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# Tracking Control with Zero Phase-Difference for Linear Switched Reluctance Machines Network

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Abstract: This paper discusses the control of the linear switched reluctance machines (LSRMs) network for the zero phase-difference tracking to a sinusoidal reference. The dynamics of each LSRM is derived by online system identification and modeled as a second-order linear system. Accordingly, based on the coupled harmonic oscillators synchronization manner, a distributed control strategy is proposed to synchronize each LSRM state to a virtual LSRM node representing the external sinusoidal reference for tracking it with zero phase-difference. Subsequently, a simulation scenario and an experimental platform with the identical parameter setup are designed to investigate the tracking performance of the LSRMs network constructed by the proposed distributed control strategy. Finally, the simulation and experimental results verify the effectiveness of the proposed LSRMs network controller, and also prove that the coupled harmonic oscillators synchronization method can improve the synchronization tracking performance and precision.

**Keywords:** linear switched reluctance machine (LSRM); coordinated network; distributed control; synchronization tracking

# 1. Introduction

Linear tracking control systems based on direct drive linear machines are vastly used in the manufacturing industry, such as parts assembly, printed circuit boarding (PCB) drilling and chip processing, etc. In addition, there are many tasks that require a cooperation of many linear machines to work harmonically. For example, in a multi-station PCB drilling machine, each linear machine acts as one working unit. The board being processed requires the linear machines to track the command position precisely and coordinates with each other to finish the whole drilling work. Therefore, each linear machine often demands the state information from other machines, so as to work cooperatively and synchronously. The overall motion control performance can be improved such as faster operation time, more efficiency and the annihilation of accumulated errors, etc., compared to a traditional sequenced working manner [1]. Furthermore, if multiple linear machines can be organized as a coordinated and distributed motion tracking network and each machine has the position controller, sensor and driver of its own, the ultimate global tracking control goal can be emerged by local communications among the independent linear machine nodes with local controllers, without the necessity of any global supervision or decision [2].

Among different types of linear machines, a linear switched reluctance motor (LSRM) has the advantages of a simple and robust mechanical structure, low cost, high reliability and free of frequent maintenance or adjustments [3]. Current motion tracking research on LSRMs mainly focuses on

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the control performance improvement for single machine based position control systems [4–7]. In [4], an adaptive position controller is inspected to compensate uncertain behaviors of a double-sided LSRM. A nonlinear proportional differential (PD) tracking controller based on the tracking differentiator is proposed for a real-time LSRM suspension system, to achieve a better dynamic position response [5]. A sliding mode position control technique is investigated in [6] and a passivity-based control algorithm is proposed for the LSRM position tracking system to overcome the inherent nonlinear characteristics and ameliorate system robustness against uncertainties and bounded disturbances [7]. From the latest development on the tracking control performance of LSRMs, the ratio of an absolute dynamic tracking error to full range of 5% can be achieved in single LSRM position control applications.

As mentioned above, by employing a multi-agent network formed by distributed control on the same product line, all LSRMs can be coordinated to work together harmonically. Up until now, the experiment and technique studies on the tracking control network based on LSRMs have gained much attention, and related research is increasing [8,9]. Current analysis of motion coordinated control of multi-agent networks mainly focuses on distributed control methods with multi-agent networks [10–16], which provides a guidance to the LSRMs network. Reference [10] primarily investigated the consensus for coordinated control of multi-agent networks, and established the connections between structural properties and the performance of networks. Cao et al. [11] elaborated the main results and the progress about coordinated control algorithms for multi-agent networks and summarized the future directions of the distributed coordination of multi-agent. At present, multi-agent network study has been classified into several major aspects, which include constrained or imperfect communication [12], delay or switching information linkage [13,14], agents with nonlinear dynamics [15], influence of noise [16], etc., Furthermore, the multi-agent networks bound by distributed control algorithms have been exploited in the regime of spacecraft cluster [17], robot coordination [18], and unmanned aerial vehicle formation [19].

It can be concluded from the above analysis that current theoretical work mainly concentrates on distributed control methods to achieve the network synchronization under some network topology constraint condition. The ultimate goal is to form a stable synchronized motion among the multiple agents within the network employing distributed and networked control algorithms. However, in most industry processes, multiple LSRMs composing a multi-agent network are not only required for motion synchronization but also to track some specific desired trajectory [20]. In practice, directly controlling every agent in a multi-agent network with a number of agents might be impossible or unnecessary. Therefore, pinning control is regarded as a desirable method [21]. Accordingly, the multi-agent network formed by the pinning control is defined as the leader-following network [2]. In a leader-following network, a reference can be accessed directly by minority agents named as leaders only, and then the rest of the agents named as followers are steered to implement the synchronized motion to the common reference by the effect of the distributed control. Wang et al. [22] elaborately reviewed advances in pinning control approaches, including the feasibility, stability and effectiveness of pinning control and pinning-based consensus and flocking control of mobile multi-agent networked systems. One of the challenges with a leader-following network is that the reference possesses different dynamic characteristics from all agents. Cao et al. [23] proposed a distributed consensus tracking algorithm for second-order dynamics guarantees global exponential tracking without acceleration measurements, and the dynamic reference was modeled as the virtual leader with time-varying velocity. Especially, in industrial processes, for implementing much of repetitive work, some periodic motion modes such as sinusoid always were as the desired motion. Wang et al. [24] proposed an internal model controller compensating the reference dynamics for output synchronization of more general heterogeneous multi-agents systems. Wieland et al. [25] proved that an internal model principle is necessary and sufficient for exponential synchronizability of the group to some common, non-trivial output trajectory, bounded by a polynomial function in time, and also note that the internal model components may give rise to the instability of the multi-agent network under the influence of parametric uncertainties.

