

Supporting information

Further Validation of Quantum Crystallography Approaches

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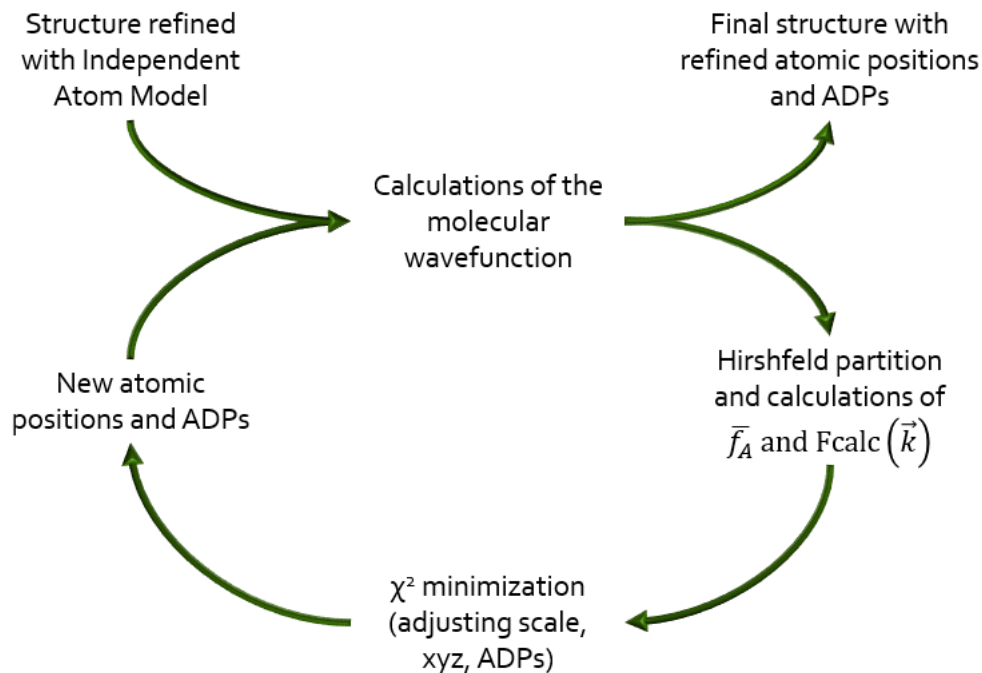
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Hirshfeld Atom Refinement



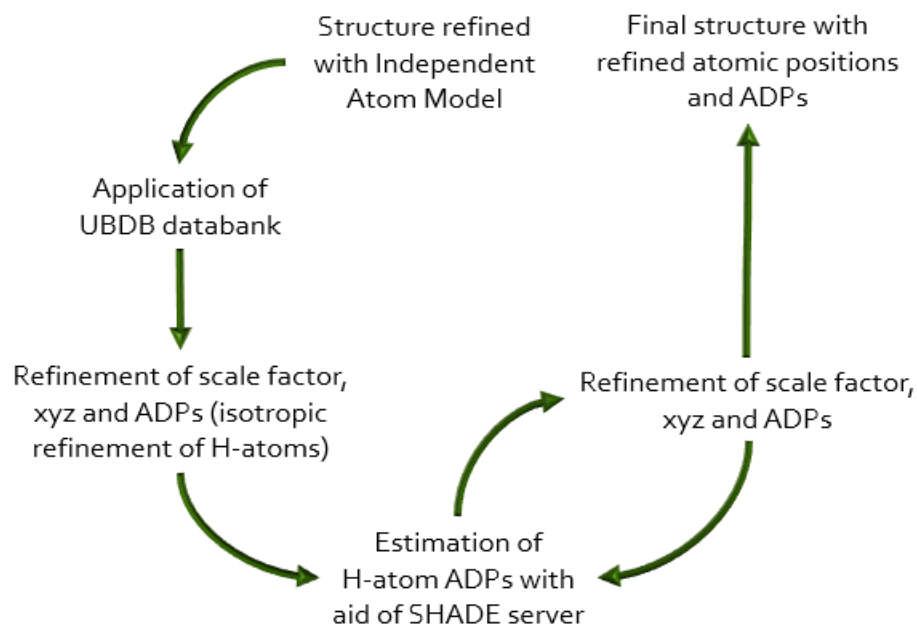
Scheme S1 Hirshfeld Atom Refinement scheme. [1]

Procedure:

After application of Independent Atom Model (to obtain starting geometry, ADPs, experimental structure factors), the wavefunction for cluster of molecules is calculated. In the next step, the molecular electron density function is divided into atomic contributions (Hirshfeld partition), and atomic scattering factors are calculated. Then, minimization is performed by adjusting parameters such as scale, atomic positions and ADPs between calculated and observed structure factors. As a result, the new atomic positions are obtained and used in next cycle of wavefunction calculations. This cycle is repeated till convergence and as a final step, the final structure with refined atomic positions and ADPs is obtained. The final structure is validated with analysis of atomic positions, residual and deformation density maps, fractal dimension plots and statistical parameters including value of χ^2 .

Procedure based on reference [1]

Transferable Aspherical Atom Model



Scheme S2 Transferable Aspherical Atom Model scheme based on references [2–7]

Procedure:

Firstly, the structure is refined with Independent Atom Model. Then, with the aid of LSDB Software (Volkov, A. et al., J. Phys. Chem. A, 2004, 108, 4283–4300), the pseudoatom parameters are transferred from UBDB Pseudoatom Databank. Multipole populations and contraction/expansion parameters in the UBDB are obtained in fitting procedure in reciprocal lattice of multipole model and electron density parameters are obtained with quantum-mechanical calculations. The atom types used in UBDB are based on mean electron density parameters for various pseudoatoms with similar topology of bonds in the model compounds, for which the geometries are obtained from experimental X-ray data.

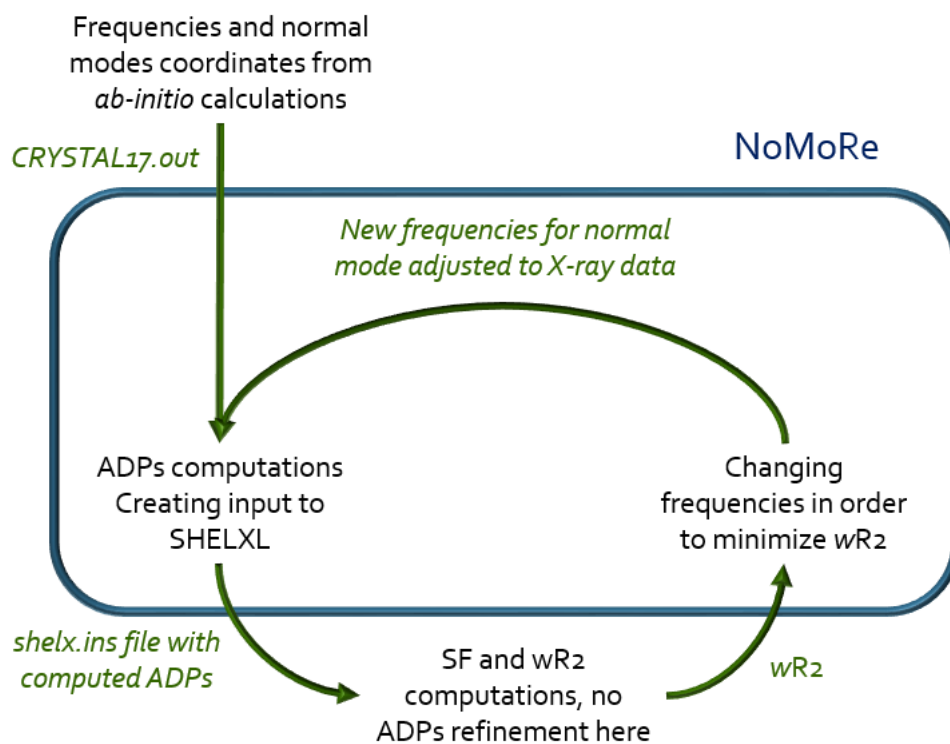
After the assignment of electron density parameters for structure refined with IAM, the scale factor, atomic positions and ADPs of heavy atoms (anisotropic) as well as hydrogen atoms (isotropic) are refined.

In the next step, the H-atoms of ADPs with the aid of SHADE server. Constraints obtained from SHADE are based on the sum of internal and external motions. Internal motions are derived from library containing results of neutron diffractions experiments, whereas external motions are obtained using TLS (Translation-Libration-Screw) model introduced by Schomaker and Trueblood in 1968. Refinements of scale factors,

atomic positions with ADPs are proceed till convergence. The final structure is validated with analysis of atomic positions, residual and deformation density maps, fractal dimension plots and statistical parameters.

Procedure based on references [2–7]

Normal Mode Refinement



Scheme S3 Normal Mode Refinement scheme based on references [8,9]

Procedure:

The first step of NoMoRe procedure is performing calculations in CRYSTAL17 to obtain frequencies at the Γ point. Based on this calculation, the ADPs are calculated. The atomic coordinates are refined whereas structure factors, as well as $wR2$, are calculated. Then, selected frequencies are optimized to achieve minimization of $wR2$. Due to adjusted the values of frequencies to X-ray diffraction data, the calculations of ADPs are repeated. ADPs obtained with NoMoRe approach may be combined with other quantum crystallography models.

Procedure based on references [8,9]

Fractal dimension plots

The fractal dimension is described with the formula:

$$d^f(\rho_0; \varepsilon) = \frac{\log(N(\varepsilon))}{\log(\frac{1}{\varepsilon})}$$

$$\frac{1}{\varepsilon} = \sqrt[3]{3(n_x - 1)(n_y - 1)(n_z - 1)}$$

whereas:

ρ_0 is residual electron density,

$d^f(\rho_0)$ is fractal dimension calculated for the specific point of ρ_0 (e.g. $\rho_0=0.05 \text{ e}\text{\AA}^{-3}$) and

n_x, n_y, n_z are dimensions of the used grid.

The fractal dimension plots show condition of residual density distribution. The shape of the plot is parabolic and related to the Gaussian distribution, therefore the deviations indicate the presence of systematic errors. Also, the width of fractal dimension plot $\Delta\rho_0$ enable evaluation of residual density distribution. Moreover, the ρ_0 is related with additional descriptors which may indicate reason of presence of systematic errors. For instance, values of the gross residual electrons (e_{gross} [e]) may indicate presence of errors related to the applied density model, data processing or presence of noise.

Table S1 Statistical details of **1**, **1-cutoff**, **1-CuK α** , **2**, **2-cutoff**, **2-CuK α** , **3**, **3-cutoff** and **3-CuK α** structures.

	Rint	Rsigma	I/sigma(I)
1-cutoff	0.0607	0.0141	71.0
1	0.0296	0.0254	39.3
1-CuKα	0.0290	0.0075	133.8
2-cutoff	Data merged from CSD	0.0190	52.7
2	Data merged from CSD	0.0317	31.6
2-CuKα	0.0464	0.0152	65.8
3-cutoff	0.0260	0.0081	123.8
3	0.0557	0.0310	32.2
3-CuKα	0.0470	0.0103	97.0

Table S2 Refined frequencies and $wR2$ for Normal Mode Refinements for **1**, **2** and **3**.

	Refined frequencies	$wR2$
1	1-33	0.0922
2	1-23	0.0699
3	1-16	0.1567

Table S3 Differences between lattice energy of analysed models and neutron. Calculations of all data were performed without geometry optimization. Results are shown in kJ/mol. Calculations were performed using CRYSTAL17 at the DFT/B3LYP level of theory and applying the DFT-D3(ATM) dispersion correction, using cc-pVDZ basis set.

	1	2	3
MM	1.12	0.58	1.05

IAM	2.49	-2.98	2.03
HAR aniso	2.59	9.39	1.04
HAR Shade	2.59	9.91	1.71
HAR NoMoRe	2.31	10.18	1.41
HAR iso	2.39	11.08	1.71
TAAM Shade	1.24	7.41	2.28
TAAM iso	1.18	7.11	2.28

Table S4 Similarity index (S) and mean similarity index (\bar{S}) calculated for **1**.

	MM	HAR_ani	HAR_SHADE	HAR_NoMoRe	TAAM
mean overlap (\bar{S})	0.71	1.43	0.70	0.57	0.72
H9A	0.49	0.95	0.48	0.54	0.49
H9B	1.43	0.87	1.41	0.72	1.48
H1N	1.31	3.62	1.24	0.61	1.26
H8	0.40	0.40	0.38	0.3	0.45
H10A	0.77	0.85	0.82	1.24	0.84
H10C	1.03	2.00	1.00	1.19	0.97
H10B	0.75	0.22	0.88	0.45	0.89
H2	0.50	2.22	0.51	0.46	0.51
H3	0.35	2.43	0.33	0.29	0.33
H7	0.47	1.66	0.43	0.36	0.48
H4	0.28	0.51	0.27	0.17	0.25

Table S5 Similarity index (S) and mean similarity index (\bar{S}) calculated for **2**.

	MM	HAR_ani	HAR_SHADE	HAR_NoMoRe	TAAM
mean overlap (\bar{S})	0.80	2.16	0.78	0.36	0.79
H1A	1.90	3.47	1.77	0.55	1.73
H5A	0.95	0.98	0.91	0.73	0.93
H5B	0.87	2.46	0.86	0.37	0.91

H11	0.64	1.17	0.65	0.33	0.70
H12	1.01	1.28	0.99	0.35	1.06
H13	0.47	2.83	0.43	0.34	0.50
H14	0.25	0.6	0.3	0.1	0.28
H15	0.78	4.7	0.78	0.4	0.78
H1B	1.63	2.52	1.64	0.29	1.57
H2	0.22	2.21	0.2	0.21	0.23
H3	0.30	1.53	0.26	0.38	0.27
H4	0.59	2.14	0.53	0.29	0.58

Table S6 Similarity index (S) and mean similarity index (\bar{S}) calculated for **3**.

	MM	HAR_ani	HAR_SHADE	HAR_NoMoRe	TAAM
mean overlap (\bar{S})	0.91	4.14	0.47	0.63	0.73
H4	1.11	3.19	0.43	1.34	1.11
H5	2.26	0.33	0.70	1.01	1.80
H3	0.49	3.31	0.51	0.18	0.30
H2	0.17	1.32	0.17	0.2	0.17
H1	0.52	12.54	0.55	0.42	0.25

Table S7 Statistical parameters of HAR and TAAM refinements of **1-cutoff**.

Model	HAR_ani	HAR_SHADE	HAR_iso	TAAM_SHADE	TAAM_iso
R[F ² > 2σ(F ²)]	0.011	0.012	0.015	0.016	0.020
wR(F ²)	0.020	0.021	0.027	0.062	0.075
# of reflections	1766	1766	1766	1766	1766
# of fit parameters	226	160	160	160	171
chi ²	2.71	3.01	4.91	n/a	n/a
Goodness of fit	1.65	1.73	2.22	2.51	3.03
Δρ _{max}	0.06	0.06	0.07	0.16	0.18
Δρ _{min}	-0.06	-0.06	-0.09	-0.14	-0.20

Table S8 Statistical parameters of HAR and TAAM refinements of **2-cutoff**.

Model	HAR_ani	HAR_SHADE	HAR_iso	TAAM_SHADE	TAAM_iso
$R[F^2 > 2\sigma(F^2)]$	0.010	0.009	0.010	0.012	0.014
wR(F ²)	0.013	0.011	0.013	0.030	0.036
# of reflections	1281	1281	1281	1281	1281
# of fit parameters	199	127	127	127	139
chi ²	1.49	1.05	1.47	n/a	n/a
Goodness of fit	1.22	1.02	1.21	1.42	1.66
$\Delta\rho_{\max}$	0.07	0.07	0.08	0.09	0.10
$\Delta\rho_{\min}$	-0.08	-0.08	-0.08	-0.13	-0.14

Table S9 Statistical parameters of HAR and TAAM refinements of **3-cutoff**.

Model	HAR_ani	HAR_SHADE	HAR_iso	TAAM_SHADE	TAAM_iso
$R[F^2 > 2\sigma(F^2)]$	0.013	0.016	0.017	0.018	0.018
wR(F ²)	0.019	0.023	0.027	0.036	0.036
# of reflections	577	577	577	577	577
# of fit parameters	88	66	66	50	60
chi ²	1.76	2.34	3.26	n/a	n/a
Goodness of fit	1.33	1.53	1.81	3.65	3.67
$\Delta\rho_{\max}$	0.04	0.05	0.06	0.21	0.21

$\Delta\rho_{\text{min}}$	-0.06	-0.06	-0.09	-0.20	-0.21
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Table S10 Similarity index (S) and mean similarity index (\bar{S}) calculated for **1-cutoff** in comparison with neutron data.

	HAR aniso	HAR_SHADE	TAAM_SHADE
H9A	0.86	0.40	0.37
H9B	2.38	1.58	1.71
H1N	8.23	1.31	1.48
H8	1.32	0.36	0.46
H10A	0.71	0.87	0.81
H10C	1.89	1.01	1.14
H10B	0.44	0.97	1.01
H2	4.01	0.81	0.81
H3	4.03	0.28	0.49
H7	3.03	0.61	0.67
H4	1.21	0.44	0.64
mean overlap:	2.55	0.79	0.87

Table S11 Similarity index (S) and mean similarity index (\bar{S}) calculated for **2-cutoff** in comparison with neutron data..

	HAR_aniso	HAR_SHADE	TAAM_SHADE
H5A	20.73	12.01	12.01
H5B	22.51	11.33	10.9
H2	17.03	11.96	12.21
H11	9.46	0.67	0.83
H12	8.17	1.03	1.18
H13	3.25	0.43	0.55
H14	3.75	0.3	0.3
H15	10.69	0.87	0.88
H4	4.08	10.79	10.43
H1B	12.21	0.22	0.31
H1A	11.09	0.29	0.36
H3	100	0.5	0.53
mean overlap	11.18/18.58	4.2	4.21

Table S12 Similarity index (S) and mean similarity index (\bar{S}) calculated for **3-cutoff** in comparison with neutron data.

	HAR_aniso	HAR_SHADE	TAAM_SHADE
H4	6.9	0.97	5.02
H5	0.17	2.03	1.03
H3	3.85	3.75	2.94
H2	14.81	3.69	3.36
H1	7.47	0.67	3.26
Mean overlap:	6.64	2.22	3.12

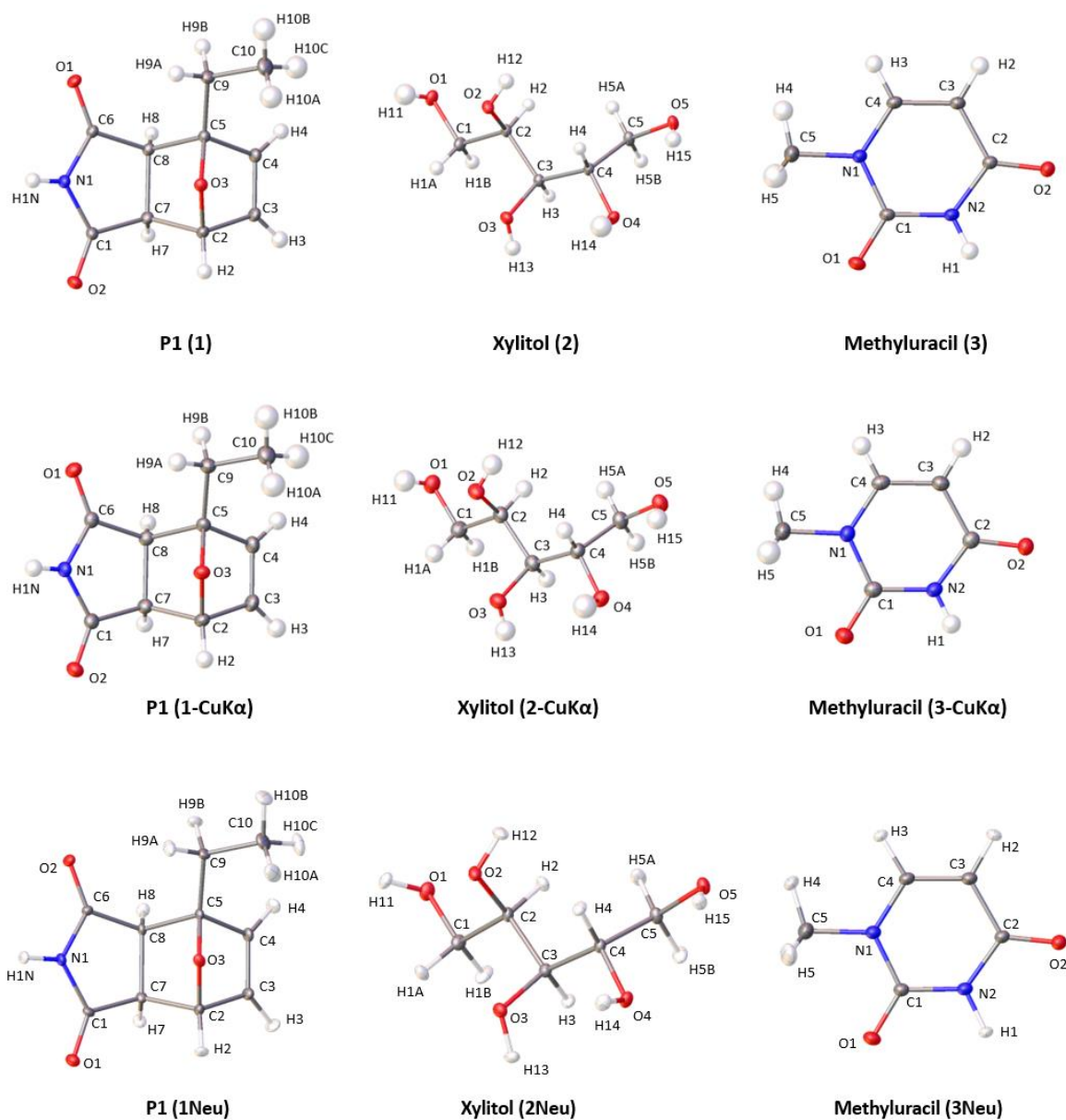
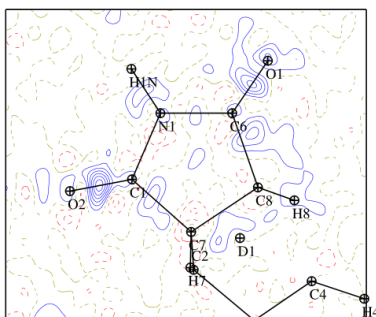
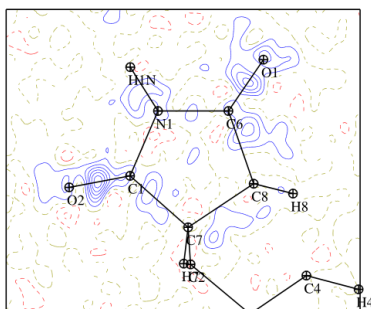


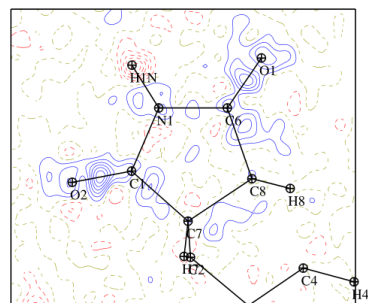
Figure S1 An ORTEP view of the molecular structure obtained with the IAM refinement of the model compounds **1Cu**, **2Cu**, **3Mo** and **3Cu**. Anisotropic atomic displacement ellipsoids are drawn at the 50% probability level. Each data are available in the CSD: **1** [23], **2** [24], **2Neu** [25], **3Neu** [26], **1-CuKα**, **2-CuKα**, **3-CuKα**, **1Neu** [12].



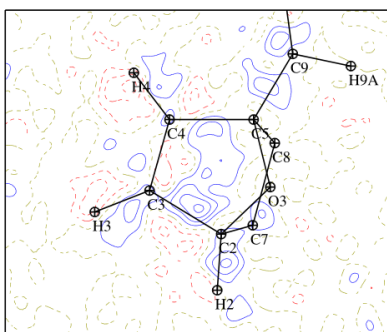
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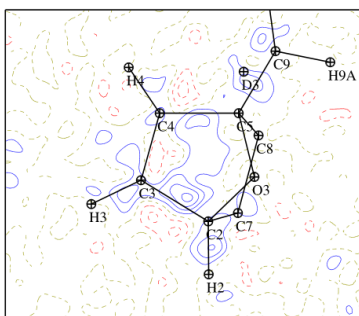
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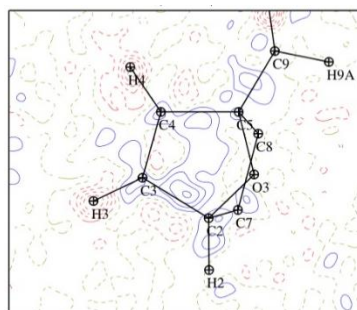
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plane determined by C4 (centre), C5
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plane determined by C4 (centre), C5 (x axis)
and C3 (y axis) atoms

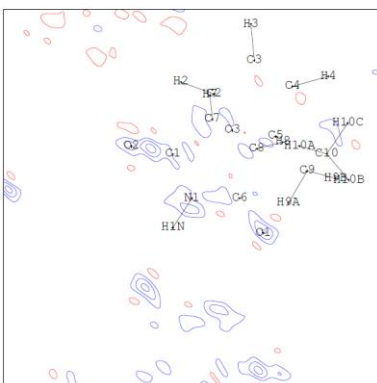


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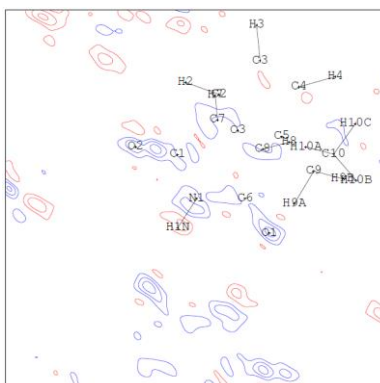
MM

TAAM Mo Shade

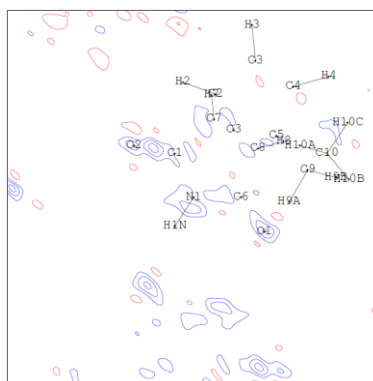
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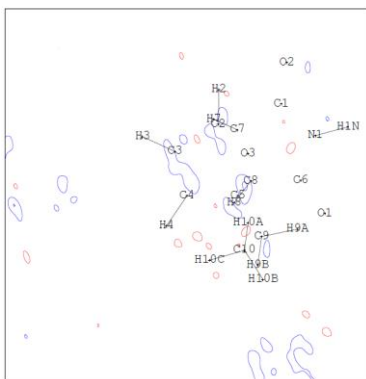
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plane determined by N1 (centre), C6 (x axis)
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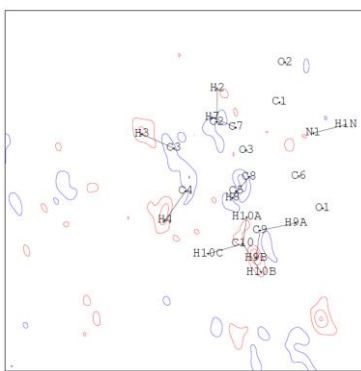


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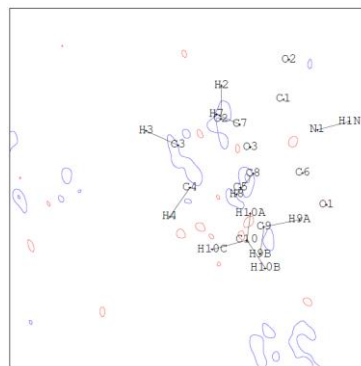
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HAR Mo aniso



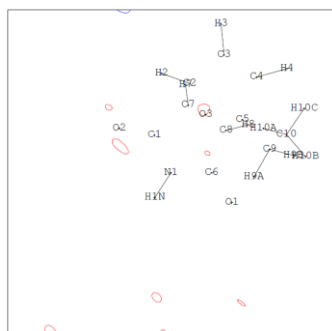
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HAR Mo iso

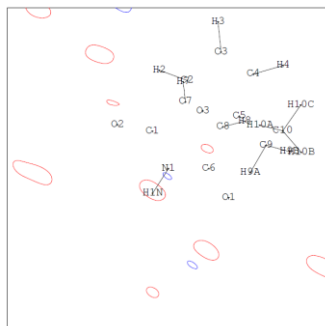


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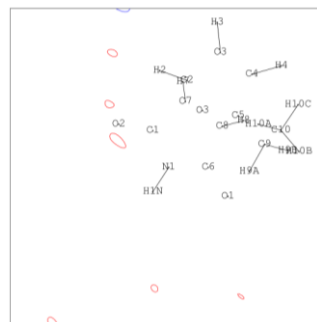
HAR Mo Shade



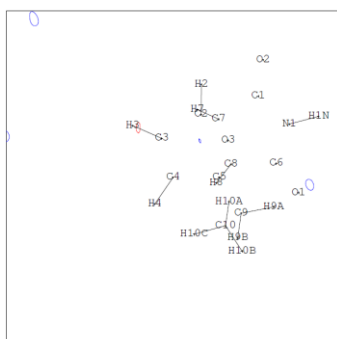
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plane determined by N1 (centre), C6 (x axis)
and C1 (y axis) atoms

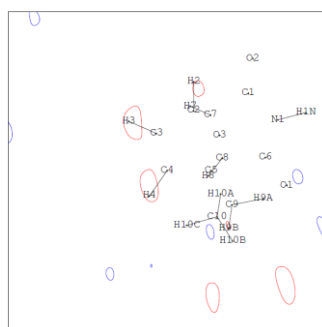


plane determined by N1 (centre), C6
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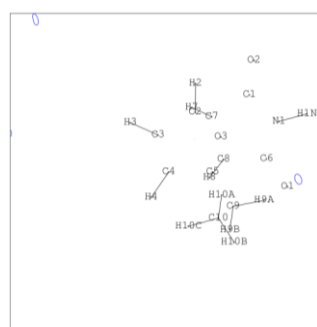
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HAR Mo aniso 0.81Å



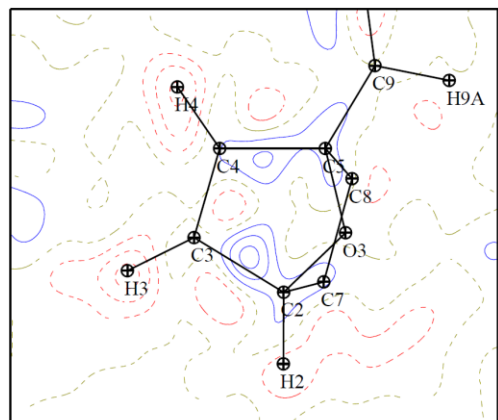
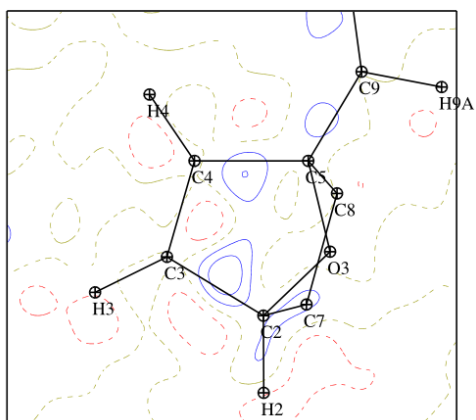
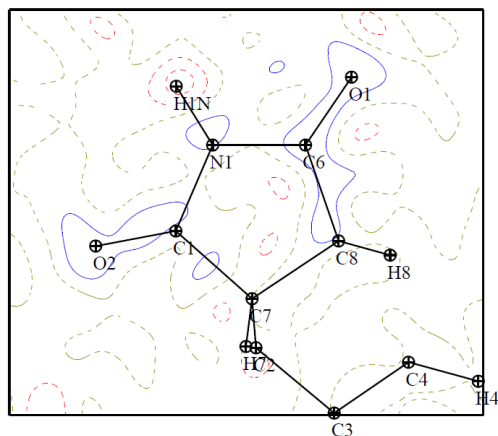
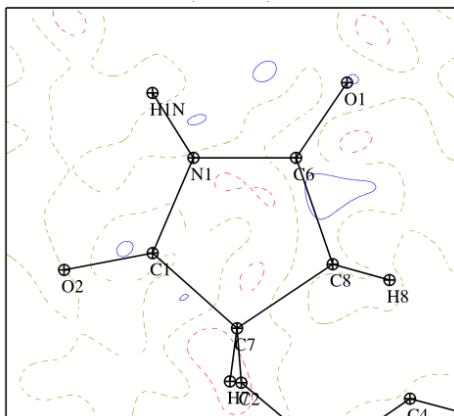
plane determined by C4 (centre), C5 (x axis)
and C3 (y axis) atoms

HAR Mo iso 0.81Å



plane determined by C4 (centre), C5
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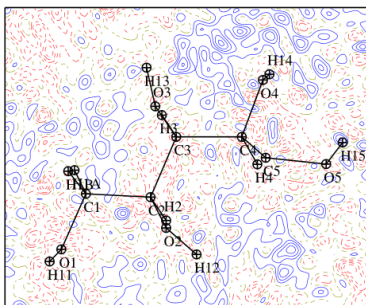
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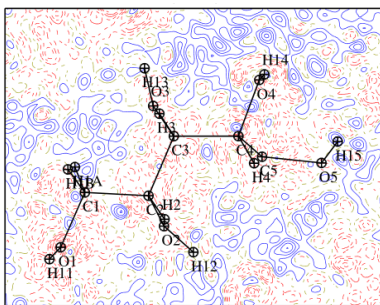
TAAM Shade 0.81Å

TAAM iso 0.81Å

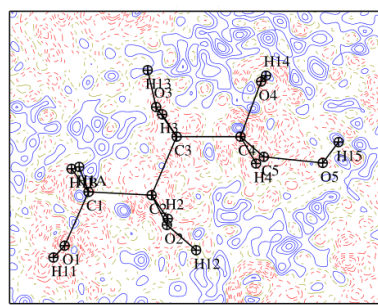
Figure S2 Residual density maps of **1** and **1-cutoff**. All maps are presented with contours levels with intervals $\pm 0.05 \text{ eÅ}^{-3}$. Blue lines represent positive values and red lines the negative ones. Maps were prepared for planes determined by N1 (centre), C6 (x axis) and C1 (y axis) atoms or C4 (centre), C5 (x axis) and C3 (y axis) atoms. Details are given below the maps.



