

Article

# In Silico Acetylene [2+2+2] Cycloadditions Catalyzed by Rh/Cr Indenyl Fragments

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**Abstract:** Metal-catalyzed alkyne [2+2+2] cycloadditions provide a variety of substantial aromatic compounds of interest in the chemical and pharmaceutical industries. Herein, the mechanistic aspects of the acetylene [2+2+2] cycloaddition mediated by bimetallic half-sandwich catalysts [Cr(CO)<sub>3</sub>IndRh] (Ind = (C<sub>9</sub>H<sub>7</sub>)<sup>−</sup>, indenyl anion) are investigated. A detailed exploration of the potential energy surfaces (PESs) was carried out to identify the intermediates and transition states, using a relativistic density functional theory (DFT) approach. For comparison, monometallic parent systems, i.e., CpRh (Cp = (C<sub>5</sub>H<sub>5</sub>)<sup>−</sup>, cyclopentadienyl anion) and IndRh, were included in the analysis. The active center is the rhodium nucleus, where the [2+2+2] cycloaddition occurs. The coordination of the Cr(CO)<sub>3</sub> group, which may be in syn or anti conformation, affects the energetics of the catalytic cycle as well as the mechanism. The reaction and activation energies and the turnover frequency (TOF) of the catalytic cycles are rationalized, and, in agreement with the experimental findings, our computational analysis reveals that the presence of the second metal favors the catalysis.

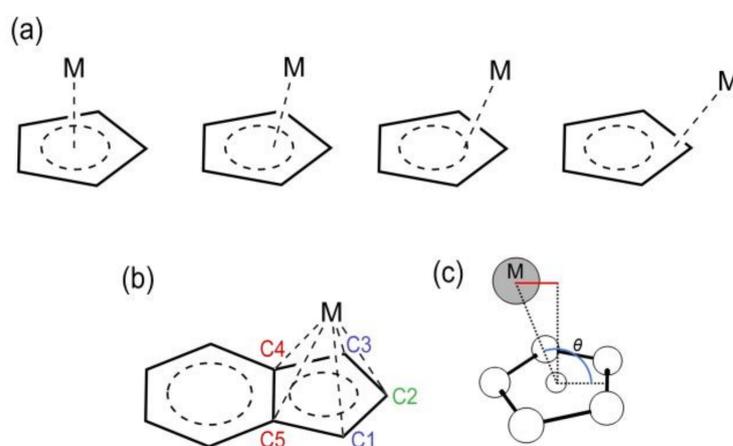
**Keywords:** acetylene [2+2+2] cycloadditions; DFT calculations; rhodium; chromium; half-sandwich catalysts; turnover frequency (TOF); activation strain analysis; indenyl effect; metal slippage; slippage span model

## 1. Introduction

The [2+2+2] cycloadditions of small unsaturated molecules, such as alkynes and nitriles, afford a variety of aromatic, heterocyclic and polycyclic compounds of paramount importance in the chemical and pharmaceutical industries [1]. In 1867, the synthesis of benzene by thermal cyclotrimerization of acetylene was reported for the first time [2]. Despite the reaction being highly exothermic, it is strongly disfavored by entropic factors, and this limits its synthetic utility. Reppe and Schweckendieck demonstrated that low valent metal nuclei catalyze these [2+2+2] cycloadditions [1]. Further studies assessed that a wide variety of metals such as Ti, Zr, Ru, Co, Rh, Ir, Ni, and Pd may play an important role as catalysts in the synthesis of benzene and its derivatives and, in the past decades, experimental results and theoretical insight have been reported to establish the correct mechanism and tune the efficiency and regioselectivity [3–7].

One important class of catalysts for alkyne [2+2+2] cycloadditions are the half-sandwich complexes, i.e., metal-cyclopentadienyl (CpM) or metal-ligand complexes in which the metal is coordinated to the Cp moiety of larger polycyclic ligands. These compounds possess peculiar structural features and reactivity properties; for this reason, and for their synthetic versatility, they are largely used [8–13]. They are denoted here with the general formula Cp'ML<sub>n</sub>, where Cp' = Cp, Ind, and L<sub>n</sub> are the ancillary ligands coordinated to the metal center (M), so that the 18-electrons rule is satisfied. Group 9 metals, i.e., cobalt, rhodium, and iridium, have been largely employed and, particularly, cobalt and rhodium have revealed significant catalytic efficiency [14–17]. The bonding mode of the metal to the Cp moiety (hapticity) is not perfectly symmetric ( $\eta^5$ ), but typically exhibits a distortion toward allylic ( $\eta^3$ )

coordination [18,19], and eventually to an extreme structure in which a  $\sigma$  metal-carbon bond forms ( $\eta^1$ ). This phenomenon is called metal slippage, and the different bonding modes are shown in Scheme 1a.



**Scheme 1.** (a) Different coordination modes (hapticities) of a metal (M) to a Cp ring. (b) Labelling scheme used in the definition of  $\Delta$  and LISP (Equations (1) and (2)). (c). Definition of  $\theta$  angle for LISP calculation.

To quantify the slippage, Basolo and coworkers [20,21] introduced the geometrical parameter  $\Delta$  (Equation (1)).

$$\Delta = \frac{(M-C4 + M-C5) - (M-C1 + M-C3)}{2} \quad (1)$$

As shown in Scheme 1b, M-C4 and M-C5 are the longest distances between M and two adjacent C atoms of the Cp ring, and M-C3 and M-C1 are the distances between M and the C atoms adjacent to C4 and C5, respectively.

The slippage variations occurring during the catalytic cycle can be quantified referring to the value of  $\Delta$ , which changes from 0 Å ( $\eta^5$ ) to nearly 0.3 Å ( $\eta^3$ ) till 0.6 Å or even higher values ( $\eta^1$ ). Some of us have recently pointed out that this definition suitably applies to symmetric systems [22], and thus have introduced another descriptor, i.e., the label independent slippage parameter (LISP) (Equation (2)).

$$\text{LISP}(\text{\AA}) = \frac{d}{N} \sum_{i=1}^N \left| \sin\left(\theta_i - \frac{\pi}{2}\right) \right| \quad (2)$$

LISP is actually the sum of the five average minimum distances from a normal vector passing through the centroid and the metal;  $d$  is the distance between the metal and the centroid of the ring of  $N$  atoms (Scheme 1c). Importantly, LISP is also suitable for describing non-symmetric displacements. In the same paper [22], a relationship between the catalytic activity of several half-sandwich group 9 metal complexes for alkyne [2+2+2] cycloadditions and the slippage span expressed in terms of LISP (computed as the difference between the maximum and the minimum value of LISP along the catalytic cycle) was established. The slippage span  $\Delta\text{LISP}$  was then related to the turn-over frequency (TOF) values, calculated with the energy span model [23], and it emerged that the lower the  $\Delta\text{LISP}$  is, the higher the TOF is. Finally, in order to improve the sensitivity of  $\Delta\text{LISP}$ ,  $\Delta\text{LISP}^*$  was introduced:

$$\Delta\text{LISP}^* (\text{\AA}) = \sum_{i=1}^{N-1} |\text{LISP}_1 - \text{LISP}_{i+1}| + \sum_{i=1}^{N-1} |\text{LISP}_i - \text{LISP}_{i+1}| + |\text{LISP}_N - \text{LISP}_1| \quad (3)$$

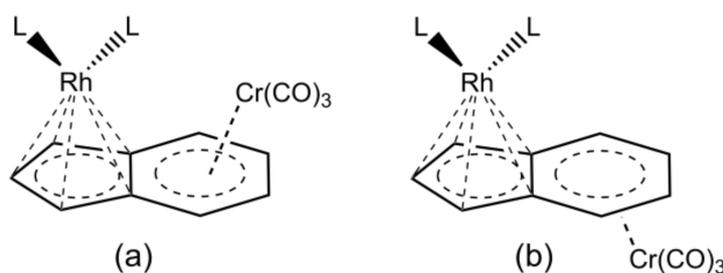
In this descriptor (Equation (3)), the first term indicates how far/close each intermediate/transition state of the catalytic cycle is from/to the starting point. The second term accounts for the slippage difference between two consecutive states along the whole catalytic cycle. The last term includes the

slippage variation between the last intermediate and the initial state. The availability of a flexible parameter to quantify the metal slippage, which intuitively influences the catalytic activity, and of a relationship between the metal slippage and the turn-over frequency is a valuable tool. So far, the slippage span model has been applied to monometallic Co and Rh half-sandwich catalysts for alkyne [2+2+2] cycloadditions [22]; in this work, we apply it to bimetallic Rh/Cr indenyl catalysts to assess its general validity.

Different strategies have been developed to tune the regioselectivity and the efficiency of the half-sandwich catalysts. Ingrosso et al. [24,25] experimentally studied the influence of organic moieties, i.e., cyclopentadienyl (Cp), indenyl (Ind) and fluorenyl (FN), in Rh(I) half-sandwich catalysts on alkyne [2+2+2] cycloadditions. Booth et al. [26] reported that IndRh initiates the reaction ten times faster as compared to CpRh, and this was related to the so-called *indenyl effect* (a phenomenon firstly reported by Adam J. Hart-Davis and Roger J. Mawby in 1969 [27], it was thoroughly explored and named by Fred Basolo [28]; it consists in an enhancement of the rate of the substitution reactions at the metal when indenyl is used instead of cyclopentadienyl aromatic ligand). It was also observed that the presence of an electron withdrawing group in the Cp ligand reduces the catalytic activity at low temperature [29,30]. Based on these studies, it emerged that structural and electronic modifications to the aromatic moiety of the half-sandwich catalyst influence its efficiency.

