

Article

# A New Dynamic Injection System of Urea-Water Solution for a Vehicular Select Catalyst Reduction System

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Academic Editor: Evangelos G. Giakoumis

Received: 28 September 2016; Accepted: 9 December 2016; Published: 23 December 2016

**Abstract:** Since the Euro-III standard was adopted, the main methods to inhibit  $\text{NO}_x$  production in diesel engines are exhaust gas recirculation (EGR) and select catalyst reduction (SCR). On these methods SCR offers great fuel economy, so it has received wide attention. However, there also exists a trade-off law between  $\text{NO}_x$  conversion efficiency and  $\text{NH}_3$  slip under dynamic conditions. To inhibit  $\text{NH}_3$  slip with high  $\text{NO}_x$  conversion efficiency, a dynamic control method for a urea water solution (UWS) injection was investigated. The variation phenomena of SCR conversion efficiency with respect to the cross-sensitivity characteristics of the  $\text{NO}_x$  sensor to  $\text{NH}_3$  have been thoroughly analyzed. The methodology of “uncertain conversion efficiency curve tangent analysis” has been applied to estimate the concentration of the slipped  $\text{NH}_3$ . The correction factor “ $\varphi$ ” of UWS injection is obtained by a comparative calculation of the  $\text{NO}_x$  conversion ability and subsequent  $\text{NH}_3$  slip. It also includes methods of flow compensation and flow reduction. The proposed control method has been authenticated under dynamic conditions. In low frequency dynamic experiments, this control method has accurately justified the  $\text{NH}_3$  slip process and inhibits the  $\text{NH}_3$  emission to a lower level thereby improving the conversion efficiency to a value closer to the target value. The results of European transient cycle (ETC) experiments indicate that  $\text{NH}_3$  emissions are reduced by 90.8% and the emission level of  $\text{NO}_x$  is close to the Euro-V standard.

**Keywords:** select catalyst reduction (SCR); urea water solution (UWS);  $\text{NH}_3$  slip; dynamic correction

## 1. Introduction

Direct injection diesel engines are preferred for their superior economy, power and emissions. Due to the high combustion temperature of the diesel engine, the nitrogen in the air is easily oxidized by oxygen and produces a large amount of  $\text{NO}_x$  which have a significant pollution impact on the environment. Therefore,  $\text{NO}_x$  emissions should be controlled. High pressure fuel injection and turbocharging technology have been used to change the ratio of particulate matter (PM) and  $\text{NO}_x$  by regulating the fuel injection strategy. From the Euro-II to the Euro-III phase, the high injection pressure (high common rail fuel injection) system has been used to optimize in-cylinder combustion and regulate the ratio of PM and  $\text{NO}_x$  to reach the emission goals. From the Euro-III to the Euro-IV phase, the main problem is how to significantly reduce PM and  $\text{NO}_x$  emissions. There are two methods at present: one is to use exhaust gas recirculation (EGR) to reduce in-cylinder  $\text{NO}_x$ , and out of the cylinder, with diesel particulate filter (DPF) to filter PM; the other method is to use select catalyst reduction (SCR) to eliminate  $\text{NO}_x$  and PM. In small diesel engines, the SCR system is limited by the exhaust gas temperature, so EGR + DPF technology is used as the main method to solve the emission problem. The exhaust temperature of medium and heavy diesel engines is high. At high exhaust

temperatures, diesel engines with SCR + high-pressure common rail (HCR) technology are more economical than diesel engines with EGR + DPF technology, so SCR is more widely used in medium and heavy duty diesel engines. From the Euro-IV to the Euro-V phase, how to further reduce  $\text{NO}_x$  has become the key problem. The main method is to optimize the SCR system to enhance the  $\text{NO}_x$  conversion efficiency and reduce the  $\text{NH}_3$  leakage [1–6].

At present, almost 99% of diesel vehicles work under dynamic operating conditions and thus their  $\text{NO}_x$  emissions are also a dynamic process. Based on this condition, excellent dynamic performance is an essential characteristic of the SCR system. SCR control strategies mainly focus on optimizing the urea water solution (UWS) injection rate algorithms and  $\text{NH}_3$  slip inhibition. However, there is a trade-off law between  $\text{NO}_x$  conversion efficiency and  $\text{NH}_3$  slip under dynamic conditions. When the actual injection rate is lower than the theoretical one, the  $\text{NO}_x$  can't be completely reduced. When the actual injection rate is higher than the theoretical value,  $\text{NH}_3$  can't be completely oxidized and thus generates secondary pollution [7–9]. Furthermore,  $\text{NH}_3$  storage and catalyst release make the  $\text{NH}_3$  slip inhibition more difficult.

Some researchers believe that an oxidation processor installed at the end of the exhaust pipe may inhibit  $\text{NH}_3$  slip [10]. Nova and Tronconi [11] added an Ammonia Slip Catalyst (ASC) to the exhaust pipe downstream of the SCR system and completed some investigations by experiment and simulation. The results showed that the studied ASC could efficiently clean up the slipped  $\text{NH}_3$ . Shrestha et al. [12] did some experiments and simulation research on multi-functional wash coated monolith catalysts. They compared the catalysts for a range of temperatures, space velocities, and feed compositions in the presence of  $\text{H}_2\text{O}$  and  $\text{CO}_2$ . Based on the data acquired from the experiments, a dynamic model of the  $\text{NH}_3$  oxidation process was established.

Some researchers supposed that it is necessary to investigate the processes of  $\text{NH}_3$  storage, release and reduction reaction as well as the SCR catalyst [13,14]. Rauch et al. [15] monitored the ammonia loading of a vanadia-based SCR catalyst by a microwave-based method. Their experimental results showed that the method can be applied to different temperatures. It was also possible to determine the storage of ammonia from the ammonia-to- $\text{NO}_x$  feed ratio. Zhang and Wang [16] focused on the simultaneous estimation of ammonia coverage ratios and input. They configured a three-state nonlinear model with the high-gain observer method by assuming the states of the SCR system are homogenous inside and the SCR cell was a continuous stirred tank reactor. The  $\text{NO}_x$  sensor was cross-sensitive to the  $\text{NH}_3$  concentration, and the  $\text{NO}_x$  sensor reading was corrected by precise  $\text{NH}_3$  sensor measurements. The simulation results showed that the designed observer worked well.

$\text{NO}_x$  sensors are used to measure the  $\text{NO}_x$  concentration downstream from the SCR system and feed it back to the SCR controller. However, research results have showed that  $\text{NO}_x$  sensors have an enhanced cross sensitivity to  $\text{NH}_3$  [17–19]. According to the structural characteristics of  $\text{NO}_x$  sensors, the  $\text{NH}_3$  inside the sensor is easily oxidized to  $\text{NO}_x$ . There are mainly three chemical reactions in this process, as described in Equations (1)–(3) [20–23]:



Wang [24] believed that the main factor is temperature, which may affect the three chemical reactions. The cross sensitivity factor of the  $\text{NO}_x$  sensor is changed as the temperature changes. Experiments proved that this factor was between 0.5 and 2 for a range of diesel engine exhaust temperatures.

This paper focuses on the trade-off law between  $\text{NO}_x$  conversion efficiency and  $\text{NH}_3$  slip by using a presented method of “uncertain conversion efficiency curve tangent analysis” based on the  $\text{NH}_3$  cross sensitivity characteristics of the  $\text{NO}_x$  sensor. The degree of  $\text{NH}_3$  slip will be obtained from the calculation of the parameters which may affect the shape and locations of this tangent. Subsequently,

the UWS injection correction factor “ $\varphi$ ” will be calculated with the dynamic flow compensation and flow reduction. Finally the accuracy of the UWS correction model and the effectiveness of  $\text{NH}_3$  slip inhibition will be verified under low-frequency and high-frequency (ETC cycle) dynamic working conditions.

