# Study of the Structural Chemistry of the Inclusion Complexation of 4-Phenylbutyrate and Related Compounds with Cyclodextrins in Solution: Differences in Inclusion Mode with Cavity Size Dependency 

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#### Abstract

PB ) and structurally related compounds hold promise for treating many diseases, including cancers. However, pharmaceutical limitations, such as an unpleasant taste or poor aqueous solubility, impede their evaluation and clinical use. This study explores cyclodextrin (CD) complexation as a strategy to address these limitations. The structural chemistry of the CD complexes of these compounds was analyzed using phase solubility, nuclear magnetic resonance (NMR) spectroscopic techniques, and molecular modeling to inform the choice of CD for such application. The study revealed that PB and its shorter-chain derivative form $1: 1 \alpha \mathrm{CD}$ complexes, while the longer-chain derivatives form 1:2 (guest:host) complexes. $\alpha$ CD includes the alkyl chain of the shorter-chain compounds, depositing the phenyl ring around its secondary rim, whereas two $\alpha$ CD molecules sandwich the phenyl ring in a secondary-to-secondary rim orientation for the longer-chain derivatives. $\beta$ CD includes each compound to form 1:1 complexes, with their alkyl chains bent to varying degrees within the CD cavity. $\gamma \mathrm{CD}$ includes two molecules of each compound to form 2:1 complexes, with both parallel and antiparallel orientations plausible. The study found that $\alpha \mathrm{CD}$ is more suitable for overcoming the pharmaceutical drawbacks of PB and its shorter-chain derivative, while $\beta C D$ is better for the longer-chain derivatives.


Keywords: cyclodextrins; 4-phenylbutyrate; inclusion complexation; structural chemistry; inclusion mode; cavity size dependency

## 1. Introduction

4-phenylbutyrate ( PB ) is a phenyl-substituted fatty acid derivative. It is used to manage urea cycle disorders (UCDs), a group of rare metabolic disorders caused by inborn deficiencies in the urea cycle and characterized by hyperammonemia [1-4]. PB exhibits many other biological activities, including acting as a low molecular weight chemical chaperone (LWCC) and histone deacetylase inhibitor, and its therapeutic effects against hemoglobinopathies, cancer, and cystic fibrosis are being investigated in clinical trials [5-8].

A series of structurally related compounds of PB (Figure 1) have been suggested to have similar biological activities as PB. In a study of PB and other LWCC in protecting human renal proximal tubule epithelial cells, the efficacy and potency of these compounds were shown to be attributable to the presence of a hydrophilic end followed by a long
hydrocarbon, with the length of the hydrophobic hydrocarbon region correlating with potency [9]. A recent study of the structural chemistry of these compounds and their binding to human serum albumin at our laboratory showed that the binding affinities between the ligands and albumin were dependent on the number of methylene units between the phenyl and carboxylate groups on the molecule, and the maximum affinity was found for 6-phenylcaproic acid (number of methylene units 5) [10]. Therefore, PB and these structurally related compounds hold potential as lead compounds for the management of various diseases.



Sodium 4-phenylbutyrate (PB)


6-phenylcaproic acid (PC)


7-phenylheptanoic acid (PH)

Figure 1. Chemical structures of PB and structurally related compounds (PP, PV, PC, and PH).
However, PB has a notoriously unpleasant taste, resulting in poor patient compliance. Furthermore, the related compounds have unfavorable pharmaceutical properties, such as poor aqueous solubility, oily physical state, or unpleasant odor and taste, impeding their evaluation and potential clinical use [5,11,12]. To fully explore the therapeutic potential of these promising compounds, it is necessary to investigate methods for addressing these limitations. One such approach is complexing these molecules with cyclodextrins (CDs). CDs are cyclic oligosaccharides comprising six, seven, eight, or more D-glucopyranose units linked by $\alpha-1,4$-glycosidic bonds that form inclusion complexes with a wide range of molecules in a host:guest fashion [13-15]. This inclusion complex formation results in profound improvements in the physicochemical and biological properties of drug substances, including improving their solubility, bioavailability, and stability, as well as masking unpleasant odors and tastes and converting liquids and oils to free-flowing powders [16-18]. Moreover, due to their favorable toxicological profile, CDs are preferred over organic solvents for in vitro/in vivo evaluation of new chemical entities [16]. Therefore, we explored CD complexation as a strategy to overcome the pharmaceutical drawbacks of PB and its structurally related compounds. From our studies, we recently reported that $\alpha \mathrm{CD}$ significantly masks the unpleasant taste of PB and can address the limitations of current market formulations [19].

Thus, in our continuing investigations, we undertook structural chemistry analyses of the PB-related compounds and their complex formation with CDs in solution using phase solubility studies, nuclear magnetic resonance (NMR) spectroscopic techniques, and molecular modeling. Though some studies on the complexation of some phenyl alkanoates with CDs have been reported, the present study provides insight into the CD cavity size dependency and the effect of guest structure on the stability, inclusion mode, and stoichiometry of CD inclusion complexes of PB and its therapeutically relevant and structurally related compounds in aqueous solution [20-22].

The findings of the present study provide the basis for selecting the most appropriate CDs for complexing PB-related compounds to overcome their pharmaceutical limitations and allow for their clinical evaluation and use.