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In this paper, the mathematical model of each LSRM is derived by the online system identification, which is essentially modeled as a general second-order linear system. Second, inspired by coupled harmonic oscillators [26,27], a distributed control is designed to track a sinusoidal reference with zero phase-difference among each LSRM and the reference as virtual node, so as to improve the tracking performance of the LSRMs network. Last, simulation and experimental verification is provided to prove the effectiveness of the network controller design scheme.

The main contributions of this paper are threefold. First, for the convenience of the coordinated motion control, the reference signal is modeled as a virtual LSRM node that has the same dynamic characteristics as three motor nodes based on the proposed distributed tracking control strategy. Second, three motor nodes and the virtual node can be realized by the synchronization control by adopting the coupled harmonic oscillators method, so as to achieve for tracking the sinusoidal reference signal with zero phase-difference. Finally, the distributed tracking control performance for the LSRMs network is investigated by a simulation and experimental platform testing.

### 2. Model and Preliminaries

#### 2.1. Mathematical Preliminaries

*Notations*: Let  $\mathbb{R}^n$  and  $\mathbb{R}^{n \times m}$  indicate the n-dimensional Euclidean space and the set of  $n \times m$  real matrices, respectively.  $I_N$  represents an N-dimension unit matrix. The Kronecker product of matrices  $A \in \mathbb{R}^{n \times m}$  and  $B \in \mathbb{R}^{p \times q}$  satisfies the following properties as:

$$(A \otimes B)(C \otimes D) = AC \otimes BD,$$

$$(A \otimes B)^{T} = A^{T} \otimes B^{T},$$

$$k(A \otimes B) = (kA) \otimes B = A \otimes (kB),$$

$$A \otimes (B_{1} + B_{2}) = A \otimes B_{1} + A \otimes B_{2}.$$
(1)

The interaction topology of the coordinated network building LSRMs network system is represented using a directed graph  $\mathcal{G}=(\mathcal{V},\mathcal{E})$ , as shown in Figure 1, which is characterized by an edge-linked node set  $\mathcal{V}$ . It denotes N local closed-loop LSRM systems termed as LSRM node  $L_i, i=1,\ldots,N$ , formed by each LSRM and its local controller individually. An edge set  $\mathcal{E}\in\mathcal{V}\times\mathcal{V}$  represents M communication linkages among all LSRM nodes, where an edge exists from LSRM node  $L_j$  to  $L_i$  if  $(j,i)\in\mathcal{E}$ . If a set composed of LSRM nodes  $L_j$  satisfies  $(j,i)\in\mathcal{E}$ , it is named as the neighbor set  $\mathcal{N}_i$  associated with the LSRM node  $L_i$ . A directed graph contains a directed spanning tree if there exists a node called root such that there is one or more than one directed path from this node to every other node, such as  $L_1$  in Figure 1. A path from  $v_1$  to  $v_k$  in  $\mathcal{G}$  is formed by the  $\mathcal{E}$  subset  $\{(v_i,v_i+1)|i=1,\ldots,k-1)\}$ .  $\mathcal{A},\mathcal{L}$  denote its adjacency matrix and Laplacian matrix of  $\mathcal{G}$ , respectively.



Figure 1. Topology of coodinated network.

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# 2.2. Model of Linear Switched Reluctance Machine Node

Any of the N three-phase LSRMs (indexed as i-th, i = 1, ..., N) can be described in the voltage equation as [4]:

$$u_{k,i} = R_{k,i}i_{k,i} + \frac{d\lambda_{k,i}}{dt}, k = a, b, c,$$
(2)

where  $u_{k,i}$ ,  $R_{k,i}$  and  $i_{k,i}$  are terminal voltage, coil resistance and current, respectively.  $\lambda_{k,i}$  represents the flux-linkage of the k-th winding. Each LSRM can also be depicted as the second-order dynamics as follows:

$$m_i \frac{d^2 x_i}{dt^2} + B_i \frac{dx_i}{dt} + fl_i = f_i, \tag{3}$$

where  $x_i$ ,  $B_i$ ,  $m_i$ ,  $f_i$  and  $fl_i$  represent position, friction coefficient, mass, total and load force of the i-th LSRM, respectively. The second-order system as Equation (3) can be further represented in the discrete-time form as [5]:

$$A(z^{-1})x_i = B(z^{-1})f_i + e_i, (4)$$

where  $A(z^{-1})$  and  $B(z^{-1})$  are polynomials to be determined, z is the discrete-time operator, and  $e_i$  denotes stochastic disturbances of the i-th LSRM.The polynomials  $A(z^{-1})$  and  $B(z^{-1})$  corresponding to the typical discrete-time form are depicted as:

$$\begin{cases} A(z^{-1}) = 1 + a_1 z^{-1} + a_2 z^{-2}, \\ B(z^{-1}) = b_0 + b_1 z^{-1}. \end{cases}$$
 (5)

