



Article Event-Triggered and Memory-Based Sliding Mode Variable Structure Control for Memristive Systems

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Abstract: This paper is concerned with a novel event-triggered sliding mode variable structure control (ESMC) scheme to achieve robust stabilization of memristive systems (MSs). First, a memory-based sliding surface, including the past and the current information of the system states, is introduced. Two switching gain matrices of such kinds of switching surfaces, which satisfy the guaranteed cost performance of the sliding reduced order dynamics, are achieved by employing linear matrix inequality techniques. Second, a sliding mode controller using an event-triggered mechanism is constructed to ensure that the trajectories of the uncertain MS slide towards the proposed memory-based switching hyperplane, and thus, the stabilization of entire MSs is reached. Finally, the effectiveness of the proposed results is demonstrated through simulations.

Keywords: sliding mode variable structure control (SMC); event-triggered control; memristive system (MS); guaranteed cost performance

1. Introduction

It is well known that there are three usual fundamental circuit elements, i.e., resistors, capacitors and inductors. Now, the so-called fourth circuit element, namely the memristor, has attracted increasing attention from scientists and engineers due to its potential applications in many engineering fields, such as super-dense nonvolatile computer memories, chaotic systems, neural networks, and so on [1–8]. On the other hand, sliding mode variable structure control (SMC) has been verified to be an efficient and pretty popular robust control technique since it owns some well-known and strong properties in disturbance rejection and insensitivity to model uncertainties and parameter variations occurring in dynamical systems [9–15]. Many works on linear-matrix-inequality (LMI)-based SMC design, such as [16–23], form the base of LMI formulations utilized in SMC design. So far, there exists a number of results on the SMC of memristive circuits [24–27]. In the very recent paper [24], on the basis of the nonlinear Takagi–Sugeno fuzzy model, robust stabilization of uncertain memristive chaotic systems was investigated. In the literature [25], the chaotic control via a terminal SMC technique is proposed to deal with memristive oscillators, as well as Chua's oscillators with memristors. In [26,27], the authors discussed two kinds of approaches to adaptive sliding mode synchronization for no-equilibrium memristive systems.

Recently, the mechanism of event-triggering has been regarded as one of the pretty useful and challenging techniques for control design since it can achieve control objectives with the minimum resource usage. For networked control systems [28], it also provides a beneficial way for decreasing network loads when data-packets are transmitted from different information

processing terminals [29–35]. Meanwhile, it also turns out that the communication with the aperiodic event-triggered mechanism is quite useful, where the measurement errors play important roles in the design of the event [36–39]. In addition, the event-triggered-based SMC, developed in [40], can make the system steady-state bound be independent of both the intervals of samplings and the bounds of disturbances.

In order to reduce the costs for controlling MSs, an important way is to adopt an event-triggered scheme. However, few related results have been reported in the literature, and what is more, no results have been presented to stabilize an MS by integrating the advantages of SMC, event-triggered schemes and memory-based techniques. In this paper, the robust stabilization issue based on an ESMC scheme is investigated for MSs. The major contribution is given as follows. First, a linear time-invariant state space model is established for the Chua's system with a memristor. Then, applying the current and the past information of MS states, a memory-based switching hyperplane is constructed, and its gains matrices, considering the guaranteed cost performance of the dynamics in the process of sliding modes, are achieved by using LMI techniques. Subsequently, an ESMC scheme is constructed such that the states of the memristive system are able to be repelled towards the desired memory-based switching manifold. Finally, robust stabilization of the entire MS is fulfilled, whose advantages and effectiveness have been verified through simulation results.

2. Description of Chua's Circuits with Memristors

Usually, the memristor is described by the following nonlinear mathematical functions [2-4,41]:

$$i = f(\phi)v,\tag{1}$$

or:

$$v = g(q)i \tag{2}$$

where $d\phi = vdt$, dq = idt, i(v) is the terminal current (voltage). The memductance $f(\phi)$ and the memristance g(q) are nonlinear functions, which are mathematically described as:

$$\begin{cases} f(\phi) := \frac{\mathrm{d}q(\phi)}{\mathrm{d}\phi} \ge 0, \\ g(q) := \frac{\mathrm{d}\phi(q)}{\mathrm{d}q} \ge 0 \end{cases}$$
(3)

Mathematically, $q(\phi)$ and $\phi(q)$ are described as the following nonlinear functions [2–4,41]:

$$q(\phi) = \begin{cases} a_1 - a_2 + a_2\phi, & \text{if } \phi > 1\\ a_1\phi, & \text{if } -1 \le \phi \le 1\\ a_2 - a_1 + a_2\phi, & \text{if } \phi < -1 \end{cases}$$
(4)

and:

$$\phi(q) = \begin{cases} a_3 - a_4 + a_4 q, & \text{if } q > 1\\ a_3 q, & \text{if } -1 \le q \le 1\\ a_4 - a_3 + a_4 q, & \text{if } q < -1 \end{cases}$$
(5)

where $a_i > 0$, $i = 1, \dots, 4$. They obviously have the piecewise-linear and monotone-increasing property, and one can consequently easily see that [2,4,8,24,41]:

$$f(\phi) = \frac{\mathrm{d}q(\phi)}{\mathrm{d}\phi} = \begin{cases} a_1, & |\phi| \le 1, \\ a_2, & |\phi| > 1, \end{cases}$$
(6)

and:

$$g(q) = \frac{d\phi(q)}{dq} = \begin{cases} a_3, & |q| \le 1, \\ a_4, & |q| > 1. \end{cases}$$
(7)

Figure 1 shows a typical MS. One can briefly describe the dynamical circuit system in Figure 1 as dynamical Equation (8) according to the basic Kirchhoff circuit laws [2,4,5]:

$$\begin{cases}
C_1 \frac{dv_1}{dt} = Gv_1 + \frac{v_2 - v_1}{R} - f(\phi)v_1 \\
C_2 \frac{dv_2}{dt} = \frac{v_1 - v_2}{R} - i \\
L \frac{di}{dt} = v_2 - ri \\
\frac{d\phi}{dt} = v_1
\end{cases}$$
(8)

As done in [42–44], the control input $\breve{u}(\phi(t))$ can be added to MS (8) to solve the stabilization problem, and the system is described as:

$$\dot{x} = \check{A}(x)x + B\check{u} \tag{9}$$

where
$$x = \begin{bmatrix} v_1 \\ v_2 \\ i \\ \phi \end{bmatrix}$$
, $\check{A} = \begin{bmatrix} \frac{GR - 1 - f(x_4)R}{C_1R} & \frac{1}{C_1R} & 0 & 0 \\ \frac{1}{C_2R} & -\frac{1}{C_2R} & -\frac{1}{C_2} & 0 \\ 0 & \frac{1}{L} & -\frac{r}{L} & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}$, $B \in R^{4 \times m}$, m is the dimension of the

control input.

