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Tools for Predicting the Nature and Magnitude of Magnetic Anisotropy in Transition Metal Complexes: Application to Co(II) Complexes

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Abstract: This work addresses the question of the identification of the excited states that are mainly responsible for the magnitude and nature of the magnetic anisotropy in high-spin mononuclear transition metal complexes. Only few states are actually responsible for the single ion magnetic anisotropy, and these states can be anticipated from rather simple rules. We show that in high-spin complexes atomic selection rules still prevail and that molecular selection rules from the symmetry point group are more selective than those of the double group. The predictive power of these rules is exemplified on a penta-coordinate Co(II) complex investigated with correlated ab initio calculations, including relativistic contributions. The electronic structure of excited states coupled to the ground state through spin-orbit coupling informs us about the nature (either axial or planar) of their contribution to the anisotropy. From this information, it is possible to anticipate the nature and strength of the ligand field and predict the magnetic anisotropy, which may guide the synthesis of improved anisotropic complexes. Such results can also be used to improve the quality of ab initio calculations of the spin Hamiltonian parameters and to reduce the computational cost.

Keywords: magnetic anisotropy; transition metal complexes; ab initio calculations; spin-orbit coupling

1. Introduction

Magnetic anisotropy is at the origin of the single molecule magnet (SMM) behavior [1–9]. Single molecule magnets are at the forefront of the domain of molecular magnetism because of their potential applications in data storage and quantum computing. Indeed, classical SMMs have a degenerate ground state with two components of opposite magnetization that could be assimilated to the 0 and 1 states of a quantum bit, for which the quantum property of superposition of states could be exploited, paving the way to quantum computing. The property of magnetic anisotropy relates to relativistic effects that induce a lift of degeneracy of the $M_S$ components of the ground spin state $S$, such that the components with the largest magnetization $+M_S$ and $-M_S$ become the ground state. As this phenomenon occurs even in the absence of an external magnetic field, it is called zero-field splitting (ZFS). There are two main ZFS parameters: $D$ and $E$ respectively characterize the axial and rhombic anisotropies. Up to now the blocking temperatures under which the property can be observed are only of a few Kelvins. The exploitation of SMMs for practical applications—as classical or quantum bits of information, for instance—thus relies on the possibility of synthesizing
molecules with higher blocking temperatures and long coherence times [10–12]. In order to achieve high blocking temperatures, several conditions must be fulfilled: (i) The axial parameter $D$ of the ZFS must be negative (by convention) to ensure an easy axis of magnetization. Indeed, a positive value characterizes an easy plane of magnetization and no blocking is observed in the absence of an applied magnetic field [13]; (ii) the absolute value of $D$ must be as large as possible, as it governs the splitting of the $M_s$ components; and (iii) the rhombic parameter $E$ must be strictly zero in order to prevent tunneling. Moreover, $E$ plays also a role on the coherence time as observed experimentally [14,15]. The physical factors governing the sign and magnitude of these parameters are the amplitude of the spin-orbit coupling (SOC) and the symmetry. In symmetry point groups for which the components of the angular momentum (which transform as $R_x$, $R_y$, and $R_z$ in character tables) appear in the same irreducible representation (such as tetrahedral, octahedral, and icosahedral symmetries), the SOC does not lift the degeneracy of the $M_s$ components, and consequently no axial magnetic anisotropy can occur. A lowering of the symmetry is therefore necessary to observe the property. Molecules with the same symmetry but with different electronic configurations of the magnetic ion (different metal ions or different oxidation states) lead to completely different magnetic anisotropies (easy axis or easy plane and with or without rhombic contribution) so that the ways to improve SMMs are far from being intuitive [16–20].

For this purpose, theory may help in providing both analytical derivations and ab initio calculations of the anisotropy parameters in transition metal compounds [19–44]. Many papers have already been devoted to such studies and it has been shown that (i) only a few excited states significantly contribute to single ion magnetic anisotropy [21]; (ii) usually these states are not easy to anticipate from chemical intuition, and calculations are required to identify them and to rationalize their contribution to magnetic anisotropy; and (iii) the energetic order and electronic structure of the excited states can be easily correlated with the ligand field [25]. The present paper shows that as the ligand field strength is weak in high-spin compounds, the rules governing SOC in isolated transition metal ions still prevail in molecular compounds. The identification of the coupled excited states can therefore be done using the Wigner–Eckart theorem and from group theory. Correlating the electronic structure of these states with the ligand field and knowing that their contribution to the ZFS decreases in proportion to their energy difference to the ground state, it becomes possible to anticipate how to improve the property by choosing ligands with appropriate ligand fields. For such a purpose, molecular selection rules based on the symmetry point group are particularly useful as they are more selective than the double group ones, and as they allow one to anticipate which part of the SOC operator, $L_z \hat{S}_z$ or $L_x \hat{S}_x + L_y \hat{S}_y$, is responsible for the coupling between the ground and excited states.