The purpose of online system identification is to correctly estimate  $a_1$ ,  $a_2$ ,  $b_0$  and  $b_1$  that contain all dynamic information of each LSRM. For the n-th estimation, Equation (4) can also be considered as a typical least square form as follows:

$$x_i(k) = \varphi^T(k-1)\theta + e_i(k), \tag{6}$$

where  $x_i(k)$  is the *i*-th LSRM state including the position and velocity at time step k, and:

$$\begin{cases}
\theta = \begin{bmatrix} a_1 & a_2 & b_0 & b_1 \end{bmatrix}^T, \\
\varphi(k-1) = \begin{bmatrix} -x_i(k-1) \cdots - x_i(k-n) f_i(k) \cdots f_i(k-n) \end{bmatrix}^T,
\end{cases}$$
(7)

where  $\theta$  is the vector to be estimated, and  $\phi$  is the matrix that include the input and output information of x and f. The parameters  $\theta$ ,  $\phi$  described in Equation (7) can be estimated by the recursive least square method as [29]:

$$\begin{cases}
\hat{\theta}(k) = \hat{\theta}(k-1) + R(k)e_i(k), \\
R(k) = P(k-1)\varphi(k-1)[\rho + \varphi^T(k)P(k-1)\varphi(k)]^{-1}, \\
P(k) = \rho^{-1}[I - K(k)\varphi^T(k)]P(k-1),
\end{cases} (8)$$

where P is the covariance matrix and R is the gain, K and I are, respectively, the gain matrix and an identity matrix with compatible dimensions, and  $\hat{\theta}$  represents the estimated value of  $\theta$  through the identification process.  $\rho$  is the forgetting factor that reflects the relationship between the converging rate and tracking ability and it falls into 0 and 1. For the LSRM,  $\rho$  is chosen as 0.98 for moderate converging ripples and a fast identification speed. For initial values, P(0) can be chosen as  $\eta \cdot I_4$  with  $\eta$  as a constant value of 50. Stochastic errors  $e_i$  can be represented as:

$$e_i(k) = x_i(k) - \varphi^T(k)\hat{\theta}(k-1).$$
 (9)

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If the relative error from the present to the last step is comparatively a small positive value  $\zeta$ , it can be regarded that the present estimated value is correct. Then, the termination criterion can be represented as:

$$\left| \frac{\hat{\theta}(k+1) - \hat{\theta}(k)}{\hat{\theta}(k)} \right| < \zeta. \tag{10}$$

Any local LSRM control system is defined as an LSRM node in the LSRMs network. The control block diagram for any LSRM node can be depicted as shown in Figure 2. The LSRM node  $L_i$  receives both the position feedback information from its linear encoder and the node  $L_j$ , and only the leader node (i.e., the node located at the root of a certain spanning tree in a coordinated network topology) accesses the external reference information, i.e., the input signal of the LSRMs network from outside. Each LSRM node is composed of a local position controller, the multiphase excitation scheme with look-up table linearization, current controllers and an LSRM, and the control scheme conforms to the typical dual-loop architecture [28]. For the LSRM node  $L_i$ , position error is decided from the difference between reference (the leader only) and actual position  $\rho_i$  of the i-th LSRM, along with the position information  $\rho_j$  from the LSRM node  $L_j$ . The position controller then calculates the control input, and the multi-phase excitation with the look-up table linearizion scheme determines the current command for the k-th phase of the i-th LSRM, according to the current position of the i-th LSRM. Then, the current controller outputs the actual current to the k-th winding.

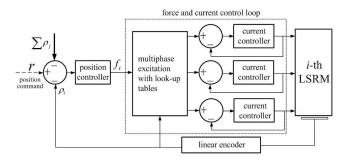


Figure 2. Control block diagram for the linear switched reluctance machine (LSRM) node.

Rearranging Equation (3) in the state-space form, we have:

$$\begin{bmatrix} \dot{\rho}_i \\ \ddot{\rho}_i \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 0 & -\frac{B_i}{m_i} \end{bmatrix} \begin{bmatrix} \rho_i \\ \dot{\rho}_i \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{1}{m_i} \end{bmatrix} u_i, \tag{11}$$

where  $u_i = f_i - fl_i$  is the control input of the *i*-th LSRM.

# 3. Synchronization Tracking Control Design

Since each LSRM is a mechatronic device fulfilling double-acting periodic line motion, some sinusoidal signals or its combinatorial patterns are often applied as the predefined trajectory planning some desired reciprocating motion for the LSRMs network. For this purpose, inspired by coupled harmonic oscillators synchronization proposed in [26,27], the distributed control law can be formulated as:

$$u_i = -\alpha \rho_i + B_i \dot{\rho}_i - \sum_{j \in \mathcal{N}_i} K_{d,i} \left[ \dot{\rho}_i(t) - \dot{\rho}_j(t) \right], \tag{12}$$

where  $\alpha$  is a parameter associated with the angular frequency  $\omega$  of the reference sinusoidal signal. Substituting Equation (12) into Equation (11), the LSRM node  $L_i$  can be depicted as:

$$\left[ \begin{array}{c} \dot{\rho}_i \\ \ddot{\rho}_i \end{array} \right] = \left\{ \left[ \begin{array}{cc} 0 & 1 \\ 0 & -\frac{B_i}{m_i} \end{array} \right] + \left[ \begin{array}{cc} 0 & 0 \\ -\frac{\alpha}{m_i} & \frac{B_i}{m_i} \end{array} \right] \right\} \left[ \begin{array}{c} \rho_i \\ \dot{\rho}_i \end{array} \right] - \sum_{j \in \mathcal{N}_i} \left[ \begin{array}{c} 0 \\ \frac{K_{d,i}}{m_i} \end{array} \right] \left[ \begin{array}{c} \dot{\rho}_i(t) - \dot{\rho}_j(t) \end{array} \right]$$

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$$= \begin{bmatrix} 0 & 1 \\ -\frac{\alpha}{m_i} & 0 \end{bmatrix} \begin{bmatrix} \rho_i \\ \dot{\rho}_i \end{bmatrix} - \sum_{j \in \mathcal{N}_i} \begin{bmatrix} 0 \\ \frac{K_{d,i}}{m_j} \end{bmatrix} \begin{bmatrix} \dot{\rho}_i(t) - \dot{\rho}_j(t) \end{bmatrix}. \tag{13}$$