On the basis of the mathematical Equation (6), one can arrange the MS (7) as:

$$\dot{x} = A_1 x + B u_1$$
, when $|x_4| \le 1$, or $\dot{x} = A_2 x + B u_2$, when $|x_4| > 1$, (10)

where
$$A_l = \begin{bmatrix} \frac{(G-a_l)R-1}{C_1R} & \frac{1}{C_1R} & 0 & 0\\ \frac{1}{C_2R} & -\frac{1}{C_2R} & -\frac{1}{C_2} & 0\\ 0 & \frac{1}{L} & -\frac{r}{L} & 0\\ 1 & 0 & 0 & 0 \end{bmatrix}$$
, $l = 1, 2$.



Figure 1. Memristive systems.

The system can be further represented as:

$$\dot{x} = (A + \delta A(t))x + Bu \tag{11}$$

where
$$A = \begin{bmatrix} \frac{(2GR-1)-(a_1+a_2)R}{2C_1R} & \frac{1}{C_1R} & 0 & 0\\ \frac{1}{C_2R} & -\frac{1}{C_2R} & -\frac{1}{C_2} & 0\\ 0 & \frac{1}{L} & -\frac{r}{L} & 0\\ 1 & 0 & 0 & 0 \end{bmatrix}$$
, and $\delta A(t)$ satisfies $\delta A(t) = DF(t)E$ with

 $D = [1 \ 0 \ 0 \ 0]^T, E = [\frac{a_2 - a_1}{2C_1} \ 0 \ 0 \ 0] \text{ and } F(t) = \begin{cases} 1 & \text{if } |x_4| \le 1 \\ -1 & \text{if } |x_4| > 1 \end{cases}$. It is obvious to see that F(t) is related

to the piece-wise linear characteristic caused by the memristor, and it also satisfies $|F(t)| \le 1$.

Further, $\delta A(t)$ here can also be used to describe the existing uncertainties about the values of the resistors, inductors and capacitors by selecting proper matrices *D* and *E* [24,42], and $\xi(t)$ can be modeled as the unknown bounded external disturbance.

Without lose of generality, MSs are represented by the dynamical model:

$$\dot{x} = (A + \delta A)x + B(u + \xi), \tag{12}$$

where $x \in \mathbb{R}^n$ is the systems state and $u \in \mathbb{R}^m$ is the control input. $\xi \in \mathbb{R}^m$ satisfies $\sup_{t\geq 0} |\xi(t)| \leq \overline{d}$ for all the evolution time of the memristive system, and \overline{d} is a bounded and known constant.

The dynamical system (12) has the standard form by a nonsingular state transformation $x(t) = T^{-1}z(t)$,

$$\dot{z} = (\bar{A} + \delta \bar{A})z + \bar{B}(u + \xi), \tag{13}$$

where $[\bar{A}, \delta \bar{A}] = T [A, \delta A] T^{-1}$, $\bar{B} = [0 \ \bar{B}_2]^T$ with $\det(\bar{B}_2) \neq 0$.

Assumption 1. The unknown model uncertainty $\delta \bar{A}(t)$ is time-varying mismatched and follows:

$$\delta \bar{A}(t) = \bar{D}F(t)\bar{E},\tag{14}$$

where $\overline{D} = TD$, $\overline{E} = ET^{-1}$ are known matrices and F(t) satisfies $det(F(t)) \le 1$. They are all assumed to be proper dimensions in this paper.

Let us choose the variables $z_1 \in \mathbb{R}^{n-m}$, $z_2 \in \mathbb{R}^m$, and denote $z = [z_1^T, z_2^T]^T$, then the dynamic Equation (13) can be changed to:

$$\dot{z_1} = (\bar{A}_{11} + \delta \bar{A}_{11})z_1 + (\bar{A}_{12} + \delta \bar{A}_{12})z_2 \tag{15}$$

$$\dot{z}_2 = (\bar{A}_{21} + \delta \bar{A}_{21})z_1 + (\bar{A}_{22} + \delta \bar{A}_{22})z_2 + \bar{B}_2(u + \xi)$$
(16)

where $\delta \bar{A}_{11} = \bar{D}_1 F(t) \bar{E}_1$, $\delta \bar{A}_{12} = \bar{D}_1 F(t) \bar{E}_2$, $\delta \bar{A}_{21} = \bar{D}_2 F(t) \bar{E}_1$, $\delta \bar{A}_{22} = \bar{D}_2 F(t) \bar{E}_2$, $\bar{D} = [\bar{D}_1^T \ \bar{D}_2^2]^T$ and $\bar{E} = [\bar{E}_1 \ \bar{E}_2]$. Denote:

$$e(t) = z(t) - z(t_i),$$
 (17)

and further:

$$e(t-d) = z(t-d) - z(t_i - d).$$
(18)

We obviously get that $e_j(t) = z_j(t) - z_j(t_i)$ and $e_j(t-d) = z_j(t-d) - z_j(t_i-d)$, j = 1, 2. Let $\bar{e}(t) = [e^T(t) e^T(t-d)]^T$, and we define the event-driven mechanism in this paper as follows:

$$|\bar{e}(t)| \le \sigma |\bar{z}(t_i)| \tag{19}$$

where $\bar{z}(t_i) = [z^T(t_i), z^T(t_i - d)]^T$ and $\sigma \in (0, 1)$ is a given event-triggering constant.

