



^{Article} ¹H NMR Study of the HCa₂Nb₃O₁₀ Photocatalyst with Different Hydration Levels

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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Abstract: The photocatalytic activity of layered perovskite-like oxides in water splitting reaction is dependent on the hydration level and species located in the interlayer slab: simple or complex cations as well as hydrogen-bonded or non-hydrogen-bonded H₂O. To study proton localization and dynamics in the HCa₂Nb₃O₁₀·yH₂O photocatalyst with different hydration levels (hydrated— α -form, dehydrated— γ -form, and intermediate— β -form), complementary Nuclear Magnetic Resonance (NMR) techniques were applied. ¹H Magic Angle Spinning NMR evidences the presence of different proton containing species in the interlayer slab depending on the hydration level. For α -form, HCa₂Nb₃O₁₀·1.6H₂O, ¹H MAS NMR spectra reveal H₃O⁺. Its molecular motion parameters were determined from ¹H spin-lattice relaxation time in the rotating frame (T_{10}) using the Kohlrausch-Williams-Watts (KWW) correlation function with stretching exponent $\beta = 0.28$: $E_a = 0.210(2)$ eV, $\tau_0 = 9.0(1) \times 10^{-12}$ s. For the β -form, HCa₂Nb₃O₁₀·0.8H₂O, the only ¹H NMR line is the result of an exchange between lattice and non-hydrogen-bonded water protons. $T_{10}(1/T)$ indicates the presence of two characteristic points (224 and 176 K), at which proton dynamics change. The γ -form, HCa₂Nb₃O₁₀·0.1H₂O, contains bulk water and interlayer H⁺ in regular sites. ¹H NMR spectra suggest two inequivalent cation positions. The parameters of the proton motion, found within the KWW model, are as follows: $E_a = 0.217(8) \text{ eV}$, $\tau_0 = 8.2(9) \times 10^{-10} \text{ s}$.

Keywords: layered perovskite-like niobate; Dion-Jacobson phase; proton NMR

1. Introduction

In recent years, layered perovskite-like oxides have attracted much attention because of their outstanding physical and chemical properties, including high-temperature superconductivity [1,2], colossal magnetoresistance [3], the capability of photocatalytic water decomposition under sunlight irradiation for further hydrogen storage [4,5], and ionic conductivity due to high mobility of interlayer cations [6,7]. The majority of ion-exchangeable layered perovskite-like oxides can be converted into their protonated forms, which, besides being proton conductors [6,8] and photocatalysts for water splitting [9–11], exhibit the ability to intercalate water [10–14] and other molecules [15,16] and/or to form graft derivatives [16–19] susceptible to further exfoliation [10,20,21].

The hydrated form of HCa₂Nb₃O₁₀ (usually referred to as HCa₂Nb₃O₁₀·1.5H₂O in the literature) belongs to the Dion-Jacobson phase and can be obtained from KCa₂Nb₃O₁₀ oxide by ion-exchange in acid solutions [22]. It was shown that HCa₂Nb₃O₁₀·1.5H₂O enables the intercalation of amines by an acid-base mechanism [23] and may be later exfoliated into nanolayers [24,25]. Both KCa₂Nb₃O₁₀ and HCa₂Nb₃O₁₀·1.5H₂O, as well as their exfoliated and restacked forms, exhibit photocatalytic properties [26–28]. Along with this form, there may be others with a lower water content. The ability to intercalate water molecules often

plays a crucial role in other intercalation reactions and photocatalysis [9,29–31]. Hydrated protonated forms may comprise protons [13,30] or charged complexes like $H^+ \dots n \cdot H_2O$ in their interlayer slab [32–34]. Obviously, water content and its state and localization should affect both the pathway and efficiency of chemical or photocatalytic reactions. From this perspective, an identification of proton-containing species and a comprehensive study of their motion in the interlayer slab is required.