Let  $\omega^2 = \frac{\alpha}{m_i}$ ,  $k_b = \frac{K_{d,i}}{m_i}$ ,  $\rho = [\rho_1, \dots, \rho_N]^T$ , the model of LSRMs network can be derived as:

$$\begin{bmatrix} \dot{\rho} \\ \ddot{\rho} \end{bmatrix} = \underbrace{\begin{bmatrix} 0_N & I_N \\ -\omega^2 \cdot I_N & -k_b \cdot \mathcal{L}(\mathcal{G}) \end{bmatrix}}_{S} \begin{bmatrix} \rho \\ \dot{\rho} \end{bmatrix}. \tag{14}$$

According to Equation (14), the LSRMs network can be reformulated as:

$$\dot{\tilde{X}} = \mathcal{S}\tilde{X},\tag{15}$$

where  $\tilde{X} = [\rho^T, \dot{\rho}^T]^T$ .

To prove the LSRMs network, Equation (15) has the ability to track a sinusoidal reference signal  $r = M \sin(\omega t + \theta)$  without phase disparity, and the following lemma is provided.

**Lemma 1.** Let  $\Psi_{l,i}$ ,  $\Psi_{r,i}$  be the left and right eigenvectors of Laplacian matrix  $\mathcal{L}$  associated to the *i*-th eigenvalue  $\psi_i$ , i = 1, ..., N, respectively. The eigenvalues of  $\mathcal{S}$  in Equation (15) can thus be represented as:

$$\lambda_{i\pm} = \frac{k_b \psi_i \pm \sqrt{k_b^2 \psi_i^2 - 4\omega^2}}{2},$$

and its left and right eigenvectors can be denoted as the following:

$$\Lambda_{l,i\pm} = [\Psi_{l,i}^T, \lambda_{i\pm} \Psi_{l,i}^T]^T, \Lambda_{r,i\pm} = [\Psi_{r,i}^T, -\frac{\lambda_{i\pm}}{\omega^2} \Psi_{r,i}^T]^T.$$

**Proof of Lemma 1.** We divide  $\Lambda_{l,i\pm}$ ,  $\Lambda_{r,i\pm}$  in two parts, denoted as  $\Lambda_{l,i\pm} = [\Lambda_{l,u}^T, \Lambda_{l,d}^T]^T$  and  $\Lambda_{r,i\pm} = [\Lambda_{r,u}^T, \Lambda_{r,d}^T]^T$ , respectively. For convenience, we omit the subscript index i or  $i\pm$ . For  $\Lambda_{l,i\pm}$ , we have:

$$\left[\begin{array}{cc} \Lambda_{l,u}^T & \Lambda_{l,d}^T \end{array}\right] \mathcal{S} = \lambda \left[\begin{array}{cc} \Lambda_{l,u}^T & \Lambda_{l,d}^T \end{array}\right]. \tag{16}$$

Similarly, for  $\Lambda_{r,i\pm}$ , we have:

$$\mathcal{S} \left[ \begin{array}{c} \Lambda_{r,u} \\ \Lambda_{r,d} \end{array} \right] = \lambda \left[ \begin{array}{c} \Lambda_{r,u} \\ \Lambda_{r,d} \end{array} \right]. \tag{17}$$

From Equation (14), Equation (16) can be derived as:

$$\Lambda_{l,d}^{T} = -\frac{\lambda}{\omega^2} \cdot \Lambda_{l,u'}^{T} \tag{18a}$$

$$\Lambda_{l,u}^T - k_b \Lambda_{l,d}^T \cdot \mathcal{L} = \lambda \cdot \Lambda_{l,d}^T. \tag{18b}$$

Likewise, we can obtain the equation as:

$$\Lambda_{r,d} = \lambda \cdot \Lambda_{r,u},\tag{19a}$$

$$-\omega^2 \cdot \Lambda_{r,u} - k_h \cdot \mathcal{L}\Lambda_{r,d} = \lambda \cdot \Lambda_{r,d}. \tag{19b}$$

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Substituting Equation (18a) into Equation (18b), we obtain:

$$\Lambda_{l,u}^{T} + \frac{k_{b}}{\omega^{2}} \lambda \cdot \Lambda_{l,u}^{T} \cdot \mathcal{L} = -\frac{\lambda^{2}}{\omega^{2}} \cdot \Lambda_{l,u}^{T}$$

$$-\Lambda_{l,u}^{T} \cdot \mathcal{L} = \frac{\lambda^{2} + \omega^{2}}{k_{b}\lambda} \Lambda_{l,u}^{T}.$$
(20)

In addition, substituting Equation (19a) into Equation (19b), we have:

$$-\omega^2 \cdot \Lambda_{r,u} - k_b \lambda \cdot \mathcal{L} \cdot \Lambda_{r,u} = \lambda^2 \cdot \Lambda_{r,u}, \tag{21a}$$

$$-\mathcal{L} \cdot \Lambda_{r,u} = \frac{\lambda^2 + \omega^2}{k_b \lambda} \cdot \Lambda_{r,u}.$$
 (21b)

According to Equation (21b), we notice  $\psi = -\frac{\lambda^2 + \omega^2}{k_b \lambda}$ ,  $\Psi_l = \Lambda_{r,u}$  are the eigenvalue and left eigenvector of Laplacian matrix  $\mathcal{L}$ , respectively. Therefore, we have:

$$\lambda^2 + k_b \psi \lambda + \omega^2 = 0. \tag{22}$$

Equation (22) can thus be solved as:

$$\lambda_{\pm} = \frac{k_b \psi \pm \sqrt{k_b^2 \psi^2 - 4\omega^2}}{2}.\tag{23}$$

In addition, from Equations (18a) and (19a), we know  $\Lambda_{l\pm} = [\Psi_l^T, -\frac{\lambda_{\pm}}{\omega^2} \Psi_l^T], \Lambda_{r\pm} = [\Psi_r^T, \lambda_{\pm} \Psi_r^T]^T$ . *Lemma 1* is proved.  $\Box$ 

**Theorem 1.** If graph G describing the coordinated network includes a directed spanning tree, and the root node can access to the reference position as sinusoidal signal  $r = \sin(\omega t + \theta)$  such as shown in Figure 3a, the LSRMs network in Equation (15) can track asymptotically the reference with zero phase-difference.



