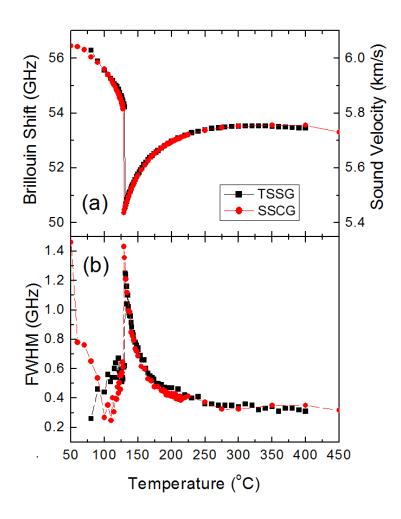


**Figure S1.** Temperature dependence of the real part of the complex permittivity and its inverse shown on the left and right ordinate, respectively, of the (a) SSCG-grown and (b) TSSG-grown BaTiO<sub>3</sub> single crystals. The solid line is the best-fitted result for the inverse dielectric constant in the paraelectric phase obtained by using the Curie–Weiss law. The data of TSSG-grown BaTiO<sub>3</sub> were the modified one reported in Reference 18.



**Figure S2.** Temperature dependence of (a) the Brillouin shift of the LA mode, (b) the FWHM of the LA mode of both TSSG-grown and SSCG-grown BaTiO<sub>3</sub> single crystals. The mode frequency and the FWHM of the TSSG-grown BaTiO<sub>3</sub> were modified from the reported values in Reference 17.