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# Relationship Between the Coordination Geometry and Spin Dynamics of Dysprosium(III) Heteroleptic Triple-Decker Complexes

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Figure S1. ESI-MS spectrum of 1 in CHCl<sub>3</sub>. The peak at 2062.47242 corresponds to [M-1<sup>+</sup>].



**Figure S2.** Experimental (top) and simulated (bottom) ESI-MS spectra of **1** in CHCl<sub>3</sub>. The peak at 2062.47242 corresponds to [M-1<sup>+</sup>].



Figure S3. ESI-MS spectrum of 2 in CHCl<sub>3</sub>. The peak at 1962.38956 corresponds to [M<sup>+</sup>].



**Figure S4.** Experimental (top) and simulated (bottom) ESI-MS spectra of **2** in CHCl<sub>3</sub>. The peak at 1962.38956 corresponds to [M<sup>+</sup>].



Figure S5. IR spectrum for 1 (top) and 2 (bottom) by using an ATR method at 298 K.



**Figure S6.** UV-vis-NIR spectra for **1** (top) and **2** (bottom) in CHCl<sub>3</sub> ( $5.1 \times 10^{-3}$  (**1**), and  $4.7 \times 10^{-3}$  (**2**)) at 298 K.

	1	2
	$C_{124}H_{72}N_{16}Cl_{12}Dy_2$	$C_{110}H_{62}N_{20}Cl_6Dy_2$
T/K	100	100
Crystal system	tetragonal	monoclinic
Space group	<i>I</i> 4/ <i>m</i>	$P 2_1/c$
<i>a</i> / Å	14.2765(3)	13.7898(4)
b∕ Å	14.2765(3)	27.5804(8)
c/ Å	25.6718(9)	23.5302(7)
α/ deg.	90 <sup>°</sup>	90 <sup>°</sup>
$\beta$ / deg.	90 <sup>°</sup>	98.541(3)
γ/ deg.	90 <sup>°</sup>	90 <sup>°</sup>
<i>V</i> / Å <sup>3</sup>	5232.39	8850.0(5)
Z	2	4
$R_1(I > 2s(I))$	0.0346	0.0612
$wR_2$ (all)	0.0822	0.1254
GOF	1.127	1.032

Table S1. Selected crystallographic data for 1 and 2

	1	2
1 <sup>st</sup> short contact (Å) (complex and complex)	2.889 (Cl1H18)	2.817 (C02GC03B)
1 <sup>st</sup> short contact (Å) (complex and CHCl <sub>3</sub> )	2.690 (C9H20)	2.574 (H53N10)
2 <sup>nd</sup> short contact (Å) (complex and CHCl <sub>3</sub> )	3.175 (Cl3H20)	2.891 (Cl03H9)

Table S2. Selected crystallographic data for 1 and 2



Short contacts in the crystal for 1 (top) and 2 (bottom)



Figure S7. PXRD patterns for 1 (top) and 2 (bottom).



**Figure S8.** Curie-Weiss plot for **1**. Linear approximation is performed over the entire *T* range, from which the values of Curie constant (*C*) (28.50 cm<sup>3</sup> K mol<sup>-1</sup>) and Weiss constant ( $\theta$ ) (–2.33 K) were obtained.



**Figure S9.** Curie-Weiss plot for **2**. Linear approximation is performed over the entire *T* range, from which the values of Curie constant (*C*) (28.20 cm<sup>3</sup> K mol<sup>-1</sup>) and Weiss constant ( $\theta$ ) (–1.97 K) were obtained.



**Figure S10** Frequency ( $\nu$ ) and temperature (*T*) dependences of the (**a**) in-phase ( $\chi$ <sup>M</sup>) and (**b**) out-of-phase ( $\chi$ <sup>M</sup>) ac magnetic susceptibilities of **1** in 0 kOe.



**Figure S11** Frequency ( $\nu$ ) and temperature (*T*) dependences of the (**a**) in-phase ( $\chi$ <sup>M</sup>) and (**b**) out-of-phase ( $\chi$ <sup>M</sup>) ac magnetic susceptibilities of **2** in 0 kOe.



**Figure S12** Frequency ( $\nu$ ) and temperature (*T*) dependences of the (**a**) in-phase ( $\chi$ <sup>M</sup>) and (**b**) out-of-phase ( $\chi$ <sup>M</sup>) ac magnetic susceptibilities of **1** in 1.3 kOe.



**Figure S13** Frequency ( $\nu$ ) and temperature (*T*) dependences of the (**a**) in-phase ( $\chi$ <sup>M</sup>) and (**b**) out-of-phase ( $\chi$ <sup>M</sup>) ac magnetic susceptibilities of **2** in 2 kOe.



