtl,v}^{0.75}$ .  
 If  $Re_{v,vtl} > 2300$  and  $M_{v,vtl} \leq 0.2$ ,

$$(f_{v,vtl} Re_{v,vtl}) = 0.038, C_{v,vtl} = \left(1 + \left(\frac{\gamma_v - 1}{2}\right) M_{vtl,v}^2\right)^{0.5} Re_{v,vtl}^{0.75}. \quad (A10)$$

$$\delta_w = \frac{0.93 (v_1 \mu_1)^{2/3}}{\sigma_1^{1/6} (\rho_1 g)^{0.5}} \quad (A11)$$

## Appendix D

The term  $\Lambda$  is a combination of the liquid- and vapour-phase pressure gradients and is given as:

$$\Lambda = \left(\frac{dP}{dz}\right)_{LO} + 2 \left[ \left(\frac{dp}{dz}\right)_{VO} - \left(\frac{dp}{dz}\right)_{LO} \right] x, \quad (A12)$$

where  $\left(\frac{dP}{dz}\right)_{LO} = -f_{LO} \frac{2 G_{he}^2}{D \rho_1}$  and  $\left(\frac{dp}{dz}\right)_{VO} = -f_{VO} \frac{2 G_{he}^2}{D \rho_g}$ .

The friction factors are given by the following relation:

$$f = 0.079 Re_D^{-0.25} \quad (A13)$$

where the Reynolds number is defined using the total mass flux and the liquid or vapour viscosity, as appropriate.

$$Re_D = \frac{GD}{\mu_k} \quad (A14)$$

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