

Article

Designing Power Transformer Using Particle Swarm Optimization with Respect to Transformer Noise, Weight, and Losses

Wahyudi Budi Pramono ^{1,2,*} , Fransisco Danang Wijaya ^{1,*} , Sasongko Pramono Hadi ¹ ,
Moh. Slamet Wahyudi ³ and Agus Indarto ⁴

¹ Department of Electrical and Information Engineering, Universitas Gadjah Mada Yogyakarta, Yogyakarta 55281, Indonesia

² Department of Electrical Engineering, Universitas Islam Indonesia Yogyakarta, Yogyakarta 55584, Indonesia

³ Elsewedy Electric Indonesia, Bogor Regency 16820, Indonesia

⁴ Faculty of Electricity and Renewable Energy, Institute of Technology PLN, Jakarta 11750, Indonesia

* Correspondence: wahyudi_budi_p@uii.ac.id (W.B.P.); danangwijaya@ugm.ac.id (F.D.W.)

Abstract: The increased use of electrical energy will encourage the installation of more power transformers in residential areas as well as in industrial areas. Each power transformer, in its operation, will generate noise that can interfere with comfort and, at some level, cause health problems. The design of the power transformer currently focuses on optimizing its economic side, so noise has not been considered at this design stage. This research is about optimizing the low noise transformer design. The main goal is to obtain a low noise power transformer with low production costs. The method used in this optimization is particle swarm optimization with a multi-objective function. The objective function consists of the minimization of load noise, core weight, and winding weight. In this study, 11 optimized variables were used. Some variables that are optimized must be in the form of integers. Therefore, the optimization process needs a mechanism for mapping variables. The results showed that a low noise power transformer could be designed at optimal cost. Design validation was performed analytically and numerically with COMSOL software. The optimization results showed a decrease in load noise, core, and winding weight by 0.86 dB, 2.12%, and 47.46%, respectively. The results of this optimization are better than the designs used regularly in the industry.

Keywords: load noise; transformer; optimization; particle swarm optimization; design



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1. Introduction

A power transformer is an essential tool in the electric power system. The power transformer is a static electrical device consisting of one, two, or more windings coupled with or without a magnetic core to connect electrical circuits [1]. The primary role of these devices is to transmit electrical energy from one voltage level to another without changing the frequency [2,3].

The increasing demand for electrical energy will encourage the installation of more power transformers in residential areas [4] and industrial environments. Each power transformer, in operation, will generate noise in the form of a sound or buzzing sound [5], which will change based on the size of the load. Noise is unwanted sound from a business or activity at a certain level and time that can cause disturbances to human health and environmental comfort [6]. The noise level standard is the maximum level of noise allowed to be discharged into the environment from a business or activity so that it does not cause human health problems and environmental discomfort [6]. Public awareness of environmental issues has been highlighted [7] and must be considered by energy providers and power transformer companies that use and produce power transformers with low noise [8,9].

The primary noise sources from a power transformer are the magnetic core, windings [5,8], and the cooling system [7,10,11]. Noise originating from the core of the power transformer is caused by the Maxwell force [12,13] and magnetostriction [5,10,12], which is the change in the shape of the core material due to exposure to changing magnetic flux [10]. The noise frequency generated from this magnetostriction process is twice the source frequency. The non-linear nature of the magnetostriction causes higher even-order harmonics to appear as a result of core vibrations [11]. The noise from the windings is caused by the interaction between the current flowing in the windings and the leaky flux that hits it, causing the Lorentz force [11,14]. The noise caused by the transformer windings due to the load current is called load noise. No-load noise is a summation of noise caused by the transformer core and the cooling system. Meanwhile, total noise is a combination of all noise components generated, namely no-load noise, load noise, and noise from the cooling device.

Optimizing any power transformer design is a complex task because it must meet the standards and specifications set by consumers to keep production costs low. The development of modern transformers has led to smaller dimensions and cheaper production costs while maintaining high energy efficiency. The main objective in power transformer design optimization is to obtain the lowest production costs (material, labor, and overhead costs) [15] and the lowest total loss and owning costs [16,17] while maintaining the highest technical specifications. The design methodology will depend on the type of transformer (distribution, power or instrumentation), its operation frequency, the core construction's characteristics, the cooling method or the type of magnetic material [18].

Aspects considered in transformer design include [19]: no-load loss, load loss, short circuit impedance, inrush current, dynamic behavior when a short circuit occurs, noise, isolation, and cooling system. So far, the design of the transformer has focused more on optimizing production costs by minimizing material costs without leaving the desired loss limit in designing power transformers.

Aspect load noise is rarely considered in power transformer designs. The problem occurs when the load noise generated by the power transformer exceeds the specifications determined by the consumer. Efforts to reduce load noise by adding dampers will increase production costs, dimensions, and weight of transformers.

Therefore, in this study, a power transformer design optimization method is proposed by including the load noise aspect as one of the objective functions, in addition to the material core and winding weight. The optimization method uses particle swarm optimization (PSO) by modifying the optimized variable mapping process. The PSO method is a method that is easy to implement and quick to get a solution.

2. Materials and Methods

The design of the power transformer includes the design of the core, the design of windings on the low-voltage side and the high-voltage side, the design of tanks and the design of cooling systems. An essential part of the design's focus is the core and winding designs. This focus is because the highest cost of the material comes from the core and winding. In this study, the steps and equations in the design of power transformers are based on [18].

2.1. The Core Design

The core in a three-phase power transformer usually has three limbs and two yokes. Within this core are laid high-voltage and low-voltage windings, and the yokes serve as a pathway for the flow of magnetic flux. The limbs for power transformers are usually arranged in a step-like pattern to get a nearly circular shape for the lowest possible regression. The number of steps is determined based on the amount of power from the transformer, which is proportional to the gross section area of the transformer core. The basic dimensions of the transformer core are the diameter of the limbs, the window's height

and width, the distance between the centers of the limb, the height of the yoke and the cross-sectional area of the limbs and yokes.

The phase voltage per turn of the winding is defined by (1). Meanwhile, the cross-sectional area of the limb and the relationship between the phase voltage per turn, frequency, and density of maximum magnetic flux is specified by (2).

$$E_t = K_t \sqrt{S} \tag{1}$$

$$A_c = \frac{E_t}{4.44 f B_m} \tag{2}$$

A constant value of the turns ratio (K_t) for a three-phase power transformer is between 0.4 and 0.7. The diameter of the core is expressed by (3).

$$d_c = 2K_s \sqrt{\frac{A_c}{\pi}} \tag{3}$$

The value of the space factor, K_s , usually has a value of 0.9.

2.2. Low Voltage (LV) Winding Design

The number of turns in LV winding (N_{LV}) compares phase voltage to voltage per turn, expressed by (4).

$$N_{LV} = \frac{V_{LV}}{E_t} \tag{4}$$

while the phase current on LV winding (I_{LV}) for delta connection is expressed by (5).

$$I_{LV} = \frac{S}{3 V_{LV}} \tag{5}$$

The cross-sectional area per turn for LV winding (A_{LV}) is determined by (6).

$$A_{LV} = \frac{I_{LV}}{\delta_{LV}} \tag{6}$$

with δ_{LV} as the current density of LV winding. Overall LV winding width (w_{LV}) is defined by (7).

$$w_{LV} = w_{LV1} \times n_{RLV} \times n_{LDLV} \tag{7}$$

with w_{LV1} as the thickness of one LV winding conductor with its insulation, n_{RLV} as the number of LV winding conductors radially per turn, and n_{LDLV} as the number of turns per disk for LV winding. The height of LV winding can be derived from (8).

$$h_{LV} = ((h_{LV1} + d_{DLV}) \times n_{DLV}) - d_{DLV} \tag{8}$$

with h_{LV1} as the height of one disk of LV winding (consisting of more than one axially arranged conductor) with its insulation, d_{DLV} distance between disks axially, n_{DLV} as the number of LV winding disks. LV winding consists of several parallel conductors to reduce eddy loss. The thickness and width of each conductor must withstand the force caused by a short circuit and keep the disk in a stable condition.