Another aspect of this work concerns the quality of the calculations and their computational cost. Indeed, as the method [21] usually employed to calculate the ZFS parameters goes through the optimization of average orbitals for all the computed excited states, the magnetic orbitals may not be optimal for the lowest-lying electronic states. As a consequence, the account of more excited states in the calculations does not lead to systematic improvements of the results and may even cause a decline in accuracy. The selection of those states that are responsible for magnetic anisotropy allows one to optimize average orbitals for a reduced set of states, leading to both a lower computational cost and an improvement of the quality of the results [21].

The paper is organized as follows. Section 2 sets out the theoretical basis of this study both in (i) recalling the rules that determine the SOC between the ground and excited states in atoms and molecules, and (ii) giving the computational information. Section 3 illustrates how these rules prevail in Co(II) molecular compounds. Starting from a model compound belonging to $D_{3h}$ symmetry point group, we have lowered its symmetry to $C_{3v}$ and changed the ligands to reach the situation that corresponds to a real compound for which experimental data are available. The complexes are studied by means of correlated ab initio calculations including SOC.
2. Selection Rules and Computational Information

2.1. Selection Rules for the Spin-Orbit Coupling in Atoms and Molecules

Symmetry properties of operators are used for a long time in order to improve the computational efficiency and to analyze spectroscopic data. Let us recall the main concepts leading to selection rules. The SOC Hamiltonian can be derived from the Dirac operator and used as a perturbative term in the one-component (Schrödinger) equation. Assuming a spherical potential, the so-defined SOC Hamiltonian for an N-electron system can be written as:

$$\hat{H}_{SOC} = -\frac{e\hbar^2}{2m^2c^2} \sum_i^N \left( \nabla V_i \times \vec{p}_i \right) \cdot \vec{s}_i = -\frac{e\hbar^2}{2m^2c^2} \sum_i^N \frac{1}{r_i} \frac{\partial V_i}{\partial r} \vec{l}_i \cdot \vec{s}_i = \sum_i^N \tilde{\xi}_i (r_i) \vec{l}_i \cdot \vec{s}_i$$

(1)

where $V_i$ is the electrostatic potential felt by electron $i$, $\vec{p}_i$, $\vec{l}_i$, and $\vec{s}_i$ are, respectively, the linear momentum, the angular momentum, and the spin operator of electron $i$. $\tilde{\xi}_i (r_i)$ is a radial operator proportional to the fine structure constant. It should be noted that other terms of lower magnitude such as spin-other-orbit or spin-spin couplings are often included in ab initio calculations as they impact the ZFS magnitude. Nevertheless, in many transition metal complexes, these effects are expected to be much smaller than those of the SOC and can be neglected in analytical derivations [45]. Let us just recall that in the case of small SOC contributions to the ZFS, spin-spin coupling may account for 20% of the total ZFS, e.g., in manganese(II) complexes [46].

The starting point for the derivation of selection rules is the Wigner–Eckart theorem, which allows one to separate the physical content of a tensor operator $T_q^{(k)}$ and its angular dependence.

$$n, J, M|T_q^{(k)}|n', J', M' = (-1)^{J-M} \left( \begin{array}{cc} J & k \\ -M & q \end{array} \right) n||T^k||n', J'$$

(2)

where $T_q^{(k)}$ is the $q^{th}$ component of an irreducible tensor of rank $k$ coupling two states labelled by the quantum numbers $n, J, M$ and $n', J', M'$, where $J, M$ and $J', M'$ are angular momentum quantum numbers, and $n$ and $n'$ are additional quantum numbers required to completely specify the states. Since angular momenta are rank 1 tensor operators, the Wigner–Eckart theorem appears to be useful to study SOC interactions. The 3-$J$ symbol of Equation (2) contains all information about angular dependences (and thus selection rules) and the reduced matrix element does not depend on $M$. The notations are those used in reference [47].