## 2. Correction Strategy Mathematical Analysis

For the SCR system control strategy, the corrected UWS injection rate is calculated by Equation (4):

$$q_{\text{uws,Act}} = (1 + \varphi) \times q_{\text{uws,Bas}} \quad (4)$$

where  $q_{\text{UWS,Act}}$  is the real-time UWS injection rate after correction,  $q_{\text{UWS,Bas}}$  is the basic UWS injection rate before correction and  $\varphi$  is the correction factor of the UWS injection rate. The Simulink model of the correction strategy is shown in Figure 1.

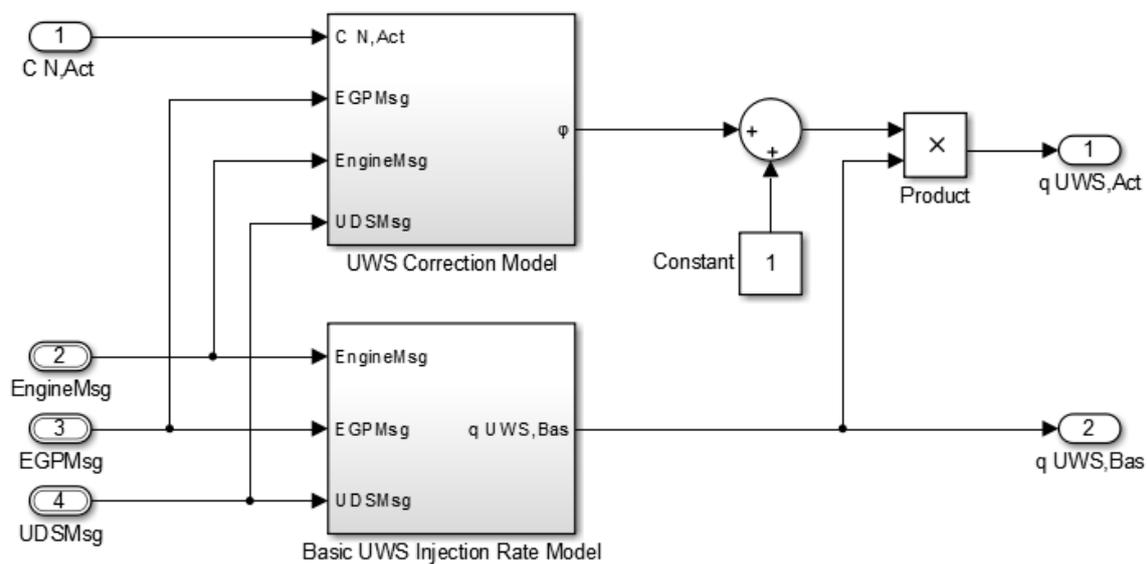


Figure 1. The correction strategy model. UWS: urea water solution.

The model consists of two sub-models. The “Basic UWS Injection Rate Model” sub-model collects three pieces of data: (1) engine operating data *EngineMsg*, which include speed, torque, original emissions, etc.; (2) exhaust gas processor data *EGPMsg*, which include exhaust temperature before and after the catalyst, gas flow, etc.; (3) injection system data *UDSMsg*. These data are combined to calculate  $q_{\text{UWS,Bas}}$ .

The “UWS Correction Model” sub-model collects four sets of data: (1) engine operating data; (2) waste gas treatment data; (3) urea injection system data; and (4)  $\text{NO}_x$  sensor data. These data are processed in the module to obtain the UWS injection rate correction factor  $\varphi$ . The  $q_{\text{UWS,Act}}$  is calculated using the factor  $\varphi$  and  $q_{\text{UWS,Bas}}$ .

The change rule of  $q_{\text{UWS,Act}}$  can be obtained from Equation (5):

$$a_{\text{UWS,Act}} = \frac{\partial q_{\text{uws,Act}}}{\partial t} = q_{\text{uws,Bas}} \frac{\partial \varphi}{\partial t} + (1 + \varphi) \frac{\partial q_{\text{uws,Bas}}}{\partial t} \quad (5)$$

where  $a_{\text{UWS,Act}}$  is the acceleration of  $q_{\text{UWS,Act}}$ , and  $t$  is the time.

The “ $\varphi$ ” (the initial value is “0”) is the key factor to correct the UWS injection and keep the SCR system at a low  $\text{NH}_3$  slip level with a high conversion efficiency. The UWS correction model is shown in Figure 2.

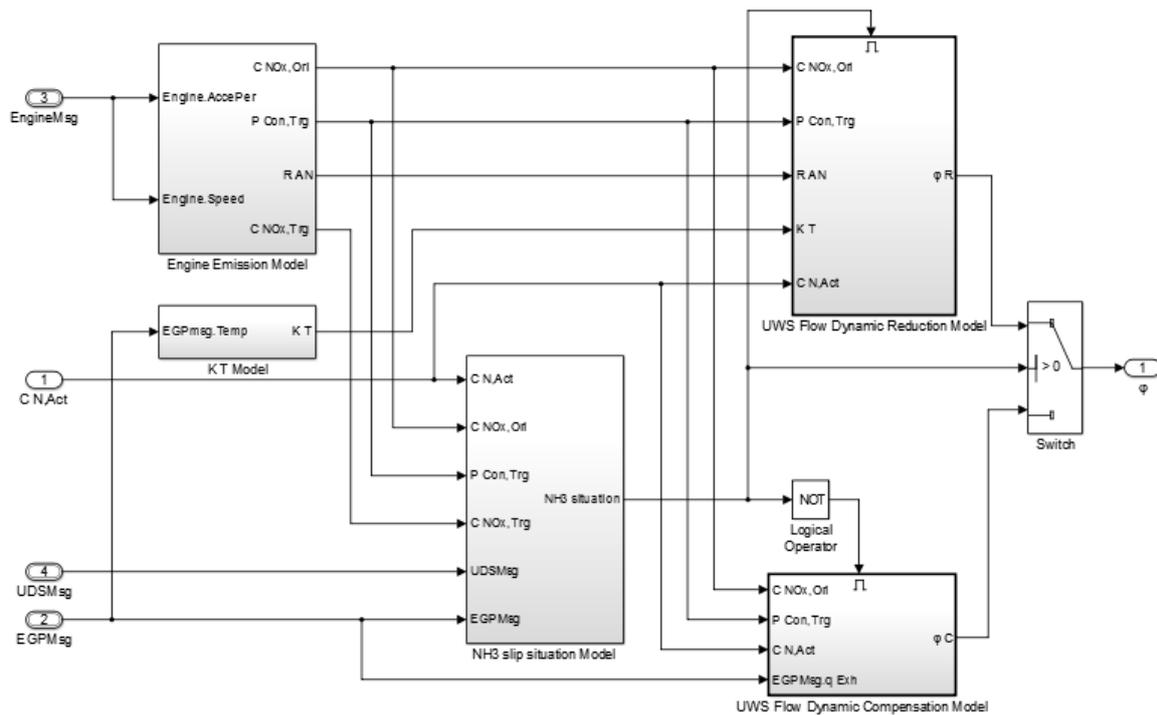


Figure 2. The UWS correction model.

The UWS correction model consists of five sub-models:

The “ $K_T$  Model” sub-model calculates the real-time  $\text{NH}_3$  sensitivity factor of the sensor based on the exhaust gas temperature near the  $\text{NO}_x$  sensor. The  $\text{NO}_x$  emission was measured by a  $\text{NO}_x$  sensor under dynamic conditions. The surrounding  $\text{NH}_3$  may be converted into  $\text{NO}_x$  easily in the  $\text{NO}_x$  sensor. Therefore, the values of  $\text{NH}_3$  and  $\text{NO}_x$  at the same time will be influenced by the data which is measured by the  $\text{NO}_x$  sensor, as given by Equation (6):

$$C_{N,Act} = C_{NO_x,Act} + K_T C_{NH_3,Act} \quad (6)$$

where  $C_{N,Act}$  is the  $\text{NO}_x$  concentration measured by the  $\text{NO}_x$  sensor.  $C_{NO_x,Act}$  is the actual  $\text{NO}_x$  concentration at the testing position.  $K_T$  is the  $\text{NH}_3$  cross sensitivity factor of the  $\text{NO}_x$  sensor which could be obtained from the  $K_T$  map and  $C_{NH_3,Act}$  is the actual  $\text{NH}_3$  concentration at the testing position.