2.3. High Voltage (HV) Winding Design

In the same way, the HV winding parameter can be determined by (9) to (14), starting from the current per phase (I_{HV}) (star connection), the number of turns in HV winding (N_{HV}), cross-sectional area per turn for HV winding (A_{HV}), the width of HV winding (w_{HV}), and height of HV winding (h_{HV}).

$$I_{HV} = \frac{S}{V_{HV} \sqrt{3}} \tag{9}$$

$$N_{HV} = \frac{V_{HV}}{E_t \sqrt{3}} \tag{10}$$

$$A_{HV} = w_{HV1} \times t_{HV} \times n_{RHV} \times n_{AHV} \tag{11}$$

$$\delta_{HV} = \frac{I_{HV}}{A_{HV}} \tag{12}$$

$$w_{HV} = w_{HV1} \times n_{RHV} \times n_{LDHV} \tag{13}$$

$$h_{HV} = ((h_{HV1} + d_{DHV}) \times n_{DHV}) - d_{DHV} \tag{14}$$

with δ_{HV} as the current density of HV winding, w_{HV1} as the thickness of one HV winding conductor with its insulation, t_{HV} as the width of one HV winding conductor, n_{RHV} as the number of HV winding conductors radially per turn and n_{LDHV} as the number of turns per disk for HV winding, h_{HV1} as the height of one turn of HV winding (may consist of more than one axially arranged conductor) with its insulation, d_{DHV} distance between disks axially, n_{DHV} as the number of HV winding disks.

The height of HV winding is not much different from that of LV winding to maintain magnetic balance in the winding. Therefore, determining the number of disks and turns per disk needs to be optimized while meeting the minimum distance between disks. In addition, the size of the conductor, the number of parallels per turn, and the number of the conductor's radial and axial directions must meet optimal conditions and stay within the predetermined restraints.

2.4. The Dimension of Winding and Core

Distance between the outer core and inner LV winding (d_{CLV}), the distance between LV winding and HV winding (d_{LV-HV}), and the distance between HV winding and HV winding in other phases (d_{F-F}) must meet the minimum distance based on the voltage at nominal frequency. Equations (15) to (18) determine the winding dimensions.

$$ID_{LV} = d_c + 2d_{CLV} \tag{15}$$

$$OD_{LV} = ID_{LV} + 2w_{LV} \tag{16}$$

$$ID_{HV} = OD_{LV} + 2d_{LV-HV} \tag{17}$$

$$OD_{HV} = ID_{HV} + 2w_{HV} \tag{18}$$

ID_{LV} and ID_{HV} are the inner diameters of LV winding and HV winding, OD_{LV} and OD_{HV} are the outer diameters of LV winding and HV winding.

The core dimensions are expressed from (19) to (21). The dimensions of the core depend on the dimensions of the winding.

$$d_{C-C} = OD_{HV} + d_{F-F} \tag{19}$$

$$h_w = h_{LV} + d_{TC} + d_{BC} \tag{20}$$

$$w_w = d_{C-C} - d_c \tag{21}$$

with h_w being window height, d_{TC} and d_{BC} being the distance between the top and bottom of the LV winding against the upper and lower yoke, w_w being the width of the window and (d_{C-C}) being the distance between the centre of limbs.

2.5. The Mass of The Power Transformer Core and Winding

2.5.1. The Mass of The Power Transformer Core

The limb and yoke's diameters are assumed equal, so the core's total length (l_C) is indicated by (22).

$$l_C = 4d_{C-C} + 3h_w + 2d_c \tag{22}$$

Equations (23) and (24) are the total volume of the core (Vol_C) and overall core weight (W_C).

$$Vol_C = l_C A_c \tag{23}$$

$$W_C = Vol_C G_c \tag{24}$$

with G_c being the weight of the core material per volume.

2.5.2. The Mass of The Power Transformer Winding

Equations (25) to (28) are the volume and weight of LV and HV winding.

$$Vol_{LV} = \pi N_{LV} A_{LV} \left(\frac{ID_{LV} + OD_{LV}}{2} \right) \tag{25}$$

$$Vol_{HV} = \pi N_{HV} A_{HV} \left(\frac{ID_{HV} + OD_{HV}}{2} \right) \tag{26}$$

$$W_{LV} = Vol_{LV} G_w \tag{27}$$

$$W_{HV} = Vol_{HV} G_w \tag{28}$$

with G_w is the weight of the winding material per volume.

2.6. Impedance

The variable (A) is the cross-sectional area of the winding passed by flux. The dimensions of the winding strongly influence the impedance of the transformer. The impedance magnitude can be derived from (29) to (36).

$$A = \pi(A1 + A2 + A3) \tag{29}$$

with

$$A1 = \frac{w_{LV}}{3} \left(\frac{ID_{LV} + OD_{LV}}{2} \right) \tag{30}$$

$$A2 = d_{LV-HV} \left(\frac{OD_{LV} + ID_{HV}}{2} \right) \tag{31}$$

$$A3 = \frac{w_{HV}}{3} \left(\frac{ID_{HV} + OD_{HV}}{2} \right) \tag{32}$$

The magnitude of leaking inductance (L) is based on the high voltage side expressed by (33).

$$L = \frac{\mu N_{HV}^2 A}{l_{ef}} \tag{33}$$

with

$$l_{ef} = \frac{h_{LV}}{K_R} \tag{34}$$

and

$$K_R = 1 - \frac{1 - e^{\frac{-\pi h_w}{(w_{LV} + d_{LV-HV} + w_{HV})}}}{\frac{\pi h_w}{(w_{LV} + d_{LV-HV} + w_{HV})}} \tag{35}$$

Value per unit of reactance when based on the HV side (X_{pu}) indicated by (36). The resistance part of the impedance is usually of little value when compared to its reactance part. Therefore, the impedance of the power transformer is equal to the reactance value.

$$X_{pu} = 2\pi f L \frac{S}{(V_{HV})^2} \tag{36}$$

Resistance of LV winding, HV winding, and total resistance based on the high voltage side was derived from (37) to (39).

$$R_{LV} = \frac{3\rho\pi N_{LV} \left(\frac{ID_{LV} + OD_{LV}}{2} \right)}{A_{LV}} \quad (37)$$

$$R_{HV} = \frac{3\rho\pi N_{HV} \left(\frac{ID_{HV} + OD_{HV}}{2} \right)}{A_{HV}} \quad (38)$$

$$R = R_{HV} + R_{LV} \left(\frac{N_{HV}}{N_{LV}} \right)^2 \quad (39)$$

2.7. Losses in The Power Transformer

The no-load losses in the power transformer are due to hysteresis and parasitic current orthogonal to the main flux in the core. They are represented in (W/kg) according to the core material and the specific magnetic flux density in the limbs and yoke [20]. According to (41), losses in the core P_C are the sum of the specific losses in the limbs and yokes. There is a more significant loss in the core connections area, so the K_J factor as (41) is needed.

$$W_{CJ} = K_J W_C \quad (40)$$

$$P_C = (W_C - W_{CJ}) \times K_L + W_{CJ} \times K_L \times K_p \quad (41)$$

The losses in LV and HV windings are defined by (42) and (43).

$$PL_{LV} = I_{LV}^2 R_{LV} \quad (42)$$

$$PL_{HV} = I_{HV}^2 R_{HV} \quad (43)$$

with R_{LV} and R_{HV} are the resistance of the LV and HV windings.