The main objective in our paper is to develop the memory-based and event-driven SMC design to achieve the robust stabilization with the guaranteed cost performance index for the uncertain MS (13).

3. Main Results

3.1. Switching Hyperplane Design

According to the theory of SMC, its design includes two steps: one is to design a proper switching surface s(t) = 0 (as we select in (20)) such that the sliding mode reduced order dynamics (as we presented in (23)) is stable with some specified control performance; the other is to develop a reaching control law for guaranteeing the reachability of s(t) = 0 and subsequently starting the process of sliding dynamics.

In this paper, we select the following memory-based switching manifold:

$$s(t) = z_2(t) - Kz_1(t) - K_d z_1(t-d),$$
(20)

where $K \in R^{m \times (n-m)}$ and $K_d \in R^{m \times (n-m)}$ are two gain matrices to be designed, and the memory parameter d > 0.

Let s(t) = 0; we have:

$$z_2(t) = K z_1(t) + K_d z_1(t-d).$$
(21)

Now, the reduced order system constructed by (15) and (20) can be considered as the dynamic system (15) regarding $z_1(t)$ and $z_2(t)$ in (21). As a result, the design issue of the sliding surface s(t) is converted into that of the solution of the control gains K and K_d .

For the control gain design, we consider the following performance index:

$$J = \int_0^\infty [z_1^T(w)Q_1 z_1(w) + z_2^T(w)R_1 z_2(w)]dw$$
(22)

where Q_1 and R_1 are given positive definite symmetric matrices.

Remark 1. Such a performance index J in (22) can be regarded as the guaranteed cost performance index for MS (15) with the virtual control input z_2 . As a consequence, how to design the sliding surface (20) with the performance index (22) is converted into the design of the control gains K, K_d satisfying the so-called guaranteed cost performance index.

The purpose of selecting the memory-based switching hyperplane lies in that the control system performance index *J* can be improved by the added memory parameter K_d , and also, the dynamical system behaviors can be improved.

Now, taking $z_2(t) = Kz_1(t) + K_d z_1(t - d)$ into (15), one can easily achieve the dynamics of sliding mode:

$$\dot{z}_1(t) = \bar{\mathbb{A}}_1 z_1(t) + \bar{A}_{12} K_d z_1(t-d) + \delta \bar{\mathbb{A}}_2 z_1(t) + \delta \bar{A}_{12} K_d z_1(t-d)$$
(23)

where $\bar{\mathbb{A}}_1 = \bar{A}_{11} + \bar{A}_{12}K$, $\delta \bar{\mathbb{A}}_2 = \delta \bar{A}_{11} + \delta \bar{A}_{12}K$. Thus, the switching surface design problem is established from Theorem 1 below.

Theorem 1. The reduced order system of the sliding mode (23) is stable and satisfies the performance index (22), if there exist matrix variables P > 0, Q > 0, X, Y, K, K_d , scalars $\alpha > 0$ and $\beta > 0$, such that for the given parameters d > 0, $Q_1 > 0$, $R_1 > 0$, the matrix inequalities (24) and (25) are kept:

$$\sum + \prod + \prod^{T} + dY < 0, \tag{24}$$

Electronics 2018, 7, 253

$$\coprod = \Theta + \left[\begin{array}{cc} Y & 0\\ 0 & 0 \end{array} \right] \ge 0, \tag{25}$$

where:

$$\sum = \begin{bmatrix} \sum_{11} & P\bar{A}_{12}K_d + K^T R_1 K_d \\ \star & -Q + \frac{1}{\beta}K_d^T \bar{E}_2^T \bar{E}_2 K_d + K_d^T R_1 K_d \end{bmatrix},$$
(26)

$$\Sigma_{11} = \left(He(P(\bar{A}_{11} + \bar{A}_{12}K)) + Q + Q_1 + K^T R_1 K + (\bar{E}_1 + \bar{E}_2 K)^T \frac{1}{\alpha} (\bar{E}_1 + \bar{E}_2 K) \right) + (\alpha + \beta) P \bar{D}_1 \bar{D}_1^T P,$$

$$\prod = \begin{bmatrix} X & -X \end{bmatrix},$$

$$\Theta = \begin{bmatrix} 0 & X \\ \star & 0 \end{bmatrix}.$$
(27)

Proof of Theorem 1. During the proof process, let us choose $V(t) = V_1(t) + V_2(t)$ as the Lyapunov functional with $V_1 = z_1^T(t)Pz_1(t)$ and $V_2 = \int_{t-d}^t z_1^T(w)Qz_1(w)dw$. Now, along the state trajectory of (23), one can easily check that (28) is right by differentiating both $V_1(t)$ and $V_2(t)$ on t.

$$\dot{V}_1 = z_1^T(t) \operatorname{He}(P\bar{\mathbb{A}}_1 + P\delta\bar{\mathbb{A}}_2) z_1(t) + 2z_1^T P\bar{A}_{12} K_d z_1(t-d) + 2z_1^T P\delta\bar{A}_{12} K_d z_1(t-d),$$
(28)

and:

$$\dot{V}_2 = z_1^T(t)Qz_1(t) - z_1^T(t-d)Qz_1(t-d).$$
(29)

Noticing that $\delta \bar{A}_{11} = \bar{D}_1 F_i(t) \bar{E}_1 \ \delta \bar{A}_{12} = \bar{D}_1 F(t) \bar{E}_2$ and using the mathematical basic inequality $x^T y + y^T x \leq \alpha x^T x + \frac{1}{\alpha} y^T y, \alpha > 0, x, y \in \mathbb{R}^q$, one can obtain (30) and (31) after some calculations.

