



Article How Does Pseudo-Jahn-Teller Effect Induce the Photoprotective Potential of Curcumin?

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Abstract: In this paper, the molecular and electronic structure of curcumin is studied. High-symmetric gas-phase tautomers and their deprotonated forms in various symmetry groups are identified. The stability of lower-symmetry structures was explained by using the Pseudo-Jahn-Teller (PJT) effect. This effect leads to stable structures of different symmetries for the neutral enol and keto forms. The presented analysis demonstrated the potential significance of the PJT effect, which may modulate the setting of electronic and vibrational (vibronic) energy levels upon photodynamic processes. The PJT effect may rationalize the photoprotection and activity of naturally occurring symmetric dyes.

Keywords: DFT; natural compounds; tautomers; molecular symmetry; electron transitions

1. Introduction

Symmetry represents a fundamental concept in physics, chemistry, and biology. Molecular symmetry explains various physical and chemical properties of compounds, and their toxicity. There are few types of biomolecules in plants and fungi that are symmetric. It is a well-known fact that high-symmetric xenobiotics may perform a negative role in living systems. For example, benzene, pyrene, or the next polycyclic hydrocarbons are highly carcinogenic [1]. If an aromatic entity is necessary in some biochemical processes, the symmetry is lowered by substituting side chains using, e.g., an alkyl, acetate, hydroxyl, alkoxy, vinyl, or acetate group. Cyclic compounds derived from symmetric tetrapyrrole porphin can be mentioned in this connection [2].

Curcumin (diferuloylmethane) has an interesting position among symmetric organic molecules in plants. This yellow pigment of turmeric (*Curcuma longa*) has been found to have antioxidant, antibacterial, anti-inflammatory, and antitumor activity in a variety of animal models of human diseases [3–5]. Curcumin has already entered clinical trials, which have demonstrated its high-dose nontoxicity and exhibited poor bioavailability in humans [6]. More recently, several studies have examined the protective effects of curcumin against skin carcinogenesis caused by chronic UV irradiation [7,8]. These are related to the diarylheptanoids structure, which consists of two aromatic rings (aryl groups) joined by a seven-carbon chain (heptane) and having various substituents. Its diketone tautomer (1E,6E)-1,7-bis(4-hydroxy-3-methoxyphenyl)hepta-1,6-diene-3,5-dione exists in keto-keto forms (Figure 1a,b) in water and in enol-keto forms (Figure 1c,d) in organic solvents [9–11]. Enols are readily deprotonated to form enolates (Figure 1e,f). Due to its hydrophobic nature, curcumin is poorly soluble in water, slightly soluble in aliphatic or alicyclic organic solvents, but easily soluble in polar organic solvents [12]. Interestingly, the solid phase [13] contains only the enol-keto tautomeric form, which can form polymorphic crystals [14].



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Figure 1. M062X/cc-pVDZ optimized curcumin structures of C_{2v} group of the neutral diketo forms (**a**,**b**), neutral enol forms (**c**,**d**), and anionic enolate forms (**e**,**f**) (C—black, O—red, H—white).

The effect of curcumin on acute photo-damage induced by higher dose UV irradiation is still unclear. In principle, its mechanism can be based on fluorescence, phosphorescence, and/or nonradiative transitions. In general, several parallel processes may be included in a photoprotectivity action. Upon the absorption of a high-energy dose, a low-energy photon may be generated because of the luminescence. Alternatively, the excited-state curcumin can interact with the highly reactive singlet oxygen molecule with the subsequent formation of the less reactive triplet oxygen molecule [15]. Such processes require the appropriate setting of energy levels of electronic and vibration (vibronic) states. From a theoretical point of view, the (Pseudo)-Jahn-Teller effect (PJTE) can particularly modulate these energy levels of symmetric compounds. Contrary to the classical Jahn-Teller effect (JTE) describing the vibronic interaction between degenerate electronic states, the PJTE is related to the vibronic interaction between two pseudo-degenerate electronic states. In some cases, the vibronic interaction within excited electronic states can be so strong that the energy surface of the lower state penetrates the ground-state adiabatic potential surface (APS) producing additional (global) minima in which the system is distorted. Such a situation is denoted as hidden JTE (for degenerate excited state) or hidden PJTE (for pseudo-degenerate excited states) [16]. The hidden JTE was first demonstrated in the structure and properties of the ozone molecule [17]. The electronic ground state of this molecule in a high-symmetry regular triangular geometry is non-degenerate. Its excited double-degenerate electronic E state produces three equivalent lower-energy APS minima, in which the configuration of the molecule is obtuse triangular.

