

Article

Accuracy in Biological Information Technology Involves Enzymatic Quantum Processing and Entanglement of Decohered Isomers

Willis Grant Cooper

International Physics Health and Energy, Inc., 5109 82nd Street, Suite 7, Lubbock, TX 79424, USA;
E-Mail: cooperwg@sbcglobal.net

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Abstract: Genetic specificity information “seen by” the transcriptase is in terms of hydrogen bonded proton states, which initially are metastable amino ($-\text{NH}_2$) and, consequently, are subjected to quantum uncertainty limits. This introduces a probability of arrangement, *keto-amino* $\rightarrow$ *enol-imine*, where product protons participate in coupled quantum oscillations at frequencies of $\sim 10^{13} \text{ s}^{-1}$ and are entangled. The enzymatic ket for the four G'-C' coherent protons is $|\psi\rangle = \alpha|++--\rangle + \beta|+- - +\rangle + \gamma| - ++ -\rangle + \delta| - + - +\rangle$. Genetic specificities of superposition states are processed quantum mechanically, in an interval $\Delta t \ll 10^{-13} \text{ s}$, causing an additional entanglement between coherent protons and transcriptase units. The input qubit at G-C sites causes base substitution, whereas coherent states within A-T sites cause deletion. Initially decohered enol and imine G' and *C isomers are “entanglement-protected” and participate in Topal-Fresco substitution-replication which, in the 2nd round of growth, reintroduces the metastable keto-amino state. Since experimental lifetimes of metastable keto-amino states at 37 °C are $\geq \sim 3000 \text{ y}$, approximate quantum methods for small times, $t < \sim 100 \text{ y}$, yield the probability, $P(t)$, of *keto-amino* $\rightarrow$ *enol-imine* as $P_p(t) = \frac{1}{2} (\gamma_p/\hbar)^2 t^2$. This approximation introduces a quantum Darwinian evolution model which (a) simulates incidence of cancer data and (b) implies insight into quantum information origins for evolutionary extinction.

Keywords: genetics information theory; biological quantum information; quantum information measurements; quantum evolutionary pressures; quantum uncertainty limits; DNA-proton-protein entanglements; quantum biology

1. Introduction

Quantum information science seeks to exploit applications of quantum theory to enhance the versatility of acquiring, storing, transmitting and processing information, using encoded information systems that exhibit unique quantum properties [1-3]. If successful, quantum information processing by a quantum computer would significantly enhance computational power and thus expand the range of computational applications [4,5]. In the context of discussing an example quantum information system [6,7], this report presents a review of evolutionarily designed quantum information processing routinely implemented by enzyme systems of bacteriophage T4 [8,9] and human DNA systems [10-13]. This model of genetic specificity implies a quantum Darwinian evolution treatment for intrinsic time-dependent DNA instabilities. Although most molecular genetic experiments did not attempt to measure consequences of quantum effects, time-dependent point mutations exhibited by T4 phage require quantum coherence for explanation. In this case, molecular genetic observations [8] and quantum chemical calculations [9-13] demonstrate that the replicase introduces metastable keto-amino complementary DNA pairs. As a consequence, quantum uncertainty limits— $\Delta x \Delta p_x \geq \frac{1}{2} \hbar$ —operate on amino DNA protons which drive arrangements, *keto-amino* $\rightarrow$ *enol-imine* (Figures 1 to 3). This populates accessible reduced energy enol-imine duplex states at rates consistent with time-dependent DNA evolution [14-18], exhibited as *stochastic* mutations. Evolution data exhibited by T4 phage DNA [8,17,18] demonstrate that the two classes of time-dependent point lesion, $G-C \rightarrow G'-C'$ & $G-C \rightarrow *G-*C$, are consequences of hydrogen bond arrangements, *keto-amino* $\rightarrow$ *enol-imine*, by symmetric and asymmetric channels [18-20]. Product enol-imine protons are shared between two indistinguishable sets of electron lone-pairs and, thus, participate in coupled quantum oscillations (Figure 2) at frequencies of $\sim 10^{13} \text{ s}^{-1}$. Observable long-term stability of coherent state $G'-C'$ and $*G-*C$ sites [8,9,17,18] implies existence of decoherence-free subspaces [10,21-24] where coupled enol-imine protons are entangled and H_2O is excluded [8,12]. Genetic specificity at a coherent superposition site— $G'-C'$, $*G-*C$ (Figure 2) or $*A-*T$ (Figure 3)—is stored as an input qubit, the quantum counterpart to the classical information bit [4]. Before decoherence [25], genetic specificities of coherent states are measured and processed by the transcriptase as an output qubit in an interval $\Delta t \ll 10^{-13} \text{ s}$, causing an additional entanglement between coherent protons and transcriptase components [9,26-28]. This entanglement ultimately yields an ensemble of decohered enol and imine isomers [8]— $G', C', *G, *C$ (Table 1)—that participate in Topal-Fresco [29] substitution replication, *i.e.*, $G'2 \ 0 \ 2 \rightarrow T$, $G'0 \ 0 \ 2 \rightarrow C$, $*G0 \ 2 \ 0^0 \rightarrow A$ & $*C2 \ 0 \ 2^2 \rightarrow T$ (see Figure 2 for notation).

However, coherent states within $*A-*T$ sites are deleted. These time-dependent substitutions, *ts*, and deletions, *td*, contribute to the spectrum of *stochastic* mutations [14-18] and imply a modest evolutionary shift favoring A-T richness, consistent with observation [30]. Since T4 phage DNA systems are susceptible to (i) fine scale genetic mapping [31], (ii) reversion analysis [32,33] and (iii) strand analysis [8,18], an individual $G'-C'$ or $*G-*C$ genetic site can be assayed at the resolution of the particular G' or $*C$ coherent state at the time of transcriptase measurement. Consistent with data [8,18], Figure 4 illustrates a “snap shot” of quantum information “seen by” the transcriptase viewing coherent states $G'2 \ 0 \ 2$, $G'0 \ 0 \ 2$ & $*C2 \ 0 \ 2^2$ and the keto-amino state, $T2^2 \ 0 \ 2^2$. In the case of $*C$ on the template strand, the transcriptase deciphers genetic specificities of quantum states, $*C2 \ 0 \ 2^2$ - $*G0 \ 2 \ 0^0 \rightleftharpoons *C0 \ 0 \ 2^2$ - $*G2 \ 2 \ 0^0$, on the basis of measurements on the cytosine carbon-6 imine

proton, which participates in coupled quantum oscillation (Figure 2f to g). Similarly in the G' case, genetic specificities residing within quantum states, $G'2\ 0\ 2-C'0\ 2\ 0$ (Figure 2c) $\rightleftharpoons$ $G'0\ 0\ 2-C'2\ 2\ 0$ (Figure 2b), are deciphered by coherent state measurements on the guanine carbon-6 enol proton. These quantum measurements of coherent states, $*C2\ 0\ 2^2$ and $G'2\ 0\ 2$, yield information corresponding to normal thymine, $T2^2\ 0\ 2^2$ (Figure 4), and consequently, phenotypically express substitutions, $*C2\ 0\ 2^2 \rightarrow T$ and $G'2\ 0\ 2 \rightarrow T$, by transcription before replication [8,18]. Specificity determination by the transcriptase is independent of the proton or electron lone-pair at the “outside” position (in the major and minor grooves) on keto, enol and imine groups (Figure 2). Otherwise, enol and imine groups on quantum states $*C2\ 0\ 2^2$ and $G'2\ 0\ 2$ could *not* simulate keto groups on $T2^2\ 0\ 2^2$ at transcription as observed. Also, this mode of determining genetic specificity is tolerant of gross structural dissimilarities between the dual ring purine, $G'2\ 0\ 2$, and single ring pyrimidines, $*C2\ 0\ 2^2$ & $T2^2\ 0\ 2^2$, as observed.

Figure 1. (a) Symmetric proton exchange and electron rearrangement at a G-C site.
(b) Asymmetric proton exchange and electron rearrangement at a G-C site.

