

# Application of the Two-Dimensional Entropy Measures in the Infrared Thermography-Based Detection of Rider:Horse Bodyweight Ratio in Horseback Riding

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**Table S1.** Details of horses and riders participating in the study. Riders represented the light (L), moderate (M), and heavy (H) riders groups.

Rider groups	Sign	Horse			Sign	Horse			Sign	Rider		
		BW	High	SW		BW	High	SW		BW	High	BMI
L	1	585	166	4.1	7	560	162	4.2	A	58	159	22.9
	2	550	154	4.5	8	545	157	4.2	B	60	160	23.4
M	3	580	158	4.2	9	570	158	4.4	C	77	172	26.0
	4	575	164	4.5	10	580	162	4.4	D	75	164	27.9
H	5	560	160	4.1	11	565	160	4.2	E	91	172	30.8
	6	550	156	4.4	12	580	166	4.2	F	92	174	30.4

SW- saddle's weight [kg]; BW- bodyweight [kg]; height [cm]; BMI- body mass index [kg/m<sup>2</sup>].

**Table S2.** Details of the rider:horse bodyweight ratio of pairs participating in the study. Riders represented the light (L), moderate (M), and heavy (H) riders groups.

Rider groups	Horse/ Rider	Rider: Horse Bodyweight Ratio											
		1	2	3	4	5	6	7	8	9	10	11	12
L	A	10.6	11.4	10.7	10.9	11.1	11.3	11.1	11.4	10.9	10.8	11.0	10.7
	B	11.0	11.7	11.1	11.2	11.4	11.7	11.5	11.8	11.3	11.1	11.4	11.1
M	C	13.9	14.8	14.0	14.2	14.5	14.8	14.5	14.9	14.3	14.0	14.4	14.0
	D	13.5	14.5	13.7	13.8	14.1	14.4	14.1	14.5	13.9	13.7	14.0	13.7
H	E	16.3	17.4	16.4	16.6	17.0	17.3	17.0	17.5	16.7	16.4	16.8	16.4
	F	16.4	17.5	16.6	16.8	17.2	17.5	17.2	17.7	16.9	16.6	17.0	16.6

Horse - from 1 to 12; Rider - from A to F.

**Table S3.** The withers area (ROI 1). Values (mean  $\pm$  SD) of entropy measures for grayscale images in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	1.14 $\pm$ 0.39	1.77 $\pm$ 0.45	1.20 $\pm$ 0.04	7.01 $\pm$ 0.51	0.93 $\pm$ 0.06
	post-ex	1.06 $\pm$ 0.25	1.63 $\pm$ 0.29	1.19 $\pm$ 0.04	7.00 $\pm$ 0.41	0.93 $\pm$ 0.04
	p	0.500	0.262	0.509	0.622	0.812
M	pre-ex	1.04 $\pm$ 0.41	1.71 $\pm$ 0.50	1.20 $\pm$ 0.03	7.08 $\pm$ 0.51	0.92 $\pm$ 0.05
	post-ex	1.21 $\pm$ 0.38	1.83 $\pm$ 0.45	1.20 $\pm$ 0.04	7.18 $\pm$ 0.37	0.92 $\pm$ 0.03
	p	0.065	0.375	0.877	0.318	> 0.999
H	pre-ex	1.20 $\pm$ 0.33	1.92 $\pm$ 0.43	1.21 $\pm$ 0.02	7.23 $\pm$ 0.36	0.93 $\pm$ 0.05
	post-ex	1.22 $\pm$ 0.43	1.78 $\pm$ 0.49	1.21 $\pm$ 0.03	7.22 $\pm$ 0.45	0.94 $\pm$ 0.03
	p	0.822	0.170	0.375	0.923	0.855

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.

**Table S4.** The thoracic spine area (ROI 2). Values (mean  $\pm$  SD) of entropy measures for grayscale images in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	<b>0.84<math>\pm</math>0.33</b>	<b>1.46<math>\pm</math>0.35</b>	<b>1.15<math>\pm</math>0.06</b>	6.80 $\pm$ 0.54	<b>0.95<math>\pm</math>0.04</b>
	post-ex	<b>1.21<math>\pm</math>0.35</b>	<b>1.75<math>\pm</math>0.41</b>	<b>1.19<math>\pm</math>0.03</b>	6.96 $\pm$ 0.43	<b>0.93<math>\pm</math>0.04</b>
	p	<b>0.001</b>	<b>0.016</b>	<b>0.001</b>	0.164	<b>0.046</b>
M	pre-ex	<b>0.81<math>\pm</math>0.33</b>	<b>1.41<math>\pm</math>0.40</b>	1.15 $\pm$ 0.05	6.82 $\pm$ 0.47	0.94 $\pm$ 0.04
	post-ex	<b>1.10<math>\pm</math>0.40</b>	<b>1.61<math>\pm</math>0.35</b>	1.18 $\pm$ 0.05	6.87 $\pm$ 0.57	0.93 $\pm$ 0.04
	p	<b>0.003</b>	<b>0.049</b>	0.051	0.944	0.114
H	pre-ex	1.07 $\pm$ 0.48	1.67 $\pm$ 0.41	1.18 $\pm$ 0.04	7.03 $\pm$ 0.43	0.92 $\pm$ 0.06
	post-ex	1.17 $\pm$ 0.47	1.72 $\pm$ 0.51	1.17 $\pm$ 0.08	6.92 $\pm$ 0.93	0.90 $\pm$ 0.08
	p	0.456	0.838	0.456	> 0.999	0.143