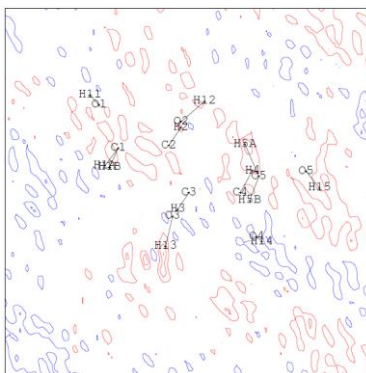
MM



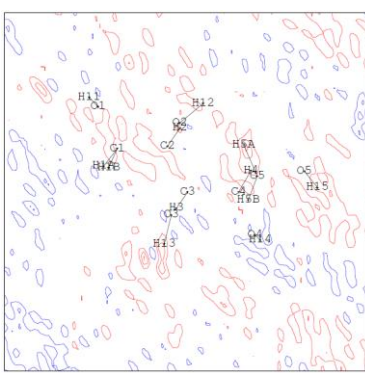
TAAM Mo Shade



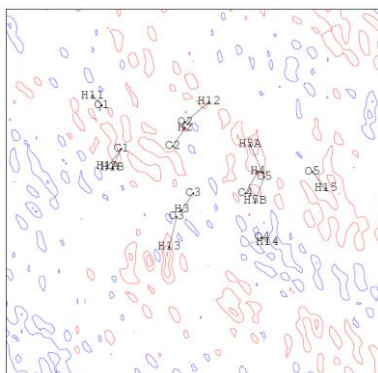
TAAM Mo iso



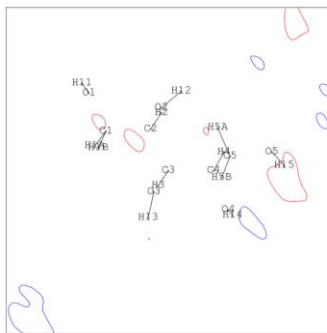
HAR Mo aniso



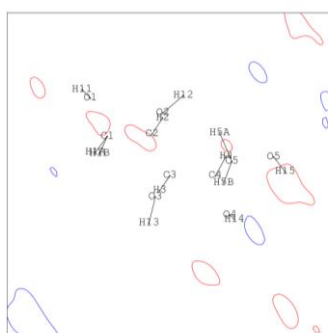
HAR Mo iso



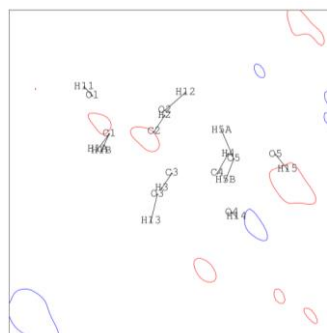
HAR Mo



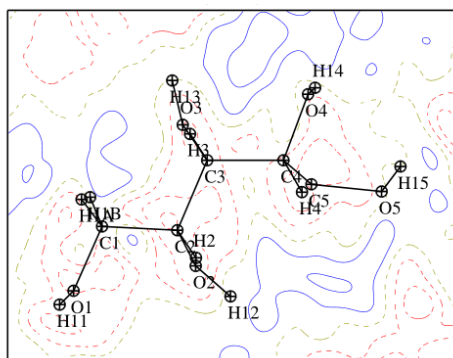
HAR Mo aniso 0.81Å



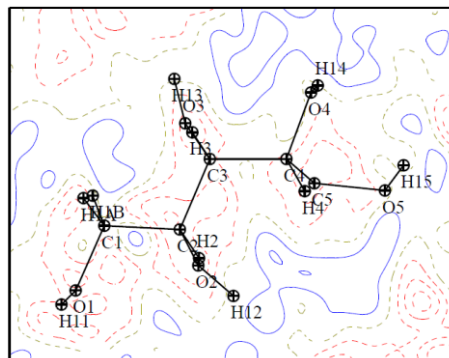
HAR Mo iso 0.81Å



HAR Mo Shade 0.81Å

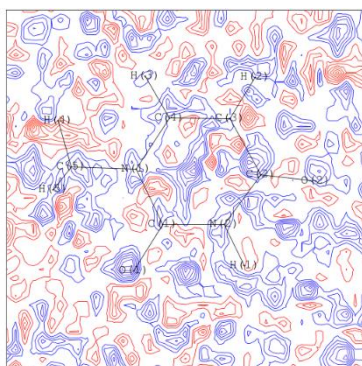


TAAM Shade 0.81Å

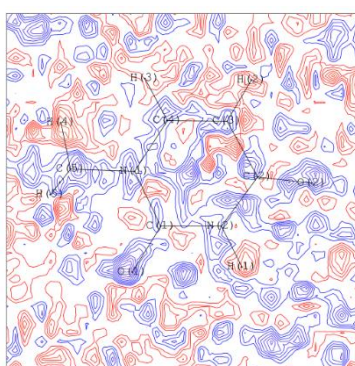


TAAM iso 0.81Å

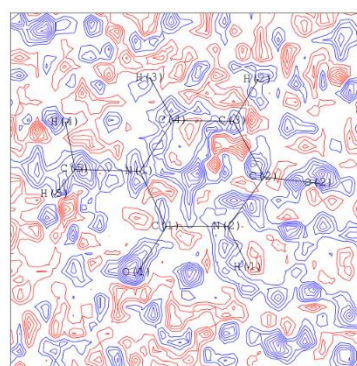
Figure S3 Residual density maps of **2** and **2-cutoff** (details are given below the maps). All maps are presented with contours levels with intervals $\pm 0.05 \text{ e}\text{\AA}^{-3}$. Blue lines represent positive values and red lines the negative ones. Maps were prepared for planes determined by C3 (centre), C4 (x axis) and C2 (y axis) atoms.



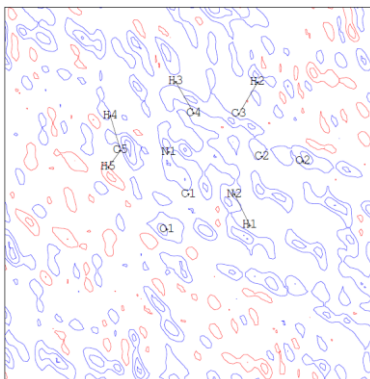
MM



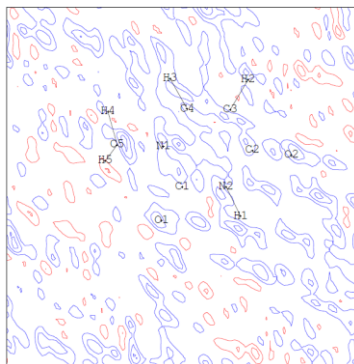
TAAM Mo Shade



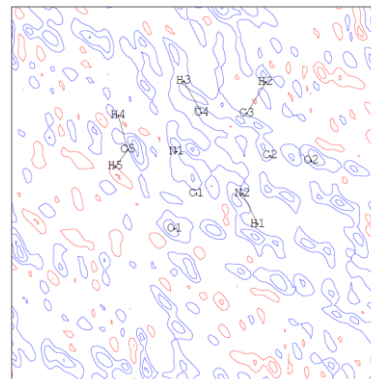
TAAM Mo iso



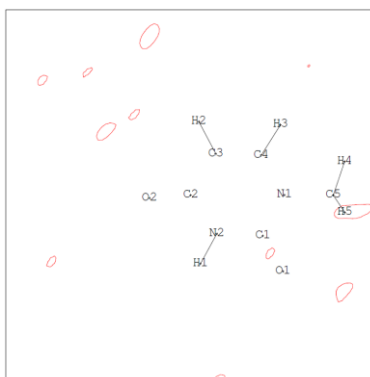
HAR Mo aniso



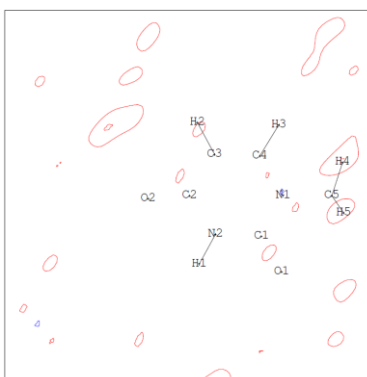
HAR Mo iso



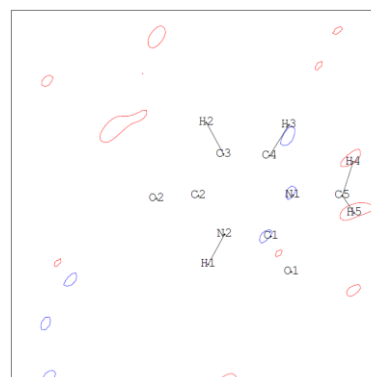
HAR Mo Shade



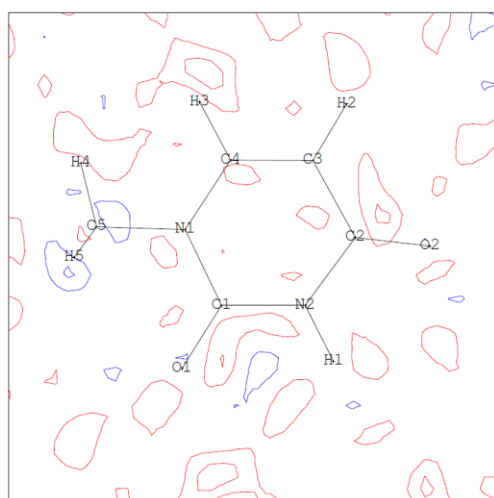
HAR Mo aniso 0.81Å



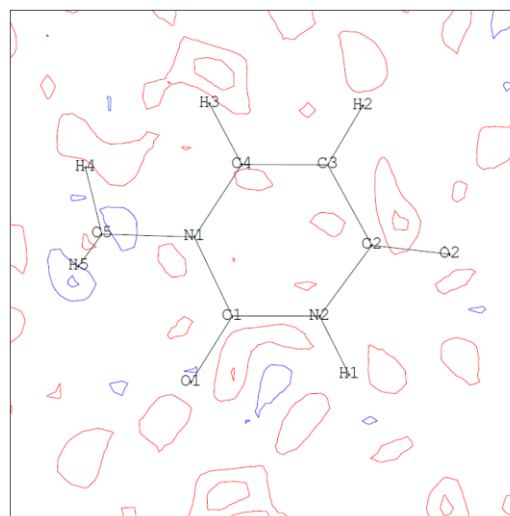
HAR Mo iso 0.81Å



HAR Mo Shade 0.81Å



TAAM Shade 0.81Å



TAAM iso 0.81Å

Figure S4 Residual density maps of **3** and **3-cutoff** (details are given below the maps). All maps are presented with contours levels with intervals $\pm 0.05 \text{ e}\text{\AA}^{-3}$. Blue lines represent positive values and red lines the negative ones. Maps were prepared for planes determined by C1 (centre), N2 (x axis) and C4 (y axis) atoms.

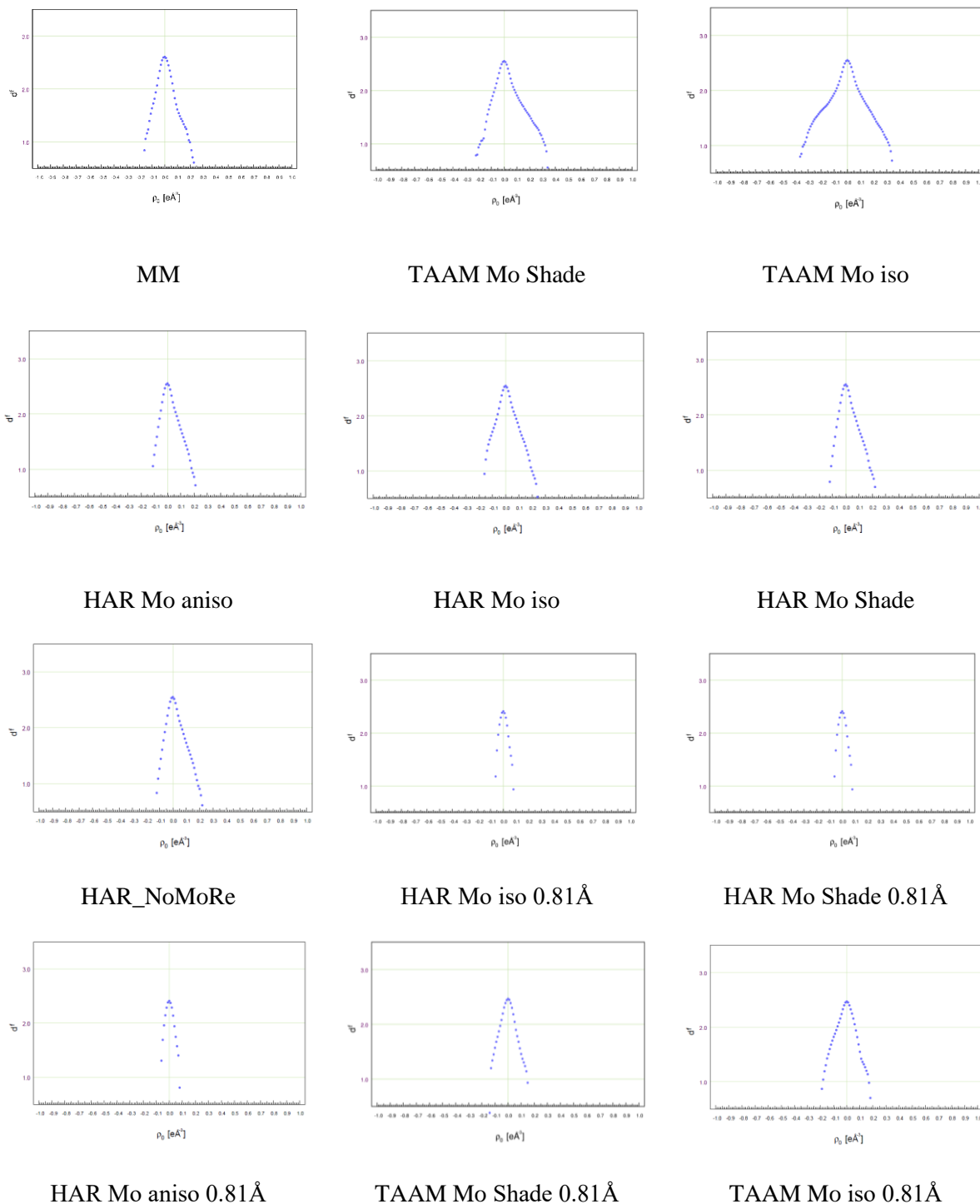


Figure S5 Fractal plots of **1** and **1-cutoff**

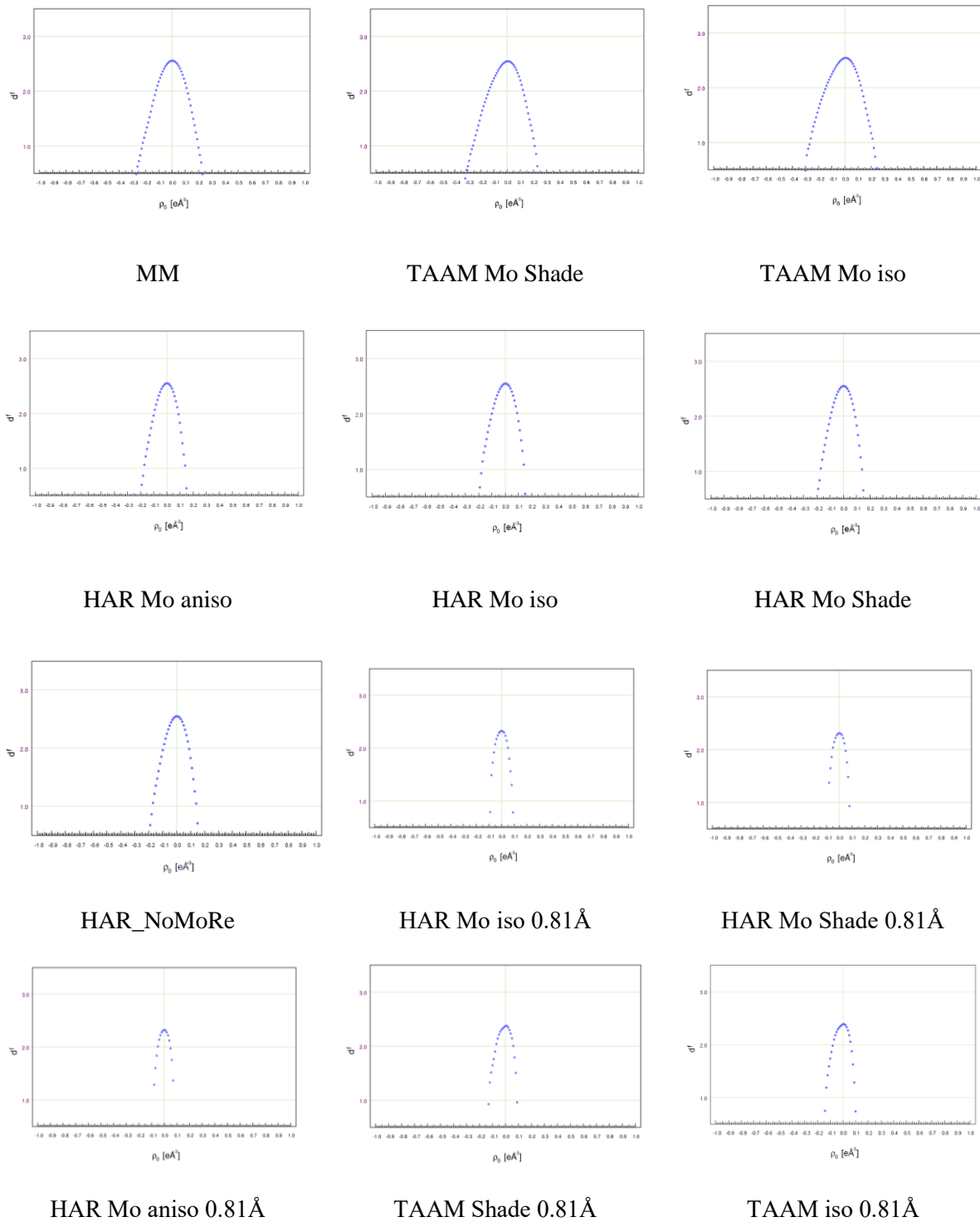


Figure S6 Fractal plots of **2** and **2-cutoff**

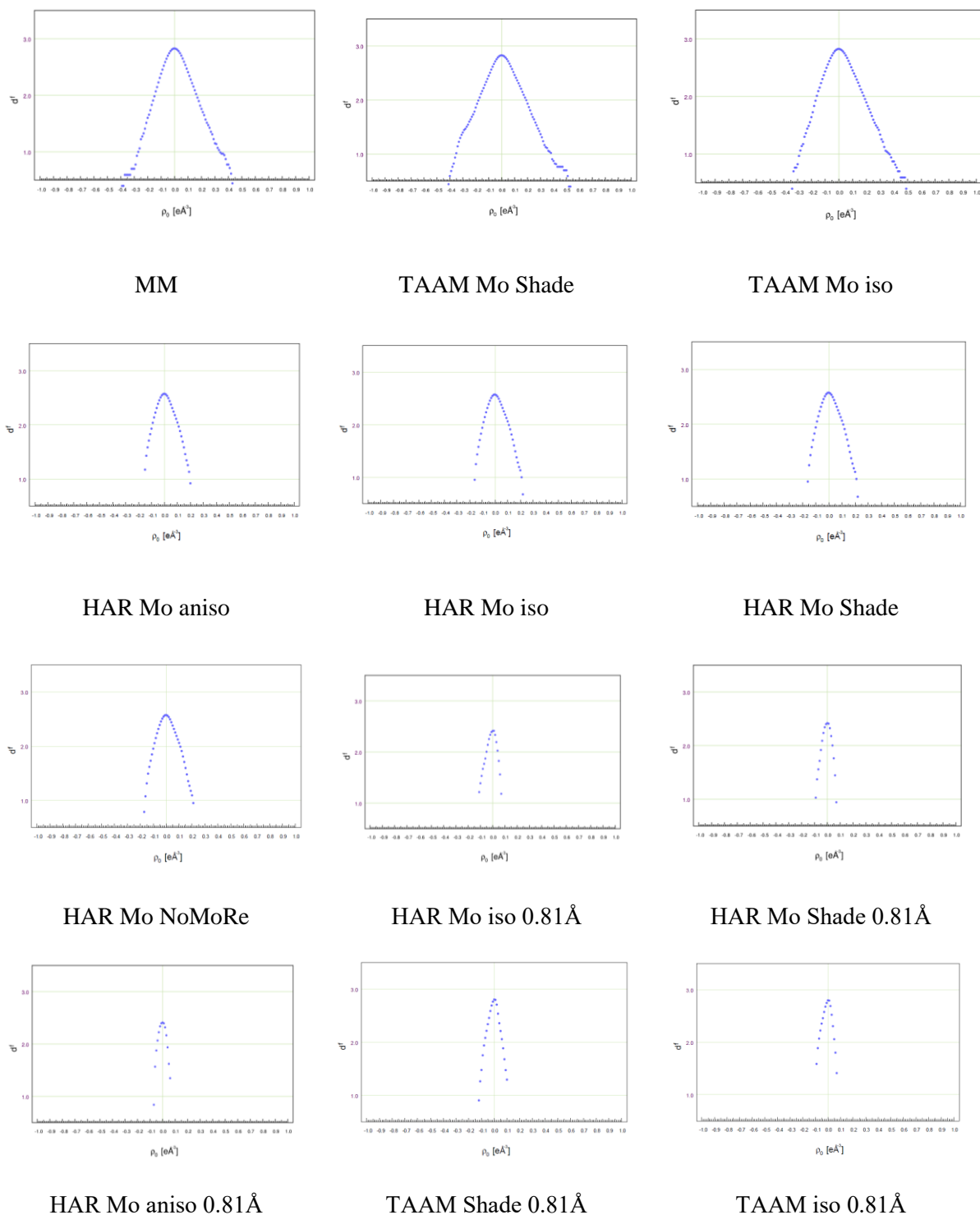
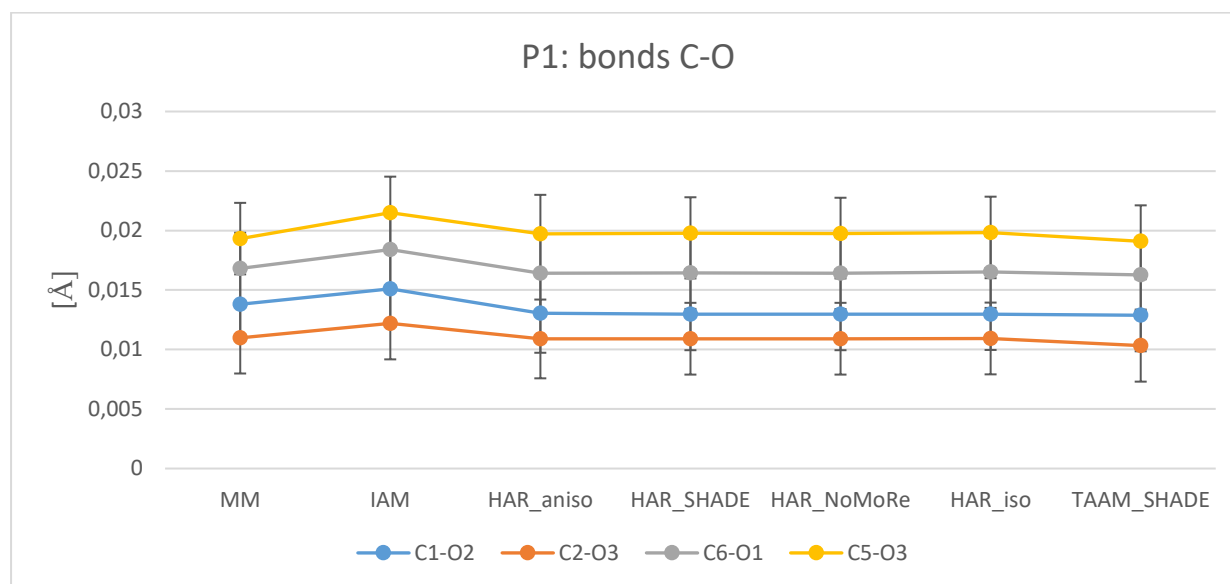


Figure S7 Fractal plots of **3** and **3-cutoff**

Table S13 Summary of the d^f maximum of the fractal dimension plots.

	1	2	3
MM	2.551	2.556	2.828
TAAM_Mo_Shade	2.551	2.545	2.827
TAAM_Mo_iso	2.546	2.542	2.827
HAR_Mo_aniso	2.546	2.550	2.577
HAR_Mo_iso	2.545	2.547	2.576
HAR_Mo_Shade	2.551	2.550	2.576
HAR_NoMoRe	2.551	2.550	2.576
HAR_Mo_iso_0.81	2.412	2.327	2.413
HAR_Mo_Shade_0.81	2.412	2.302	2.418
HAR_Mo_aniso_0.81	2.412	2.321	2.410
TAAM_Mo_Shade_0.81	2.464	2.373	2.780
TAAM_Mo_iso_0.81	2.473	2.387	2.780



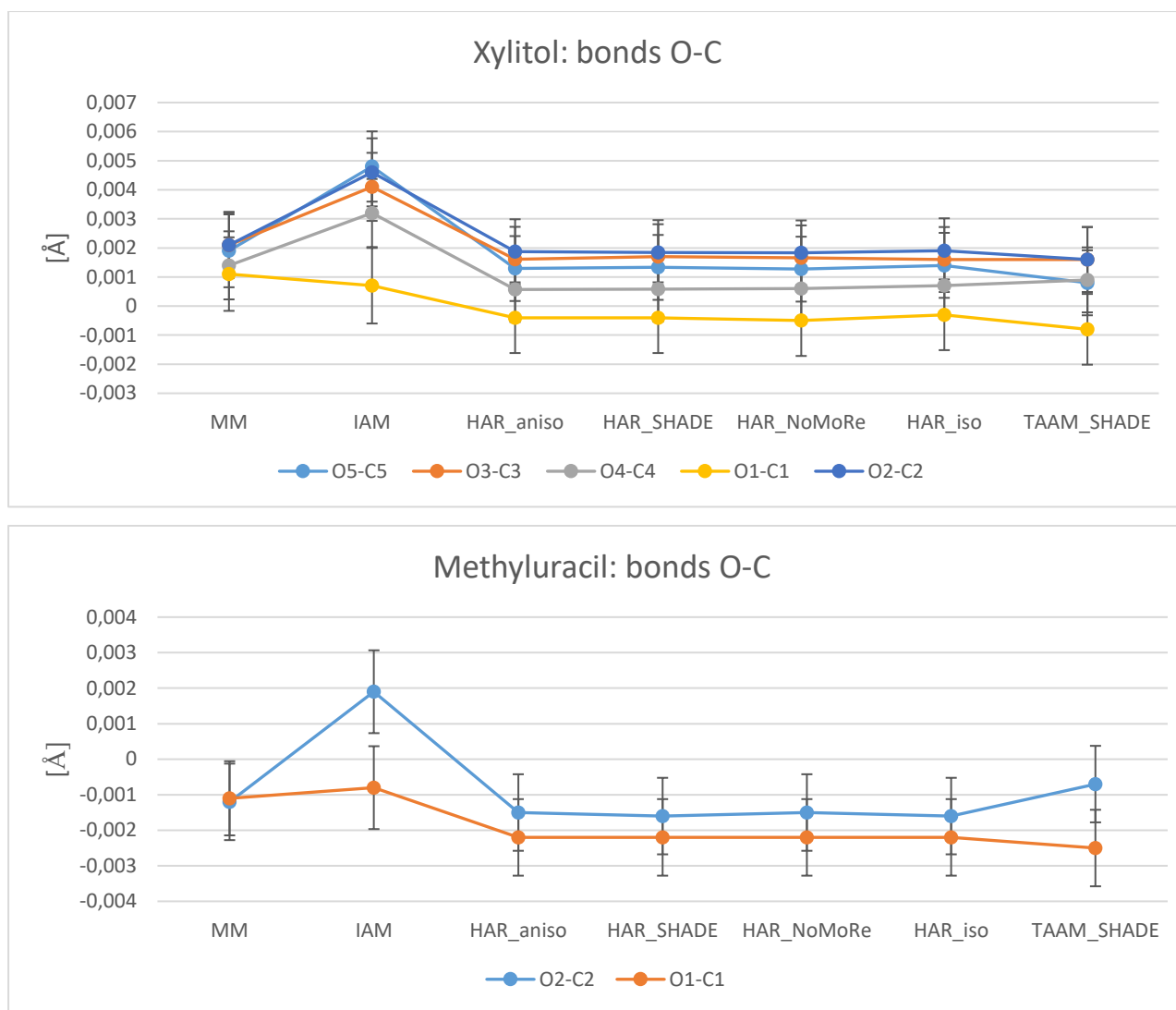


Figure S8 Comparison of O-C bonds for IAM, MM, HAR and TAAM refinements of **1**, **2** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.