Equations (44) to (47) are used to calculate eddy losses in LV winding (PE_{LV}) and HV winding (PE_{HV})

$$(PE_{LV})_{mean} = \frac{\omega^2 w_{LV1}^2 B_{gp}^2}{h_{LV}} \quad (44)$$

$$PE_{LV} = (PE_{LV})_{mean} \times Vol_{LV} \quad (45)$$

$$(PE_{HV})_{mean} = \frac{\omega^2 w_{HV1}^2 B_{gp}^2}{h_{HV}} \quad (46)$$

$$PE_{HV} = (PE_{HV})_{mean} \times Vol_{HV} \quad (47)$$

B_{gp} is the magnetic flux density peak in the LV and HV winding gap. Total load losses in the winding (PL_W) is expressed by (48).

$$PL_W = PL_{LV} + PE_{LV} + PL_{HV} + PE_{HV} \quad (48)$$

while stray losses in structural components, such as frames, and tank plates, are generally assumed to be 20% of the total load losses in the winding, that total load loss (PL) is expressed by (49).

$$PL = PL_w + 0.2PL_w \quad (49)$$

The total losses (P_T) and efficiency of the power transformer (η) are expressed by (50) and (51).

$$P_T = P_C + PL \quad (50)$$

$$\eta = \frac{S \times pf}{(S \times pf) + P_C + PL} \times 100 \quad (51)$$

2.8. The Power Transformer Noise

The primary sound source that causes the transformer’s noise is the core’s magnetostriction process [5,10,12], coil vibrations due to electromagnetic forces, tank walls, magnetic shunts, and cooling devices [7,10,11]. Noise caused by the magnetostriction process is often referred to as no-load noise, while noise caused by winding vibrations due to load current is called load noise.

There are several sources of noise generated in the transformer core. The two main components that should be suspected as being the sources of noise in the transformer core (when the transformer is at no load) are the Maxwell force and the magnetostriction process due to the characteristics of the magnetic core [12,13].

Recently, an experiment was conducted to determine the noise and vibration caused by magnetostriction [9,20–22]. The absence of a complete physical model hindered the analysis and quantification of these physical phenomena. Another way to determine noise and vibration from the core is by numerical modelling with the help of the finite element method (FEM) [10,17–19,23–27]. This method is often used to analyze the magnetostriction phenomenon in the transformer core by playing with the various variables of the core. Although this numerical method is considered to have advantages, it still requires computation time and is less flexible when changing the variables.

Another method transformer designers often use to obtain load noise predictive results is the equations from statistical data [7,28,29]. The advantages of this method are faster results and increased flexibility when playing with the variable values.

According to [30], the load noise (L_L) can be predicted by using an artificial neural network model with input in the form of comparison between the height and width of the winding (r_{hw}), log of the nominal power (S), the impedance (X_{pu}), and the weight of the LV and HV windings ($W_{LV} + W_{HV}$). The relationship of load noise to the input variable is presented in (52). Whereas according to [31], the no load noise (L_{NL}) can be calculated based on (53), where H_C is the height of the core and nl is the number of limbs.

$$L_L = f(S, X_{pu}, (W_{LV} + W_{HV}), r_{hw}) \tag{52}$$

$$L_{NL} = 9.63 \log(S) + 194.25 \log(B) + 44.13 \log\left(\frac{W_C}{A_C + H_C}\right) - 11.8(nl) + 148.24 \tag{53}$$

2.9. Formulation of Power Transformer Design Optimization Problem

The primary purpose of power transformer design optimization is to obtain a low-load noise power transformer design while minimizing core and winding material but with some restraints. These restraints are to meet consumer demands and standards.

2.9.1. Optimized Design Variables

In this study, 11 design variables will be optimized, namely, the K_t factor, the maximum magnetic flux density (B_m), the current density on LV winding (δ_{LV}), the number of conductors of LV winding radially ($n_{R_{LV}}$), the number of conductors of HV winding radially ($n_{R_{HV}}$), the number of conductors of LV winding axially ($n_{A_{LV}}$), the number of conductors of HV winding axially ($n_{A_{HV}}$), the conductor thickness for LV winding (w_{LV1}) and HV winding (w_{HV1}), the number of turns per disk for LV winding ($n_{LD_{LV}}$), and the number of turns per disk for HV winding ($n_{LD_{HV}}$).

The K_t factor and B_m directly influence the cross-sectional area of the core, so it will affect the dimensions and weight of the core. Furthermore, it will certainly affect the material cost of the core. While the current density in LV winding has a strong correlation to the size and dimensions of the winding, it will also affect the weight and cost of the winding material. At the same time, the current density in HV winding is one of the predetermined restraints. The dimensions of the conductor and the number of turns per disk will affect the dimensions of the winding. The dimensions of the winding based on (29) to (35) will affect the reactance of the transformer. However, load noise based on the

artificial neural network model strongly correlates to the power transformer’s weight of winding and reactance. Therefore, selecting 11 optimization variables is appropriate in determining the optimum design.

2.9.2. Objective Function (OF)

The primary purpose of this study is to design a low-load noise power transformer. Therefore, the objective function is to minimize the load noise and weight of the primary material. The equations (54) and (55) derive the OF equations from this study.

$$f_1 = \min L_L(C) \tag{54}$$

and

$$f_2 = \min(W_C + 2(W_{LV} + W_{HV})) \tag{55}$$

According to (55), the weight of the winding is twice as much as the weight of the core since the price of the winding material is twice as high.

2.9.3. Constraints

Minimization of f_1 and f_2 must meet the predetermined constraints. Equations (56) to (63) are constraints that must be appropriate in the transformer design.

$$lb_i \leq x_i \leq ub_i \tag{56}$$

$$X_{pu} - 0.075sX_{pu} < 0 \tag{57}$$

$$X_{pu} + 0.075sX_{pu} < 0 \tag{58}$$

$$1200 \leq h_{LV} \leq 2200 \tag{59}$$

$$8 \leq t_{LV} \leq 14 \tag{60}$$

$$8 \leq t_{HV} \leq 14 \tag{61}$$

$$3 \leq \delta_{HV} \leq 4 \tag{62}$$

$$L_{NL} - L_L < 0 \tag{63}$$

where sX_{pu} is a guaranteed reactance, t_{LV} and t_{HV} are the conductor width of LV and HV winding, L_{NL} is the no load noise and δ_{HV} is the current density of HV winding. At the same time, lb_i and ub_i are the lower and upper limits of the optimized variables. Table 1 is a type of optimized design variable along with its lower and upper bounds.

Table 1. The lower and upper bounds of the optimized design variables.

Variable	Lower Bound	Upper Bound	Unit
w_{LV1}	1	3	mm
$n_{R_{LV}}$	1	6	conductor
$n_{A_{LV}}$	1	2	conductor
$n_{LD_{LV}}$	6	12	turn
w_{HV1}	1	3	mm
δ_{LV}	3	4	A/mm ²
$n_{R_{HV}}$	1	6	conductor
$n_{A_{HV}}$	1	2	conductor
$n_{LD_{HV}}$	6	12	turn
B_m	1.4	1.7	T
K_t	0.4	0.7	-

2.10. Principle of Particle Swarm Optimization (PSO)

PSO is an optimization search algorithm based on swarm behavior. PSO is an algorithm based on population, exploiting the population to find potential solutions in the search space. The population is called a swarm, and the individual is called a particle [32].

$$S = \{x_1, x_2, x_3 \dots, x_N\} \tag{64}$$

$$x_i = (x_{i1}, x_{i2}, x_{i3} \dots, x_{iN})^T \in A \tag{65}$$

The objective function, $f(x)$, is assumed to be available for all points in space A , so each particle has a unique function value. The particles are assumed to move in search space A with velocity v_i .

$$v_i = (v_{i1}, v_{i2}, v_{i3} \dots, v_{iN})^T \quad i = 1, 2, \dots, N \tag{66}$$

The particle velocity is updated based on the information obtained from the previous step so that each particle can store the best position it has ever obtained. This velocity is adjusted interactively to allow the particle to find any point in space A . The last position of the i -th particle and its velocity, after the t -iteration, is denoted by $x_i(t)$ and $v_i(t)$.