(P)JTE is responsible for a variety of phenomena in chemical reactivity, spectroscopy, stereochemistry, crystal chemistry, molecular, and solid-state physics, and materials sci-

ence [18]. This effect has been demonstrated for a variety of metal complexes, inorganic, and organic compounds of different sizes [19–23]. In this context, we can mention the research of photosynthetic conversion of water to molecular oxygen in Photosystem II occurring in cyanobacteria, algae, and plants. The photosynthetic process is catalyzed by the inorganic Mn₄CaO₅ cluster, where the orientation of the Mn^{III} bonding is ascribed to the orientational pseudo-Jahn-Teller isomerism [24]. However, we have not found any research in the literature on this treatment of naturally occurring dyes to date.

With respect to the facts mentioned above, we decided to present the theoretical DFT (Density functional theory) [25,26] calculations of curcumin tautomers (see Figure 1). This molecule represents a suitable model of a symmetric natural dye molecule where the PJTE can appear. The partial aims of this study are systematic geometry optimization of the gas-phase structures in various symmetric groups and an explanation of their stable structures of lower symmetry using PJTE treatment. Finally, the theoretical results for optical spectra will be compared with the available experimental data. The possible photoprotective role of curcumin tautomers will be discussed.

2. Theory

According to the Jahn-Teller (JT) theorem [27], a non-linear configuration of atomic nuclei in a degenerate electron state is unstable. It implies the existence of at least one stable nuclear configuration of lower symmetry where the electron degeneracy is removed. An analytical formula for the APS of such systems can be obtained using a perturbation theory, and the atomic coordinates of the corresponding stable systems are evaluated by its minimization [28]. For large systems, this analytical formula for APS description is too complicated to be solved. In such a case, a group-theoretical treatment is used to predict the symmetry of the stable structures. Subsequently, geometry optimization within the predicted symmetry group is performed using any quantum-chemical method.

The method of step-by-step symmetry descent [29,30] is based on consecutive splitting of the degenerate electron state (i.e., its multidimensional irreducible representation) of a parent 'unstable' symmetry group simultaneously with the removal of symmetry elements. As the non-degenerate electron state (i.e., its one-dimensional irreducible representation) of an immediate subgroup is obtained, this is denoted as 'stable', and any further symmetry descent stops. Various symmetry descent paths are possible because no or only partial splitting might be obtained by symmetry descent to some immediate subgroups.

The epikernel principle method [31,32] represents an alternative treatment. It is based on the Jahn-Teller active distortion coordinate Q of Λ representation for a degenerate electron state Ψ of Γ representation within the parent symmetry group. Λ must belong to the non-totally symmetric part of the symmetrized direct product of Γ as implied by a non-vanishing value of $\langle \Psi | \frac{\partial \hat{H}}{\partial Q} | \Psi \rangle$ integrals, where \hat{H} denotes Hamiltonian. Thus, the following relation must be valid:

$$\Lambda \in [\Gamma \otimes \Gamma] \tag{1}$$

Totally symmetric vibrations ($\Lambda = A$, A_1 , A_{1g} , or A') do not change the symmetry of the system, and so the corresponding coordinates are not denoted as JT active. If the molecule of a symmetry group G undergoes the distortion Q of Λ representation, the molecule adopts the symmetry of its kernel or epikernel subgroup. The kernel subgroup K(G, Λ) of the parent group G for the Q coordinate of Λ representation is the minimal group that contains symmetry operations of G that leave the Λ representation invariant (i.e., with the same characters as the identity operation). The epikernel subgroup E(G, Λ) of the parent group G for the degenerate Q coordinate of the multidimensional Λ representation contains symmetry operations of the group G that leave the Λ representation invariant in a part of the distortion space (i.e., some components of this representation). In other words, epikernels are intermediate subgroups between the parent group and the kernel group. According to the epikernel principle, extremum points on a JT energy surface correspond to the kernels and epikernels of the parent group. As a rule, stable APS minima correspond to maximal epikernel symmetry. As this method is based on the perturbation theory with the linear terms of the Taylor expansion of the perturbation operator, $\left(\frac{\partial \hat{H}}{\partial Q}\right)\Delta Q$, it includes the most essential terms only and cannot predict the symmetries of all stable structures, e.g., groups containing C₅ rotations [30].

Similar instability may be observed for pseudodegenerate electronic states. Sufficiently strong vibronic coupling between any two non-degenerate electronic states (often ground and excited) with an energy gap between them, which leads to instability and distortion of the polyatomic configuration, is known as the PJTE [22,28]. In the simplest case of two interacting electronic states Ψ_1 and Ψ_2 of different space symmetries, we obtain their APS in the form:

$$E(Q) = \frac{1}{2}KQ^2 \pm \left[\frac{\Delta^2}{4} + F^2Q^2\right]^{1/2}.$$
(2)

where *E* is the energy of the electronic state, *Q* is the distortion coordinate, Δ is the energy difference between the two electronic states in the undistorted geometry, *K* is the primary force constant (without vibronic coupling), and *F* is the vibronic coupling constant. If energy difference:

$$\Delta < 2\frac{F^2}{K} \tag{3}$$

the curvature of the lower state is negative, which implies instability in the Q direction. Otherwise, Q = 0 for the stable structure and its symmetry is preserved despite the APS curvature being lowered (but positive). We cannot predict the maximal energy difference Δ between pseudodegenerate electronic states that cause the instability of PJT because it depends on the strength F of their mutual coupling (in relation to the K value), which depends on the system under study. The PJT interaction decreases with Δ and is restricted to the states of the same spin multiplicity only (because of the orthogonality of the spin states). In principle, PJT interactions (despite being very weak) are possible in any system of atomic nuclei, but PJTE is considered only in such systems where its consequences (in spectra, structure, reactivity, etc.) are observed.

The epikernel principle method [31,32] can be used to predict the symmetry of the stable structures due to PJTE. In this case, the symmetry Λ of the JT active coordinate Q for non-vanishing values of $\langle \Psi_1 | \frac{\partial \hat{H}}{\partial Q} | \Psi_2 \rangle$ integrals are defined as:

$$\mathbf{A} \in \Gamma_1 \otimes \Gamma_2 \tag{4}$$

where Γ_1 and Γ_2 are representations of electronic states Ψ_1 and Ψ_2 , respectively, in the unperturbed parent geometry [33], see Table S1.

Δ

3. Results

The highest identified possible structure of curcumin is that of C_{2v} symmetry group. We studied its symmetric neutral keto-keto (I) and enol-keto (II models) forms, and anionic enolate (III) forms. PJTE is connected with a symmetry decrease, so it cannot be observed in nonsymmetric molecules (C₁ symmetry group). The PJT symmetry descent $C_s \rightarrow C_1$ or $C_2 \rightarrow C_1$ is too simple and often can be considered as the final parts of more complex PJTE within their C_{2v} supergroup. Therefore, we investigate the C_{2v} symmetry containing the alkene linker in an all-trans configuration with both 4-hydroxy-3-methoxyphenolic groups either in anti- (Ia, IIa, and IIIa models) or in syn- (Ib, IIb, and IIIb models) conformations of methoxyl and central C-O groups. Geometry optimizations of these systems began in the C_{2v} symmetry group. Subsequently, their geometries were reoptimized within its C_2 , C_s , and C_1 subgroups. The obtained structures are briefly presented in Table 1 and visualized in Figure 1 and Figure S1 in Supplementary materials. The electronic excited states for every optimized geometry were evaluated, and the first five lowest energy transitions are collected in Table 2. Equation (2) for PJT interaction is based on a perturbation principle, so we can suppose that the oscillator strengths f for the electron transitions between corresponding electron states in the parent group and its subgroups do not change significantly during

PJT symmetry decrease. Thus, we use the *f* values to identify the corresponding excited states in the subgroups.