The “Engine Emission Model” sub-model is used to calculate the original engine  $\text{NO}_x$  emissions, the target conversion efficiency, the ammonia-nitrogen ratio and the target  $\text{NO}_x$  emission concentration which would support service for the other models as shown in Figure 3. For example the targeted conversion efficiency could be calculated using Equation (7):

$$C_{NO_x,Trg} = C_{NO_x,Ori} \cdot P_{Con,Trg} \quad (7)$$

where  $P_{Con,Trg}$  is the target conversion efficiency (the highest value without  $\text{NH}_3$  slip) which can be obtained from the engine emission map,  $C_{NO_x,Ori}$  is the original  $\text{NO}_x$  concentration of the engine before after treatment and can be obtained by inserting the value calculation of the steady map and  $C_{NO_x,Trg}$  is the target  $\text{NO}_x$  concentration.

The “ $\text{NH}_3$  Slip Situation Model” sub-model is based on the output of the first two models to determine the current  $\text{NH}_3$  leak situation; more details can be seen in Section 2.1. The “UWS Flow Dynamic Reduction Model” sub-model is triggered when an  $\text{NH}_3$  leak occurs. When there is no  $\text{NH}_3$  leakage, it is necessary to consider whether there is little UWS injection and trigger the “UWS Flow Dynamic Compensation Model”.

The “UWS Flow Dynamic Compensation Model” and “UWS Flow Dynamic Reduction Model” sub-models are used to calculate the correction factor and compensation factor of the UWS injection rate, respectively (see Sections 2.2 and 2.3 for more details).

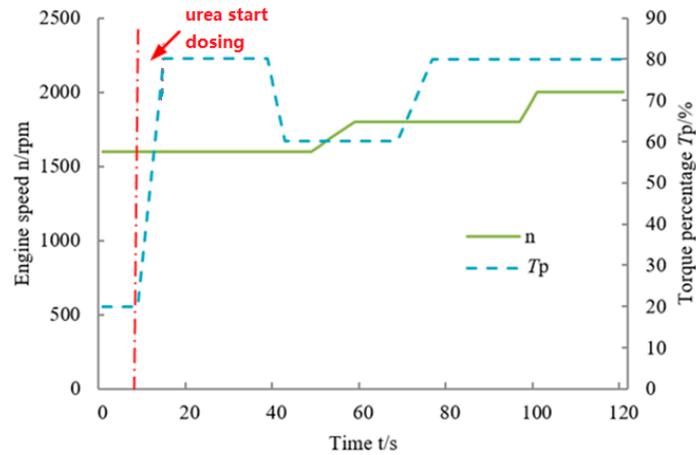


Figure 3. Low frequency dynamic process.

### 2.1. NH<sub>3</sub> Slip Situation Analysis

In order to justify and analyze the real-time NH<sub>3</sub> slip situation of the engine, a method called “uncertain conversion efficiency curve tangent analysis” is presented. From the real-time measured value  $C_{N,Act}$ , the uncertain conversion efficiency  $P_{Con,Fuz}$  can be calculated using Equation (8). The absolute conversion efficiency  $P_{Con,Abs}$  can be obtained from the calculated value  $C_{NO_x,Act}$  by Equation (9):

$$P_{Con,Fuz} = \frac{C_{NO_x,Ori} - C_{N,Act}}{C_{NO_x,Ori}} = 1 - \frac{C_{N,Act}}{C_{NO_x,Ori}} \quad (8)$$

$$P_{Con,Abs} = \frac{C_{NO_x,Ori} - C_{NO_x,Act}}{C_{NO_x,Ori}} = \frac{[C_{NO_x,Ori} - (C_{N,Act} - K_T C_{NH_3,Act})]}{C_{NO_x,Ori}} = P_{Con,Fuz} + \frac{K_T C_{NH_3,Act}}{C_{NO_x,Ori}} \quad (9)$$

According to the results of Equations (8) and (9), the relative conversion efficiency can be calculated with Equation (10):

$$P_{Con,Rel} = P_{Con,Abs} - P_{Con,Trg} = P_{Con,Fuz} + \frac{K_T C_{NH_3,Act}}{C_{NO_x,Ori}} - P_{Con,Trg} \quad (10)$$

The change rules of  $P_{Con,Fuz}$ ,  $P_{Con,Abs}$ , and  $P_{Con,Rel}$  can be obtained from Equations (11)–(13):

$$v_{Con,Fuz} = \dot{P}_{Con,Fuz} = - \frac{\partial \left( \frac{C_{N,Act}}{C_{NO_x,Ori}} \right)}{\partial t} \quad (11)$$

$$v_{Con,Abs} = \dot{P}_{Con,Abs} = \frac{\partial P_{Con,Fuz} + \partial \left( \frac{K_T C_{NH_3,Act}}{C_{NO_x,Ori}} \right)}{\partial t} \quad (12)$$

$$v_{Con,Rel} = v_{Con,Abs} - v_{Con,Trg} = \frac{\partial P_{Con,Fuz} + \partial \left( \frac{K_T C_{NH_3,Act}}{C_{NO_x,Ori}} \right) - \partial P_{Con,Trg}}{\partial t} \quad (13)$$

where  $v_{Con,Abs}$ ,  $v_{Con,Rel}$ , and  $v_{Con,Fuz}$  are their velocities. There are several kinds of NH<sub>3</sub> slip situations, as follows:

$$(1) P_{\text{Con,Fuz}} > P_{\text{Con,Trg}}$$

For the original map of  $P_{\text{Con,Trg}}$  obtained from the engine calibration experiments, from the theoretically point of view, with the  $P_{\text{Con,Fuz}} \leq P_{\text{Con,Trg}}$  under any circumstances. In the actual conditions when the engine calibration points are not enough, engine working instability or sensor testing errors might occur and lead to an abnormal circumstance (like  $P_{\text{Con,Fuz}} > P_{\text{Con,Trg}}$ ). For such an instance the  $\text{NH}_3$  slip is assumed to be zero, thus the UWS need not be corrected.

$$(2) 0 \leq P_{\text{Con,Fuz}} \leq P_{\text{Con,Trg}}, \text{ and } \tan\theta < 0 (v_{\text{Con,Fuz}} < 0)$$

In this case, the uncertain conversion efficiency is lower than its target and stays away from the target value gradually. According to Equation (8),  $P_{\text{Con,Fuz}}$  becomes smaller due to the increase of the  $C_{\text{N,Act}}$ . The enlargement of the  $C_{\text{N,Act}}$  may be caused by the following two cases:

- The first case is that the excessively injected UWS caused an acceleration of the process and subsequently an increasing  $\text{NH}_3$  slip due unreacted ammonia.
- The second case is that insufficient UWS may cause a slowing the process and lead to a growing amount of  $\text{NO}_x$  remaining unreduced due to unavailability of reactant.