The velocity and position of each particle can be shown as, (67) and (68):

$$v_{ij}(t + 1) = v_{ij}(t) + c_1 R_1 (p_{ij}(t) - x_{ij}(t)) + c_2 R_2 (p_{ij}(t) - x_{ij}(t)) \tag{67}$$

$$x_{ij}(t + 1) = x_{ij}(t) + v_{ij}(t + 1) \tag{68}$$

where R_1 and R_2 are random variables with normal distribution, c_1 and c_2 are weighting factors or cognitive and social parameters, and t is the number of iterations. After updating and evaluating the particles in each iteration, the best position of the particles will be updated. This algorithm has advantages such as a simple program, high-quality solution, and fast convergence [32].

Figure 1 explains that evaluating the particle’s fitness begins with mapping a particular variable into a specified range value. There are at least six variables that need to be mapped, namely the number of conductors of LV winding radially (n_{RLV}), the number of conductors of HV winding radially (n_{RHV}), the number of conductors of LV winding axially (n_{ALV}), the number of conductors of HV winding axially (n_{AHV}), the number of turns per disk for LV winding (n_{LDLV}), and the number of turns per disk for HV winding.

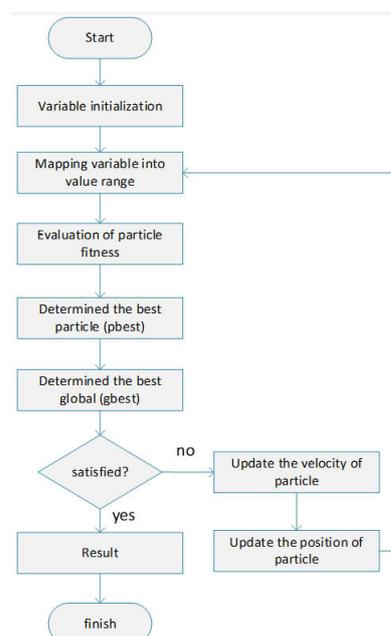


Figure 1. The flowchart of the PSO model.

2.11. Case Study

This design is applied to three-phase power transformers, with the specifications shown in Table 2.

Table 2. The power transformer specifications.

Parameter	Symbol	Value	Unit
Power	(S)	80	MVA
Frequency	(f)	50	Hz
Voltage of HV side	(V_{HV})	110	kV
Voltage of LV side	(V_{LV})	33	kV
Limbs		3	-
Phase		3	-
Impedance	(Z)	12	%

The restraints are used based on Equations (56) to(63), and the lower bounds and upper bounds of each optimized design variable are presented in Table 1. In contrast, the PSO parameters are shown in Table 3.

Table 3. The PSO parameters.

Parameter	Value
Number of particles	250
Number of optimized variables	11
Number of the maximum iteration	25
Cognitive parameter	2
Social parameter	4

3. Results

The results for optimization variables by the PSO method are presented in Table 4. All optimization variables are within predetermined limits.

Table 4. The result of optimized variables.

Variable	Value	Unit
w_{LV1}	1.67	(mm)
n_{RLV}	6	cond.
n_{ALV}	2	cond.
n_{LDLV}	6	Turn
w_{HV1}	1.00	(mm)
δ_{LV}	3.636	A/mm ²
n_{RHV}	5	cond.
n_{AHV}	2	cond.
n_{LDHV}	12	turn
B_m	1.496	T
K_t	0.4471	

Figure 2 shows that from the PSO process results obtained, the lowest global minimum value is 0.474 (redpoint). The global minimum is reached after the 25th iteration.

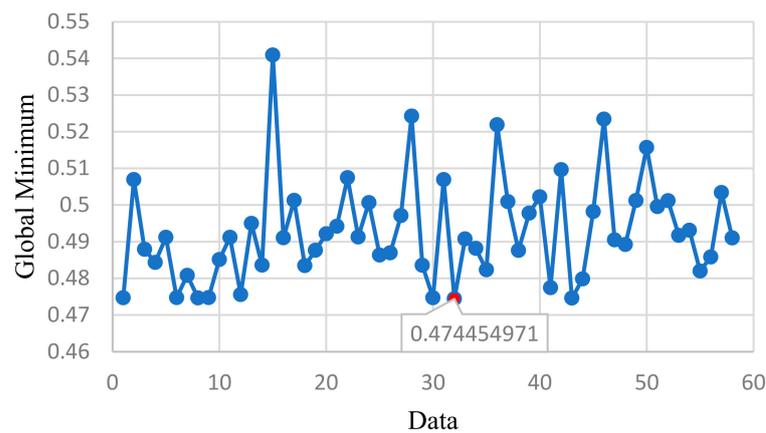


Figure 2. The optimization results.

4. Discussion

Figure 2 shows that from several experiments conducted, the minimum global value is obtained at 0.474. At the position, 11 parameters of the optimization results are presented in Table 4. The entire parameter of the optimization results is within limits determined from the beginning, so it can be used as a parameter for designing transformers.

4.1. Design Validation

The results of the optimization of the low-noise power transformer design are analytically and numerically validated with COMSOL and compared with the industry’s designs. These optimization variables are used as inputs in calculating the power transformer design. Based on (1), the voltage per turn (E_t) and the maximum magnetic flux are 126.46 V/turn and 0.5696 Wb, respectively. Based on (2), we obtained the cross-sectional area of the core (A_c), which is 0.3806 m². The transformer core is arranged from a laminated sheet, and then a space correction factor of 0.9 is required so that the diameter of the core (d_c) based on (3) is 0.6264 m. Taking into account (1) and (2), it can be seen that the cross-sectional area of the transformer core is strongly influenced by the power, frequency of the voltage sources, and density of the magnetic flux. A greater magnetic flux density will reduce the cross-sectional area of the core and vice versa.

The number of windings per phase at low voltage (N_{LV}) is a division of the low voltage side phase voltage (V_{LV}) divided by the voltage per turn (E_t). Therefore, based on (4), the number of windings per phase at low voltage is 261.

According to (5), the magnitude of the phase current at the LV winding (I_{LV}) is 808.08 A, and the cross-sectional area per turn for LV windings is 222.22 mm². The current density is obtained from the optimization process of the PSO algorithm.

A turn is divided into several conductors arranged in parallel to reduce power losses due to eddy currents. The optimization process gives the number of conductors in one turn for LV winding 11 pieces. The arrangement of such conductors is two axially and six radially, shown in Figure 3. The optimization results show that the thickness of one conductor at a low-voltage winding is 1.67 mm, and the width of one conductor is 12.07 mm.

The optimization process gives the number of turns in one disk for LV winding six turns. According to (7), the width of the overall low voltage winding (w_{LV}) is 66.26 mm. The number of disks for LV windings is the number of total turns of LV winding divided by the number of turns per disk. A total of 44 disks is obtained with a distance between disks of 2.65 mm. Only some disks contain six turns because the overall number of turns is 261, so there will be three disks containing five turns. The height of each disk is 25.14 mm, so based on (8), the height of the low-voltage winding is 1224 mm. The arrangement of low-voltage windings with 44 disks and six turns per disk is shown in Figure 4.

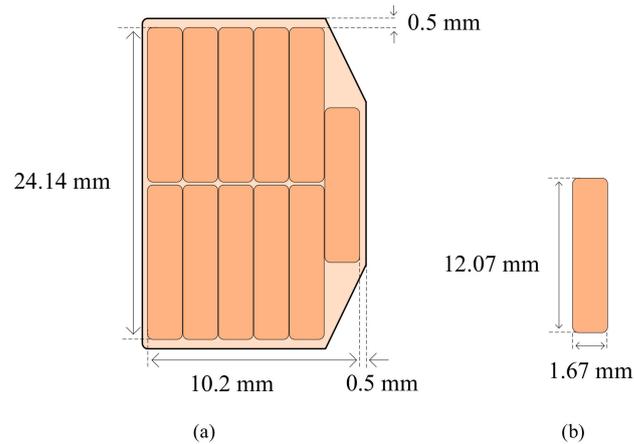


Figure 3. (a) The dimension and the arrangement of one turn and (b) the dimension of one conductor for LV winding.