Table 1. Selected structural data and relative DFT energies (in kJ/mol) of optimized molecules for different electronic states. Stable structures are indicated by bold text. The dihedral angles (in degrees) are denoted by Greek symbols, distances d are in Å.

Model	Form	C=O vs. OCH ₃ Conformation	Group	State	DFT Energy	Imaginary Vibration	Θ(OC-CO) (Central)	Ω (H ₃ CO-OCH ₃)	d(O-H) (Central)
Ia	keto-keto	anti, anti	C _{2v}	X^1A_1	0.00	a ₂	0.0	0.0	-
			C ₂	X ¹ A	-19.88	-	-111.1	-155.0	-
Ib	keto-keto	syn, syn	C_{2v}	X^1A_1	-0.24	a ₂	0.0	0.0	-
			C ₂	X ¹ A	-28.15	-	167.7	179.4	-
IIa	enol-keto	anti, anti	C_{2v}	X^1A_1	-38.12	b_1	0.0	0.0	1.289 (2×)
			Cs	X^1A'	-59.73	-	0.0	0.0	1.023 1.522
			Cs	$1^1 A''$	-26.81	a″	0.0	0.0	0.969 1.913
			C1	X ¹ A	-45.50	-	0.7	38.9	1.029 1.499
IIb	enol-keto	syn, syn	C_{2v}	X^1A_1	-36.78	b_1	0.0	0.0	1.289 (2×)
			Cs	X^1A'	-58.42	-	0.0	0.0	1.023 1.521
			Cs	$1^1 A''$	-25.47	a″	0.0	0.0	0.969 1.915
			C1	X ¹ A	-48.18	-	0.3	6.5	1.030 1.493
IIIa	enolate	anti, anti	C_{2v}	X^1A_1	1438.35	-	0.0	0.0	-
IIIb	enolate	syn, syn	C_{2v}	X^1A_1	1441.61	-	0.0	0.0	-

Table 2. Symmetry group/electronic ground state (GS), excitation energies (E_{exc}) in eV and oscillator strengths (f) in atomic units for the corresponding electron transitions of the excited states for the optimized structures in relevant electron states (PJT active electron states in bold).