## 2. Results and Discussion

### 2.1. Phase Solubility Studies

Figure 2 shows the phase solubility diagrams of the interactions between the CDs and PB or related compounds. $\alpha$ CD showed $A_{L}$-type phase solubility diagrams with PP, PB, and PV; however, it showed $B_{S}$-type diagrams for PC and PH. $\beta C D$ and $\gamma C D$ showed $B_{S}$-type diagrams with PB and all of the related compounds. Table 1 shows the guest/host ratios of the systems derived from analyses of their phase solubility diagrams. The results indicate that PP, PB, and PV form 1:1 complexes, whereas PC and PH form 1:2 (guest:host) complexes with $\alpha$ CD. Moreover, all of the guest compounds form 1:1 and 2:1 (host:guest) complexes with $\beta$ and $\gamma \mathrm{CD}$, respectively [23]. The apparent stability constants (K), estimated from the initial linear portion of the diagrams, are shown in Table 2. The complex stability trend was $\beta C D>\alpha C D>\gamma C D$ for all the guest compounds except for PP and PB, where the $\alpha$ CD complexes were the most stable. The stability constants for the PP and PB systems agree reasonably with the values from previous reports [20,24]. The apparent stability constants increased as the guest methylene chain length increased. Moreover, there was a strong positive correlation between $\log \mathrm{K}$ and the partition coefficient, $\log \mathrm{P}$, of the compounds (correlation coefficient, $\mathrm{R}^{2}>0.982$ for all the CD systems) (Figure 3a,b). These findings suggest that hydrophobic interactions play a critical role in the stability of the complexes [21].


Figure 2. Phase solubility diagrams of (a) PP-CD; (b) PB-CD; (c) PV-CD; (d) PC-CD; (e) PH-CD systems in 0.1 M phosphate buffer ( pH 2.1 ) at $25^{\circ} \mathrm{C}$. Each point represents the mean $\pm \mathrm{SD}(\mathrm{n}=3)$. Open square; $\alpha C D$, open circle; $\beta C D$, open triangle; $\gamma C D$. Data used to construct (b) are from our previous work [19].

Table 1. Guest/Host ratios of PB and structurally related compounds with the natural CDs derived from analyses of the diagrams from phase solubility studies in 0.1 M phosphate buffer ( pH 2.1 ) at $25^{\circ} \mathrm{C}$.

| Compound | Guest/Host Ratio |  |  |
| :---: | :---: | :---: | :---: |
|  | $\alpha$ CD | $\beta C D$ | $\gamma$ CD |
| PP | $-^{\mathrm{a}}$ | $1.03 \pm 0.08$ | $1.97 \pm 0.18$ |
| PB | $-{ }^{\mathrm{a}}$ | $1.02 \pm 0.05^{\mathrm{b}}$ | $2.14 \pm 0.08^{\mathrm{b}}$ |
| PV | $-{ }^{\mathrm{a}}$ | $0.99 \pm 0.05$ | $2.21 \pm 0.03$ |
| PC | $0.55 \pm 0.03$ | $1.08 \pm 0.01$ | $2.30 \pm 0.03$ |
| PH | $0.44 \pm 0.01$ | $1.02 \pm 0.01$ | $2.20 \pm 0.01$ |

$\overline{\left.{ }^{a} A_{L} \text {-type diagram (guest/host ratio }=1\right) .{ }^{b} \text { Data from our previous work [19]. The values are mean } \pm \mathrm{SD}(\mathrm{n}=3) \text {. } . . . . ~}$

Table 2. Apparent stability constant $(\mathrm{K})$ of PB and structurally related compounds with the natural CDs in 0.1 M phosphate buffer ( pH 2.1 ) at $25^{\circ} \mathrm{C}$.

| Compound | $\mathbf{K ~}^{\left(\mathbf{M}^{-\mathbf{1}}\right)}$ |  |  |
| :---: | :---: | :---: | :---: |
|  | $\alpha \mathbf{C D}$ | $\beta \mathbf{C D}$ | $\gamma \mathbf{C D}$ |
| PP | $226 \pm 5$ | $74 \pm 3$ | $34 \pm 1$ |
| PB | $481 \pm 26^{\mathrm{a}}$ | $178 \pm 23^{\mathrm{a}}$ | $119 \pm 9^{\mathrm{a}}$ |
| PV | $639 \pm 20$ | $838 \pm 52$ | $223 \pm 7$ |
| PC | $1185 \pm 35$ | $2283 \pm 134$ | $499 \pm 59$ |
| PH | $2500 \pm 50$ | $7458 \pm 52$ | $1213 \pm 18$ |

${ }^{\text {a }}$ Data from our previous work [19]. The values are mean $\pm$ SD ( $\mathrm{n}=3$ ).

(a)

(b)


Figure 3. Relationship between (a) $\log \mathrm{K}$ and number ( n ) of $-\mathrm{CH}_{2}$ - groups; (b) $\log \mathrm{K}$ and partition coefficient ( $\log$ P) of PB and structurally related compounds. Each point represents the mean $\pm$ SD $(n=3)$. Log P values were estimated by Chem Bio Draw. Open square; $\alpha C D$, open circle; $\beta C D$, open triangle; $\gamma \mathrm{CD}$ ).

