Effect of Twisting and Stretching on Magneto Resistance and Spin Filtration in CNTs

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Abstract: Spin-dependent quantum transport properties in twisted carbon nanotube and stretched carbon nanotube are calculated using density functional theory (DFT) and non-equilibrium green’s function (NEGF) formulation. Twisting and stretching have no effect on spin transport in CNTs at low bias voltages. However, at high bias voltages the effects are significant. Stretching restricts any spin-up current in antiparallel configuration (APC), which results in higher magneto resistance (MR). Twisting allows spin-up current almost equivalent to the pristine CNT case, resulting in lower MR. High spin filtration is observed in PC and APC for pristine, stretched and twisted structures at all applied voltages. In APC, at low voltages spin filtration in stretched CNT is higher than in pristine and twisted ones, with pristine giving a higher spin filtration than twisted CNT.

Keywords: twisted carbon nanotube (twisted CNT); stretched carbon nanotube (stretched CNT); magneto resistance (MR); spin efficiency

1. Introduction

Spintronics involves investigations associated with the electron’s spin, magnetic moment, and charge. Magnetic junction has usefulness in magnetic device applications, for example, magneto-resistive random access memory (MRAM), read heads of hard disk drives, programmable logic, and so on [1,2]. A two probe magnetic junction is a three-layer device in which nonmagnetic material is sandwiched between two electrodes. Electrodes are basically made up of ferromagnetic materials. The ferromagnetic material is chosen because of its unique electronic properties; that is, that spin-up and spin-down electrons pass from one electrode to other electrode through the magnetic junction with different Fermi energies. High tunnel magneto resistance and high spin filtration are required for a CNT-based spintronic device to deliver better performance and ensure its use in spin valves and other spintronic-based devices. The above requirements can be satisfied by the use of half-metallic ferromagnets with 100% polarization as electrodes [3]. Though dozens of systems have been predicted to be half-metallic, CrO$_2$ is essentially the only material that has been experimentally shown to definitively be a half-metal [4]. Magnetic tunnel junctions were experimentally fabricated using thin films of the half-metallic ferromagnet CrO$_2$, employing SnO$_2$ tunnel barriers in [5].

Carbon nanotube (CNT) was discovered in the 1990s [6]. CNT has high electrical conductivity and thermal conductivity. It can be metallic or a semiconductor [7–10]. Carbon nanotubes (CNTs) can be used in spintronic devices due to their nanoscale size and very large spin flip scattering lengths [2]. Spin can be transported in CNTs over large lengths of about 130 nm. So far, carbon nanotube-based magnetic junctions are one of the most interesting one-dimensional magnetic junctions, where CNT is sandwiched between magnetic metals [11]. (6, 0) zigzag nanotubes have semiconducting properties. There are many works that have been done using (6, 0) carbon nanotubes as a barrier in magnetic junction [11,12]. In the past, our group has even used (8, 0) SiCNTs for the same reasons, as well as
their popularity [11,12]. It is therefore of interest to use (6, 0) CNT and understand how twisting or stretching of CNT affect its spin transport properties. The quantum transport properties of pristine CNT are reported in [13]. It is understood that during the fabrication process some defects may occur in CNTs. Defects such as twisting of CNT, stretching of CNT, and bending of CNT can inevitably occur. CNTs can also be radially expanded and axially elongated during transfer to the substrate. Due to twisting and stretching defects, CNTs can undergo change in the transmission spectrum and band structure. It is therefore of interest to understand how twisting and stretching in CNTs affect its spin transport properties.

In [14], spin filtering in oligopeptide monolayers was investigated, and the authors reported that electron conduction through oligopeptides is spin-dependent. However, in this study, we demonstrate spin-dependent quantum transport properties in twisted carbon nanotube and stretched carbon nanotube. We present a comparative analysis of spin transport in twisted CNT, stretched CNT, and pristine CNT. The current-voltage characteristics, transmission spectrum, magneto resistance, and spin efficiency of twisted and stretched CNTs are calculated using density functional theory (DFT) and non-equilibrium green’s function (NEGF). The results are compared with pristine CNT to understand the effect of twisting and stretching on magneto resistance and spin filtration in CNTs.

2. Simulation Method and Setup

Figures 1 and 2 show the two-probe geometry of the magnetic junction made up of twisted carbon nanotube and stretched carbon nanotube sandwiched between two CrO$_2$ HMF electrodes. Figure 3 shows comparison among all the three structures.