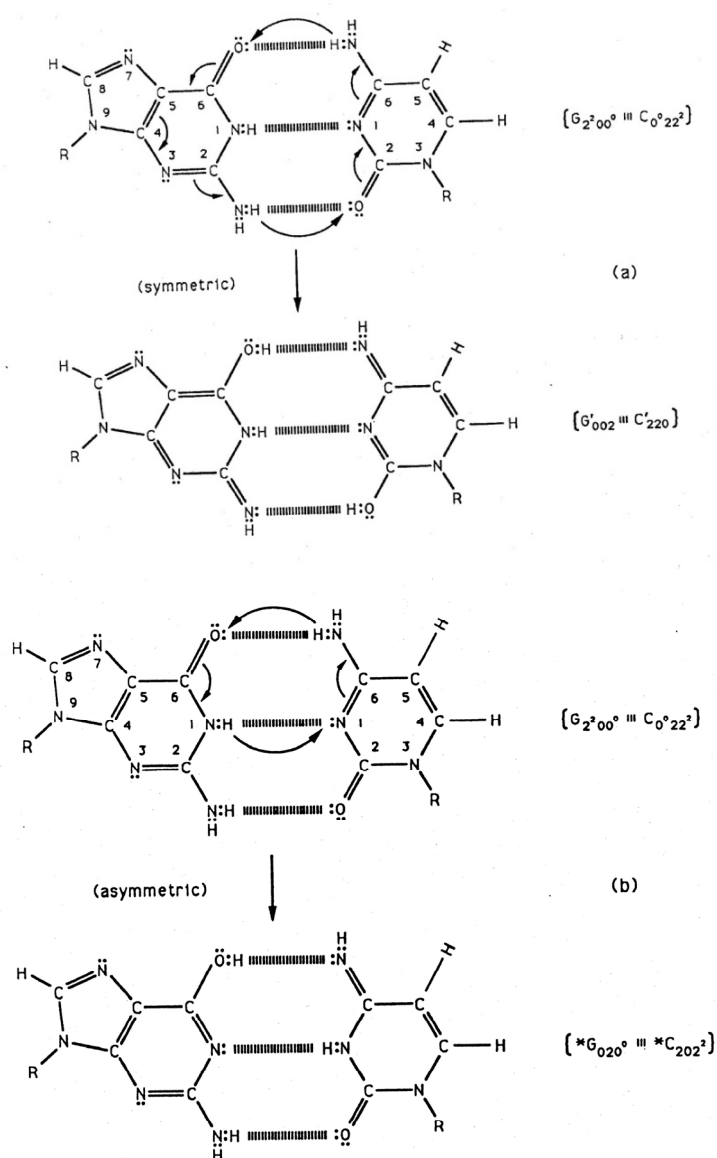
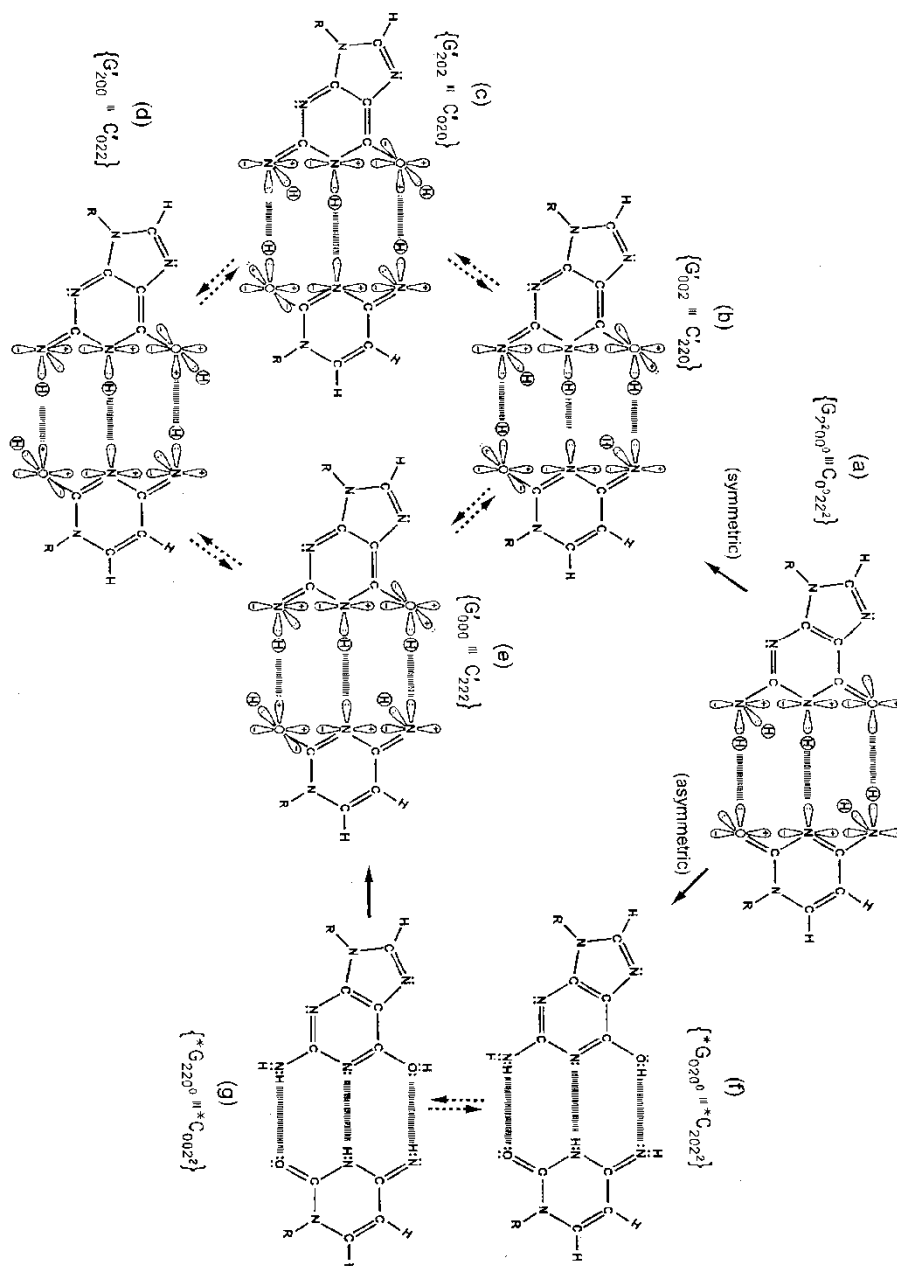
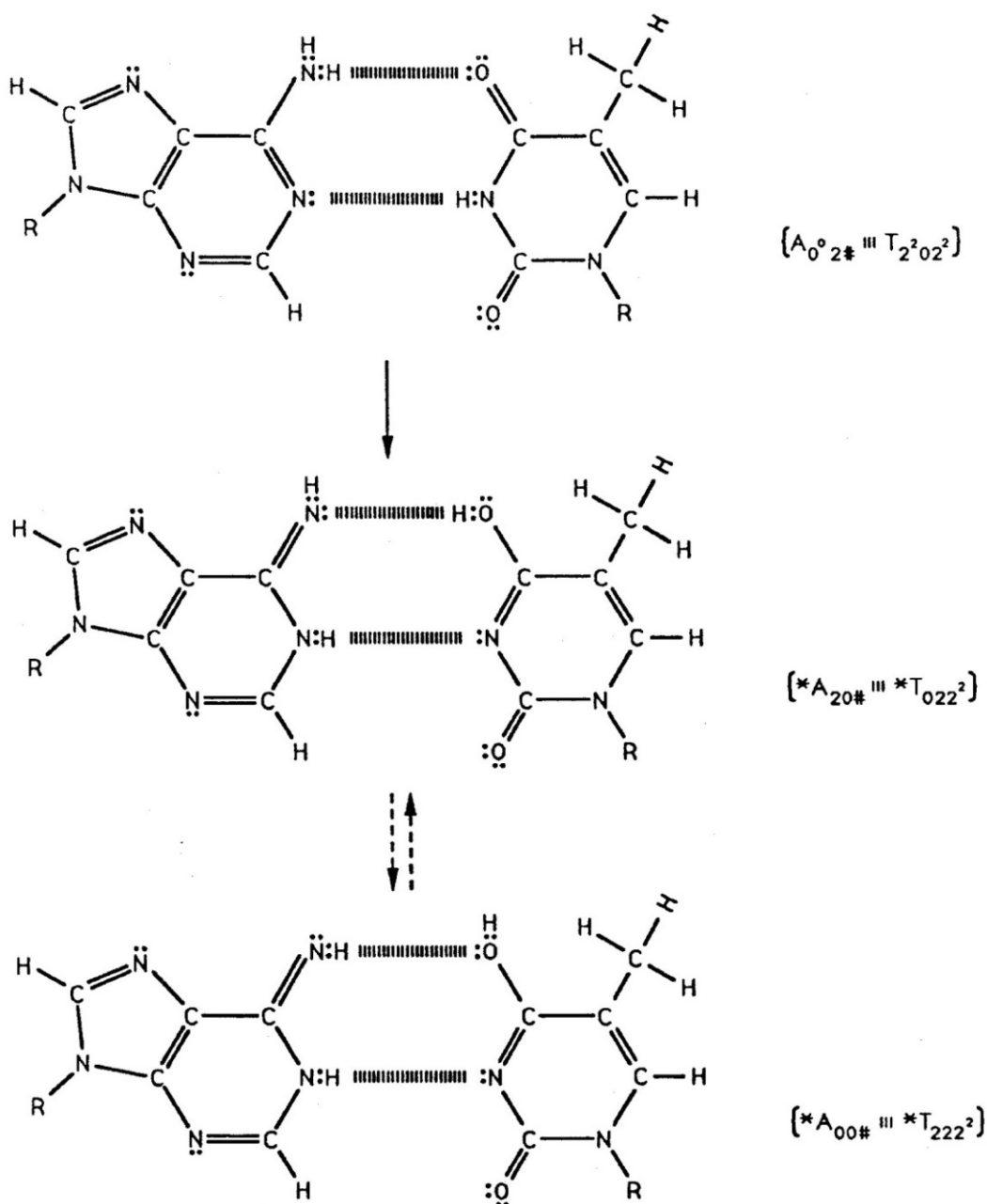