**Figure 3.** LSRMs network with the virtual LSRM modeling reference. (**a**) with reference; and (**b**) with virtual node.

**Proof of Theorem 1.** According to [29], for a directed graph  $\mathcal{G}$  with a spanning tree in the network topology, its Laplacian matrix  $-\mathcal{L}(\mathcal{G})$  has the left eigenvector  $\Psi_{l,1} = \mathbf{p}_N$  and the right eigenvector  $\Psi_{r,1} = \mathbf{1}_N$ . They correspond to a simple zero eigenvalue  $\psi_1 = 0$  of  $\mathcal{L}$ , and all rest of eigenvalues  $\psi_i$ ,  $i = 2, \ldots, N$  satisfy  $\text{Re}(\psi_i) < 0$ , where  $\text{Re}(\cdot)$  is the real part of a complex number. Furthermore,  $\mathbf{p}_N$  satisfies:

$$\mathbf{p}_N \ge 0,$$

$$\mathbf{p}_N^T \mathbf{1}_N = 1.$$
(24)

According to Lemma 1, the first two eigenvalues of S in Equation (15) are  $\lambda_{1\pm}=\pm\jmath\omega$ ,  $\jmath$  is the imaginary unit. Accordingly, the left eigenvector and right eigenvector are  $\Lambda_{l,1\pm}=[\mathbf{p}_N^T,\pm\jmath\omega\mathbf{p}_N^T]^T$ ,  $\Lambda_{r,1\pm}=[\mathbf{1}_N^T,\pm\frac{1}{l\omega}\mathbf{1}_N^T]^T$ , respectively. We have:

$$S = \mathcal{PMP}, \tag{25}$$

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where

$$\mathcal{P} = \left[\begin{array}{cc} \Lambda_{l,1\pm}, \ldots, \Lambda_{l,N\pm} \end{array}
ight], \mathcal{P}^{-1} = \left[\begin{array}{cc} \Lambda_{r,1\pm}, \ldots, \Lambda_{r,N\pm} \end{array}
ight]^T, \mathcal{M} = \left[\begin{array}{ccc} \jmath\omega & 0 & 0_{1 imes(2N-2)} \ 0 & -\jmath\omega & 0_{1 imes(2N-2)} \ 0_{(2N-2) imes1} & 0_{(2N-2) imes1} & J(\lambda_k) \end{array}
ight].$$

Here,  $J(\lambda_k)$  is the Jordan block matrix associated to  $k=2\pm,\ldots,N\pm$ . Since  $e^{\mathcal{S}t}=\mathcal{P}e^{\mathcal{M}t}\mathcal{P}^{-1}$ ,  $\lim_{t\to\infty}J(\lambda_k)=0_{(2N-2)\times(2N-2)}$ , it follows that:

$$\lim_{t \to \infty} e^{St} = [\Lambda_{l,1+}^T, \Lambda_{l,1-}^T] e^{\mathcal{M}_{1\pm}t} [\Lambda_{r,1+}^T, \Lambda_{r,1-}^T]$$

$$= \frac{1}{2} e^{J\omega t} \begin{bmatrix} \mathbf{1}_N \\ J\omega \cdot \mathbf{1}_N \end{bmatrix} \begin{bmatrix} \mathbf{p}_N \\ \frac{1}{J\omega} \mathbf{p}_N \end{bmatrix}^T + \frac{1}{2} e^{-J\omega t} \begin{bmatrix} \mathbf{1}_N \\ -J\omega \cdot \mathbf{1}_N \end{bmatrix} \begin{bmatrix} \mathbf{p}_N \\ \frac{-1}{J\omega} \mathbf{p}_N \end{bmatrix}^T$$

$$= \frac{[\cos(\omega t) + j\sin(\omega t)]}{2} \begin{bmatrix} \mathbf{1}_N \\ J\omega \cdot \mathbf{1}_N \end{bmatrix} \begin{bmatrix} \mathbf{p}_N \\ \frac{1}{J\omega} \mathbf{p}_N \end{bmatrix}^T$$

$$+ \frac{[\cos(-\omega t) + j\sin(\omega t)]}{2} \begin{bmatrix} \mathbf{1}_N \\ -J\omega \cdot \mathbf{1}_N \end{bmatrix} \begin{bmatrix} \mathbf{p}_N \\ \frac{-1}{J\omega} \mathbf{p}_N \end{bmatrix}^T$$

$$= \begin{bmatrix} \frac{\cos(\omega t) + j\sin(\omega t)}{2} & \frac{\cos(\omega t) + j\sin(\omega t)}{2\omega j} \\ \frac{\omega J[\cos(\omega t) + j\sin(\omega t)]}{2} & \frac{\cos(\omega t) + j\sin(\omega t)}{2\omega j} \end{bmatrix} \otimes \mathbf{1}_N \mathbf{p}_N^T$$