Model	Group/GS	Excited el. State	E _{exc}	f	Group/GS	Excited el. State	Eexc	f
Ia	C_{2v}/X^1A_1	$1^{1}B_{1}$	3.443	0.00	C_2/X^1A	1^1B	3.616	0.00
		1^1A_2	3.621	0.00		1^1A	3.688	0.01
		$1^{1}B_{2}$	4.191	1.38		$2^{1}B$	4.154	1.39
		$1^{1}A_{1}$	4.378	0.13		2^1 A	4.340	0.10
		$2^{1}B_{2}$	4.900	0.08		$3^{1}B$	4.714	0.00
Ib	C_{2v}/X^1A_1	$1^{1}B_{1}$	3.441	0.00	C_2/X^1A	1^1B	3.484	0.02
		1^1A_2	3.621	0.00		1^1A	3.699	0.00
		$1^{1}B_{2}$	4.171	1.34		$2^{1}B$	3.960	0.91
		$1^{1}A_{1}$	4.353	0.13		$2^{1}A$	4.190	0.32
		$2^{1}B_{2}$	4.867	0.02		$3^{1}B$	4.813	0.01
IIa	C_{2v}/X^1A_1	$1^{1}B_{1}$	3.388	1.75	$C_s(\sigma_v)/X^1A'$	$1^1 A'$	3.475	1.81
		$1^{1}B_{2}$	4.048	0.00		$1^1 A''$	3.850	0.00
		$1^{1}A_{1}$	4.164	0.07		$2^{1}A'$	4.159	0.08
		$2^{1}B_{1}$	4.472	0.07		$3^1A'$	4.610	0.02
		2^1A_1	4.770	0.00		$4^{1}A'$	4.792	0.00
IIa	$C_s/1^1 A''$	$1^1 A'$	3.371	1.77	C_1/X^1A	1^1A	3.446	1.40
		$1^1 A''$	3.217	0.00		2^1 A	3.884	0.00
		$2^1 A'$	3.957	0.13		3 ¹ A	4.177	0.19
		$3^1A'$	4.551	0.02		$4^{1}A$	4.583	0.05
		$4^1 A'$	4.687	0.01		5^1A	4.797	0.00
IIb	C_{2v}/X^1A_1	$1^{1}B_{1}$	3.372	1.78	$C_s(\sigma_v)/X^1A'$	$1^1 A'$	3.459	1.83
		$1^{1}B_{2}$	4.044	0.00		$1^1 A''$	3.848	0.00
		$1^{1}A_{1}$	4.120	0.07		$2^{1}A'$	4.118	0.07
		$2^{1}B_{1}$	4.441	0.04		$3^{1}A'$	4.593	0.01
		2^1A_1	4.790	0.00		$4^{1}A'$	4.800	0.01
IIb	$C_{s}/1^{1}A''$	$1^1 A'$	3.352	1.80	C_1/X^1A	1^1A	3.424	1.48
		$1^{1}A''$	3.216	0.00		2^1 A	3.892	0.00
		$2^1 A'$	3.916	0.11		$3^{1}A$	4.149	0.17
		$3^1A'$	4.536	0.02		$4^{1}A$	4.573	0.05
		$4^1 A'$	4.695	0.02		5^1A	4.810	0.00
IIIa	C_{2v}/X^1A_1	$1^{1}B_{2}$	2.952	0.00				
		$1^{1}B_{1}$	3.045	0.72				
		$1^{1}A_{2}$	3.612	0.00				
		$1^{1}A_{1}$	3.637	0.01				
		$2^{1}B_{1}$	4.404	0.00				
IIIb	C_{2v}/X^1A_1	$1^{1}B_{2}$	2.955	0.00				
		$1^{1}B_{1}$	3.056	0.79				
		$1^{1}A_{2}$	3.621	0.00				
		$1^{1}A_{1}$	3.680	0.00				
		$2^{1}B_{1}$	4.373	0.02				

In the case of curcumin keto–keto forms **Ia** and **Ib**, we have found unstable geometries of C_{2v} symmetry with a single imaginary a_2 vibration and stable C_2 symmetry geome-

tries without any imaginary vibration that correspond to their kernel subgroup (Table S1, Figure S2 in Supplementary materials). This symmetry descent can be explained by the PJT vibronic interaction between the ground electron state X^1A_1 and the second excited state 1^1A_2 within the C_{2v} symmetry. Due to symmetry reasons (see Table S2), this electronic state corresponds to the second excited state 1^1A within the C_2 symmetry with an increased energy difference between both pseudo-JT interacting states, as proved by the corresponding excitation energy (see Table 2). This relation is confirmed by similar oscillator strengths corresponding to both excited states within structures of different symmetries. The **Ib** form is more stable and its pseudo-JT stabilization energy is higher as well (see Table 1).

Geometry optimization of curcumin enol forms IIa and IIb leads to unstable structures of symmetry C_{2v} with a single imaginary b_1 vibration (Figure S3 in Supplementary materials), which corresponds to the movement of central enolic hydrogen to oxygen, and stable geometries of C_s and C_1 without imaginary vibrations (Table 1). The C_s symmetry group with the preserved σ_v mirror plane, which coincides with the molecular plane of curcumin and is denoted as $C_s(\sigma_v)$, corresponds to the kernel group $K(C_{2v}, b_1)$ (Table S1 in Supplementary materials). This symmetry descent can be ascribed to the PJT vibronic interaction between the ground electron state X^1A_1 and the first excited state 1^1B_1 within the C_{2v} symmetry (see Table 2 and Equation (3)). Due to symmetry reasons (see Table S2 in Supplementary materials), this electron state corresponds to the first excited state $1^{1}A'$ within the C_s symmetry group, in agreement with similar oscillator strengths for electron transitions and increased energy difference between the electronic states X¹A' and 1¹A' in this group compared to the energy difference between the states X^1A_1 and 1^1B_1 within the C_{2v} group (see excitation energies in Table 2). An analogous PJT interaction between $X^{1}A_{1}$ and $2^{1}B_{1}$ within the C_{2v} group is also possible, but should be much weaker due to their higher energy difference. The JT stabilization energies ($E_{\rm IT}$) of the **IIa** and **IIb** models (Table 3) are the same, although the **IIa** model is slightly more stable (Table 1). These energies are comparable to the values published for Si₃, CuF₃, and CuO₆ [34] or C_{60}^{3-} [35]. Moreover, our results confirm that the enol-keto forms are more stable than the keto-keto forms, which is in agreement with the literature data [36].