## 2.2. ${ }^{1}$ H NMR Spectroscopy

### 2.2.1. ${ }^{1} \mathrm{H}$ NMR Chemical Shift Changes

Table 3 shows the changes in the chemical shift of PB or related compounds in the presence of equimolar amounts of CDs. The $\alpha$ CD systems mostly showed downfield changes, while the $\beta$ and $\gamma$ CD systems had the opposite effect. This indicates that the guest compounds may have different orientations within the different CD complexes [25]. Furthermore, in the $\beta$ and $\gamma \mathrm{CD}$ systems, the aromatic protons showed larger displacements compared to the alkyl protons, while the opposite was observed in the $\alpha$ CD systems. This suggests that the size of the CD cavity affects the orientation and disposition of the guest
compounds. A certain specificity of CDs with respect to inclusion complex formation has been recognized in the early work of CD research, where the guest molecule must fit at least partially into the CD cavity $[15,26]$. The results indicate that the smaller $\alpha C D$ cavity preferentially includes the alkyl chain of the PB and related compounds and only partially includes the aromatic ring, while both the alkyl chain and the aromatic ring are deeply included in the larger $\beta C D$ and $\gamma C D$ cavities. This assertion is supported by the changes in the chemical shift of the CDs in the presence of equimolar amounts of the guest compounds, as shown in Table 4. Typically, the inner H3' and H5' protons of CDs in inclusion complexes experience shift changes due to the hydrophobic or ring current effect of guest compounds [26]. The H3' proton of $\alpha$ CD showed significant upfield shift changes with all the guest compounds, while the $\mathrm{H}^{\prime}$ proton showed negligible changes with PP, PB, and PV but significant changes with PC. This indicates that PC and PH, which have longer alkyl chains, are more deeply included in the $\alpha \mathrm{CD}$ cavity compared to $\mathrm{PP}, \mathrm{PB}$, and PV [27]. On the other hand, the guest compounds caused upfield shift changes in the $\mathrm{H3}^{\prime}$ and $\mathrm{H}^{\prime}$ protons of both the $\beta$ CD and $\gamma \mathrm{CD}$ systems. However, the changes were more significant in the $\beta C D$ system. This indicates that the guest compounds fit better in the $\beta C D$ cavity despite being included deeply in both CD cavities. However, considering the case with PP and PB, whose $\alpha$ CD complexes were more stable, it is important to note that even though the $\beta C D$ cavity appears to be the most suitable in terms of spatial fit, this does not necessarily imply that the $\beta$ CD complex will be the most stable for all the guest compounds. Other factors, such as the optimization of the host-guest interaction distance and entropic changes, may result in a less optimal fit being more stable [28].

Table 3. Changes in ${ }^{1} \mathrm{H}$ NMR chemical shifts of PB and related compounds $\left(5.0 \times 10^{-3} \mathrm{M}\right)$ in the presence of the natural CDs $\left(5.0 \times 10^{-3} \mathrm{M}\right)$ in 0.1 M sodium borate $/ \mathrm{D}_{2} \mathrm{O}$ at $25^{\circ} \mathrm{C}$.

|  |  |  <br> Change in Chemical Shift, $\Delta \delta$ (with CD - without CD) (ppm) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CD | Compound | A | B | C | D | E | F | X | Y | Z |
| $\alpha \mathrm{CD}$ | PP | 0.010 | 0.006 |  |  |  |  | 0.012 | 0.012 | 0.006 |
|  | PB | 0.028 | 0.026 | 0.002 |  |  |  | 0.020 | 0.020 | - ${ }^{\text {a }}$ |
|  | PV | 0.044 | 0.045 | - ${ }^{\text {a }}$ | -0.025 |  |  | 0.008 | 0.033 | 0.022 |
|  | PC | 0.050 | 0.046 | 0.066 | -0.013 | -0.006 |  | 0.000 | 0.046 | - ${ }^{\text {a }}$ |
|  | PH | 0.041 | 0.044 | 0.096 | -0.015 | 0.009 | 0.004 | -0.022 | 0.061 | 0.040 |
| $\beta$ CD | PP | 0.009 | -0.008 |  |  |  |  | -0.016 | -0.005 | 0.003 |
|  | PB | 0.004 | -0.003 | -0.029 |  |  |  | -0.072 | -0.028 | - ${ }^{\text {a }}$ |
|  | PV | -0.016 | 0.009 | -0.037 | -0.014 |  |  | -0.150 | -0.056 | 0.026 |
|  | PC | -0.032 | -0.007 | -0.061 | -0.019 | -0.015 |  | -0.168 | -0.050 | 0.020 |
|  | PH | -0.054 | -0.023 | -0.086 | -0.028 | -0.029 | -0.001 | -0.188 | -0.049 | 0.034 |
| $\gamma \mathrm{CD}$ | PP | 0.003 | 0.002 |  |  |  |  | -0.001 | 0.001 | 0.002 |
|  | PB | -0.001 | 0.003 | -0.003 |  |  |  | -0.009 | -0.005 | -0.002 |
|  | PV | -0.011 | -0.004 | -0.006 | 0.002 |  |  | -0.026 | -0.006 | 0.000 |
|  | PC | -0.031 | -0.018 | -0.023 | -0.005 | 0.000 |  | -0.047 | -0.008 | -0.001 |
|  | PH | -0.067 | -0.055 | -0.048 | -0.042 | -0.021 | -0.014 | -0.087 | -0.020 | -0.003 |

[^0]Table 4. Changes in ${ }^{1} \mathrm{H}$ NMR chemical shifts of the natural CDs $\left(5.0 \times 10^{-3} \mathrm{M}\right)$ in the presence of PB and related compounds $\left(5.0 \times 10^{-3} \mathrm{M}\right)$ in 0.1 M sodium borate $/ \mathrm{D}_{2} \mathrm{O}$ at $25^{\circ} \mathrm{C}$.

