## Methods for Compositional Data Analyses (CoDA)

The following CoDA procedures were adopted from prior published work that used accelerometer physical activity time use data. Steps per school day during physical education (PE), recess (RECESS,) lunchtime (LUNCH), and the academic class time (CLASS) were converted to percentage of total school day step activity within each segment so that their sum was equal to $100 \%$. The geometric means were calculated for each school segment. The geometric compositional value represents percentage of total school day step activity based on a 7-h school day.

Compositional data occupy a quotient space which can be represented in a D-part simplex with four compositional parts. However, in order to analyze the data in real space, log-ratio data transformations were performed. Isometric Log Ratio coordinates (ilrs) were calculated using the following equations:

$$
\begin{align*}
& \text { ilr } 1=\sqrt{\frac{3}{4}} \ln \left(\frac{\mathrm{PE}}{(\text { RECESS } \times \text { LUNCH } \times \text { CLASS })^{\frac{1}{3}}}\right)  \tag{1}\\
& i l r 2=\sqrt{\frac{2}{3}} \ln \left(\frac{\mathrm{RECESS}}{(\mathrm{LUNCH} \times \text { CLASS })^{\frac{1}{2}}}\right)  \tag{2}\\
& i l r 3=\sqrt{\frac{1}{2}} \ln \left(\frac{\mathrm{LUNCH}}{\text { CLASS }}\right) \tag{3}
\end{align*}
$$

Here, ilr 1 expresses the ratio of percentage of school step activity during PE to percentage of school step activity during all other non-PE school day segments. The ilr2 is the ratio of percentage of school steps during RECESS in relation to LUNCH and CLASS. Finally, ilr3 is the ratio of percentage of school day steps during LUNCH in relation to \% of steps accrued during CLASS. These three ilrs were included in the linear regression analyses; however, the inferences about the primary contrast of interest (i.e., PE relative to the three non-PE school segments) was based ilr . Because of this, additional ilrs were calculated by permutating school segments in a sequential manner to obtain interpretable parameter estimates for the other segments, specifically: RECESS (ilrs 4-6), LUNCH (ilrs 7-9) and CLASS (ilrs 1012).

$$
\begin{align*}
& \text { ilr } 4=\sqrt{\frac{3}{4}} \ln \left(\frac{\text { RECESS }}{(\text { PE } \times \text { LUNCH } \times \text { CLASS })^{\frac{1}{3}}}\right)  \tag{4}\\
& \text { ilr } 5=\sqrt{\frac{2}{3}} \ln \left(\frac{\text { PE }}{(\text { LUNCH } \times \text { CLASS })^{\frac{1}{2}}}\right)  \tag{5}\\
& \text { ilr } 6=\sqrt{\frac{1}{2}} \ln \left(\frac{\text { LUNCH }}{\text { CLASS }}\right)  \tag{6}\\
& \text { ilr } 7=\sqrt{\frac{3}{4}} \ln \left(\frac{\mathrm{LUNCH}}{(\text { PE } \times \text { RECESS } \times \text { CLASS })^{\frac{1}{3}}}\right)  \tag{7}\\
& \text { ilr } 8=\sqrt{\frac{2}{3}} \ln \left(\frac{\text { PE }}{(\text { RECESS } \times \text { CLASS })^{\frac{1}{2}}}\right)  \tag{8}\\
& \text { ilr } 9=\sqrt{\frac{1}{2}} \ln \left(\frac{\text { RECESS }}{\text { CLASS }}\right)  \tag{9}\\
& \text { ilr } 10=\sqrt{\frac{3}{4}} \ln \left(\frac{\text { CLASS }}{(\text { PE } \times \text { RECESS } \times \text { LUNCH })^{\frac{1}{3}}}\right)  \tag{10}\\
& \text { ilr } 11=\sqrt{\frac{2}{3}} \ln \left(\frac{\text { PE }}{(\text { RECESS } \times \text { LUNCH })^{\frac{1}{2}}}\right)  \tag{11}\\
& \text { ilr } 12=\sqrt{\frac{1}{2}} \ln \left(\frac{\text { RECESS }}{\text { LUNCH }}\right) \tag{12}
\end{align*}
$$

Therefore, the ilrs from Equations (1)-(3) were entered into each linear model to obtain the parameter estimate for $i l r$ PERECESSXLUNCHXCLASS, the ilrs from Equations (4)-(6) were entered into each linear model to obtain the parameter estimate for $i l r$ recessspexLunchxclass, the ilrs from Equations (7)-(9) were entered into each linear model to obtain the parameter estimate for ilr $_{\text {LUNCH/ PExRECESS } \times \text { LASS }}$, and the ilrs from Equations (10)-(12) were entered into each linear model to obtain the parameter estimate for ilr CLASS $/$ PExRECESSXLUNCH. Because of the permutation principle, each respective linear model with four school day segments (PE, RECESS, LUNCH, CLASS) will have the same estimated fit, intercept, and $p$-value per permutation.

Table S1. Arithmetic and geometric compositional step count means and \%'s for each school day segment (based on a 7-h school day).

|  | Arithmetic Mean |  | Compositional Mean |  |
| :--- | :--- | :--- | :--- | :--- |
|  | Steps/day | \% of Total School <br> Day Steps | Steps/day | of Total School <br> Pay Steps |
| PE | 1600 | $29.3 \%$ | 1482 | $31.1 \%$ |
| RECESS | 1071 | $19.6 \%$ | 978 | $20.5 \%$ |
| LUNCH | 1508 | $27.6 \%$ | 1418 | $29.8 \%$ |
| CLASSROOM | 1276 | $23.4 \%$ | 888 | $18.6 \%$ |

Note: PE is step counts during physical education; RECESS is step counts during recess; LUNCH is step counts during lunch period; CLASS is step counts within the academic classroom.

Table S2. Compositional variation matrix.

|  | PE | RECESS | LUNCH | CLASS |
| :--- | :--- | :--- | :--- | :--- |
| PE | - |  |  |  |
| RECESS | 0.40 | - |  |  |
| LUNCH | 0.18 | 0.14 | - |  |
| CLASS | 1.39 | 1.23 | 1.12 | - |

Note: PE is step counts during physical education; RECESS is step counts during recess; LUNCH is step counts during lunch period; CLASS is step counts within the academic classroom; Lower cell values indicate greater co-dependence between school segment steps; higher cell values indicate greater independence between school segment steps.


Figure S1. Geometric mean bar plot showing the log ratio of $\%$ of total school day step counts accrued within physical education, recess, lunch, and within the academic classroom, stratified by sex.

Note: Each bar represents the geometric mean of the specific group $\left(\mathrm{g}_{\mathrm{k}}\right)$, expressed as a ratio measured on a logarithmic scale to the geometric mean of the entire sample $\left(\ln g_{k} / g\right)$. A ratio of 0 reflects that the geometric means of the specific group and the entire sample are equal. Positive and negative values show that the group geometric mean is larger and smaller than the entire sample, respectively. PE is step counts during physical education; RECESS is step counts during recess; LUNCH is step counts during lunch period; CLASS is step counts within the academic classroom.