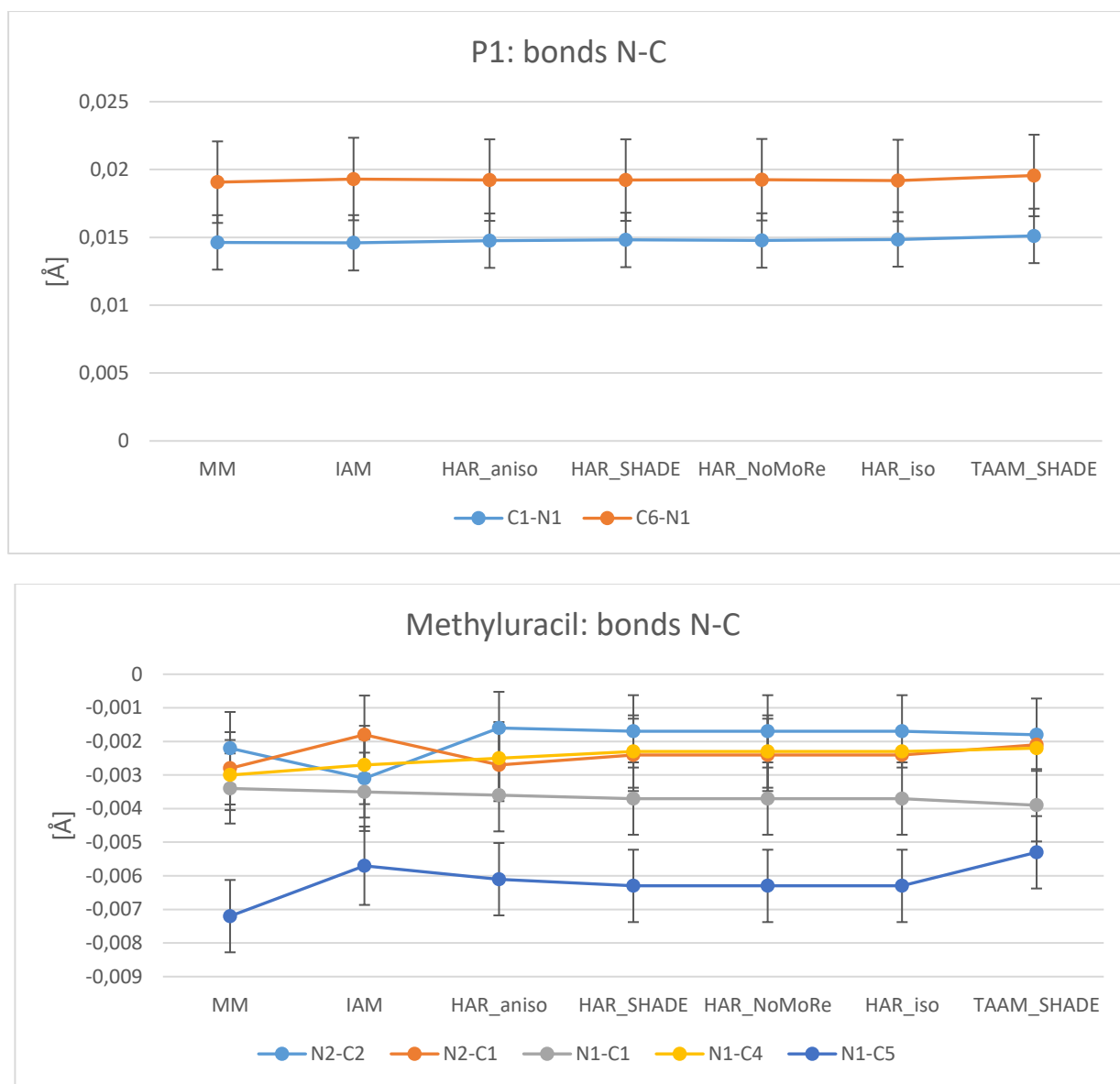
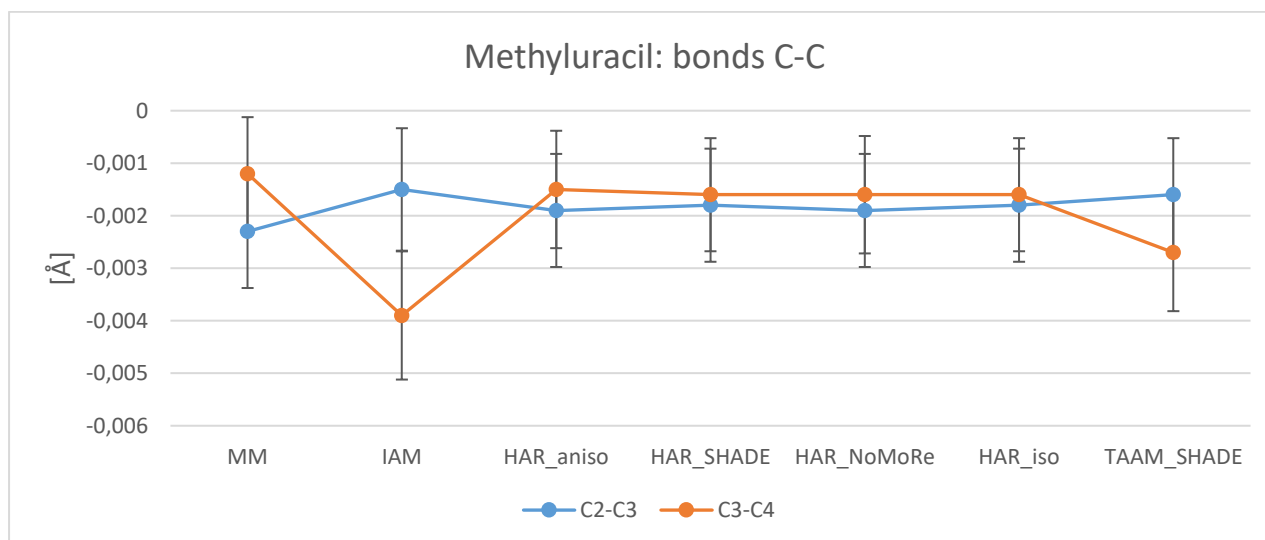
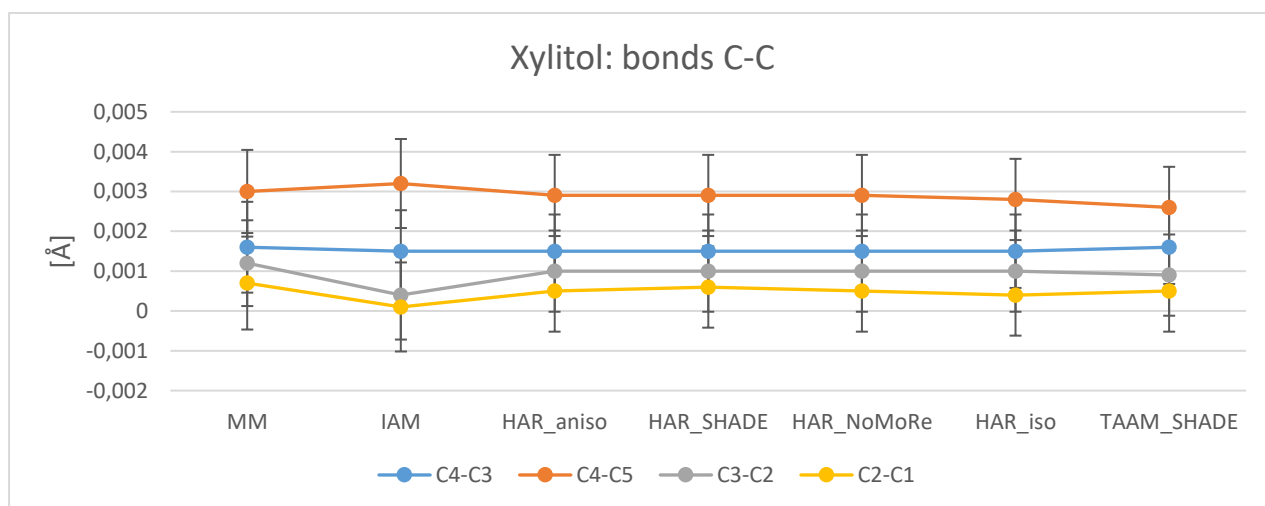
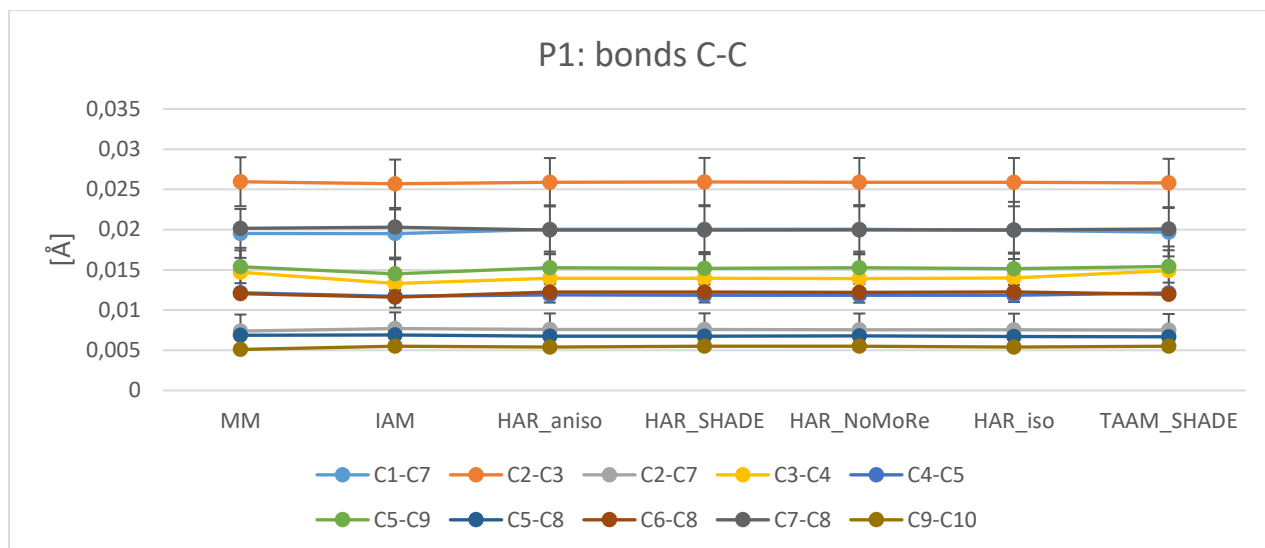
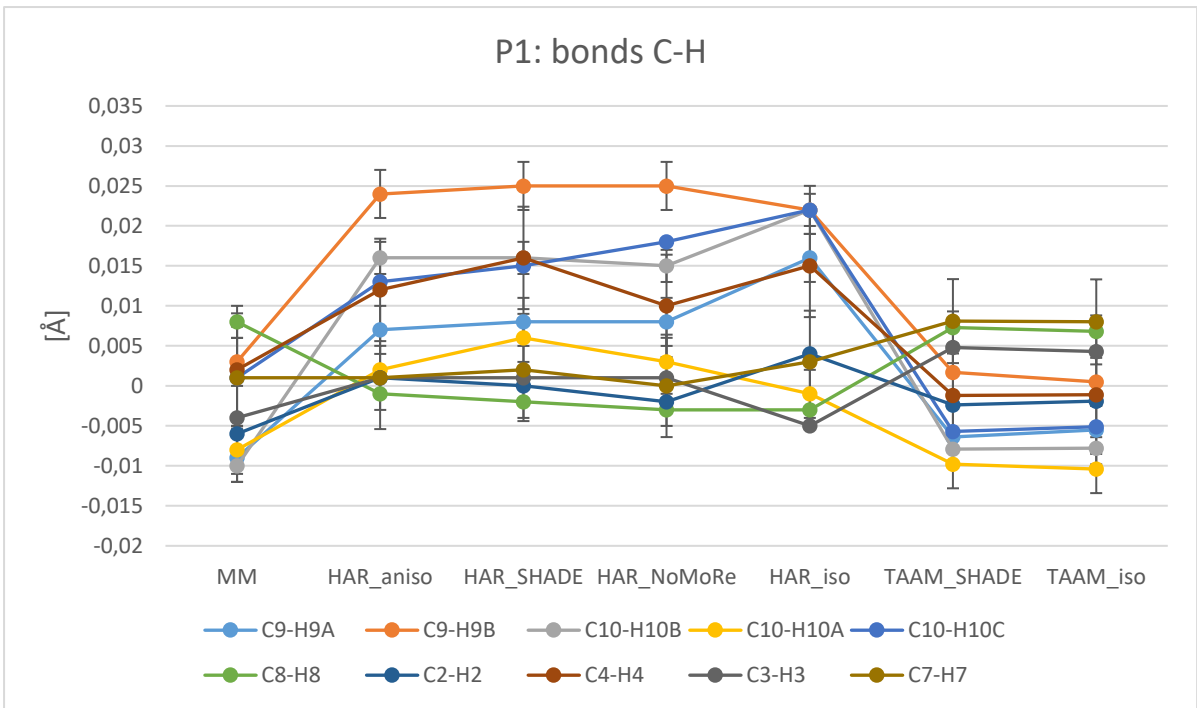


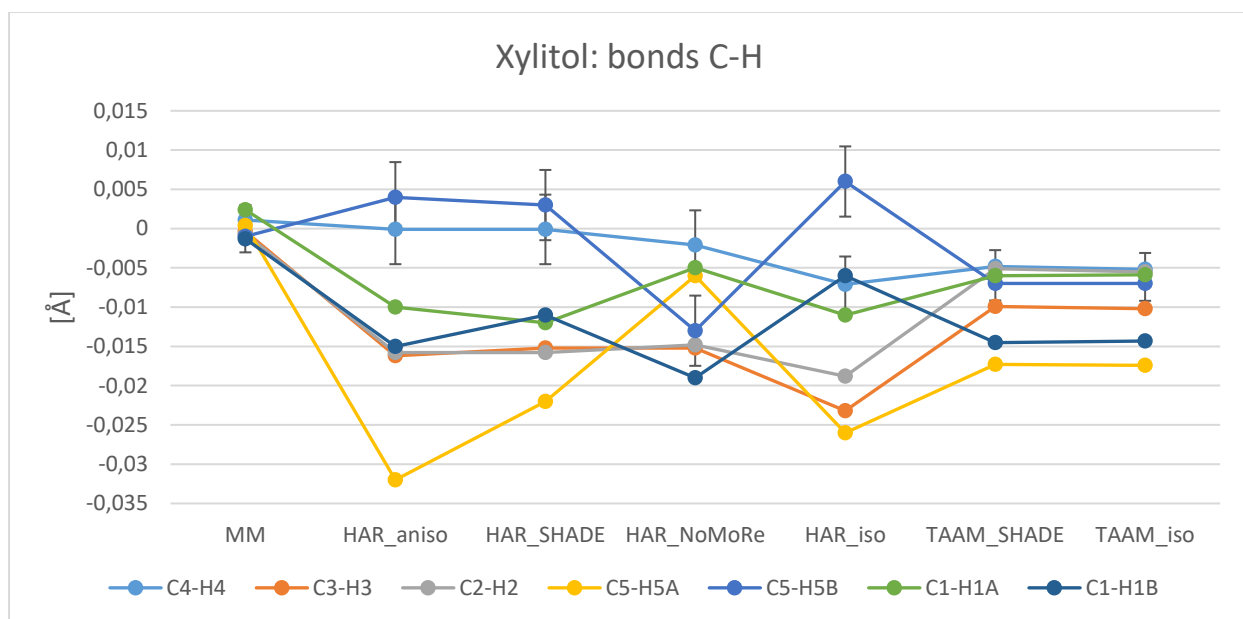
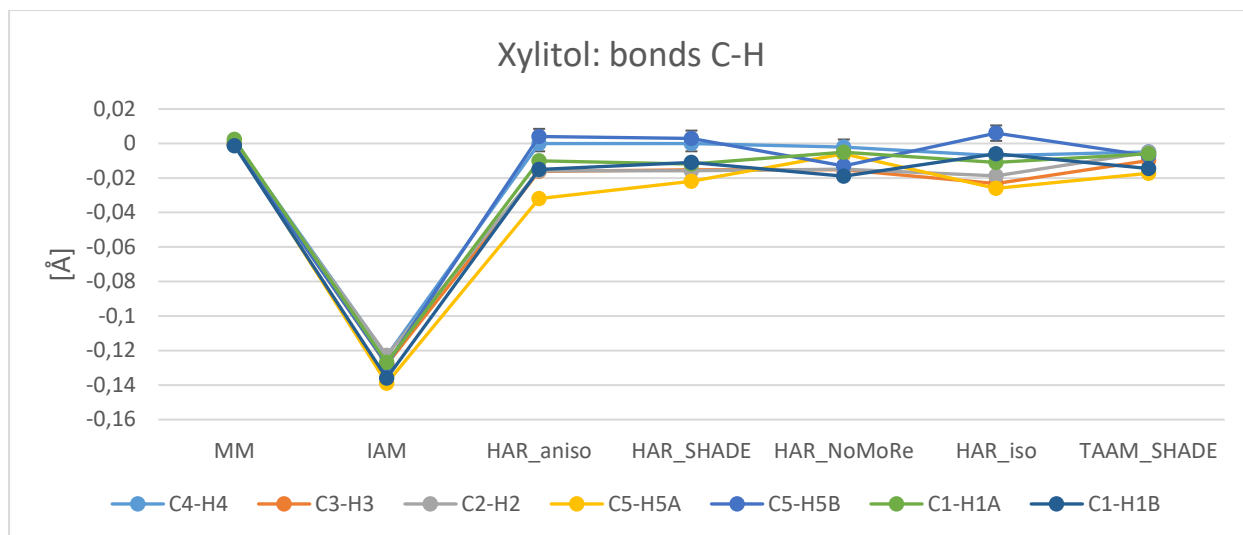
Figure S9 Comparison of N-C bonds for IAM, MM, HAR and TAAM refinements of **1** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.



P1: bonds C-H

Bond	MM	IAM	HAR_aniso	HAR_SHADE	HAR_NoMoRe	HAR_iso	TAAM_SHADE
C9-H9A	0.00	-0.12	0.01	0.01	0.01	0.02	0.00
C9-H9B	0.00	-0.11	0.02	0.02	0.02	0.02	0.00
C10-H10B	0.00	-0.13	0.01	0.01	0.01	0.01	0.00
C10-H10A	0.00	-0.14	0.01	0.01	0.01	0.01	-0.01
C10-H10C	0.00	-0.12	0.01	0.01	0.01	0.02	0.00
C8-H8	0.00	-0.11	0.00	0.00	0.00	0.00	0.00
C2-H2	0.00	-0.12	0.01	0.01	0.01	0.01	0.00
C4-H4	0.00	-0.16	0.01	0.01	0.01	0.01	0.00
C3-H3	0.00	-0.11	0.00	0.00	0.00	0.00	0.00
C7-H7	0.00	-0.11	0.00	0.00	0.00	0.00	0.00





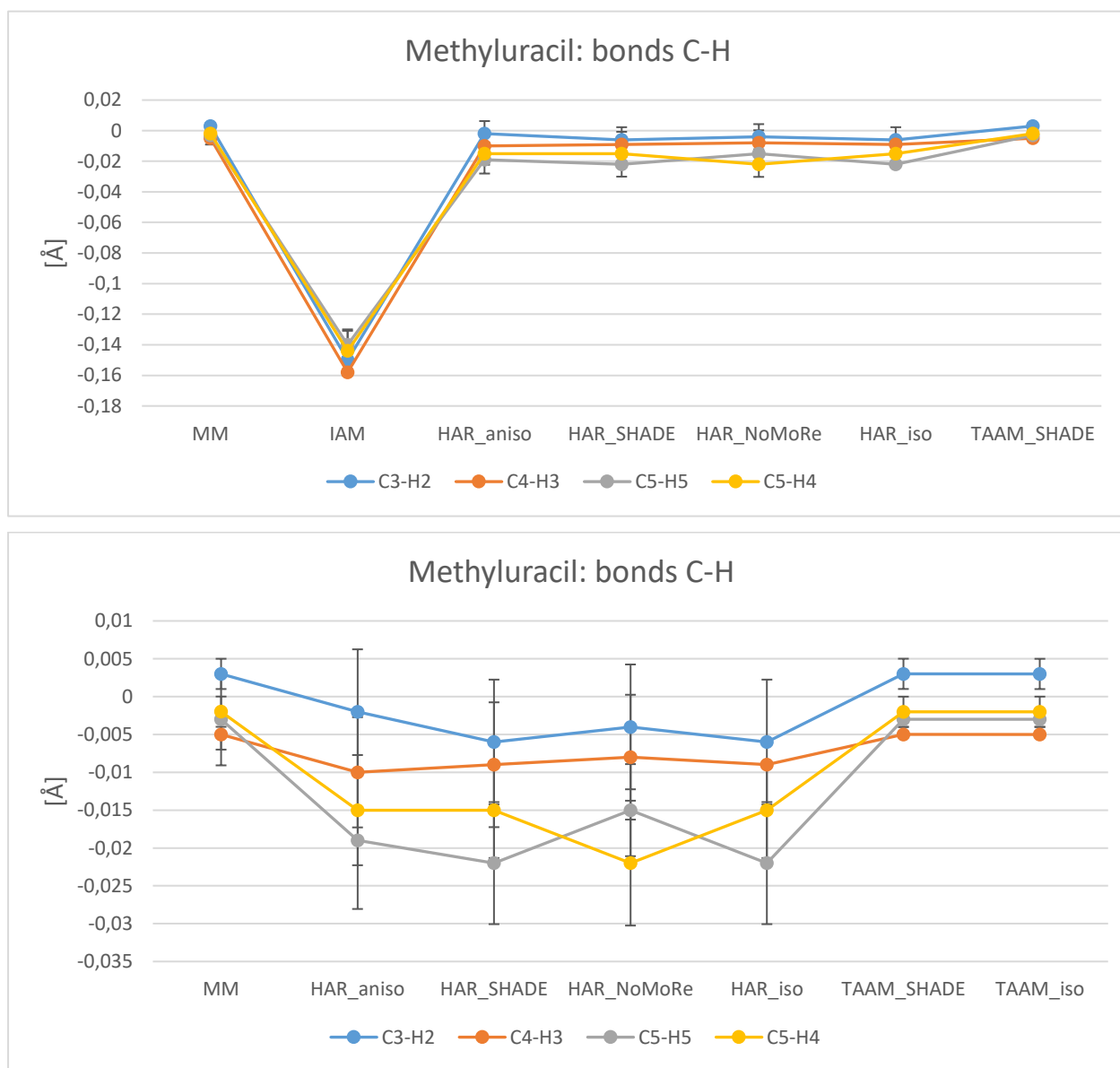
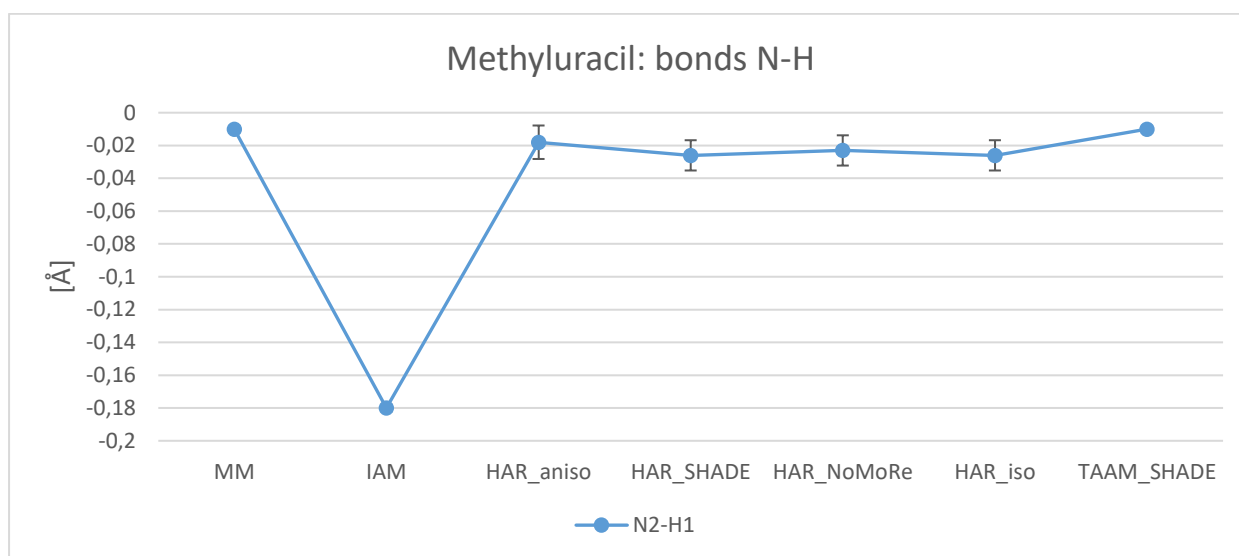
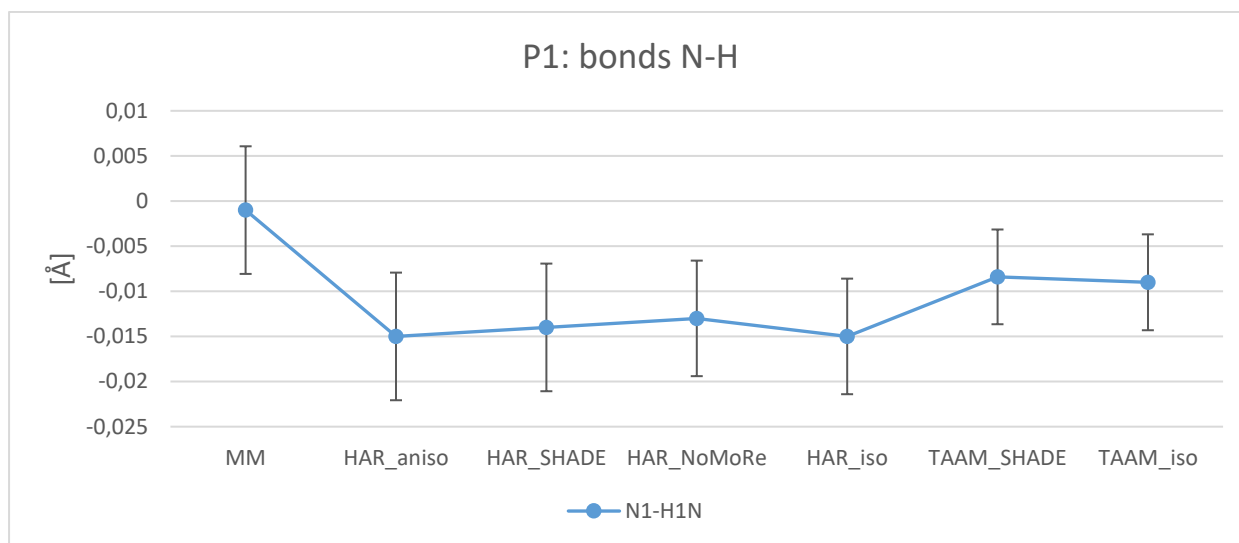
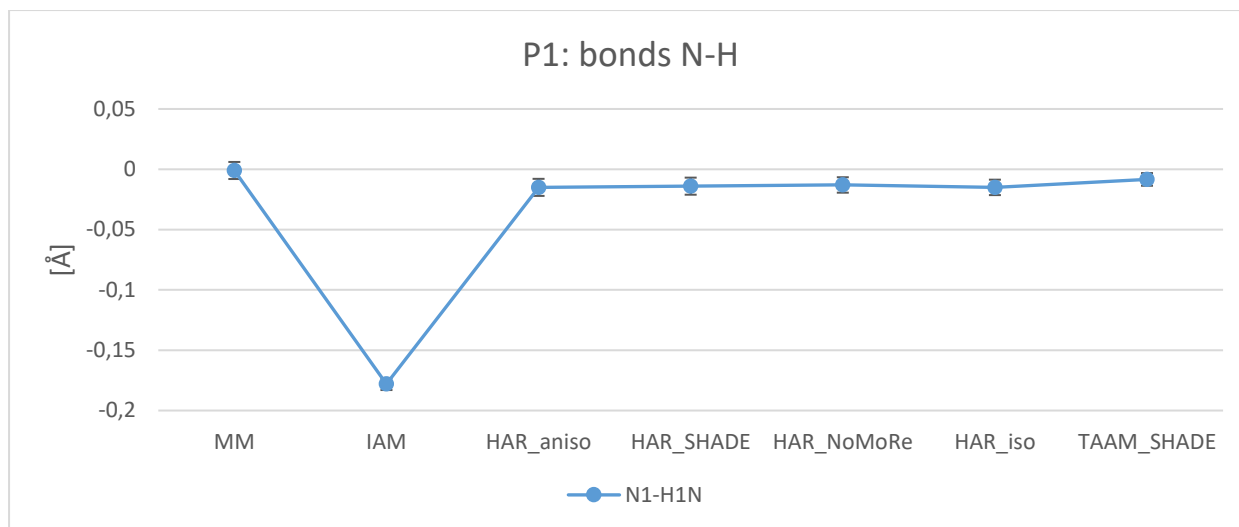


Figure S11 Comparison of C-H bonds for IAM, MM, HAR and TAAM refinements of **1**, **2** and **3**. For clarity, additional plots without IAM are presented. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.



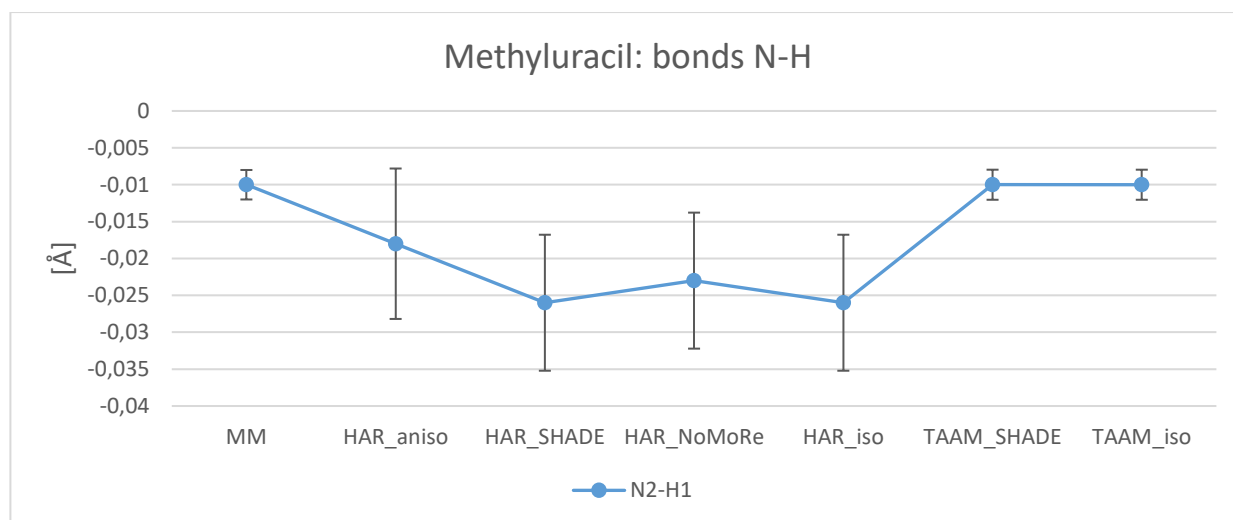
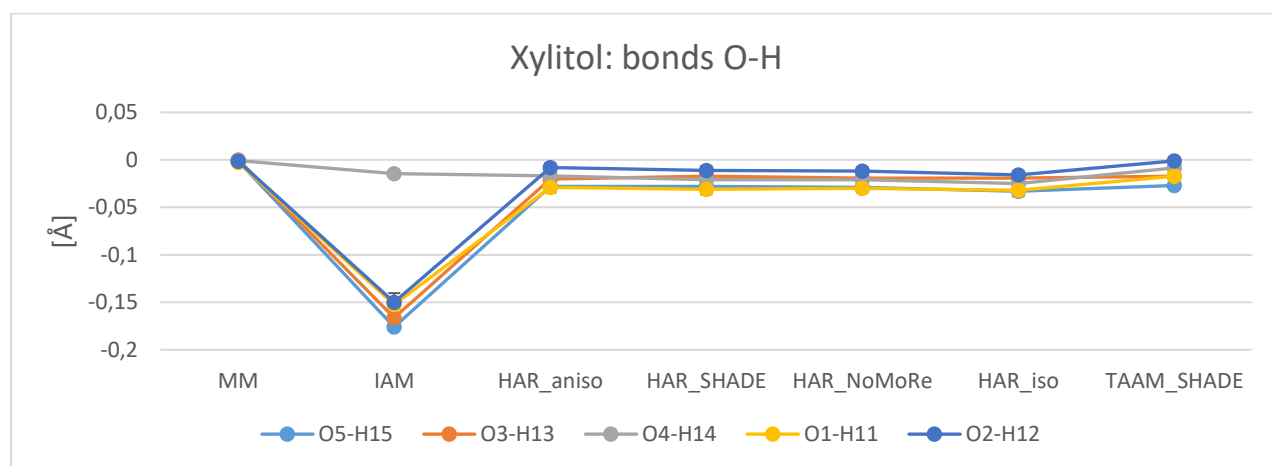


Figure S12 Comparison of N-H bonds for IAM, MM, HAR and TAAM refinements of **1** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. For clarity, additional plots without IAM are presented. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.



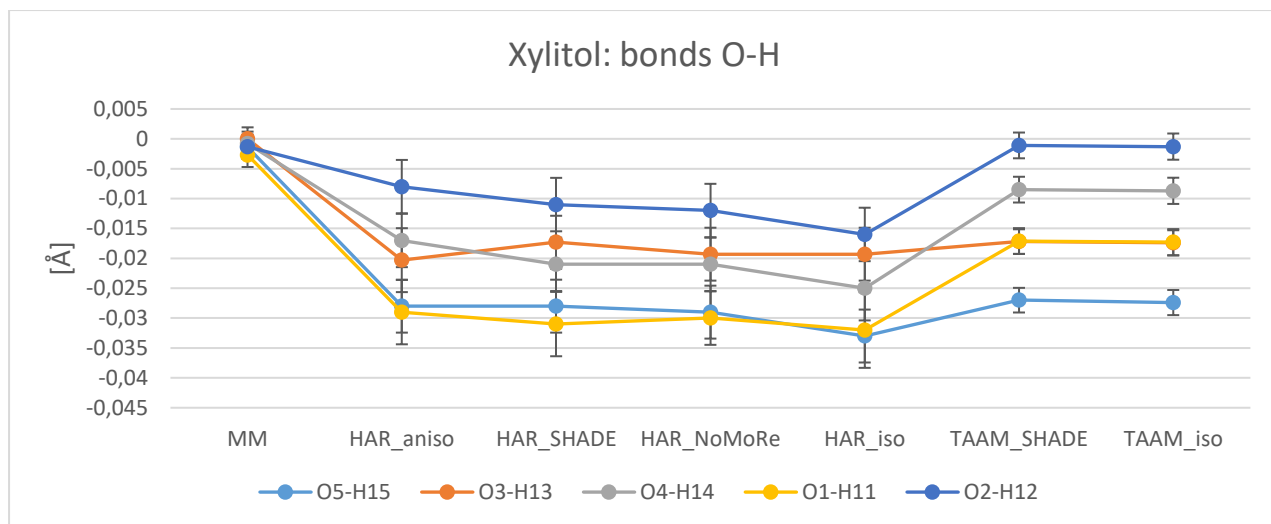
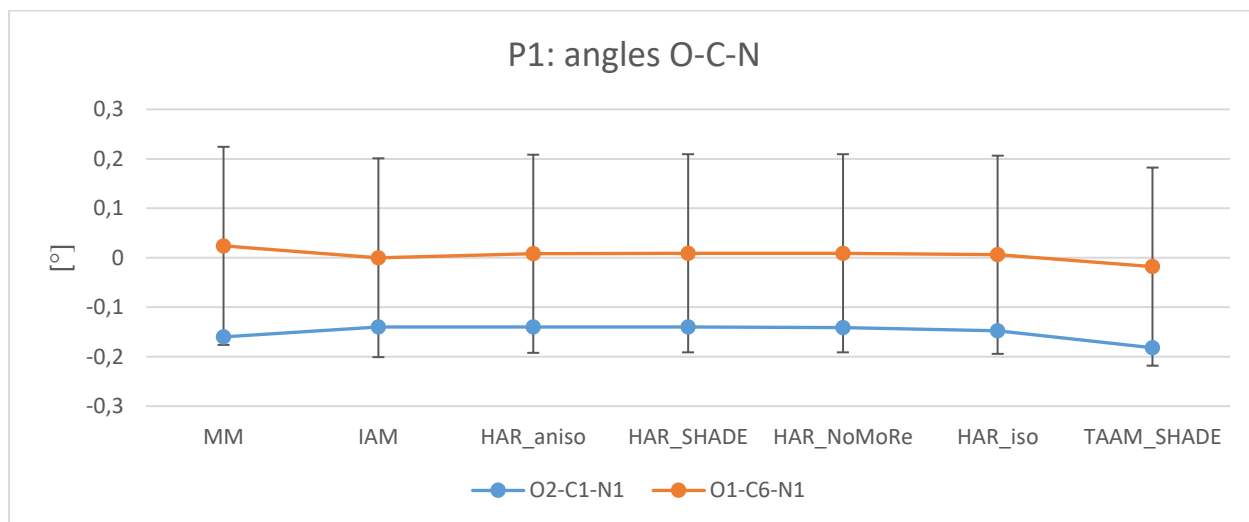


Figure S13 Comparison of O-H bonds for IAM, MM, HAR and TAAM refinements of **2**. For clarity, additional plot without IAM are presented. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.