Changing the metal also plays a role. For example, considering group 9 metals, Co is highly preferred when compared to Rh and Ir [31,32].

Finally, another modification to a half-sandwich catalyst is the coordination of a second metal to form a bimetallic complex [1] when the aromatic ligand is polycyclic; the second metal can be in syn or anti position. A very nice example, reported by Cecon et al. [33–35], is  $[\text{Cr}(\text{CO})_3\text{IndRh}]\text{L}_2$  (Scheme 2). The idea behind the design of these compounds was that the presence of two metal centers within the same molecule may profoundly affect both the physical properties and the reactivity of the catalyst. In fact, it was found that the presence of a second metal in the anti position strongly enhances the reactivity as compared to monometallic complexes (*extra-indenyl effect*) [36].



**Scheme 2.** Anti-(a) and syn-(b)  $[\text{Cr}(\text{CO})_3\text{IndRh}]\text{L}_2$ .

Nowadays, DFT computational methodologies make it possible to investigate the mechanistic details of catalytic reactions, defining with accuracy their thermodynamic (reaction energies) as well as their kinetic (activation energies) features. After the pioneering work by Albright and co-workers on CpCo catalyzed acetylene [2+2+2] cycloaddition to benzene [37], several important computational studies were carried out by Calhorda and Kirchner on CpRuCl [38–40], Orian and Bickelhaupt on CpRh and IndRh [41–43] and analogous heteroaromatic Rh(I) catalysts [44], Koga and co-workers on CpCo [31,45,46], and Hapke et al. on CpIr [45]. To the best of our knowledge, no theoretical mechanistic investigation on the use of bimetallic half-sandwich catalysts has been reported so far. The use of bimetallic complexes as catalysts in organic synthesis is interesting, because the reaction rate and selectivity can be tuned via possible inter-metal cooperative effects. Cecon et al. have provided rather complete information on anti- and syn- $[\text{Cr}(\text{CO})_3\text{IndRh}]\text{L}_2$ . Particularly, they studied the cyclotrimerization of methylpropiolate (MP) and dimethyl-acetylenecarboxylate (DMAD) with mono and bimetallic catalysts, i.e., IndRh(COD), *p*-NO<sub>2</sub>-IndRh(COD) and bimetallic anti- $[\text{Cr}(\text{CO})_3\text{IndRh}(\text{COD})]$ . They found that the Rh/Cr catalyst leads to a greatly enhanced catalytic

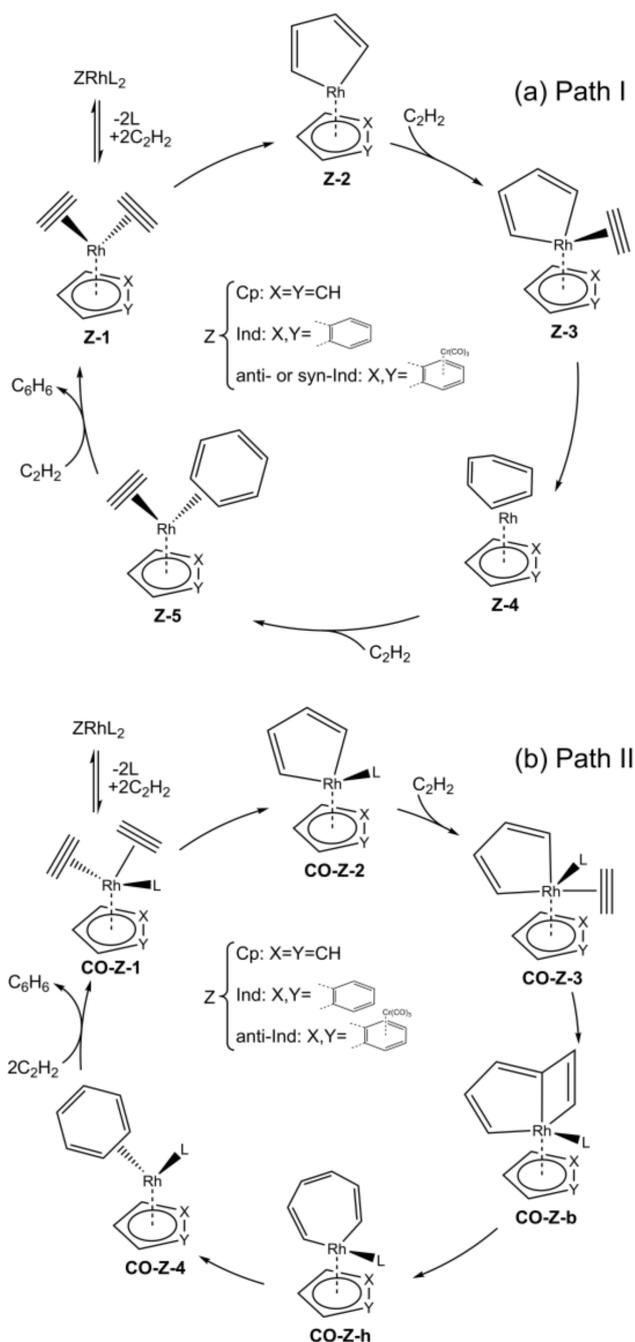
efficiency compared to the monometallic one. This increase of catalytic activity was ascribed to a synergic or “cooperative” interaction between the two metals in activating the substrate of interest [33–35].

The main goal of this study is the detailed investigation of the mechanism of acetylene [2+2+2] cycloaddition catalyzed by Rh/Cr indenyl fragments, particularly focusing on (i) the presence of the second metal, i.e., Cr, on the mechanism and energetics; (ii) the relationship between rhodium slippage and catalytic activity, and (iii) the outline of general guidelines for the design of Rh(I) half-sandwich catalysts based on the slippage span model. Points (i) and (ii) will be presented in the Results section, while point (iii) will be treated in the Discussion.

## 2. Results

The computational mechanistic investigation of acetylene [2+2+2] cycloaddition to benzene catalyzed by the monometallic catalysts CpRh and IndRh was first reported in 2006 [41]. In Scheme 3a (Path I), the well-known and widely accepted mechanism, proposed by Albright for CpCo catalysis [47,48] is shown. The catalytic cycle begins with the replacement of the ancillary ligands L of the catalyst precursor, i.e., Cp-or Ind-RhL<sub>2</sub> (L = CO, PPh<sub>3</sub> or COD (1,5-cyclooctadiene)) by two molecules of acetylene, leading to the bis-acetylene complex **Z-1**. The coordinated acetylene molecules undergo oxidative coupling and the unsaturated 16-electrons rhodacycle **Z-2** forms. This elementary step typically has the highest activation energy and was recently discussed in detail for group 9 metal-Cp fragments [49]. The subsequent coordination of a third acetylene molecule occurs without an appreciable activation energy and leading to **Z-3**, and, after its addition to the  $\pi$ -electron system of the rhodacycle, the intermediate **Z-4** is obtained, which is characterized by an unsaturated bent six-membered ring. By further stepwise addition of two acetylene molecules, the intermediate **Z-5** first forms and then the initial catalyst is regenerated with the cleavage of benzene.

An alternative mechanism was postulated by Booth and co-workers [26] on the basis of their experimental findings, which implies that a ligand of the catalyst precursor remains bonded to the metal center throughout the whole catalytic cycle; this is shown in Scheme 3b (Path II). This mechanism was rationalized by Orian et al. [43] in a recent systematic study on the *indenyl effect* and its connection to metal slippage. The presence of an ancillary ligand imposes strong hapticity variations in both CpRh and IndRh catalysis. In addition, the bicyclic **CO-Z-b**, and the heptacyclic **CO-Z-h** were located along this catalytic path, which resembles the one described for CpRuCl catalysis [38].