|  |  | Change in Chemical Shift, $\Delta \delta$ <br> (with Compound - without Compound) (ppm) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CD | Proton | PP | PB | PV | PC | PH |
| $\alpha \mathrm{CD}$ | H1 ${ }^{\prime}$ | -0.005 | -0.003 | -0.001 | 0.005 | 0.009 |
|  | H2 ${ }^{\prime}$ | -0.006 | -0.005 | -0.007 | -0.011 | -0.007 |
|  | H3' | -0.016 | -0.025 | -0.032 | -0.053 | -0.060 |
|  | H4' | -0.004 | -0.006 | 0.003 | - ${ }^{\text {a }}$ | - ${ }^{\text {a }}$ |
|  | H5' | 0.001 | 0.008 | 0.003 | -0.014 | - ${ }^{\text {a }}$ |
|  | H6'a | 0.005 | -0.004 | -0.005 | -0.007 | -0.008 |
| $\beta$ CD | H1 ${ }^{\prime}$ | -0.009 | -0.015 | -0.017 | -0.016 | -0.014 |
|  | H2' | 0.001 | -0.006 | -0.009 | -0.011 | -0.008 |
|  | H3' | -0.022 | -0.042 | -0.053 | -0.061 | -0.061 |
|  | H4' | 0.005 | 0.003 | 0.009 | 0.022 | 0.033 |
|  | H5' | -0.063 | -0.122 | -0.172 | -0.206 | -0.211 |
|  | H6'a | 0.009 | -0.004 | -0.021 | -0.032 | -0.040 |
| $\gamma \mathrm{CD}$ | H1 ${ }^{\prime}$ | -0.002 | -0.007 | -0.008 | -0.006 | -0.006 |
|  | H2 ${ }^{\prime}$ | -0.002 | -0.003 | -0.005 | -0.003 | -0.006 |
|  | H3' | -0.004 | -0.006 | -0.008 | -0.016 | -0.028 |
|  | H4' | -0.002 | -0.002 | -0.002 | -0.001 | -0.001 |
|  | H5' | - ${ }^{\text {a }}$ | 0.000 | -0.009 | -0.032 | -0.055 |
|  | H6'a | -0.003 | -0.007 | -0.014 | -0.015 | -0.022 |

${ }^{\text {a }}$ Could not be determined due to overlap with other signals. Chemical shift changes of $\mathrm{H}^{\prime} \mathrm{b}$ protons could not be monitored due to overlap with other signals.

### 2.2.2. Stoichiometry and Inclusion Equilibrium

Figure 4 shows the continuous variation plots for the inclusion complexation of PB and related compounds with the CDs, obtained by monitoring the chemical shift changes of proton $Y$ for the $\alpha C D$ systems and proton $X$ for the $\beta C D$ and $\gamma C D$ systems. The total concentration of the guests and CDs was kept constant at $1.0 \times 10^{-2} \mathrm{M}\left(1.0 \times 10^{-2} \mathrm{M}\right.$ for the PH- $\alpha$ CD system). For the $\alpha$ CD systems (Figure 4a), PP and PB achieved maxima at 0.5 guest/(guest + host) mole fraction, whereas PV, PC, and PH achieved maxima at 0.35 . This suggests a tendency of the stoichiometry to change from 1:1 toward 1:2 (guest:host) as the number of methylene units increases beyond $3(\mathrm{~PB})$. On the other hand, the $\beta C D$ and $\gamma C D$ systems (Figure $4 b, c$ ) achieved maxima at a 0.5 and 0.67 guest/ (guest + host) mole fraction, respectively, for all of the guest compounds. These results confirm that $\beta C D$ and $\gamma C D$ with relatively larger cavity sizes form 1:1 and 2:1 (guest:host) inclusion complexes, respectively, with the guest compounds. The stoichiometry of CD inclusion complexes usually obeys the law of constant proportions, i.e., the binding molar ratio of guest/host are integral with each other. This implies that when a guest molecule is too large to be included in one CD cavity, or the host cavity is too small to form inclusion complexes with a guest molecule, more than one CD is available for the inclusion complexation [15,26]. For instance, Utsuki et al. previously reported that tranilast, a cinnamic acid derivative, forms inclusion complexes of 1:2, 1:1, and 2:1 stoichiometries with $\alpha, \beta$, and $\gamma \mathrm{CD}$, respectively, in aqueous solution [29]. Therefore, the obtained complex stoichiometries of guest compounds with the CDs are consistent with this inclusion complexation behavior.


Figure 4. Continuous variation plots of the ${ }^{1} \mathrm{H}$ NMR chemical shift changes for the inclusion complexation of PB and related compounds with (a) $\alpha \mathrm{CD}$; (b) $\beta \mathrm{CD}$; and (c) $\gamma \mathrm{CD}$ in 0.1 M sodium borate $/ \mathrm{D}_{2} \mathrm{O}$ at $25^{\circ} \mathrm{C}$. The chemical shift of proton Y was monitored for the $\alpha \mathrm{CD}$ systems, whereas proton $X$ was monitored for the $\beta$ and $\gamma C D$ systems. The total concentration of $P B$ (or related compound) and CDs was $1.0 \times 10^{-2} \mathrm{M}\left(2.0 \times 10^{-2} \mathrm{M}\right.$ for the $\mathrm{PH}-\alpha \mathrm{CD}$ system $)$. Closed circle: PP, closed square: PB, open triangle: PV, open circle: PC, open square: PH. Data used to construct the PB plots are from our previous work [19].