Assuming a spherical symmetry and a Russell–Saunders coupling scheme, a first application of the Wigner–Eckart theorem on the SOC Hamiltonian allows one to re-write the SOC Hamiltonian for atoms as $\hat{H}_{SOC} = A \vec{L} \cdot \vec{S}$ with $\vec{L} = \sum_i \vec{l}_i$, $\vec{S} = \sum_i \vec{s}_i$ and $A$ is the spin-orbit constant [48]. As $A$ has no angular dependence, selection rules are only imposed by the $\vec{L} \cdot \vec{S}$ operator. Then, the application of the Wigner–Eckart theorem leads to the expression [47]:

$$L, S, J, M|\vec{L} \cdot \vec{S}|L', S', J', M' = (-1)^{J+L+S} \delta_{J', M} \delta_{MM'} \left\{ \begin{array}{ccc} L' & S' \\ L & S \end{array} \right\} L||L||L'S||S'$$

(3)

where $J$ is the total angular momentum quantum number (which is a good quantum number for the atom) that parameterizes the total angular momentum resulting from the coupling of the angular and spin momenta. $M$ is the quantum number of its associated component. Equation (3) involves 6-$J$ symbols (in the curly brackets). Selection rules therefore arise from the Kronecker $\delta$ symbols and 6-$J$ symbol properties and are written [47]:

$$\Delta L = 0, \pm 1$$

$$\Delta S = 0, \pm 1$$

$$\Delta J = \Delta M = 0$$

(4)
In most cases, the fine structure of an atom can be well described by taking the SOC interaction only at the first-order of the perturbation theory (interaction of $2S+1L$ terms with themselves), as second-order effects are weaker by orders of magnitude. Nevertheless, as it will be shown in the next section, second-order SOC may be of crucial importance to describe the ZFS in molecules and the selection rules (see Equation (4)) will be helpful to unravel the physics governing the magnetic properties of transition metal complexes.

In molecules, SOC is much more difficult to apprehend. Indeed, the orbital angular momentum $\vec{L}$, well defined in a spherical atom, does not commute with the total Hamiltonian if the symmetry is lowered. Furthermore, one should notice that a non-spherical symmetry implies $\nabla V \neq \frac{1}{2} \frac{\partial V}{\partial r} \vec{r}$, thus the second equality in Equation (1) is not valid anymore. Nevertheless, the Hamiltonian commutes with the symmetry operators of the symmetry point group to which the molecule belongs. Information about the total orbital angular momentum of an electronic state is therefore contained in the spatial symmetry, i.e., the irreducible representation $\Gamma$ of this state. The derivation of selection rules for SOC in molecules also relies on the Wigner–Eckart theorem, and can be found written in different ways. We use here the notation and the rules derived in [49]. The authors derived SOC selection rules for both the double group and point group formalisms. Despite the fact that the Co(II) complex studied here has a half-integer spin, we chose to use the symmetry point group formalism for reasons that will be clarified later. The wave functions of the spin-free electronic states can be written as $|\Gamma, S, M_S\rangle$, where $\Gamma$ is an irreducible representation of the molecular symmetry point group of the considered state, and $S, M_S$ are the spin quantum numbers. The SOC Hamiltonian used here is the phenomenological $\hat{H}_{\text{SOC}} = A \vec{L} \cdot \vec{S}$ as we wish to correlate the SOC in magnetic complexes and in atoms. For symmetry based selection rules, the matrix elements to evaluate are $\Gamma, S, M_S |\vec{L} \cdot \vec{S}| \Gamma', S', M'_S$. The application of the Wigner–Eckart theorem on the spin part of the Hamiltonian leads to the expression [49]:

$$
\Gamma, S, M_S |\vec{L} \cdot \vec{S}| \Gamma', S', M'_S = \sum_{q=-1}^{1} (-1)^q \begin{pmatrix} S & 1 \\ -M_S & q \end{pmatrix} \Gamma, S |\vec{L}_{-q} \cdot \vec{S}| \Gamma', S' \tag{5}
$$

where $q$ is a component of the angular momentum operator $\vec{L}$ in spherical coordinates. The spin operator in the right hand side reduced matrix element of Equation (5) is now invariant under rotation. From this expression, the following selection rules can be extracted:

$$
\Delta S = 0, \pm 1 \\
\Delta M_S = 0, \pm 1 \\
\Gamma \otimes \Gamma_{L_q} \otimes \Gamma' \ni \Gamma_1 
$$

The two first rules on spin quantum numbers are a consequence of the properties of the $3J$ symbols. The last selection rule arises from the reduced matrix element. As the spin operator is now a scalar invariant under symmetry transformations, the selection rule only depends on the symmetry of the $\vec{L}$ operator. In the double group formalism, $\vec{L} \cdot \vec{S}$ belongs to the totally symmetric irreducible representation. Thus the selection rule for SOC in double group formalism is $\Gamma = \Gamma'$ and it will be shown that it is less restrictive than symmetry point group rules. Another main reason for using point group rules instead of the double group ones is that our goal is to provide magneto-structural correlations, as the geometry of a molecule can be chemically controlled by the choice of appropriate ligands. Finally, one may note that the half-integer spin is fully accounted for by the Wigner–Eckart theorem [49].