$$2z_1^T(t)P\delta\mathbb{A}_2 z_1(t) \le \alpha z_1^T(t)P\bar{D}_1\bar{D}_1^T P z_1(t) + \frac{1}{\alpha} z_1^T(t) \left(\bar{E}_1 + \bar{E}_2 K\right)^T \left(\bar{E}_1 + \bar{E}_2 K\right) z_1(t)$$
(30)

and:

$$z_{1}^{T}(t)P\delta\bar{A}_{12}K_{d}z_{1}(t-d) + z_{1}^{T}(t-d)K_{d}^{T}\delta\bar{A}_{12}^{T}Pz_{1}(t)$$

$$\leq \beta z_{1}^{T}(t)P\bar{D}_{1}\bar{D}_{1}^{T}Pz_{1}(t) + \frac{1}{\beta}z_{1}^{T}(t-d)K_{d}^{T}\bar{E}_{2}^{T}\bar{E}_{2}K_{d}z_{1}(t-d)$$
(31)

Thanks to the relation:

$$2\omega^{T}(t)X\left[\int_{t-d}^{t} \dot{z}_{1}(w)dw - z_{1}(t) + z_{1}(t-d)\right] = 0$$
(32)

where $X \in R^{2(n-m)\times(n-m)}$ and $\omega^T(t) = \begin{bmatrix} z_1^T(t), & z_1^T(t-d) \end{bmatrix}$, it is not easily checked that:

$$\dot{V}(t) = \omega^{T}(t) \left(\begin{bmatrix} \Sigma_{11} - Q_{1} - K^{T} R_{1} K & P \bar{A}_{12} K_{d} \\ \star & -Q + \frac{1}{\beta} K_{d}^{T} \bar{E}_{2}^{T} \bar{E}_{2} K_{d} \end{bmatrix} + \Pi + \Pi^{T} \right) \omega(t)$$

$$- 2\omega^{T}(t) X \int_{t-d}^{t} \dot{z}_{1}(s) ds$$
(33)

6 of 18

Electronics 2018, 7, 253

One can further obtain from the free-weight matrix $\int_{t-d}^{t} \omega^{T}(t) Y \omega(t) dw - d\omega^{T}(t) Y \omega(t) = 0$ and the equation $2\omega^{T}(t) X \int_{t-d}^{t} \dot{z}_{1}(w) dw = \int_{t-d}^{t} \eta^{T}(t, w) \Theta \eta(t, w) dw$ that:

$$\dot{V}(t) \le \omega^{T}(t) \left(\begin{bmatrix} \Sigma_{11} - Q_1 - K^{T} R_1 K & P \bar{A}_{12} K_d \\ \star & -Q + \frac{1}{\beta} K_d^{T} \bar{E}_2^{T} \bar{E}_2 K_d \end{bmatrix} + \operatorname{He}(\prod) + dY \right) \omega(t)$$
(34)

According to (24), this implies that:

$$\dot{V} \le \omega^T(t) \begin{bmatrix} -Q_1 - K^T R_1 K & -K^T R_1 K_d \\ \star & -K_d^T R_1 K_d \end{bmatrix} \omega(t) = -z_1^T Q_1 z_1 - u^T R_1 u < 0$$
(35)

Thus, one can see that the reduced order systems (23) is asymptotical stable. Furthermore, one can achieve the following inequality by integrating the inequality (35) from both sides in [0, T]:

$$z_{1}^{T}(T)Pz_{1}(T) - z_{1}^{T}(0)Pz_{1}(0) + \int_{T-d}^{T} z_{1}^{T}(s)Q_{1}z_{1}(s)ds - \int_{-d}^{0} z_{1}^{T}(s)Q_{1}z_{1}(s)ds$$

$$< -\int_{0}^{T} \omega^{T}(s) \begin{bmatrix} Q_{1} + K^{T}R_{1}K & K^{T}R_{1}K_{d} \\ \star & K_{d}^{T}R_{1}K_{d} \end{bmatrix} \omega(s)ds$$

Due to the closed-loop system being asymptotical stable, when $T \rightarrow \infty$ and $z_1(t) = 0, t \in [-d, 0)$, we have:

$$J = \int_0^\infty \omega^T(s) \begin{bmatrix} Q_1 + K^T R_1 K & K^T R_1 K_d \\ \star & K_d^T R_1 K_d \end{bmatrix} \omega(s) ds \le z_1^T(0) P z_1(0)$$
(36)

The proof is thus completed. \Box

Based on the LMI technique, the solution to the gain matrices of the switching surface is presented in Theorem 2 below.

Theorem 2. The sliding mode reduce order system (23) is stable with the performance index J in (22), if there exist $\mathcal{P} > 0$, $\mathcal{Z} > 0$, $\mathcal{X}_1, \mathcal{X}_2, \mathcal{Y}, \mathcal{K}, \mathcal{K}_d$, scalars $\alpha > 0$, $\beta > 0$, such that for the given parameter d > 0, matrices $Q_1 > 0$ and $R_1 > 0$, the following LMIs hold:

$$\begin{bmatrix} \Omega_{11} & \bar{A}_{12}\mathcal{H}_{d} & \mathcal{P}\bar{E}_{1}^{T} + \mathcal{K}^{T}\bar{E}_{2}^{T} & 0 & \mathcal{P} & \mathcal{K} \\ \star & -\mathcal{Q} & 0 & \mathcal{H}_{d}^{T}\bar{E}_{2} & 0 & \mathcal{H}_{d}^{T} \\ \star & \star & -\alpha I & 0 & 0 & 0 \\ \star & \star & \star & & -\beta I & 0 & 0 \\ \star & \star & \star & \star & & -\beta I & 0 & 0 \\ \star & \star & \star & \star & \star & & -R_{1}^{-1} \end{bmatrix} \\ + H\left(\begin{bmatrix} \operatorname{He}(\mathcal{H}_{1}) & \mathcal{H}_{2}^{T} - \mathcal{H}_{1} \\ \star & -\operatorname{He}(\mathcal{H}_{2}) \end{bmatrix} + d\mathcal{H} \right) H^{T} < 0, \qquad (37)$$
$$\Xi + \begin{bmatrix} \mathcal{Y} & 0 \\ 0 & 0 \end{bmatrix} \ge 0, \qquad (38)$$

where:

$$\Omega_{11} = \operatorname{He}(\bar{A}_{11}\mathscr{P} + \bar{A}_{12}\mathscr{K}) + \mathscr{Q} + (\alpha + \beta)\bar{D}_1\bar{D}_1^T$$
(39)

$$\Xi = \begin{bmatrix} 0 & \begin{bmatrix} \mathscr{X}_1 \\ \mathscr{X}_2 \end{bmatrix} \\ \star & 0 \end{bmatrix}$$
(40)

$$H = \left[\begin{array}{c} I_{2(n-m)} \\ 0_{(3(n-m)+2)\times(2(n-m))} \end{array} \right].$$