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.

**Table S5.** The withers area (ROI 1). Values (mean  $\pm$  SD) of entropy measures for red color component in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	0.61 $\pm$ 0.35	1.38 $\pm$ 0.60	1.17 $\pm$ 0.05	<b>7.25<math>\pm</math>0.39</b>	<b>0.83<math>\pm</math>0.15</b>
	post-ex	0.94 $\pm$ 0.74	1.15 $\pm$ 0.29	1.19 $\pm$ 0.04	<b>6.57<math>\pm</math>0.47</b>	<b>0.50<math>\pm</math>0.14</b>
	p	0.089	0.218	0.345	<b>&lt; 0.0001</b>	<b>&lt; 0.0001</b>
M	pre-ex	0.55 $\pm$ 0.31	<b>1.34<math>\pm</math>0.58</b>	1.17 $\pm$ 0.05	<b>7.34<math>\pm</math>0.42</b>	<b>0.85<math>\pm</math>0.14</b>
	post-ex	0.55 $\pm$ 0.42	<b>0.99<math>\pm</math>0.24</b>	1.19 $\pm$ 0.04	<b>6.87<math>\pm</math>0.68</b>	<b>0.59<math>\pm</math>0.21</b>
	p	0.584	<b>0.020</b>	0.152	<b>0.005</b>	<b>&lt; 0.0001</b>
H	pre-ex	0.54 $\pm$ 0.27	<b>1.39<math>\pm</math>0.50</b>	<b>1.15<math>\pm</math>0.04</b>	<b>7.45<math>\pm</math>0.35</b>	<b>0.90<math>\pm</math>0.09</b>
	post-ex	0.59 $\pm$ 0.31	<b>1.14<math>\pm</math>0.27</b>	<b>1.22<math>\pm</math>0.08</b>	<b>7.11<math>\pm</math>0.55</b>	<b>0.64<math>\pm</math>0.23</b>
	p	0.550	<b>0.034</b>	<b>&lt; 0.0001</b>	<b>0.007</b>	<b>&lt; 0.0001</b>

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.

**Table S6.** The thoracic spine area (ROI 2). Values (mean  $\pm$  SD) of entropy measures red color component in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	<b>0.82<math>\pm</math>0.83</b>	<b>0.91<math>\pm</math>0.37</b>	<b>1.13<math>\pm</math>0.06</b>	<b>6.05<math>\pm</math>0.69</b>	<b>0.81<math>\pm</math>0.14</b>
	post-ex	<b>1.98<math>\pm</math>1.60</b>	<b>1.52<math>\pm</math>0.32</b>	<b>1.18<math>\pm</math>0.04</b>	<b>6.34<math>\pm</math>0.71</b>	<b>0.63<math>\pm</math>0.14</b>
	p	<b>0.001</b>	<b>&lt; 0.0001</b>	<b>0.004</b>	<b>0.037</b>	<b>0.0001</b>
M	pre-ex	<b>0.61<math>\pm</math>0.69</b>	<b>0.84<math>\pm</math>0.36</b>	<b>1.13<math>\pm</math>0.06</b>	<b>6.18<math>\pm</math>0.60</b>	<b>0.82<math>\pm</math>0.14</b>
	post-ex	<b>1.16<math>\pm</math>0.89</b>	<b>1.42<math>\pm</math>0.36</b>	<b>1.17<math>\pm</math>0.06</b>	<b>6.68<math>\pm</math>0.93</b>	<b>0.66<math>\pm</math>0.14</b>
	p	<b>0.001</b>	<b>&lt; 0.0001</b>	<b>0.033</b>	<b>0.025</b>	<b>0.0001</b>
H	pre-ex	<b>0.56<math>\pm</math>0.67</b>	<b>0.86<math>\pm</math>0.30</b>	1.15 $\pm$ 0.06	<b>6.36<math>\pm</math>0.76</b>	<b>0.87<math>\pm</math>0.12</b>
	post-ex	<b>1.11<math>\pm</math>1.08</b>	<b>1.41<math>\pm</math>0.40</b>	1.18 $\pm$ 0.05	<b>6.91<math>\pm</math>0.99</b>	<b>0.67<math>\pm</math>0.19</b>
	p	<b>0.003</b>	<b>&lt; 0.0001</b>	0.160	<b>0.018</b>	<b>0.002</b>

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.