Therefore, it may be concluded that with the condition  $a_{\text{UWS,Act}} \leq 0$  and  $P_{\text{Con,Abs}} \leq P_{\text{Con,Trg}}$ , there is no  $\text{NH}_3$  slip, thus UWS compensation could be continued. When  $a_{\text{UWS,Act}} > 0$  and  $P_{\text{Con,Abs}} = P_{\text{Con,Trg}}$ ,  $\text{NH}_3$  slip is severely increased, thus UWS injection should be reduced.

$$(3) 0 \leq P_{\text{Con,Fuz}} \leq P_{\text{Con,Trg}}, \text{ and } \tan\theta \geq 0 (v_{\text{Con,Fuz}} \geq 0)$$

In this case, the uncertain conversion efficiency is lower than its target and becomes close to the target value gradually. In this case it can be concluded that when  $a_{\text{UWS,Act}} > 0$  and  $P_{\text{Con,Abs}} \leq P_{\text{Con,Trg}}$ , there is no  $\text{NH}_3$  slip like the previous cases, thus UWS compensation should be continued. With the condition  $a_{\text{UWS,Act}} \leq 0$  and  $P_{\text{Con,Abs}} \geq P_{\text{Con,Trg}}$ , UWS injection should be reduced as  $\text{NH}_3$  slip is going to increase.

$$(4) P_{\text{Con,Fuz}} < 0$$

This particular case emerges on ruling out the test error and the engine calibration map error, thus under these circumstances  $C_{\text{NO}_x,\text{Act}} \leq C_{\text{NO}_x,\text{Ori}}$  (theoretically), whereas,  $C_{\text{N,Act}} > C_{\text{NO}_x,\text{Ori}}$  ( $P_{\text{Con,Fuz}} < 0$ ),  $C_{\text{NH}_3,\text{Act}} > 0$  as shown in Equation (7). This case indicates a seriously high level of  $\text{NH}_3$  slip therefore UWS injection must be stopped immediately.

## 2.2. Urea Water Solution Flow Dynamic Compensation

There was no  $\text{NH}_3$  slip during the process of the UWS dynamic compensation. Therefore:

$$\begin{cases} C_{\text{NH}_3,\text{Act}} \equiv 0 \\ C_{\text{NO}_x,\text{Act}} \equiv C_{\text{N,Act}} \end{cases} \quad (14)$$

It is indicated that the actual amount of injected UWS (including the  $\text{NH}_3$  released from the catalyst) was less than the demand of SCR reaction. The condition is  $0 \leq P_{\text{Con,Abs}} \leq P_{\text{Con,Trg}}$  and zero  $\text{NH}_3$  slip. Therefore, the correction factor  $\varphi$  can be calculated using Equation (15):

$$\varphi \equiv \frac{\Delta \dot{Q}_{\text{NO}_x,\text{Red}}}{\dot{Q}_{\text{NO}_x,\text{ActRed}}} \quad (15)$$

where  $Q_{NO_x,Red}$  ( $NO_x$  conversion potential) is the difference between the target value and actual value of the total reduced  $NO_x$  in a period as shown by Equation (16) and  $Q_{NO_x,ActRed}$  is the actual value of the total reduced  $NO_x$  in a specific period given by Equation (17):

$$\begin{aligned} \Delta Q_{NO_x,Re} &= \int C_{NO_x,Ori} P_{Con,Trg} q_{Exh} dt - \int (C_{NO_x,Ori} - C_{NO_x,Act}) q_{Exh} dt \\ &= \int [C_{N,Act} - C_{NO_x,Ori} (1 - P_{Con,Trg})] q_{Exh} dt \end{aligned} \quad (16)$$

$$Q_{NO_x,ActRed} = \int (C_{NO_x,Ori} - C_{NO_x,Act}) q_{Exh} dt = \int (C_{NO_x,Ori} - C_{NO_x,N}) q_{Exh} dt \quad (17)$$

$$\varphi = \frac{\partial \Delta Q_{NO_x,Red} / \partial t}{\partial Q_{NO_x,ActRed} / \partial t} = \frac{[C_{N,Act} - C_{NO_x,Ori} (1 - P_{Con,Trg})] q_{Exh}}{(C_{NO_x,Ori} - C_{N,Act}) q_{Exh}} = \frac{C_{NO_x,Ori} P_{Con,Trg}}{(C_{NO_x,Ori} - C_{N,Act})} - 1 \quad (18)$$

$$C_{N,Act} \leq C_{NO_x,Ori} \quad (19)$$

For the control method, the calculation of UWS injection rate and its acceleration may be accomplished with Equation (20) or Equation (21):

$$\begin{cases} q_{uws,Act} = \frac{C_{NO_x,Ori} P_{Con,Trg}}{(C_{NO_x,Ori} - C_{NO_x,N})} q_{uws,Bas} \\ a_{uws,Act} = q_{uws,Bas} \frac{\partial \left( \frac{C_{NO_x,Ori} P_{Con,Trg}}{C_{NO_x,Ori} - C_{N,Act}} \right)}{\partial t} + \\ \left( \frac{C_{NO_x,Ori} P_{Con,Trg}}{C_{NO_x,Ori} - C_{N,Act}} \right) \frac{\partial q_{uws,Bas}}{\partial t} \\ C_{N,Act} \leq C_{NO_x,Ori} \end{cases} \quad (20)$$

$$\begin{cases} q_{uws,Act} = 0 \\ a_{uws,Act} = 0 \\ C_{N,Act} \leq C_{NO_x,Ori} \end{cases} \quad (21)$$

where  $NH_3$  slip is assumed to be zero.

The value of  $NO_x$  emission in this process may be obtained with:

$$\begin{cases} Q_{NO_x} = \int C_{N,Act} q_{Exh} dt \\ Q_{NH_3} \equiv 0 \end{cases} \quad (22)$$

### 2.3. Urea Water Solution Flow Dynamic Reduction

During the UWS dynamic process, reduction is the response of increasing  $NH_3$  slip. Therefore:

$$\begin{cases} C_{NH_3,Act} \neq 0 \\ C_{NO_x,Act} + K_T \cdot C_{NH_3,Act} = C_{N,Act} \end{cases} \quad (23)$$

The case of  $0 \leq P_{Con,Abs} \leq P_{Con,Trg}$  and presence of evident  $NH_3$  slip shows that the actual amount of injected UWS (including the  $NH_3$  released from the catalyst) is much more than the demand of the SCR reaction. This current situation indicates that the SCR reaction is saturated as shown by Equation (24):

$$C_{NO_x,Act} = C_{NO_x,Ori} (1 - P_{Con,Trg}) \quad (24)$$

According to Equation (7):

$$C_{NH_3,Act} = \frac{C_{N,Act} - C_{NO_x,Ori} (1 - P_{Con,Trg})}{K_T} \quad (25)$$

The correction factor  $\varphi$  can be calculated as Equation (26):

$$\varphi = - \frac{\dot{Q}_{\text{NH}_3}}{R_{\text{AN}} \left( \dot{Q}_{\text{NO}_x, \text{TrgRed}} + \frac{\dot{Q}_{\text{NH}_3}}{R_{\text{AN}}} \right)} = - \frac{\dot{Q}_{\text{NH}_3}}{\left( R_{\text{AN}} \dot{Q}_{\text{NO}_x, \text{TrgRed}} + \dot{Q}_{\text{NH}_3} \right)} \quad (26)$$

where  $\dot{Q}_{\text{NH}_3}$  is the total  $\text{NH}_3$  emission amount in a specific period of time given by Equation (27),  $\dot{Q}_{\text{NO}_x, \text{TrgRed}}$  is the total reduced  $\text{NO}_x$  with target conversion efficiency of Equation (28) and  $R_{\text{AN}}$  is the ammonia nitrogen ratio constant set in the SCR system control strategy:

$$\dot{Q}_{\text{NH}_3} = \int C_{\text{NH}_3, \text{Act}} q_{\text{Exh}} dt = \int \left[ \frac{C_{\text{N}, \text{Act}} - C_{\text{NO}_x, \text{Ori}} (1 - P_{\text{Con}, \text{Trg}})}{K_T} \right] q_{\text{Exh}} dt \quad (27)$$

$$\begin{aligned} \varphi &= - \frac{\partial \dot{Q}_{\text{NH}_3} / \partial t}{\partial (R_{\text{AN}} \dot{Q}_{\text{NO}_x, \text{TrgRed}} + \dot{Q}_{\text{NH}_3}) / \partial t} \\ &= \frac{[C_{\text{NO}_x, \text{Ori}} (1 - P_{\text{Con}, \text{Trg}}) - C_{\text{N}, \text{Act}}] q_{\text{Exh}}}{K_T \left( R_{\text{AN}} P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}} - \frac{C_{\text{NO}_x, \text{Ori}} (1 - P_{\text{Con}, \text{Trg}}) - C_{\text{N}, \text{Act}}}{K_T} \right) q_{\text{Exh}}} \\ &= \frac{C_{\text{NO}_x, \text{Ori}} (1 - P_{\text{Con}, \text{Trg}}) - C_{\text{N}, \text{Act}}}{K_T R_{\text{AN}} P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}} - C_{\text{NO}_x, \text{Ori}} (1 - P_{\text{Con}, \text{Trg}}) + C_{\text{N}, \text{Act}}} \end{aligned} \quad (28)$$