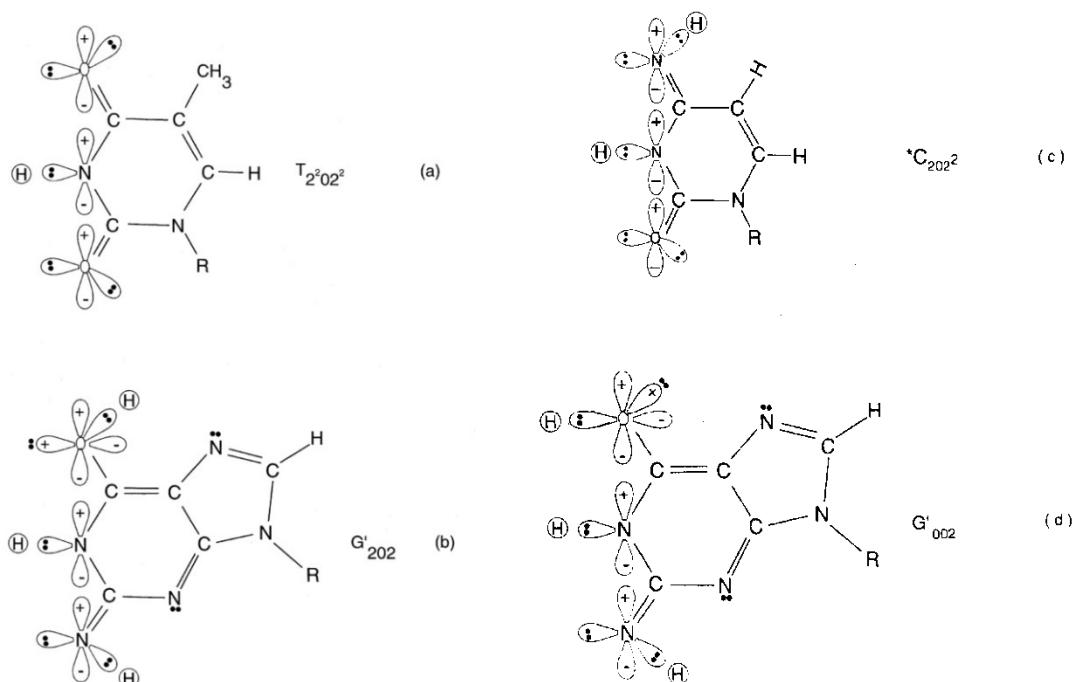
Figure 2. Array of possible coherent states at a G'-C' or *G-*C site.

(Symmetric, asymmetric and second asymmetric (unlabeled) channels ($\rightarrow$) by which metastable keto-amino G-C protons populate enol-imine states. Dashed arrows identify pathways for quantum mechanical flip-flop of enol-imine protons. Approximate electronic structures for hydrogen bond end groups and corresponding proton positions are shown for the metastable keto-amino duplex (a) and for enol-imine G'-C' coherent states (b-e). The asymmetric channel introduces the hybrid state superposition, *G-*C (f, g). Electron lone-pairs are represented by double dots and a proton by a circled H. Proton states are specified by a compact notation, using letters G, C, A, T for DNA bases with 2's and 0's identifying electron lone-pairs and protons, respectively, donated to the hydrogen bond by—from left to right—the 6-carbon side chain (see Figure 1 for numbering of atom positions), the ring nitrogen and the 2-carbon side chain. Superscripts identify the component at the outside position (in major and minor grooves) as either an amino group proton, designated by 0^0 , or a keto group electron lone-pair, indicated by 2^2 . Superscripts are suppressed for enol and imine groups).

Figure 3. Metastable and coherent A-T states.

(Pathway for metastable keto-amino A-T protons to populate enol-imine states. Dashed arrows indicate proton flip-flop pathway between coherent enol-imine *A-*T states. Notation is given in Figure 2 legend. The # symbol indicates the position is occupied by ordinary hydrogen unsuitable for hydrogen bonding).

Figure 4. Approximate proton electron hydrogen bonding structure “seen by” transcriptase systems when encountering (a) normal thymine, $T_2^2 0 2^2$; (b) coherent enol-imine $G'2 0 2$; (c) coherent imino cytosine, $*C2 0 2^2$, and (d) coherent enol-imine $G'0 0 2$.



Transcriptase quantum processing [8-13] of coherent enol-imine states includes selecting particular decohered enol and imine isomers to participate in time-dependent substitutions, *ts*, or time-dependent deletions, *td*. The fact that mutation frequencies, $G'2 0 2 \rightarrow T$ & $*C2 0 2^2 \rightarrow T$, phenotypically expressed via quantum transcription are identical to subsequent substitution frequencies, $G'2 0 2 \rightarrow T$ & $*C2 0 2^2 \rightarrow T$, expressed as a consequence of Topal-Fresco replication of decohered isomers indicates that consequences of *keto-amino* $\rightarrow$ *enol-imine* arrangements are “hard wired” into the DNA code [8,9]. In these cases of $G'2 0 2 \rightarrow T$ and $*C2 0 2^2 \rightarrow T$, transcriptase quantum processing specifies subsequent DNA replication substitution at G' and $*C$ sites. Otherwise one cannot explain how ~100% of the expressed coherent state population, e.g., $G'2 0 2$, exhibited by transcription is subsequently decohered to form the complementary mispair, $G'2 0 2$ -syn- $A0^0 2 \#$ (Table 1; Figure 5), *all of which* successfully participate in the $G'2 0 2 \rightarrow T$ substitution at replication [8,18]. The observed absence of reequilibration implies quantum entanglement participation [8,9]. In the next round of replication, coherent states and entanglement are absent, so ~20% of imine $*C2 0 2^2$ exhibits reequilibration, $*C2 0 2^2 \rightarrow C0^0 2 2^2$. Data [8,17,18] and the model [9-13] provide evidence that evolutionary pressures have selected quantum probability laws over laws of classical kinetics for (i) introducing time-dependent “point” genetic alterations, (ii) transcription of coherent states occupying decoherence-free subspaces and (iii) subsequent replication-substitution or deletion of selected decohered isomers. The present and previous reports [8-13] imply that the classical double helix of duplex DNA contains an embedded microphysical subset of hydrogen bonded protons and electron lone-pairs that (a) obey quantum probability laws and (b) govern time-dependent specificity of DNA information. These evolutionarily acquired quantum mechanisms for operating microphysical genetic systems imply gains in evolutionary advantages. Enhanced advantages include (A) possibilities of favorable population responses to changing environmental conditions and, concomitantly, (B) mechanisms of protecting the gene pool against

acquiring unsafe levels of mutation [8,13,34]. As a consequence of identifying quantum origins of *stochastic* mutations, *ts* + *td*, a quantum Darwinian evolution model is developed that simulates manifestation of cancer as a function of intrinsic DNA instability [35], and further, implies a quantum mechanism for evolutionary extinction.

Based on molecular genetic data [8,14-18] and the attendant model [9-13], genetic specificity within a DNA base pair is dependent on states of hydrogen-bonded DNA protons, which are allowed the possibility of transitioning through a cycle of physical states. This sequence of proton states can be visualized in terms of qualitative terminology: *classical amino* → *unperturbed coherent quantum entangled (enol-imine)* → *transcriptase quantum entanglement* → *entanglement-decoherence* → *decohered isomer* → *classical amino*. This model is a combination of the Löwdin [19] and Topal-Fresco [29] models, referred to as the LTF model, where consequences of entanglement are included. The next section identifies available genetic information as a function of hydrogen bonded proton states. Section 3 discusses molecular genetic observations requiring quantum theory for explanations. This is followed by introducing a two qubit model for coupled enol-imine proton oscillations created by quantum uncertainty limits on metastable amino protons. Section 5 develops a quantum Darwinian evolution model for time-dependent DNA instabilities. The model simulates incidence of cancer data and implies insight into evolutionary extinction. The final section contains the discussion. The Appendix develops an approximate quantum model for *keto-amino* → *enol-imine* arrangement.