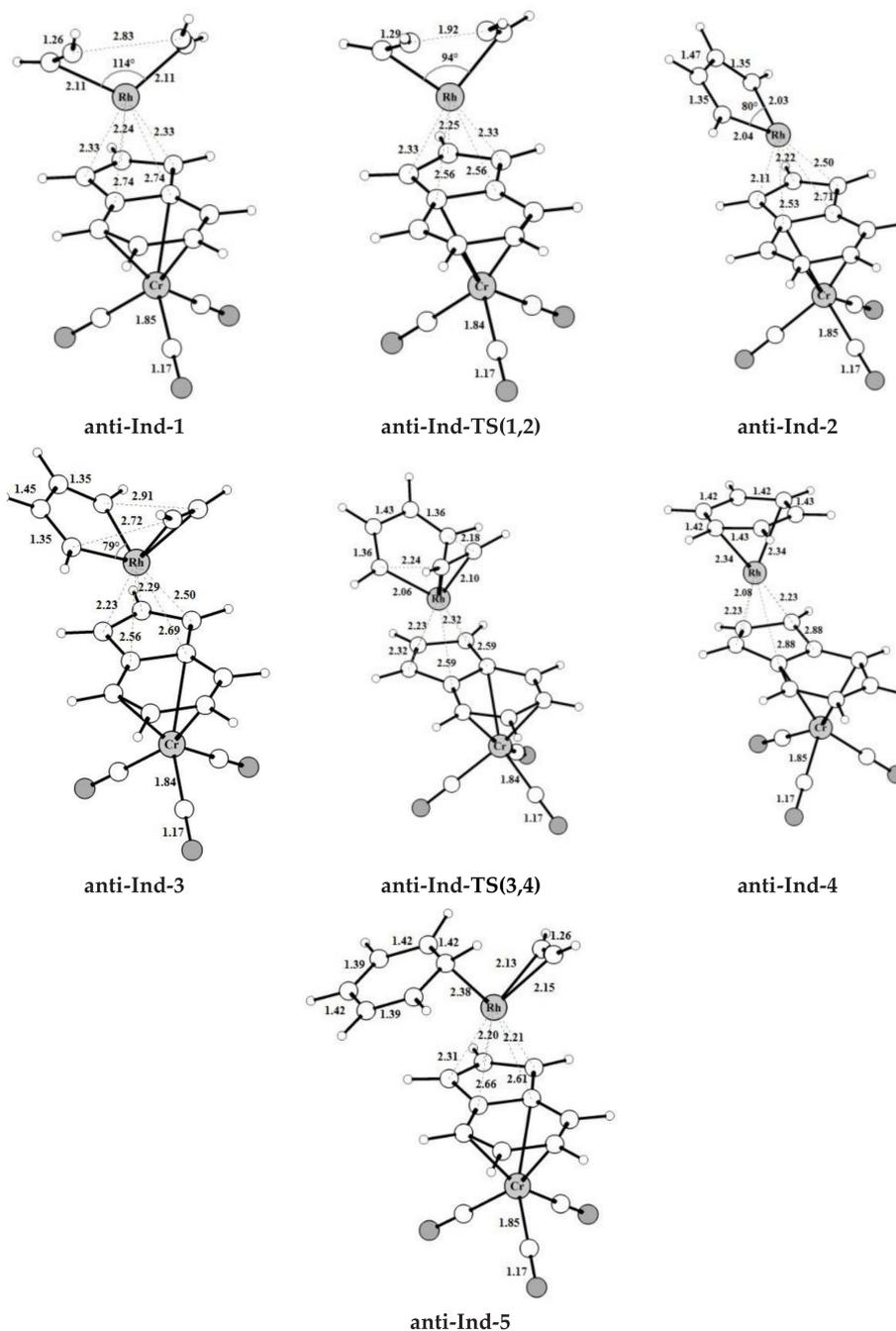
**Scheme 3.** Mechanism of acetylene [2+2+2] cycloaddition to benzene catalyzed by ZRh (Z = Cp, Ind and anti or syn-Ind) (Path I) (a) and by CO-ZRh fragments (Z = Cp, Ind and anti-Ind; L = CO) (Path II) (b).

Inspired by the experimental work by Ceccon et al. [33–35], we chose the bimetallic catalyst [Cr(CO)<sub>3</sub>IndRhL<sub>2</sub>], where the second metal group Cr(CO)<sub>3</sub> can be coordinated both in anti and syn conformations and examined both paths I and II of Scheme 3. The optimized molecular structures (ZORA-BLYP/TZ2P) of anti- and syn-[Cr(CO)<sub>3</sub>IndRh(CO)<sub>2</sub>] (Figure S1) are in good agreement with the X-ray crystallographic structures (labelled as HEXPOP [50] and HAPPOD [34] in the Cambridge database (CSD) [51]). Significant geometry parameters are compared in Table S1.

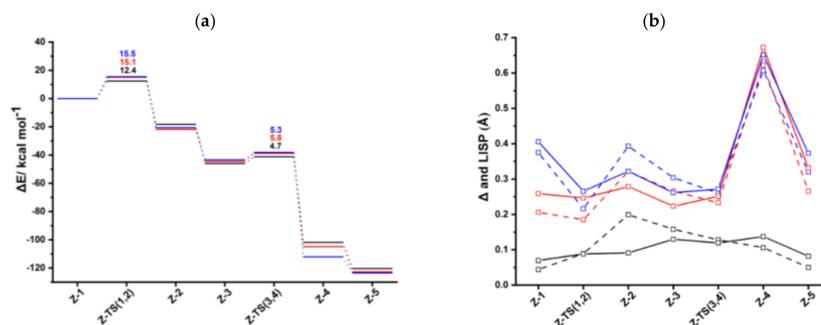
For simplicity, in the ongoing discussion, anti- and syn-[Cr(CO)<sub>3</sub>IndRh] fragments are abbreviated as anti- or syn-IndRh (Scheme 3).

### 2.1. Acetylene [2+2+2] Cycloaddition Catalyzed by Anti-[Cr(CO)<sub>3</sub>IndRh] Fragment: Reaction Mechanism and PES (Path I)

The intermediates and transition states found for acetylene [2+2+2] cycloaddition catalyzed by the bimetallic anti-IndRh along Path I (Scheme 3a), are shown in Figure 1. Those found on the PES of the parent monometallic catalysts, i.e., CpRh and IndRh, are in Figures S2 and S3, respectively. The computed energy profile for anti-RhInd is shown in Figure 2a.



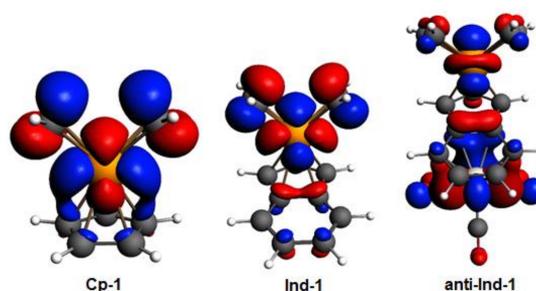
**Figure 1.** Optimized structures with selected interatomic distances (Å) and angles (deg) of the intermediates and transition states located on the PES of the anti-IndRh catalyzed acetylene [2+2+2] cycloaddition to benzene (Path I, Scheme 2a). Level of theory: ZORA-BLYP/TZ2P.



**Figure 2.** (a) Energy profiles of acetylene [2+2+2] cycloaddition to benzene catalyzed by CpRh (black), IndRh (red), and bimetallic anti-IndRh (blue) (Scheme 3a, Path I). (b) Profiles of the slippage parameters  $\Delta$  (dashed line) and LISP (solid line) for the acetylene [2+2+2] cycloaddition cycles catalyzed by CpRh (black), IndRh (red), and bimetallic anti-IndRh (blue) along Path I (Scheme 3a). Level of theory: ZORA-BLYP/TZ2P.

The catalytic cycle mediated by anti-IndRh is very similar to the cycle described for the monometallic parent catalysts CpRh and IndRh [41] since the  $\text{Cr}(\text{CO})_3$  group is coordinated in anti, and thus there is no steric effect. It begins with replacement of the ancillary ligands L by two acetylene molecules to form a bis-acetylene complex labelled **anti-Ind-1** (Scheme 3a). This process usually occurs experimentally by thermal or photochemical activation and might be dissociative or associative depending on the nature of the metal, on the electrophilicity of the ligands and on the substituents on the Cp ring [21,28,52]. In **anti-Ind-1**, the acetylene molecules are slanted with respect to the plane of the indenyl ring and the C-C bond length is 1.26 Å. The Rh-C $_{\alpha}$  and Rh-C $_{\beta}$  bond lengths are 2.11 Å and 2.13 Å, respectively; they are shorter as compared to those of **Ind-1** (2.13 Å and 2.16 Å). This suggests that acetylene is more tightly bonded, likely due to the electron withdrawing effect of the second metal group  $\text{Cr}(\text{CO})_3$ . Additionally, the Rh-Cp coordination is more distorted in **anti-Ind-1** than in the parent **Cp-1** and **Ind-1**, as also quantified by the metal slippage parameters  $\Delta$  and LISP, which were calculated for the intermediates and the transition states along the whole catalytic cycle (Figure 2b).

By inspecting the frontier molecular orbitals of **Cp-1**, **Ind-1** and **anti-Ind-1** shown in Figure 3, the  $\pi$ -antibonding character between Cp'- $\pi$  system and valence  $d$  orbitals of Rh is found to increase in the order **Cp-1** < **Ind-1** < **anti-Ind-1**, leading to a corresponding increase of metal slippage. Calhorda et al. have reported the same observation in their pioneering work on the nature of indenyl effect, which was related to the nodal characteristics of Cp'- $\pi$  orbitals of CpRh and IndRh [19,44]. Herein, it is found that the metal- $\pi$  anti-bonding nature with Ind- $\pi$  system is further enhanced in the presence of  $\text{Cr}(\text{CO})_3$  in **anti-Ind-1** compared to the parent **Ind-1**, leading to extra slippage of rhodium in the former.



**Figure 3.** Kohn-Sham HOMOs of **Cp-1**, **Ind-1**, and **anti-Ind-1**; level of theory: ZORA-BLYP/TZ2P. The isodensity value is 0.03.

The oxidative coupling of the two coordinated acetylene molecules in **anti-Ind-1** leads to the 16-electrons unsaturated rhodacyclic intermediate **anti-Ind-2** (Figure 2), crossing an activation barrier of 15.5 kcal mol $^{-1}$ , which is higher than those computed for the formation of **Ind-2**

(15.1 kcal mol<sup>-1</sup>) and **Cp-2** (12.4 kcal mol<sup>-1</sup>). This reaction step is exothermic by 20.6 kcal mol<sup>-1</sup>. These metallacycles are generally described by two resonating structures, i.e., a metallacyclopentadiene, as found for CpCo-(C<sub>4</sub>H<sub>4</sub>) [37,49] and CpRh-(C<sub>4</sub>H<sub>4</sub>) [41,49], and a metallacyclopentatriene, as for CpRuCl-(C<sub>4</sub>H<sub>4</sub>) [38]. In **anti-Ind-2**, the C<sub>α</sub>-C<sub>β</sub> and C<sub>β</sub>-C<sub>β'</sub> distances are 1.35 Å and 1.47 Å, respectively, which are rather well matched to the length of the ethylene double bond and to the length of the σ-bond between two carbon atoms, respectively. This suggests the character of rhodacyclopentadiene of **anti-Ind-2**.