In addition, the gain matrices K and K_d can be achieved by:

$$K = \mathscr{K} \mathscr{P}^{-1}, \quad K_d = \mathscr{K}_d \mathscr{P}^{-1}.$$
(41)

Proof of Theorem 2. Let us multiply both sides of \sum in (26) by diag{ P^{-1} , P^{-1} }, and using the Schur lemma, it can be easily checked that:

$$\begin{bmatrix} \operatorname{He}(\bar{A}_{11}\mathscr{P} + \bar{A}_{12}\mathscr{K}) + \mathscr{Q} + (\alpha + \beta)\bar{D}_{1}\bar{D}_{1}^{T} & \bar{A}_{12}\mathscr{K}_{d} & \mathscr{P}\bar{E}_{1}^{T} + \mathscr{K}^{T}\bar{E}_{2}^{T} & 0 & \mathscr{P} & \mathscr{K} \\ & \star & -\mathscr{Q} & 0 & \mathscr{K}_{d}^{T}\bar{E}_{2} & 0 & \mathscr{K}_{d}^{T} \\ & \star & \star & -\alpha I & 0 & 0 & 0 \\ & \star & \star & \star & -\beta I & 0 & 0 \\ & \star & \star & \star & \star & -\beta I & 0 & 0 \\ & \star & \star & \star & \star & \star & \star & -R_{1}^{-1} \end{bmatrix}$$
(42)

where $\mathscr{P} = P^{-1}$, $\mathscr{Q} = P^{-1}QP^{-1}$, $\mathscr{K} = KP^{-1}$ and $\mathscr{K}_d = K_dP^{-1}$.

Further, after a congruence transformation on Π in (27) with the diagonal matrix diag{ \mathscr{P}, \mathscr{P} }, it is easily obtained that:

$$\operatorname{diag}\{\mathscr{P},\mathscr{P}\}\Pi\operatorname{diag}\{\mathscr{P},\mathscr{P}\} = \begin{bmatrix} \mathscr{P} & 0 \\ 0 & \mathscr{P} \end{bmatrix} X\mathscr{P} & -\begin{bmatrix} \mathscr{P} & 0 \\ 0 & \mathscr{P} \end{bmatrix} X\mathscr{P} \\ X\mathscr{P} & -\begin{bmatrix} 0 & 0 \\ 0 & \mathscr{P} \end{bmatrix} X\mathscr{P} \end{bmatrix}$$
(43)

Let
$$X = \begin{bmatrix} X_1 \\ X_2 \end{bmatrix}$$
, where X_1 , X_2 have the same dimension; it is easy to see that:

diag{
$$\mathscr{P}, \mathscr{P}$$
}He(\Pi)diag{ \mathscr{P}, \mathscr{P} } = $\begin{bmatrix} \operatorname{He}(\mathscr{X}_1) & \mathscr{X}_2^T - \mathscr{X}_1 \\ \star & -\operatorname{He}(\mathscr{X}_2) \end{bmatrix}$ (44)

where $\mathscr{X}_1 = \mathscr{P}X_1\mathscr{P}, \mathscr{X}_2 = \mathscr{P}X_2\mathscr{P}.$ Let us denote:

$$\mathscr{Y} = \operatorname{diag}\{\mathscr{P}, \mathscr{P}\} \operatorname{Y} \operatorname{diag}\{\mathscr{P}; \mathscr{P}\}$$

$$\tag{45}$$

thus, by (42), (44) and (45), we have the first inequality (37).

Now, let us perform a congruence transformation on Θ by $\mathscr{S} = \text{diag} \{ \mathscr{P}, \mathscr{P}, \mathscr{P} \}$; one can get that:

$$\mathscr{S}\Theta_{i}\mathscr{S} = \begin{bmatrix} 0 & \left[\begin{array}{c} \mathscr{X}_{1} \\ \mathscr{X}_{2} \\ \star & 0 \end{array} \right] = \Xi$$
(46)

Further, by performing a congruence transformation on $\begin{bmatrix} \mathcal{Y} & 0 \\ 0 & 0 \end{bmatrix}$ with \mathscr{S} and noticing (45), one can convert (25) into (38).

One can thus get the conditions of stability (37) and (38).

Now, the optimal control performance for sliding dynamics with the performance index (22) can be achieved by minimizing the value of γ subject to the LMIs (38), (48) and (49).

$$\min_{\alpha>0,\beta>0,\mathscr{P}>0,\mathscr{Z}>0,\mathscr{K},\mathscr{K}_{d},\mathscr{X}_{1},\mathscr{X}_{2},\mathscr{Y},\mathscr{Q}_{1},\mathscr{R}_{1}}\gamma$$
(47)

subject to (38), (48) and (49).

$$\begin{bmatrix} \Omega_{11} \quad \bar{A}_{12}\mathcal{K}_d \quad \mathscr{P}\bar{E}_1^T + \mathscr{K}^T\bar{E}_2^T & 0 & \mathscr{P} & \mathscr{K} \\ \star & -\mathscr{Q} & 0 & \mathscr{K}_d^T\bar{E}_2 & 0 & \mathscr{K}_d^T \\ \star & \star & -\alpha I & 0 & 0 & 0 \\ \star & \star & \star & -\beta I & 0 & 0 \\ \star & \star & \star & \star & -\beta I & 0 \\ \star & \star & \star & \star & \star & -\mathscr{Q}_1^{-1} & 0 \\ \star & \star & \star & \star & \star & -\mathscr{Q}_1^{-1} \end{bmatrix} \\ + H\left(\begin{bmatrix} \operatorname{He}(\mathscr{X}_1) & \mathscr{X}_2^T - \mathscr{X}_1 \\ \star & -\operatorname{He}(\mathscr{X}_2) \end{bmatrix} + d\mathscr{Y} \right) H^T < 0, \tag{48}$$

$$\begin{bmatrix} -\gamma & z_1^T(0) \\ \star & -\mathscr{P} \end{bmatrix} < 0. \tag{49}$$

where $\Omega_{11} = \text{He}(\bar{A}_{11}\mathscr{P} + \bar{A}_{12}\mathscr{K}) + \mathscr{Q} + (\alpha + \beta)\bar{D}_1\bar{D}_1^T$, $H = \begin{bmatrix} I_{2(n-m)} \\ 0_{(3(n-m)+2)\times(2(n-m))} \end{bmatrix}$, By solving the minimum problem (47), one can achieve that the performance index $J < z_1^T(0)Pz_1(0) < \gamma$.