Proton Nuclear Magnetic Resonance (NMR) is one of the most versatile experimental methods. It enables the identification of the proton-containing species and provides insight on the local structure [13,32,35–37] and information at the microscopic level on the dynamics of intercalated species [13,16,32,35,36,38]. In particular, by using ¹H NMR, it was shown that both the local environment and the dynamics of hydrogen in these materials are affected by the stacking sequence of the perovskite-like slabs [39].

Here, we report on the results of the proton NMR spectroscopy and relaxation studies of the layered perovskite-like niobate $HCa_2Nb_3O_{10}$ with different hydration levels: hydrated— α -form, dehydrated— γ -form, and intermediate— β -form. The details of their synthesis can be found in Section 3.

2. Results and Discussion

2.1. X-ray and TG Analysis

Figure 1a shows the X-ray Diffraction (XRD) patterns of the studied $HCa_2Nb_3O_{10}\cdot yH_2O$ samples with different hydration levels. The XRD shows that the samples are practically monophase. All the samples can be described by the *P4/mmm* space group. The unit cell is shown in Figure 1b. The lattice parameters are listed in Table 1.



Figure 1. XRD powder patterns for the studied forms of $HCa_2Nb_3O_{10} \cdot yH_2O$ with different hydration levels (**a**) and the unit cell of $HCa_2Nb_3O_{10} \cdot yH_2O$ (**b**) with possible sites for the water oxygen O_w .

| Parameters | α-Form | β-Form | γ -Form |
|---------------------|------------|-------------|----------------|
| a (Å) | 3.86517(3) | 3.86550(9) | 3.89267(8) |
| c (Å) | 16.2627(2) | 15.1125(7) | 14.5254(4) |
| V (Å ³) | 242.957(6) | 225.812(18) | 220.102(14) |

Table 1. Lattice parameters (*a*, *c*) and unit cell volume (*V*) for the studied forms of $HCa_2Nb_3O_{10}\cdot yH_2O$.

The thermogravimetric (TG) curves that represent the mass decay due to the water release are shown in Figure 2a. As can be seen from the thermogravimetric curves, α -HCa₂Nb₃O₁₀·*y*H₂O exhibits behavior typical for a low-stable highly hydrated protonated form. Its thermal decomposition proceeds in two main steps, which is typical of protonated layered perovskite-like oxides [40–42]. The first step (T < 373 K) is associated with the release of the intercalated water and the formation of a dehydrated protonated compound:

$$HCa_2Nb_3O_{10} \cdot yH_2O \to HCa_2Nb_3O_{10} + yH_2O.$$
⁽¹⁾



Figure 2. (a) TG curves for the studied forms of $HCa_2Nb_3O_{10} \cdot yH_2O$ with different hydration levels; (b) number of H_2O molecules per formula units (*y*) versus the interlayer space (*d*).

The second step of the mass loss that occurs at about $525 \div 550$ K is related with thermal degradation, or so-called topochemical condensation:

$$HCa_2Nb_3O_{10} \rightarrow Ca_2Nb_3O_{9.5} + 0.5H_2O.$$
 (2)

The thermal decomposition of the γ -form demonstrates similar trends, but the mass loss at the first step is essentially low due to the much lower content of the intercalated water. Thermolysis of the β -form appears to be a more complex process, including gradual evolution of interlayer water in the temperature range of $373 \div 525$ K, with the subsequent topochemical condensation of the protonated compound. The absence of the mass loss for the β -form at the beginning part of the TG curve indicates its greater thermal stability in comparison with the α -form.

According to the TG analysis, all the studied forms are fully protonated compounds with a substitution degree of K⁺ cations for protons H⁺ close to 100%. The water content as determined from TG curves results in 1.6, 0.8, and 0.1 H₂O molecules per formula unit for α -, β -, and γ -forms, respectively. When describing layered structures, an important parameter is the interlayer distance *d*, the distance between the center of the adjacent perovskite slabs. For the studied structures, *d* = *c*; Figures 1b and 2b show the correlation between the *d* parameter and the water content, which confirms that water molecules are located within the interlayer space.

