

Supplementary material

The convergence curves showing the stability in the zeroth-order reflectance as a function of the number of diffracted orders are shown in Figure S1 and Figure S2. The two figures show all the marginal cases and polarization directions in this study, including:

Figure S1a: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=0\text{ rad}$

Figure S1b: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=0\text{ rad}$

Figure S1c: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=\pi/2\text{ rad}$

Figure S1d: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=\pi/2\text{ rad}$

Figure S1e: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=0\text{ rad}$

Figure S1f: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=0\text{ rad}$

Figure S1g: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=\pi/2\text{ rad}$

Figure S1h: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=0\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=\pi/2\text{ rad}$

Figure S2a: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=0\text{ rad}$

Figure S2b: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=0\text{ rad}$

Figure S2c: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=\pi/2\text{ rad}$

Figure S2d: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=0\text{ rad}$ and $\psi=\pi/2\text{ rad}$

Figure S2e: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=0\text{ rad}$

Figure S2f: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=0\text{ rad}$

Figure S2g: $\lambda=633\text{nm}$, $\lambda_g=1\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=\pi/2\text{ rad}$

Figure S2h: $\lambda=633\text{nm}$, $\lambda_g=25\mu\text{m}$, $\theta_0=1.45\text{ rad}$, $\phi=\pi/2\text{ rad}$ and $\psi=\pi/2\text{ rad}$

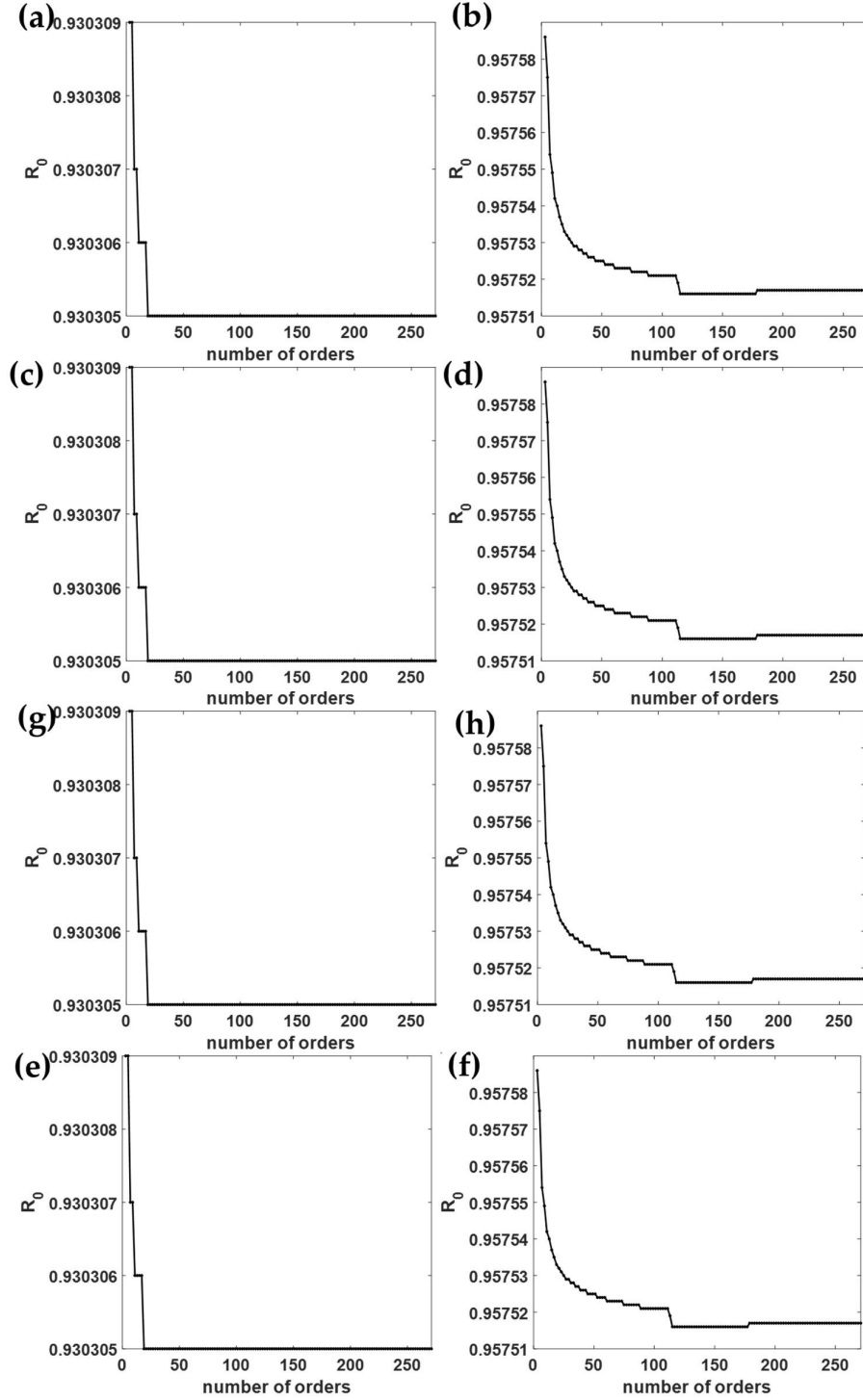


Figure S1. Shows RCWA simulation convergence tests using the incident wavelength λ of 633nm and (a) $\lambda_g=1\mu\text{m}$, $\theta_0=0$ rad, $\phi=0$ rad and $\psi=0$ rad, (b) $\lambda_g=25\mu\text{m}$, $\theta_0=0$ rad, $\phi=0$ rad and $\psi=0$ rad, (c) $\lambda_g=1\mu\text{m}$, $\theta_0=0$ rad, $\phi=0$ rad and $\psi=\pi/2$ rad, (d) $\lambda_g=25\mu\text{m}$, $\theta_0=0$ rad, $\phi=0$ rad and $\psi=\pi/2$ rad, (e) $\lambda_g=1\mu\text{m}$, $\theta_0=0$ rad, $\phi=\pi/2$ rad and $\psi=0$ rad, (f) $\lambda_g=25\mu\text{m}$, $\theta_0=0$ rad, $\phi=\pi/2$ rad and $\psi=0$ rad, (g) $\lambda_g=1\mu\text{m}$, $\theta_0=0$ rad, $\phi=\pi/2$ rad and $\psi=\pi/2$ rad, and (h) $\lambda_g=25\mu\text{m}$, $\theta_0=0$ rad, $\phi=\pi/2$ rad and $\psi=\pi/2$ rad