In this article, we only study transition metal complexes having orbitally non-degenerate ground states, as the ZFS Hamiltonian is only defined in this context. However, it is worth noting that the rules presented above also apply to orbitally degenerate ground states.
2.2. Computational Information

Calculations have been performed with the Molcas 7.8 package [50–52]. The following ANO-RCC basis sets are used: (6s5p3d2f1g) for Co, (4s3p2d1f) for N, (3s2p1d) for C, (5s4p2d1f) for Cl and (2s) for H. Calculations proceed in two steps. In the first step, the energies and wave functions of the ground and excited states are computed at the CAS(7,10)SCF level, i.e., a double d shell is used, involving the 3d orbitals of the Co(II) ion and additional more diffuse d orbitals. Then the CASSCF wave function spin-components are coupled through spin-orbit interactions to form the state-interaction spin-orbit matrix (SO–SI method) [53]. The parameters of the ZFS are extracted from the computed spin-orbit energies and wave functions using the effective Hamiltonian theory [54,55], as explained in details in reference [53].

3. Results and Discussion

The main goals of this section are to illustrate: (i) How the physics of high-spin molecular complexes is reminiscent of that of the atom. For this purpose, it will be shown on a [Co(NCH)3]2+ model complex belonging to the $D_{3h}$ symmetry point group that the main spin-orbit coupling effects arise from electronic states issued from atomic terms, which are coupled though SOC in the Co(II) ion. (ii) How the various selection rules presented in the previous section are selective for the calculation of the ZFS of a real complex. For this second study, geometrical distortions and chemical substitutions were imposed to the model complex to reach the geometry of the real [Co(Me₆tren)(Cl)]⁺ one [18]. Starting from the initial $D_{3h}$ geometry (with $d_{Co-N}$ fixed to 2 Å; note that $d_{Co-N} = 2.15$ Å in the real compound, see Figure 1), we applied a progressive angular deformation by varying the angle $\alpha$ between the three equatorial NCH ligands and the xOy plane. The symmetry was thus lowered from $D_{3h}$ to $C_{3v}$. $\alpha$ was increased until 9° and then the NCH ligand located on the z axis was replaced by a Cl atom.

![Figure 1. (a) Lowest spin-orbit free states of [Co(NCH)3]2+ model complex of $D_{3h}$ symmetry computed at the CASSCF level; (b) $^4F$ spectrum (see text) of the lowest spin-orbit states of [Co(NCH)3]2+ model complex of $D_{3h}$ symmetry as a function of $d_{Co-N}$ computed at the spin-orbit state-interaction (SO–SI) level.](image)