Figure 5 shows the chemical shift displacement of PP and PH protons as a function of CD concentration. For the PP- $\alpha$ CD system (Figure 5a), all PP protons shifted downfield regardless of CD concentration. However, for the PH- $\alpha$ CD system (Figure 5d), protons D and X shifted upfield, while E and F shifted downfield at low CD concentrations. Notably, these directions were reversed at higher CD concentrations. These biphasic shift changes could be attributed to the CD concentration-dependent change in stoichiometry of the PH- $\alpha$ CD complex [27]. This supports the earlier assertion that the stoichiometry shifts from 1:1 to 1:2 (guest:host) as the alkyl chain length increases. For the $\beta C D$ systems, proton $A$ was displaced downfield for PP (Figure 5b) but upfield for PH (Figure 5e). This suggests a slight difference in the orientation of the guest compounds within the $\beta C D$ cavity as the alkyl chain length increases from PP to PH [25]. However, no biphasic shift changes were observed in either the PP or PH systems, confirming that the guest compounds, independent of alkyl chain length, form 1:1 complexes with $\beta$ CD. In the $\gamma \mathrm{CD}$ systems, PP protons $X$ and $Y$ shifted downfield at low $C D$ concentrations, but were reversed at higher concentrations (Figure 5c). PH protons A, B, and Y showed similar behavior (Figure 5f). These suggest a CD concentration-dependent change in the stoichiometry of the $\gamma C D$ complexes and confirm that the guest compounds form 2:1 (guest:host) complexes with $\gamma C D$, regardless of the alkyl chain length [27].

The stability constants ( $\mathrm{K}_{1: 1}$ ) of the PH-CD complexes estimated by analyzing the first-order dependences of the chemical shift change of PH protons on CD concentration were $123 \pm 2 \mathrm{M}^{-1}$ (determined from protons A and Y ), $2513 \pm 469 \mathrm{M}^{-1}$ ( A and X ), and $370 \pm 6 \mathrm{M}^{-1}(\mathrm{C}$ and X$)$ for the $\alpha \mathrm{CD}, \beta C D$, and $\gamma \mathrm{CD}$ complexes, respectively. These values represent a 20 -fold reduction for the $\alpha C D$ complex and a 3 -fold reduction for the $\beta C D$ and $\gamma$ CD complexes, compared to the estimated values at pH 2.1 (obtained from phase solubility studies). This indicates that the ionization of PH (free acid) has a greater destabilizing effect on the $\alpha \mathrm{CD}$ complex than on the $\beta \mathrm{CD}$ and $\gamma \mathrm{CD}$ complexes. A possible explanation is that the ionized acid is highly hydrated, making it less compatible with the smaller cavity of $\alpha \mathrm{CD}$ [21].

### 2.2.3. 2D ROESY Spectroscopy

Two-dimensional ROESY studies were conducted on the PH-CD systems to elucidate the inclusion structures of the complexes. Figure 6 shows the partial contour plots of the 2D ROESY spectra of the PH-CD systems. For the $\alpha$ CD system (Figure 6a), correlation peaks were observed between the CD inner $\mathrm{H}^{\prime}$ and $\mathrm{H}^{\prime}$ protons and all the PH protons, except between protons A and B and the $\mathrm{H}^{\prime}$ ' proton. This implies that the alkyl chain of PH is deeply included in the $\alpha$ CD cavity, entering from the secondary hydroxyl end and
traversing the CD cavity, with the carboxylate moiety deposited just outside the primary hydroxyl end of the cavity. This appears reasonable since molecular models indicate that about six methylene groups threaded through a CD cavity essentially fill the cavity [30]. The aromatic ring of PH is deposited around the secondary hydroxyl end of the CD cavity and is shallowly included by a second $\alpha$ CD molecule to form a 1:2 PH- $\alpha$ CD inclusion complex. For the $\beta$ CD system (Figure 6b), correlation peaks between the inner H3' proton and all the PH protons were observed. Additionally, the inner $\mathrm{H}^{\prime}$ protons showed correlation peaks with PH protons B, C, and D. This indicates that the aromatic ring of PH is deeply included in the $\beta C D$ cavity with the alkyl chain bending at the mid-section ( $B, C$, and $D$ ) within the CD cavity. The terminal section (E, F) of the alkyl chain and the carboxylate moiety point back into the CD cavity around the secondary hydroxyl end of the cavity. In the case of the $\gamma \mathrm{CD}$ system (Figure 6 c ), correlation peaks between the inner $\mathrm{H}^{\prime}$ and $\mathrm{H}^{\prime}$ protons of the CD and all of the PH protons were observed. This result suggests that two PH molecules are deeply included in the large $\gamma$ CD cavity, possibly entering from either end of the CD cavity and aligned in an antiparallel or parallel orientation to each other. Considering that host-guest inclusion complex formation is a dynamic process, these two modes of inclusion may exist simultaneously [31].