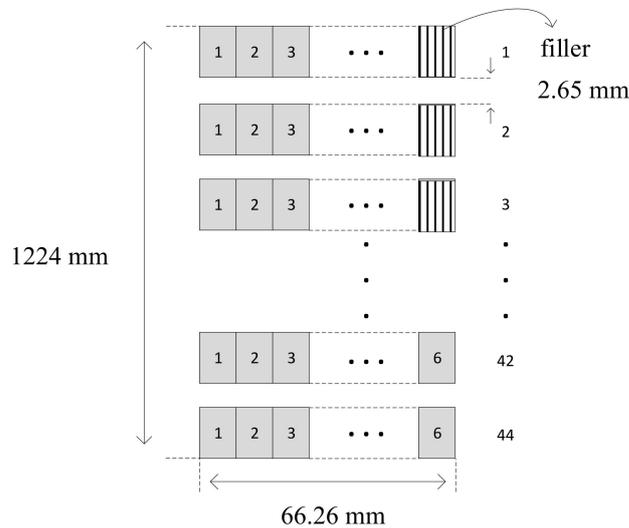


Figure 4. The arrangement of disk for LV winding.

Based on (9), the phase current (I_{HV}) for the high-voltage winding (star connecting) is 419.89 A. According to (10), the number of turns per phase of HV winding (N_{HV}) is 503. The optimization process gives the number of conductors per turn in HV winding nine pieces, with two winding axially and five winding radially. The arrangement of the conductors and disk of HV winding is shown in Figures 5 and 6. The dimensions of one conductor having a thickness of 1.00 mm and a width of 11.80 mm are indicated in Figure 5b. Based on (13), the overall width of HV winding (w_{HV}) is 74.46 mm. According to (11), the cross-sectional area per turn at the HV winding (A_{HV}) is 106.33 mm². The current density (δ_{HV}) of HV winding based on (12) is 3.95 A/mm².

The optimization process gives the number of turns per disk for HV windings 12 turns. The number of disks of HV winding is the total turns of HV winding divided by the number of turns per disk, which makes the number of disks 42. Only some disks contain 12 turns because the overall number of turns is 503, so there will be one disk containing 11 turns. Therefore, to maintain its balance, a filler is needed. According to (14), the height of HV winding (h_{HV}) is 1221 mm. The height of the HV winding is similar to that of the LV winding. The height similarity is to maintain magnetic balance in the winding.

The winding and core dimensions for one window are shown in Figure 7. The diameter of the core (d_c) and the diameter of the yoke are equally large at 626.4 mm. The tap winding (TW) is located separately from its primary winding and is placed in the middle between the HV windings for its phases. The distance between the HV windings and the tap

windings equals the distance between the LV windings and the HV windings. At the same time, the distance between the tap windings is equal to the distance between the core and the LV windings. Table 5 is a summary of the core and winding dimensions.

The diameters of the limb and yoke are the same size, so based on (22), the total length of the core (l_C) is 12,704.13 mm. This core length includes all the limbs and yoke of the top and bottom. Using the core weight per volume (G_c) of 7650 kg/m³, then by (23) and (24), the total weight of the core (W_C) is 36,993.10 kg.

The volume of the winding is calculated by taking the average diameter of each winding. Based on (25) and (26), the volumes of low-voltage and high-voltage windings are respectively 0.3906 m³ and 0.4738 m³. The weight per volume for the winding material (G_w) is 8890 kg/m³, so the weight of the LV winding (W_{LV}) and the HV winding (W_{HV}) is 3472.21 kg and 4212.11 kg.

The LV winding resistance (R_{LV}) and the HV winding resistance (R_{HV}) were calculated using (37) and (38) so that the resistance of LV winding is 0.1669 Ω and HV winding is 0.8842 Ω, respectively. The total resistance of the transformer (R) based on its high voltage side can be derived by (39), obtaining 1.5040 Ω.

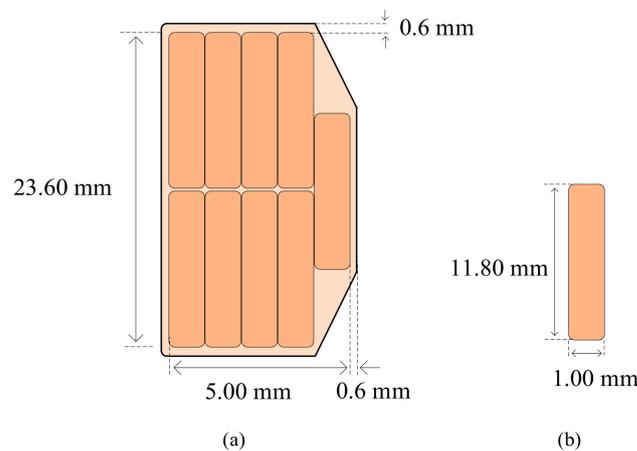


Figure 5. (a) The dimension and the arrangement of one turn, and (b) the dimension of one conductor for HV winding.

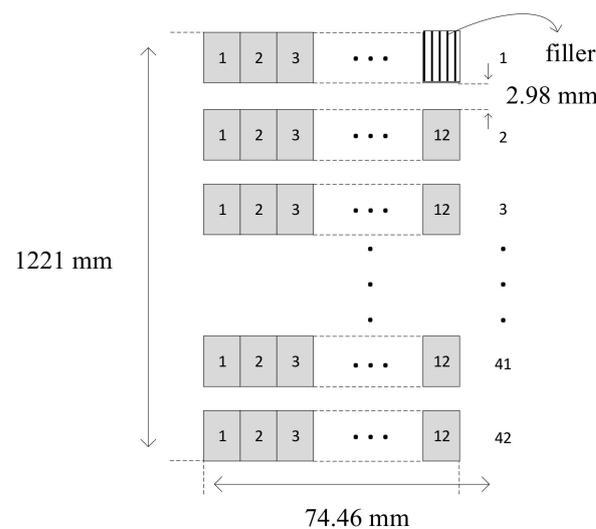


Figure 6. The arrangement of disk for HV winding.

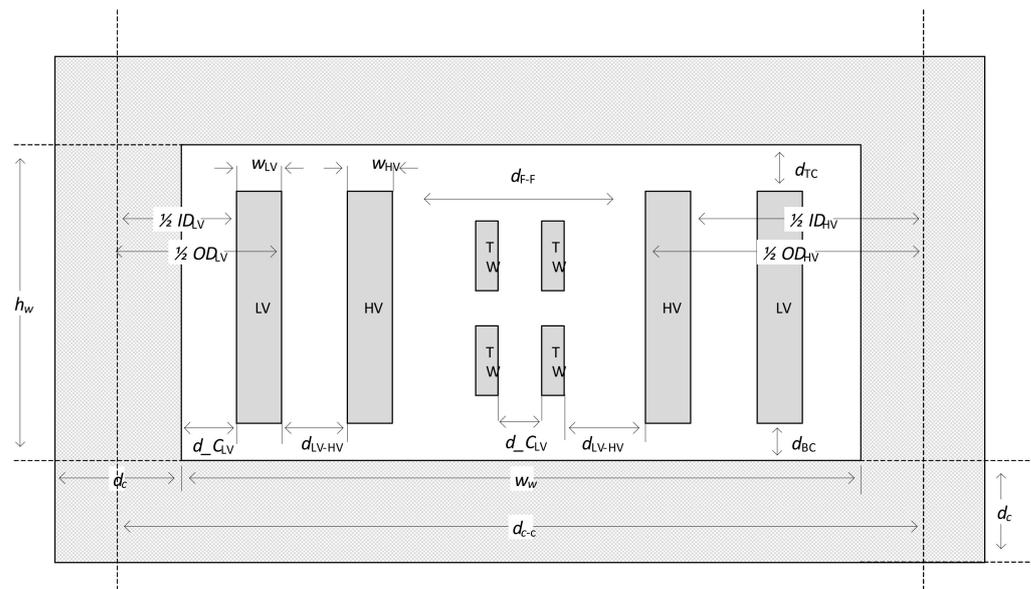


Figure 7. Dimension of the core and the winding in one window.