Due to  $q_{\text{UWS}, \text{Act}} \geq 0$  and  $1 + \varphi \geq 0$ :

$$C_{\text{N}, \text{Act}} \geq C_{\text{NO}_x, \text{Ori}} - (1 + K_T R_{\text{AN}}) P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}} \quad (29)$$

In the presence of  $\text{NH}_3$  Slip, the control method may be applied to calculate the UWS injection rate and its acceleration is given by Equation (30) or Equation (31):

$$\begin{cases} q_{\text{uws}, \text{Act}} = \left( 1 - \frac{1}{K_T R_{\text{AN}}} + \frac{C_{\text{NO}_x, \text{Ori}} - C_{\text{N}, \text{Act}}}{K_T R_{\text{AN}} P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}}} \right) q_{\text{uws}, \text{Bas}} \\ a_{\text{uws}, \text{Act}} = q_{\text{uws}, \text{Bas}} \frac{\partial \left( \frac{C_{\text{NO}_x, \text{Ori}} - C_{\text{N}, \text{Act}}}{R_{\text{AN}} P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}} - \frac{1}{K_T R_{\text{AN}}} \right)}{\partial t} + \\ \left( 1 - \frac{1}{K_T R_{\text{AN}}} + \frac{C_{\text{NO}_x, \text{Ori}} - C_{\text{N}, \text{Act}}}{K_T R_{\text{AN}} P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}}} \right) \frac{\partial q_{\text{uws}, \text{Bas}}}{\partial t} \\ C_{\text{N}, \text{Act}} \geq C_{\text{NO}_x, \text{Ori}} - (1 + K_T R_{\text{AN}}) P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}} \end{cases} \quad (30)$$

$$\begin{cases} q_{\text{uws}, \text{Act}} = 0 \\ a_{\text{uws}, \text{Act}} = 0 \\ C_{\text{N}, \text{Act}} \geq C_{\text{NO}_x, \text{Ori}} - (1 + K_T R_{\text{AN}}) P_{\text{Con}, \text{Trg}} C_{\text{NO}_x, \text{Ori}} \end{cases} \quad (31)$$

The amount of  $\text{NO}_x$  emission and  $\text{NH}_3$  emission in this process could be determined by:

$$\begin{cases} \dot{Q}_{\text{NO}_x} = \int C_{\text{NO}_x, \text{Act}} q_{\text{Exh}} dt = \int C_{\text{NO}_x, \text{Ori}} (1 - P_{\text{Con}, \text{Trg}}) q_{\text{Exh}} dt \\ \dot{Q}_{\text{NH}_3} = \int [C_{\text{N}, \text{Act}} - C_{\text{NO}_x, \text{Ori}} (1 - P_{\text{Con}, \text{Trg}})] q_{\text{Exh}} dt \end{cases} \quad (32)$$

#### 2.4. Special Case

For the special case of  $P_{\text{Con}, \text{Abs}} > P_{\text{Con}, \text{Trg}}$ , the actual value is more than the target value of the system conversion efficiency and  $\text{NH}_3$  slip is assumed to be zero, as can be seen Equation (33):

$$\begin{cases} C_{\text{NH}_3, \text{Act}} \equiv 0 \\ C_{\text{NO}_x, \text{Act}} \equiv C_{\text{N}, \text{Act}} \end{cases} \quad (33)$$

The UWS injection rate doesn't require any dynamic adjustment thus  $\varphi \equiv 0$ . Therefore, it can be described with Equation (34) as follows:

$$\begin{cases} q_{uws,Act} = q_{uws,Bas} \\ a_{uws,Act} = \frac{\partial q_{uws,Bas}}{\partial t} \end{cases} \quad (34)$$

The amount of  $\text{NO}_x$  emission and  $\text{NH}_3$  emission in this process are:

$$\begin{cases} Q_{\text{NO}_x} = \int C_{N,Act} q_{Exh} dt \\ Q_{\text{NH}_3} \equiv 0 \end{cases} \quad (35)$$

While in another special case where  $P_{Con,Fuz} < 0$  indicates that  $\text{NH}_3$  slip is very high. Thus UWS injection must be stopped immediately. Now  $\varphi \equiv 0$ , and:

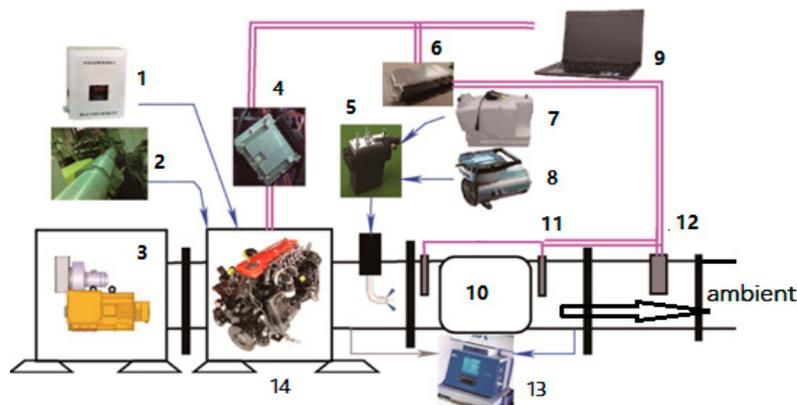
$$\begin{cases} q_{uws,Act} = 0 \\ a_{uws,Act} = 0 \end{cases} \quad (36)$$

The amount of  $\text{NO}_x$  emission and  $\text{NH}_3$  emission in this case can be described as follows:

$$\begin{cases} Q_{\text{NO}_x} = \int C_{N,Act} q_{Exh} dt = \int C_{\text{NO}_x, Ori} (1 - P_{Con, Trg}) q_{Exh} dt \\ Q_{\text{NH}_3} = \int [C_{N,Act} - C_{\text{NO}_x, Ori} (1 - P_{Con, Trg})] q_{Exh} dt \end{cases} \quad (37)$$

### 3. Experiments and Result Analysis

The low-frequency dynamic working conditions of the engine are reproduced as shown in Figure 1. The detailed dynamic process is shown in Figure 3. The related parameters of the SCR system are changed in a slower manner for this process by an explicit analysis of their relationships and interaction factors. Changes of  $\text{NO}_x$  emission and  $\text{NH}_3$  slip are compared before and after the UWS dynamic correction. The ETC cycle was adopted for the high-frequency dynamic process for further verification of the UWS control method performance. The engine experiment platform is shown in Figure 4.



**Figure 4.** Engine experiment platform block diagram. 1: Fuel consumption; 2: Air flowmeter; 3: Dynamometer; 4: Electronic control unit (ECU); 5: Unified diagnostic services (UDS); 6: SCR control unit (SCU); 7: UWS tank; 8: Air pump; 9: Monitor; 10: Exterior gateway protocol (EGP); 11: Temperature sensor; 12:  $\text{NO}_x$  sensor; 13: Emissions analyzer; and 14: Diesel engine.