3.1. Reminiscence of the Physics of the Atom in the Molecular Spectrum

As we are interested in magnetic properties, the ligand field must be weak enough to generate a high-spin ground state. In the chosen molecular compound, a weak ligand field is created by linear NCH ligands and the complex is studied for various Co–N bond lengths ranging from 2 (weak ligand field) to 3.5 Å (negligible field). Figure 1a shows the evolution of the electronic spectrum as a function of $d_{Co-N}$. 
Each molecular electronic state can easily be related to an atomic term. We will focus on those molecular electronic states that can be related with the $4^F$, $4^P$, and $2^G$ atomic spectroscopic terms for different reasons. Firstly, the other excited states are higher in energy and their effect on the lowest energy spectrum through SOC is negligible (see the various spectra given in Supporting Information). Secondly, the states coming from $4^F$ and $4^P$ are well separated in energy, and the $4^P$ and $2^G$ terms, despite having different spins, possess similar energies. Finally, as the $2^G$ is coupled to the $4^F$ through SOC while the $4^P$ is not (see selection rules in Equation (4)), the discussion can be limited to these terms for illustrating the idea proposed in this section, i.e., the selection rules for SOC in the isolated metal ion are not (or at least just partially) quenched by the weak applied ligand field. It can be noted that calculations have been performed with all the states of the $d^7$ configuration and the results show that contributions of the other excited states to the low energy spin-orbit states are negligible. Since we are interested in the effect of SOC between $4^F$ and excited states issued from the $4^P$ and $2^G$ atomic terms, we need first to account for the effect of SOC between the states coming from the $4^F$ term. Let us first define what we call the $4^F$-SO spectrum. The $4^F$ term is split in the four levels $4^F_{9/2}$, $4^F_{7/2}$, $4^F_{5/2}$, and $4^F_{3/2}$ by the spin-orbit coupling giving rise to 28 components that can be obtained by the diagonalization of the SOC Hamiltonian matrix when only the 7 spin-orbit free states issued from the $4^F$ term are taken into account. In the same way, we define the $(4^F + 4^P)$ SO spectrum (respectively the $(4^F + 2^G)$ SO spectrum), i.e., the lowest 28 components of the spin-orbit states (levels) obtained when the $4^F + 4^P$ (respectively $4^F + 2^G$) states coming from $4^F$ and $4^P$ (respectively $2^G$) terms are included in the spin-orbit state-interaction matrix. The $4^F$ SO spectrum is depicted in Figure 1b. One may notice that the $4^F_{9/2}$, $4^F_{7/2}$, $4^F_{5/2}$, and $4^F_{3/2}$ are split by the ligand field in, respectively, 5, 4, 3, and 2 molecular spin-orbit states, each of them being degenerate due to Kramer’s theorem. The three computed spectra ($4^F$ SO, $(4^F + 4^P)$ SO and $(4^F + 2^G)$ SO) are very similar and their plots only show small differences (the spectra are given in Tables S1–S3 in Supporting Information). We define $\Delta_{(4F+4P)-(4F)}$ and $\Delta_{(4F+2G)-(4F)}$ as the sum of the energy shifts (in absolute values, see Tables S4 and S5) experienced by the 14 spin-orbit states between the $4^F$ SO spectrum and the $(4^F + 4^P)$ SO and $(4^F + 2^G)$ SO spectra, respectively. The values of $\Delta$ reflect the SOC effects of the states coming from the $4^P$ or $2^G$ terms on those issued from the $4^F$ term. $\Delta_{(4F+4P)-(4F)}$ and $\Delta_{(4F+2G)-(4F)}$ as a function of $d_{Co-N}$ are shown in Tables S6 and S7 and Figure S1. The values of $\Delta$ when the ligand field is negligible ($d_{Co-N} = 3.5$ Å) are in agreement with the selection rules for the isolated atom. $\Delta_{(4F+4P)-(4F)}$ is equal to 0 because the $4^F$-4P SOC is not allowed. On the other hand, the $4^F$-2G coupling is allowed and $\Delta_{(4F+2G)-(4F)}$ is quite large ($\approx 600$ cm$^{-1}$). When the ligand field increases, $\Delta_{(4F+4P)-(4F)}$ increases to $\approx 40$ cm$^{-1}$ and $\Delta_{(4F+2G)-(4F)}$ slowly decreases to reach $\approx 450$ cm$^{-1}$ at $d_{Co-N} = 2$ Å. For a ligand field of this magnitude, the SOC between electronic states coming from the $4^F$ and $4^P$ atomic terms is very small in comparison to the one between states coming from $4^F$ and $2^G$ atomic states. One should keep in mind that the $4^P$ state leads to three spin-free states while the $2^G$ leads to nine spin-free states, however these different degeneracies cannot explain alone such differences in the SOC magnitude. The main result here is that the SOC strength between the molecular ground state (GS) and excited states (ES) can be ranked as $GS(4^F) - ES(4^F) > GS(4^F) - ES(2^G) > GS(4^F) - ES(4^P)$. In other words, the main effect of the SOC in the molecular electronic states stem from those related to the atomic $4^F$ and $2^G$ states, while those coming from the $4^P$ state can be neglected.