A third acetylene molecule easily coordinates to **anti-Ind-2**, which is converted into **anti-Ind-3**. This step is barrierless and exothermic by 22.8 kcal mol<sup>-1</sup>, about 5 kcal mol<sup>-1</sup> less exothermic than the formation of **CpRh-3**; this value is almost identical to the reaction energy computed for the formation of **IndRh-3**. Subsequently, by Diels-Alder-like [4+2] addition of the coordinated acetylene to the rhodacycle, **anti-Ind-4** forms, with an activation energy of 5.3 kcal mol<sup>-1</sup> (Figure 2a). This step is strongly exothermic by 68.6 kcal mol<sup>-1</sup>, 8.4 kcal mol<sup>-1</sup> more exothermic than the same step in the IndRh catalytic cycle; conversely, the energy barriers are very similar. Structurally, **anti-Ind-4** (Figure 1) is characterized by the presence of a six-carbon arene ring coordinated to rhodium in η<sup>6</sup> fashion, while η<sup>3</sup> coordination is found in the Cp-Rh moiety. A similar bonding mode of rhodium is found in **Ind-4**; conversely, in **Cp-4**, η<sup>4</sup> hapticity is observed with the arene ring and η<sup>3</sup>+η<sup>2</sup> coordination to Cp moiety. This pronounced slippage in **Ind-4** and **anti-Ind-4** explains the spikes in the profiles of Δ and LISP (Figure 2b). The coordination of another acetylene leads to the formation of **anti-Ind-5** (Figure 2a), accompanied by a variation of hapticity from η<sup>3</sup> to η<sup>3</sup>+η<sup>2</sup> in the anti-IndRh fragment and by the release of 11.5 kcal mol<sup>-1</sup>. The cleavage of benzene by the incoming second acetylene completes the cycle with the regeneration of the catalyst. The released energy is 16.4 kcal mol<sup>-1</sup>. Summarizing, the η<sup>3</sup>+η<sup>2</sup> coordination is found along the whole cycle catalyzed by **anti-IndRh** except in intermediate **anti-Ind-4**, where η<sup>3</sup> coordination is predicted.

Consistently with CpRh and IndRh catalysis, the first step **Z-1** → **Z-2**, that is the oxidative coupling of the acetylene molecules, has the highest energy barrier along the cycle (Figure 2a). To gain insight on the origin of this barrier, an activation strain analysis (ASA) has been carried out and compared to those already reported for CpRh and IndRh [49]. For this purpose, the complexes were divided into two fragments, i.e., Cp'Rh (Cp' = Cp, Ind, and anti-[Cr(CO)<sub>3</sub>Ind]) and the C<sub>4</sub>H<sub>4</sub> moiety. Being an intramolecular reaction, the activation energy ΔE<sup>‡</sup> is conveniently given as the change, upon going from the reactant to the TS, in strain within the two fragments plus the change, upon going from the reactant to the TS, in the interaction between these two fragments [53].

$$\Delta E^{\ddagger} = \Delta \Delta E_{\text{strain}} + \Delta \Delta E_{\text{int}} \quad (4)$$

The results are shown in Table 1. The ΔΔE<sub>strain</sub> contributions increase from CpRh to IndRh and to anti-IndRh and are very similar for the Cp'Rh fragments (ranging from 2.4 to 2.7 kcal mol<sup>-1</sup>), but increase significantly for the C<sub>4</sub>H<sub>4</sub> fragment going from 33.2 to 37.0 and 37.3 kcal mol<sup>-1</sup>, respectively. Since ΔΔE<sub>int</sub> are very similar, varying from -23.2 kcal mol<sup>-1</sup> (CpRh) to -24.6 kcal mol<sup>-1</sup> (IndRh) and -24.5 kcal mol<sup>-1</sup> (anti-IndRh), the increase of the barrier in the indenyl catalysts is mainly due to the strain effects localized on the bis-acetylene moiety. Based on the identical ΔΔE<sub>int</sub> for IndRh and anti-IndRh, no influence of the second metal of the latter is found in the barrier of this oxidative coupling.

**Table 1.** Activation strain analysis for the oxidative coupling **Z-1** → **Z-2** (Path I); all values are in kcal mol<sup>-1</sup>. The fragments are Cp'Rh (Cp' = Cp, Ind, and anti-[Cr(CO)<sub>3</sub>Ind]) and the C<sub>4</sub>H<sub>4</sub> moiety (the reference are two acetylene molecules).

	$\Delta\Delta E_{\text{strain}}$			$\Delta\Delta E_{\text{int}}$	$\Delta E^\ddagger$
	2(C <sub>2</sub> H <sub>2</sub> )	Cp'Rh	Total		
<b>Cp-1/Cp-TS (1,2)</b>	33.21	2.36	35.57	-23.16	12.41
<b>Ind-1/Ind-TS (1,2)</b>	37.02	2.66	39.68	-24.59	15.09
<b>anti-Ind-1/anti-Ind-TS (1,2)</b>	37.31	2.72	40.03	-24.52	15.51
<b>syn-Ind-1/syn-Ind-TS (1,2)</b>	39.67	46.98	86.65	-71.47	15.18

We also examined **Z-4**, which was found to be more stable in the case of anti-IndRh than in the cases of IndRh and CpRh. ASA was carried out on **Z-4**, by considering these two fragments: Cp'Rh, where (Cp' = Cp, Ind, and anti-[Cr(CO)<sub>3</sub>Ind]) and the C<sub>6</sub>H<sub>6</sub> moiety; the results are listed in Table 2. A very high total  $\Delta E_{\text{strain}}$  is found in **Cp-4** compared to **Ind-4** and **anti-Ind-4**, which comes out from the benzene fragment and reflects the structural differences. In fact, benzene is bent in **Cp-4** with  $\eta^4$  coordination (Figure S2), while in **Ind-4** and **anti-Ind-4**, the ring is almost planar and coordinated to rhodium in  $\eta^6$  fashion and  $\eta^3$  coordination is found for the Rh coordination to the Cp ring. On the other hand, the large  $\Delta E_{\text{strain}}$  of **Cp-4** is well balanced by a large negative  $\Delta E_{\text{int}}$ , which leads to larger  $\Delta E$  by about 12.2 kcal/mol than **Ind-4** and **anti-Ind-4**.

**Table 2.** Activation strain analysis for **Cp-4**, **Ind-4**, and **anti-Ind-4**; all values are in kcal mol<sup>-1</sup>. The fragments are Cp'Rh (Cp' = Cp, Ind, and anti-[Cr(CO)<sub>3</sub>Ind]) and C<sub>6</sub>H<sub>6</sub> moiety (the reference is benzene).

	$\Delta E_{\text{strain}}$			$\Delta E_{\text{int}}$	$\Delta E$
	C <sub>6</sub> H <sub>6</sub>	Cp'Rh	Total		
<b>Cp-4</b>	39.14	4.95	44.09	-83.44	-39.35
<b>Ind-4</b>	1.86	1.45	3.31	-30.44	-27.13
<b>anti-Ind-4</b>	1.64	1.26	2.90	-31.60	-28.70

Although the catalytic center is rhodium, we also investigated the coordination of Cr(CO)<sub>3</sub> in all the intermediates and transition states of the anti-IndRh catalyzed cycle. ASA was carried out using as fragments Cr(CO)<sub>3</sub> and IndRhX<sub>i</sub> (Table 3). Significantly larger  $\Delta E_{\text{strain}}$  values are found for **anti-Ind-TS (1,2)** and **anti-Ind-TS (3,4)**; the biggest contribution comes from the IndRhL<sub>n</sub> fragment, reflecting the changes occurring at the Rh center. The  $\Delta E_{\text{strain}}$  of Cr(CO)<sub>3</sub> fragment remains almost equal along the path, reflecting the fact that no important structural changes occur within the Cr(CO)<sub>3</sub> moiety.  $\Delta E_{\text{int}}$  values fluctuate in the range -47–54 kcal mol<sup>-1</sup>. In **anti-Ind-4**, a sudden increase of  $\Delta E_{\text{int}}$  is computed. In fact, on the opposite side of the indenyl ligand, Rh-Cp coordination is highly slipped (Figure 2). Therefore, in order to compensate for the weakening of Rh-Cp coordination, Cr(CO)<sub>3</sub> binds more tightly the benzene moiety of the aromatic ligand. In **anti-Ind-4**, the increased  $\Delta E_{\text{int}}$  is due to a larger electrostatic contribution which is not sufficiently counterbalanced by an increase of  $\Delta E_{\text{Pauli}}$ .