The specifications of main equipment in the engine experiment platform are listed in Table 1.

**Table 1.** Specifications of main equipment.

Name	Type	Manufacturer	Location	Remark
Diesel engine	ISDe270 40	DCEC	Xiangfan, China	L6
Dynamometer	GWD300	POWERLINK	Changsha, China	Eddy current style
Fuel consumption	FC2210	POWERLINK	Changsha, China	Quality style
Air flow meter	ToCeil	Shanghai ToCeil Engine Testing Equipment	Shanghai, China	Hot film style
Emissions analyzer	SESAM4.0	AVL	Graz, Austria	Fourier transform infrared spectroscopy

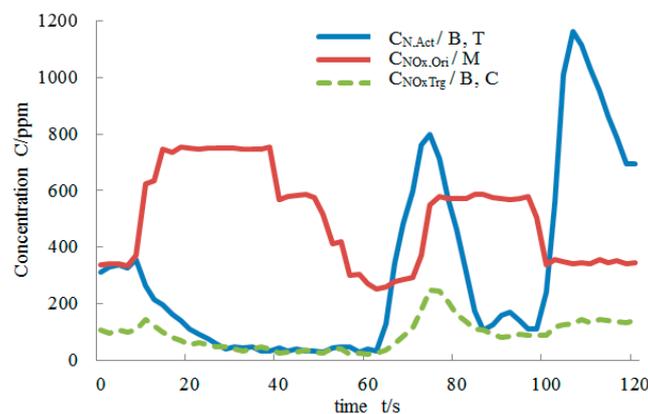
The heavy duty diesel engine parameters used in the experiment are given in Table 2.

**Table 2.** Parameters of ISDe270 40 diesel engine.

Cylinder Number	Bore/Stroke	Capacity	Compression Ratio	Rated Power/Speed	Max Torque	Fuel Supply Type
-	mm/mm	L	-	kW/rpm	Nm/rpm	-
L6	107/124	6.7	17.3:1	198/2500	970/1400	high pressure common rail

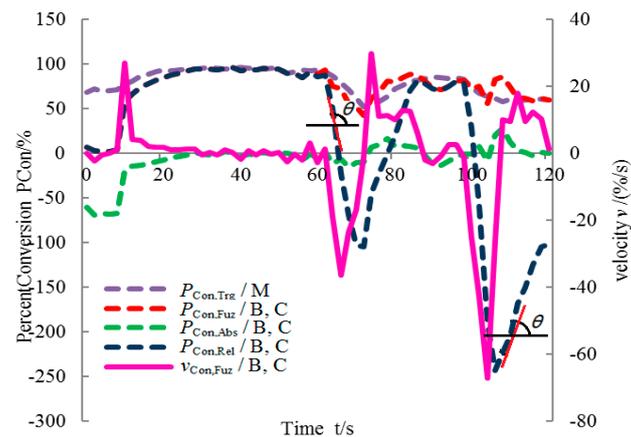
### 3.1. Mathematical Model Validation

As shown in Figure 5 (in this paper, A indicates the values after correction, B indicates the values before correction, T indicates the values obtained from equipment testing, C indicates the values obtained from calculation and M indicates the values obtained from the maps). The UWS injection was started at the 6th second. It can be seen in Figure 5 that the  $C_{N,Act}$  curve declined gradually in the first 30 s, became stable at a very low level in the second 30 s, and two noticeable humps can be observed in the last 60 s. Considering the  $NH_3$  cross sensitivity of the  $NO_x$  sensor, it could be initially assumed that the conversion efficiency was low in the first 30 s as the UWS injection was not sufficient. The  $NH_3$  slip increased significantly in the position of the two humps with the severely overloaded UWS injection. The UWS correction under dynamic conditions is critical for improving SCR conversion efficiency and  $NH_3$  slip inhibition.

**Figure 5.**  $NO_x$  emissions in dynamic conditions before the correction.

The change rules of the four kinds of conversion efficiency which have been discussed in Section 2.1 are shown in Figure 6.

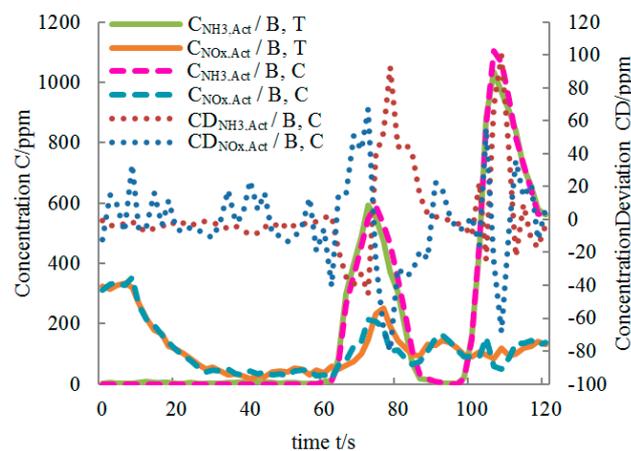
- (1) In the beginning,  $P_{Con,Abs}$  was less than the target value  $P_{Con,Trg}$ . However, these two values are the same as that after the 30th second.
- (2)  $P_{Con,Fuz}$  and  $P_{Con,Abs}$  remain the same as that before the 60th second. Then, two serious sinks appeared in the  $P_{Con,Fuz}$  curve.
- (3) After the beginning of UWS injection,  $P_{Con,Rel}$  was stable near a 0 value between the 20th and 60th second and fluctuated in a range of  $\pm 30\%$  between the 60th and 120th second.



**Figure 6.** The conversion efficiency tangents.

As a result, between the 30th and 60th second, the  $\text{NH}_3$  slip is assumed to be zero thus the UWS needs no correction. Between 60th and 90th or 100th and 120th second,  $\text{NH}_3$  slip is severely increased, thus UWS injection should be reduced. Between the 0th and 30th second there is no  $\text{NH}_3$  slip, thus UWS compensation be continued. The calculated value and actual experimental value of the  $\text{NO}_x$  and  $\text{NH}_3$  are compared in the low-frequency process. The results are shown in Figure 7.

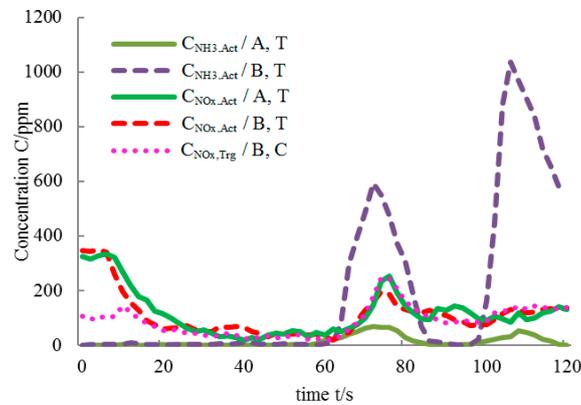
- (1) From the 0 to the 60th second and the 90th to 100th second, the experimental value of the  $\text{NH}_3$  concentration downstream from the SCR system is almost 0 ppm. The  $\text{NO}_x$  concentration and  $\text{NH}_3$  concentration calculated by the correction model completely overlap with the experimental values.
- (2) From the 60th to 90th second and the 100th to 120th second, there are slight deviations in the hump position between the calculated value and the experimental value of the  $\text{NH}_3$  concentration. The two compared values of  $\text{NO}_x$  concentration no longer completely overlap, but the range and the change rate are apparently the same.
- (3) At zero  $\text{NH}_3$  slip condition, the calculation deviation of  $\text{NH}_3$  concentration was between  $-10$  and  $0$  ppm and that of the  $\text{NO}_x$  concentration was between  $-20$  and  $20$  ppm.
- (4) Under high  $\text{NH}_3$  slip conditions, the calculation deviation of  $\text{NH}_3$  concentration was between  $-40$  and  $100$  ppm and that of  $\text{NO}_x$  concentration was between  $-70$  and  $70$  ppm.