### 3.2. Selection Rules for the Calculation of the ZFS in Molecular Complexes

Let us now focus on the ZFS of molecular complexes. Both model complexes (on which progressive distortions were applied) and the real complex [Co(Me$_2$tre)]$^+$, previously studied by the authors [18], have been theoretically investigated. All these complexes are depicted in Figure 2 where the calculated $D$ values are reported. The low energy spectrum and each excited-state contribution to $D$ are also shown.
As we only deal with quartet and doublet states, the two first selection rules are not selective in 
(or pseudo) vector under symmetry operations, group theory enables one to evaluate whether or 

Indeed, in the $D_{3h}$ symmetry point group, the model complex exhibits an easy-plane type magnetic anisotropy ($D > 0$). The main contribution to $D$ comes from the SOC between the $^4A_2'$ ground state and the excited $^4E''$ state which provides a positive contribution to $D$. Indeed, in the $D_{3h}$ symmetry point group, $\hat{L}_x$ and $\hat{L}_y$ span the $E''$ irreducible representation and the tensor product $A_2' \otimes E'' \otimes E'' = A_1' \oplus A'_2 \oplus E'$ contains the totally symmetric irreducible representation. Another non-negligible contribution comes from the $^2A'$ issued from the $^2G$ term. The interaction is now brought by the $L_z \hat{S}_z$ part of $\hat{H}_{SOC}$ ($L_z$ spans the $A_2'$ irreducible representation and $A_2' \otimes A'_2 \otimes A'_1 = A'_1$). In this symmetry (and for the four depicted excited states), no other coupling

**Figure 2.** Structure of studied complexes and their calculated axial anisotropy parameter $D$ (top). Low energy spectrum of the spin-orbit free states and contributions (in cm$^{-1}$) to $D$ of each excited states (bottom). Red arrows indicate couplings between the states through the $\hat{L}_z \hat{S}_z$ operator while blue arrows indicate couplings through the $L_z \hat{S}_x + L_y \hat{S}_y$ operator.

### 3.2.1. Molecular Selection Rules Based on the Symmetry Point Group

Let us first analyze the results on the basis of molecular selection rules (see Equation (6)). We use here the approximation that the ligand field effects are much stronger than the SOC ones, which allows us to treat SOC in a perturbative way. This is well verified for first row transition metal complexes. As we only deal with quartet and doublet states, the two first selection rules are not selective in the present case and only the last rule is important. Expressing the SOC Hamiltonian in Cartesian coordinates $\hat{H}_{SOC} = \mathcal{A} (\hat{L}_x \hat{S}_x + \hat{L}_y \hat{S}_y + \hat{L}_z \hat{S}_z)$ and noting that the $\hat{L}_z$ operator transforms like an axial (or pseudo) vector under symmetry operations, group theory enables one to evaluate whether or not an excited state is coupled to the ground state. It also allows one to determine from which part ($\hat{L}_x \hat{S}_x$, $\hat{L}_y \hat{S}_y$, or $\hat{L}_z \hat{S}_z$) of $\hat{H}_{SOC}$ the coupling occurs. In complex with an axial symmetry of order greater than two, $\hat{L}_x$ and $\hat{L}_y$ belong to the same irreducible representation. Furthermore, as already observed in the case of pentacoordinated Co(II) complex [18,56] with a $C_3$ axis, for states with same (respectively different) spin multiplicity, if the coupling occurs through the $\hat{L}_z \hat{S}_z$ part of $\hat{H}_{SOC}$ the coupling between the ground and excited states leads to a negative (respectively positive) contribution to $D$, while a coupling caused by $\hat{L}_y \hat{S}_y + \hat{L}_z \hat{S}_x$ leads to a positive (respectively negative) contribution.
is symmetry allowed. As the symmetry is lowered to $C_{3v}$, the $D$ value decreases and becomes negative for the last complex, indicating a switch from easy plane to an easy axis type anisotropy. Note that the anisotropy of the [Co(NCH)$_3$Cl]$^+$ model complex with $\alpha = 9^\circ$ is in qualitative agreement with that of the [Co(Me$_8$tren)(Cl)]$^+$ complex despite the differences between them. Electron paramagnetic resonance (EPR) spectroscopy studies on [Co(Me$_8$tren)(Cl)]$^+$ gave $D = -8.12$ cm$^{-1}$. The decrease of $D$ as the distortion increases can easily be explained by noting that, while both couplings between the $^4A_2$ GS and the excited $^4E$ (4$E''$ in $D_{3h}$) and $^2A_1$ ($^2A'_1$ in $D_{3h}$) states still leads to a positive contribution to $D$, the coupling between the $^4A_2$ and the $^4A_1$ ($^4A''_2$ in $D_{3h}$) states is now allowed through the $\hat{L}_z\hat{S}_z$ part of $\hat{H}_{SOC}$ ($\hat{L}_z$ spans the $A_2$ irreducible representation and $A_2 \otimes A_2 \otimes A_1 = A_1$) and contributes negatively to $D$.