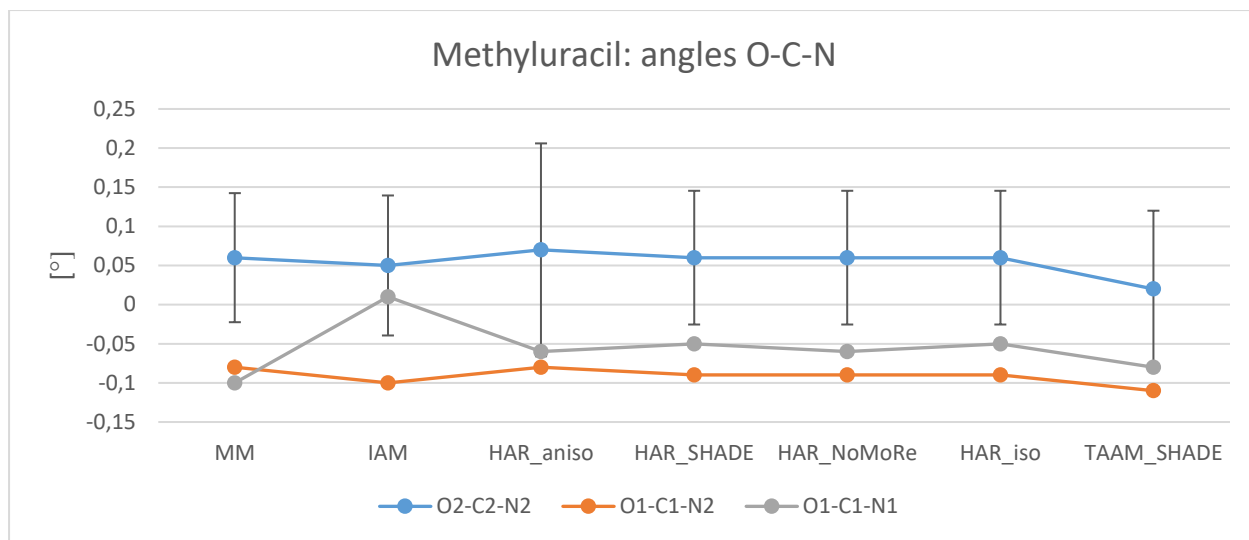
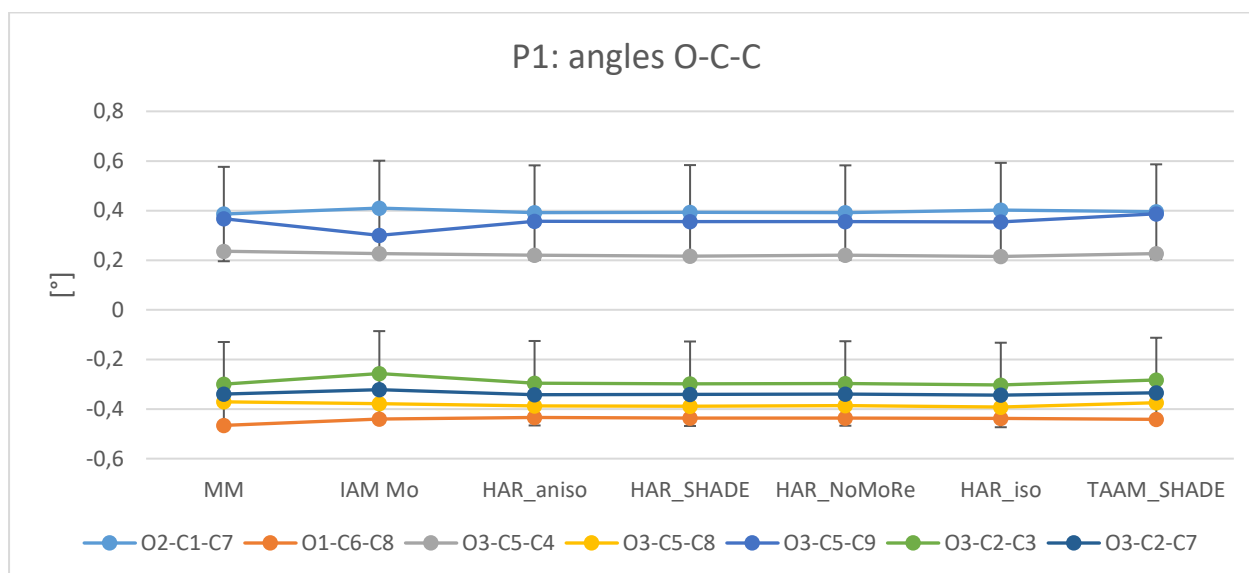


Figure S14 Comparison of O-C-N angles for MM, IAM, HAR and TAAM refinements of **1** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For clarity standard deviations were added only for O1-C6-N1 (for P1) and O2-C2-N2 angles (for methyluracil).



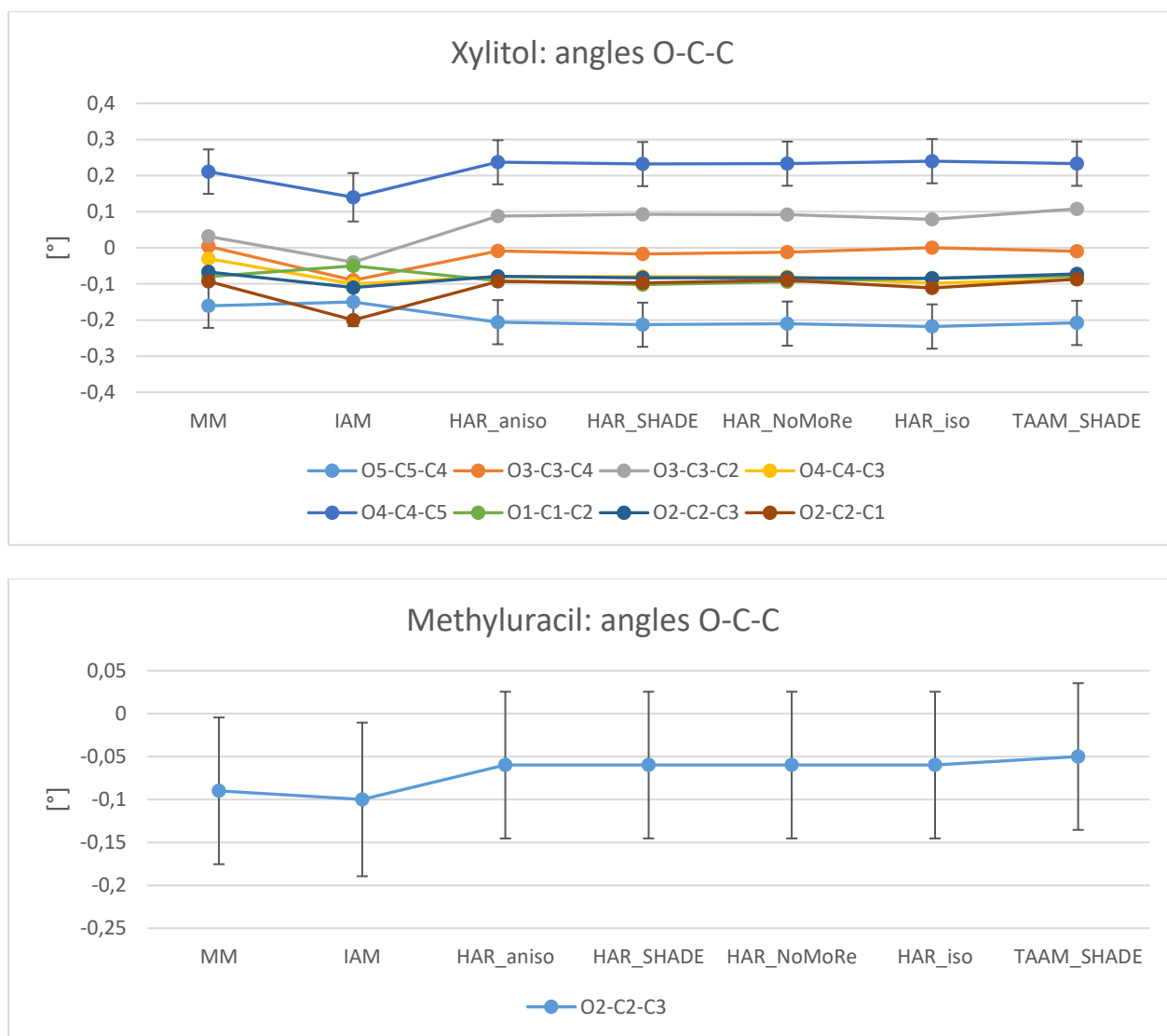


Figure S15 Comparison of O-C-C angles for MM, IAM, HAR and TAAM refinements of **1**, **2** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For clarity estimated standard deviations for **1** were added only for O2-C1-C7 and O3-C2-C3 angles, whereas for **2** only for O5-C5-C4 and O4-C4-C5 angles.

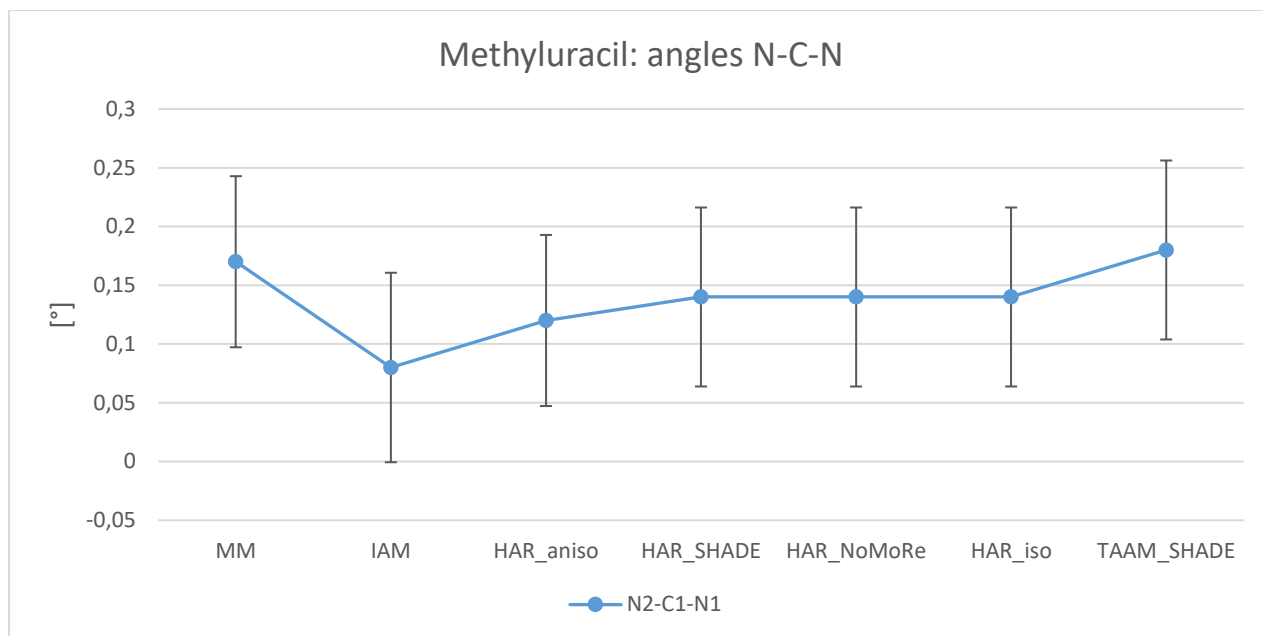
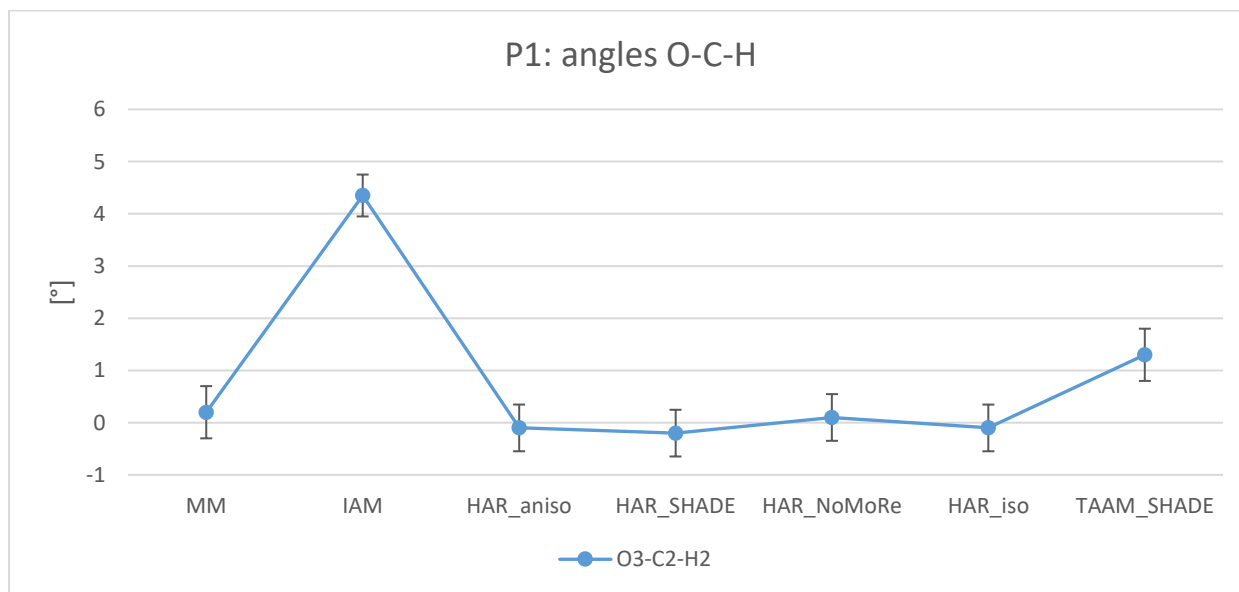


Figure S16 Comparison of N-C-N angles for MM, IAM, HAR and TAAM refinements of **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. Estimated standard deviations were added.



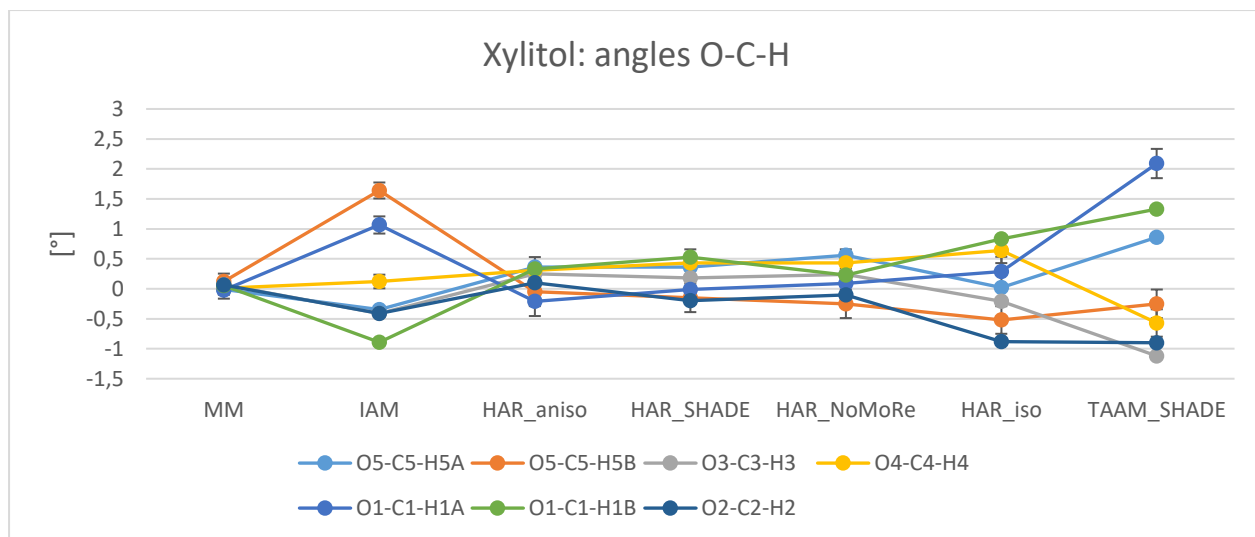
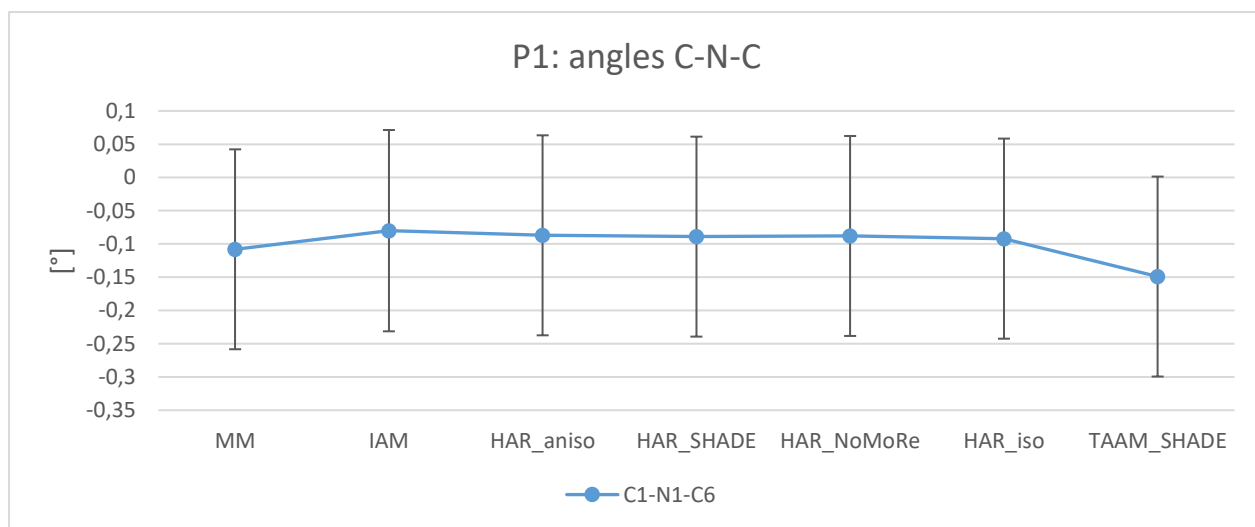


Figure S17 Comparison of O-C-H angles for MM, IAM, HAR and TAAM refinements of **1** and **2**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For clarity estimated standard deviations for **2** were added only for O4-C4-H4, O5-C5-H5B and O2-C2-H2 angles.



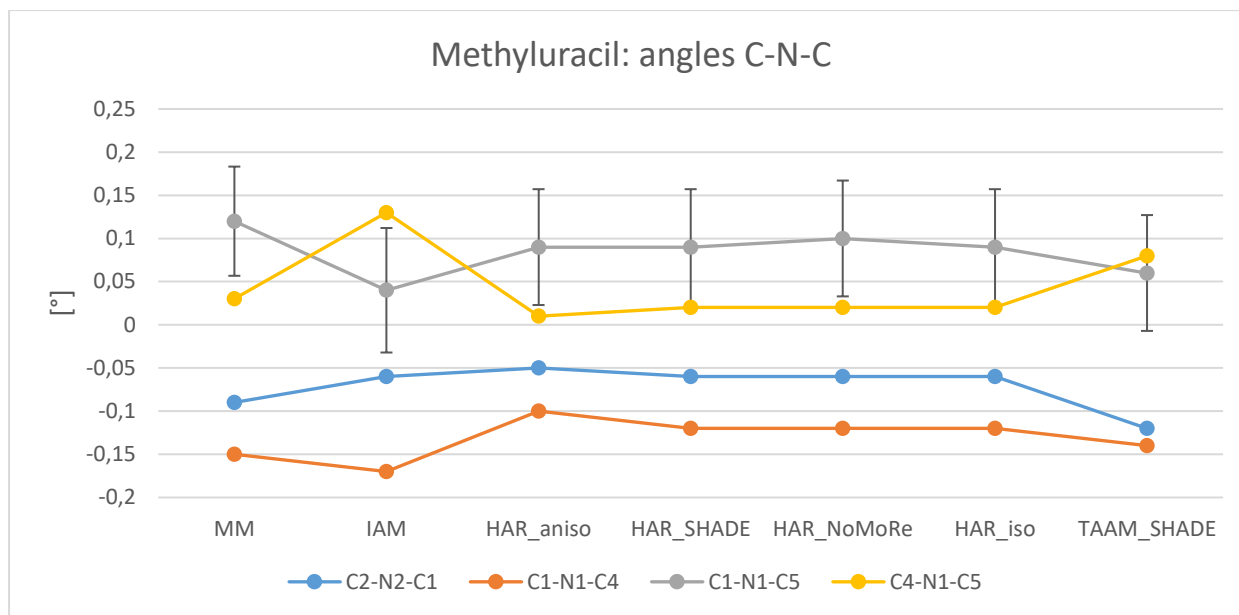
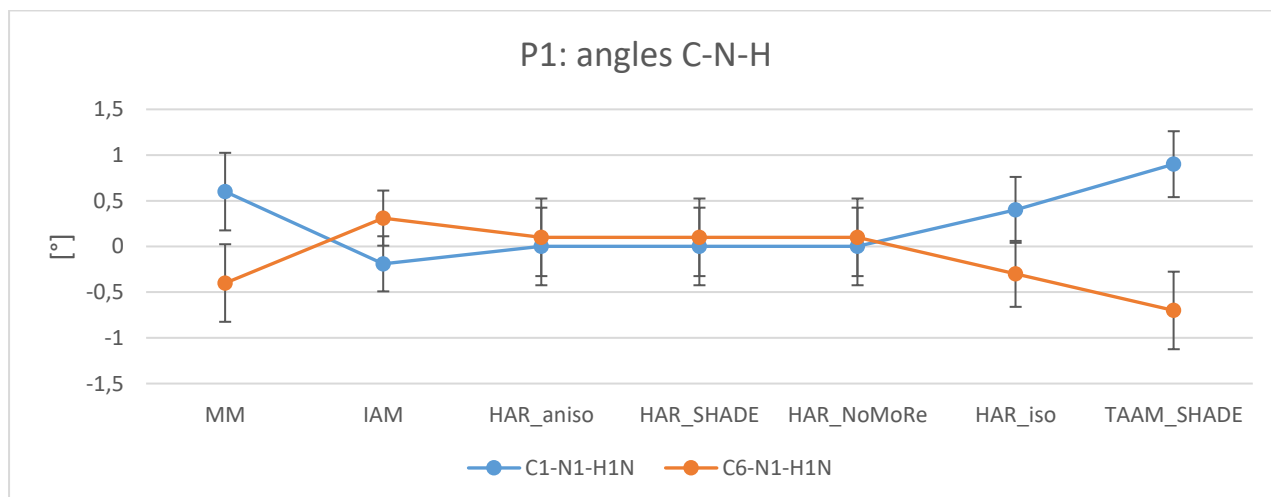


Figure S18 Comparison of C-N-C angles for MM, IAM, HAR and TAAM refinements of **1** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For clarity estimated standard deviations for **3** were added only for C1-N1-C5 angles.



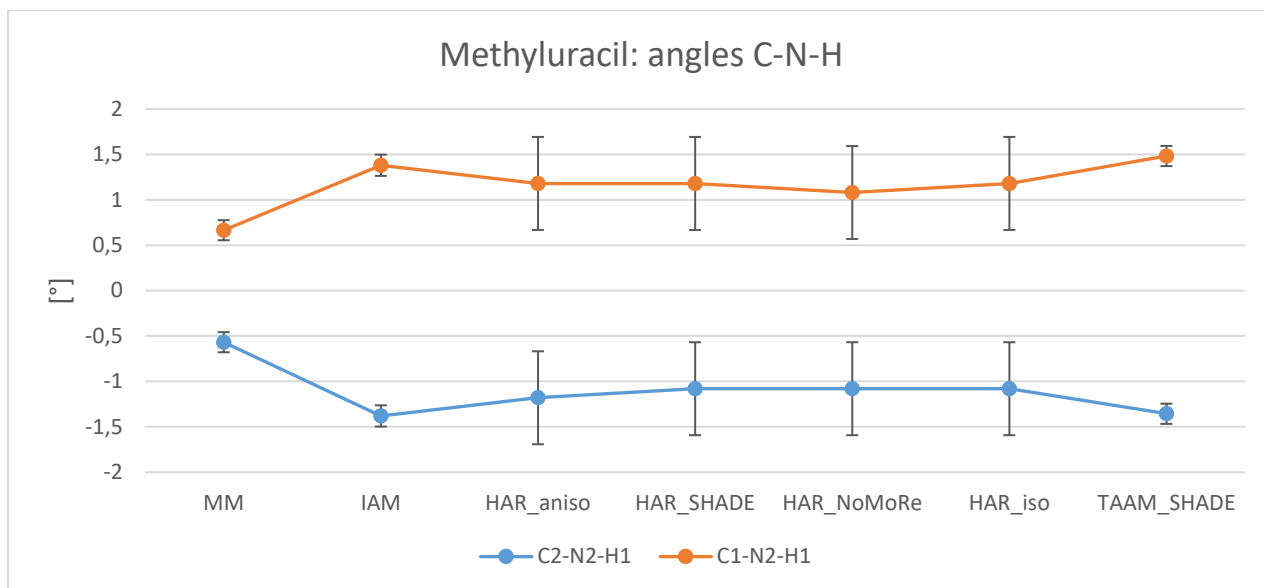


Figure S19 Comparison of C-N-H angles for MM, IAM, HAR and TAAM refinements of **1** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.

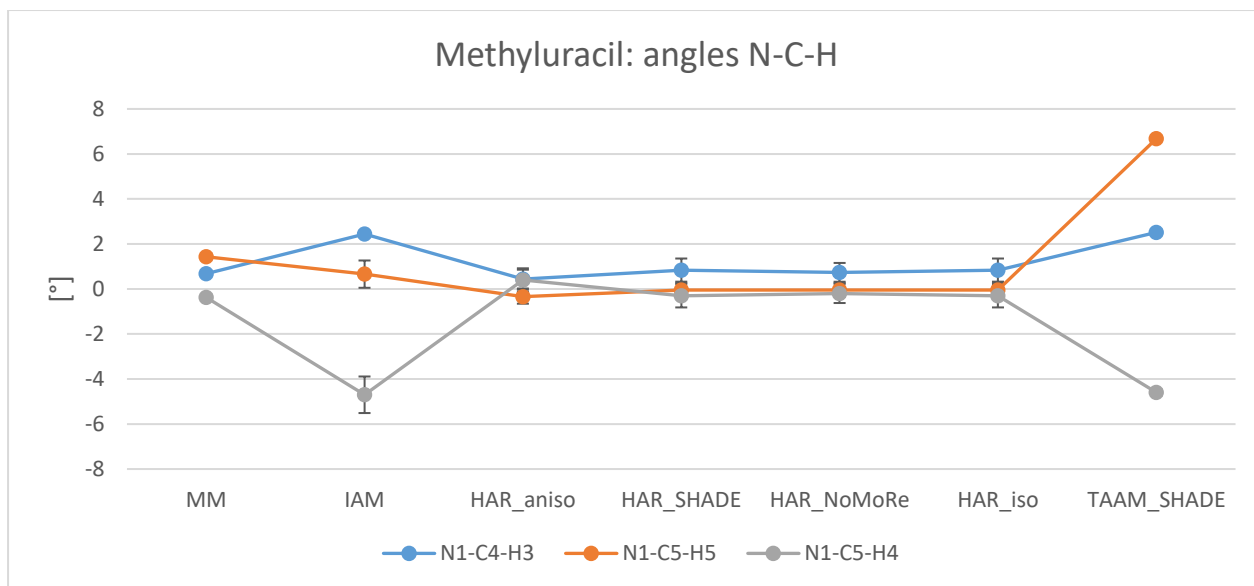
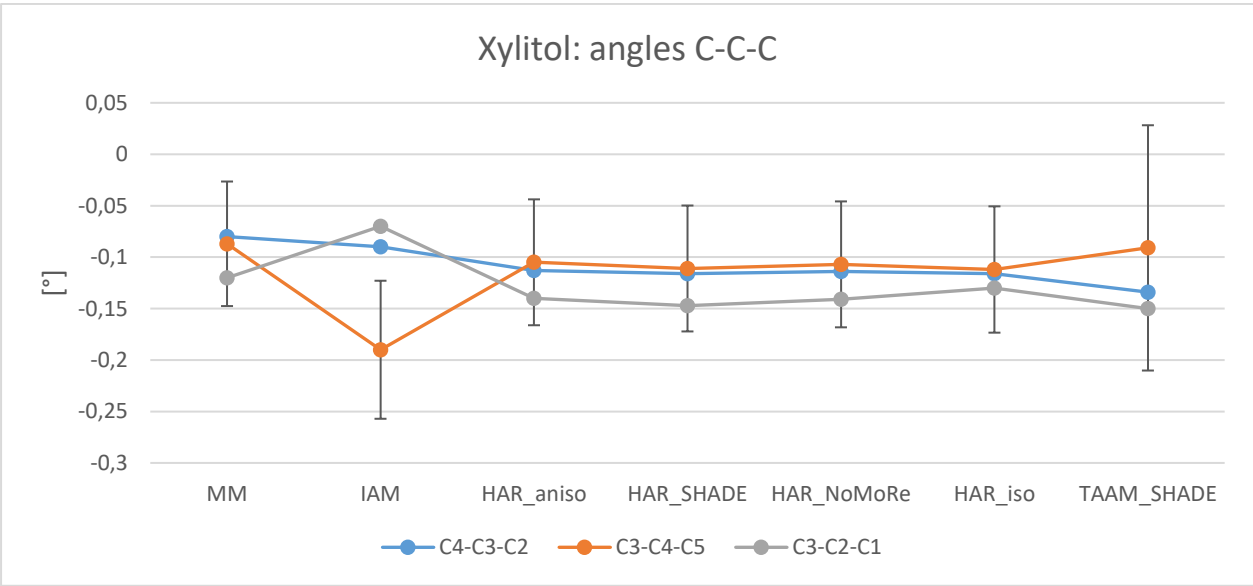
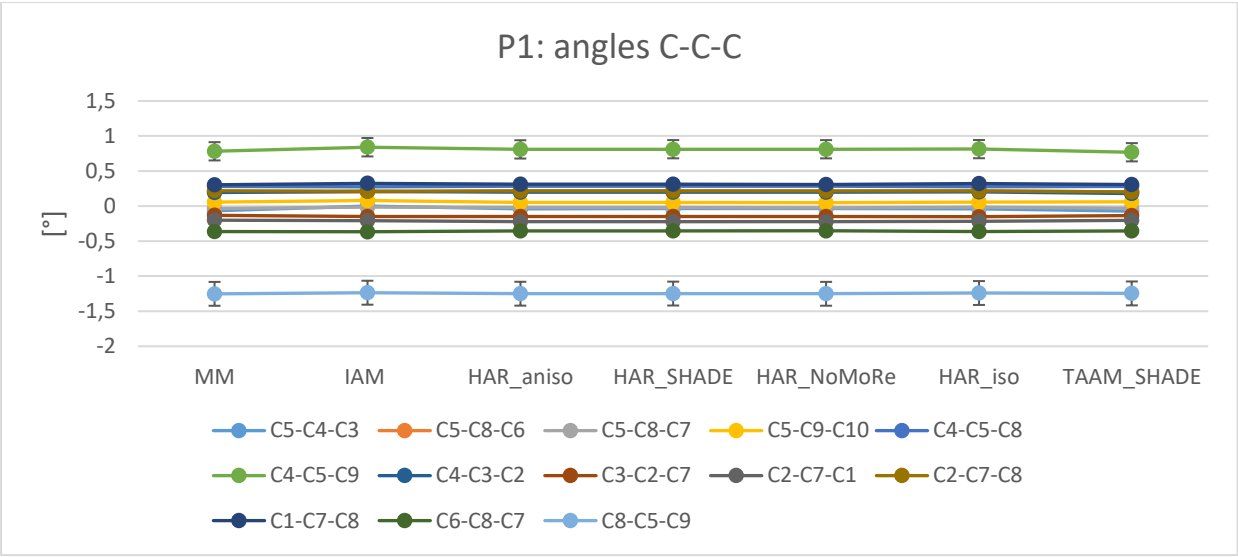


Figure S20 Comparison of N-C-H angles for MM, IAM, HAR and TAAM refinements of **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.



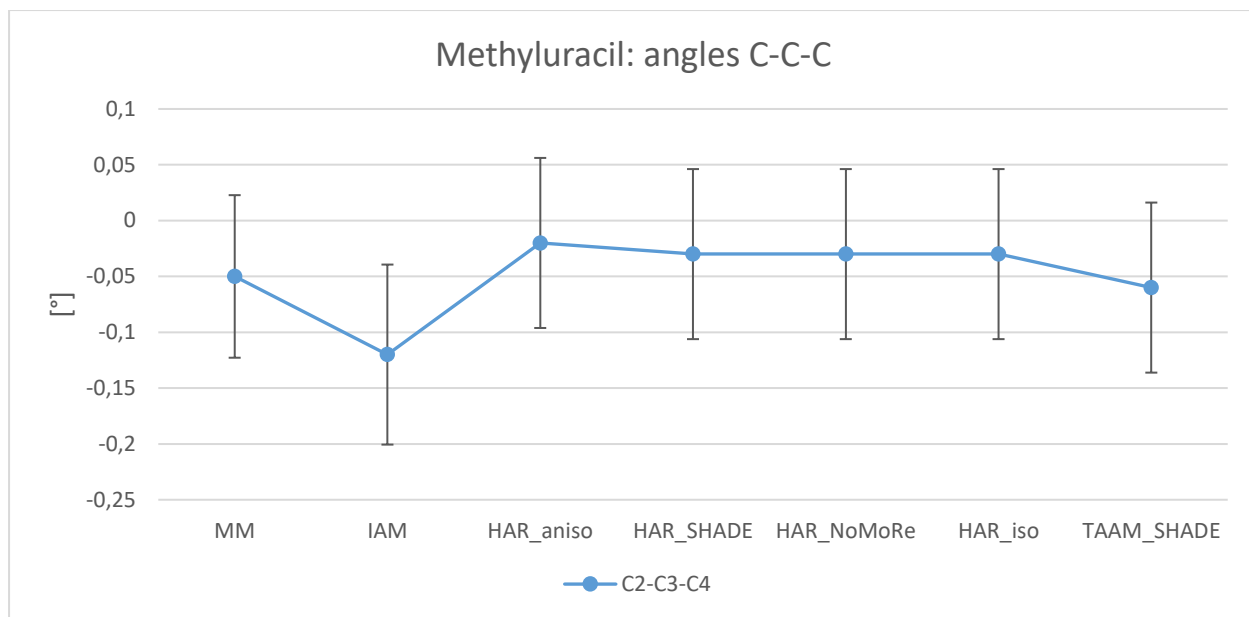
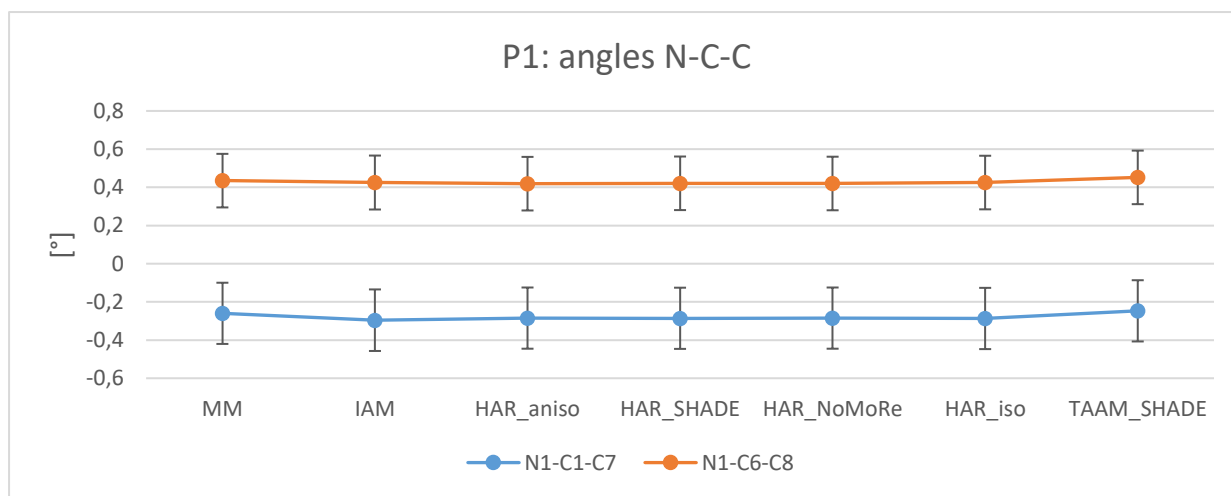


Figure S21 Comparison of C-C-C angles for MM, IAM, HAR and TAAM refinements of **1**, **2** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For clarity estimated standard deviations for **1** were added only for C4-C5-C9 and C8-C5-C9 angles, whereas for **2** only for C3-C4-C5 angles.