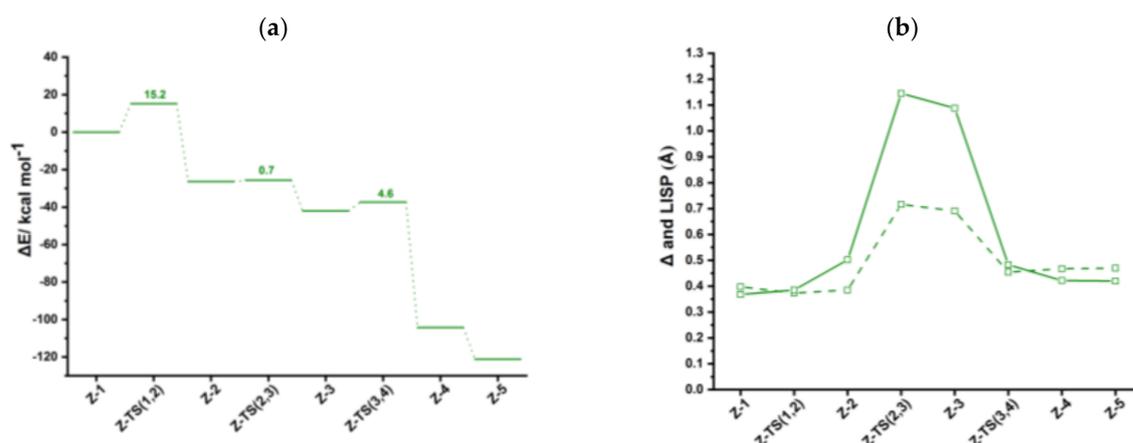
**Table 3.** Activation strain analysis (ASA) of all the intermediates and transition states of the anti-IndRh catalyzed cycle (Path I); all the values are in kcal mol<sup>-1</sup>. The fragments are Cr(CO)<sub>3</sub> and IndRhX<sub>i</sub>.

	$\Delta E_{\text{strain}}$			$\Delta V_{\text{elstat}}$	$\Delta E_{\text{Pauli}}$	$\Delta E_{\text{oi}}$	$\Delta E_{\text{int}}$	$\Delta E$
	Cr(CO) <sub>3</sub>	IndRhX <sub>i</sub>	Total					
<b>anti-Ind-1</b>	1.23	2.29	3.52	-76.47	129.17	-101.20	-48.50	-44.98
<b>anti-Ind-TS(1,2)</b>	1.26	17.17	18.43	-73.37	124.90	-99.39	-47.86	-29.43
<b>anti-Ind-2</b>	1.67	1.78	3.45	-73.03	130.93	-105.13	-47.24	-43.79
<b>anti-Ind-3</b>	1.36	1.85	3.21	-73.99	129.02	-102.09	-47.06	-43.85
<b>anti-Ind-TS(3,4)</b>	1.28	7.77	9.05	-73.38	125.83	-100.03	-47.58	-38.53
<b>anti-Ind-4</b>	1.23	1.17	2.40	-80.45	128.03	-101.74	-54.16	-51.76
<b>anti-Ind-5</b>	1.25	1.65	2.90	-73.39	123.39	-97.75	-47.75	-44.85

### 2.2. Acetylene [2+2+2] Cycloaddition Catalyzed by Syn-[Cr(CO)<sub>3</sub>IndRh] Fragment: Reaction Mechanism and PES (Path I)

As stated above, the coordination of the Cr(CO)<sub>3</sub> group to the benzene moiety of IndRh catalyst may occur in anti or syn conformation [54]. Ceccon and co-workers have illuminated the stereochemistry of the syn catalyst, i.e., syn-[Cr(CO)<sub>3</sub>IndRh], and found that it is kinetically more stable because of a Rh-Cr interaction.

First, we investigated the acetylene [2+2+2] cycloaddition to benzene catalyzed by syn-IndRh catalyst along Path I (Scheme 3a). The structures of the intermediates and transition states found on the PES with their relevant parameters are shown in Figure S4, while the computed energy profile is in Figure 4a. Like for anti-IndRh catalysis, at the beginning of the cycle, the ancillary ligands L are replaced by two molecules of acetylene, leading to the formation of the bis-acetylene complex **syn-Ind-1** (Figure S4). In **syn-Ind-1**, the Rh-C<sub>α</sub> bond length is 2.15 Å, the distance C<sub>β</sub>-C<sub>β'</sub> of two acetylenes coordinated to rhodium is 2.91 Å, and the angle C<sub>α</sub>-Rh-C<sub>α'</sub> is 91°. To quantify the Rh-Cp slippage along the catalytic cycle,  $\Delta$  and LISP parameters were computed for all the intermediates and transition states and are shown in Figure 4b. In **syn-Ind-1**, their values are 0.40 Å and 0.37 Å, respectively, with no appreciable difference with respect to **anti-Ind-1**; this might be ascribed to Rh-Cr interaction, despite high steric effects are present.



**Figure 4.** (a) Energy profile of acetylene [2+2+2] cycloaddition to benzene catalyzed by syn-IndRh (Scheme 3a, Path I). (b) Profiles of the slippage parameters (dashed line) and LISP (solid line) along the acetylene [2+2+2] cycloaddition cycle catalyzed by syn-IndRh (Scheme 3a, Path I). Level of theory: ZORA-BLYP/TZ2P.

The oxidative coupling in **syn-Ind-1** leads to the formation of the five-membered ring rhodacycle **syn-Ind-2** with an activation energy of 15.2 kcal mol<sup>-1</sup>, nearly the same as found for anti-IndRh. Notably, in **syn-Ind-2** complex, one CO of Cr(CO)<sub>3</sub> interacts with Rh. In fact, the distance between

the CO ligand and rhodium is 2.30 Å, and the distance between Cr and Rh center is smaller by 0.34 Å than in **syn-Ind-1**, implying stabilization of **syn-Ind-2**. In this situation, the rhodacycle **syn-Ind-2** is a nearly 18-electron saturated complex, in contrast to **anti-Ind-2** and the parent **Ind-2** and **Cp-2**. The conversion of **syn-Ind-1** into **syn-Ind-2** is exothermic by 26.4 kcal mol<sup>-1</sup>, about 6 kcal mol<sup>-1</sup> more than in the anti-catalyst and in the parent IndRh (Figure 3a). Finally, in this step, an hapticity shift from  $\eta^3+\eta^2$  to  $\eta^3$  occurs (Figure 4b).

The coordination of the third acetylene to **syn-Ind-2** occurs from the upper side with a low barrier of 0.7 kcal mol<sup>-1</sup>, via **syn-Ind-TS (2,3)** (Figure S4) and a large slippage variation (LISP changes by approximately 0.6 Å) leading to almost  $\eta^1$  coordination. The conversion **syn-Ind-2**  $\rightarrow$  **syn-Ind-3** occurs only with a slight modification in the carbon-carbon bonds of the rhodacycle. The reaction is exothermic by 15.6 kcal mol<sup>-1</sup>. In the next step, **syn-Ind-4** forms, crossing a barrier of 4.6 kcal mol<sup>-1</sup>. The LISP value drops from 1.09 Å to 0.42 Å (Figure 4b). **syn-Ind-4** has a six-carbon arene ring coordinated to rhodium in  $\eta^4$  fashion, while in Rh-Cp the coordination is  $\eta^3+\eta^2$ . Thus, the bonding mode of rhodium is different from **anti-Ind-4** (Figure 2), where  $\eta^6$  coordination and  $\eta^3$  coordination are found between the six-carbon arene ring and rhodium and the Cp ring and rhodium, respectively. However, **syn-Ind-4** resembles the case of the parent **Cp-4** [41]. This step is exothermic by 62.3 kcal mol<sup>-1</sup>.

Finally, the coordination of another acetylene leads to the formation of **syn-Ind-5** with no appreciable activation energy and with the release of 16.8 kcal mol<sup>-1</sup> (Figure 4a). It is less exothermic than the formation of **Ind-5** but more exothermic by 5 kcal/mol than the formation of **anti-Ind-5**. The cleavage of benzene promoted by another acetylene completes the cycle and leads to the regeneration of the catalyst. The energy released in this last step is 18.8 kcal mol<sup>-1</sup>. During the catalysis, the Rh-Cr distance varies in the range 3.05–3.51 Å, but remains close to the crystallographic value of 3.1 Å [34].

The hapticity variations along the catalytic cycle are definitively more pronounced in syn-IndRh catalysis than in the anti-IndRh one.

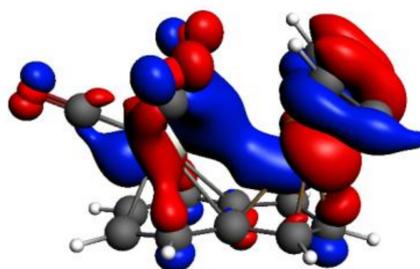
By inspecting the energy profile (Figure 4a), in the syn-IndRh catalyzed process the oxidative coupling **Z-1**  $\rightarrow$  **Z-2** has the highest energy barrier. From ASA (Table 1), a very high  $\Delta\Delta E_{\text{strain}}$  contribution to the barrier  $\Delta E^\ddagger$  has been found compared to anti-IndRh and also to the parent catalysts IndRh and CpRh. However,  $\Delta\Delta E_{\text{int}}$  is a pretty strongly stabilizing term and compensates for the strain, resulting in a lowering of  $\Delta E^\ddagger$ . In contrast to anti-IndRh, the strain arising from the Cp/Rh fragment is very high (Table 1) because of the steric effects and because Cr(CO)<sub>3</sub> undergoes deformation to interact with the Rh center.