**Figure 7.** The values and deviations of the  $\text{NO}_x$  and  $\text{NH}_3$  before the correction.

### 3.2. Low-Frequency Dynamic Process Correction Result

The low-frequency process has been repeated with the dynamic correction of the UWS injection. The  $\text{NO}_x$  and  $\text{NH}_3$  emissions after the correction are shown in Figure 8.



**Figure 8.** The  $\text{NO}_x$  and  $\text{NH}_3$  emissions before and after the correction.

- (1) From the UWS injection starting position to 60th second there was no  $\text{NH}_3$  slip. Between the 60th and 120th second the second two humps appeared in the  $\text{NH}_3$  concentration curve at less than 80 ppm. That's because of the fractionally unreacted  $\text{NH}_3$  slip downstream of the SCR system.
- (2) In the low-frequency process, the actual tested value of the  $\text{NO}_x$  emission was almost the same as the target value. The actual tested value was slightly lower than the target value in the hump region of the  $\text{NH}_3$  slip. That's because of the undue UWS injection and more  $\text{NO}_x$  was restored by the excessive  $\text{NH}_3$ .
- (3) In the hump region of the  $\text{NH}_3$  slip, the measured value is slightly higher than the target value of the  $\text{NO}_x$  concentration. That's because the  $\text{NO}_x$  sensor was influenced by  $\text{NH}_3$  and  $\text{NO}_x$  at the same time as shown in Equation (7).

Comparing the engine emissions before and after the UWS dynamic correction:

- (1) The  $C_{\text{NO}_x,\text{Act}}$  was slightly reduced in the last 60 s on application of the UWS dynamic correction. However, the control method has no significant effect on the value of  $C_{\text{NO}_x,\text{Act}}$  in the low-frequency process.
- (2) The  $C_{\text{NH}_3,\text{Act}}$  was also significantly reduced in the last 60 s after the UWS dynamic correction application. The values of  $C_{\text{NH}_3,\text{Act}}$  in the low-frequency process are also greatly influenced by the application of the correction.
- (3) Overall, the application of UWS dynamic control method has reduced  $\int C_{\text{NH}_3,\text{Act}} dt$  by 92.68%, respectively. Moreover it has also improved  $\int C_{\text{NO}_x,\text{Act}} dt$  by 5.58%.

The change trends of the all four kinds of conversion efficiencies are compared after applying the control method as shown in Figure 9.

- (1) In the beginning of the low-frequency process,  $P_{\text{Con,Abs}}$  was smaller than  $P_{\text{Con,Trg}}$ . However, the two curves overlapped after the 15th second.
- (2) From 0 to 60th second,  $P_{\text{Con,Fuz}}$  was the same as  $P_{\text{Con,Abs}}$ , whereas, after the 60th second  $P_{\text{Con,Fuz}}$  started to deviate with a slightly sinking trend.
- (3) Initially  $P_{\text{Con,Abs}}$  was less than 0 with a rising trend, whereas, it became stable when close to 0 and 15th to 60th second, while from 60th to 120th second it fluctuated many times with an amplitude between  $-15\%$  and  $15\%$ .

- (4)  $P_{Con,Abs}$  and  $P_{Con,Trg}$  were achieved in a shorter period as compared to Figure 4. The sinking amplitude of the  $P_{Con,Fuz}$  curve has significantly decreased after the 60th second and became stable in the last 60 s.

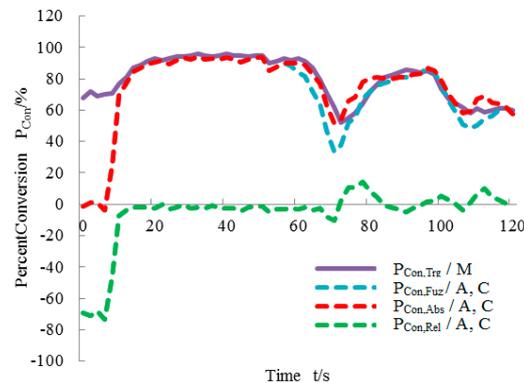


Figure 9. The four kinds of conversion efficiency after the correction.

The calculated values and experimental values of the  $NO_x$  and  $NH_3$  were further compared to ensure that the revised data can be well trusted as shown in Figure 10.

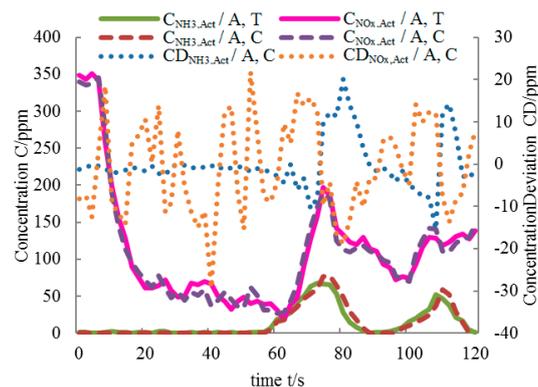


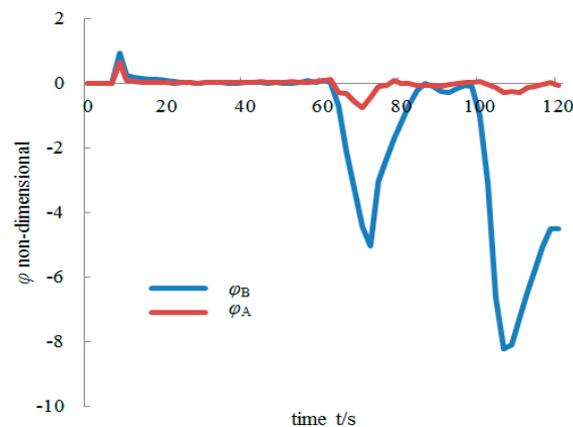
Figure 10. The values and deviations of the  $NO_x$  and  $NH_3$  after the correction.

- (1) In the corrected low-frequency process the trend of the calculated  $NH_3$  concentration was the same with that of the experimental value. The deviation of the calculation was more obvious in the region of high  $NH_3$  slip as compared to the results shown in Figure 7. The deviation oscillated between  $-10$  to  $0$  ppm and  $-5$  to  $0$  ppm with  $NH_3$  slip and between  $-40$  to  $100$  ppm and  $-20$  to  $15$  ppm without  $NH_3$  slip.
- (2) Moreover, during the corrected low-frequency process trend of the calculated  $NO_x$  concentration was the same as the actual tested value. The calculation deviation was uniformly distributed and oscillated between  $-70$  to  $70$  ppm and  $-20$  to  $20$  ppm as compared with Figure 7.
- (3)  $NO_x$  concentration calculation and  $NH_3$  concentration downstream of the SCR system would become more accurate with application of the UWS dynamic correction.

It is compared by the correction factor  $\varphi$  before and after applying the UWS dynamic control method as illustrated in Figure 11 ( $\varphi_A$  and  $\varphi_B$  indicate the correction factors after and before applying the control method, respectively).

- (1) From the UWS injection starting to 20th second,  $\varphi_B$  remained at more than 0 with a gradually declining trend. That is for the catalyst  $NH_3$  storage characteristic therefore UWS injection should be compensated.