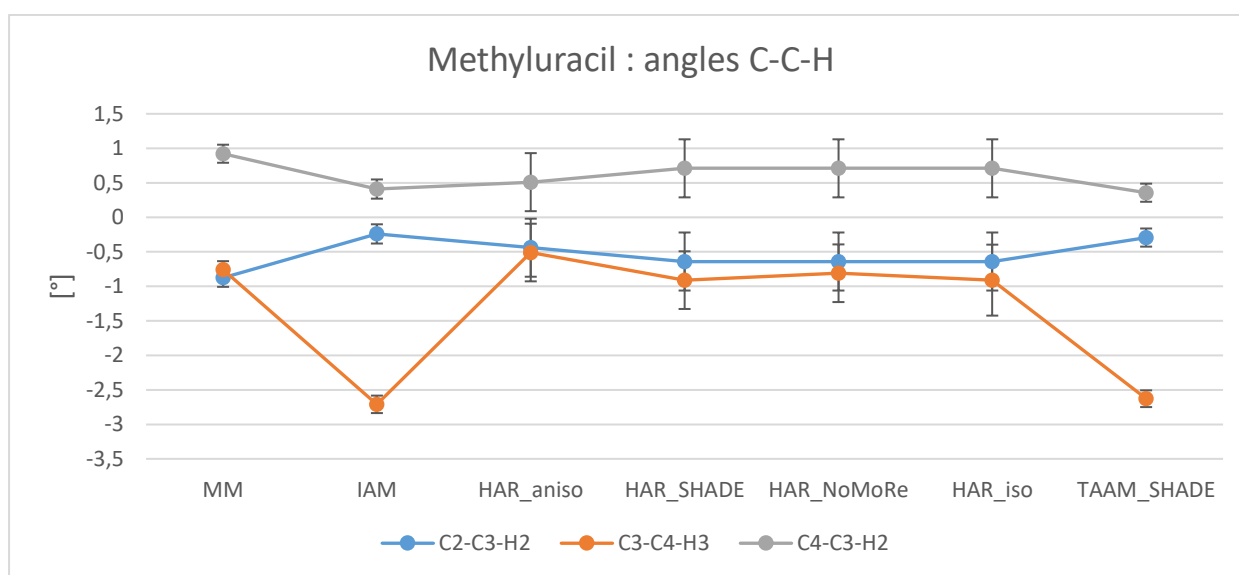
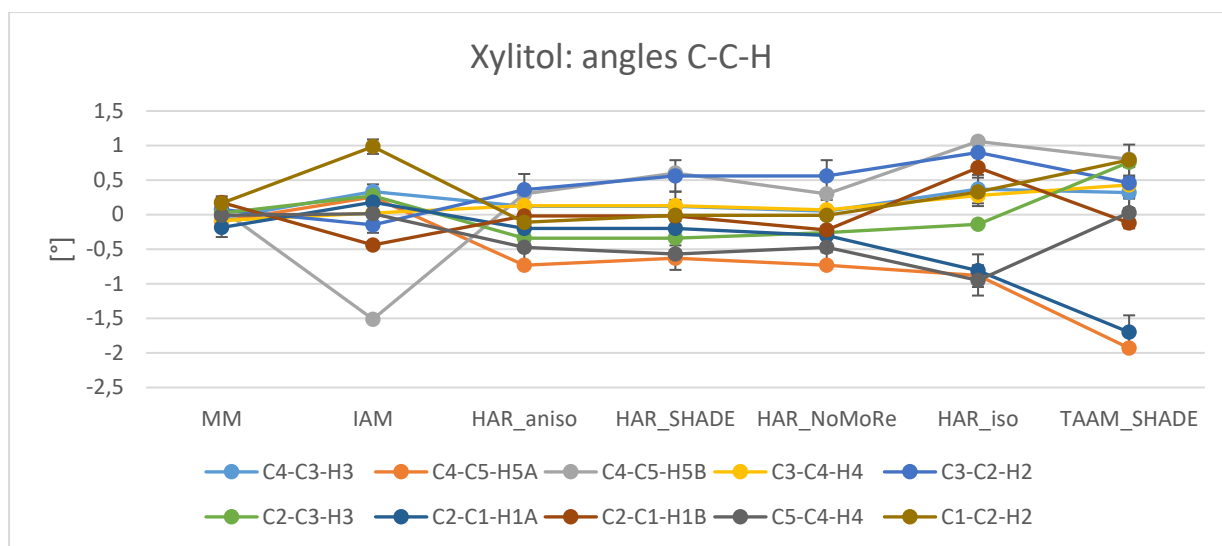


Figure S23 Comparison of C-C-H angles for MM, IAM, HAR and TAAM refinements of **1**, **2** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.

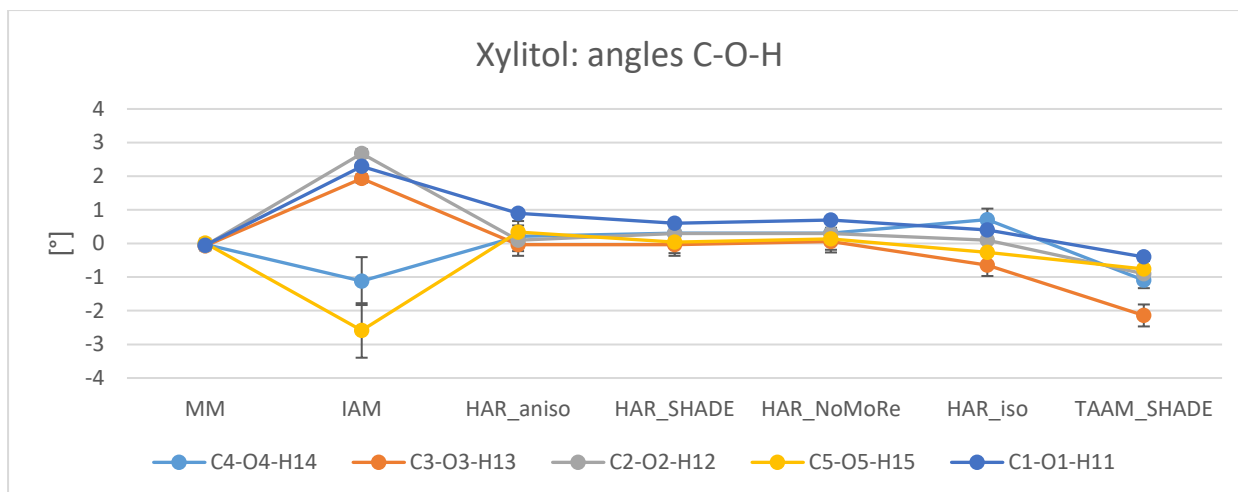


Figure S24 Comparison of C-O-H angles for MM, IAM, HAR and TAAM refinements of **2**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.

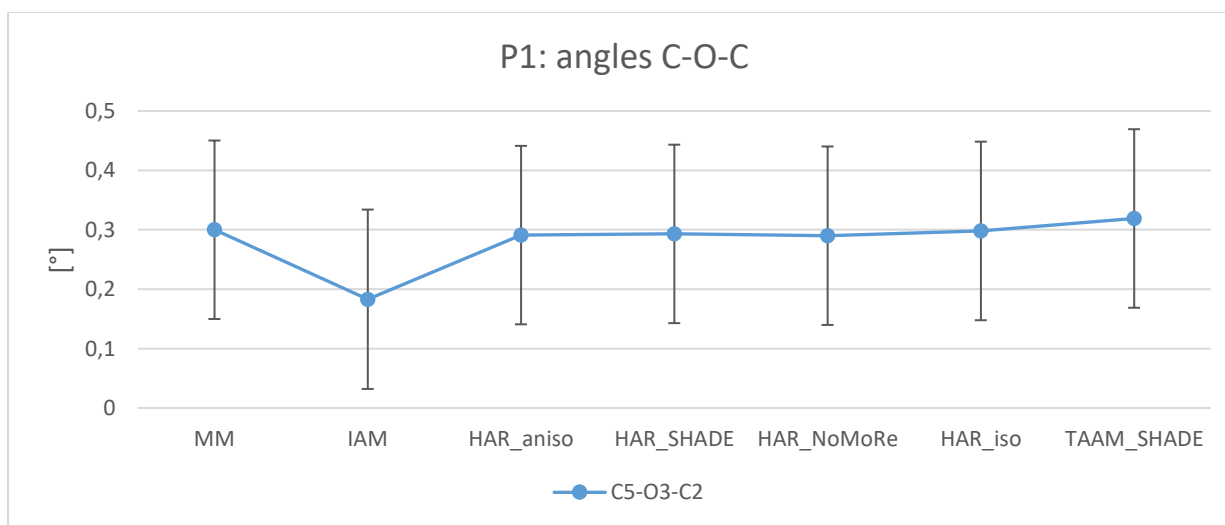


Figure S25 Comparison of C-O-C angles for MM, IAM, HAR and TAAM refinements of **1**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. Estimated standard deviations were added.

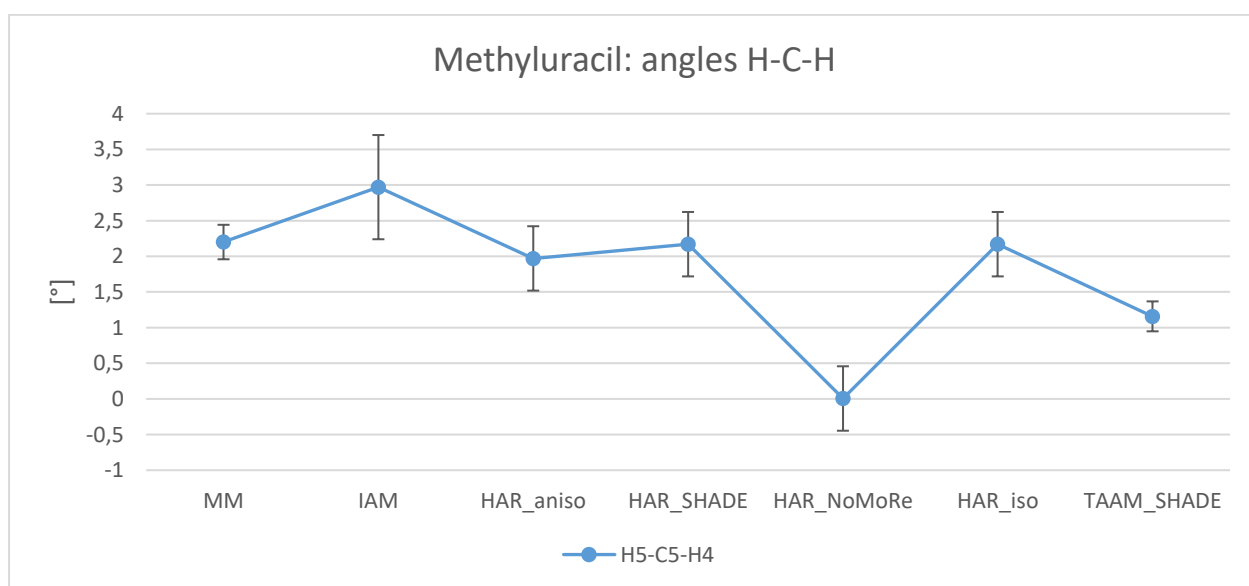
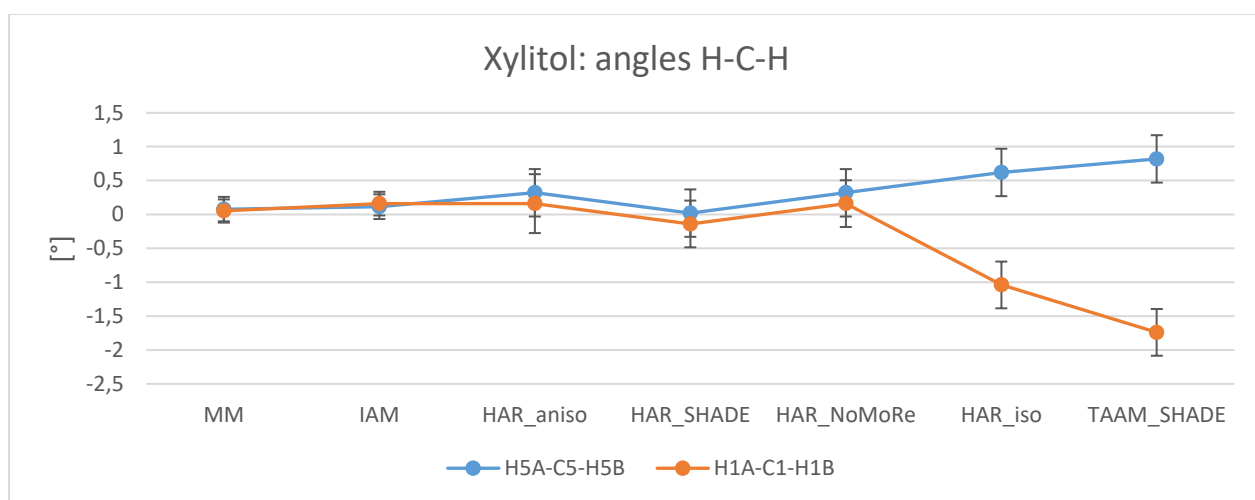
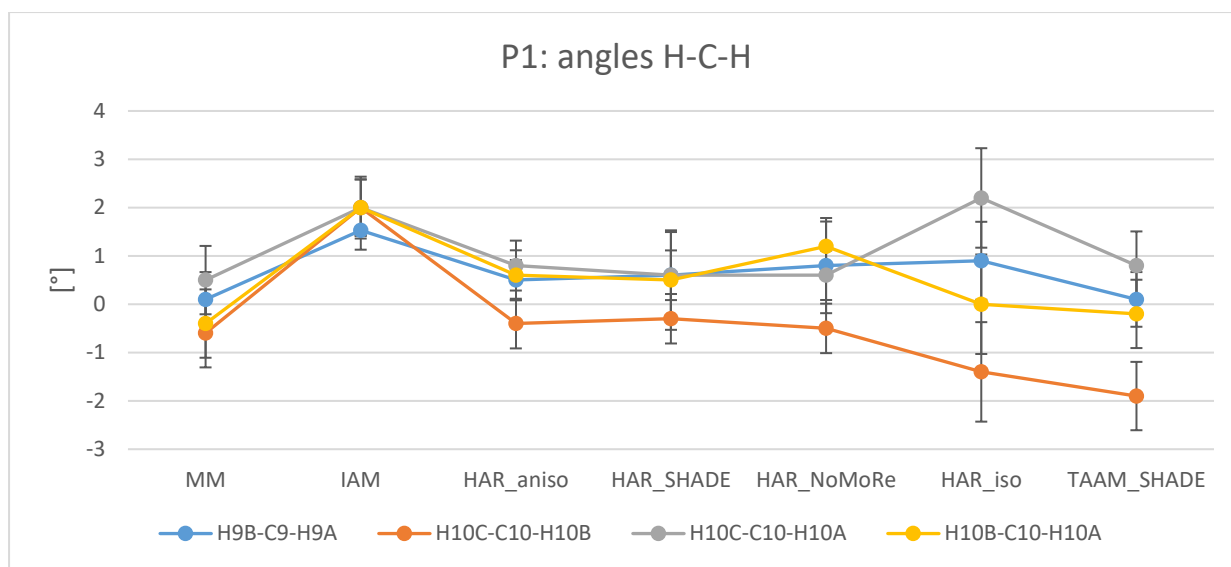
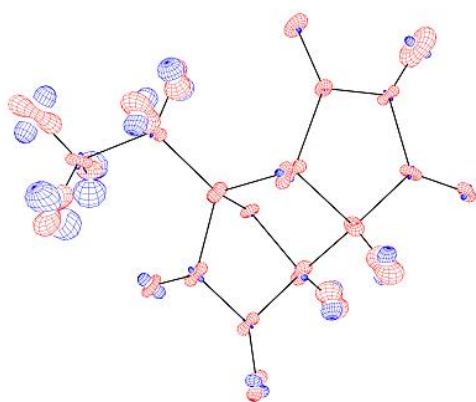
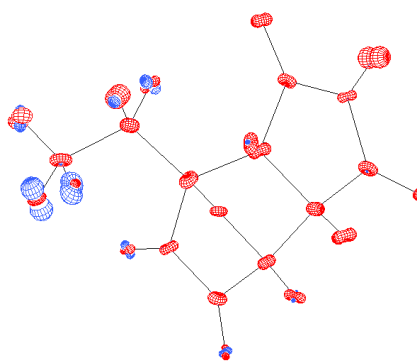


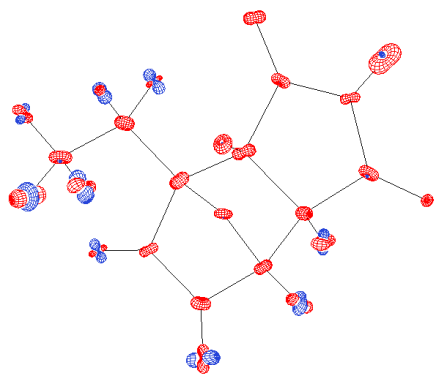
Figure S26 Comparison of H-C-H angles for MM, IAM, HAR and TAAM refinements of **1**, **2** and **3**. Values on plot represent difference between values obtained with analysed model and neutron data in degrees. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.



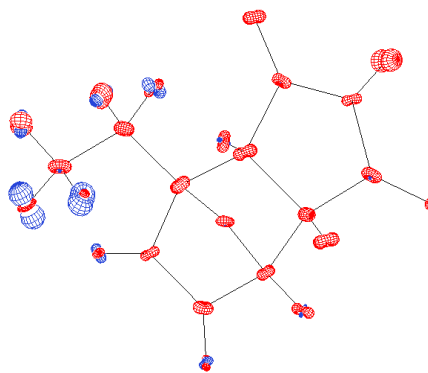
MM



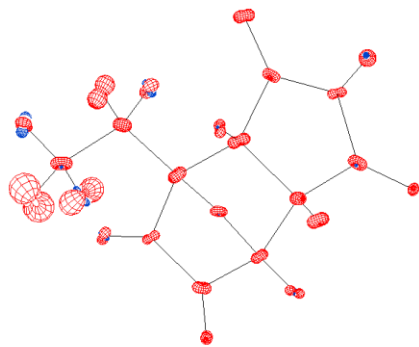
TAAM_Shade



HAR_aniso

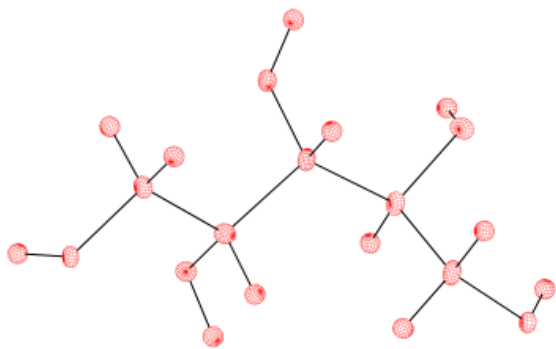


HAR_Shade

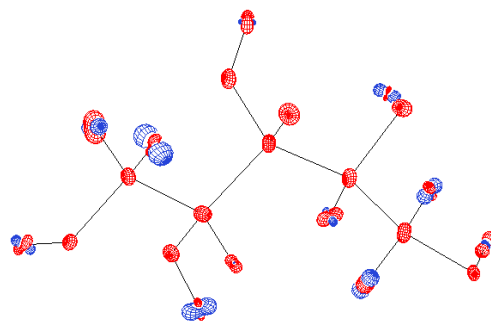


HAR_NoMoRe

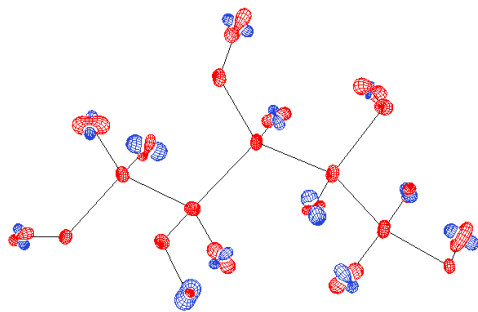
Figure S27 Difference between ADPs of neutron and analysed model for MM, HAR and TAAM refinements of **1**. Two-step overlay algorithm and 2.0 scale were applied using PEANUT software.



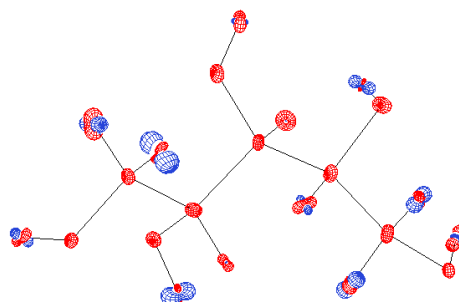
MM



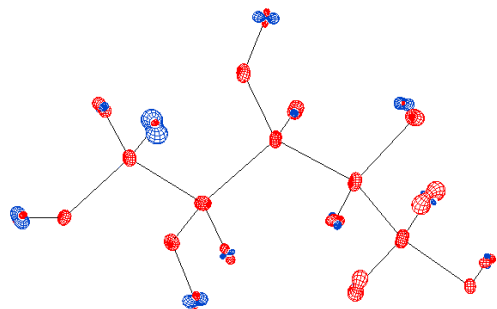
TAAM_Shade



HAR_aniso

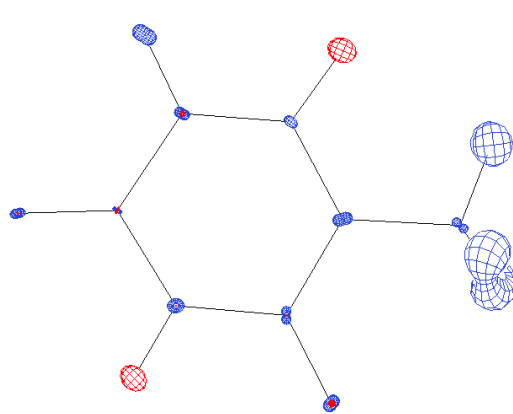


HAR_Shade

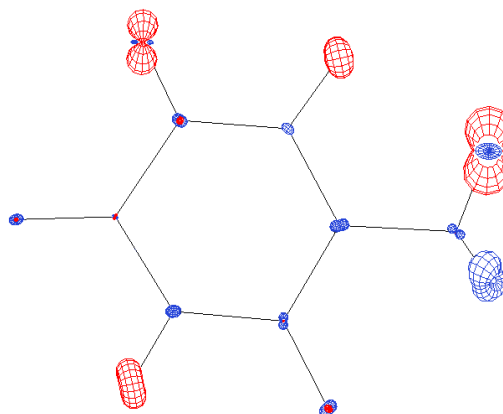


HAR_NoMoRe

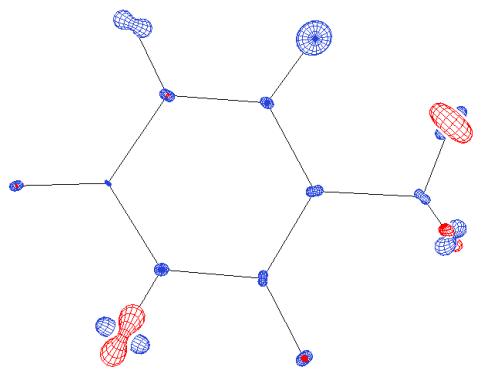
Figure S28 Difference between ADPs of neutron and analysed model for MM, HAR and TAAM refinements of **2**. Two-step overlay algorithm and 2.0 scale were applied using PEANUT software.



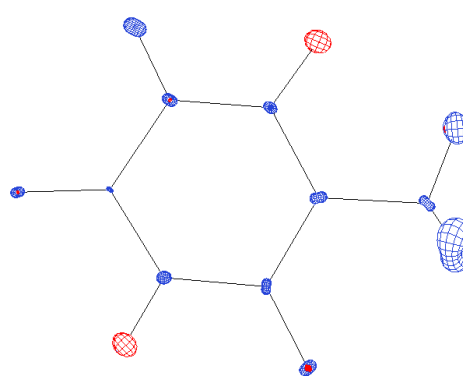
MM



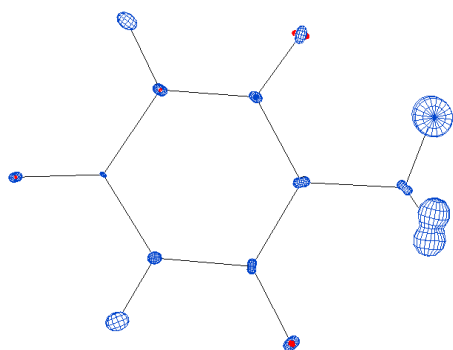
TAAM_Shade



HAR_aniso

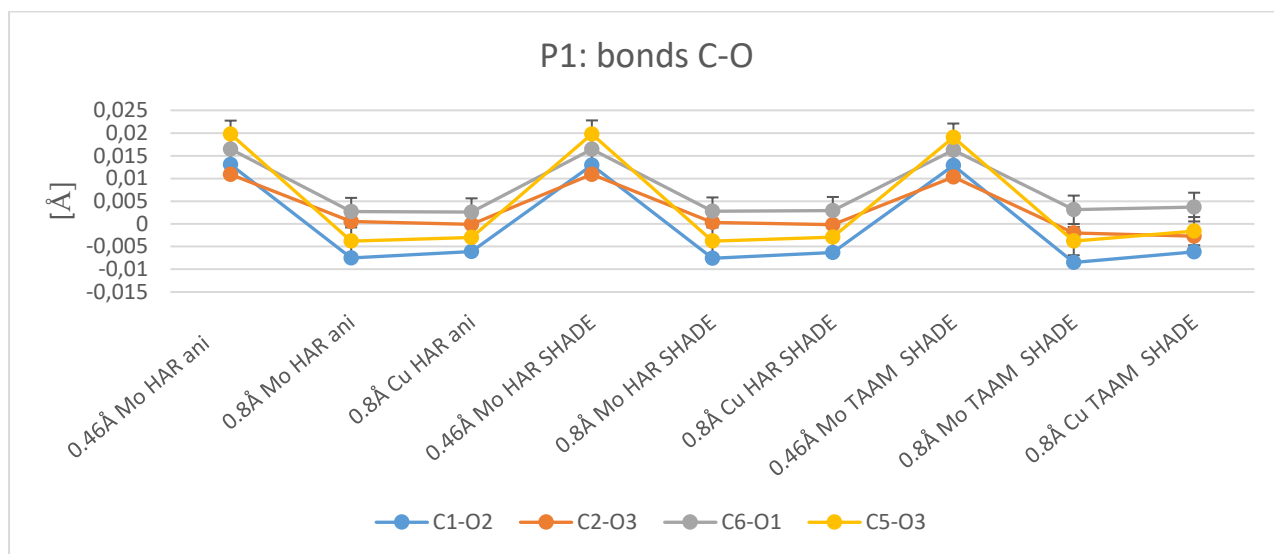


HAR_Shade



HAR_NoMoRe

Figure S29 Difference between ADPs of neutron and analysed model for MM, HAR and TAAM refinements of **3**. Two-step overlay algorithm and 2.0 scale were applied using PEANUT software.



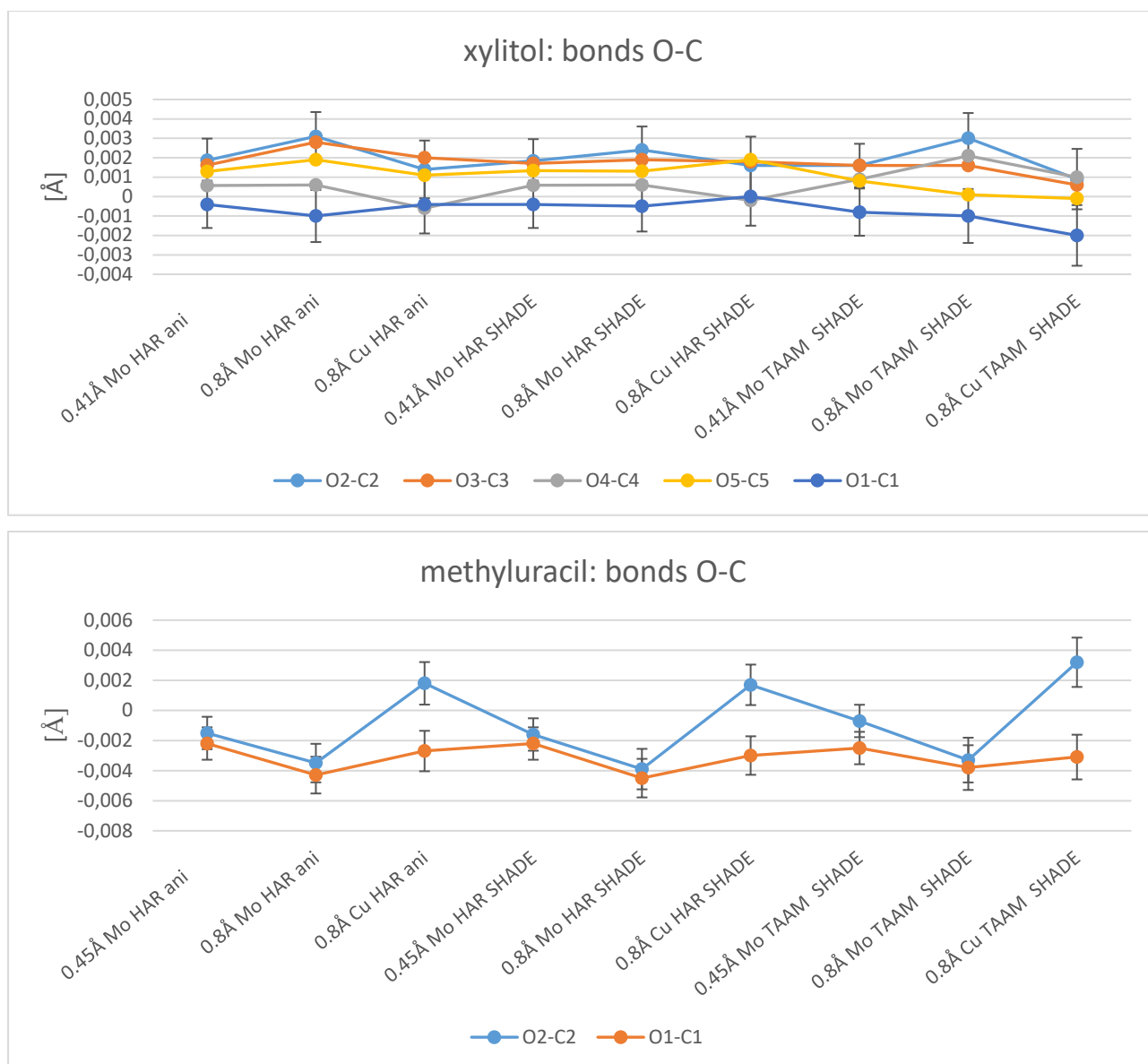


Figure S30 Comparison of O-C bonds for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuK α** , **2-CuK α** and **3CuK α** . Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For each plot estimated standard deviations were added.