To further assess the interaction and the role of Cr(CO)<sub>3</sub> in the syn-IndRh catalyzed process, ASA was carried out for the intermediates and transition states of the whole catalytic cycle, considering Cr(CO)<sub>3</sub> and IndRhX<sub>i</sub> fragments; the results are reported in Table 4.  $\Delta E_{\text{int}}$  are in the range ~49–58 kcal mol<sup>-1</sup>, larger than those computed for the anti-IndRh molecular species (Table 3), suggesting Rh-Cr stabilizing interaction in the former case. On the other hand,  $\Delta E_{\text{strain}}$  is also larger. This is mainly ascribed to steric factors. In particular, the contribution of Cr(CO)<sub>3</sub> to  $\Delta E_{\text{strain}}$  in **syn-Ind-2**, **syn-Ind-TS (2,3)** and **syn-Ind-3** is higher, suggesting some structural differences from the anti-analogous species. In fact, in these structures one carbonyl ligand is coordinated to Rh (Figure S4). This feature also leads to larger  $\Delta E_{\text{int}}$  in syn-Ind-2.

**Table 4.** Activation strain analysis (ASA) of all the intermediates and transition states along the syn-IndRh catalyzed cycle (Path I); all the values are in kcal mol<sup>-1</sup>. The fragments are Cr(CO)<sub>3</sub> and IndRhX<sub>i</sub>.

	$\Delta E_{\text{strain}}$			$\Delta V_{\text{elstat}}$	$\Delta E_{\text{Pauli}}$	$\Delta E_{\text{oi}}$	$\Delta E_{\text{int}}$	$\Delta E$
	Cr(CO) <sub>3</sub>	IndRhX <sub>i</sub>	Total					
syn-Ind-1	1.65	5.02	6.67	-80.49	132.33	-102.88	-51.04	-44.37
syn-Ind-TS (1,2)	1.62	20.29	21.91	-79.52	130.84	-102.42	-51.10	-29.19
syn-Ind-2	2.25	4.31	6.56	-117.69	195.36	-133.21	-55.54	-48.98
syn-Ind-TZ (2,3)	2.57	7.56	10.13	-117.3	188.69	-129.83	-58.45	-48.32
syn-Ind-3	2.52	11.78	14.30	-87.65	141.15	-109.59	-56.09	-41.79
syn-Ind-TS (3,4)	1.82	12.54	14.36	-81.06	135.13	-105.64	-51.57	-37.21
syn-Ind-4	1.15	4.50	5.65	-79.61	129.57	-99.01	-49.04	-43.39
syn-Ind-5	1.56	5.28	6.84	-78.6	128.78	-99.76	-49.58	-42.74

As an example of an existing favorable inter-metal interaction, in Figure 5, we show HOMO-3 of syn-Ind-1, which is formed by the contributions of the HOMOs of Cr(CO)<sub>3</sub> and IndRh(C<sub>2</sub>H<sub>2</sub>)<sub>2</sub> fragments, whose metal *d*-based molecular orbitals (MOs) indicate stabilizing *d-d* bonding between Rh-Cr.



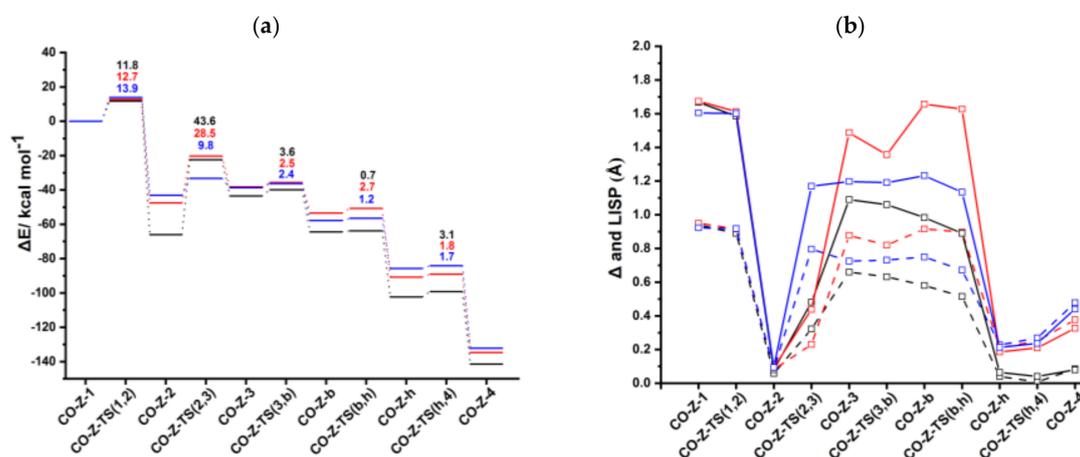
**Figure 5.** HOMO-3 of syn-Ind-1; the isodensity value is 0.03.

### 2.3. Acetylene [2+2+2] Cycloaddition Catalyzed by Anti-[Cr(CO)<sub>3</sub>IndRh] Fragment: Reaction Mechanism and PES (Path II)

According to the alternative mechanistic path by Booth et al. [26], an ancillary ligand of the catalyst precursor remains bonded to rhodium during the catalytic cycle; this mechanism is denoted Path II (Scheme 3b). For CpRh(CO) and IndRh(CO), this path has been thoroughly explored, making it possible to give an interpretation of the higher efficiency of the indenyl catalyst observed in the experiment [35]. Thus, here we considered the same hypothesis for anti-IndRh(CO) catalyzed acetylene [2+2+2] cycloaddition. The structures of the intermediates and transition states found on the PES with their relevant parameters are in Figures S5–S7. The energy profile of the process is shown in Figure 6a.

**CO-anti-Ind-1** is characterized by  $\eta^1$  coordination which is due to the presence of two acetylenes and the CO ligand, as observed for CpRh(CO) and IndRh(CO) catalysis [43].  $\Delta$  and LISP values are 0.92 Å and 1.60 Å, respectively (Figure 6b). The initial oxidative coupling leads to the formation of **CO-anti-Ind-2**, in which rhodium is coordinatively saturated due to the presence of CO. The energy barrier required to cross **CO-anti-Ind-TS (1,2)** is 13.9 kcal mol<sup>-1</sup> slightly higher if compared to those computed for CpRh(CO) and IndRh(CO) catalysis (by about 1–2 kcal mol<sup>-1</sup>). This is the same energy trend observed along Path I. The conversion of **CO-anti-Ind-1** into **CO-anti-Ind-2** is accompanied by the hapticity change from  $\eta^1$  to distorted  $\eta^5$  and is exothermic by 43.1 kcal mol<sup>-1</sup> (Figure 6a), 4.5 kcal mol<sup>-1</sup> and 23.0 kcal mol<sup>-1</sup> less than the analogous step in IndRh(CO) and CpRh(CO) catalysis, respectively. The addition of the third acetylene leads to the formation of the  $\eta^1$  **CO-anti-Ind-3** with an activation energy of 9.8 kcal mol<sup>-1</sup>. The barriers for this step are much higher in the cases of IndRh(CO) and CpRh(CO) catalysis, i.e., 28.5 and 43.6 kcal mol<sup>-1</sup>, respectively. Thus, this step is kinetically favored with the bimetallic anti-IndRh(CO). In addition, the formation of **CO-anti-Ind-3** is endothermic by 4.4 kcal mol<sup>-1</sup>, that is overall less endothermic if compared to the same step in IndRh(CO) and

CpRh(CO) catalysis, for which  $9.3 \text{ kcal mol}^{-1}$  and  $22.5 \text{ kcal mol}^{-1}$  are computed, respectively. Thus, the bimetallic catalyst has also a thermodynamic advantage. In the next step, the activation energy of  $2.4 \text{ kcal mol}^{-1}$  is necessary to cross **CO-anti-Ind-TS (3,b)** and generate the bicyclic intermediate **CO-anti-Ind-b** (Figure S7), with negligible difference from the IndRh(CO) catalyzed step and lower by  $1.2 \text{ kcal mol}^{-1}$  than in CpRh(CO) catalyzed step. The formation of **CO-anti-Ind-b** is accompanied by the release of  $19.1 \text{ kcal mol}^{-1}$ , being  $3.8 \text{ kcal mol}^{-1}$  more exothermic than the formation of the parent **CO-Ind-b** but  $1.8 \text{ kcal mol}^{-1}$  less exothermic than **CO-Cp-b**. One can notice that the bicyclic intermediate in CpRh(CO) catalysis has a higher energy while in bimetallic anti-IndRh(CO) and IndRh(CO) catalysis it lies at a lower energy (Figure 6a), suggesting a better catalytic efficiency in these latter cases. By crossing a modest barrier of  $1.2 \text{ kcal mol}^{-1}$ , the bicyclic **CO-anti-Ind-b** readily transforms into the heptacyclic intermediate **CO-Ind-h**; this step is accompanied by the haptotropic shift  $\eta^1 \rightarrow$  distorted  $\eta^5$  and by the release of  $28.0 \text{ kcal mol}^{-1}$ , a value lower than those computed for the parent catalysts, i.e.,  $-37.4 \text{ kcal mol}^{-1}$  in the case of IndRh(CO) and  $-37.8 \text{ kcal mol}^{-1}$  in the case of CpRh(CO), respectively. **CO-anti-Ind-h** undergoes reductive elimination with an activation energy of  $1.7 \text{ kcal mol}^{-1}$ . **CO-anti-Ind-4** forms and  $46.4 \text{ kcal mol}^{-1}$  are released. Finally, benzene is cleaved from **CO-anti-Ind-4** by stepwise addition of two acetylene molecules and the catalyst is regenerated.