Table 5. Dimension of the core and the winding.

Variable	Symbol	Value (mm)
Diameter of the core	d_c	626.4
Distance between core and LV winding	d_{C-LV}	10.77
Width of LV winding	w_{LV}	66.26
Inner diameter of LV winding	ID_{LV}	647.96
Outer diameter of LV winding	OD_{LV}	780.47
Distance between LV and HV winding	d_{LV-HV}	42.31
Width of HV winding	w_{HV}	74.46
Inner diameter of HV winding	ID_{HV}	865.09
Outer diameter of HV winding	OD_{HV}	1014.02
Distance between center of limb	d_{C-C}	1779.82
Distance between HV winding	d_{F-F}	139.37
Distance between top winding and yoke	d_{TC}	110
Distance between bottom winding and yoke	d_{BC}	110
Height of the window	h_w	1444
Width of the window	w_w	1153.4

The dimensions of the winding strongly influence the impedance of the transformer. The impedance can be derived from (29) to (36). The cross-sectional area of the winding passed by the flux (A) is 0.2323 m^2 , and the Rogowski factor is 0.9597, then the leakage inductance based on the high voltage side (L) is 0.0579 H, and the leakage reactance of the transformer (X) is 18.20Ω . The impedance of the power transformer is usually considered equal to the value per unit of its reactance. So (X_{pu}) for this transformer when based on the side of high voltage is 12.04%. The impedance is still within the allowable limit range.

Copper losses are divided into two, namely copper losses on LV windings (PL_{LV}) and HV windings (PL_{HV}). In addition, there are losses due to eddy currents and stray losses. Based on (42) and (43), the copper losses in the LV and HV windings were 86.77 kW and 124.12 kW, respectively. Meanwhile, stray loss in structural components (frame and plate tank) is assumed to be 20% of the losses in the windings. So based on (49), the total load losses (PL) is 210.89 kW.

Two components dominate core losses (P_C): eddy loss and hysteresis loss. For practical purposes, the value of the two losses is a multiplier factor (K_L) between 1 and 1.25 of the core weight. The density loss at the core joint is higher than in other places. The equation assumes the weight at the core joint with a penalty factor (K_p). By taking $K_L = 1$ and

$K_J = 0.3$, and $K_p = 1$, the core loss (P_C) can be determined based on (41) as 36.99 kW. Based on (50) and (51) and considering all the losses obtained, the efficiency at full load and power factor unity is obtained by 99.56%. Based on (52) and (53), load noise (L_L) and no-load noise (L_{NL}) can be obtained by 69.33 and 69.32 dB. Total noise is a logarithmic aggregation of the three types of noise, so by excluding noise due to the cooling system, the noise coming from the core and winding is 71.3 dB.

4.2. Vibration and Noise Analysis with Finite Element Method

Accurate modeling of vibration and noise is highly dependent on the excellent coupling of magnetic, electrical, and mechanical domains [33]. This study modelled a three-phase power transformer with 80 MVA, three limbs, and double windings as a cylinder type. The core structure consists of four stages, and for simplicity, the power transformer tank is designed in the shape of a geometry box. The power transformer structure data obtained from the design optimization results using PSO are shown in Tables 5 and 6.

Table 6. Comparison of the results of design and optimization parameters with PSO.

Parameter	Symbol	Results		Unit
		Design	PSO	
Power	S	80		MVA
Frequency	f	50		Hz
HV side voltage	V_{HV}	110		kV
LV side voltage	V_{LV}	33		kV
Number of limbs		3		
Phase		3		
Nominal current of LV winding	I_{LV}	808.1	808.1	A
Nominal current of HV winding	I_{HV}	419.6	419.6	A
Impedance	Z_{pu}	12	12.04	%
Number of LV windings	N_{LV}	243	261	turn
Number of HV windings	N_{HV}	468	503	turn
LV winding height	h_{LV}	1587	1224	mm
High winding HV	h_{HV}	1553	1221	mm
LV winding width	w_{LV}	93	66.26	mm
HV winding width	w_{HV}	95	74.46	mm
Outer diameter of LV winding	OD_{LV}	966	780.47	mm
Outer diameter of HV winding	OD_{HV}	1236	1014.02	mm
LV winding weight	W_{LV}	6412	3472.21	kg
HV winding weight	W_{HV}	8214	4212.11	kg
LV current density	δ_{LV}	2.3	3.636	A/mm ²
HV current density	δ_{HV}	2.35	3.95	A/mm ²
Magnetic flux density	B_m	1.562	1.496	T
Core weight	W_C	37,795	36,993.10	kg
Core cross-sectional area	A_c	3914	3806.4	mm ³
Core losses	P_C	28.5	36.99	kW
Winding losses	PL	198.5	210.89	kW
Load noise	L_L	70.19	69.33	dB
No load noise	L_{NL}	69.57	69.32	dB

Finite element mesh is applied for core and winding in the form of free tetrahedral with maximum element size 0.6 m, minimum size 0.108 m, maximum element growth rate 1.5, curvature factor 0.6, and resolution of narrow regions 0.5. The number of vertex elements is 284, the number of edge elements is 4757, the number of tetrahedra elements is 97,265, and the number of triangles elements is 25,697 with minimum element quality is 0.09535. According to [34], mesh size does not significantly affect the results but affects calculation time. The Figure 8 shows the finite element mesh for the designed power transformer.

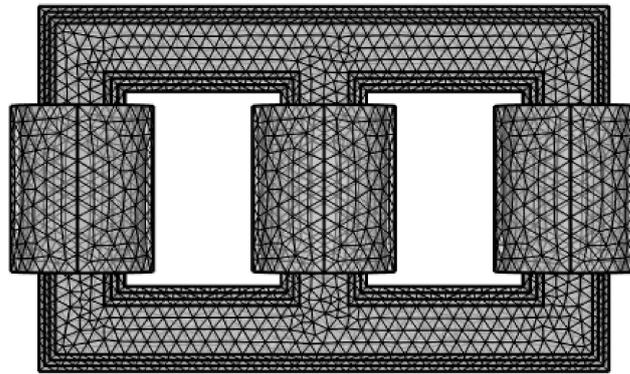


Figure 8. Developed mesh.

4.2.1. Electromagnetic Field Analysis

The current flowing in the winding is assumed to be evenly distributed. The strength of the electromagnetic field will build up around the winding with varying values depending on the supply in the winding, the permeability of the core, air, and surrounding materials. Furthermore, the boundary is in the shape of a box that is used as magnetic shielding. The electromagnetic field is calculated by software simulation based on Maxwell’s Theory in Equations (69) to (71) as presented by [34].

$$J^e = \sigma \frac{\partial A}{\partial t} + \nabla \times (\alpha_0^{-1} \cdot \alpha_r^{-1} \nabla \times A) \tag{69}$$

$$B = \alpha_0 \alpha_r = \nabla \times A \tag{70}$$

$$J = \sigma E + J^e \tag{71}$$

The magnetic field module based on Equations (69) to (71) is solved by setting the variables A_x , A_y , A_z , and ψ . The maximum magnetic density for the core is 1.5 T. While the winding conductor is chosen as a circular coil type with a homogenized numeric multiturn coils model, with the conductivity of copper as 5.89×10^7 S/m.