Figure 5. ${ }^{1} \mathrm{H}$ NMR chemical shift changes of PP and PH as a function of the concentration of $(\mathbf{a}, \mathbf{d}) \alpha C D ;(\mathbf{b}, \mathbf{e}) \beta C D ;$ and $(\mathbf{c}, \mathbf{f}) \gamma \mathrm{CD}$ in 0.1 M sodium borate $/ \mathrm{D}_{2} \mathrm{O}$ at $25^{\circ} \mathrm{C}$. The changes in chemical shifts are expressed as $\Delta \delta=\delta$ with CD $-\delta$ without CD. The concentration of PP was $5.0 \times 10^{-3} \mathrm{M}$ for all CD systems, whereas the concentration of PH was $5.0 \times 10^{-3} \mathrm{M}$ for the $\alpha \mathrm{CD}$ system, and $2.5 \times 10^{-3} \mathrm{M}$ for the $\beta$ and $\gamma \mathrm{CD}$ systems. Proton key: Open triangle: A , open diamond: B , closed triangle: C , closed diamond: D , closed square: E , closed circle: F , open circle: X , open square: Y , checked circle: Z .

### 2.3. Molecular Modeling

To obtain reasonable structural representations of the inclusion complexes of PP and PH with the CDs, molecular modeling was performed. The resulting structures are presented in Figure 7. In the PP- $\alpha$ CD complex (Figure 7a), the alkyl chain and carboxylate moiety are located inside the CD cavity, while the phenyl ring is at the rim of the secondary hydroxyl end. For the PH- $\alpha$ CD complex (Figure 7b), the alkyl chain is inside the CD cavity, with the primary methylene and carboxylate moieties protruding from the primary end of the cavity, while the phenyl ring is located just outside the rim of the secondary end and is
shallowly included by another $\alpha$ CD molecule that approaches with its secondary end. On the other hand, for the $\beta C D$ complexes, PP is included inside the $C D$ cavity with the phenyl ring located towards the secondary end, while the alkyl chain slightly bends within the CD cavity, as shown in Figure 7c. For the PH- $\beta$ CD complex (Figure 7d), both the phenyl ring and alkyl chain of PH are located within the CD cavity, with the phenyl ring oriented towards the primary end of the cavity and the alkyl chain bending significantly and leaving the carboxylate moiety around the secondary rim of the cavity. For the $\gamma$ CD complexes, two inclusion modes each were calculated for PP (Figure 7e,g) and PH (Figure 7f,h), where two molecules of PP or PH are included in the large $\gamma \mathrm{CD}$ cavity in a parallel or antiparallel orientation. The MOE-calculated structures agree reasonably with the results of the NMR spectroscopic studies despite using the unionized forms of the guest compounds for the calculation. The inclusion complex structures of the ionized forms in water may be almost identical to those of the unionized forms using MOE, as shown in the predicted structure of ionized PH with $\beta$ CD in water using the density functional theory (DFT) (Figure S1) [32,33]. This predicted structure appears almost the same as the structure of the unionized form (Figure 7d). The only difference between the two structures is the degree of bending. The unionized form bends more into the CD cavity to increase complex stability.



Figure 6. Partial contour plots of the ROESY spectra of (a) PH- $\alpha$ CD; (b) PH- $\beta$ CD; and (c) PH- $\gamma \mathrm{CD}$ in 0.1 M sodium borate $/ \mathrm{D}_{2} \mathrm{O}$ at $25^{\circ} \mathrm{C}$. The concentration of the guest and the host were $2.5 \times 10^{-2} \mathrm{M} /$ $1.0 \times 10^{-1} \mathrm{M}(\mathrm{PH} / \alpha \mathrm{CD}), 1.5 \times 10^{-2} \mathrm{M} / 2.5 \times 10^{-2} \mathrm{M}(\mathrm{PH} / \beta \mathrm{CD})$, and $2.5 \times 10^{-2} \mathrm{M} / 2.5 \times 10^{-2} \mathrm{M}$ ( $\mathrm{PH} / \gamma \mathrm{CD}$ ).


Figure 7. Possible inclusion structures of $\mathrm{PP}-\mathrm{CD}$ and $\mathrm{PH}-\mathrm{CD}$ complexes estimated by molecular docking model calculation: (a) PP- $\alpha \mathrm{CD}$; (b) PH- $\alpha \mathrm{CD}$; (c) PP- $\beta \mathrm{CD}$; (d) PH- $\beta \mathrm{CD}$; (e) PP- $\gamma \mathrm{CD}$ parallel orientation; (f) PH- $\gamma \mathrm{CD}$ parallel orientation; (g) PP- $\gamma \mathrm{CD}$ antiparallel orientation; and (h) PH- $\gamma \mathrm{CD}$ antiparallel orientation. The relative molecular sizes of the complexes are arbitrary. The green ball and stick represent the guest compound ( PP or PH ). The upper and lower sides of the CDs are the secondary and primary rims, respectively.

## 3. Materials and Methods

### 3.1. Materials

PB, 5-phenylvaleric acid (PV), and 6-phenylcaproic acid (PC) were obtained from Tokyo Chemical Industry Co., Ltd. (Tokyo, Japan). 3-phenylpropionic acid (PP) was purchased from Wako Pure Chemical Industries Ltd. (Osaka, Japan). 7-phenylheptanoic acid (PH) was sourced from Alfa Aesar (Heysham, UK). $\alpha$ CD, $\beta$ CD, and $\gamma$ CD were purchased from Nacalai Tesque Inc. (Kyoto, Japan). All other chemicals were obtained from commercial sources and were of the highest analytical grade.