The above two-probe geometry is simulated using Atomistix software [15–18] to obtain current-voltage characteristics (see Figures 4 and 5) and transmission spectrum (Figures 6 and 7) in both configurations (PC and APC). The electronic transport properties are calculated using self-consistent calculations. The self-consistent calculations are performed on the basis of DFT and NEGF formulation. For exchange-correlation, spin-polarized generalized gradient approximation (SGGA) is used, because the current is due to spin-polarized electron transport [13]; exact exchange potential of atoms is used to analyze generalized gradient approximations (GGAs) [19]. In general, spin-polarized GGA is more accurate than local-spin density approximation (LSDA) in atomic structure and energetic, but the difference between the former and the latter in terms of the electronic properties of solid-state systems is relatively small [20]. The experimental data is currently unavailable for this structure. Pristine, twisted, and stretched CNTs are also shown in Figure 3.

![Figure 1](image1.png)

**Figure 1.** Two-probe geometry in which twisted CNT is sandwiched between CrO$_2$ electrodes.

![Figure 2](image2.png)

**Figure 2.** Two-probe geometry in which stretched CNT is sandwiched between CrO$_2$ electrodes.
A zigzag (6, 0) twisted CNT and zigzag (6, 0) stretched CNT with a bond length of 1.421 Å between carbon atoms and length of 15.629 Å is considered in the simulations, as in [13]. The bond length between carbon and chromium is kept at ~2.09 Å [13]. The distance between the electrodes is 19.809 Å The effect may arise from the electric field as well. The authors in [21] have mentioned that the “electric field assisted switching in magnetic tunnel junction”. The I–V characteristics and transmission spectrums are acquired by simulating this geometry. The parameters used in the simulation are in accordance with [22–24]. The basis set used is double zeta polarized for carbon nanotube and single zeta polarized for both CrO₂ electrodes. The mesh cutoff and electron temperature are assumed to be 150 Ry and 1800 K, respectively. The k point sampling in x, y, and z directions are assumed to be 3, 3, 100, respectively, as in [13]. In the simulations, magnetization of the electrodes can be simply changed to either up or down by assuming 1 or −1 spin polarization values. We have done simulation-based studies by assuming parallel magnetization and antiparallel magnetization of the electrodes. The relative spin in a parallel configuration of both electrodes and carbon atoms of twisted or stretched CNT are assumed to be 1, 0, 1. Whereas, in an antiparallel configuration, the right electrode atom spin is assumed to be −1, so the spin sequence will be 1, 0, −1. The direction of spin polarization—parallel or antiparallel—is in relation to the electron’s velocity.

The same is true for the effect of the magnet, how the magnetic field is applied, and what the magnitude of the field is, all of which are demonstrated in the experimental studies reported in [24]. How the resistance depend on field strength is little tricky. When the magnetization of both the electrodes is in same direction (similarly polarized electrodes), potential difference applied across electrodes creates a transverse electric field in the channel (CNT). The higher the potential difference is, the more the electric field in the channel is, and the less the resistance will be. However, in antiparallel polarization alignment of the electrodes—that is, electrode magnetization in opposite direction—the varying electric field will have a negligible change in resistance. One more important observation from the experiments is that high electric fields, when applied to individual electrodes, can reverse their magnetization polarization. The resistance can be low or high, depending upon the relative orientation of ferromagnet magnetization, which can be parallel (P) or antiparallel (AP) [2].

The transmission spectrum indicates the probability of an electron moving from the left electrode to the right electrode under the influence of applied voltage. The current can be evaluated by using the relation [1,15–17]:

\[
I^\uparrow (\downarrow) = e/h \int_{-\infty}^{+\infty} T^\uparrow (\downarrow) (E, V_B) [F(E - \mu_L) - F(E - \mu_R)] \, dE
\]

where \( T^\uparrow (\downarrow) (E, V_B) \) represents the Transmission coefficient, \( E \) as Energy, \( F \) as Fermi-Dirac distribution function, \( \mu_R \) and \( \mu_L \) are the chemical potential for right and left electrodes.
3. Results and Discussion

For PC and APC configurations, the current-voltage characteristics are shown in Figures 4 and 5. In Figure 4, for PC, $I_{\uparrow}$ is always less than $I_{\downarrow}$ in all the three structures (pristine, twisted, and stretched). The spin-up current increases with an increase in bias, with spin-down current being negligible in all three structures, as shown in Figure 4. The total equilibrium conductance of pristine, twisted and stretched CNTs at zero bias are found to be $0.48G_0$, $0.59G_0$ and $0.58G_0$, respectively, where $G_0$ represents conductance quanta, $G_0 = 2e^2/h$ [1].