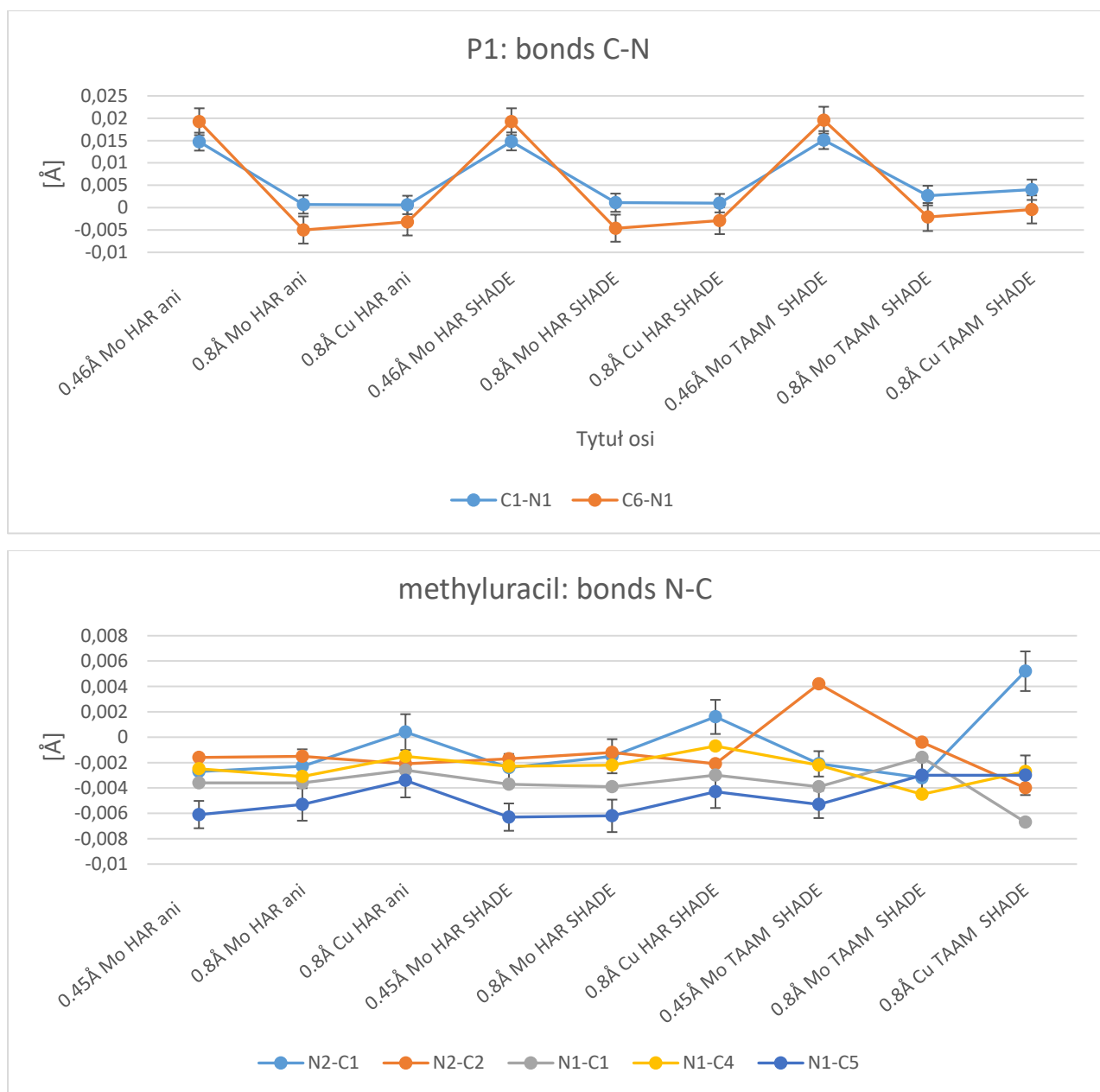
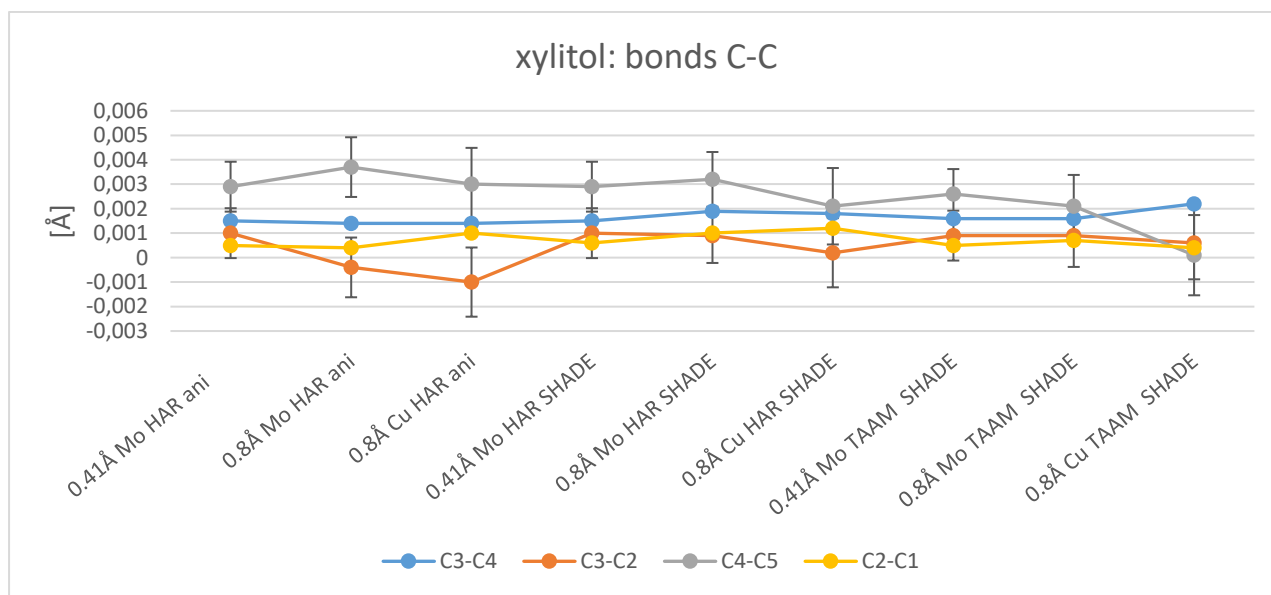
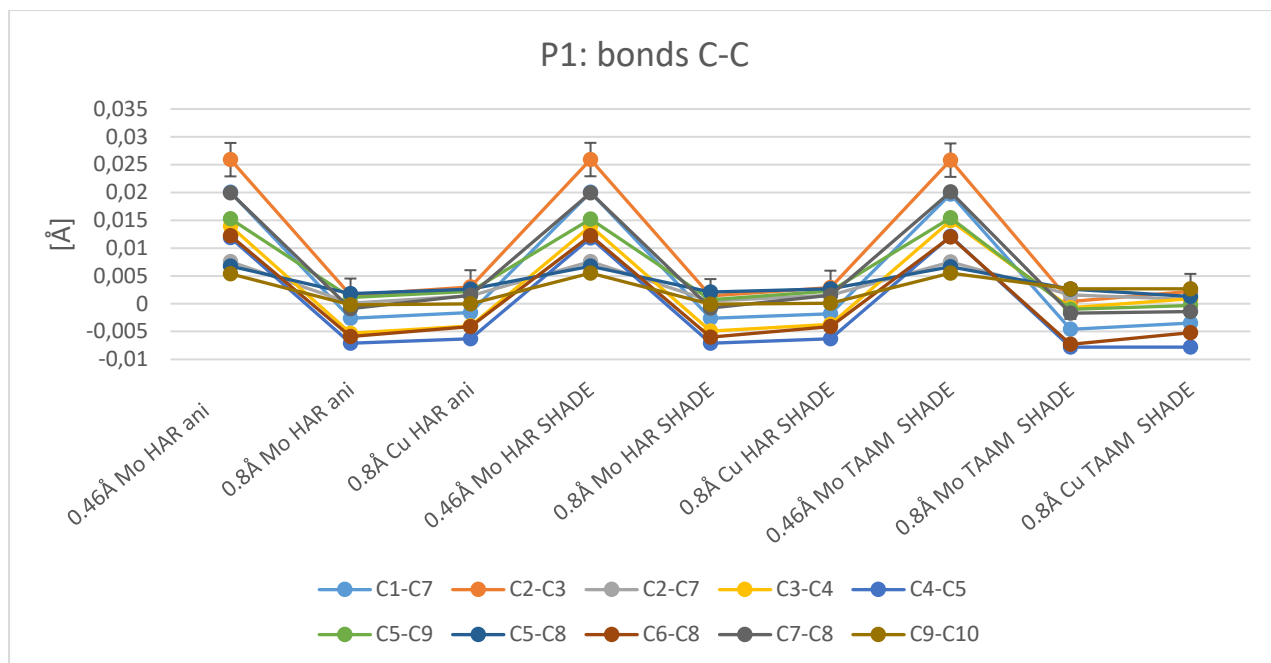


Figure S31 Comparison of N-C bonds for HAR and TAAM refinements of **1**, **3**, **1-cutoff**, **3-cutoff**, **1-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For each plot of **1**, **1-cutoff**, **1-CuKa** and selected plot of **3**, **3-cutoff**, **3-CuKa** (N2-C1, N1-C5, N1-C4) estimated standard deviations were added.



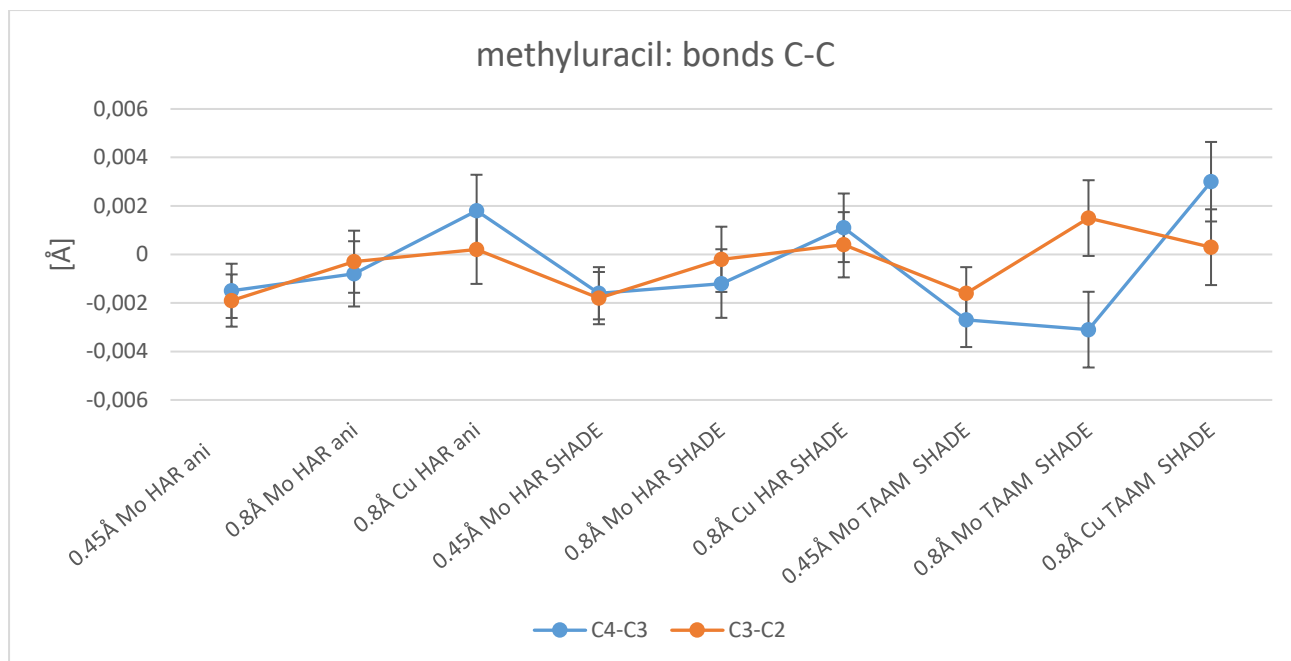
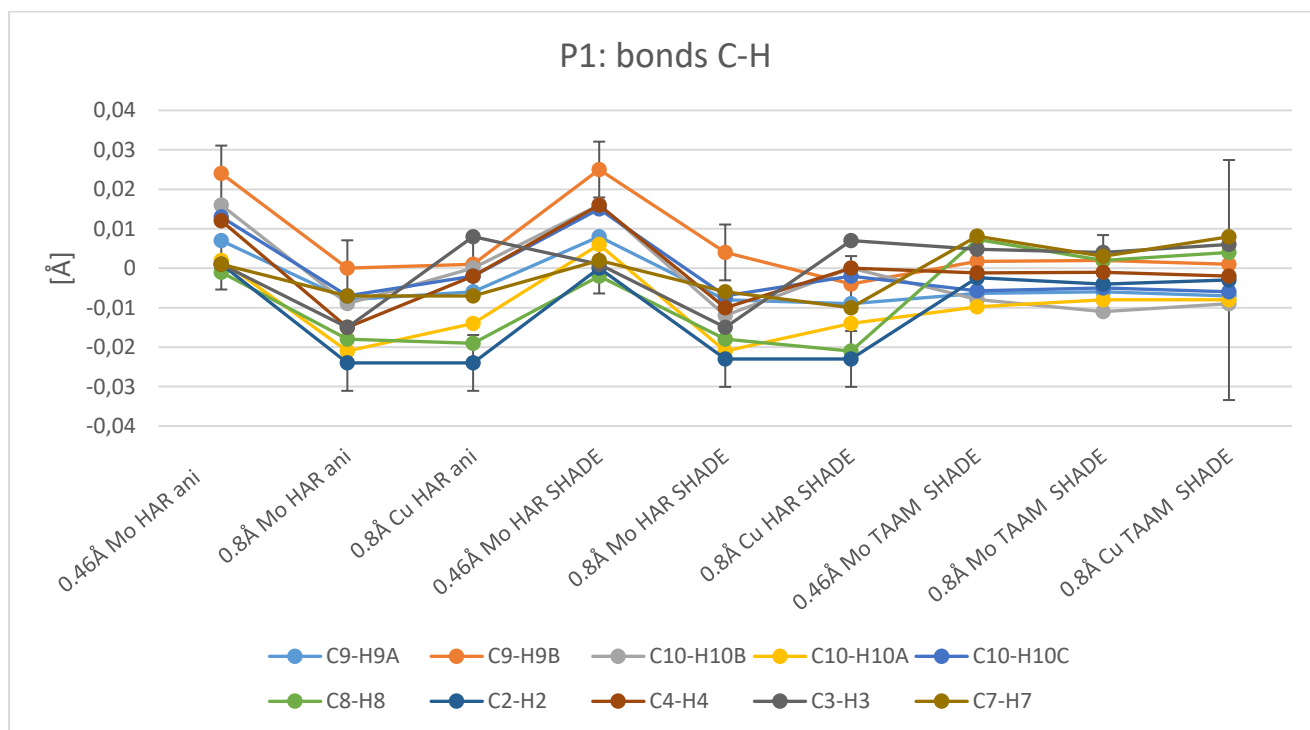


Figure S32 Comparison of C-C bonds for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuKa**, **2-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.



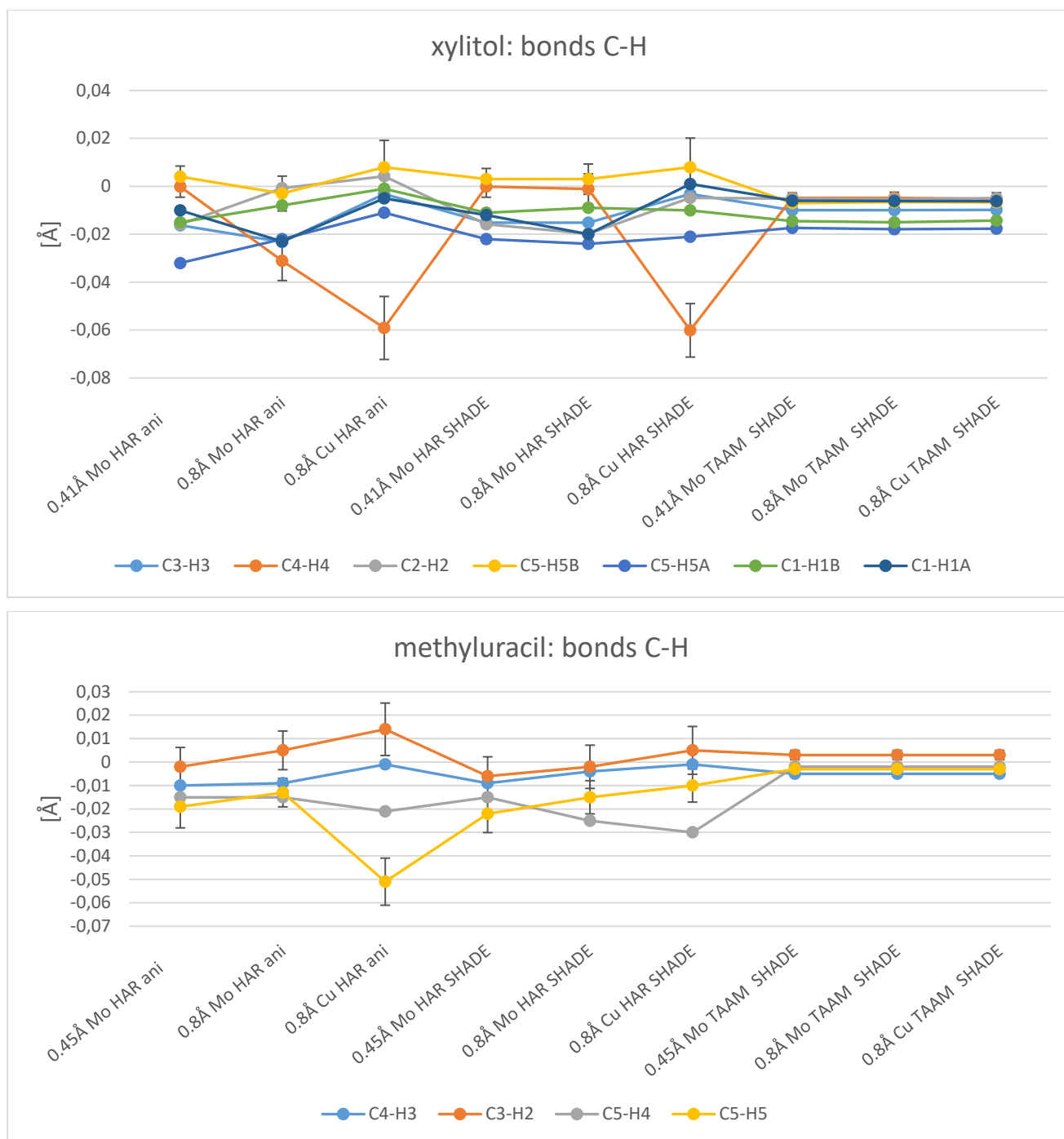


Figure S33 Comparison of C-H bonds for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuK α** , **2-CuK α** and **3CuK α** . Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

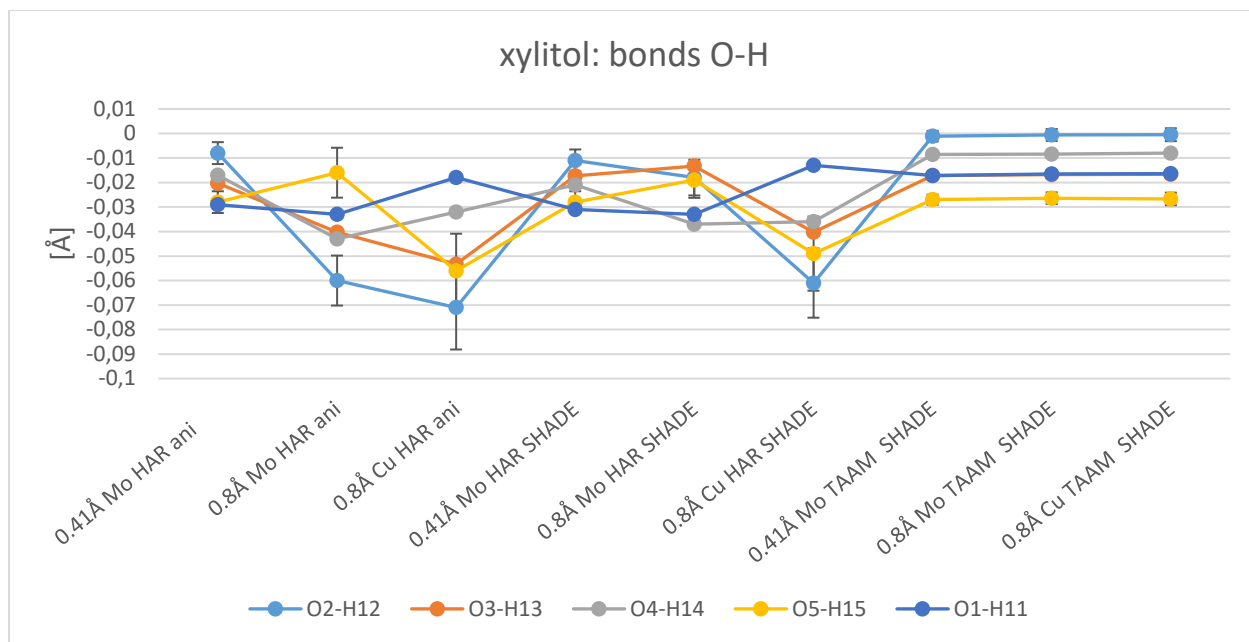
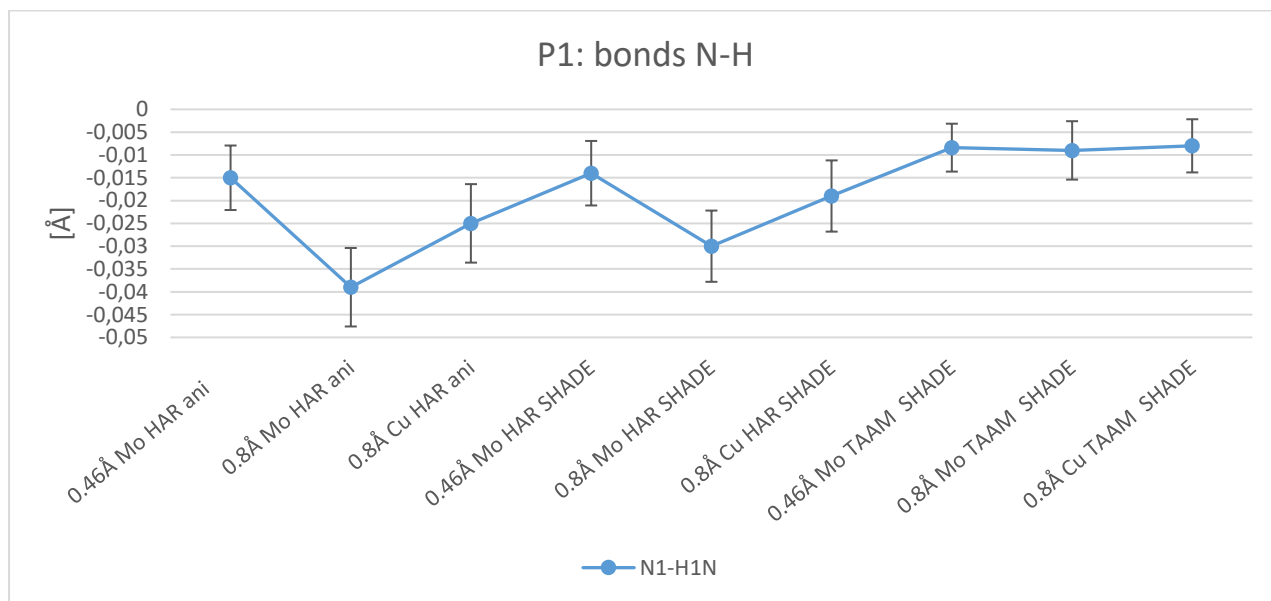


Figure S34 Comparison of O-H bonds for HAR and TAAM refinements of **2**, **2-cutoff** and **2-CuK α** . Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.



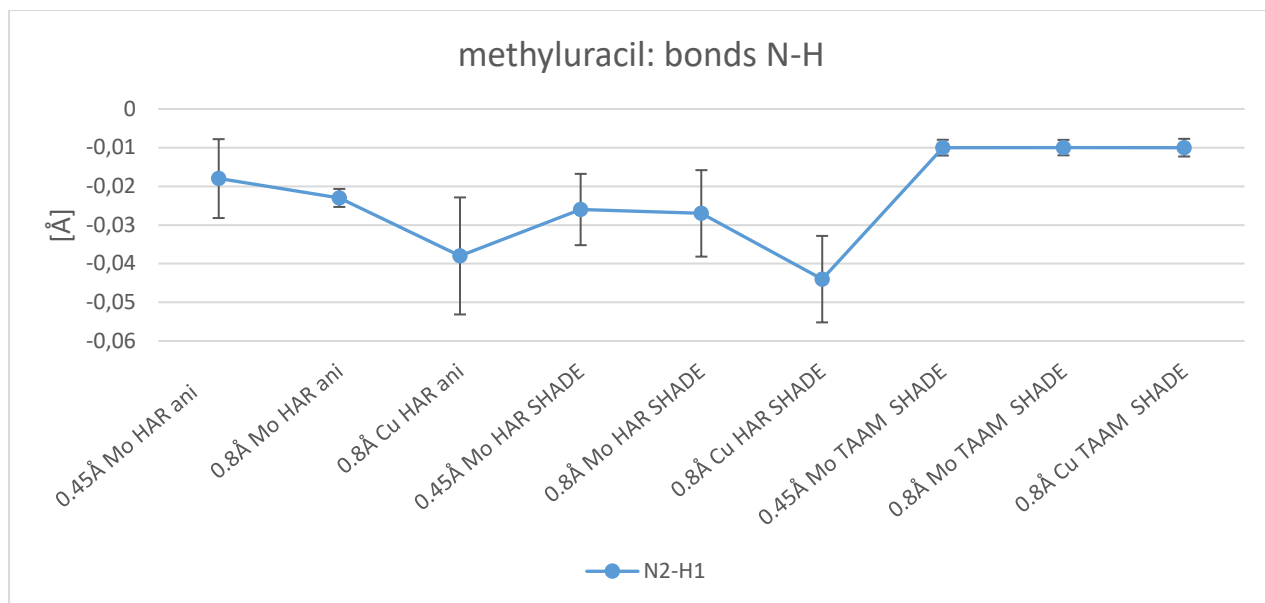
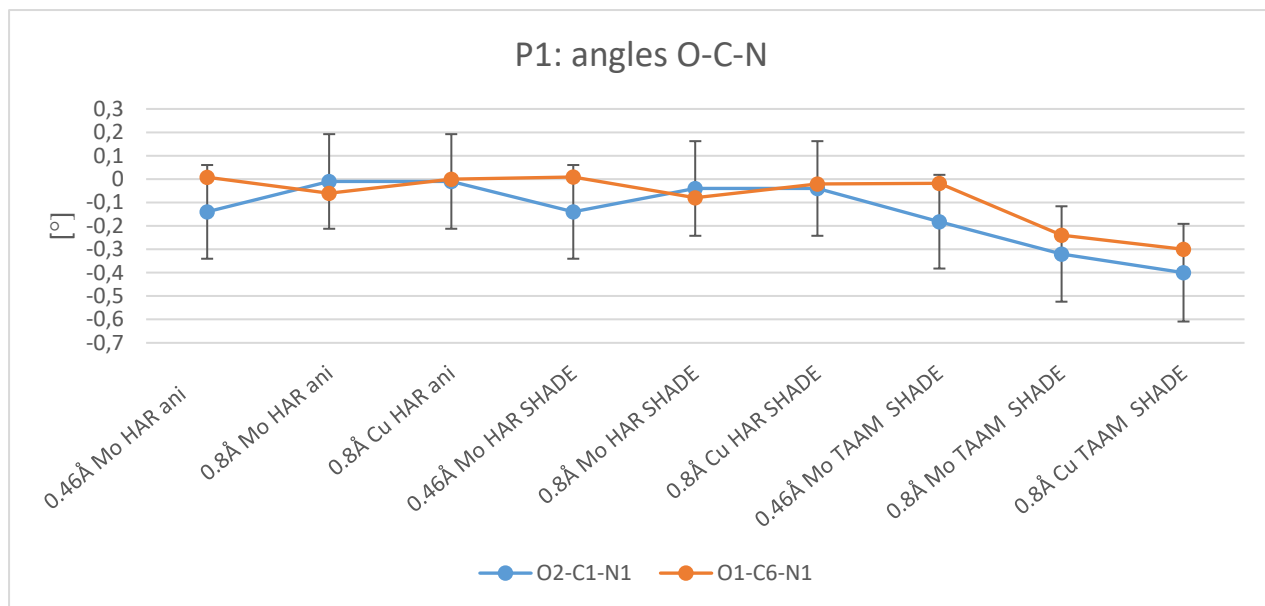


Figure S35 Comparison of N-H bonds for HAR and TAAM refinements of **3**, **3-cutoff** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. Estimated standard deviations were added to each plot.



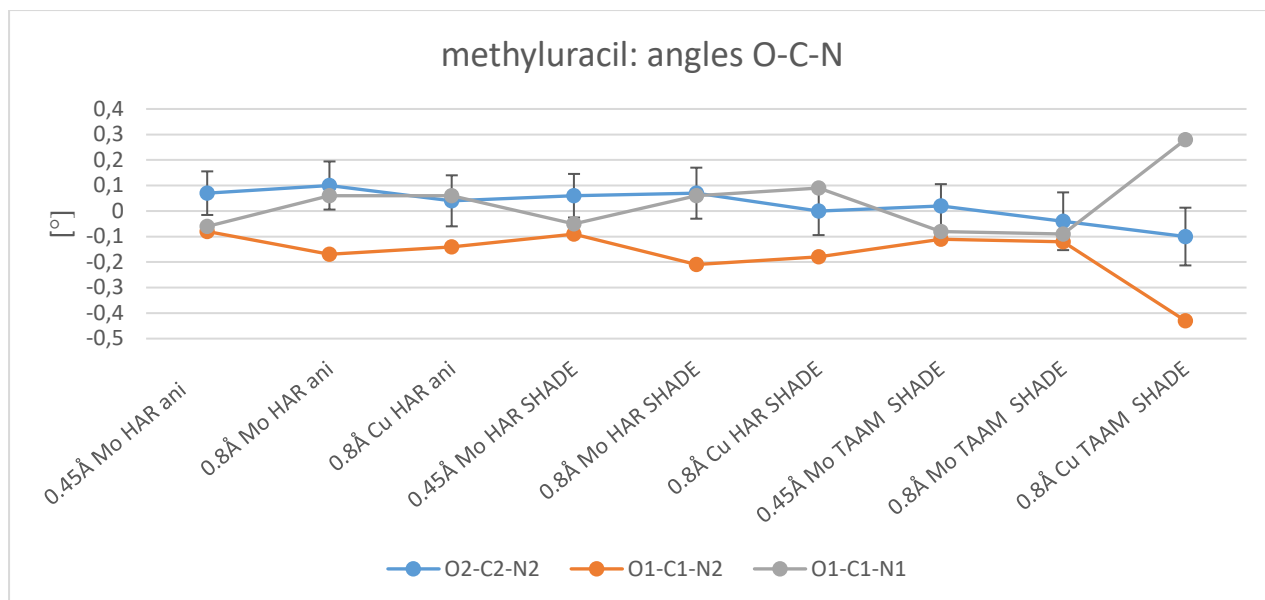
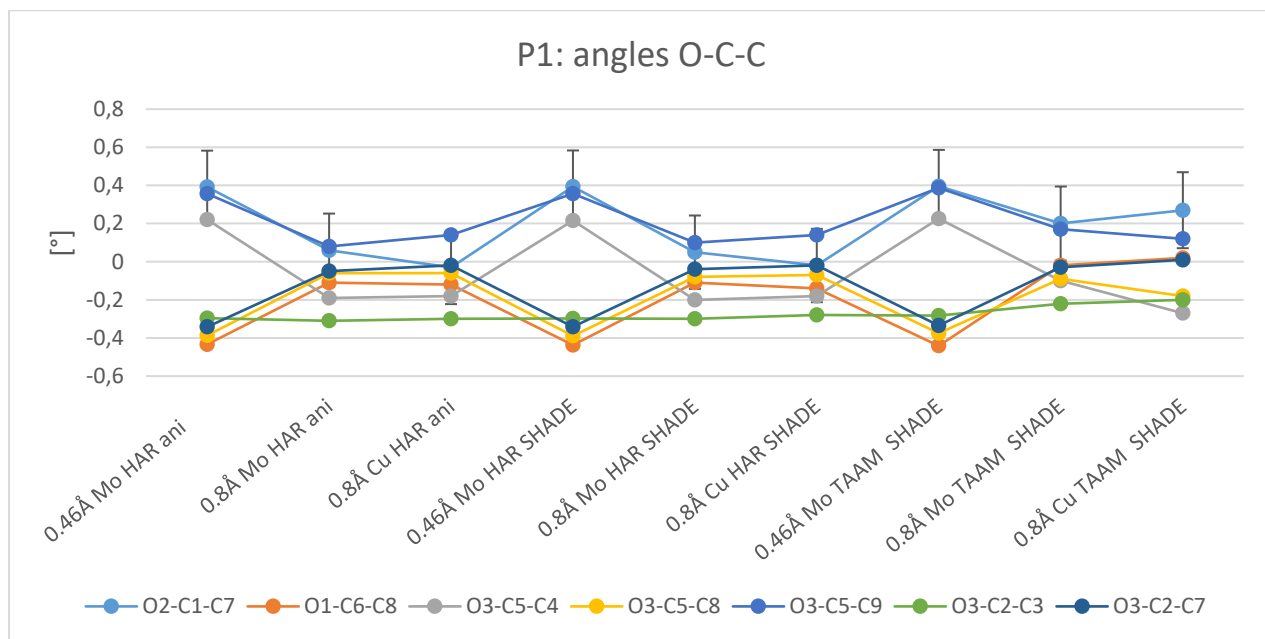


Figure S36 Comparison of O-C-N angles for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuKa**, **2-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.