### 3.2. Methods

### 3.2.1. Phase Solubility Studies

Phase solubility studies were conducted according to the method described by Higuchi and Connors [23]. Briefly, 1 mL of CD solutions ( 0 to $14 \mathrm{mM}, \mathrm{pH} 2.1$ ) were added to excess amounts of PB or related compounds placed in screw cap tubes. The resulting samples were shaken for 72 h at $25^{\circ} \mathrm{C}$ and 120 rpm (Multi Shaker MMS-3020 in a temperature control chamber FMC-1000; Eyela Co., Ltd., Tokyo, Japan). The resulting suspensions were filtered through $0.2 \mu \mathrm{~m}$ membrane filters (Minisart RC 4, Sartorius Stedim Lab Ltd., Stonehouse, UK) and diluted appropriately. The solubility of PB or related compounds was determined by HPLC, and the data were used to construct phase solubility diagrams. The guest/host ratios for the systems showing $\mathrm{B}_{\mathrm{S}}$-type solubility diagrams were estimated as the quotient of the amount of undissolved guest at the start of the plateau region and the CD concentration range corresponding to the plateau region [23]. The stability constants $\left(\mathrm{K}_{1: 1}\right)$ of the interactions, assuming the formation of $1: 1$ complexes, were also calculated according to Equation (1) [23]:

$$
\begin{equation*}
\mathrm{K}_{1: 1}=\frac{\text { Slope }}{\mathrm{S}_{0}(1-\text { Slope })} \tag{1}
\end{equation*}
$$

where $\mathrm{S}_{0}$ is the intrinsic solubility (solubility in the absence of CD) of PB or related compound at $25^{\circ} \mathrm{C}$, and the slope is the slope of the initial linear portion of the respective phase solubility diagrams.

## HPLC Conditions

HPLC measurements were performed according to a previous report using a JASCO HPLC system (Jasco Corp., Tokyo, Japan) [10]. A YMC-PACK ODS AM 303 column ( $5 \mu \mathrm{~m}$, $250 \mathrm{~mm} \times 4.6 \mathrm{~mm}$, YMC Co., Kyoto, Japan) was used as the stationary phase and was maintained at $40^{\circ} \mathrm{C}$. A linear gradient elution system was employed with a mobile phase comprised two solvents, A ( 0.05 M sodium dihydrogen phosphate) and B ( 0.05 M sodium dihydrogen phosphate, and acetonitrile ( $30: 70, v / v)$ ), programmed for PP, PB, and PV as follows: $0-7 \mathrm{~min}(30-100 \%$ B), $7-10 \mathrm{~min}(100 \%$ B), $10-15 \mathrm{~min}(100-30 \%$ B). For PC and PH, the elution program used was $0-7 \mathrm{~min}(50-100 \% \mathrm{~B}), 7-10 \mathrm{~min}(100 \% \mathrm{~B})$, and $10-15 \mathrm{~min}$ $(100-50 \% \mathrm{~B})$ at a constant flow rate of $1 \mathrm{~mL} / \mathrm{min}$. A detection wavelength of 210 nm was used and monitored for 15 min for each sample, with retention times of 7.4, 8.9, 9.6, 9.4, and 10.7 min for PP, PB, PV, PC, and PH, respectively.

### 3.2.2. ${ }^{1} \mathrm{H}$ NMR Spectroscopy

${ }^{1} \mathrm{H}$ NMR spectra were obtained using a JEOL-A500 spectrometer (Tokyo, Japan) operating at 500 MHz in 5 mm sample tubes at $25^{\circ} \mathrm{C}$ using $\mathrm{D}_{2} \mathrm{O} / 0.1 \mathrm{M}$ sodium borate ( pH meter reading of 9.4) as solvent. The resonance at 4.68 to 4.75 ppm , due to residual solvents $\left(\mathrm{H}_{2} \mathrm{O}\right.$ and HOD), was used as an internal reference. Chemical shifts are given as parts per million (ppm), with an accuracy of $\pm 0.001$. No external reference was used to avoid possible interactions with the CDs. The ${ }^{1} \mathrm{H}$ NMR signals of the guests ( PB and related compounds) were assigned by $2 \mathrm{D}{ }^{1} \mathrm{H}-{ }^{1} \mathrm{H}$ correlation spectroscopy (COSY), whereas those of the CDs were assigned according to a previous report [34]. The complex stoichiometries
were determined by the continuous variation method, where the total concentrations of CD and guest were kept constant at $1.0 \times 10^{-2} \mathrm{M}$. In addition, the changes in the chemical shift of CDs and the guest protons in their equimolar systems ( $5.0 \times 10^{-3} \mathrm{M}$ ) were monitored. Due to the low solubility of the longer-chain guest compounds and their CD complexes, a medium of pH 9.4 was used to obtain sufficiently high concentrations of the complexes needed for ${ }^{1} \mathrm{H}$ NMR measurements, particularly for the 2D ROESY NMR, which has a low sensitivity [35]. The CD concentration dependence of the chemical shift changes and stoichiometry of the complexes were studied by performing molar ratio titrations using PP and PH, where the concentration of PP or PH was maintained constant $\left(5.0 \times 10^{-3} \mathrm{M}\right)$ while changing the concentration of the CDs [36]. The stability constant values of the complexes formed by PH were determined from the curves. Two-dimensional ROESY NMR experiments were performed for the CD-PH systems in the phase-sensitive mode using the same spectrometer. Each spectrum consisted of a matrix of F2 by F1 covering a sweep width of 5000 Hz with 36 scans. The spin-lock mixing time was 800 ms , with a relaxation delay of 4 s , and a $90^{\circ}$ pulse width of $11.8 \mu \mathrm{~s}$. The concentration of guest and host were $2.5 \times 10^{-2} \mathrm{M} / 1.0 \times 10^{-1} \mathrm{M}(\mathrm{PH} / \alpha \mathrm{CD}), 1.5 \times 10^{-2} \mathrm{M} / 2.5 \times 10^{-2} \mathrm{M}$ $(\mathrm{PH} / \beta \mathrm{CD})$, and $2.5 \times 10^{-2} \mathrm{M} / 2.5 \times 10^{-2} \mathrm{M}(\mathrm{PH} / \gamma \mathrm{CD})$. The stability constants $\left(\mathrm{K}_{1: 1}\right)$ of the PH-CD complexes were estimated by analyzing the first-order dependences of the chemical shift change of PH protons on CD concentration using Equation (2) [37]:

$$
\begin{equation*}
\delta_{\mathrm{obs}}=\frac{\delta_{0}+\delta_{1} \mathrm{~K}_{1: 1}[\mathrm{CD}]_{\mathrm{f}}}{1+\mathrm{K}_{1: 1}[\mathrm{CD}]_{\mathrm{f}}} \tag{2}
\end{equation*}
$$

where $\delta_{0}$ and $\delta_{\text {obs }}$ are chemical shifts of PH protons without or with CD, respectively, and $\delta 1$ is the chemical shift of PH protons in the 1:1 complex.

The equation was analyzed by the iteration method since the concentration of free $C D\left([C D]_{f}\right)$ is unknown unless $K_{1: 1}$ had been determined beforehand. Moreover, the total CD concentration ( $[C D]_{t}$ ) was not high enough to ignore the concentration of the CDs in complex under the experimental conditions. Therefore, by setting $[C D]_{f}=[C D]_{t}$ as a first approximation, Equation (2) was analyzed by a nonlinear least-squares method, and, in turn, $[C D]_{f}$ values were calculated using the obtained apparent $\mathrm{K}_{1: 1}$ value. This procedure was repeated until the $\mathrm{K}_{1: 1}$ value converged at a constant value.

### 3.2.3. Molecular Modeling

Molecular docking of PP and PH to CDs was performed using the molecular operating environment, MOE version 2019 (Chemical Computing Group Inc., Montreal, QC, Canada) [19]. According to the company's recommendations, the Amber10: EHT force field was used for energy minimization. Crystal structures of CDs were obtained from the Protein Data Bank (PDB entry codes: 5E6Y, 2V8L, and 2ZYK for $\alpha, \beta$, and $\gamma$ CD, respectively) and were used in the molecular docking studies. All ligand molecules in the PDB structures were eliminated for the docking study. Hydrogen atoms were added with the appropriate geometry, and their energies were minimized. The docking of PP and PH as ligands into CDs as receptors was conducted with the default values for the parameters. The docking scores were ranked by the parameter S score which is calculated using the London dG scoring function. A pose with the highest docking score (i.e., the lowest S) was chosen as the optimum docking pose. For the docking of PH to $\alpha$ CD, a molecule of PH was sandwiched by two $\alpha$ CD molecules, considering the most probable inclusion modes estimated by the NMR study. Additionally, for the docking of PP and PH to $\gamma \mathrm{CD}$, two molecules of each compound were inserted consecutively since the hydrophobic cavity of $\gamma \mathrm{CD}$ is large enough to accommodate two molecules, as indicated by the NMR study. DFT calculations were also performed to verify the inclusion complex structures. This is described in the Supplementary Information.

## 4. Conclusions

In this study, the structural chemistry of the CD complexes of PB and its therapeutically relevant, structurally related compounds were analyzed to inform on the choice of CD for addressing the pharmaceutical limitations of these compounds. The study's findings reveal the CD cavity size dependency of the stability, inclusion mode, and stoichiometry of the complexes. The smaller $\alpha$ CD forms more stable and soluble 1:1 complexes with bitter-tasting PB and its foul-smelling shorter-chain derivative (PP). Thus, $\alpha$ CD would be useful for masking their unpleasant organoleptic properties. In contrast, the $\beta C D$ cavity size is ideal for the longer-chain PB-related compounds such as PC and PH, which are poorly soluble viscous oils. $\beta$ CD forms stable 1:1 complexes with these compounds, implying a less bulky formulation compared to $\alpha C D$, which forms less stable 1:2 (guest:host) complexes. Thus, $\beta C D$ would be useful for obtaining free-flowing complex powders of these longer-chain compounds, albeit with limited solubility. $\gamma \mathrm{CD}$ forms less stable 2:1 complexes of limited solubility with all of the compounds and, therefore, would be undesirable for overcoming the limitations of PB and related compounds. These findings using the natural $C D$ s provide the basis for expanding the study to include $C D$ derivatives such as 2-hydroxypropyl- $\beta$ CD and sulfobutylether- $\beta C D$, which are known to form more soluble complexes and may prove more effective for overcoming the limitations of PB and related compounds.

Supplementary Materials: The supporting information can be downloaded at: https:/ /www.mdpi. com/article/10.3390/ijms242015091/s1.
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[^0]:    ${ }^{\text {a }}$ Could not be determined due to overlap with other signals.