$$+ \begin{bmatrix} \frac{\cos(\omega t) - j\sin(\omega t)}{2} & \frac{-\cos(\omega t) + j\sin(\omega t)}{2\omega j} \\ \frac{\omega J[-\cos(\omega t) + j\sin(\omega t)]}{2} & \frac{-\cos(\omega t) - j\sin(\omega t)}{2\omega j} \end{bmatrix} \otimes \mathbf{1}_N \mathbf{p}_N^T$$

$$= \begin{bmatrix} \cos(\omega t) & \frac{1}{\omega}\sin(\omega t) \\ -\omega\sin(\omega t) & \cos(\omega t) \end{bmatrix} \otimes \mathbf{1}_N \mathbf{p}_N^T$$

where  $\mathcal{M}_{1\pm} = \begin{bmatrix} \omega_{J} & 0 \\ 0 & -\omega_{J} \end{bmatrix}$  is a block matrix of  $\mathcal{M}$  associated to  $\lambda_{1\pm} = \pm \omega_{J}$  and the simple zero eigenvalue of  $-\mathcal{L}$ .

Let  $\tilde{X} = \left[\rho^T, \dot{\rho}^T\right]^T$ , the solution of LSRMs network in Equation (14) can be obtained as:

$$\tilde{X}(t) = e^{\mathcal{S}t}\tilde{X}(0). \tag{27}$$

Moreover, according to Equation (26):

$$\lim_{t \to \infty} \tilde{X}(t) = \lim_{t \to \infty} e^{St} \cdot \tilde{X}(0)$$

$$= \left\{ \begin{bmatrix} \cos(\omega t) & \frac{1}{\omega}\sin(\omega t) \\ -\omega\sin(\omega t) & \cos(\omega t) \end{bmatrix} \otimes \mathbf{1}_{N} \mathbf{p}_{N}^{T} \right\} \tilde{X}(0)$$

$$= \left\{ \begin{bmatrix} \cos(\omega t) & \frac{1}{\omega}\sin(\omega t) \\ -\omega\sin(\omega t) & \cos(\omega t) \end{bmatrix} \otimes \mathbf{1}_{N} \right\} \cdot \left[ \mathbf{1}_{2} \otimes \mathbf{p}_{N}^{T} \right] \tilde{X}(0)$$

According to Equation (24), it can be seen that  $\mathbf{p}_N$  can be set as  $[1, \mathbf{0}_{N-1}^T]^T$  in Equation (28). Therefore, Equation (28) is derived as:

$$\lim_{t \to \infty} \tilde{X}(t) = \left\{ \begin{bmatrix} \cos(\omega t) & \frac{1}{\omega}\sin(\omega t) \\ -\omega\sin(\omega t) & \cos(\omega t) \end{bmatrix} \otimes \mathbf{1}_N \right\} x_1(0), \tag{29}$$

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where  $x_1(0)$  is the initial value of the LSRM node  $L_1$  as the root of a directed spanning tree in the coordinated network topology  $\mathcal{G}$ , as shown in Figure 1. In addition, the states of LSRM nodes  $L_i$ , i = 2, ..., N converge to the steady state as:

$$\begin{cases}
\rho_i(t) = \cos(\omega t)\rho_1(0) + \frac{1}{\omega}\sin(\omega t)\dot{\rho}_1(0), \\
\dot{\rho}_i(t) = -\omega\sin(\omega t)\rho_1(0) + \cos(\omega t)\dot{\rho}_1(0).
\end{cases} (30)$$

Obviously, the steady state values are determined by the initial values  $[\rho_1(0), \dot{\rho}_1(0)]$  of root node  $L_1$ . Therefore, the states of other N-1 LSRM nodes  $L_i$ ,  $i=2,\ldots,N$  converge to the state of root without phase disparity. The fact verifies, under the effect of the coordinated control Equation (12), that the states of LSRMs network can track the state of root node  $L_1$  represented as:

$$\begin{cases}
\rho_1(t) = \cos(\omega t)\rho_1(0) + \frac{1}{\omega}\sin(\omega t)\dot{\rho}_1(0), \\
\dot{\rho}_1(t) = -\omega\sin(\omega t)\rho_1(0) + \cos(\omega t)\dot{\rho}_1(0).
\end{cases} (31)$$

Letting  $\sin \theta = \rho_1(0)$ ,  $\cos \theta = \frac{1}{\omega} \dot{\rho}_1(0)$ , Equation (31) is rewritten as:

$$\begin{cases} \rho_1(t) = \sin(\omega t + \theta), \\ \dot{\rho}_1(t) = \omega \cos(\omega t + \theta). \end{cases}$$
(32)

Accordingly, if the reference sinusoidal position signal  $r = \sin(\omega t + \theta)$  in Figure 3a and its derivative is regarded as the state  $[\rho_r, \dot{\rho}_r]^T$  of a virtual root node  $L_r$ , as shown in Figure 3b, the sinusoidal reference signal can be tracked asymptotically by the LSRMs network Equation (15) in a coupled harmonic oscillators synchronization manner . *Theorem* 2 is proved.

**Remark 1.** By selecting appropriate initial values of virtual root node  $L_r$ , the LSRMs network Equation (15) can converge to the specified sinusoidal reference, which has phase  $\theta = \arcsin(\rho_r(0))$  and angular frequency  $\omega = \frac{\dot{\rho}_r(0)}{\cos \theta}$ .

# 4. Illustrative Examples

**Example 1.** The sinusoidal reference r is modeled as a virtual LSRM node  $L_r$ , and its initial phase and amplitude are  $\frac{\pi}{2}$ , 30 mm, respectively. In addition, the angular frequency of  $L_r$  is set as  $2\pi$  to investigate the system control feature tracking a higher frequency sine signal.