**Table S7.** The withers area (ROI 1). Values (mean  $\pm$  SD) of entropy measures for green color component in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	<b>1.13<math>\pm</math>0.49</b>	2.22 $\pm$ 0.61	<b>1.16<math>\pm</math>0.04</b>	<b>7.45<math>\pm</math>0.26</b>	<b>0.88<math>\pm</math>0.07</b>
	post-ex	<b>0.89<math>\pm</math>0.29</b>	1.96 $\pm$ 0.45	<b>1.14<math>\pm</math>0.03</b>	<b>7.71<math>\pm</math>0.25</b>	<b>0.98<math>\pm</math>0.02</b>
	p	<b>0.038</b>	0.106	<b>0.025</b>	<b>0.0002</b>	<b>&lt; 0.0001</b>
M	pre-ex	<b>1.05<math>\pm</math>0.32</b>	2.16 $\pm$ 0.46	<b>1.17<math>\pm</math>0.04</b>	<b>7.52<math>\pm</math>0.25</b>	<b>0.88<math>\pm</math>0.08</b>
	post-ex	<b>0.82<math>\pm</math>0.25</b>	1.96 $\pm$ 0.47	<b>1.15<math>\pm</math>0.03</b>	<b>7.74<math>\pm</math>0.19</b>	<b>0.97<math>\pm</math>0.02</b>
	p	<b>0.004</b>	0.065	<b>0.039</b>	<b>0.0004</b>	<b>&lt; 0.0001</b>
H	pre-ex	1.06 $\pm$ 0.43	2.13 $\pm$ 0.59	<b>1.17<math>\pm</math>0.04</b>	<b>7.48<math>\pm</math>0.27</b>	<b>0.85<math>\pm</math>0.06</b>
	post-ex	0.93 $\pm$ 0.34	2.06 $\pm$ 0.54	<b>1.14<math>\pm</math>0.02</b>	<b>7.76<math>\pm</math>0.33</b>	<b>0.97<math>\pm</math>0.03</b>
	p	0.240	0.650	<b>0.0008</b>	<b>0.003</b>	<b>&lt; 0.0001</b>

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.

**Table S8.** The thoracic spine area (ROI 2). Values (mean  $\pm$  SD) of entropy measures green color component in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	<b>0.73<math>\pm</math>0.32</b>	<b>1.79<math>\pm</math>0.54</b>	1.12 $\pm$ 0.04	<b>7.28<math>\pm</math>0.46</b>	<b>0.92<math>\pm</math>0.05</b>
	post-ex	<b>1.45<math>\pm</math>0.41</b>	<b>2.86<math>\pm</math>0.61</b>	1.10 $\pm$ 0.04	<b>7.69<math>\pm</math>0.22</b>	<b>0.85<math>\pm</math>0.07</b>
	p	<b>&lt; 0.0001</b>	<b>&lt; 0.0001</b>	0.088	<b>0.0007</b>	<b>0.0004</b>
M	pre-ex	<b>0.76<math>\pm</math>0.35</b>	<b>1.84<math>\pm</math>0.68</b>	1.13 $\pm$ 0.04	<b>7.38<math>\pm</math>0.39</b>	<b>0.95<math>\pm</math>0.05</b>
	post-ex	<b>1.07<math>\pm</math>0.41</b>	<b>2.23<math>\pm</math>0.63</b>	1.13 $\pm$ 0.05	<b>7.70<math>\pm</math>0.34</b>	<b>0.89<math>\pm</math>0.07</b>
	p	<b>0.008</b>	<b>0.044</b>	0.793	<b>0.004</b>	<b>0.004</b>
H	pre-ex	0.91 $\pm$ 0.45	2.07 $\pm$ 0.62	1.12 $\pm$ 0.05	<b>7.10<math>\pm</math>0.53</b>	<b>0.97<math>\pm</math>0.03</b>
	post-ex	1.12 $\pm$ 0.63	2.27 $\pm$ 0.99	1.13 $\pm$ 0.04	<b>7.71<math>\pm</math>0.53</b>	<b>0.92<math>\pm</math>0.06</b>
	p	0.303	0.812	0.353	<b>0.0002</b>	<b>0.0002</b>

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.