4.2.2. Structure Dynamics

The structural analysis deformation components u , v , and w are obtained by Equations (72) to (73). The coil domain is assumed to be a linear elastic material with the core as a magnetostrictive material

$$\frac{\partial M}{\partial \sigma} = \frac{\sigma}{E\zeta} (M_{on} - M) + c \frac{\partial M_{on}}{\partial \sigma} \tag{72}$$

$$\epsilon = \frac{1}{M\Delta^2 + c\Delta + K} \cdot \frac{A_r E}{l_r} \cdot \rho \tag{73}$$

The effective field in the core can be derived by Equation (74).

$$H_{eff} = H + \frac{3\lambda_m}{\alpha_0 \eta_s^2} \times M \tag{74}$$

The coefficient M describes the interaction of magnetism and stress. Meanwhile, the magnetization model can be defined by Equation (75).

$$\vartheta = \coth \left(\frac{3X_m H_{eff}}{\eta_s} \right) - \frac{\eta_s}{3X_m H_{eff}} \tag{75}$$

Some displacements as a result of simulation with COMSOL are shown in Figure 9. Each frequency gives different displacement results. The final resultant is the summation of all displacements to determine the deformation of the core.

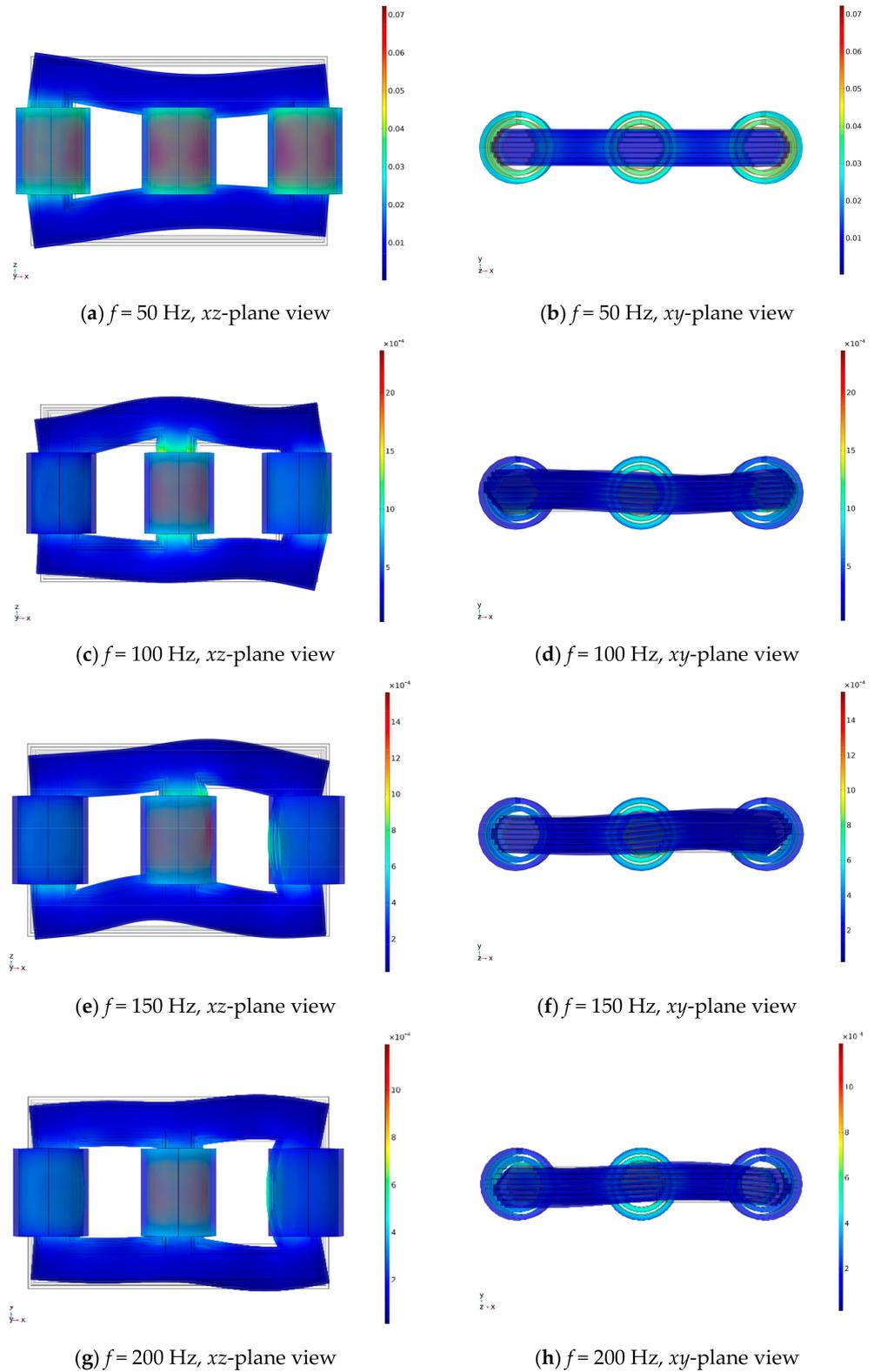


Figure 9. Cont.

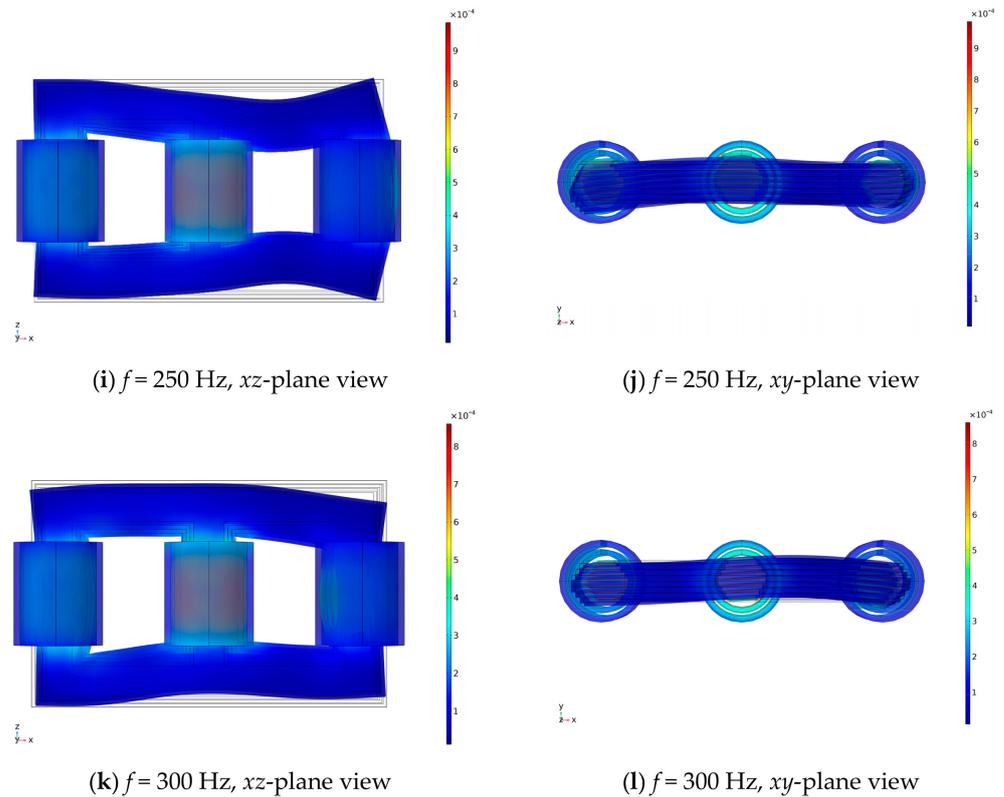


Figure 9. Vibration displacement with varying frequency.