Each LSRM can be characterized by the second-order dynamics Equation (11). According to the method proposed in [8], system matrices  $A_i$  and  $B_i$  (i = 1, 2, 3) can be obtained by the online least squares identification [4] with a sampling time of T = 0.001 s, and they can be derived as:

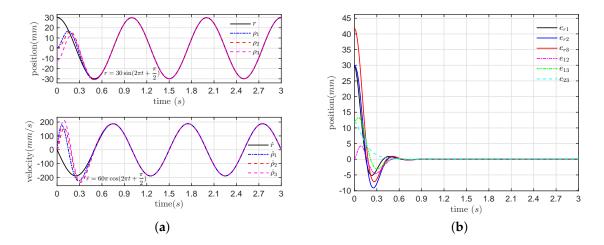
$$A_i = \begin{bmatrix} 0 & 1 \\ 0 & 0.3333 \end{bmatrix}, B_i = \begin{bmatrix} 0 \\ 0.6667 \end{bmatrix}.$$

The initial positions of three LSRM nodes are set as  $\rho_1(0) = 0$ ,  $\rho_2(0) = 0$ ,  $\rho_3(0) = -12$ , respectively, and all velocities of three LSRM nodes are 0. The control gain  $k_b$  is set as 0.25 empirically (according to some parameter tuning experience). The topology of the LSRMs network is depicted as Figure 3.

The results of the state and position error responses are depicted in Figure 4a,b, respectively. Figure 4a illustrates that the LSRMs network Equation (14) tracks the reference  $r = \sin(2\pi t + \frac{\pi}{2})$  in a zero phase-difference and asymptotic manner by applying the proposed control law Equation (12).

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The position errors among all nodes including  $\{L_r, L_1, L_2, L_3\}$  are illustrated in Figure 4b. The disparity of position errors are eliminated for all LSRM nodes after about 0.9 s.



**Figure 4.** (a) Position and velocity response and (b) relative position error response.

**Example 2.** To further verify the effectiveness of the proposed control strategy, a comparative study with Example 1 is addressed. We locate the initial positions of three LSRM nodes at  $\rho_1(0) = 0$ ,  $\rho_2(0) = 0$ ,  $\rho_3(0) = 12$ , respectively, and three LSRM nodes start work from static state. We set the reference r initial phase as  $\frac{\pi}{2}$ , and the angular frequency are selected as  $\frac{\pi}{4}$  to test the track feature to a lower frequency sine wave. The other systems parameters, such as the control gain, etc., are given the identical values as in Example 1.

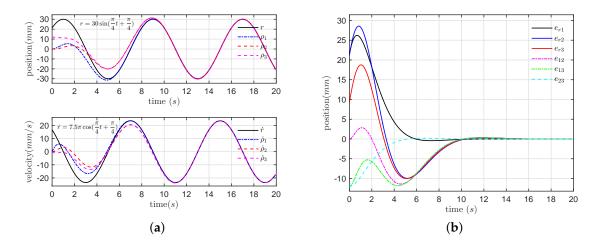


Figure 5. (a) Position and velocity response and (b) relative position error response.

The simulation results are shown in Figure 5a,b, respectively. The control performance from the proposed control method shows that a slower dynamic response can be achieved with a lower frequency sinusoidal reference, and compared to Example 1 for the same system without considering uncertain parameters and external disturbances. The results also demonstrate that the LSRMs network has successfully achieved the stable state without phase-difference after 10s. Therefore, the proposed tracking control scheme has certain superior stability.

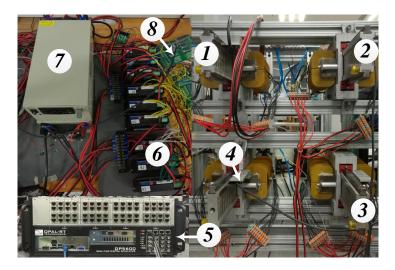
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**Remark 2.** From two example comparative results, it is noted that the response effectiveness of Example 2 is counterintuitive, since the state consensus process of Example 2 takes a longer time rather than Example 1, as expected. The main cause is that the angular frequency of the reference sinusoidal signal strongly affects the response rate of each LSRM node through Equation (12).

# 5. System Construction and Experimental Results

### 5.1. System Construction

The experimental platform on the LSRMs network is exhibited in Figure 6. The platform applies an RT-LAB (OP5600) real-time digital simulator (Opal-RT Technologies, Montreal, Quebec, Canada) as the distributed controllers on each LSRM node, and builds a virtual LSRM node  $L_r$  modeling the specific sinusoidal reference r. The position state of each LSRM node is measured and collected by a linear magnetic encoder and inspected by the host PC which is the management terminal remotely. The sampling frequency of the position control loop is 1 kHz. The current drivers of each LSRM node are connected to RT-LAB through the analog-to-digital converters. The current control is realized by three commercial amplifiers that are capable of inner current regulation based on the proportional-integral-differential algorithm with a switching frequency of 20 kHz. The sampling frequency of the position control loop is 1 kHz. The proposed distributed tracking control algorithm Equation (12) can be programmed under the MATLAB/Simulink® (R2015a, MathWorks, Natick, Massachusetts, USA) environment, and the developed algorithm can be downloaded to the digital signal processor of RT-LAB. All control parameters can be modified online. The real time state response waveforms of all LSRM nodes of the LSRMs network are monitored and recorded by the host PC.