2. Biological Information as a Function of Proton States: Classical Amino → Coherent Entangled Enol-imine → Transcriptase Entanglement → Decoherence-Entanglement → Decohered → Classical Amino

Consistent with evolutionary design, standard replication creates metastable, complementary keto-amino DNA base pairs where quantum uncertainty limits operate on amino DNA protons. The physical state of hydrogen bonded DNA protons plays a significant role in determining the nature of genetic information available to the biological system. The different hydrogen bond DNA proton environments at G-C sites are first (i), after replication, keto-amino protons are subjected to quantum uncertainty limits which introduces a probability of *keto-amino* → *enol-imine* arrangement via symmetric or asymmetric channels (Figures 1 to 2). Second (ii), unperturbed and entangled enol-imine hydrogen bonded protons participate in coupled quantum oscillations between near symmetric double minima at frequencies of $\sim 10^{13} \text{ s}^{-1}$ (Figure 2). Third (iii), the transcriptase implements its measurement on coherent protons, generating an output qubit of genetic specificity. Forth (iv), an entanglement state is created between coherent protons and transcriptase components. Fifth (v), an enzyme-entanglement participates in creating complementary Topal-Fresco mispairs (Table 1; Figure 5) consisting of non-reequilibrated enol and imine isomers, G', C', *G, & *C. Sixth (vi), entanglement ultimately generates a decoherent transition from quantum to classical, which allows non-reequilibrated enol and imine isomers to form complementary mispairs that are incorporated as *ts*. Seventh (vii), in the next round of replication, quantum coherence and entanglement are absent; so, reequilibration is allowed and keto-amino states are replicated into DNA.

As a consequence of transcriptase quantum processing of coherent states at G'-C' and *G-*C sites, an entanglement is created between coherent protons and transcriptase components. This entanglement state is evidently responsible for recognizing an initially “measured” quantum state (e.g., G'2 0 2) and preserving

this particular state and information through its decoherent transition, *i.e.*, G'2 0 2 (coherent) $\rightarrow$ G'2 0 2 (decohered isomer). After transcriptase quantum processing within an interval $\Delta t \ll 10^{-13}$ s [8,9], the initial round of replication involves the formation of complementary mispairs [8,18,29], e.g., G'2 0 2–syn-A0⁰ 2 # (Table 1; Figure 5b), between an entanglement preserved decohered enol-imine isomer (e.g., G'2 0 2) and, in this case, syn-A0⁰ 2 #. In the absence of entanglement between coherent G'2 0 2 protons and transcriptase components, the originally transcribed G'2 0 2 state would be exposed to H₂O. This would cause decoherence and introduce reequilibration, *i.e.*, G'2 0 2 (enol-imine) $\rightarrow$ G² 0 0⁰ (keto-amino). In fact, observation [8] shows that ~100% of quantum processed coherent G'2 0 2 and *C2 0 2² states subsequently contribute—in their decohered isomer form—to the replication-substitution step required for finalizing molecular clock substitutions, *ts*. In the absence of entanglement protection of enol and imine states, the observed *ts*—G'2 0 2 $\rightarrow$ T, *C2 0 2² $\rightarrow$ T, G'0 0 2 $\rightarrow$ C, *G0 2 0⁰ $\rightarrow$ A—would be at classical background levels governed by reequilibration, thereby eliminating detection of a time-dependent molecular clock [8,13,14,18]. These data further imply that enzymes responsible for quantum information processing of coherent states also participate in replicating particular *ts*. As noted, in the second round of replication after transcriptase quantum processing, coherent states and entanglement are absent. This allows ~20% of imine *C2 0 2² to exhibit reequilibration [8].

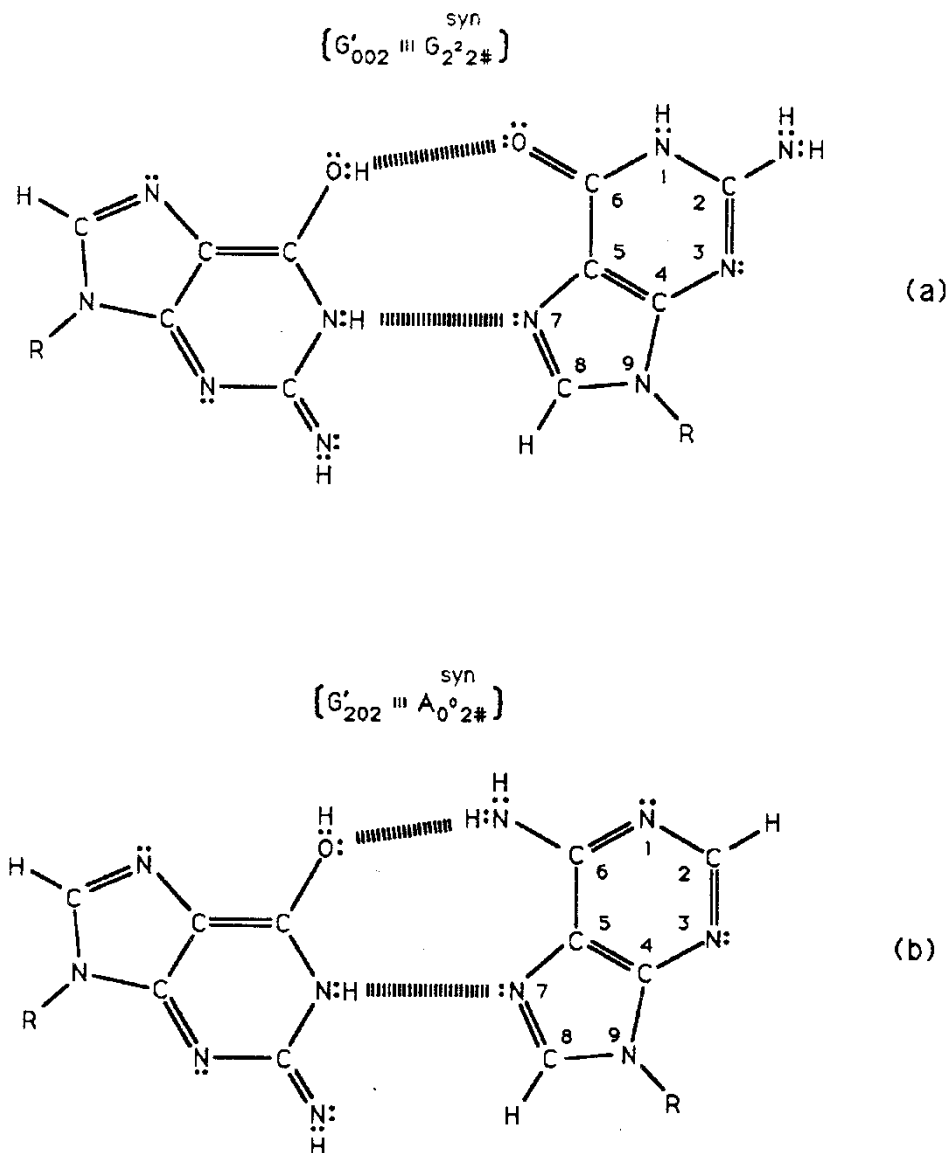
Table 1. Relation between coherent states, transcribed message and base substitution of decohered isomers.

←----- Allowable Pair Formation at Replication-----→							
←----- NORMAL ISOMERS-----→←----- SYN-Purines-----→							
Quantum States	G ² 00 ⁰	C ⁰ 22 ²	A ⁰ 2#	T ² 02 ²	G ² 2#	A ⁰ 2#	Transcribed Message
G'002					GC $\rightarrow$ CG		U [†]
G'202						GC $\rightarrow$ TA	T ² 02 ²
G'200		opaque					G ² 00 ⁰
G'000							U
*G020 ⁰				GC $\rightarrow$ AT			U
*G220 ⁰							U
C'220							U
C'020							U
C'022	opaque						C ⁰ 22 ²
C'222							U
*C202 ²			GC $\rightarrow$ AT				T ² 02 ²
*C002 ²							U
*A20#		AT $\rightarrow$ GC				AT $\rightarrow$ TA	U
*A00#					AT $\rightarrow$ CG		U
*T022 ²	AT $\rightarrow$ GC						C ⁰ 22 ²
*T222 ²							U

† Undefined.

Transcribed messages of coherent states, decohered isomers and formation of complementary mispairs for Topal-Fresco replication. Normal tautomers (top row) and coherent quantum flip-flop states/decohered tautomers (left column) are listed in terms of the compact notation for hydrogen-bonding configurations identified in Figure 2 Legend. Consistent with Topal-Fresco [29], base pair substitution notation at the respective row-column juncture identifies decohered tautomers that will form a complementary mispair with a normal base, including syn-purines. Transcribed messages obtained from a coherent quantum state are identified in the right hand column. Unusual pairs that do not exhibit mutation are identified as “opaque”.

Figure 5. Complementary mispairs between (a) enol-imine G'002 (Figure 2b) and syn-guanine (syn-G2²2#) and (b) enol-imine G'202 (Figure 2c) and syn-adenine (syn-A0⁰2#). The # symbol indicates the position is occupied by ordinary hydrogen unsuitable for hydrogen bonding.