**Table S9.** The withers area (ROI 1). Values (mean  $\pm$  SD) of entropy measures for blue color component in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	<b>1.09<math>\pm</math>0.71</b>	<b>1.71<math>\pm</math>0.51</b>	1.19 $\pm$ 0.03	<b>7.77<math>\pm</math>0.22</b>	<b>0.86<math>\pm</math>0.09</b>
	post-ex	<b>1.54<math>\pm</math>0.45</b>	<b>2.41<math>\pm</math>0.43</b>	1.18 $\pm$ 0.02	<b>7.02<math>\pm</math>0.26</b>	<b>0.72<math>\pm</math>0.11</b>
	p	<b>0.013</b>	<b>&lt; 0.0001</b>	0.050	<b>&lt; 0.0001</b>	<b>0.021</b>
M	pre-ex	<b>0.83<math>\pm</math>0.40</b>	<b>1.51<math>\pm</math>0.41</b>	<b>1.20<math>\pm</math>0.02</b>	<b>7.65<math>\pm</math>0.28</b>	<b>0.87<math>\pm</math>0.08</b>
	post-ex	<b>1.17<math>\pm</math>0.41</b>	<b>2.04<math>\pm</math>0.45</b>	<b>1.18<math>\pm</math>0.02</b>	<b>7.21<math>\pm</math>0.35</b>	<b>0.80<math>\pm</math>0.11</b>
	p	<b>0.007</b>	<b>&lt; 0.0001</b>	<b>0.045</b>	<b>&lt; 0.0001</b>	<b>&lt; 0.0001</b>
H	pre-ex	<b>0.70<math>\pm</math>0.31</b>	<b>1.43<math>\pm</math>0.30</b>	1.19 $\pm$ 0.03	<b>7.65<math>\pm</math>0.33</b>	<b>0.89<math>\pm</math>0.09</b>
	post-ex	<b>1.10<math>\pm</math>0.35</b>	<b>1.96<math>\pm</math>0.40</b>	1.19 $\pm$ 0.02	<b>7.37<math>\pm</math>0.35</b>	<b>0.84<math>\pm</math>0.09</b>
	p	<b>0.0003</b>	<b>&lt; 0.0001</b>	0.288	<b>0.010</b>	<b>0.032</b>

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.

**Table S10.** The thoracic spine area (ROI 2). Values (mean  $\pm$  SD) of entropy measures blue color component in light (L), moderate (M), and heavy (H) groups. The pre-exercise (pre-ex) and post exercise (post-ex) data series were compared. When features differed significantly ( $p < 0.05$ ) for all three groups (L, M, H), the values were marked in bold.

Groups		SampEn	FuzzEn	PermEn	DispEn	DistEn
L	pre-ex	<b>1.33<math>\pm</math>0.52</b>	<b>2.08<math>\pm</math>0.44</b>	1.18 $\pm$ 0.04	<b>7.89<math>\pm</math>0.20</b>	<b>0.84<math>\pm</math>0.09</b>
	post-ex	<b>1.78<math>\pm</math>0.49</b>	<b>2.34<math>\pm</math>0.49</b>	1.19 $\pm$ 0.02	<b>7.45<math>\pm</math>0.30</b>	<b>0.71<math>\pm</math>0.11</b>
	p	<b>&lt; 0.0001</b>	<b>0.004</b>	0.327	<b>&lt; 0.0001</b>	<b>&lt; 0.0001</b>
M	pre-ex	1.18 $\pm$ 0.46	1.97 $\pm$ 0.41	1.19 $\pm$ 0.02	<b>7.82<math>\pm</math>0.13</b>	<b>0.86<math>\pm</math>0.07</b>
	post-ex	1.39 $\pm$ 0.49	2.04 $\pm$ 0.46	1.19 $\pm$ 0.04	<b>7.57<math>\pm</math>0.26</b>	<b>0.77<math>\pm</math>0.11</b>
	p	0.128	0.527	0.812	<b>0.0001</b>	<b>0.0008</b>
H	pre-ex	1.26 $\pm$ 0.50	2.03 $\pm$ 0.46	1.19 $\pm$ 0.03	<b>7.84<math>\pm</math>0.12</b>	<b>0.85<math>\pm</math>0.08</b>
	post-ex	1.38 $\pm$ 0.80	1.97 $\pm$ 0.65	1.19 $\pm$ 0.02	<b>7.66<math>\pm</math>0.27</b>	<b>0.81<math>\pm</math>0.07</b>
	p	0.790	0.591	0.931	<b>0.016</b>	<b>0.026</b>

ROI - regions of interest. SampEn - two-dimensional sample entropy, FuzzEn - two-dimensional fuzzy entropy, PermEn - two-dimensional permutation entropy, DispEn - two-dimensional dispersion entropy, DistEn - two-dimensional distribution entropy. p - the level of marginal significance; SD - standard deviation.