2.2. ¹H MAS NMR Study

Figure 3 shows the ¹H MAS NMR spectra for the studied forms of HCa₂Nb₃O₁₀·*y*H₂O acquired at 259 K. As one can see, depending on the hydration level of HCa₂Nb₃O₁₀·*y*H₂O, the spectra differ from each other by the number of spectral lines, their position, and the linewidths. This shows the presence of different proton-containing species in the α -, β -, and γ -forms and their different mobilities.



Figure 3. ¹H MAS NMR spectra in the α - (**a**), β - (**b**), and γ -forms (**c**) of HCa₂Nb₃O₁₀·*y*H₂O at 297 K.

At room temperature (297 K), the ¹H spectrum of α -HCa₂Nb₃O₁₀ (Figure 3a) consists of two narrow intense Lorentzian lines at 3.1 and 6.8 ppm, L1 and L2, respectively, and two lines of lower intensities: Lorentzian line L3 at about 4.1 ppm and Gaussian line G4 at 6.0 ppm. For β -HCa₂Nb₃O₁₀ (Figure 3b), it consists of only one rather broad Lorentzian line at 3.6 ppm, whereas for γ -HCa₂Nb₃O₁₀ (Figure 3c), the main signal is observed at 8.2 ppm (L2), with a shoulder at 5.9 ppm (L1) (a signal at about -2 ppm can be associated with surface defects and is not discussed further).

To assign the spectral lines to the H-containing species, the evolution of the proton spectra with the temperature decreasing was studied; see Figure 4. As temperature decreases, the spectral lines broaden, and a redistribution of line intensities occurs. Let us first discuss the temperature evolution of the ¹H MAS NMR spectrum of γ -form, HCa₂Nb₃O₁₀·0.1H₂O, which is characterized by the lowest water content. At room temperature, the contribution of the L2 line dominates, the relative intensity of L1 is of about 10%, and with sample cooling the line broadens and then disappears. Below 259 K, only the L2 line presents, and with the temperature further decreasing it splits into two lines: Lorentzian type at 8.9 ppm and Gaussian type at 7.8 ppm; see Figure 5. The temperature evolution of the spectral line parameters, namely the isotropic chemical shift (δ_{iso}), the full width at half maximum ($\Delta v_{1/2}$), and the relative intensities are shown in Figure 6a–c, respectively.



Figure 4. ¹H MAS NMR spectra in the α - (**a**), β - (**b**), and γ -forms (**c**) of HCa₂Nb₃O₁₀·*y*H₂O with the temperature decreasing.



Figure 5. ¹H MAS NMR spectra at 151 K in γ -HCa₂Nb₃O₁₀·*y*H₂O and its decomposition.



Figure 6. Temperature dependencies of the ¹H isotropic chemical shift (the upper row), the line width at half maximum (the middle row), and the integral intensities (the bottom row) for the α - (**a**), β - (**b**), and γ - (**c**) forms of HCa₂Nb₃O₁₀·*y*H₂O.

Based on the TG analysis, one can attribute L1 line to the bulk water. Normally its signal is expected at 5.5 ppm [22], but in a charged nanoconfinement it can be shifted towards a higher frequency. Its contribution is low with the temperature decreasing because of the slowing down of the molecular motion; thus, the line becomes too broad to be resolved. The most intensive line, L2, at about 8 ppm can be associated with the lattice protons in regular sites; e.g., in Ruddlesden–Popper phase $H_2La_2Ti_3O_{10}\cdot 0.13H_2O$, the signal of isolated H⁺ was reported at 11–13 ppm [13,37]. The splitting of the line at low temperatures may point to two inequivalent cation positions. It is worth noting that down to 151 K, the linewidth of the spectral lines is almost unchanged. This indicates that within the studied temperature range, the proton mobility (translational diffusion) does not change significantly.