3.2. The Design of Event-Based Sliding-Mode Reaching Controller

The ESMC design is presented below to ensure the arrival of the desired memory-based switching manifold (20).

Theorem 3. State trajectories of uncertain MSs (15) and (16) can be repelled into the switching surface (20) in a limited time, when the ESMC is constructed as follows:

$$u(t) = u_1(t_i) + u_2(t_i), t \in [t_i, t_{i+1})$$
(50)

$$u_1(t_i) = -\bar{B}_2^{-1} \left[C_1 z_1(t_i) + C_2 z_2(t_i) + C_3 z_1(t_i - d) + C_4 z_2(t_i - d) \right]$$
(51)

$$u_2(t_i) = -\bar{B}_2^{-1}\rho(|z(t_i)|, |z(t_i - d)|)sign(s(t_i))$$
(52)

where:

$$\rho(|z(t_i)|, |z(t_i - d)|) = \begin{cases} |\bar{B}_2|\bar{d} + (\sigma(|C| + Y) + Y)(|z(t_i)| + |z(t_i - d)|) + \mu & sign(s(t)) = sign(s(t_i)) \\ -|\bar{B}_2|\bar{d} - (\sigma(|C| + Y) + Y)(|z(t_i)| + |z(t_i - d)|) - \mu & sign(s(t)) \neq sign(s(t_i)) \end{cases}$$
(53)

 $C = [C_1, C_2, C_3, C_4], C_1 = \bar{A}_{21} - K\bar{A}_{11}, C_2 = \bar{A}_{22} - K\bar{A}_{12}, C_3 = -K_d\bar{A}_{11}; C_4 = -K_d\bar{A}_{12}; Y = -K_d\bar{A}_{12$ $Y_1 + Y_2 + Y_3 + Y_4$; $Y_1 = |D_2||E_1| + |K||D_1||E_1|$, $Y_2 = |D_2||E_2| + |K||D_1||E_2|$; $Y_3 = |K_d||D_1||E_1|$; $Y_4 = |K_d||D_1||E_2|$; μ is an arbitrary positive scalar; and σ is defined by (19).

Proof of Theorem 3. Let us select $V(t) = \frac{1}{2}s^T(t)s(t)$. As a consequence, along the state trajectories of (15) and (16), we have:

$$\dot{V} = s^{T}(t) \left\{ \left[(\bar{A}_{21} - K\bar{A}_{11}) + (\delta\bar{A}_{21} - K\delta\bar{A}_{11}) \right] z_{1}(t) + \left[(\bar{A}_{22} - K\bar{A}_{12}) + (\delta\bar{A}_{22} - K\delta\bar{A}_{12}) \right] z_{2}(t) - K_{d}(\bar{A}_{11} + \delta\bar{A}_{11}) z_{1}(t-d) - K_{d}(\bar{A}_{12} + \delta\bar{A}_{12}) z_{2}(t-d) + \bar{B}_{2}(u+\xi) \right\}$$
(54)

Substituting (50)–(52) into (54) and using the relations (17) and (18), then one can check by some calculations:

$$\begin{split} \dot{V}(t) &= s^{T}(t) \left\{ C_{1}e_{1}(t) + C_{2}e_{2}(t) + C_{3}e_{1}(t-d) + C_{4}e_{2}(t-d) + \left[(\delta\bar{A}_{21} - K\delta\bar{A}_{11})e_{1}(t) \right. \right. \\ &+ (\delta\bar{A}_{22} - K\delta\bar{A}_{12})e_{2}(t) \right] - \left[K_{d}\delta\bar{A}_{11}e_{1}(t-d) + K_{d}\delta\bar{A}_{12}e_{2}(t-d) \right] \\ &+ \left[(\delta\bar{A}_{21} - K\delta\bar{A}_{11})z_{1}(t_{i}) + (\delta\bar{A}_{22} - K\delta\bar{A}_{12})z_{2}(t_{i}) \right] \\ &- \left[K_{d}\delta\bar{A}_{11}z_{1}(t_{i}-d) + K_{d}\delta\bar{A}_{12}z_{2}(t_{i}-d) \right] + \bar{B}_{2}u_{2}(t_{i}) + \bar{B}_{2}\xi \right\} \end{split}$$
(55)
$$&= s^{T}(t) \left\{ C\bar{e}(t) + \Theta\bar{e}(t) + \Theta_{1}z_{1}(t_{i}) + \Theta_{2}z_{2}(t_{i}) + \Theta_{3}z_{1}(t_{i}-d) + \Theta_{4}z_{2}(t_{i}-d) \right. \\ &+ \left. \bar{B}_{2}u_{2}(t_{i}) + \bar{B}_{2}\xi \right\} \end{split}$$

where $\Theta = [\Theta_1, \Theta_2, \Theta_3, \Theta_4]$, $\Theta_1 = \delta \bar{A}_{21} - K \delta \bar{A}_{11}$, $\Theta_2 = \delta \bar{A}_{22} - K \delta \bar{A}_{12}$, $\Theta_3 = -K_d \delta \bar{A}_{11}$, $\Theta_4 = -K_d \delta \bar{A}_{12}$. Noticing that $\delta \bar{A}_{11} = \bar{D}_1 F(t) \bar{E}_1$, $\delta \bar{A}_{12} = \bar{D}_1 F(t) \bar{E}_2$, $\delta \bar{A}_{21} = \bar{D}_2 F(t) \bar{E}_1$, $\delta \bar{A}_{22} = \bar{D}_2 F(t) \bar{E}_2$ and $F(t) F^T(t) \leq I$, we have:

$$\begin{split} |\Theta| &\leq |\Theta_1| + |\Theta_2| + |\Theta_3| + |\Theta_4| \\ &\leq |D_2||E_1| + |K||D_1||E_1| + |D_2||E_2| + |K||D_1||E_2| + |K_d||D_1||E_1| + |K_d||D_1||E_2| \\ &= Y_1 + Y_2 + Y_3 + Y_4 = Y. \end{split}$$