**Figure 6.** (a) Energy profiles of acetylene [2+2+2] cycloaddition to benzene catalyzed by CpRh(CO) (black), IndRh(CO) (red), and anti-IndRh(CO) (blue) (Scheme 3b, Path II). (b) Profiles of the slippage parameters  $\Delta$  (dashed line) and LISP (solid line) along the acetylene [2+2+2] cycloaddition cycles catalyzed by CpRh(CO) (black), IndRh(CO) (red), and anti-IndRh(CO) (blue) (Scheme 3b, Path II). Level of theory: ZORA-BLYP/TZ2P.

With the formation of the 18-electron intermediate **CO-Z-2**, a rather flat portion of the PES begins (Figure 6a). ASA was carried out on **CO-Z-2** considering CO-Cp'Rh (Cp' = Cp, Ind and anti-[Cr(CO)<sub>3</sub>Ind]) and the C<sub>4</sub>H<sub>4</sub> moiety as fragments; the results are listed in Table 5. The similar strain in fragment C<sub>4</sub>H<sub>4</sub> computed for **CO-Cp-2**, **CO-Ind-2**, and **CO-anti-Ind-2** (Table 5) revealed that the structure of this moiety is very similar in the three catalysts (see also Figures S5–S7). The strain contribution of the fragment CO-Cp'Rh is much higher in **CO-anti-Ind-2** and **CO-Ind-2** than in **CO-Cp-2**. This is related to the least slippage predicted for this last species. The stronger interaction  $\Delta E_{\text{int}}$  in **CO-Ind-2** and **CO-anti-Ind-2** does not counterbalance their strain term and thus **CO-Cp-2** results the most stabilized among the three.

**Table 5.** Activation strain analysis (ASA) of **CO-Cp-2**, **CO-Ind-2**, and **CO-anti-Ind-2**; all values are in kcal mol<sup>-1</sup>. The fragments are: CO-Cp'Rh (Cp' = Cp, Ind, and anti-[Cr(CO)<sub>3</sub>Ind]) and the C<sub>4</sub>H<sub>4</sub> moiety (the reference are two acetylene molecules).

	$\Delta E_{\text{strain}}$			$\Delta E_{\text{int}}$	$\Delta E$
	C <sub>4</sub> H <sub>4</sub>	CO-Cp'RhL <sub>n</sub>	Total		
<b>CO-Cp-2</b>	50.63	6.08	56.71	-138.15	-81.44
<b>CO-Ind-2</b>	50.96	34.04	85.00	-153.65	-68.65
<b>CO-anti-Ind-2</b>	50.89	36.06	86.95	-149.23	-62.28

In the subsequent step, i.e., the addition of third acetylene to the 18-electrons rhodacycle **CO-Z-2**, an energy barrier is found along the catalytic Path II (Figure 6a). **CO-Z-TS (2,3)** was divided into two fragments, i.e., CO-Cp'Rh(C<sub>4</sub>H<sub>4</sub>) (Cp' = Cp, Ind and anti-[Cr(CO)<sub>3</sub>Ind]) and acetylene and ASA was performed. The results are shown in Table 6. The acetylene in all cases is only slightly deformed, whereas CO-Cp'Rh(C<sub>4</sub>H<sub>4</sub>) is highly strained.

**Table 6.** Activation strain analysis (ASA) of the transition states **CO-Cp-TS (2,3)**, **CO-Ind-TS (2,3)** and **CO-anti-Ind-TS (2,3)**; all values are in kcal mol<sup>-1</sup>. The fragments are CO-Cp'RhL<sub>n</sub> (Cp' = Cp, Ind, and anti-[Cr(CO)<sub>3</sub>Ind]) and acetylene.

	$\Delta E_{\text{strain}}$			$\Delta E_{\text{int}}$	$\Delta E$
	C <sub>2</sub> H <sub>2</sub>	CO-Cp'RhL <sub>n</sub>	Total		
<b>CO-Cp-TS (2,3)</b>	0.18	43.96	44.14	-0.50	43.64
<b>CO-Ind-TS (2,3)</b>	0.06	28.83	28.89	-0.34	28.55
<b>CO-anti-Ind-TS (2,3)</b>	0.12	14.27	14.39	-4.58	9.81

To summarize, we found that most of the steps are kinetically as well as thermodynamically more favored in the bimetallic anti-IndRh(CO) catalysis. At a glance, this can be seen also from the energy profile (Figure 6a), which is flatter in the case of anti-IndRh(CO) than in the parent IndRh(CO) and CpRh(CO) catalyzed processes. Alternatively, the slippage variations quantified with  $\Delta$  and LISP (Figure 6b) are less pronounced in anti-IndRh(CO) than those computed for the parent monometallic catalysts. Thus, the smaller slippage variations and the flatter potential energy profile of the bimetallic anti-IndRh(CO) suggest an higher catalytic efficiency than the monometallic IndRh(CO) and CpRh(CO), which is consistent with the experimental findings [26]. The phenomena of *indenyl effect* for IndRh and *extra-indenyl effect* for the bimetallic anti-IndRh can be fully explained when considering the mechanism of path II.

Notably, path II has been excluded for syn-IndRh(CO) because in this particular case the rhodium center would be too much crowded.

### 3. Discussion

To quantify the catalytic efficiency, we calculated the turnover frequencies (TOFs) for the studied catalytic cycles by using the energy span model [23,55]. Calculations were run at standard room temperature (298.15 K), as well as at the reflux temperature of toluene, i.e., 383.65 K, which is occasionally used in alkyne [2+2+2] cycloadditions as solvent [25,26,29]; the values are listed in Table 7.

Following the catalytic Path I (Scheme 3a), the TOFs are in the order CpRh > IndRh > anti-IndRh, suggesting that the bimetallic catalyst anti-IndRh is worse than the monometallic parent catalysts IndRh and CpRh. This is in contrast with the experimental results [36]. Also, no appreciable difference in terms of TOF is found between IndRh and anti-IndRh, suggesting that the influence of the second metal group, i.e., Cr(CO)<sub>3</sub>, on the efficiency of the catalyst is negligible. In all these cases, the TOF determining intermediate (TDI) is the bis-acetylene intermediate **Z-1** and the TOF determining transition state (TDTS) is the subsequent transition state **Z-TS (1,2)** (Figure 2a).

Conversely, along the catalytic Path II (Scheme 3b), in terms of TOF, a significant enhancement of the catalytic activity of the bimetallic anti-IndRh(CO) is found compared to those of the parent catalysts IndRh(CO) and CpRh(CO). On the basis of the TOF values reported in Table 7, the following trend can be established anti-IndRh(CO) > IndRh(CO) > CpRh(CO), which is consistent with the experimental observation [26]. In this case, the intermediate **CO-Z-2** is the TDI and the subsequent transition state **CO-Z-TS (2,3)** is the TDTS (Figure 6a). We can thus confirm that the coordination of Cr(CO)<sub>3</sub> favors the catalytic activity.

As recently reported [22], the slippage variations in intermediates and transition states along the catalytic cycle may be related to the chemical activity of the half-metallocene catalysts in this class of reactions. For this purpose, the slippage span  $\Delta\text{LISP}^*$  was calculated. Along Path I (Scheme 3a),  $\Delta\text{LISP}^*$  values follow the trend anti-IndRh > IndRh > CpRh. Since TOFs' trend is reverse, i.e., anti-IndRh < IndRh < CpRh, this indicates that the higher the slippage span along the catalytic cycle is, the lower the performance of the catalyst is [22]. When following Path II,  $\Delta\text{LISP}^*$  values follow the trend anti-IndRh(CO) < IndRh(CO) < CpRh(CO), while TOFs follow the reverse trend anti-IndRh(CO) > IndRh(CO) > CpRh(CO), in agreement with the presence of extra indenyl and indenyl effect in the bimetallic and monometallic Ind catalysts, respectively.

The mechanism for syn-IndRh catalyzed acetylene [2+2+2] cycloaddition is different, and so we cannot directly compare the TOF values. However, the higher energy barriers and higher slippage variations certainly do not favor the syn catalyst.

**Table 7.** Calculated TOF (s<sup>-1</sup>) and slippage span  $\Delta\text{LISP}^*$  (Å) for the catalytic Path I and II of the [2+2+2] cycloaddition of acetylene to benzene.