The ¹H spectra of α -HCa₂Nb₃O₁₀ exhibits the most dramatic changes with temperature: the high field part of the spectrum rapidly disappears with cooling; see Figure 4a. The temperature changes of the spectral parameters are plotted in Figure 6a. As one can see, with the temperature decreasing, the intensities of the spectral lines L1 and G1 rapidly drop, and after cooling down below 245 K, only L2 and L3 remain. Below 200 K, only the L2 peak is visible. Such a complex temperature behavior of the ¹H MAS NMR spectrum of the α -form, as well as its structure, reflect (i) the variety of types of interlayer proton-containing species due to the high content of intercalated water in comparison with the other studied forms, and (ii) the non-obvious mechanisms of interaction between them in a charged environment. Interestingly, in α -form there is no signal associated with isolated protons. Moreover, despite a rather high water content, the only signal that can be associated with the bulk water, the line G4 at 6.1 ppm, has a very low intensity and, similar to the γ -form, rapidly disappears with cooling. Altogether, this suggests the presence of charged water complexed like H⁺ ... xH₂O.

According to Ref. [43], the ¹H chemical shift of H_3O^+ (x = 1), calculated for water solutions of mineral acids, is expected at 13.3 ppm. With x increasing, the ¹H chemical shift decreases, e.g., for H⁺ ... 2H₂O it was predicted at 8.0 ppm. Our calculations carried out for isolated complexes give 7.3 and 4.6 (17.5) ppm for the isotropic chemical shift for free H_3O^+ and $H_5O_2^+$ clusters, respectively (the number in parenthesis corresponds to the central proton). These calculations are supported by several experimental studies of hydrated layered oxides, in which the signal at 8–11 ppm was assigned to the H_3O^+ [32,36,44–46]. Hence, following both theoretical and experimental studies of other complex layered oxides, and accounting that for α -form of HCa₂Nb₃O₁₀·*y*H₂O there are 1.6 H₂O molecules and one interlayer proton per one formula, it can be suggested that one water molecule participates in the formation of H_3O^+ , the signal L2 at about 7 ppm, whereas other signals correspond to water molecules that are localized in different sites of the charged interlayer space or are part of the more extended charged complexes, like H⁺ ... 2H₂O.

The temperature behavior of the L2 linewidth, Figure 6a, is typical for solids [13,47,48] and reflects the slowing down of the molecular motion. Using the onset temperature of motional narrowing, $T_{\rm MN} = 150$ K, one can estimate the activation energy of the line narrowing process within the semi-empirical Waugh-Fedin expression [49]:

$$E_{a}(eV) \approx 1.61 \times 10^{-3} \cdot T_{MN}(K).$$
 (3)

This results in $E_a \approx 0.24(2)$ eV.

The ¹H MAS NMR spectrum of the β -form consists of one line centered at about 3.6 ppm, which almost does not shift within the studied temperature range; see Figure 5. Taking into account that, according to the TG analysis, the β -form contains 0.8 H₂O molecules per formula unit, and hence per interlayer cation H⁺, and no signal from H₃O⁺ or H⁺ is observed, one can suppose that this line is the result of an exchange between the lattice protons (an expected signal at about 8 ppm as in the γ -form) and the non-hydrogenbounded water (an expected signal at about 0.8 ppm).

2.3. ${}^{1}HT_{1\rho}$ Study

To elucidate dynamic processes for all the studied compounds, the temperature dependencies of spin lattice relaxation times in the rotating frame, $T_{1\rho}$ were measured. Relaxation measurements are more sensitive to changes in molecule dynamics than spectroscopic ones [47,50]. For the studied systems, the NMR relaxation is issued mainly by fluctuating strengths of ¹H–¹H dipole coupling. The latter, being dependent on the relative position of the interacting nuclear spins, is altered by motional processes. As a result, this leads to fluctuations of the Larmor frequency. This process can be described through a correlation function, G(t):

$$G(t) = \langle \Delta \omega(0) \cdot \Delta \omega(t) \rangle = G(0) \cdot g(t) \tag{4}$$

where the brackets represent the ensemble average; g(t) contains information about dynamic processes, and its exact expression depends on the spin interaction and diffusion mechanism; G(0) is determined by the mutual nuclear spin arrangement.