If the system trajectories start from a region where $sign(s(t_i)) = sign(s(t))$, then one can see by combining with (19), (51)–(53) and $|\xi| \le \overline{d}$ that:

$$\dot{V}(t) \le -\mu|s(t)| \tag{56}$$

If it occurs that $sign(s(t_i)) = sign(s(t))$, one can see that from (52) and (53) that:

$$u_{2}(t_{i}) = -\bar{B}_{2}^{-1}[-|\bar{B}_{2}|\bar{d} - (\sigma(|C|+Y)+Y)(|z(t_{i})|+|z(t_{i}-d)|) - \mu]\operatorname{sign}(s(t_{i}))$$

$$=\bar{B}_{2}^{-1}[|\bar{B}_{2}|\bar{d} + (\sigma(|C|+Y)+Y)(|z(t_{i})|+|z(t_{i}-d)|) + \mu]\operatorname{sign}(s(t_{i}))$$

$$= -\bar{B}_{2}^{-1}[|\bar{B}_{2}|\bar{d} + (\sigma(|C|+Y)+Y)(|z(t_{i})|+|z(t_{i}-d)|) + \mu]\operatorname{sign}(s(t))$$
(57)

Thus, by virtue of (19), (57), $|\xi| \leq \overline{d}$ and $|\Theta| \leq Y$, it is not hard to get that:

$$\dot{V}(t) = s^{T}(t) \left\{ C\bar{e}(t) + \Theta\bar{e}(t) + \Theta_{1}z_{1}(t_{i}) + \Theta_{2}z_{2}(t_{i}) + \Theta_{3}z_{1}(t_{i}-d) + \Theta_{4}z_{2}(t_{i}-d) - \left[|\bar{B}_{2}|\bar{d} + (\sigma(|C|+Y)+Y)(|z(t_{i})| + |z(t_{i}-d)|) + \mu \right] \operatorname{sign}(s(t)) + \bar{B}_{2}\xi \right\}$$

$$\leq -\mu|s(t)|$$
(58)

As a result, one can observe that the sliding mode reachability condition is well established. \Box

Due to the inherent execution restrictions in digital processors, the event-triggering implementation time from one to another cannot result in Zeno phenomena in the execution of the MSs.

Theorem 4. Consider the system (13). Let $\{t_i\}$ be the generated triggering instant sequence from:

$$t_{i+1} = \inf\{t : t > t_i, \sigma | \bar{z}(t_i) | \le |\bar{e}(t)|\}$$
(59)

for any given $\sigma \in (0, 1)$. T_i is then given as:

$$T_i \ge \frac{1}{2\pi} \ln \left(1 + \frac{2\pi\sigma |\bar{z}(t_i)|}{\epsilon + \kappa (|z(t_i)|)} \right),\tag{60}$$

where $\kappa(|z(t_i)|)$ and ϵ are defined as:

$$\kappa(|z(t_i)|) := 2\pi |(z(t_i)| + z(t_i - d)) + (1 + \sigma)|\bar{B}_2^{-1}||\mathbb{B}|(|C| + Y)(|z(t_i)| + 2|z(t_i - d)| + |z(t_i - 2d)|)$$
(61)

and:

$$\pi := |\bar{A}| + |\bar{D}||\bar{E}|, \ \epsilon := 2|\mathbb{B}|(|\bar{B}_2|\bar{d} + \mu)|\bar{B}_2^{-1}|, \ \mathbb{B} = diag\{\bar{B}, \bar{B}\}$$
(62)

Proof of Theorem 4. Consider $\Gamma = \{t \in [t_i, \infty) : |\bar{e}(t)| = 0\}$. For all $t \in [t_i, t_{i+1}) \setminus \Gamma$, using the relations (17) and (18), one can check after some careful calculations that:

$$\frac{\mathrm{d}|\bar{e}(t)|}{\mathrm{d}t} \le \left|\mathbb{A}\bar{e}(t) + \bar{\mathbb{A}}\bar{z}(t_i) + \mathbb{B}\left[\begin{array}{c}\vartheta(t)\\\vartheta(t-d)\end{array}\right]\right| \tag{63}$$

where the matrices $\mathbb{A} = \text{diag}\{\bar{A} + \delta\bar{A}, \bar{A} + \delta\bar{A}\}, \bar{\mathbb{A}} = \begin{bmatrix} \bar{A} + \delta\bar{A} \\ \bar{A} + \delta\bar{A} \end{bmatrix} \bar{z}(t_i) = \begin{bmatrix} z(t_i) \\ z(t_i - d) \end{bmatrix}$ and $\vartheta(t) = u(t) + \xi(t)$. One can further get from Assumption 1 that:

$$\frac{d|\bar{e}(t)|}{dt} \le 2\pi |\bar{e}(t)| + 2\pi (|z(t_i)| + |z(t_i - d)|) + |\mathbb{B}| \Big[|\vartheta(t)| + |\vartheta(t - d))| \Big]$$
(64)

According to (50)–(52), we have:

$$|\vartheta(t)| \le |\bar{B}_2^{-1}| \Big[(1+\sigma)(|C|+Y)(|z(t_i)|+|z(t_i-d)|) + \mu + \bar{d}|\bar{B}_2| \Big]$$

and:

$$|\vartheta(t-d)| \le |\bar{B}_2^{-1}| \Big[(1+\sigma)(|C|+Y)(|z(t_i-d)|+|z(t_i-2d)|) + \mu + \bar{d}|\bar{B}_2| \Big]$$