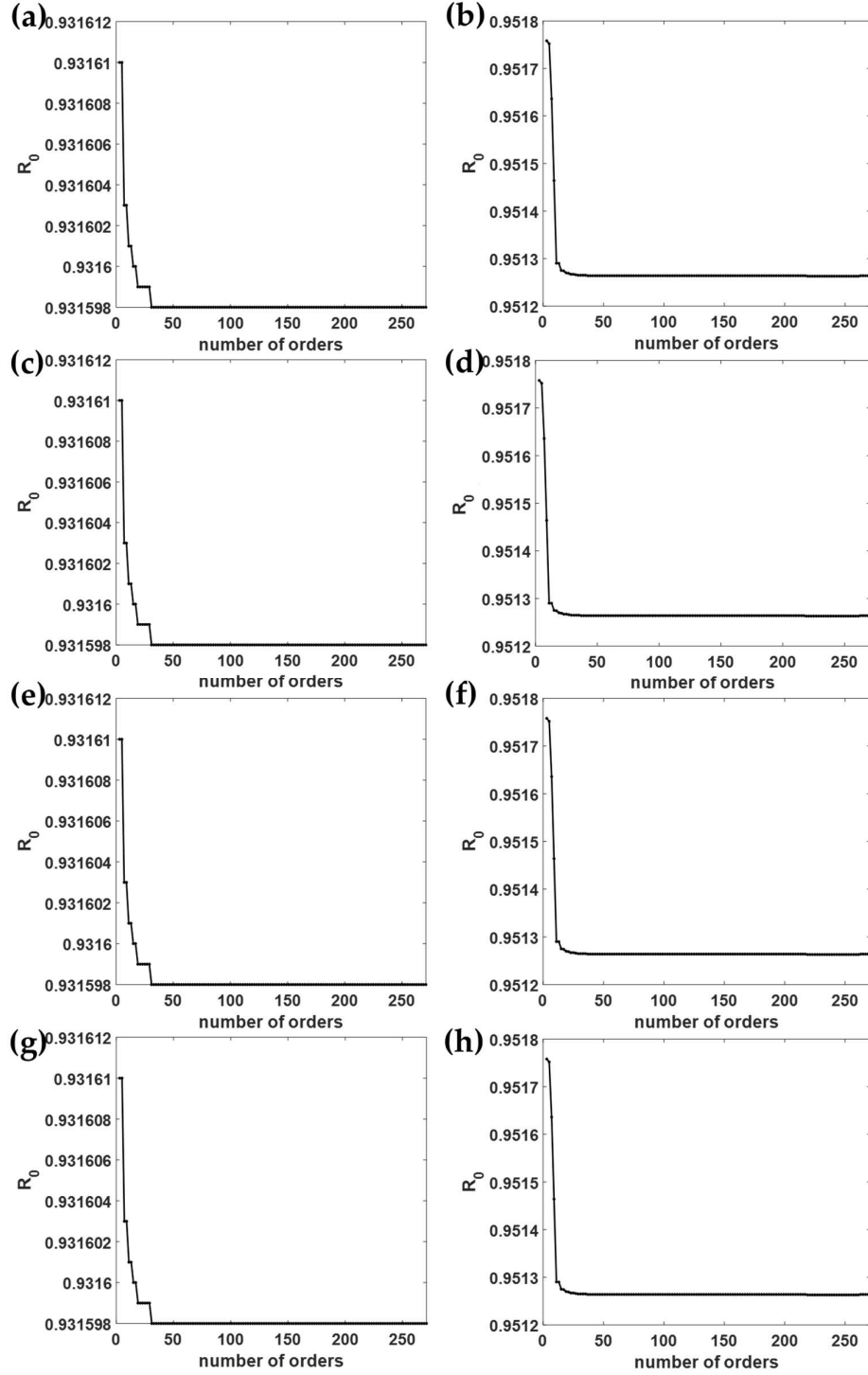


Figure S2. Shows RCWA simulation convergence tests using the incident wavelength λ of 633nm and (a) $\lambda_g=1\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=0$ rad and $\psi=0$ rad, (b) $\lambda_g=25\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=0$ rad and $\psi=0$ rad, (c) $\lambda_g=1\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=0$ rad and $\psi=\pi/2$ rad, (d) $\lambda_g=25\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=0$ rad and $\psi=\pi/2$ rad, (e) $\lambda_g=1\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=\pi/2$ rad and $\psi=0$ rad, (f) $\lambda_g=25\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=\pi/2$ rad and $\psi=0$ rad, (g) $\lambda_g=1\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=\pi/2$ rad and $\psi=\pi/2$ rad, and (h) $\lambda_g=25\mu\text{m}$, $\theta_0=1.45$ rad, $\phi=\pi/2$ rad and $\psi=\pi/2$ rad

In conclusion, the 271 diffracted orders employed in the RCWA simulations can provide convergence for all the cases in the scope of the study.