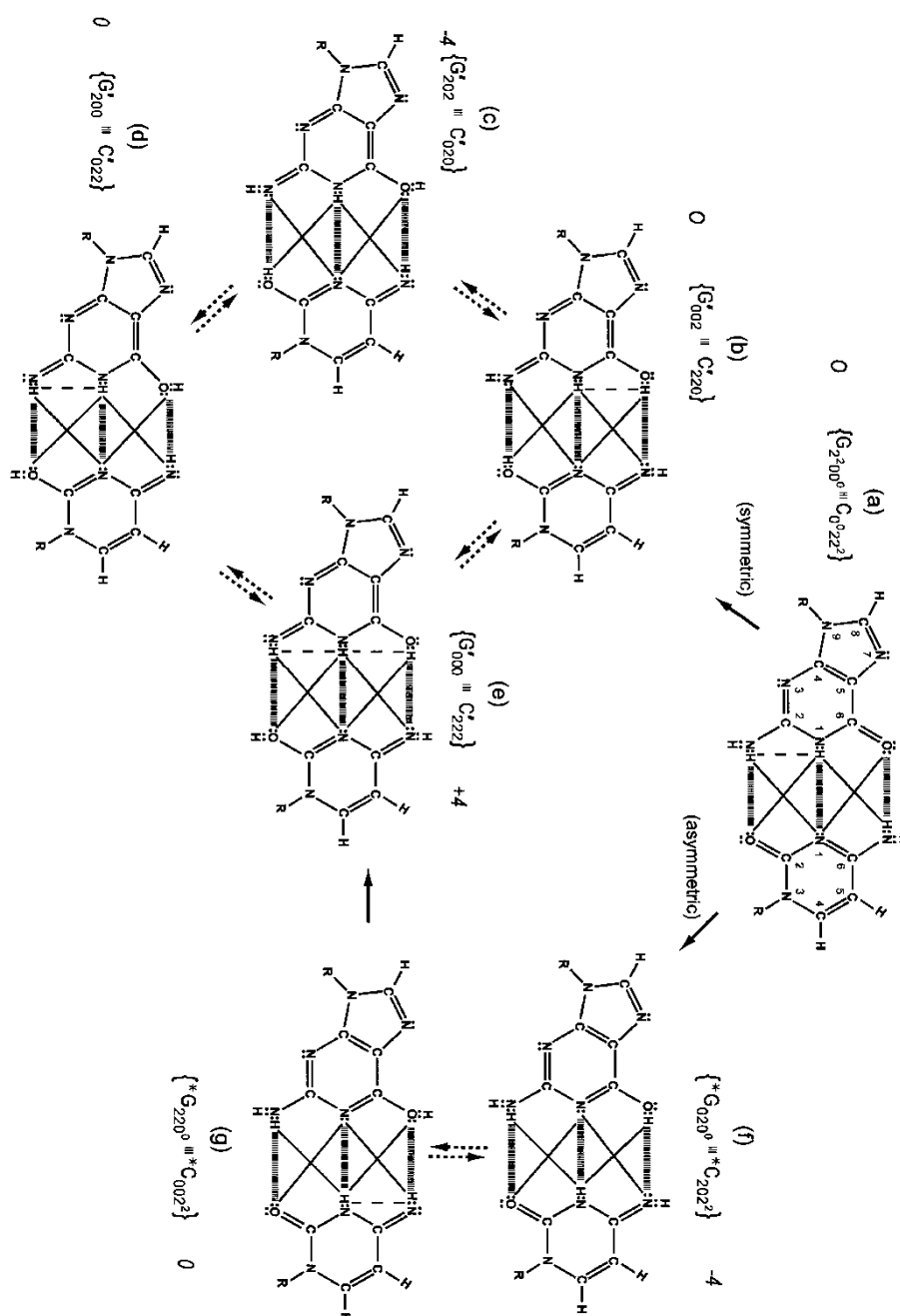
Metastable keto-amino duplex DNA implies the arrangement, *keto-amino* $\rightarrow$ *enol-imine*, and subsequent *ts* + *td* (stochastic mutations) should be observable in human DNA systems. Hwang and Green [13] have clearly shown that mammalian DNA exhibits time-dependent, replication independent molecular clock events, CpG $\rightarrow$ TpG substitutions, at the DNA level. The terminology, “CpG substitutions”, indicates C $\rightarrow$ T and/or G $\rightarrow$ A substitutions at a CpG site. Time-dependent CpG substitutions are the most frequent point mutation observed in the human genome and the rate is ~ 15 -fold greater when cytosine is methylated [16]. Since replicated keto-amino DNA duplex is metastable [8-13] and the observed CpG substitutions, C $\rightarrow$ T and G $\rightarrow$ A [14,16], are two of the four time-dependent substitutions exhibited by the high resolution T4 phage DNA system (*i.e.*, also, G'2 0 2 $\rightarrow$ T and G'0 0 2 $\rightarrow$ C), the argument is made that a significant component of CpG substitution is a consequence of *keto-amino* $\rightarrow$ *enol-imine* arrangements,

which are ultimately replicated as *ts* + *td* stochastic mutations [15]. A consequence of methylated cytosine (at carbon-5) is an enhancement of quantum uncertainty limits on cytosine $-\text{NH}_2$ protons, *i.e.*, $-\text{NH}_2 - - \text{H}_3\text{C}-$. From the uncertainty relation, $\Delta x \Delta p_x \geq \frac{1}{2} \hbar$, amino proton momentum can be expressed, approximately, as $p \approx \hbar/\Delta x$; so, proton kinetic energy can be approximated by $mv^2/2 = p^2/2m = \hbar^2/[2m(\Delta x)^2]$. However additional proton-proton interactions, $-\text{NH}_2 - - \text{H}_3\text{C}-$, would increase the probability of confining cytosine amino protons to too small of space, Δx . This would create more energetic cytosine amino ($-\text{NH}_2$) protons which would enhance the rates of *keto-amino* $\rightarrow$ *enol-imine* via the asymmetric channel, introducing $\text{C} \rightarrow * \text{C} \rightarrow \text{T}$ and $\text{G} \rightarrow * \text{G} \rightarrow \text{A}$ as observed [8,16-18]. Thus the ~ 15 -fold increase in $\text{CpG} \rightarrow \text{TpG}$ when cytosine is methylated is consistent with the quantum origin of *ts*. Also Elango *et al.* [16] note that vague mechanisms responsible for inserting H_2O between DNA strands are invoked if time-dependent $\text{CpG} \rightarrow \text{TpG}$ [14] events are explained in terms of hydrolytic deamination of cytosine.