3.2.2. Molecular Selection Rules Based on the Double Group Theory

We have focused here on the [Co(NCH)$_3$Cl]$^{2+}$ model complex with $D_{3h}$ symmetry but the same reasoning could be applied to the $C_{3v}$ complexes. Figure 3 shows the low energy electronic (O(3)) and spin-orbit (O(3)$^*$) spectra for the isolated ion and electronic ($D_{3h}$) and spin-orbit ($D_{3h}^*$) spectra of the molecular complex. All molecular electronic states can be correlated with an atomic term. The GS and the ground state $E_{1/2}$ is split into $E_{1/2}$ and $E_{3/2}$ in the $D_{3h}^*$ double group under the effect of the SOC. The ZFS is then described by the energy difference between $E_{1/2}$ and $E_{3/2}$ ($M_S = \pm 1/2$) and $E_{3/2}$ ($M_S = \pm 3/2$). The ground states $E_{1/2}$ and $E_{3/2}$ in $D_{3h}^*$ are coming from the $^4F_{9/2}$ in O(3)$^*$ and the ground state $^4A'_2$ is issued from the atomic $^4F$ term in $D_{3h}$. As can be seen in the column $D_{3h}^*$, the excited states which have the same symmetry as the two lowest states in the double group are numerous and selection rules of the double group are therefore less restrictive than those of the symmetry point group.

3.2.3. Atomic Selection Rules

Finally, we can link the molecular selection rules for SOC with the atomic ones. In $D_{3h}$ symmetry point group and according to the symmetry based selection rule, the $^4A_2$ ground state can only be coupled with states of $^2A'_1$ ($\hat{L}_z\hat{S}_z$) and $E''$ ($\hat{L}_z\hat{S}_z + \hat{L}_y\hat{S}_y$) symmetries. Under a $D_{3h}$ ligand field, the $^4P$ term is split into $^4A_2 \oplus ^4E''$. Calculations show that only the $^4E''$ state is coupled to the GS and gives a positive contribution to $D$ of 0.58 cm$^{-1}$. The $^2G$ state in $D_{3h}$ symmetry reduces as $^2A'_1 \oplus ^2E' \oplus ^2A''_1 \oplus ^2A''_2 \oplus ^2E''$. As expected, the $^2A'_1$ and $^2E''$ states are coupled to the GS. Their contributions to $D$ are, respectively, 13.02 and $-3.03$ cm$^{-1}$. The contribution of $^4E''$ ($^4P$) is one order of magnitude weaker than the contributions of $^2A'_1(2G)$ and $^2E''(2G)$ The SOC strength, and thus the contributions of excited states to $D$, therefore strongly depends on the atomic origin of the molecular state, and the almost negligible contribution of $^4E''$ ($^4P$) to $D$ can be attributed to the atomic selection rules (Equation (4)). Indeed, we expect that the $^4E''$ ($^4P$) contribution will decrease if we lower the ligand field as the contribution of the $^4P$ term must reach zero for negligible ligand field. These couplings are summarized in Figure 3.
3.3. Rationalization of the ZFS Nature

The energetic order of the d orbitals is given in Figure 4, as well as the excitation processes giving rise to the spin-orbit couplings and the determinants of the excited states that are coupled through SOC to the main determinant of the ground state. The information useful to improve the nature and magnitude of the ZFS can easily be extracted from the nature of the determinants involved in the SOC and the sign of their contribution to \( D \). From a simple analysis of the here-reported theoretical results, the following recommendations can be stated:

(i) If an easy axis of magnetization is needed (negative \( D \) value), the symmetry lowering from \( D_{3h} \) to \( C_{3v} \) is beneficial because it allows a coupling with the first excited state that brings a negative contribution to \( D \).

(ii) In order to obtain a more negative overall \( D \) value, one can decrease its positive contribution by destabilizing the \( ^4E(C_{3v}) \) excited state. As the main determinant of this state coupled to the ground state has a double occupancy in the \( d_x^2 \) orbital, ligands with a strong field in axial positions would be appropriate to do so.