In Figure 5, both $I_{\uparrow}$ and $I_{\downarrow}$ in APC are almost zero for the applied voltage range of 0 to 0.8 V for all three structures, but spin-up current increases slowly at applied voltages of above 0.8 V while spin-down current stays around zero. The total equilibrium conductance of pristine, twisted and stretched CNTs is found to be $2.18G_0$, $2.64G_0$ and $7.0G_0$, respectively.

The MR is calculated by utilizing the usual definition, $MR = (I_{PC} - I_{APC})/I_{PC}$ [25], where $I_{PC}$ and $I_{APC}$ are the total currents in parallel configuration and antiparallel configuration. From the current-voltage curve, it can be seen that at zero volts, total current in all three structures is zero, and MR is calculated by utilizing equilibrium conductance. The MR obtained at zero bias is ~100%. At low bias, $I_{APC}$ is negligible for all three structures; however, at high bias voltages, $I_{APC}$ marginally increases in the case of pristine and twisted CNTs, and is greater in pristine CNT (see Figure 5). For stretched CNT, $I_{APC}$ remains negligible even at high bias voltages. This results in higher MR in stretched CNT than in twisted and pristine CNTs (see Figure 8). The physical phenomenon behind the higher MR in stretched and twisted CNTs can be directly associated with the number of electronic states available near Fermi level.

![Graph showing current-voltage characteristics for parallel configuration](image)

**Figure 4.** Comparison of current-voltage curves in PC for all three structures. The total spin current of twisted CNT is greater than that of stretched CNT, and the total spin current of stretched CNT is greater than that of pristine CNT.
However, (see Figure 8) and low IAPC (see Figure 5).

**Figure 5.** Comparison of I-V curves in APC for all three structures. The total spin current for all three structures is zero for low biases, but for higher biases, spin-down current remains zero, and spin-up current of pristine CNT is greater than that of twisted CNT and the spin-up current of stretched CNT is greater than that of pristine CNT.

![I-V curves comparison](image)

**Figure 6.** Transmission spectrum T(E, V_b) with respect to energy ranging from −0.3 eV to +0.3 eV for different applied voltages for PC. At zero volts, the comparative transmission probability for all three structures, shown separately for spin-up (a) and spin-down (b).

There are almost negligible states in all the three structures, in which the current is very small. However, the lowest number of states for twisted structure (see Figure 7a) results in high resistance (see Figure 8) and low I_{APC} (see Figure 5).
Figure 7. Transmission spectrum $T(E, V_b)$ with respect to energy ranging from $-0.3$ eV to $+0.3$ eV for different applied voltages for APC. At zero volts, the comparative transmission probability for all three structures, shown separately for spin-up (a) and spin-down (b).

![Graph showing transmission spectrum](image)

Figure 8. Comparative plots for magneto resistance with respect to applied voltages. For high bias voltage, MR of stretched CNT is higher than that of twisted CNT, and MR of twisted CNT is higher than that of pristine CNT.

![Graph showing magneto resistance](image)

Spin injection factor ($\eta$) is calculated by utilizing the following definition: $\eta = (I_{\uparrow} - I_{\downarrow})/(I_{\uparrow} + I_{\downarrow})$ [2], and is plotted in Figure 9. At zero volts, total current in all three structures is zero, and spin injection factor is calculated by utilizing equilibrium conductance. Parallel configuration $I_{\uparrow}$ is nearly equal, and $I_{\downarrow}$ is negligible in all three cases (see Figure 4), resulting in only carriers with up-spin being allowed to propagate through the CNT, and blocking down-spin carriers, resulting in high spin filtration ($\eta$) in the case of PC at all bias points.

![Graph showing spin injection factor](image)

Figure 9. Spin injection factor with respect to applied voltages for all three structures in parallel configuration and antiparallel configuration.
In APC, stretching increases the spin filtration at all bias points in comparison to pristine and twisted structures, and is ~100% at high bias voltages. However, twisting results in lower spin filtration than in pristine and stretched CNTs at low bias voltages, and also negative spin filtration (see Figure 9) due to $I_↓$ being greater than $I_↑$.

4. Conclusions

The spin-dependent quantum transport properties in twisted CNT and stretched CNT are investigated, and it is found that the magneto resistance (MR) of stretched CNT is higher than that of twisted CNT, and the MR of twisted CNT is higher than that of pristine CNT, and that higher spin filtration is obtained in stretched CNT in comparison to pristine CNT. High MR and high spin filtration show the importance of twisted and stretched carbon nanotube for use in spin valves and other applications.

Author Contributions: Anil Kumar Singh performed the experiment, analyzed the data and wrote the paper under the guidance of Sudhanshu Choudhary.

Conflicts of Interest: The authors declare no conflict of interest.

References