4.2.3. Acoustics Analysis

Equations (76) to (77) are used to calculate the acoustics of the power transformer.

$$\nabla \cdot \left(-\frac{1}{\rho_c} \nabla \rho_t \right) - \frac{k_{eq}^2}{\rho_c} \rho_t \tag{76}$$

$$k_{eq}^2 = \left(\frac{\omega}{C_c} \right)^2 \tag{77}$$

where ρ_0 is the density of the fluid, p is the pressure, c is the speed of sound, ω is the angular frequency, and C_c is the bulk modulus. The acoustics interface is used for acoustics studies. This interface is the result of coupled study with structural dynamics.

4.3. Numerical Design Validation

Numerical design validation of the power transformer is performed using COMSOL software. The 3D model illustration, including cores and windings, is shown in Figure 10. Based on data from Tables 5 and 6. The parameters of relative conductivity, relative permeability, and relative magnetic permeability in the core are set to 1. A three-phase voltage source with 120° phase difference is connected to the HV winding, and the LV winding is assumed to flow nominal current for each phase.

Noise verification is performed by taking simulated data at several measurement points (MP). The measurement points are located at a distance of 0.3 m from the tank and at half the height of the transformer. The distance between measurement points is 0.5 m. The Table 7 shows the data taken from the simulation for 34 measurement points. Table 7 is the noise taken from several measurement points.

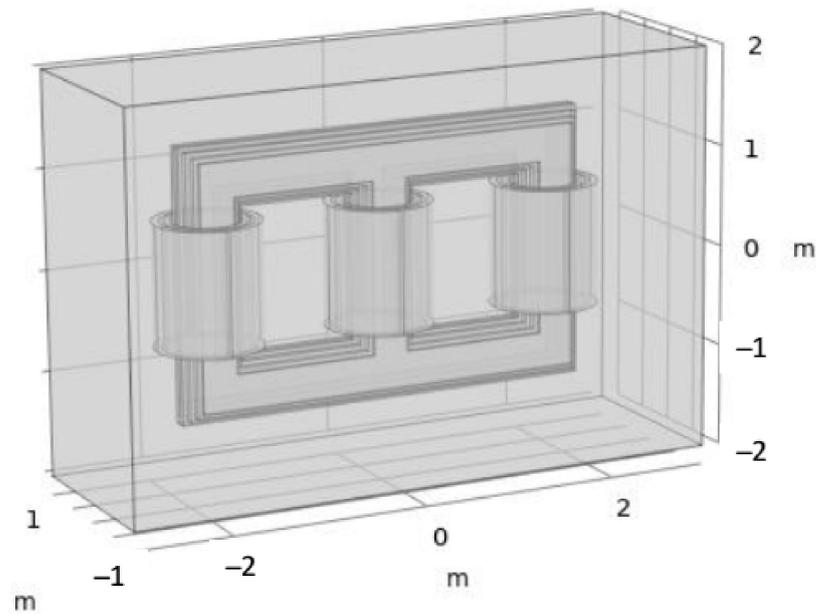


Figure 10. The 3D model of power transformer.

Table 7. Noise data from measurement points.

MP	Noise (dB)	MP	Noise (dB)
1	73.93	18	66.29
2	73.38	19	63.57
3	71.82	20	61.45
4	69.33	21	73.40
5	66.22	22	71.87
6	63.77	23	69.47
7	61.59	24	66.42
8	73.33	25	63.69
9	71.79	26	61.59
10	69.21	27	62.49
11	66.25	28	63.16
12	63.51	29	63.15
13	61.45	30	62.47
14	73.89	31	62.49
15	73.36	32	63.17
16	71.81	33	63.15
17	69.36	34	62.57

According to [35], the average of sound power level can be calculated by

$$\overline{L_{pA0}} = 10 \log_{10} \left(\frac{1}{N} \sum_{i=1}^N 10^{0.1 L_{pAi}} \right) \tag{78}$$

where $\overline{L_{pA0}}$ is the average of sound power level, N is number of measurement point, and L_{pAi} is the sound power level in the measurement point. According to (78), the average sound power level is 69.25 dB. Figure 11 illustrates the sound power distribution seen from top and side of power transformer.

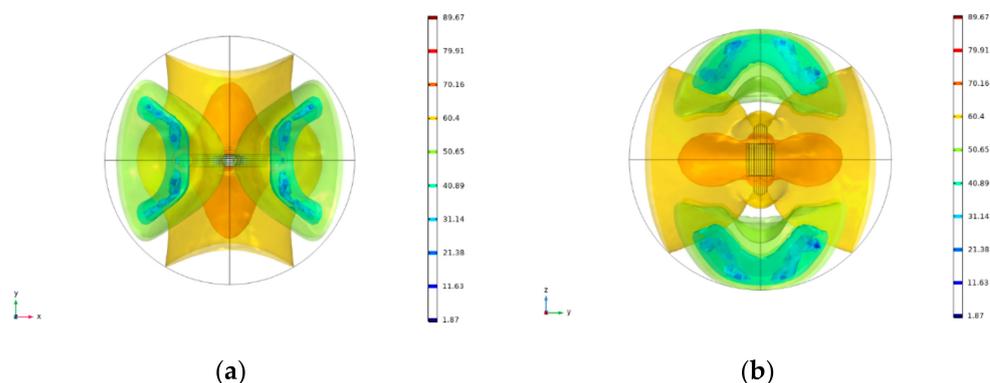


Figure 11. Sound power level distribution viewed from (a) top and (b) side.

4.4. Comparison of Design and Optimization

A comparison of design and optimization results is presented in Table 6. The optimization results provide a higher current density value than the design results. A higher current density will result in a smaller cross-sectional area for one turn, affecting the weight of the winding and its dimensions. The increase in current density is directly proportional to the decrease in winding material weight. The increase in current density in LV winding by 1.336 A/mm² or 58% will reduce the weight of winding material by 2939.8 kg. While the increase in current density in HV winding by 1.6 A/mm² or 68% will reduce the weight of HV winding material by 4.001 kg. However, another consideration is that with the current’s high density, the temperature increase will be higher, impacting the cooling system. The method to reduce the temperature rise is to add an extra radiator so that it does not impact the transformer noise. The winding height of the optimization result is lower than the design result and has a lower winding width. The core weight of the optimization results has a lower value than the design results, around 801.9 kg or a decrease of 2.12%. The winding weight of the optimization result is lighter than the design result, with a difference of 6941.68 kg or a decrease of 47.46%. These two parameters obtained significant savings, which will lower the cost of production. On the contrary, core losses and winding losses have increased compared to the design results. The primary cause of the increase in winding losses is the current density.

Based on (52), load noise is affected by the weight of the winding and the dimension ratio of the winding. Thus, with a decrease in winding weight and height, the optimization results provide a load noise value of 69.33 dB lower than the design results.

The objective function of this optimization is to minimize the weight of the core material, winding material, and load noise. The core’s material cost is cheaper than the material costs for its winding. For comparison, the price of winding material today is two times more expensive than that of the core material. Therefore, the optimization results provide a much cheaper material cost value while still getting a lower load noise. The optimization method with PSO can be used to design a low noise power transformer. The PSO method is beneficial in determining the optimal variables to produce a transformer design that meets the standards, is low-cost, and has low noise.

5. Conclusions

The paper introduced the optimization of low-load noise power transformer design. The PSO method can obtain optimum values of 11 variables that can be used to design low-load noise power transformers. The paper has set up a multi-objective function for optimal load noise, the weight of the core, and the weight of the winding. The optimization results showed a decrease in load noise, core weight, and winding weight by 0.86 dB, 2.12%, and 47.46%, respectively. The industry will benefit by applying this method, such as a low-noise power transformer design and obtaining economic benefits by optimizing the

core and winding weight. The results of this optimization are better than the designs used regularly in the industry.

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