(iii) Finally, one may question the role of the chemical substitution by chlorine. To answer this query and separate the role of the distortion brought by the change of the value of the angle \( \alpha \) from that of the electronic effect of chlorine, we have also substituted an axial NCH ligand in a slightly distorted (\( \alpha = 3^\circ \)) complex. In both cases (\( \alpha = 3^\circ \) and \( \alpha = 9^\circ \)), the main effect comes from the first excited state that for chlorine has a two-fold stronger coupling (see Figure S2) to the ground state, resulting in a much larger negative contribution to \( D \). From this last observation, one may learn that not only the energy differences between the states (diagonal elements of the

**Figure 3.** Schematic (not scaled) energy spectrum. As mixing of states with same symmetry in the \( D_{3h}^* \) are possible only a few dashed lines are indicated to guide the eyes. Blue plain line arrows indicate allowed couplings between states, the dotted arrow indicates a coupling allowed at the molecular level but forbidden in the atom. Red, green and purple lines respectively indicate \( E_{3/2}, E_{1/2} \) and \( E_{5/2} \).
state interaction matrix) but also the magnitude of the coupling (off diagonal elements which are proportional to the fine structure constant and depend on the chemical nature of the ligand, i.e., electronic effect) can be tuned with the choice of appropriate ligands.

\[ ^4E''(D_{3h}) ; ^4E(C_{3v}) \quad ^2A'_{1}(D_{3h}) ; ^2A_{1}(C_{3v}) \quad ^4A''_{1}(D_{3h}) ; ^4A_{1}(C_{3v}) \]

![Diagram](image)

**Figure 4.** All depicted excited states are multireference. Only the main determinants of the ground (bottom) and excited states coupled through SOC are represented. The labels and energetic order of the d orbitals are indicated. Only one of the two determinants equivalent by left-right symmetry is represented. The excitation leading to these excited states and the part either \( L_z \hat{S}_z \) (purple arrow) or \( L_z \hat{S}_z + L_y \hat{S}_y \) (red arrow) of the spin-orbit coupling (SOC) operator which is involved are also depicted.

4. **Summary**

For weak ligand field complexes the spin-orbit spectrum is dominated by the SOC between the states issued from the ground atomic term. The most important coupling with excited states issued from other terms essentially fulfills the atomic selection rule.

Although the ZFS is a very fine effect introducing tiny energy differences between \( M_S \) components of the high-spin ground state, the reminiscence of the physics of the atom in the molecular complex is still present. An appropriate a priori selection of these states may lead to both (i) a computational gain as the size of the state-interaction matrix can be reduced, and (ii) a gain in quality of the ab initio results as the number of states used in the average optimization of the orbitals may be reduced to its bare essential. Finally, as theory may guide the synthesis of molecular complexes with targeted magnetic anisotropy, the main object of this work concerns the possible rationalization of the magnitude and nature of the ZFS from analytical derivation using second-order perturbation theory. Regarding this peculiar aspect, the selection of the states that will bring the main contributions to the ZFS is crucial. For this purpose, we have analyzed the selectivity of the various selection rules derived from the Wigner–Eckart theorem. The main conclusions are:

(i) The atomic selection rules are essentially fulfilled. The contribution to \( D \) of the single excited state that is coupled to the ground state in the molecular complex but not in the atom is only 0.58 cm\(^{-1}\) and can be safely neglected in any attempt of rationalization of the SOC nature.

(ii) The double group selection rule is less restrictive than the symmetry point group ones.

(iii) From the symmetry point group selection rules, one may not only determine the excited states that are coupled to the ground state but also identify which part of the SOC operator, \( L_z \hat{S}_z \) or \( L_z \hat{S}_z + L_y \hat{S}_y \), is responsible for the coupling and therefore the sign of their contribution to \( D \).
Supplementary Materials: The following are available online at www.mdpi.com/2312-7481/2/3/31/s1: Table S1: 4F SO spectrum (cm⁻¹), Table S2: (4F + 4P) SO spectrum (cm⁻¹), Table S3: (4F + 2G) SO spectrum (cm⁻¹), Table S4: Difference between (4F) and (4F + 4P) SO spectra (cm⁻¹), Table S5: Difference between (4F) and (4F + 2G) SO spectra (cm⁻¹), Table S6: ∆(4F + 4P) – (4F) (cm⁻¹), Table S7: ∆(4F + 2G) – (4F) (cm⁻¹), Figure S1: ∆(4F + 4P) – (4F) (blue) and ∆(4F + 2G) – (4F) (red) as a function of dC_o-N, Figure S2: Most important contributions to D for the [Co(NCH3)4Cl]⁺ (α = 3°) complex.

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Abbreviations

The following abbreviations are used in this manuscript:

ZFS Zero-Field Splitting
CASSCF Complete Active Space Self-Consistent Field
SO–SI Spin-Orbit State Interaction
SOC Spin-orbit coupling

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