Commonly, to describe relaxation processes one uses a spectral relaxation function $j(\omega)$, which is a Fourier-transformed correlation function, g(t). In terms of $j(\omega)$, the dipole contribution to NMR spin-lattice relaxation time T_1 , a characteristic time for magnetization recovery after a perturbating pulse, can be written as follows:

$$1/T_1 = G(0) \cdot \left[\frac{1}{3}j(\omega_0) + \frac{4}{3}j(2\omega_0)\right],$$
(5)

where ω_0 is the ¹H NMR frequency. By analyzing the temperature dependence of spin lattice relaxation within an appropriate model, one can extract parameters of molecular motion, such as activation energies and correlation times. However, solids normally exhibit slower dynamics as compared to liquids. For such systems, the spin-locking technique is much more fruitful: by applying a locking field ω_1 , one can shift the minimum of the temperature dependence of the spin-lattice relaxation time towards the lower temperature in such a way that it falls within the measured temperature range [51–55]. More details can be found in Ref. [13]. At condition $\omega_1 \ll \omega_0$, the relaxation time can be written as

$$1/T_{1\rho} = G(0) \cdot \left[\frac{1}{2}j(2\omega_1) + \frac{5}{6}j(\omega_0) + \frac{1}{3}j(2\omega_0)\right].$$
(6)

For HCa₂Nb₃O₁₀·*y*H₂O, the upper limit of temperature is restricted by the water desorption, which according to the TG analysis (Figure 2a) occurs at T > 300 K. Application of the spin-locking technique helps to determine the spin motion parameters in a more accurate way.

The relaxation times $T_{1\rho}$ for the studied forms of HCa₂Nb₃O₁₀·*y*H₂O plotted versus inverse temperature are shown in Figure 7a–c. It should be noted that for all the studied forms within the experimental temperature range, the magnetization recovery is mainly described by a two-exponential function, with characteristic spin-lattice relaxation times $T_{1\rho}'$, $T_{1\rho}''$ differing from each other in one order of magnitude, except α -form, in which a mono-exponential behavior was observed above 200 K. Examples of the magnetization recovery curves (mono and two-exponential) are shown in Figure 8.



Figure 7. ¹H relaxation times $T_{1\rho}'$, $T_{1\rho}''$ (**a**–**c**) and their relative contributions A', A'' to the magnetization recovery (**d**–**f**) for α - (**a**,**d**), β - (**b**,**e**), and γ - (**c**,**f**) forms of HCa₂Nb₃O₁₀·*y*H₂O versus inverse temperature. The solid lines show the fitting using the KWW correlation function.



Figure 8. ¹H magnetization recovery curves for the α -form of HCa₂Nb₃O₁₀·*y*H₂O at 297 and 167 K with the exponential fit (solid lines); for 167 K the line corresponds to the slow component only.

As it is clearly seen from Figure 7, depending on the hydration level, $HCa_2Nb_3O_{10}$ · yH_2O demonstrates rather different $T_{1\rho}(1/T)$ behaviors. Let us first discuss the γ -form. The temperature dependence of $T_{1\rho}$ for the least hydrated form of $HCa_2Nb_3O_{10}\cdot yH_2O$ exhibits features similar to $H_{1.83}K_{0.17}La_2Ti_3O_{10}\cdot 0.17H_2O$ [13]. However, it should be noted that the applied locking field was not sufficient to displace the minimum in the middle of the studied temperature range. This complicates the analysis of the experimental data, but the higher pulse power would heat the system excessively.