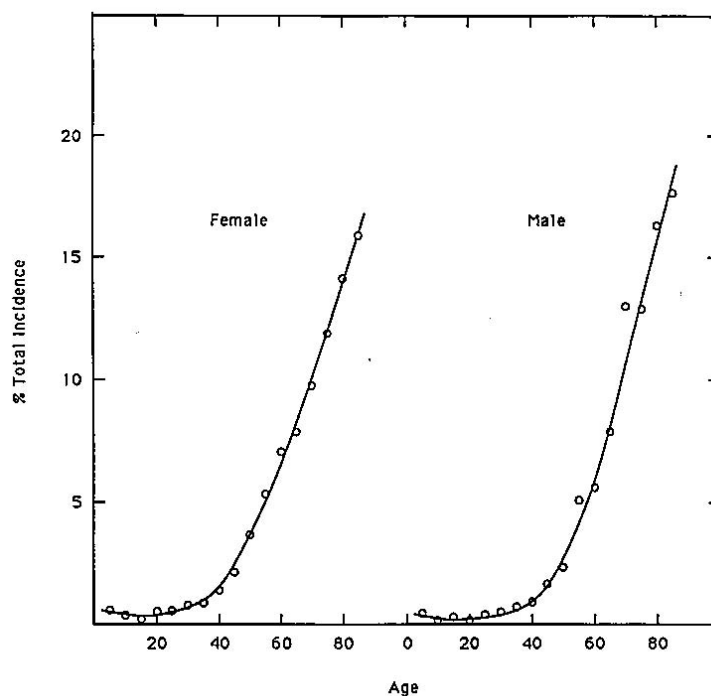
Observations consistent with quantum origins of stochastic mutations, *ts* and *td*, include (i) the prediction of a modest evolutionary shift favoring A-T richness [14]. Second (ii), when G' or $* \text{C}$ is on the template strand, mutation frequencies, $\text{G}' 2 0 2 \rightarrow \text{T}$ & $* \text{C} 2 0 2^2 \rightarrow \text{T}$, phenotypically expressed by quantum transcription—before replication—are identical to subsequent frequencies, $\text{G}' 2 0 2 \rightarrow \text{T}$ & $* \text{C} 2 0 2^2 \rightarrow \text{T}$, exhibited as consequences of genotypic incorporation by replication from decohered isomers. This implies participation of quantum entanglement [10,26-28]. In the next round of replication, quantum coherence and entanglement are absent; so, $\sim 20\%$ of imine cytosine (5HMC), $* \text{C} 2 0 2^2$, exhibits reequilibration, $* \text{C} 2 0 2^2 \rightarrow \text{C}^0 0 2^2$. This eliminates deamination of cytosine as the mechanism responsible for these time-dependent $\text{C}^0 0 2^2 \rightarrow * \text{C} 2 0 2^2 \rightarrow \text{T}$ events [8,17]. Third (iii), quantum processing by the transcriptase explains how enol and imine groups on quantum states $\text{G}' 2 0 2$ and $* \text{C} 2 0 2^2$ can simulate keto groups on normal $\text{T} 2^2 0 2^2$ at transcription, as observed [8,9]. This mode of determining specificity distinguishes the quantum state $\text{G}' 2 0 2$ ($\text{G}' 2 0 2 \rightarrow \text{T}$) from quantum state $\text{G}' 0 0 2$ ($\text{G}' 0 0 2 \rightarrow \text{C}$) and is tolerant of gross structural dissimilarities between the dual ring purine, $\text{G}' 2 0 2$, and the single ring pyrimidines, $* \text{C} 2 0 2^2$ and $\text{T} 2^2 0 2^2$, as observed [8,9]. Forth (iv), the fact that the yield of $\text{G}' 2 0 2 \rightarrow \text{T}$ is ~ 3 -fold (rather than 2-fold) greater than $\text{G}' 0 0 2 \rightarrow \text{C}$ is explained by arguments that the duplex quantum state, $\text{G}' 2 0 2 - \text{C}' 0 2 0$ (Figure 2c), is “preferred” compared to the duplex quantum state, $\text{G}' 0 0 2 - \text{C}' 2 2 0$ (Figure 6). Fifth (v), the ~ 15 -fold increase in $\text{CpG} \rightarrow \text{TpG}$ rates when cytosine is methylated is consistent with quantum expectations for increased proton-proton interactions, $-\text{NH}_2 - - \text{H}_3\text{C}-$, causing enhanced reaction rates, $\text{C}^0 0 2 2^2 \rightarrow * \text{C} 2 0 2^2 \rightarrow \text{T}$, via the asymmetric channel. Since time-dependent CpG substitutions are the most frequent point mutation observed in the human genome [16], these $\text{CpG} \rightarrow \text{TpG}$ events should contribute to the stochastic mutation spectrum in Equation (18). However, deamination of cytosine disallows the quantum mechanical term, βt , in Equation (13). Thus, deamination of cytosine is not in agreement with a model, Equation (18), which satisfies data, Figure 7 [35]. Also the facts that (a) after $* \text{C} 2 0 2^2 \rightarrow \text{T}$, imine $* \text{C} 2 0 2^2$ exhibits reequilibration, $* \text{C} 2 0 2^2 \rightarrow \text{C}^0 0 2 2^2$, in the second round of growth [8] and (b) mechanism for inserting H_2O between DNA strands exhibit difficulties [16] argue against deamination of cytosine as the mechanism responsible for time-dependent $\text{CpG} \rightarrow \text{TpG}$ [13]. Additionally, the extensive investigation by Ripley [17] could not identify evidence supporting deamination of cytosine (5HMC) as the mechanism responsible for the time-dependent substitution, $\text{C} \rightarrow * \text{C} \rightarrow \text{T}$. Sixth (vi), the time-dependent substitutions observed at a mammalian CpG site, $\text{C} \rightarrow \text{T}$ and/or $\text{G} \rightarrow \text{A}$, represent 50% of coherent state *ts* exhibited by the higher resolution T4 phage DNA system, *i.e.*, also $\text{G}' 2 0 2 \rightarrow \text{T}$, $\text{G}' 0 0 2 \rightarrow \text{C}$ and $* \text{A} - * \text{T} \rightarrow \text{deletion}$ [8,9]. These six observations are consistent with quantum uncertainty limits operating on metastable amino DNA protons, which drive the arrangements, *keto-amino* $\rightarrow$ *enol-imine*, thereby populating accessible lower

energy enol-imine coherent states, $G'-C'$, $*G-*C$ and $*A-*T$ (Figures 1 to 3). Since the wave function for coherent enol-imine protons cannot be expressed as a tensor product, these protons are entangled [27,28]. Subsequent transcriptase quantum processing introduces a new entanglement between coherent protons and transcriptase components. Ultimately this entanglement yields decohered enol and imine isomers that are replicated as *ts* and *td*, which contribute to the spectrum of *stochastic* mutations [8-18].

Figure 6. Qualitative representation of more abundant and less abundant coherent G-C states.



(Secondary interaction model [36,37] applied to coherent superposition $G'-C'$ and $*G-*C$ states for purposes of identifying relative base pairing energies. A +1 is assigned to each secondary interaction between opposite charges and a -1 for an interaction between same sign charges, yielding a +4 for state (e) and a -4 for flip-flop states (c) and (f). The remaining four states—(a), (b), (d), (g)—are intermediate with base pairing energy values of 0. The dashed lines identify intramolecular proton-proton repulsion).

Figure 7. Cancer incidence as a function age.

Average age distribution of all “Class 1” tumors (those with a single peak incidence at age > 50 y) classified by the Connecticut Tumor Registry between 1968 and 1972 (Graph reproduced from Figure 2 of Dix *et al.* [35]).

3. Explicit Evidence Exhibiting Quantum Information Technology by a Biological System

3.1. Multiple Genetic Specificities Exhibited by a ‘Point’ Mutation G' Site

Time-dependent transversions originate at G'-C' sites [8,17,18] where a complementary duplex contains a superposition of four quantum states illustrated in Figure 2b-e. In the case of rUV74 $rII \rightarrow r^+$ transversion revertants, G' is on the T-strand. Data demonstrate that 350 of the 460 (76%) revertants detected express G'2 0 2 $\rightarrow$ T as a consequence of transcription *before* replication was initiated, but 110 of the 460 (24%) revertants required replication (passage) to express G'0 0 2 $\rightarrow$ C. In this case, genetic specificities originating within quantum states, G'2 0 2-C'0 2 0 (Figure 4b) $\rightleftharpoons$ G'0 0 2-C'2 2 0 (Figure 4d), are deciphered by the transcriptase on the basis of different coherent states for the guanine carbon-6 enol proton, which participates in coupled quantum oscillation. State G'0 0 2 communicates that it is *not* a transcription analog of C0⁰ 2 2² or T2² 0 2²; so, passage (replication) is required for expression of the G'0 0 2 $\rightarrow$ C substitution, which involves Topal-Fresco replication of the complementary mispair, G'0 0 2-syn-G2² 2 # (Figure 5), to insert normal C0⁰ 2 2². Compared to state G'0 0 2, expression of state G'2 0 2 was enhanced by a single round of transcription *before* replication was initiated. After transcription and before replication, the template quantum state, G'2 0 2, was *not* subjected to H₂O and reequilibration, but was preserved by entanglement between coherent protons and transcriptase components. Additionally, *all* decohered G'2 0 2 isomers formed complementary mispairs, G'2 0 2-syn-A0⁰ 2 # (Table 1; Figure 5), required for the G'2 0 2 $\rightarrow$ T substitution resulting from Topal-Fresco replication. Given these two conditions, straightforward analysis predicts the number of G'2 0 2 $\rightarrow$ T events should be ~2-fold greater (after passage) than the number of G'0 0 2 $\rightarrow$

C events. However observation shows $G'2\ 0\ 2 \rightarrow T$ (76%) is ~ 3 -fold more numerous than $G'0\ 0\ 2 \rightarrow C$ (24%). Since the quantum state $G'2\ 0\ 2$ is “preferred” compared to state $G'0\ 0\ 2$ (Figure 6; Section 3.2), this would cause an enhanced availability of quantum $G'2\ 0\ 2$ at transcription and a corresponding increased yield of the decohered $G'2\ 0\ 2$ isomer at replication, which would explain the greater than expected yield, *i.e.*, 3-fold rather than 2-fold, of $G'2\ 0\ 2 \rightarrow T$ compared to $G'0\ 0\ 2 \rightarrow C$.