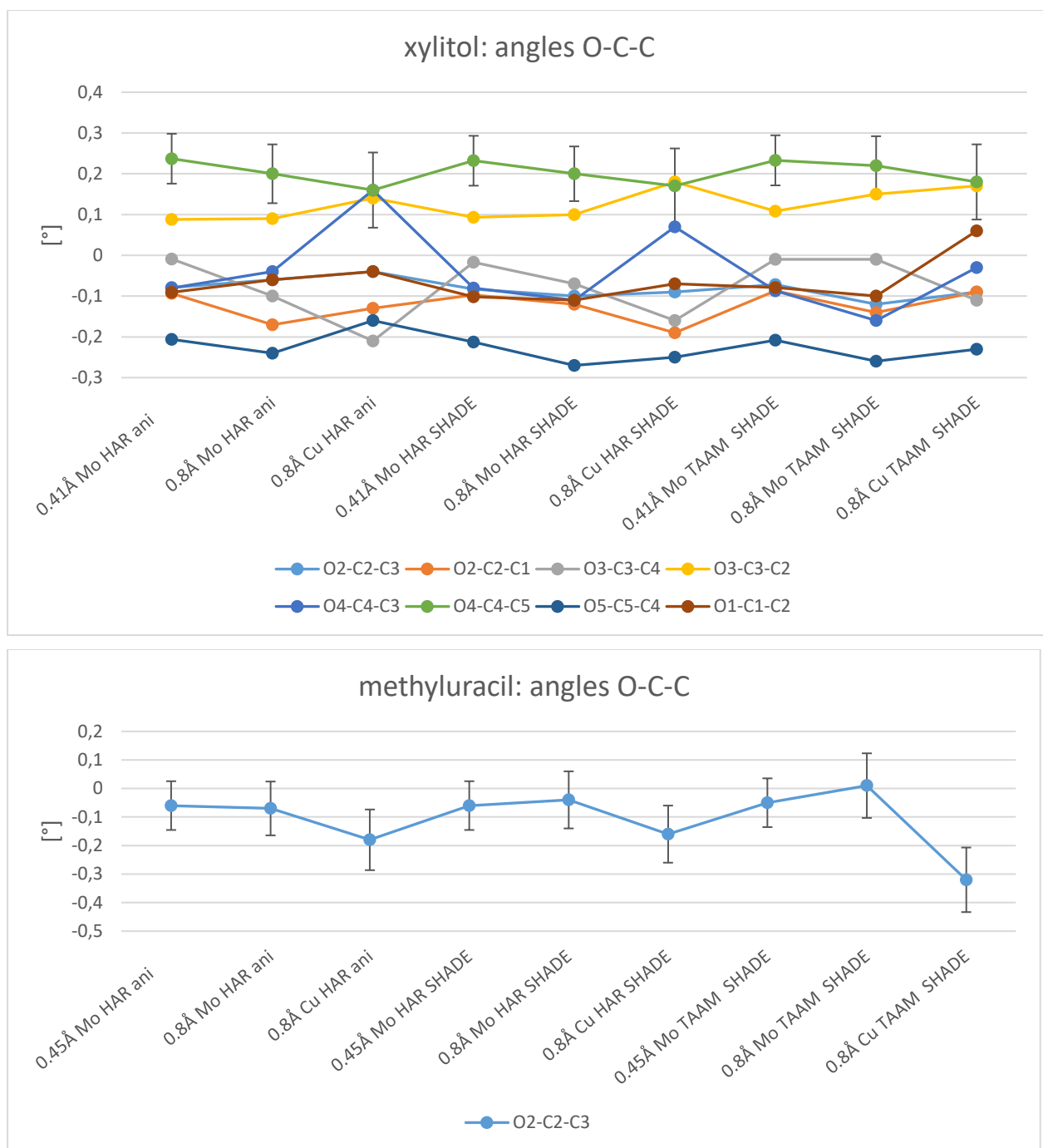


Figure S37 Comparison of O-C-C angles for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuKa**, **2-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

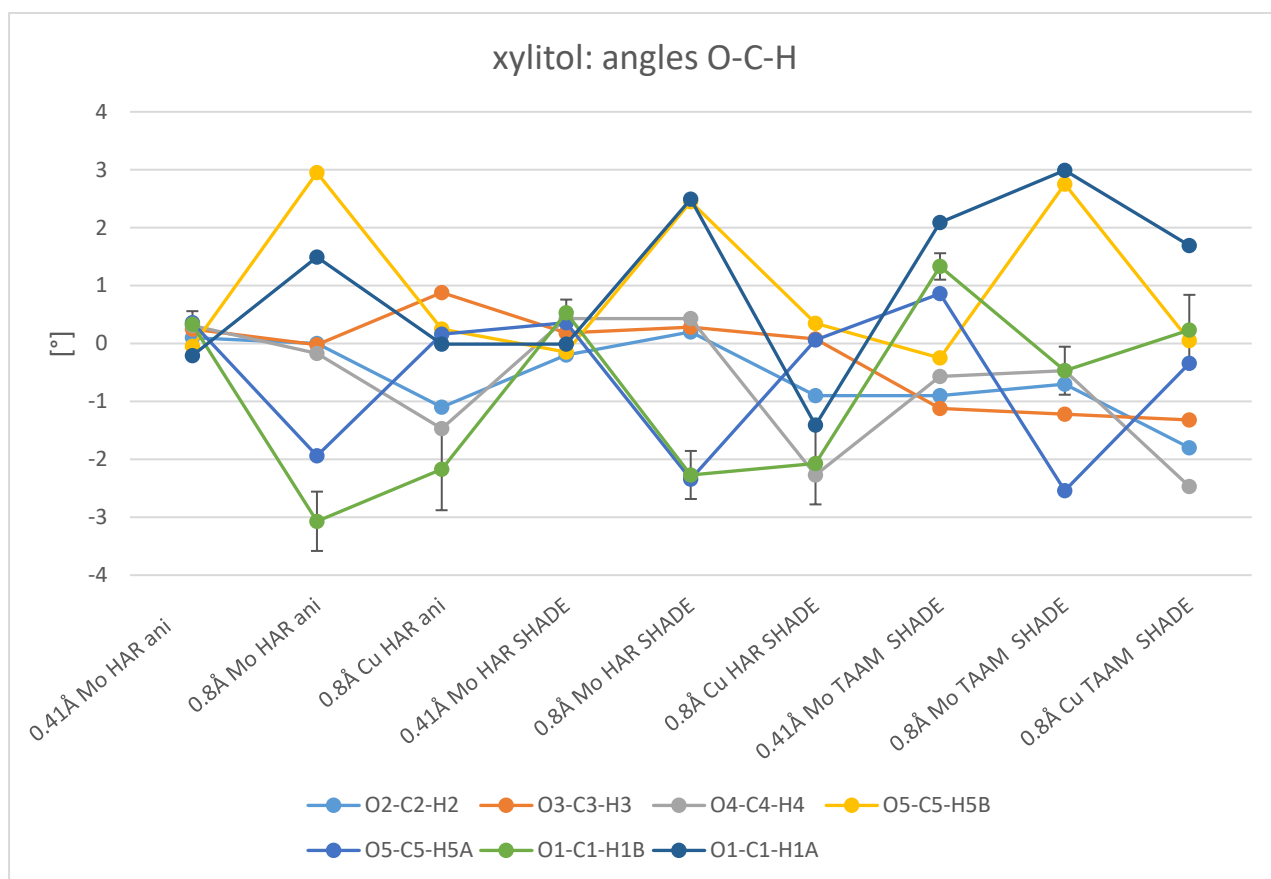
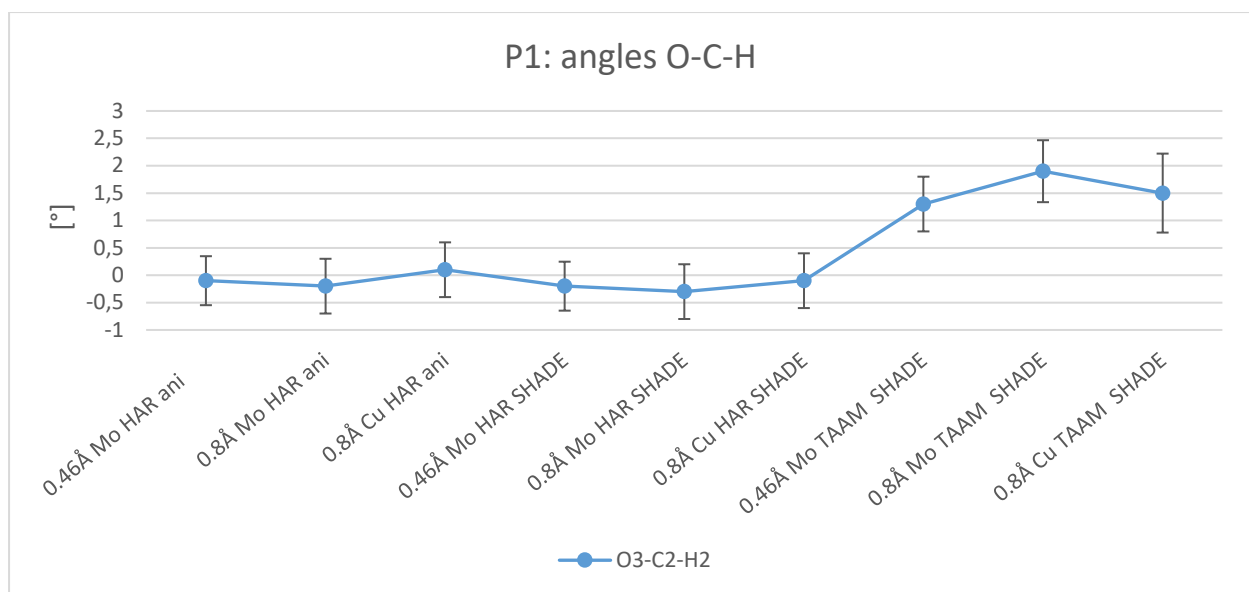


Figure S38 Comparison of O-C-H angles for HAR and TAAM refinements of **1**, **2**, **1-cutoff**, **2-cutoff**, **1-CuKa** and **2-CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

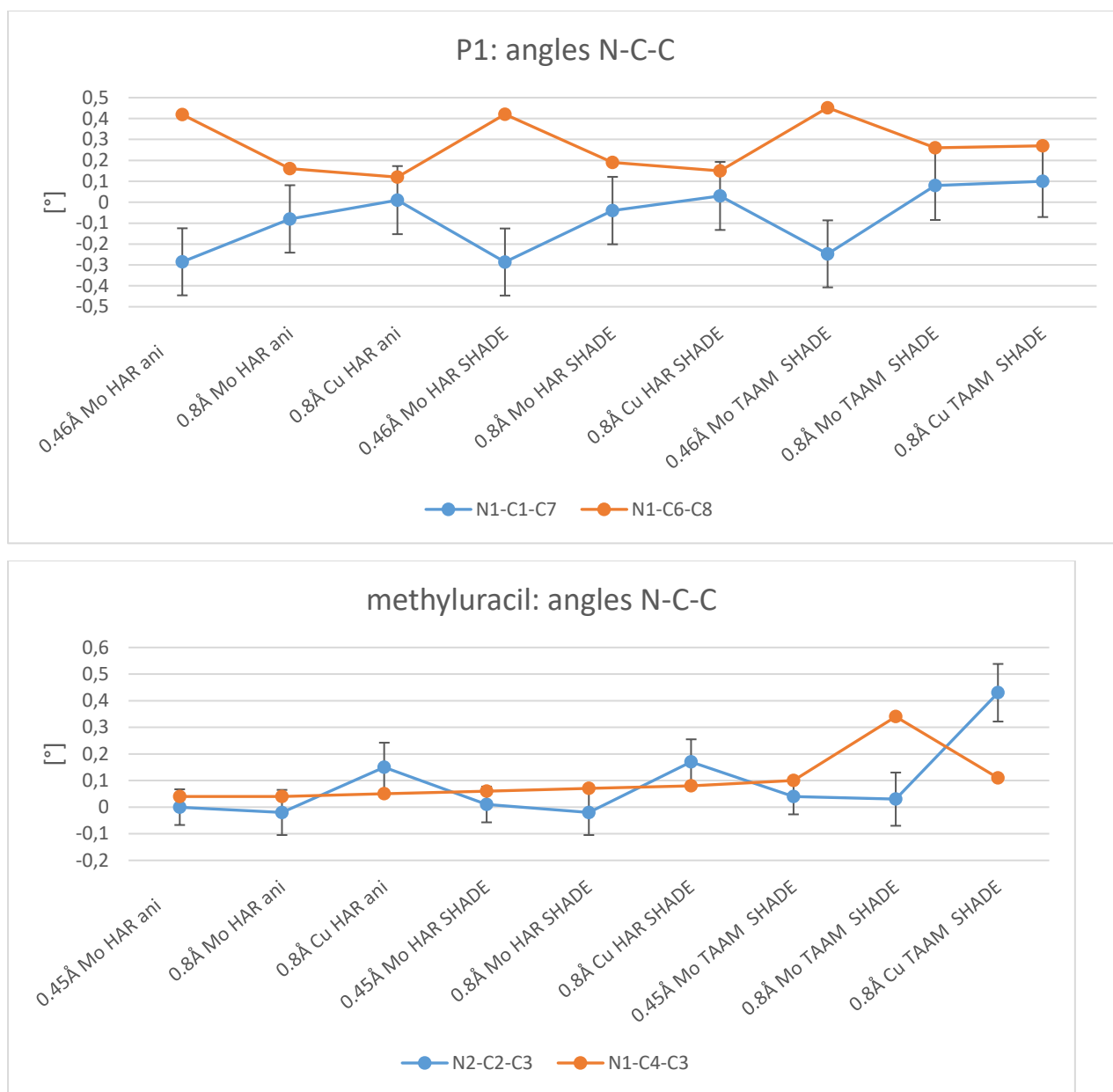


Figure S39 Comparison of N-C-C angles for HAR and TAAM refinements of **1**, **3**, **1-cutoff**, **3-cutoff**, **1-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

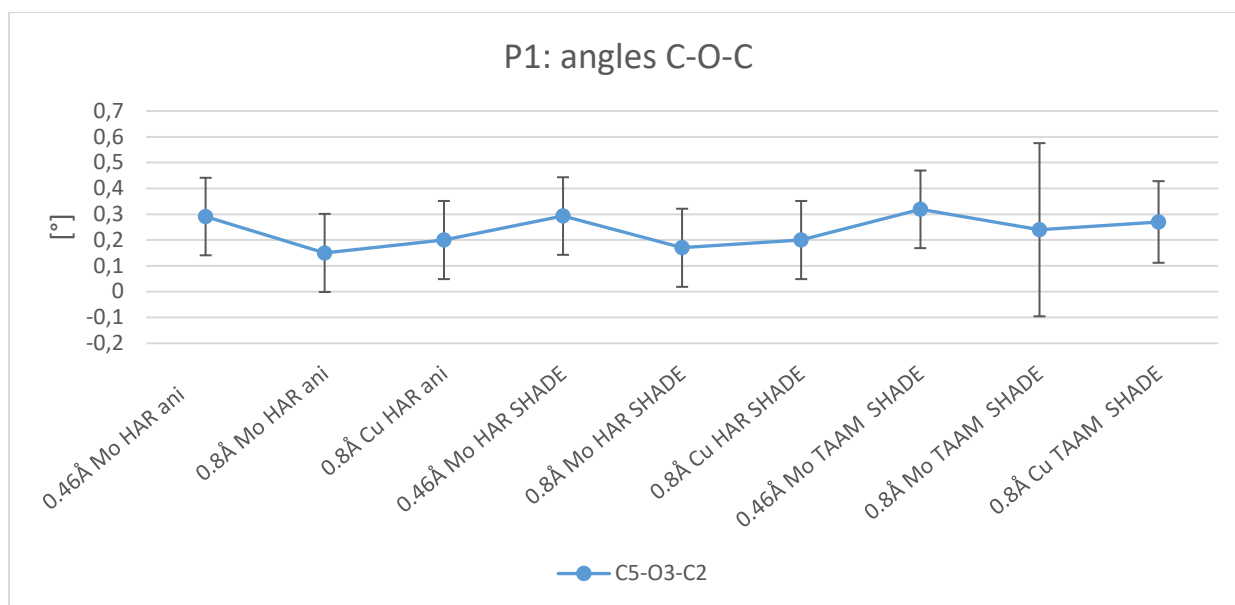


Figure S40 Comparison of C-O-C angles for HAR and TAAM refinements of **1**, **1-cutoff** and **1-CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. Estimated standard deviations were added to the plot.

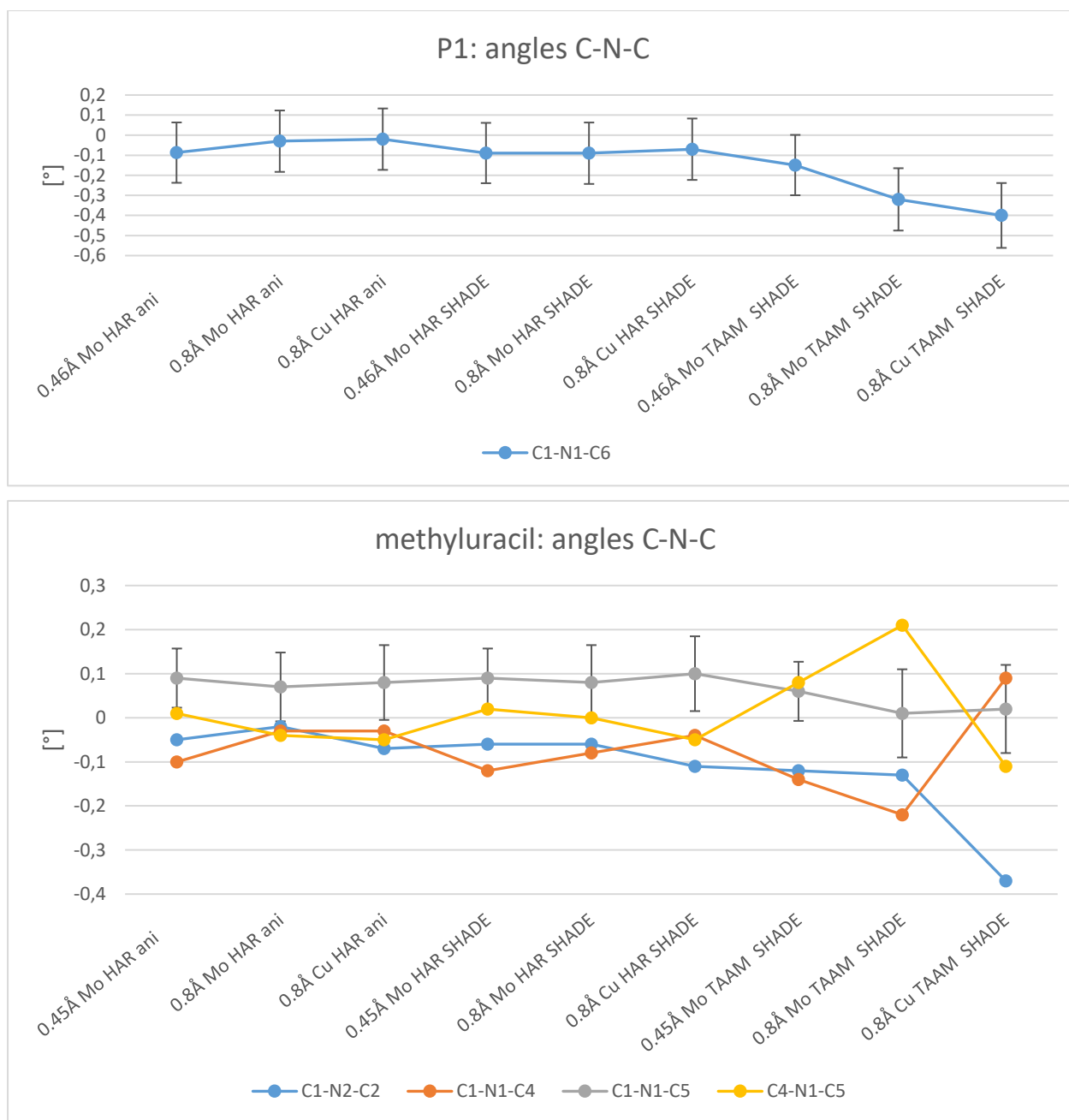


Figure S41 Comparison of C-N-C angles for HAR and TAAM refinements of **1**, **3**, **1-cutoff**, **3-cutoff**, **1-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

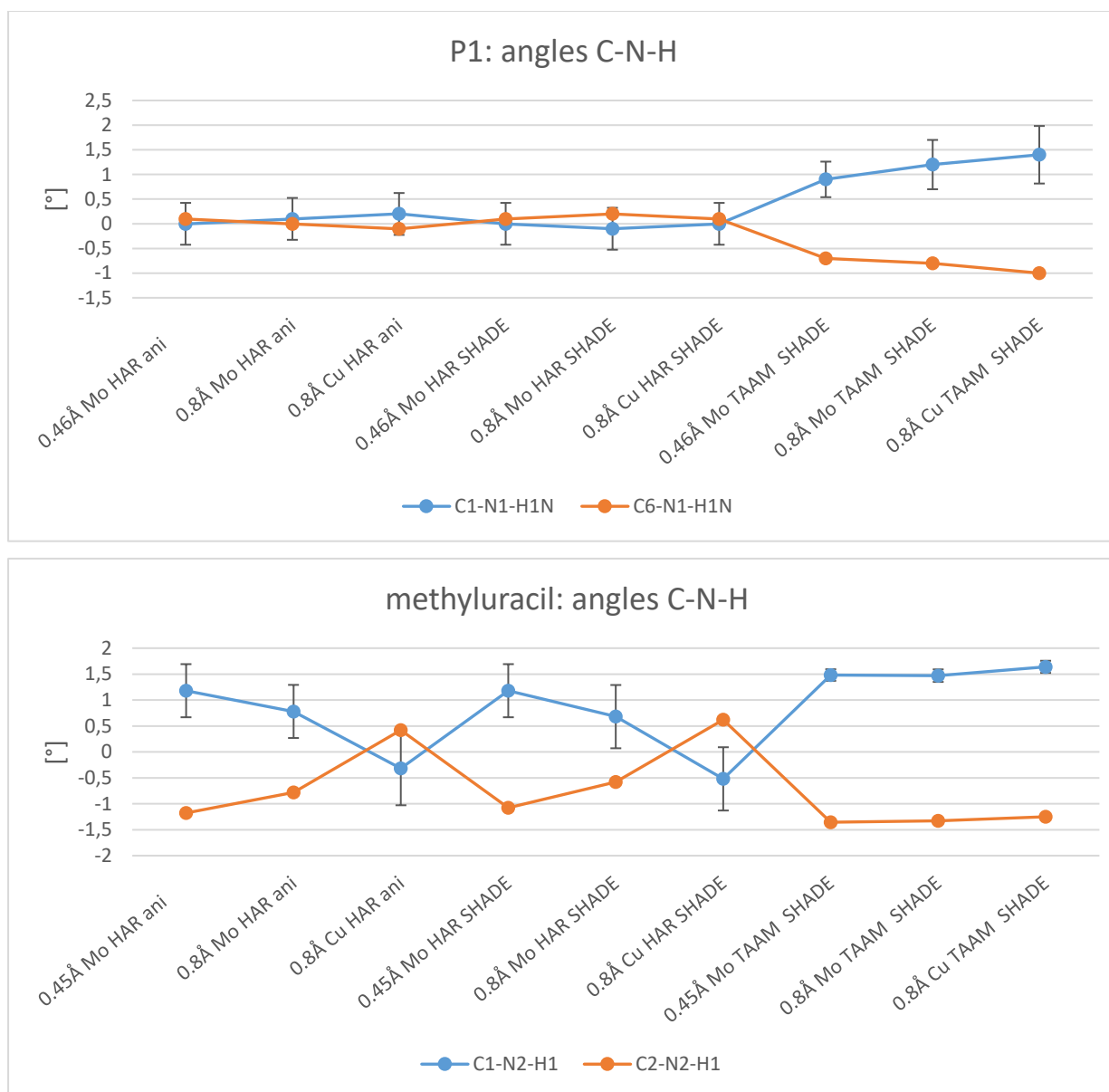


Figure S42 Comparison of C-N-H angles for HAR and TAAM refinements of **1**, **3**, **1-cutoff**, **3-cutoff**, **1-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

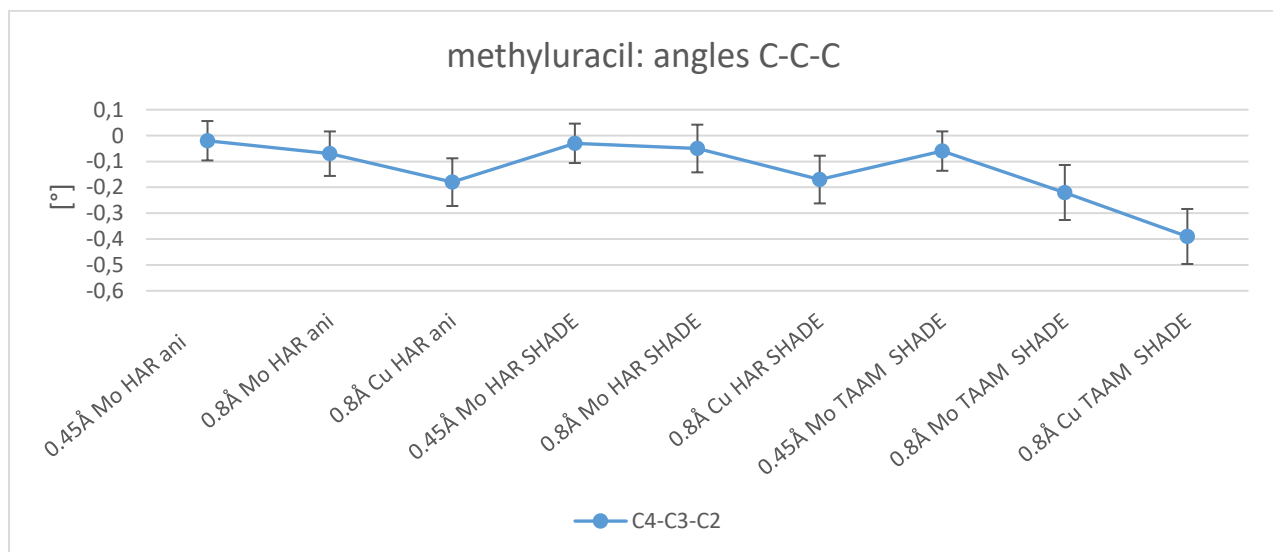
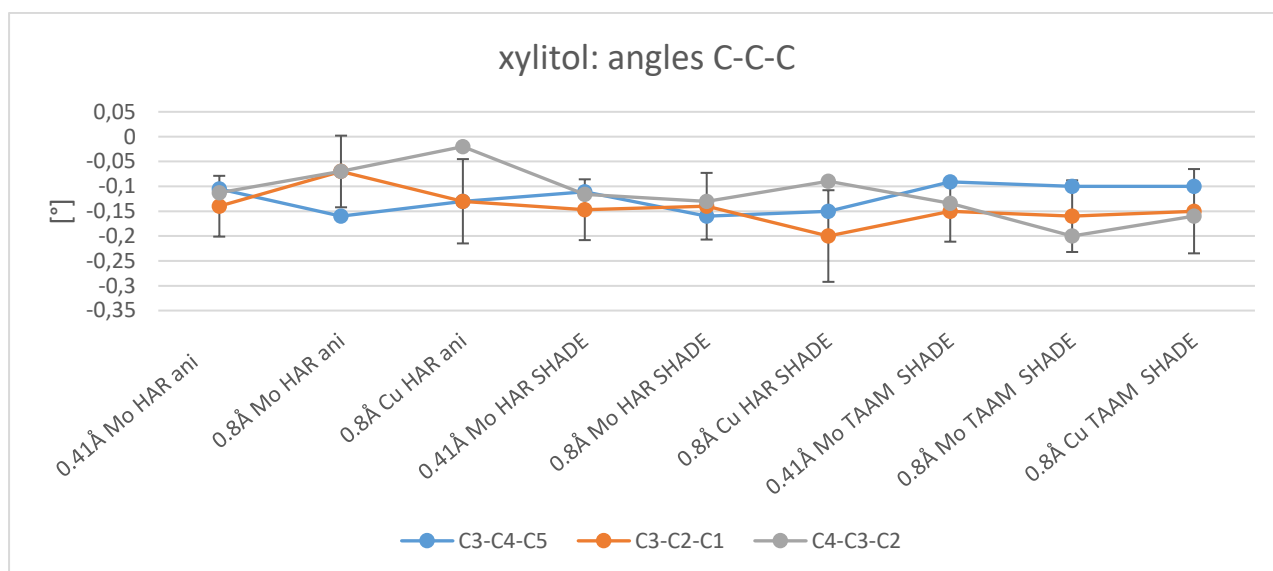
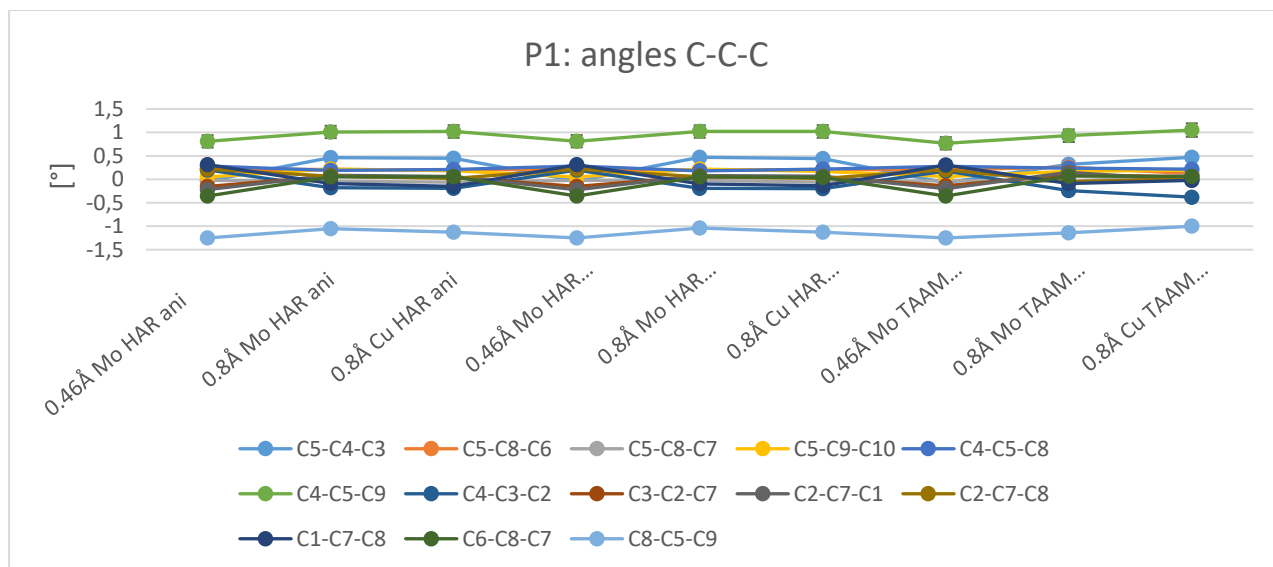
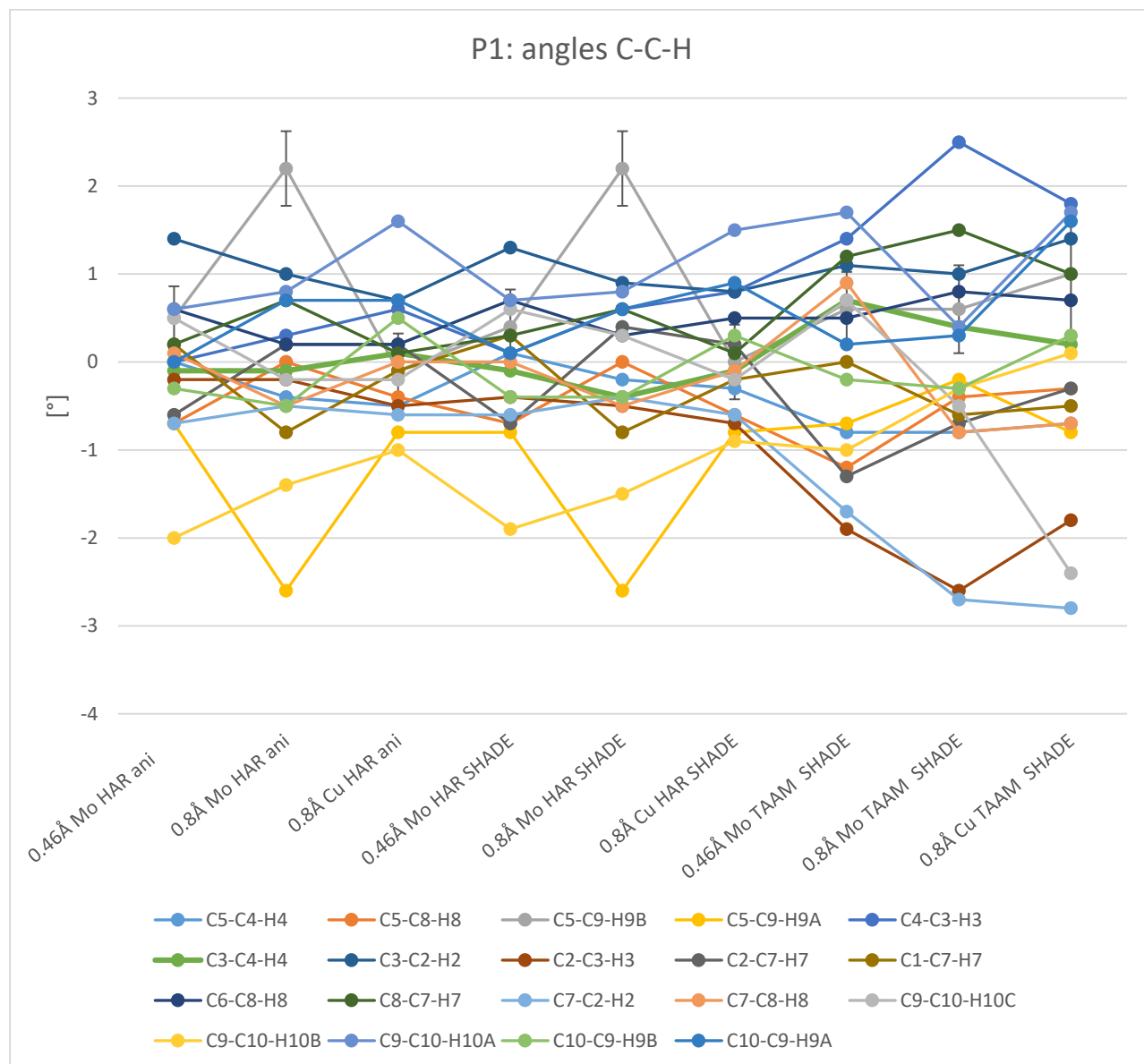


Figure S43 Comparison of C-C-C angles for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuKa**, **2-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.