To determine the proton motion parameters, we used the Kohlrausch-Williams-Watts (KWW) model [56–58] successfully applied to $H_{1.83}K_{0.17}La_2Ti_3O_{10}\cdot 0.17H_2O$ [13]. Commonly, the relaxation in isotropic systems like liquids is described by the well-known Bloembergen-Purcell-Pound (BPP) model [59], which supposes that the exponential function g(t) is as follows:

$$g(t) = e^{-|t|/\tau_c}$$
(7)

and that the correlation time τ_c obeys the Arrhenius law: $\tau_c = \tau_0 \exp\left(\frac{E_a}{k_B T}\right)$. Here E_a is the activation energy of hydrogen motion, k_B is the Boltzmann constant, and τ_0 is a pre-exponential factor. The function in Equation (7) results in the following form of the spectral density:

$$j(\omega) = \frac{2\tau_{\rm c}}{1 + (\omega\tau_{\rm c})^2}.$$
(8)

This model can be applied to solids, e.g., to describe the translational motion of hydrogen in metallic lattice, but requires some corrections to account for activation energy distribution [47,48], contribution of conduction electrons [60–62], and an exchange between different fractions [48,61,63].

In anisotropic systems, such as ionic conductors, the $T_1(1/T)$ dependence is asymmetric, and a stretched exponential KWW correlation function $g(t) = e^{-(|t|/\tau_s)^{\beta}}$ is more appropriate for its description. This means that the motion is correlated. These cooperative effects, similar to conduction electrons, contribute mainly at low temperatures, and the corresponding slope is reduced by β [55–58,64]. The spectral density function in this case can be written as

$$j(\omega) = \frac{2\tau_{\rm c}}{1 + (\omega\tau_{\rm c})^{1+\beta}},\tag{9}$$

with the stretching exponent β ranging from 0 to 1.

As was mentioned above, due to the system limitations for the γ -form of HCa₂Nb₃O₁₀· *y*H₂O, one cannot observe the high temperature slope of the $T_{1\rho}(1/T)$ (Figure 7c), and hence one cannot determine correctly the stretching exponent. That is why to estimate the activation energy we used the parameter $\beta = 0.28$, as determined for H_{1.83}K_{0.17}La₂Ti₃O₁₀·0.17H₂O[13].

As seen from Figure 7c, the fast $(T_{1\rho}')$ and slow $(T_{1\rho}'')$ components of $T_{1\rho}$ exhibit very similar temperature dependencies. Moreover, within the studied temperature range, their contributions are almost tantamount. The fitting within the KWW model results in the very close values of E_a and τ_0 : { $E_a' = 0.223(2) \text{ eV}$, $\tau_0' = 8.8(5) \times 10^{-10} \text{ s}$ } and { $E_a'' = 0.213(4) \text{ eV}$, $\tau_0'' = 7.8(3) \times 10^{-10} \text{ s}$ } for the slow and fast components, respectively. Accounting for the ¹H MAS NMR data, one can suggest that these lines correspond to the isolated interlayer H⁺ ions or those in the vicinity of the water molecules.

For the most hydrated α -form above 200 K, the magnetization recovery is described by a single exponent, and the relaxation time $T_{1\rho}$ rapidly decreases with temperature decreasing; see Figure 7a. However, as was mentioned above, below 200 K the character of the magnetization recovery changes, and a second exponent with a longer relaxation time appears. With further temperature decreases, the values of the both short $(T_{1\rho}')$ and slow $(T_{1\rho}'')$ components do not change much; nevertheless, the contribution of the $T_{1\rho}''$ component becomes more important and achieves about 44% at 145 K; see Figure 7d. It should be noted that, according to ¹H MAS NMR spectra (Figure 5a), below 200 K there is only one spectral line at about 7 ppm. Such temperature dependencies of the both relaxation times and spectral parameters implicitly show the changes in dynamics of protoncontaining species at 200 K. To estimate parameters of the proton motion in α -form, we applied the abovementioned KWW model to the high temperature branch of the $T_{1\rho}'(1/T)$. This results in the parameters $E_a = 0.210(2) \text{ eV}$, $\tau_0 = 9.0(1) \times 10^{-12} \text{ s}$, which can be associated with the translational motion of H₃O⁺. Although above 200 K the magnetization recovery curve is described by a single exponential decay, ¹H MAS NMR spectra exhibit the existence of different hydrogen-containing species in α -HCa₂Nb₃O₁₀·*y*H₂O (H₃O⁺, H₂O and other); see Figure 6a. This suggests a fast exchange between the species involved in the translational motion. Below 200 K, with the slowing down of the translation, other types of motion (e.g., reorientation) became more important.