3.2. Consequences of the “Favored Status” for the Quantum State, $G'2\ 0\ 2$

Although quantum proton oscillations are the order of $\sim 10^{13}\ s^{-1}$ [9,10], the relative distribution of quantum duplex $G'-C'$ states can be qualitatively estimated, using Jorgensen’s model [36,37] for secondary electrostatic interactions within a superposition of complementary duplex states. This is illustrated in Figure 6 where the duplex state $G'000-C'222$ (Figure 6e) exhibits the maximum *intramolecular* proton-proton repulsion and thus is the least preferred configuration. This state is identified by an energy pairing value of +4. The preferred states exhibit the minimum intrabase proton-proton repulsion interactions and are identified in Figure 6c, 6f. These preferred configurations yield energy pairing values of −4. Since the $G'2\ 0\ 2-C'0\ 2\ 0$ duplex (Figure 6c) is a favored “relaxed” configuration compared to $G'0\ 0\ 2-C'2\ 2\ 0$ (Figure 6b), this would cause an enhanced availability of quantum $G'2\ 0\ 2$ at transcription and a corresponding increased yield of the decohered $G'2\ 0\ 2$ isomer at replication, which would explain the greater than expected yield, *i.e.*, 3-fold rather than 2-fold, of $G'2\ 0\ 2 \rightarrow T$ compared to $G'0\ 0\ 2 \rightarrow C$. This observation implies that local electric and magnetic fields and currents created by coherent enol-imine protons (Figure 4) may allow “delicate”, evolutionarily designed information processing by transcriptase measurements of genetic specificities on, *e.g.*, $G'2\ 0\ 2$ and $G'0\ 0\ 2$. Note that quantum duplex states $G'2\ 0\ 2-C'0\ 2\ 0$ (Figure 6c) and $*G'0\ 2\ 0^0-^*C'2\ 0\ 2^2$ (Figure 6f) are the only “preferred” configurations in Figure 6. Additionally quantum states, $G'2\ 0\ 2$ and $*C'2\ 0\ 2^2$, are each transcribed as normal $T2^2\ 0\ 2^2$ and, therefore, are responsible for the 2-fold “transcription enhancement” of mutation, $G'2\ 0\ 2 \rightarrow T$ and $*C'2\ 0\ 2^2 \rightarrow T$ [8]. Evidently this is a component of the time-dependent evolutionary scheme favoring A-T richness [8].

4. Transcriptase Measurement of Entangled Proton Bonds at $G'-C'$ Sites

The symmetric *keto-amino* $\rightarrow$ *enol-imine* arrangement converts the two standard keto-amino G-C hydrogen bonds into two sets of coupled two-level enol-imine proton bonds where the four coherent enol and imine protons “participate equally” in coupled quantum oscillations between the eight available sets of near symmetric electron lone-pairs, illustrated in Figure 2b to 2e. The transcriptase implements its measurements from the T-strand orientation and deciphers information from the distribution of coherent states exhibited by enol-imine proton bonds at the carbon-6 and carbon-2 side chain positions of a $G'-C'$ duplex (Figure 2). Quantum measurements by the transcriptase ultimately transform this information into observable biochemical instruction, *e.g.*, $G'2\ 0\ 2 \rightarrow T$ versus $G'0\ 0\ 2 \rightarrow C$. The fact that transcriptase measurements on coherent $G'-C'$ states yield decohered observable results that are in qualitative agreement with the distribution of $G'-C'$ states predicted by Jorgensen’s [36,37] model (Figure 6) implies the transcriptase “reads”, processes and executes information derived from coupled coherent protons states within an interval, $\Delta t \ll 10^{-13}\ s$.

The quantum state of the enol-imine proton bond at the G'-C' carbon-6 side chain is taken as state $|+->$ when the enol proton on G' is positioned to participate in interstrand bonding and is in state $|->$ when this enol proton is "outside", in the major or minor groove. In this notation, the second symbol in state $|+->$ identifies the "-" or "+" quantum state of the coupled imine C' proton in the carbon-6 side chain proton bond. Similarly, the imine-enol proton bond at the G'-C' carbon-2 side chain is in state $|+->$ when the imine proton on G' is positioned to participate in interstrand bonding and is in state $|->$ when this imine proton is "outside", in the major or minor groove. The proton bonds at the carbon-6 and carbon-2 side chains can each be described in terms of two quantum states, $|+->$ and $|->$. In this discussion, state $|+->$ is taken as $|g>$ and state $|->$ is defined as $|c>$. These two states obey the relation, $\langle g|c\rangle = \delta_{gc}$, and provide a computational basis for the carbon-6 and carbon-2 side chain proton bonds, hereafter identified by b_6 and b_2 , respectively.

Coherent enol-imine proton bonds at a G'-C' site constitute two subspaces, $\epsilon_x(6)$ and $\epsilon_x(2)$, of the combined space, ϵ_x . Other pure states of the proton bond can be expressed as a superposition, $\alpha|g> + \beta|c>$, for some α and β where $|\alpha|^2 + |\beta|^2 = 1$. The position states of proton bond b_6 form a two-dimensional subspace $\epsilon_x(6)$, and likewise, the position state of proton bond b_2 is defined by a ket belonging to a two-dimensional state space, $\epsilon_x(2)$. The position observables of b_6 and b_2 are designated by $\mathbf{x}_6$ and $\mathbf{x}_2$, respectively. In $\epsilon_x(6)$ and $\epsilon_x(2)$, the basis eigenkets of $\mathbf{x}_6$ and $\mathbf{x}_2$ are designated by $|6: g>$, $|6: c>$ and $|2: g>$, $|2: c>$. The general ket of $\epsilon_x(6)$ can be written as

$$|\chi(6)> = \alpha_6|6: g> + \beta_6|6: c> \quad (1)$$

and that of $\epsilon_x(2)$ is given by

$$|\zeta(2)> = \alpha_2|2: g> + \beta_2|2: c> \quad (2)$$

where $\alpha_6, \beta_6, \alpha_2, \beta_2$ are arbitrary complex numbers. The proton bonds, b_6 and b_2 , can be coalesced into a four-dimensional state space, ϵ_x , by expressing the tensor products of $\epsilon_x(6)$ and $\epsilon_x(2)$ as

$$\epsilon_x = \epsilon_x(6) \otimes \epsilon_x(2) \quad (3)$$

This yields the following ket notation as

$$\begin{aligned} |g g> &= |6: g> |2: g> \\ |g c> &= |6: g> |2: c> \\ |c g> &= |6: c> |2: g> \\ |c c> &= |6: c> |2: c> \end{aligned} \quad (4)$$

where $\langle g|$ is the conjugate bra of the ket $|g>$. Since the bases $\{|6: gc>\}$ and $\{|2: gc>\}$ are orthonormal in $\epsilon_x(6)$ and $\epsilon_x(2)$ respectively, the basis given by Eq (4) is orthonormal in ϵ_x , expressed as

$$\langle \epsilon_6 \epsilon_2 | \epsilon_6 \epsilon_2 \rangle = \delta_{\epsilon_6 \epsilon_6} \delta_{\epsilon_2 \epsilon_2} \quad (5)$$

Also the system of vectors in Equation (4) satisfy a closure relation in ϵ_x given by

$$\sum_{\epsilon_6 \epsilon_2} |\epsilon_6 \epsilon_2\rangle \langle \epsilon_6 \epsilon_2| = |g g\rangle \langle g g| + |g c\rangle \langle g c| + |c g\rangle \langle c g| + |c c\rangle \langle c c| = 1 \quad (6)$$

A ket of ϵ_x can be constructed in terms of an arbitrary ket of $\epsilon_x(6)$ and an arbitrary ket of $\epsilon_x(2)$, given by

$$|\chi(6)> |\zeta(2)> = \alpha_6 \alpha_2 |g g> + \alpha_6 \beta_2 |g c> + \alpha_2 \beta_6 |c g> + \beta_6 \beta_2 |c c> \quad (7)$$

The components of Equation (7) in the basis of Equation (4) are the products of $|\chi(6)\rangle$ and $|\zeta(2)\rangle$ in the bases of $\epsilon_x(6)$ and $\epsilon_x(2)$, which were used to construct Equation (4). However, not all kets of ϵ_x can be expressed as tensor products. The most general ket of ϵ_x is an arbitrary linear combination of the basis vectors given by

$$|\psi\rangle = \alpha |gg\rangle + \beta |gc\rangle + \gamma |cg\rangle + \delta |cc\rangle = \alpha |++--\rangle + \beta |+- - +\rangle + \gamma |-++-\rangle + \delta |-+-+\rangle \quad (8)$$

where for normalization, $|\alpha|^2 + |\beta|^2 + |\gamma|^2 + |\delta|^2 = 1$. Equation (8) cannot generally be expressed as a tensor product of $|\chi(6)\rangle$ and $|\zeta(2)\rangle$, in which case Equation (8) would be the form for an entangled state. In order for Equation (8) to be the form of Equation (7), the condition, $\alpha/\beta = \gamma/\delta$, is required, which is not necessarily satisfied.