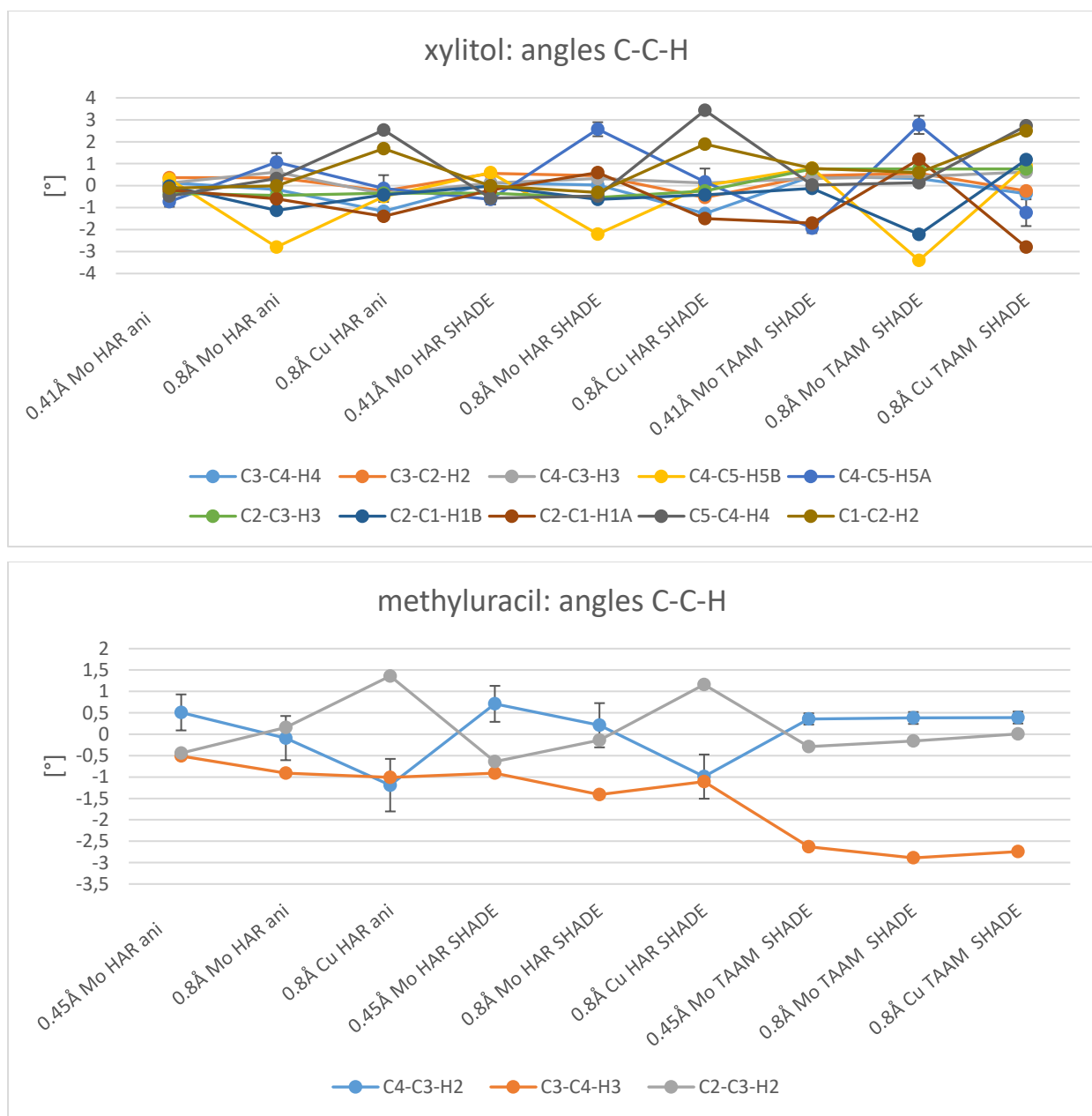


Figure S44 Comparison of C-C-H angles for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuKa**, **2-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

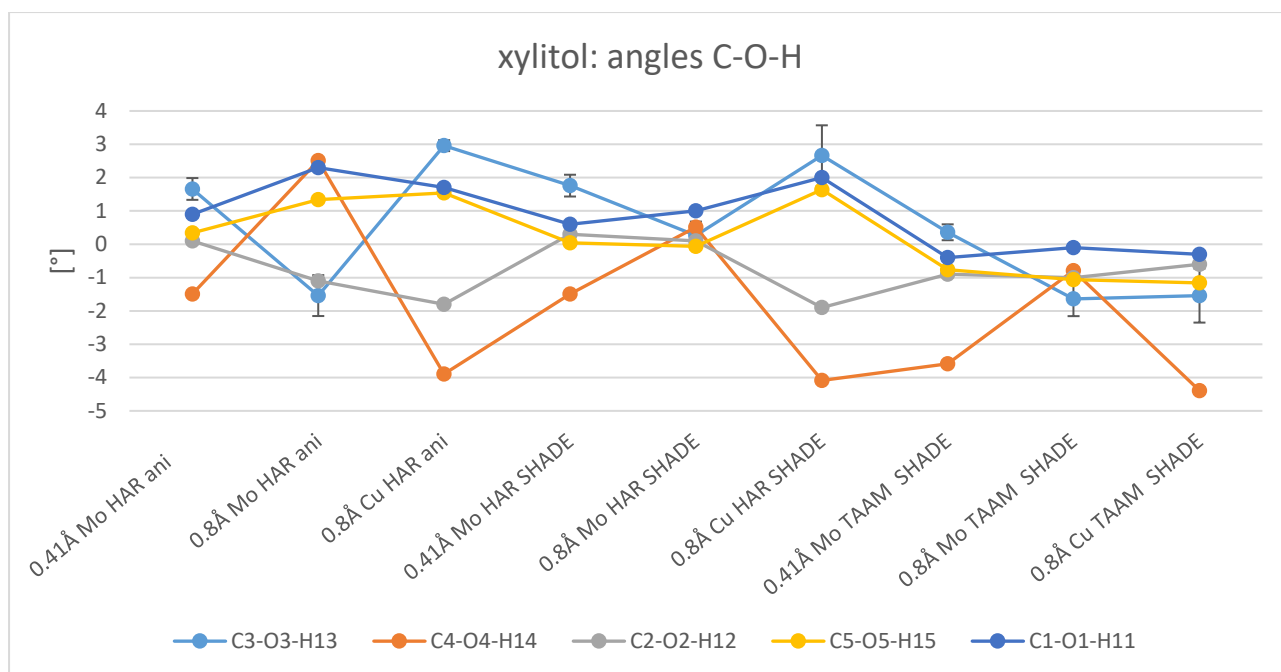
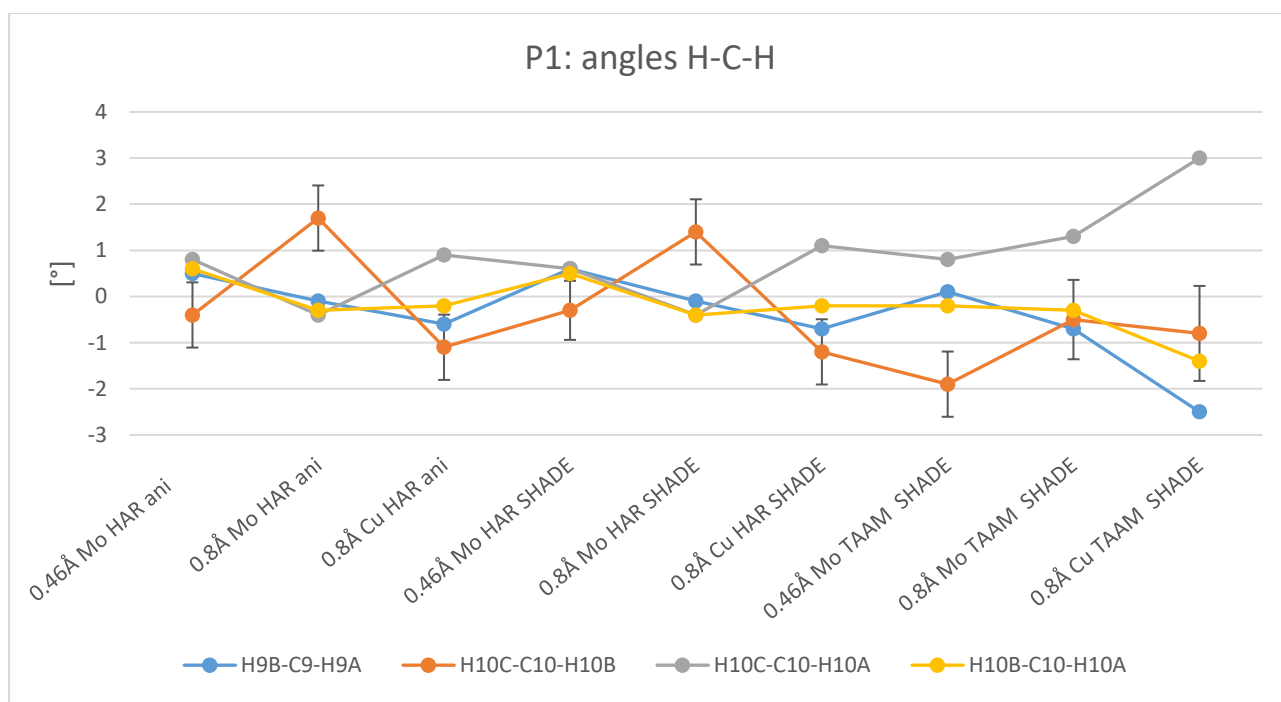


Figure S45 Comparison of C-O-H angles for HAR and TAAM refinements of **2**, **2-cutoff** and **2-CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.



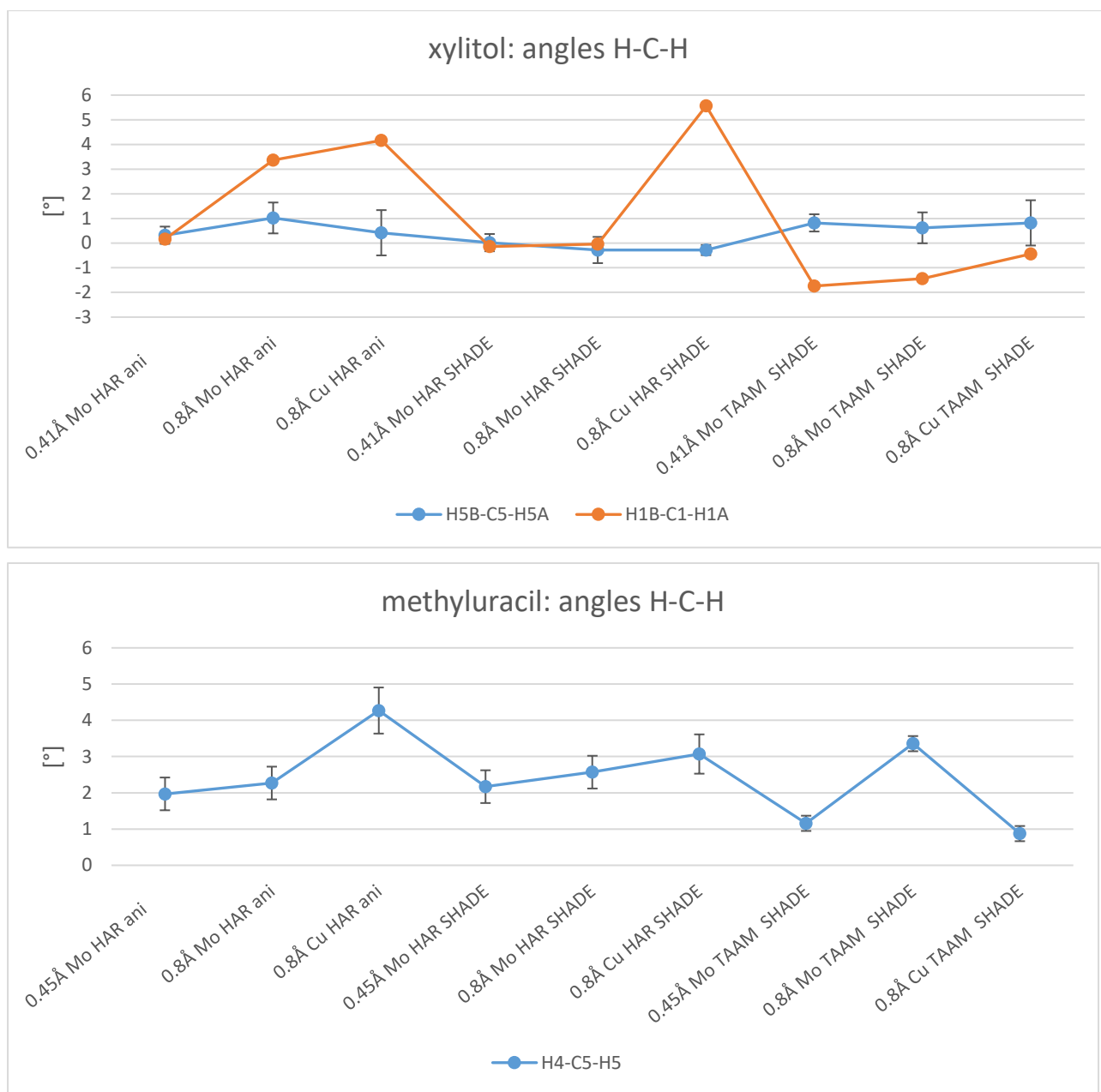


Figure S46 Comparison of H-C-H angles for HAR and TAAM refinements of **1**, **2**, **3**, **1-cutoff**, **2-cutoff** and **3-cutoff**, **1-CuKa**, **2-CuKa** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

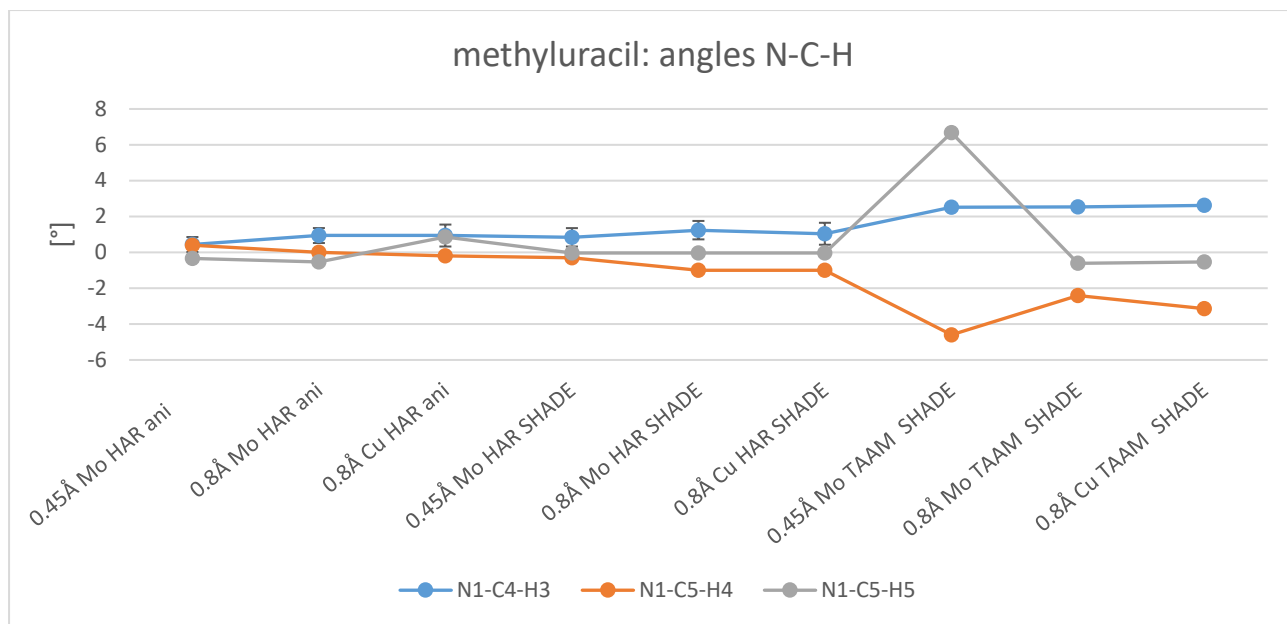


Figure S47 Comparison of N-C-H angles for HAR and TAAM refinements of **3**, **3-cutoff** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to the selected plots.

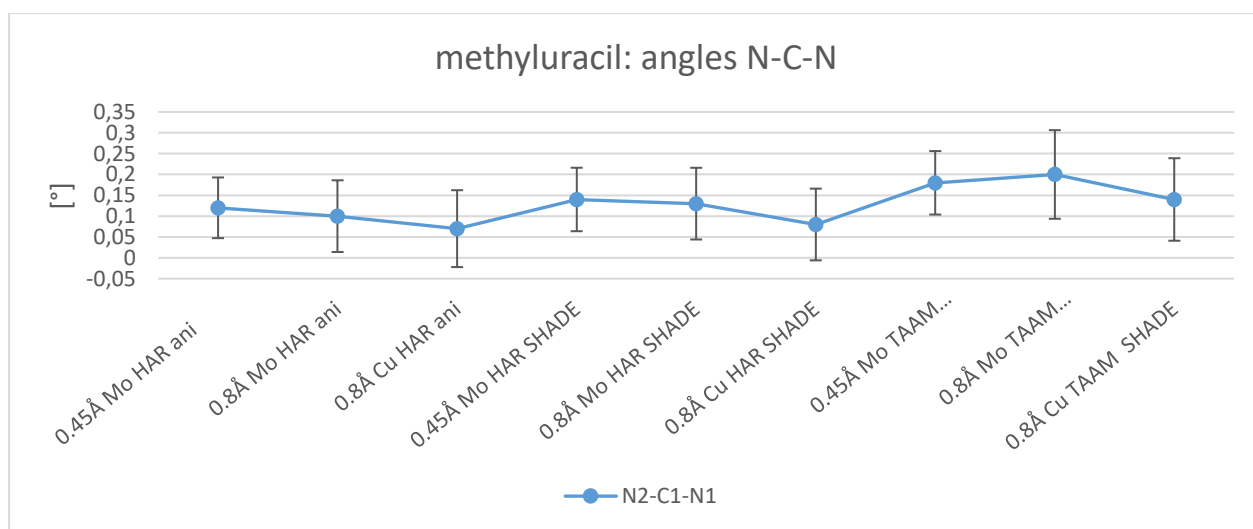
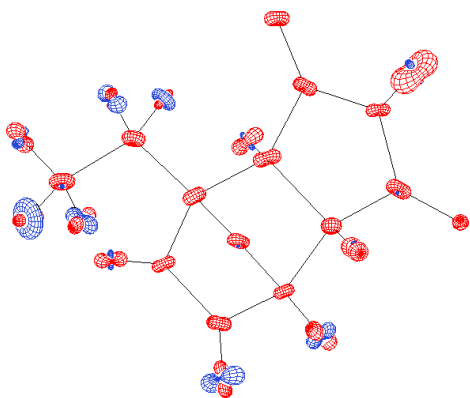
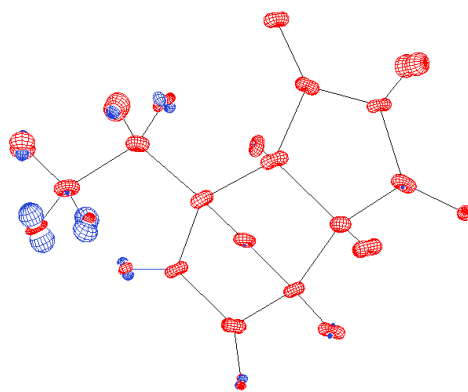


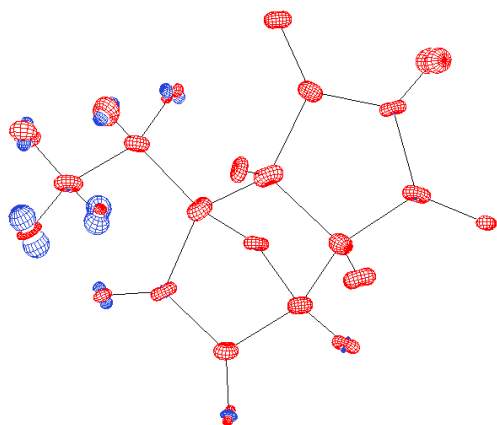
Figure S48 Comparison of N-C-H angles for HAR and TAAM refinements of **3**, **3-cutoff** and **3CuKa**. Values on plot represent difference between values obtained with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. Estimated standard deviations were added to the plot.



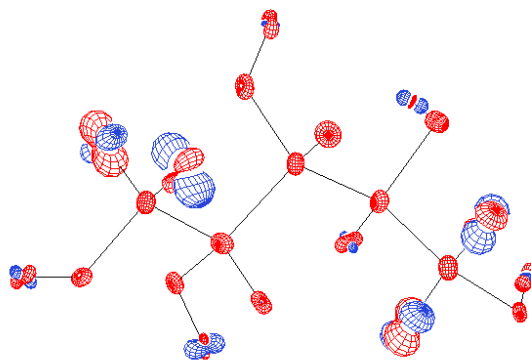
1-cutoff: HAR aniso



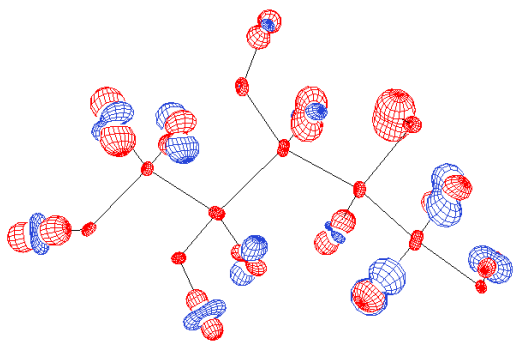
1-cutoff: HAR SHADE



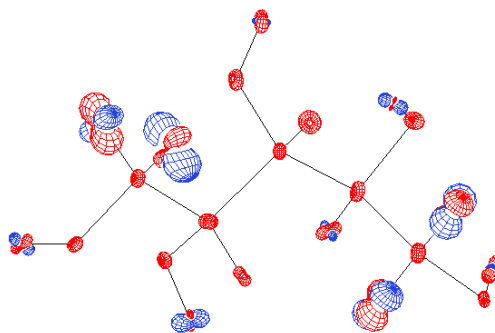
1-cutoff: TAAM SHADE



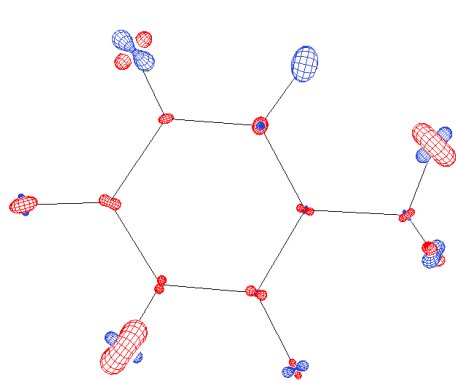
2-cutoff: TAAM SHADE



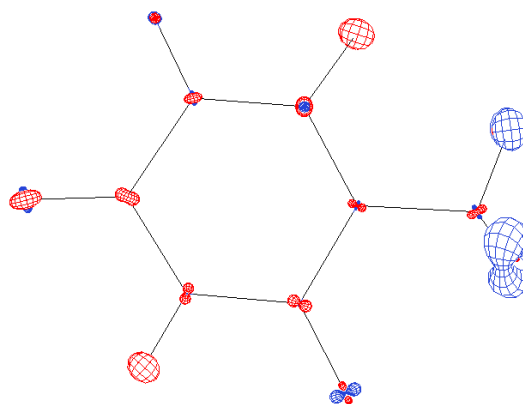
2-cutoff: HAR aniso



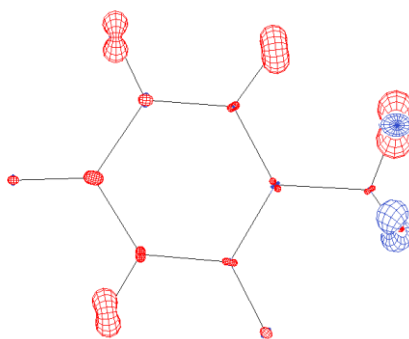
2-cutoff: HAR SHADE



3-cutoff: HAR aniso



3-cutoff: HAR SHADE



3-cutoff: TAAM SHADE

Figure S49 Difference between ADPs of neutron and analysed model for HAR and TAAM refinements of **1-cutoff**, **2-cutoff** and **3-cutoff**. Two-step overlay algorithm and 2.0 scale were applied using PEANUT software.

Section S1. Combination of Normal Mode Refinement with the Multipole Model

Starting from TAAM structure of **1** ([10] CSD deposition number: 2008296 (1)) the high resolution X-ray diffraction data for **1** were refined using Mo-ProSuite. [11] In the refinement, the following parameters were refined consecutively: valence populations (P_{val}) multipoles (P_{lm} , *i.e.* dipoles, quadrupoles, octupoles and for oxygen atoms hexadecapoles), expansion and contraction parameters (κ and κ'). After each block refinement of κ s, the xyz and Uij parameters were re-fined. As the ADPs of H-atoms were obtained from the Normal Mode Refinement (procedure described in the Section 2.4 in ms. and Scheme S3 in SI). Moreover, the X-H distances were extended to the mean neutron values as restraints with a standard deviation of 0.001. [12] Final structure is present in the Fig. S50 (in the middle) and statistical parameters are present in the Table S14. Based on the geometry of the final structure, statistical parameters, fractal dimension plot and residual density maps (Fig. S51) we can judge the **1MM_NoMoRe** structure as a reliable. However, we excluded detail analysis of this approach in the ms. as the NoMoRe ADPs were already analysed in the Section 3.3. in ms. and the restraints were applied for the X-H bonds. Therefore, the influence on X-H bonds in the MM_NoMoRe refinement is not significant as in the case of HAR_NoMoRe refinement whereas the X-H bonds are refined freely (Fig. S52). However, based on the residual density maps (Fig. S51) we can see the differences arise from the ADPs modelling on the electron density. Furthermore, combination of both refinements *i.e.* MM and NoMoRe were already reported [9].

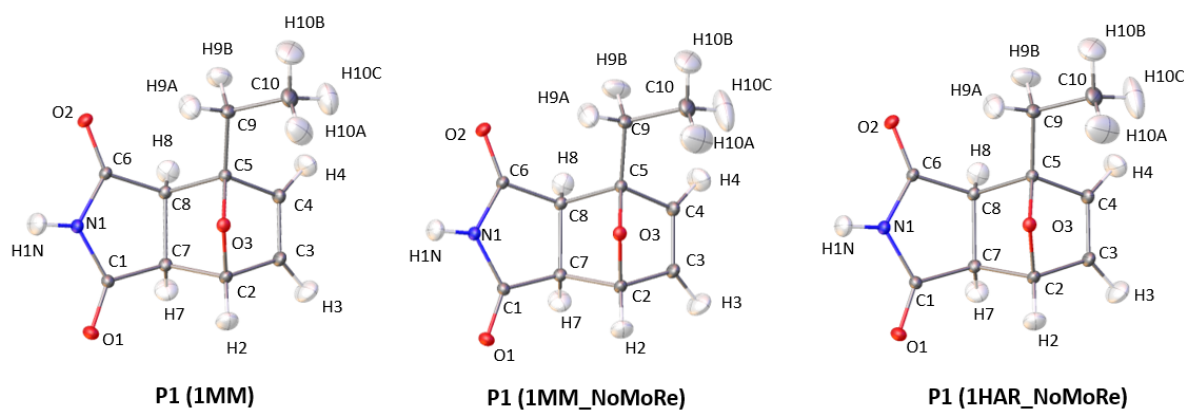
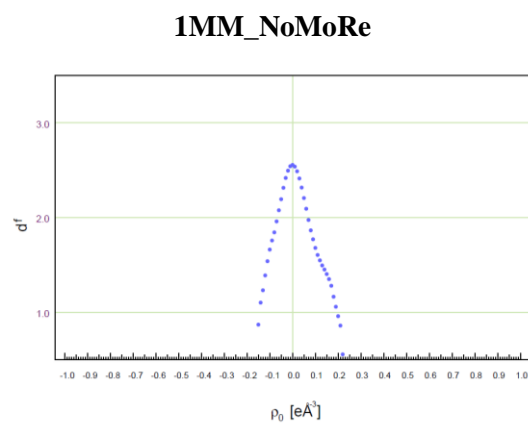
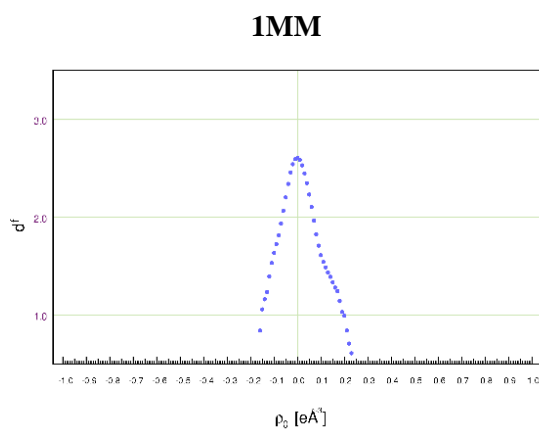


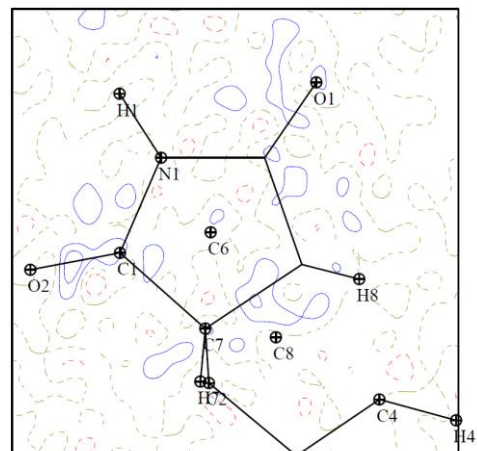
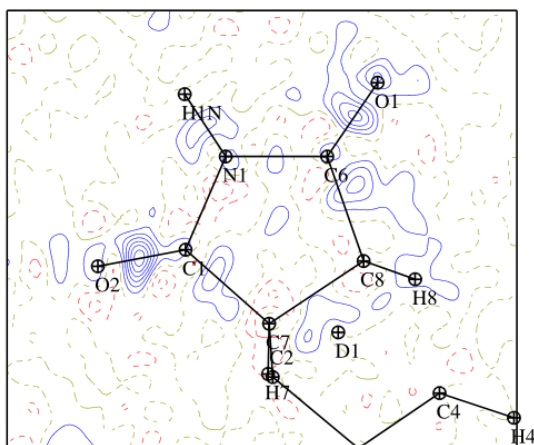
Figure S50 Labelling of atoms and visualisation and comparison of atomic ADPs in molecular structures of the studied compound **1** obtained with the MM, MM_NoMoRe and HAR_NoMoRe refinements. Anisotropic atomic displacement ellipsoids are drawn at the 50% probability level.

Table S14 Statistical parameters of MM NoMoRe refinement of **1** with comparison to the MM and HAR NoMoRe.

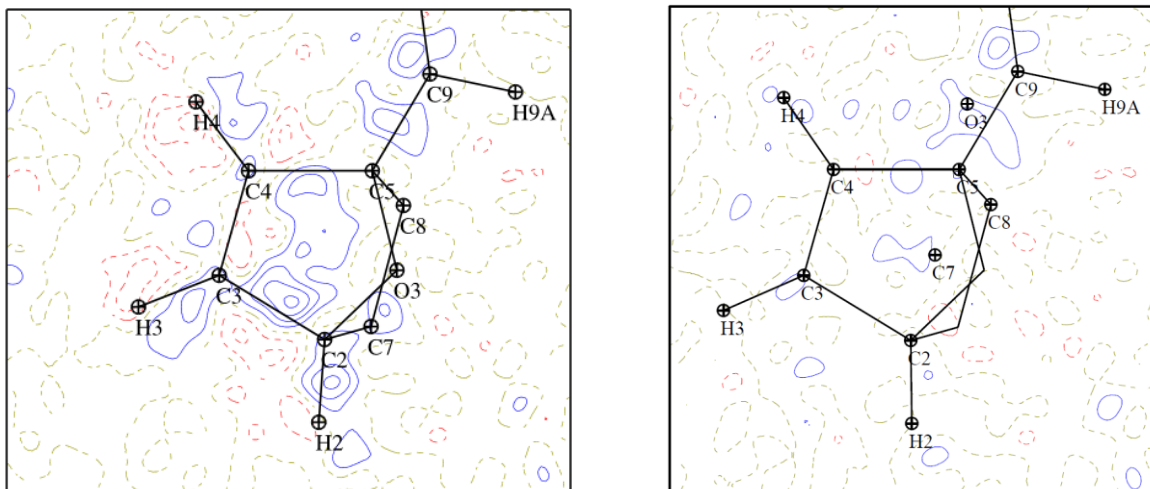
Compound	Parameters	MM	MM NoMoRe	HAR NoMoRe
1	$R[F > 2\sigma(F)]$	0.013	0.014	0.015
	$wR(F^2)$	0.043	0.043	0.045
	# of reflections	9849	9849	9828
	# of fit parameters	160	160	160
	χ^2	n/a	n/a	2.41
	Goodness of fit	1.35	1.34	1.55
	ΔQ_{\max}	0.22	0.22	0.21
	ΔQ_{\min}	-0.16	-0.15	-0.15



Fractal dimension plots.



Residual density maps, plane determined by N1 (centre), C6 (x axis) and C1 (y axis) atoms. Maps are presented with contours levels with intervals $\pm 0.05 \text{ e}\text{\AA}^{-3}$. Blue lines represent positive values and red lines the negative ones



Residual density maps, plane determined by C4 (centre), C5 (x axis) and C3 (y axis) atoms. Maps are presented with contours levels with intervals $\pm 0.05 \text{ e}\text{\AA}^{-3}$. Blue lines represent positive values and red lines the negative ones

Figure S51 Fractal dimension plots and residual density maps for MM (SHADE, NoMoRe) refinements of **1**.

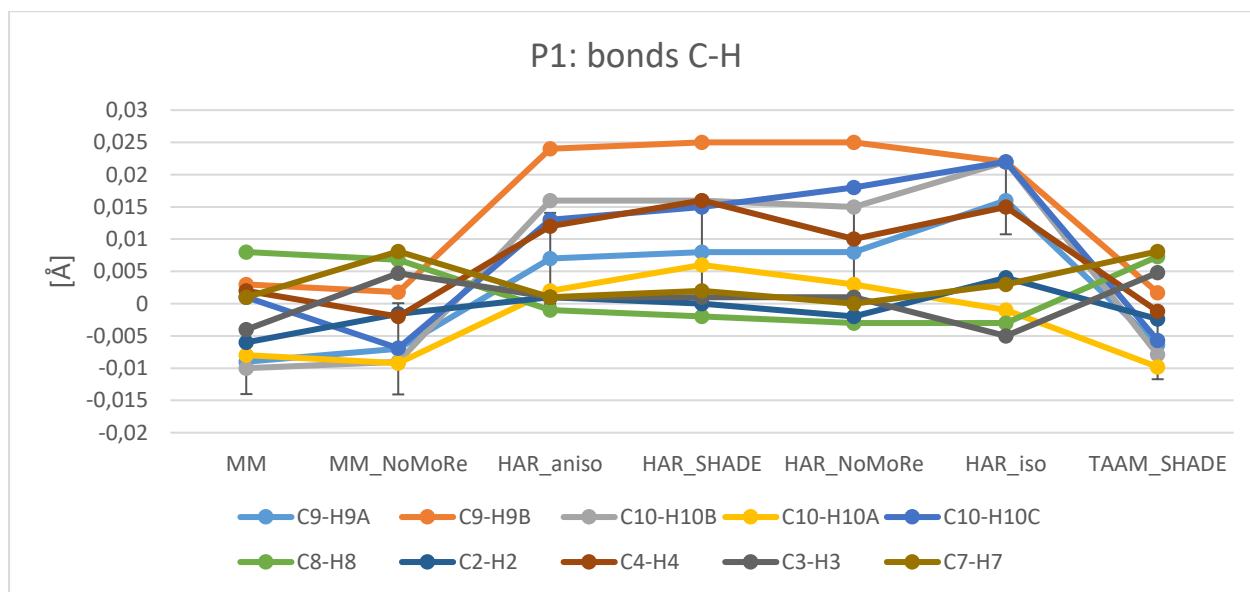


Figure S52 Comparison of C-H bonds for MM (SHADE, NoMoRe), HAR (SHADE, NoMoRe, aniso, iso) and TAAM (SHADE) refinements of **1**. Values on plot represent difference between values obtained

with analysed model and neutron data in angstroms. Lines on plot have no physical meaning, however help in visual analysis. For clarity, estimated standard deviations were added to selected plot (C9-H9A).

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1. Capelli, S.C.; Bürgi, H.-B.; Dittrich, B.; Grabowsky, S.; Jayatilaka, D. Hirshfeld Atom Refinement. *IUCrJ* **2014**, *1*, 361–379, doi:10.1107/S2052252514014845.
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3. Jelsch, C.; Pichon-Pesme, V.; Lecomte, C.; Aubry, A. Transferability of Multipole Charge-Density Parameters: Application to Very High Resolution Oligopeptide and Protein Structures. *Acta Cryst D* **1998**, *54*, 1306–1318, doi:10.1107/S0907444998004466.
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5. Dittrich, B.; Hübschle, C.B.; Pröpper, K.; Dietrich, F.; Stolper, T.; Holstein, J. The Generalized Invariom Database (GID). *Acta Cryst B* **2013**, *69*, 91–104, doi:10.1107/S2052519213002285.
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