Table 3. PJT stabilization energies E_{JT} for the relevant electron states of the stable optimized structures of JT subgroups related to the ones of their parent groups and electron states (the preserved σ_v mirror plane is coincident with the curcumin molecular plane).

M- 1-1	Parei	nt Group	Su	E _{JT}	
Model	Symmetry	Electron State	Symmetry	Electron State	/eV
Ia	C _{2v}	X^1A_1	C ₂	X^1A	0.206
Ib	C_{2v}	X^1A_1	C ₂	X^1A	0.289
IIa	C_{2v}	X^1A_1	$C_s(\sigma_v)$	X^1A'	0.224
	Cs	$1^1 A''$	C1	X^1A	0.194
IIb	C_{2v}	X^1A_1	$C_s(\sigma_v)$	X^1A'	0.224
	Cs	$1^1 A''$	C ₁	X^1A	0.235

The ground-state DFT energies of the C_1 symmetry structures of the **IIa** and **IIb** model systems are higher than those of the C_s ones. Their existence can be explained by the PJT interaction between the excited electron states of the C_s symmetry structures (hidden JT effect [14]). The geometry optimization of both model systems of C_s symmetry in their second excited state $1^1A''$ leads to the structures with a single imaginary vibration of a'' symmetry (Figure S4 in the Supplementary materials). As C_1 is its kernel subgroup K(C_s , a''), it can be explained by the PJT interaction between $1^1A''$ and near A' excited electron states within the C_s symmetry group. This is most probable with the $1^1A'$ state because their energy order is reversed compared to C_s/X^1A' optimized structures, and their energy difference in the C_1 symmetry structure increased most of all. The JT stabilization energy for the **IIa** model is lower, despite its higher stability compared to the **IIb** one. We have found

curcumin enolate structures **IIIa** and **IIIb** of C_{2v} symmetry only without any imaginary frequency. Therefore, the pseudo-JT effect in these systems is too weak (lower vibronic coupling constant *F* and/or higher primary force constant *K* values) to be observed, despite the much lower excitation energies than in the keto–keto and enol–keto forms of curcumin (a much lower Δ value is demanded according to Equation (3)).

The experimental absorption spectrum of the curcumin enol-keto forms recorded in acetonitrile and methanol exhibits a broad band with maximum absorbance peaks at 418 nm (2.97 eV) and 422 nm (2.94 eV) [12], respectively, which could be assigned to low $\pi \rightarrow \pi^*$ excitations [37]. The values of the calculated gas-phase TD-M062X excitation energies corresponding to the $S_0 \rightarrow S_1$ transitions for **IIa** and **IIb** (see Table 2) are overestimated by approximately 0.5 eV. The TD-B3LYP(SMD = water)/aug-cc-pVDZ//M062X/cc-pVDZ electron transitions for the studied forms (see Tables S3-S6) exhibit lower excitation energies related to the TD-M062X ones. For example, the calculated energies of 2.73 eV (454 nm) and 2.70 eV (459 nm) for the C_s symmetry are in better agreement with the available experiment for the enol-keto forms (see Figure 2). The experimental spectrum for keto-keto forms Ia and **Ib** measured in aqueous solution [38] also shows a single peak at 340 nm (3.65 eV). In this case, minimal differences between experiment and theory were found for the third and fourth TD-B3LYP electron transitions with high oscillator strengths, i.e., 373 nm (3.33 eV) and 417 nm (2.97 eV), respectively. In organic solvents under strong basic conditions, the deprotonated sample absorbs at a longer wavelength with a broad peak at \approx 480 nm [39]. The predicted corresponding excitation energies are 410 nm (3.02 eV) and 412 nm (3.01 eV) for IIIa and IIIb, respectively.