As a consequence, it is easy to verify that:

$$\frac{\mathrm{d}|\bar{e}(t)|}{\mathrm{d}t} \le 2\pi |\bar{e}(t)| + \epsilon + \kappa(|z(t_i)|) \tag{65}$$

Applying the method of constant variation for the ordinary differential equation with the initial condition $\bar{e}(t_i) = |e(t_i - d))|$, it is easy to achieve that the solution of (65) is:

$$\left|\bar{e}(t)\right| \le \frac{\epsilon + \kappa(|z(t_i)|)}{2\pi} (e^{2\pi(t-t_i)} - 1) \tag{66}$$

for *t* in the interval $[t_i, t_{i+1})$. Applying the event-triggering rule (59), one can observe that the right-hand side of (60) always has a non-zero lower boundary. \Box

4. Example

For the proposed ESMC design methodology of the linear uncertain MS, we show an example in this section to validate its effectiveness. During the MATLAB simulation, the following data are chosen: $a_1 = 0.3$, $a_2 = 0.8$, $c_1 = 0.1$, $c_2 = 1$, R = 1, L = 1/15, G = 1.5, $\frac{r}{L} = 0.3$. Now, suppose that the control input is added to the memristive system as done in [24,42]; thus, we have:

$$A = \begin{bmatrix} -0.5 & 10 & 0 & 0 \\ 1 & -1 & -1 & 0 \\ 0 & 15 & -0.3 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}, \quad B = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}.$$

Taking the nonsingular transform matrix $T = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{bmatrix}$, we further have:
 $\bar{A} = \begin{bmatrix} -0.3 & 15 & 0 & 0 \\ -1 & -1 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 10 & 0 & -0.5 \end{bmatrix}, \quad \bar{B} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 1 \end{bmatrix}.$

In the simulation, we take $\overline{D} = [-0.5 \ 1 \ -0.5 \ 0.2]^T$, $\overline{E} = [1 \ -1 \ 1 \ 0.1]$, $F = 0.5 \sin(t)$, $\xi = 0.9 \cos(2t)$ and the initial state $z_0 = [1 \ 2 \ -1 \ 0.5]^T$.

Taking the memory parameter d = 0.001, one can get by solving the LMIs (47)–(49) that:

 $K = [-3.2024 - 2.0482 - 3.6933], K_d = [1.0159 - 1.8031 0.9422]$

with the performance index J = 27.0648. Then, the switching hyperplane is:

$$s(t) = z_2(t) - [-3.2024 - 2.0482 - 3.6933]z_1(t) - [1.0159 - 1.8031 0.9422]z_1(t - 0.001).$$

Let us choose $\mu = 0.1$, $\bar{d} = 0.9$ and $\sigma = 0.25$, the response curves of system states, the control input, switching function and event-triggered executions are given in Figures 2–6, respectively. From Figures 2 and 5, one can easily see that the state trajectories of MS are able to be compelled to the desired switching manifold s(t) = 0 in a limited time, and they then asymptotically slide towards the origin; thus, the robust stabilization of the memristive system is well established. Furthermore, it is not hard to see from Figure 6 that the triggering intervals are larger than zero, and as a result, the Zeno behavior does not arise in the whole dynamical evolution of MS.

In order to show the advantage of the proposed design method in this paper, we provide some comparison results with the ESMC with traditional memoryless switching hyperplane design approach. By solving LMIs with d = 0, one can get $K = \begin{bmatrix} -2.1849 & -3.8514 & -2.7581 \end{bmatrix}$. At the same time, the performance index J = 27.1055, which is bigger than the 27.0648 obtained by the proposed design method in this paper. The responding simulation results are shown in Figures 2–5 and 7. It can be observed from the state response curves that the control input response curve and the switching function response curve that better control the performance are achieved by the proposed method in this paper.

Furthermore, we also presented the corresponding simulation results with the ESMC in [24], where $s(t) = \begin{bmatrix} 2.9447 & 3.4825 & 1.9250 & 1 \end{bmatrix} z = 0$, $\eta = 0.02$ and $\epsilon = |\overline{D}||\overline{E}|$. The simulation results, including the response curves of system states, the control input, the switching function and event-triggered behavior, are shown in Figures 8–11. By comparison, one can see that though the proposed method [24] can stabilize the memristive system, it needs many more event-triggered behaviors, especially during the reaching phase of SMC.

Thus, it is verified that the proposed memory-based ESMC design method is effective in the robust stabilization of the MSs.



Figure 2. The system states' evolution curves (the proposed method with solid lines, the memoryless design method with dashed lines).



Figure 3. The system states' evolution curves (the proposed method with solid lines, the memoryless design method with dashed lines).



Figure 4. The control input evolution curves (the proposed method with solid lines, the memoryless design method with dashed lines).



Figure 5. The switching function response curves (the proposed method with solid lines, the memoryless design method with dashed lines).



Figure 6. Evolution of the execution time interval (the proposed design method).



Figure 7. Evolution of the execution time interval (the memoryless design method).







Figure 10. The switching function response curve.



Figure 11. Evolution of the execution time interval.

5. Conclusions

Based on an event-triggered technique, the robust memory-based SMC design of uncertain MSs has been presented in this paper. At first, the uncertain Chua system with memristors has been described to be a linear uncertain system based on the memristor features. A memory-based sliding surface has then been introduced, and its design has been converted into the control gain design with the guaranteed cost performance index and can be solved by solutions to a set of LMIs. Thus, the ESMC has been presented for achieving robust stabilization of MS in spite of unknown external disturbances and uncertainties. In addition, the lower boundary for the event-triggered execution time interval has been given. An example has been finally presented for showing its effectiveness via simulation.

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Abbreviations

The following abbreviations are used in this manuscript:

- ESMC Event-triggered sliding mode variable structure control
- SMC Sliding mode variable structure control
- MS(s) Memristive system(s)
- LMI Linear matrix inequality

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