Figure S14  $\chi {\mbox{\sc m}}^{\prime\prime}/\chi {\mbox{\sc m}}^{\prime}$  versus T (2.5–4 K) plot for 1



**Figure S15**  $\chi$ M''/ $\chi$ M' versus *T* (2.5–4 K) plot for **2** 

## The extended Debye model [1] (eqn. S1–S3)

The real ( $\chi_M'$ ) and imaginary parts ( $\chi_M''$ ) of the ac magnetic susceptibilities are given by eqns. S2 and S3, respectively.

$$\chi_{\text{total}}(\omega) = \chi_{S} + (\chi_{T} - \chi_{S}) \left[ \frac{\beta}{1 + (i\omega\tau_{1})^{1-\alpha_{1}}} + \frac{1-\beta}{1 + (i\omega\tau_{2})^{1-\alpha_{2}}} \right]$$
(S1)

$$\chi'(\omega) = \chi_{S} + (\chi_{T} - \chi_{S}) \left\{ \frac{\beta [1 + (i\omega\tau_{1})^{1-\alpha_{1}} \sin(\pi\alpha_{1}/2)]}{1 + 2(\omega\tau_{1})^{1-\alpha_{1}} \sin(\pi\alpha_{1}/2) + (\omega\tau_{1})^{2-2\alpha_{1}}} + \frac{(1-\beta) [1 + (i\omega\tau_{2})^{1-\alpha_{2}} \sin(\pi\alpha_{2}/2)]}{1 + 2(\omega\tau_{2})^{1-\alpha_{2}} \sin(\pi\alpha_{2}/2) + (\omega\tau_{2})^{2-2\alpha_{2}}} \right\}$$
(S2)

$$\chi' \quad (\omega) = (\chi_T - \chi_S) \left[ \frac{\beta(\omega\tau_1)^{1-\alpha_1} \cos(\pi\alpha_1/2)}{1 + 2(\omega\tau_1)^{1-\alpha_1} \sin(\pi\alpha/2) + (\omega\tau_1)^{2-2\alpha_1}} + \frac{(1-\beta)(\omega\tau_2)^{1-\alpha_2} \cos(\pi\alpha_2/2)}{1 + 2(\omega\tau_2)^{1-\alpha} \sin(\pi\alpha_2/2) + (\omega\tau_2)^{2-2\alpha_2}} \right]$$
(S3)



**Figure S16.** Argand plots ( $\chi$ M<sup>"</sup> versus  $\chi$ M<sup>'</sup>) for **1** at 1.8 K in several dc magnetic fields (0-5 kOe). Black solid lines were guides for eye.



**Figure S17.** Argand plots ( $\chi_M$ " versus  $\chi_M$ ') for **2** at 1.8 K in several dc magnetic fields in the range of 0–5 kOe. Black solid lines were guides for eye.

## The equation for fitting the Arrhenius plot

In  $H/\tau$  plot, the contributions of the spin lattice relaxation and QTM processes were included the following eqn. 1

	$A[S^{-1}K^{-1}]$	n	<b>B</b> 1	<b>B</b> <sub>2</sub>	$D[S^{-1}]$
<b>1</b> (Low ν)	1.69	0	3.36	0.260	0
<b>1</b> (High <i>v</i> )	$2.98 \times 10^{3}$	2.81	$2.84\times10^{10}$	$8.29 \times 10^{6}$	0
<b>2</b> (Low ν)	0	-	3.45	3.90	1.35
<b>2</b> (High <i>v</i> )	0	-	0	-	$5.97 \times 10^{3}$

**Table S3.** Parameters for fitting the  $\tau$  verses *H* plots



**Figure S18.** Argand plots ( $\chi$ M<sup>"</sup> versus  $\chi$ M<sup>'</sup>) for **1** in 1.3 kOe in the *T* range of 1.8–4.5 K. Black solid lines are guides for the eye.



**Figure S19.** Argand plots ( $\chi$ M<sup>"</sup> versus  $\chi$ M<sup>'</sup>) for **1** in 2 kOe field in the *T* range of 1.8–4.5 K. Black solid lines are guides for the eye.

#### The equation for Arrhenius plot

In  $\tau$  verses *T* plot, contribution of each spin lattice relaxation and QTM process were assigned with following eqn.5

	$A[S^{-1}K^{-1}]$	n	$C$ $[S^{-1}K^{-m}]$	т	$ au_{ ext{QTM}}^{-1}$ [s]
<b>1</b> (Low ν)	0	-	0	-	0.161
<b>1</b> (High $v$ )	$2.98 \times 10^{3}$	2.57	30.6	9	$1.77 \times 10^{22}$
2 (Low v)	$2.84\times10^{10}$	1.71	0	-	0
<b>2</b> (High <i>v</i> )	0	-	0	-	$2.84\times10^{10}$

**Table S4.** Parameters of fitting for  $\tau$  verses *T* plot

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