	TOF <sub>298.15 K</sub> (s <sup>-1</sup> )	Ratio <sub>298.15 K</sub>	TOF <sub>383.65 K</sub> (s <sup>-1</sup> )	Ratio <sub>383.65 K</sub>	$\Delta\text{LISP}^*$ (Å)
<i>Path I</i>					
<b>CpRh</b>	$4.83 \times 10^3$	$1.82 \times 10^2$	$6.66 \times 10^5$	$5.79 \times 10^1$	0.85
<b>IndRh</b>	$5.23 \times 10$	1.97	$2.00 \times 10^4$	1.74	1.75
<b>anti-IndRh</b>	$2.66 \times 10$	1	$1.15 \times 10^4$	1	1.81
<b>syn-IndRh</b>	$4.57 \times 10$	–	$1.78 \times 10^4$	–	3.42
<i>Path II</i>					
<b>CpRh(CO)</b>	$6.10 \times 10^{-20}$	1	$1.07 \times 10^{-12}$	1	15.59
<b>IndRh(CO)</b>	$6.41 \times 10^{-8}$	$1.05 \times 10^{12}$	$2.35 \times 10^{-3}$	$2.20 \times 10^9$	14.11
<b>anti-IndRh(CO)</b>	$3.97 \times 10^2$	$6.51 \times 10^{21}$	$9.55 \times 10^4$	$8.93 \times 10^{16}$	10.54

#### 4. Materials and Methods

All the equilibrium and transition state geometries were fully optimized (i.e., without any constraint) in gas-phase using density functional theory (DFT) approach as implemented in the Amsterdam Density Functional (ADF 2016, SCM, Vrije Universiteit: Amsterdam, The Netherlands, 2016) program [56,57]. The BLYP [58–61] function in combination with the TZ2P basis set was applied for all elements. The scalar relativistic effects were accounted for within the zeroth-order regular approximation (ZORA), which is an excellent approximation of the relativistic Dirac equation [62–64]. The TZ2P basis set [65] is a large uncontracted set of Slater-type orbitals (STOs) of triple- $\zeta$  quality and has been augmented with two sets of polarization functions on each atom: 2p and 3d for H, 3d, and 4f for C and O, 4p and 4f for Cr, and 5p and 4f for Rh. The frozen-core approximation was adopted for core electrons: up to 1s for C and O, up to 2p for Cr and up to 3d for Rh. This level of theory has been applied with success in previous studies [22,41–44,49].

Frequency calculations were computed to confirm that all the intermediates have positive frequencies, whereas the transition states have one imaginary frequency. The character of the normal mode associated with this imaginary frequency was carefully examined to verify that the correct transition state was found.

Activation strain analyses (ASA) were performed on selected geometries [66,67]. ASA is an approach based on molecule fragmentation, useful to understand the properties of the chemical

bonding. For this purpose, the total energy of a complex can be decomposed as the sum of a strain contribution ( $\Delta E_{\text{strain}}$ ) and an interaction contribution ( $\Delta E_{\text{int}}$ ) (Equation (5)):

$$\Delta E = \Delta E_{\text{strain}} + \Delta E_{\text{int}} \quad (5)$$

$\Delta E_{\text{strain}}$  is the energy required for the geometrical deformation of the fragments when they are brought from infinite distance to the geometry they acquire in the complex, while  $\Delta E_{\text{int}}$  is the actual energy change when the deformed fragments are combined to form the overall complex.  $\Delta E_{\text{int}}$  can be further decomposed into electrostatic interaction ( $\Delta V_{\text{elstat}}$ ), Pauli repulsion ( $\Delta E_{\text{Pauli}}$ ) and orbital interactions ( $\Delta E_{\text{oi}}$ ) in the framework of Kohn-Sham molecular orbital (MO) theory (Equation (6)):

$$\Delta E_{\text{int}} = \Delta V_{\text{elstat}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{oi}} \quad (6)$$

According to Fernandez et al. [53], who proposed an extension to the activation strain model for unimolecular reaction steps, the activation barrier can be given as the change, upon going from the reactant to the TS, in strain within the two defined fragments plus the change, upon going from the reactant to the TS, in the interaction between the same two fragments:

$$\Delta E^\ddagger = \Delta \Delta E_{\text{strain}} + \Delta \Delta E_{\text{int}} \quad (7)$$

This situation is encountered in the present study, when the five-membered rhodacycle is formed from the bis-acetylene precursor.

The turnover frequency (TOF) was calculated by using the energy span model proposed by Kozuch and Shaik [23,55]. The expression is:

$$\text{TOF} = \frac{k_B T}{h} \frac{e^{-\frac{\Delta G_r}{RT}} - 1}{\sum_{i,j=1}^N e^{(T_i - I_j - \delta G_{i,j})/RT}} \quad (8)$$

where  $\Delta G_r$  is reaction Gibbs free energy,  $T_i$  and  $I_j$  are Gibbs free energies of the  $i$ th transition state and intermediate, respectively.  $\delta G_{i,j}$ , called the energy span, is equal to  $\Delta G_r$  if  $i > j$  or to 0 if  $i \leq j$ . Instead of Gibbs free energies, electronic energies were used, as it was demonstrated that there are no significant differences in the energy profiles and corresponding TOF ratios for analogous catalytic cycles [44].

## 5. Conclusions

We performed a theoretical investigation of the bimetallic system  $[\text{Cr}(\text{CO})_3\text{IndRh}]$ -mediated [2+2+2] cycloaddition of acetylene to benzene. Through a detailed exploration of the potential energy surfaces (PESs), the intermediates and transition states were located using density functional theory (DFT) methods following two mechanistic paths, i.e., Path I and II (Scheme 3a,b). The bimetallic catalysts anti- and syn- $[\text{Cr}(\text{CO})_3\text{IndRh}]$  were tested in silico and compared to the monometallic parent catalysts CpRh and IndRh. The anti or syn coordination of  $\text{Cr}(\text{CO})_3$  affects the energetics of the cycle and also to the mechanism. The reaction energies and barriers, the turn over frequency (TOF) and the change of the slippage parameters along the catalytic cycles are discussed.

Considering Path I, the established trend for the slippage span  $\Delta \text{LISP}^*$  is anti-IndRh > IndRh > CpRh while TOF values follow the opposite order, i.e., CpRh > IndRh > anti-IndRh. This leads to the conclusion that the lower slippage span along the catalytic cycle, the higher the catalytic performance. In any case, this does not explain the highest catalytic efficiency of the bimetallic Rh/Cr compound (*extra-indenyl effect*).

Conversely, if we follow the catalytic cycle along Path II, a dramatic TOF enhancement of the bimetallic system anti-IndRh(CO) relative to the parent CpRh(CO) and IndRh(CO) is found. On the basis of the TOF, the following trend of catalytic efficiency can be established anti-IndRh(CO) > IndRh(CO) > CpRh(CO), in agreement with experimental findings. In this case, the slippage span is

inverted, too, i.e.,  $\text{CpRh}(\text{CO}) > \text{IndRh}(\text{CO}) > \text{anti-IndRh}(\text{CO})$ , which again leads us to conclude that the lower the slippage span is, the higher the catalytic efficiency is. We can thus conclude that the coordination of  $\text{Cr}(\text{CO})_3$  in the bimetallic indenyl catalyst improves the efficiency along Path II.

The hapticity variations of intermediates and transition states along the catalytic cycle are highly pronounced in the syn bimetallic conformer, implying low TOF values and leading to the conclusion that the syn- $[\text{Cr}(\text{CO})_3\text{IndRh}]$  catalyzed process is not favored.

**Supplementary Materials:** The following are available online at <http://www.mdpi.com/2073-4344/9/8/679/s1>: Figure S1: Optimized geometries of anti- and syn- $[\text{Cr}(\text{CO})_3\text{IndRh}(\text{CO})_2]$ . Level of theory: ZORA-BLYP/TZ2P; Figure S2: Optimized structures with relevant geometric parameters, i.e., bond lengths (Å) and angles (deg) of the intermediates and transition states along Path (I) for acetylene [2+2+2] cycloaddition catalyzed by CpRh fragment; Figure S3: Optimized structures with relevant geometric parameters, i.e., bond lengths (Å) and angles (deg) of the intermediates and transition states along Path (I) for acetylene [2+2+2] cycloaddition catalyzed by IndRh fragment; Figure S4: Optimized structures with relevant geometric parameters, i.e., bond lengths (Å) and angles (deg) of the intermediates and transition states along Path (I) for acetylene [2+2+2] cycloaddition catalyzed by syn-IndRh fragment; Figure S5: Optimized structures with relevant geometric parameters, i.e., bond lengths (Å) and angles (deg) of the intermediates and transition states along Path (II) for acetylene [2+2+2] cycloaddition catalyzed by CpRh(CO) fragment; Figure S6: Optimized structures with relevant geometric parameters, i.e., bond lengths (Å) and angles (deg) of the intermediates and transition states along Path (II) for acetylene [2+2+2] cycloaddition catalyzed by IndRh(CO) fragment; Figure S7: Optimized structures with relevant geometric parameters, i.e., bond lengths (Å) and angles (deg) of the intermediates and transition states along Path (II) for acetylene [2+2+2] cycloaddition catalyzed by anti-IndRh(CO) fragment, Table S1: Selected geometric parameters of the anti- and syn- $[\text{Cr}(\text{CO})_3\text{IndRh}(\text{CO})_2]$ , computed at ZORA-BLYP/TZ2P level of theory, Table S2: Cartesian coordinates (in Å) and ADF total energies (in kcal mol<sup>-1</sup>) of all the intermediates and the transition states along Path I catalyzed by anti- $[\text{Cr}(\text{CO})_3\text{IndRh}]$  fragment, computed at ZORA-BLYP/TZ2P level of theory, Table S3: Cartesian coordinates (in Å) and ADF total energies (in kcal mol<sup>-1</sup>) of all the intermediates and the transition states along Path I catalyzed by syn- $[\text{Cr}(\text{CO})_3\text{IndRh}]$  fragment, computed at ZORA-BLYP/TZ2P level of theory, Table S4: Cartesian coordinates (in Å) and ADF total energies (in kcal mol<sup>-1</sup>) of all the intermediates and the transition states along Path I catalyzed by anti- $[\text{Cr}(\text{CO})_3\text{IndRh}]$  fragment, computed at ZORA-BLYP/TZ2P level of theory.

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