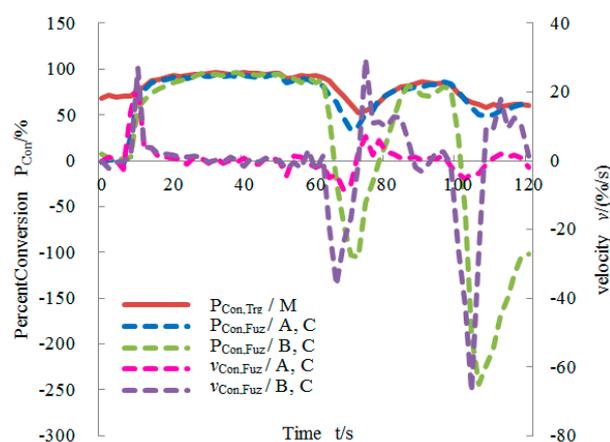
- (2) From 20th to 60th second,  $\varphi_B$  remained constant and close to 0. Now catalyst  $\text{NH}_3$  storage has been saturated without  $\text{NH}_3$  slip so UWS injection may not be corrected.
- (3) From 60th to 120th second,  $\varphi_B$  was less than 0. As compared to Figure 7 it is observed that the change trend of  $\varphi_B$  was contrary to the change trend of  $\text{NH}_3$  concentration. It is because of the severely increasing  $\text{NH}_3$  slip and UWS injection must be reduced.
- (4)  $\varphi_A$  and  $\varphi_B$  were greater than 0 and declined gradually from the starting position of UWS injection till the 20th second. However, the decrease of  $\varphi_A$  was faster than that of  $\varphi_B$ .
- (5)  $\varphi_A$  and  $\varphi_B$  remained close to 0 from 20th till the 60th second.
- (6) Values of both the factors ( $\varphi_A$  and  $\varphi_B$ ) became less than 0 during the last 60 s. Both factors shared two troughs. The trough values of  $\varphi_B$  ranged from  $-5$  to  $-8$  and that of the  $\varphi_A$  was  $-1$  to 0 in curve.



**Figure 11.** The dynamic correction fact before and after the correction.

The uncertain conversion efficiency  $P_{\text{Con,Fuz}}$  and its velocity  $v_{\text{Con,Fuz}}$  before and after applying the UWS dynamic correction are compared as shown in Figure 12:

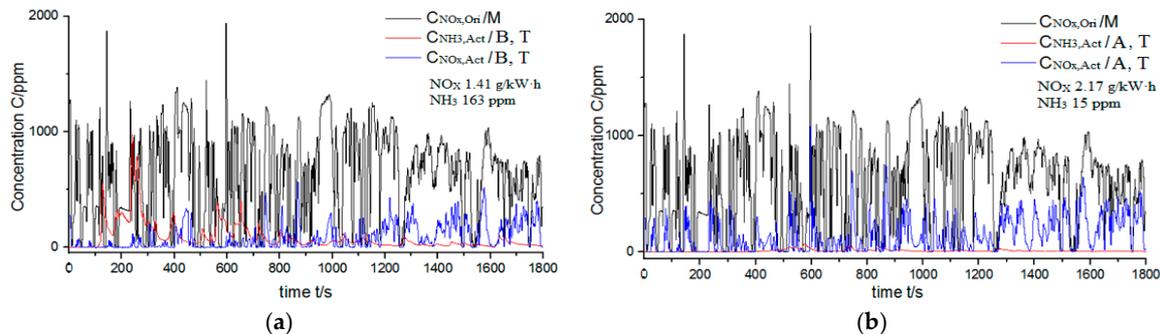
- (1)  $P_{\text{Con,Fuz}}$  and  $v_{\text{Con,Fuz}}$  were changed in the last 60 s on applying UWS injection dynamic correction during a high level of  $\text{NH}_3$  slip.
- (2) The  $P_{\text{Con,Fuz}}$  after correction appeared more close to  $P_{\text{Con,Trg}}$  and its range was reduced from  $-250\%$ – $95\%$  to  $40\%$ – $95\%$  compared to the values before correction.
- (3) The range of the  $v_{\text{Con,Fuz}}$  was reduced from  $-70\%$ – $30\%$  to  $-10\%$ – $10\%$  compared to the value before correction.



**Figure 12.** Conversion efficiency and its velocity before and after correction.

### 3.3. High-Frequency Dynamic Process Correction Result

The emission data comparison in ETC cycle before and after the UWS dynamic control method application is shown in Figure 13.



**Figure 13.** Emissions in the engine ETC cycle. (a) Before UWS injection dynamic correction; and (b) after UWS injection dynamic correction.

The result indicated a great high efficiency of  $\text{NO}_x$  conversion in the two tests. The  $\text{NO}_x$  emission was improved by 53.9% and the  $\text{NH}_3$  slip was reduced by 90.8% with the application of the control method. The  $\text{NH}_3$  slip was also inhibited significantly. The levels of engine  $\text{NO}_x$  emissions and  $\text{NH}_3$  slip were improved and conform to the Euro-V standard.

## 4. Conclusions

- (1) It can be generalized that the “uncertain conversion efficiency curve tangent analysis” method can accurately justify the different  $\text{NH}_3$  slip situation.
- (2) The calculation deviation can be controlled with  $\text{NO}_x$  between  $-20$  ppm and  $20$  ppm and  $\text{NH}_3$  between  $-20$  ppm to  $15$  ppm by application of UWS dynamic correction in a low-frequency process. The  $\text{NO}_x$  emission was improved by 5.58% and  $\text{NH}_3$  slip was reduced by 92.68%.
- (3) In the application of UWS dynamic correction in high-frequency process (i.e., during of ETC test), in spite the fact the  $\text{NO}_x$  emission has been improved by 53.9%, the  $\text{NH}_3$  slip was reduced by 90.8%. The level of engine  $\text{NO}_x$  emissions and  $\text{NH}_3$  slip has been improved up to Euro-IV and closer to the Euro-V standard. The newly developed method presents a significant  $\text{NH}_3$  slip inhibition.

**Author Contributions:** Long Li and Wei Lin made the method. Long Li and Wei Lin designed the experiment and organized the entire experiment process. Youtong Zhang made many experimental suggestions and collated the experiment data.

**Conflicts of Interest:** The authors declare no conflict of interests.

## Abbreviations

ASC	Ammonia slip catalysts
ETC	European transient cycle
HCR	High-pressure common rail
PM	Particulate matter
SCR	Select catalyst reduction
UWS	Urea water solution

## Symbols

$a_{UWS,Act}$	Acceleration of $q_{UWS,Act}$
$C_{N,Act}$	$NO_x$ concentration measured by the $NO_x$ sensor
$C_{NO_x,Act}$	Actual $NO_x$ concentration at the testing position
$C_{NO_x,Ori}$	Original $NO_x$ concentration of the engine before aftertreatment
$C_{NO_x,Trg}$	The target of $NO_x$ concentration downstream SCR system
$C_{NH_3,Act}$	Actual $NH_3$ concentration at the testing position
$C_{DNH_3,Act}$	Test error of actual $NH_3$ concentration
$C_{DNO_x,Act}$	Test error of actual $NO_x$ concentration
$K_T$	Cross sensitive factor
$P_{Con,Fuz}$	Uncertain conversion efficiency
$P_{Con,Abs}$	Absolute conversion efficiency
$P_{Con,Rel}$	Relative conversion efficiency
$P_{Con,Trg}$	Targeted conversion efficiency
$q_{UWS,Act}$	Real-time UWS injection rate after correction
$q_{UWS,Bas}$	Basic UWS injection rate before correction
$Q_{NO_x,Red}$	$NO_x$ conversion potential
$Q_{NO_x,AcRed}$	Actual value of the total reduced $NO_x$
$Q_{NO_x,TrgRed}$	Total reduced $NO_x$ under target conversion efficiency
$R_{AN}$	Ammonia nitrogen ratio set in the SCR control strategy
$\varphi$	Correction factor of the UWS injection rate
$\varphi_A$	Correct factor after applying the control method
$\varphi_B$	Correct factor before applying the control method Reference

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