**Figure 6.** Experimental platform of LSRMs network. (1) LSRM 1; (2) LSRM 2; (3) LSRM 3; (4) linear encoder; (5) RT-LAB; (6) current amplifier; (7) power supply; and (8) connection interface to RT-LAB.

The control objects of three LSRM nodes are three identical LSRMs that conform to the 6/4 switched reluctance machine structure. A double-sided machine arrangement guarantees a more stable and reliable output performance and the asymmetry of the stators ensures a higher force-to-volume ratio. The major machine specifications of the LSRM are demonstrated in Table 1 [28]. LSRM parameters can be obtained as  $a_1 = 0.3$ ,  $a_2 = 0.315$ ,  $b_0 = 0.026$ ,  $b_1 = 0.014$ , and through the online recursive least square parameter identification scheme.

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Quantity	Value
Mass of moving platform	3.8 kg
Mass of stator	5.0 kg
Pole pitch	12 mm
Pole width	6 mm
Air gap length	0.3 mm
Phase resistance	2 ohm
Number of turns	200
Stack length	50 mm
Rated power	250 W
Voltage	50 v
Encoder resolution	1 μm

**Table 1.** Main specifications of linear switched reluctance machine (LSRM).

### 5.2. Experimental Results

In order to validate the proposed control scheme based on coupled harmonic oscillators, the experiment of the tracking control is implemented for the LSRMs network based on the designed controller. Moreover, to compare with two aforementioned simulation examples, the system scenario and its parameters, including initial states of the reference and LSRM nodes and its controller gain, are given the same values as in Examples 1 and 2.

The tracking response waveforms for the three LSRMs node are shown in Figures 7 and 8.

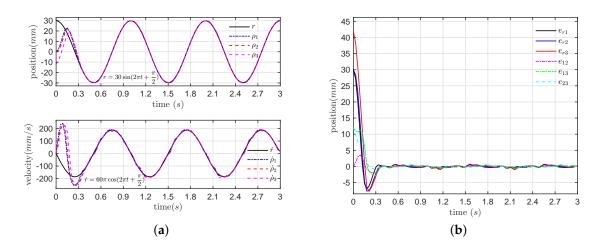


Figure 7. Position and velocity of reference and three LSRMs corresponding with Example 1.

Figure 7a illustrates that the tracking control of three LSRM nodes takes the zero phase-difference effect at about the time of  $0.4 \, s$ . From Figure 7b, the relative position errors among three LSRMs and the reference fall into  $1.2 \, mm$  in stable state after the transient time of  $0.4 \, s$ .

Figure 8a illustrates the dynamic position response waveforms under tracking control of three LSRM nodes. It is clear that the zero phase-difference effect is taken at about the time of 11 s. From the dynamic error response profiles as Figure 8b, it is clear that the maximum error values fall into 0.5 mm at the steady state. Figure 8c is the steady-state position response profiles under the distributed PD control strategy [8]. It can be seen that the phase errors of the LSRMs network under the distributed PD control is greater than the phase-difference response from the proposed control strategy.

According to the tracking profiles of the three LSRMs in Figures 7 and 8, the LSRMs network is all capable of following the position reference signal in zero phase-difference manner. However, the

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control performance from the three LSRMs is in disagreement and fluctuating slightly, especially in the steady state. This is mainly due to the imperfect manufacture and assembly of three LSRMs, which results in the asymmetric control performance from the positive and negative transitions. However, from Figures 4, 5, 7 and 8, it can be seen that the tracking control effect displays high similarity to the aforementioned numerical simulative examples. It can be concluded that the proposed control method is effective.

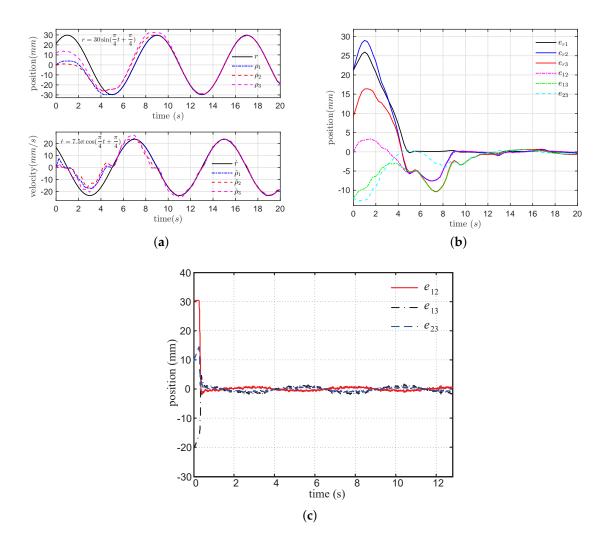


Figure 8. Position and velocity of reference and three LSRMs corresponding with Example 2.

### 6. Conclusions

A distributed control strategy of the LSRMs network is proposed for tracking a sinusoidal reference in a zero phase-difference manner. The dynamics of the LSRM nodes are modeled as general second-order linear systems by online system identification. Subsequently, inspired by the coupled harmonic oscillators synchronization, a distributed control is presented to track a sinusoidal reference without the phase-difference among each LSRM and the reference. Simulation and experimental results verify that the proposed control improves the synchronization and tracking accuracy performance of the LSRMs network through eliminating the phase-difference among LSRM nodes and virtual node modeling the sinusoidal reference. To further improve the tracking precision, it is suggested that the advanced internal model compensation schemes are introduced into the feedback control design of the LSRMs network. For the tracking control of some general periodical reference signals, the combined frequency domain analysis is also recommended for better control schemes. Furthermore, future

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work will also focus on the methods to annihilate load influence on the entire systems, including load influence on different topologies, dynamic load influence, etc.

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