Figure 2. TD-B3LYP(SMD = water)/aug-cc-pVDZ//M062X/cc-pVDZ absorption wavelengths and oscillator strengths predicted for models **Ia** (C_2 symmetry), **Ib** (C_2 symmetry), **IIa** (C_s symmetry), and **IIb** (C_s symmetry). The size of the square symbols reflects the oscillator strength.

Useful information on the electronic structure of enol–keto and keto–keto tautomers could be deduced from the analysis of molecular orbitals that contribute to the lowest electronic transition with significant oscillator strength. The calculated frontier orbital distributions for the selected structures, computed at the B3LYP(SMD = water)/aug-cc-pVDZ//M062X/cc-pVDZ level with an iso-value of 0.05 atomic units, are presented in Figures 3–5. In the case of keto–keto forms, the electron clouds are either delocalized only

over one-half of the molecular length (see **Ia**) or well separated (see **Ib**). For enol–keto forms, the electrons are excited from the enolic part to the center. Interestingly, enolic **IIIa** and **IIIb** forms have significant differences in the shapes of the HOMO orbitals. All the depicted transitions have a $\pi \rightarrow \pi^*$ character.



Figure 3. TD-B3LYP(SMD = water)/aug-cc-pVDZ//M062X/cc-pVDZ electron transition forming $2^{1}B$ state of curcumin keto-form **Ia** (**a**) and **Ib** (**b**) of C₂ group. The depicted orbital isosurface is 0.05 a.u. The oscillator strengths (in atomic units) are in parentheses.



Figure 4. TD-B3LYP(SMD = water)/aug-cc-pVDZ//M062X/cc-pVDZ electron transition forming 1^{1} A' state of curcumin keto-form **Iia** (**a**) and **Iib** (**b**) of C_s group. The depicted orbital isosurface is 0.05 a.u. The oscillator strengths (in atomic units) are in parentheses.





4. Methods

Gaussian16 software was used for all quantum-chemical calculations [40]. Geometries of various forms of curcumin in singlet ground or excited states were optimized within C_{2v} , C_2 , C_s , or C_1 symmetries using the M062X hybrid functional [41] with standard cc-pVDZ basis sets for all atoms from the Gaussian library. The stability of the obtained geometry was checked by vibrational analysis in the absence of imaginary vibrations. The Time-dependent DFT (TD-DFT) treatment [42,43] for up to 30 vertical electronic states was used for excited state calculations. For comparison, optical transitions were also calculated using the 3-parameter hybrid B3LYP functional [44] with standard aug-cc-pVDZ basis sets for all atoms of the Gaussian library in aqueous solutions within an SMD solvent model approximation (denoted as TD-B3LYP(SMD = water)/aug-cc-pVDZ//M062X/cc-pVDZ) [45]. MOLDRAW software [46] was used for geometry manipulation and visualization purposes. Molecular orbitals were drawn using Molekel software [47].

5. Conclusions

The systematic theoretical study of symmetric curcumin tautomers was performed using the hybrid functional granting reliable results on the structure of organic compounds in our previous studies. According to Jacquemin and Adamo [48], this functional is a reasonable choice for computation of long oligomers with alternating bond lengths. The symmetry point groups were identified for the investigated keto–keto, enol–keto, and enolate forms. Based on the normal mode analysis, unstable geometries with corresponding symmetries were determined. The indicated symmetry descent was ascribed to the PJT vibronic interaction between the ground electron state and the selected excited states.