The relaxation times for the β -form of HCa₂Nb₃O₁₀·*y*H₂O, Figure 7b, show a complex temperature dependence: within the studied temperature range there are at least two characteristic points (224 and 176 K) at which the proton dynamics change. These changes can also be observed in the temperature dependence of the proton linewidth, but they are less significant.

Therefore, the state of protons and water molecules located in the interlayer space, as well as their dynamics, are determined by the level of hydration. It is noteworthy that the formation of H_3O^+ is confirmed for the most hydrated α -form only, in which it is quite mobile even at low temperatures. For the γ -form, water molecules are not involved in the formation of hydronium ions; protons, behaving as lattice cations, can occupy at least two nonequivalent positions and participate in translational motion. The β -form is the most mysterious. The isotropic chemical shift of only the ¹H spectral line indicates an exchange between different species, but it is not possible to unambiguously identify these species from the data obtained. The presence of two characteristic points on the temperature dependence of the proton relaxation time indicates that the mechanism of this exchange is temperature-dependent.

3. Materials and Methods

 $KCa_2Nb_3O_{10}$, a precursor for further synthesis of the protonic form, was synthesized by the standard ceramic method at normal conditions (air atmosphere and pressure) using CaO, Nb₂O₅, and K₂CO₃ as parent materials. CaO and Nb₂O₅ were taken in amounts to satisfy the stoichiometry of the reaction:

$$4CaO + 3Nb_2O_5 + K_2CO_3 = 2KCa_2Nb_3O_{10} + CO_2 \uparrow .$$
(10)

To compensate for losses during calcination, potassium carbonate was taken with a 30% excess. All the components were mixed and ground in a planetary ball mill in n-heptane. The obtained powder was pelletized and then calcined at 800 $^{\circ}$ C for 12 h. After that, it was ground in an agate mortar, pelletized again, and calcined at 1100 $^{\circ}$ C for 24 h.

The first hydrated protonated form of KCa₂Nb₃O₁₀, named as α -form of HCa₂Nb₃O₁₀. *y*H₂O, was prepared by acid processing of KCa₂Nb₃O₁₀, with an excess of 12 M HNO₃ (50 mL per 2.5 g of the oxide), at room temperature for 24 h. The product was centrifuged, washed with 50 mL of water three times to remove acid residues, and dried over CaO for 24 h. Subsequently, it was stored in a humid air atmosphere.

The second hydrated protonated form of KCa₂Nb₃O₁₀, named as β -form of HCa₂Nb₃O₁₀· *y*H₂O, was prepared by hydrothermal treatment of the α - form. For this, 0.5 g of the latter was placed in the laboratory autoclave with 35 mL of water (volume filling approximately 80%) and processed at 150 °C for 7 d. The product obtained was centrifuged and dried over CaO for 24 h.

To obtain the dehydrated protonated form of KCa₂Nb₃O₁₀, named as γ -form of HCa₂Nb₃O₁₀·*y*H₂O, the α -form was dried in a desiccator with a vacuum pump (about 1×10^{-4} atm) for 24 h.

Powder XRD analysis was done on a Rigaku Miniflex II diffractometer using monochromatic CuK_{α} radiation (λ = 0.154056 nm). Diffractograms were recorded in the 2 θ range of $3-120^{\circ}$ (step width 0.02°). The lattice parameters were calculated in the tetragonal system on the basis of all the reflections observed using DiffracPlus Topas 4.2 software.

TG analysis was carried out using a Netzsch TG 209 F1 Libra thermobalance. Analysis of samples was carried out in the temperature range 30–900 $^{\circ}$ C at a heating rate of 10 $^{\circ}$ C/min in an argon stream at a rate of 90 mL/min.

¹H NMR experiments were done using a Bruker Avance IIITM 400 MHz solid-state NMR spectrometer (operating with Topspin version 3.2) using a double-resonance 4 mm low-temperature MAS probe. The temperature was changed within a temperature range of 139 to 297 K and controlled with an accuracy of 0.5 K. ¹H NMR MAS spectra were recorded at rotor frequency 12 kHz. To measure T_1 relaxation times, the spin-locking technique was applied, with the rf frequency of the locking pulse equal to 40 kHz. Tetramethylsilane (TMS) was used as an external standard.

The ¹H magnetic shielding tensor for H_2O , H_3O^+ , and $H_5O_2^+$ was calculated using the Gauge-Independent Atomic Orbital (GIAO) method [65] for the geometries optimized at the B3LYP/6-311G level of theory, as implemented in Gaussian 09 [66]. The theoretical isotropic chemical shift was estimated relative to the magnetic shielding tensor in TMS, calculated at the same level of theory.

4. Conclusions

The results of a comprehensive ¹H NMR study of three different forms of the layered perovskite-like niobate $HCa_2Nb_3O_{10}$ ·*y*H₂O can be summarized as follows:

- For the most hydrated α -form, HCa₂Nb₃O₁₀·1.6H₂O, ¹H MAS NMR spectra reveal the presence of different proton-containing species: H₃O⁺, which comprises all the lattice protons (there is no signal that can be associated with H⁺ in regular sites), and water molecules that are localized in different sites of the interlayer slab and supposedly participate in the formation of charged complexes like H⁺ ... 2H₂O. With the temperature decreasing, the signal from the water proton is so broad that it is undetectable; the only detectable signal is from H₃O⁺. The activation energy determined from the onset temperature of motional narrowing of 0.24(2) eV is in fair agreement with the relaxation data. Application of the KWW model with the stretching exponent $\beta = 0.28$ to the $T_{1\rho}(1/T)$ experimental dependence results in the following molecular motion parameters, which can be associated with the translational diffusion of H₃O⁺: $E_a = 0.210(2)$ eV, $\tau_0 = 9.0(1) \times 10^{-12}$ s. Below 200 K, with the slowing down of the translational motion, other types of motion, such as reorientation, became more important.
- ¹H MAS NMR spectrum of the β-form, HCa₂Nb₃O₁₀·0.8H₂O, within the studied temperature range consists of one line centered at about 3.6 ppm, which is the result of an exchange between lattice protons and the non-hydrogen-bounded water protons. The temperature dependence of the relaxation time evidences the presence of two characteristic points (224 and 176 K), at which proton dynamics changes.
- The proton NMR spectroscopy study of the γ -form, HCa₂Nb₃O₁₀·0.1H₂O, which is characterized by the lowest water content, reveals the presence of bulk water and interlayer H⁺ in two inequivalent positions. The temperature dependencies of the spin-lattice relaxation time in the rotating frame treated withing the KWW model with $\beta = 0.28$ results in the following parameters of the proton motion: $E_a = 0.217(8)$ eV, $\tau_0 = 8.2(9) \times 10^{-10}$ s.

We expect that the results obtained will clarify the relationship between the hydration level (and hence the type and, possibly, localization of hydrogen-containing species) and the photocatalytic activity of this class of layered materials. Currently, studies of the photocatalytic activity of the different forms of $HCa_2Nb_3O_{10}\cdot yH_2O$ are under evaluation.

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