It can be expected that the use of other DFT functionals—with or without dispersion correction—should not cause any qualitative differences in our conclusions. The discrep-

ancy between M062X and B3LYP in describing electronic excitation with a small amount of charge transfer character is well known. The computed wavelengths are systematically guided by the percentage of exact exchange included at intermediate interelectronic distances [49].

However, solvent-effect inclusion improves the agreement of TD-DFT results with experimental electron spectra, but forbids our treatment that uses imaginary vibrations of PJT unstable structures to predict the symmetry of PJT active electronic states. Polarizable continuum models create the solute cavity via a set of overlapping spheres that are approximated by polyhedron with non-vanishing edges. Due to inconsistency of the symmetry of such cavities with the molecular symmetry (especially for large molecules), additional imaginary vibrations are produced if the molecular symmetry is to be preserved during geometry optimization within integrals and their derivatives evaluation (keyword Symmetry) [40].

The photobiological action of curcumin can be elucidated by the deactivation mechanisms of its first excited singlet state with intramolecular proton transfer between the enol and keto moiety as the leading nonradiative deactivation pathway [50]. Our theoretical results demonstrated the potential significance of the PJT effect, which may modulate the setting of electronic and vibration (vibronic) energy levels upon photodynamic processes. We have shown that this effect leads to stable structures of the different symmetries of enol and keto forms. This might significantly affect the deactivation rate. Although our study does not directly address photodynamics and related photoprotection problems, the results obtained may rationalize the photoprotection action and activity of naturally occurring dyes. Our findings open new ways of studying and understanding the photodynamic processes of (quasi)symmetric organic molecules in plants and fungi. Further experimental and theoretical studies in this field are needed.

Supplementary Materials: The following supporting information can be downloaded at: https://www.action.com/actionals //www.mdpi.com/article/10.3390/molecules28072946/s1, Table S1: Kernel groups $K(\Gamma, \Lambda)$ of the parent groups Γ for active coordinates of Λ symmetry; Table S2: Relations between the irreducible representations Λ_0 of the parent group Γ_0 and the irreducible representations Λ_1 of its 1st order subgroups Γ_1 ; Table S3: (a) TD-M062X/cc-pVDZ electron transitions of stable keto-keto forms (model Ia and Ib) of C₂ symmetry, (b) TD-B3LYP(SMD=water)/aug-cc-pVDZ//M062X/cc-pVDZ electron transitions of stable keto-keto forms (model Ia and Ib) of C₂ symmetry; Table S4: (a) TD-M062X/cc-pVDZ electron transitions of stable enol-keto forms (model IIa and IIb) of C₅ symmetry, (b) TD-B3LYP(SMD=water)/aug-cc-pVDZ//M062X/cc-pVDZ electron transitions of stable enol-keto forms (model IIa and IIb) of C_s symmetry; Table S5: (a) TD-M062X/cc-pVDZ electron transitions of stable enol-keto forms (model **IIa** and **IIb**) of C₁ symmetry, (b) TD-B3LYP(SMD=water)/aug-ccpVDZ/M062X/cc-pVDZ electron transitions of stable enol-keto forms (model IIa and IIb) of C_1 symmetry; Table S6: (a) TD-M062X/cc-pVDZ electron transitions of stable anionic enolate forms (model IIIa and IIIb) of C_{2V} symmetry, (b) TD-B3LYP(SMD=water)/aug-cc-pVDZ//M062X/ccpVDZ electron transitions of stable anionic enolate forms (model IIIa and IIIb) of C_{2V} symmetry; Figure S1: M062X/cc-pVDZ optimized curcumin structures of C_1 , C_2 and C_s groups of the neutral diketo forms (a,b), and neutral enol forms (c-f); Figure S2: Pseudo-JT active vibration of a_2 symmetry in curcumin keto-forms Ia (left) and Ib (right) of C_{2v} group; Figure S3: Pseudo-JT active vibration of b₁ symmetry in curcumine enol-forms IIa (left) and IIb (right) of C_{2v} group; Figure S4: Pseudo-JT active vibration of a" symmetry in curcumine enol-forms **IIa** (left) and **IIb** (right) of C_s group. Reference [32] is cited in the supplementary materials.

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