Given Equation (8) describes the four-state G'-C' (Figure 2b to 2e) superposition system just before transcriptase measurement, one can express the probability of finding the system in each of its states. For example, the probability of the system being in state G'0 0 0-C'2 2 2 as assayed by transcriptase measurement is expressed as

$$| \langle ++-- | \psi \rangle |^2 = |\alpha|^2 \quad (9)$$

Similarly, the probabilities of the system being in states G'0 0 2-C'2 2 0, G'2 0 0-C'0 2 2 and G'2 0 2-C'0 2 0 are given respectively by

$$| \langle +- - + | \psi \rangle |^2 = |\beta|^2 \quad (10)$$

$$| \langle - + + - | \psi \rangle |^2 = |\gamma|^2 \quad (11)$$

$$| \langle - + - + | \psi \rangle |^2 = |\delta|^2 \quad (12)$$

Observables yielded by transcriptase measurements, e.g., $| \langle - + - + | \psi \rangle |^2 = |\delta|^2$ and $| \langle ++-- | \psi \rangle |^2 = |\alpha|^2$, are in qualitative agreement with the distribution of G'-C' states predicted by Jorgensen's [36,37] model shown in Figure 6. The relative contribution of the "preferred" state, G'2 0 2-C'0 2 0, is quantified by $|\delta|^2$, which is observed as the no. of G'2 0 2 $\rightarrow$ T events. Observation shows that $|\delta|^2$ is ~3-fold, rather than 2-fold, $> |\beta|^2$, which is consistent with Figure 6. Data and Figure 6 imply that $|\beta|^2 \approx |\gamma|^2$, which provides the relation $|\delta|^2 = 3|\beta|^2 = 3|\gamma|^2$. These values in the normalization expression yield $|\alpha|^2 = -2/9$, so $\alpha = \frac{\pm i\sqrt{2}}{3}$. The condition, $\alpha/\beta = \gamma/\delta$, is not satisfied by these values for α , β , γ & δ , indicating Equation (8) cannot be expressed as a tensor product of $|\chi(6)\rangle$ and $|\zeta(2)\rangle$; so, Equation (8) is the form for entangled enol-imine proton states. Since the transcriptase reads G'2 0 0-C'0 2 2 as normal G2² 0 0⁰-C0⁰ 2 2², the condition that $|\beta|^2 \approx |\gamma|^2$ could also be determined from clonal analysis [17]. Decohered observables from transcriptase measurements yield the relative distribution of quantum duplex G'-C' states at time of measurement, which are in qualitative agreement with Figure 6 predictions.

Consistent with an embedded microphysical subset designed to store and expresses quantum information, coherent states in duplex DNA are introduced into decoherence-free subspaces as consequences of quantum uncertainty limits on "metastable" amino DNA protons. Before decoherence, these states are measured by a transcriptase "quantum reader". Molecular genetic data [8,14] in terms of quantum theory suggest that complementary C'-state protons and electron lone-pairs

could be “replaced by” an active transcriptase site that simulates C'-contributions in the G'-C' duplex. This would allow the evolutionarily designed transcriptase system to identify, process and preserve the particular quantum distribution of coherent G'-states, which is ultimately decohered into non-reequilibrated enol and imine G'-isomers suitable for Topal-Fresco replication-substitution. Evolutionarily selected decohered enol and imine isomers participate in particular time-dependent base substitutions, ts , $G'2 \ 0 \ 2 \rightarrow T$, $G'0 \ 0 \ 2 \rightarrow C$, $*G0 \ 2 \ 0^0 \rightarrow A$, $*C2 \ 2 \ 2^2 \rightarrow T$ —and deletions, td , $*A-*T \rightarrow$ deletion. Consistent with observation [8,14], the quantum molecular clock [13] implies a modest evolutionary shift in A-T richness. Additionally, the quantum Darwinian evolution model, Section 5, predicts time-dependent increases in *stochastic* mutations, *i.e.*, $ts + td$, which satisfy incidence of cancer data, Figure 7. The evolutionarily selected quantum mechanisms responsible for generating coherent G'-C' & *G-*C states and decohered enol and imine isomers further employ a process of disallowing reequilibration before the initial round of replication. If re-equilibration were allowed, quantum contributions to the molecular clock— $\sum_j (\beta_j/12) t^4$ terms in Equation (18)—would *not* be allowed, which is inconsistent with observation [8,13,14]. Therefore the selected quantum processes responsible for exhibiting a time-dependent molecular clock include a “protection mechanism” which is assumed to involve contributions by quantum entanglement states. These apparent entanglements between coherent protons and transcriptase components play a central role in forming decohered, complementary mispairs (Table 1) responsible for genotypic Topal-Fresco substitution-replication. Evolutionary pressures at the quantum level have selected effective mechanisms for implementing quantum information processing at biological temperatures. Coupled entangled enol-imine states contributed by both DNA strands would enhance quantum stability and, thus, improve the accuracy of transcriptase quantum processing. Further study of this evolved qubit system may provide insight into the dynamics of avoiding decoherence [21–25] and an improved understanding of entanglement [5,26–28] and the transition from quantum to classical.

5. Quantum Instabilities in Genetic Specificities Imply a Quantum Darwinian Evolution Model for Origin of Tumors

5.1. Polynomial Expression

Quantum uncertainty limits [38] operating on amino DNA protons in metastable keto-amino base pairs introduce arrangements [8–13], *keto-amino* $\rightarrow$ *enol-imine* (Figure 2), consistent with evolutionary design. This implies an evolutionary origin of cancer hypothesis [39–41] where particular sensitive genes, *e.g.*, oncogenes & tumor suppressor genes [15,42], have been selected to participate in species preservation by removing from the gene pool those genomes that have accumulated unsafe levels of $ts + td$, which are consequences of *keto-amino* $\rightarrow$ *enol-imine* arrangements. These genes containing sensitive “genetic domains” are referred to as “p53-type” genes. Data in Figure 7 exhibit the average percentage total incidence of all 74 classifications of class 1 tumors (those with a single incidence peak at age > 50 year) classified by the Connecticut Tumor Registry between 1968 and 1972 [35]. These data illustrate increasing incidence of cancer in populations of advancing age. The hypothesis [39] that cancer is an inevitable part of evolution is consistent with observations [14] that multiple *stochastic* mutations [16,43] are responsible for the final conversion to malignancy in colorectal cancer [15]. In

fact, detailed mechanisms of *stochastic* mutations [8-13] imply that age-related degenerative diseases, including cancers, are evolutionarily implemented as consequences of *stochastic* mutations revealing contents of “latent” genetic information. Expression of “latent” genetic information, e.g., *K-ras* or *p53* containing a threshold level of *stochastic* mutations, can be manifested as a lethal cancer [15,42], consistent with protecting the gene pool against unsafe levels of mutation [8,34]. Since molecular genetic observations of time-dependent mutations require quantum coherence [8,18] and quantum chemical calculations identify keto-amino duplex DNA as metastable [9-13], Figure 7 data imply time-dependent genetic consequences [14,15]. In particular, a mathematical relationship is implied for phenotypic expression of cancer as a function of time-dependent alteration of genetic specificities in a normal target domain of “p53-type” genes, *g*. This model considers *M* individuals ($M \geq 100,000$)—the population—who have inherited a normal target domain of “p53-type” genes. Since experimental lifetimes of metastable keto-amino states at 37 °C are $\geq \sim 3000$ year [9], approximate quantum methods for small times, $t < \sim 100$ year, yield the probability, $P(t)$, of *keto-amino* $\rightarrow$ *enol-imine* arrangements as $P_p(t) = \frac{1}{2} (\gamma_p / \hbar)^2 t^2$ where γ_p is the energy shift between states (see Appendix). The time derivative of biological noise, dN/dt , accumulating in the particular gene, *g*, can be expressed as

$$dN/dt = \lambda + \beta t \quad (13)$$

Here λ is the classical constant mutational load discussed by Muller [44] and $\beta = (\gamma/\hbar)^2$, which is the proportionality constant for the *keto-amino* $\rightarrow$ *enol imine* arrangement. A general expression for the total biological noise, $N(t)$, in all *M* individual genes, *g*, in the population at age *t* is given by

$$N(t) = M \left\{ N_0 + \sum_{i=1}^m \lambda_i t + \sum_{j=1}^m \left(\frac{\beta_j}{2} \right) t^2 \right\} \quad (14)$$

where N_0 is the average number of mutations per gene *g* in the population of *M* at $t = 0$. The sum $\sum_{i=1}^m$ is over all *m* G-C + A-T pairs in the gene where mutations originate by classical mechanisms. The sum $\sum_{j=1}^m$ is over the same G-C + A-T pairs where mutations are consequences of *keto-amino* $\rightarrow$ *enol imine* arrangements that yield *ts* + *td* [8,9].

This model assumes that target gene *g* can—as a consequence of accumulating an evolutionarily defined level of alterations in genetic specificities—be “converted” into a disease producing mode. The time rate of change of converted target genes, $dg(t)/dt$, is proportional to the total number of *ts* + *td* in the relevant genetic domain plus generation dependent mutations contained in all *M* genes, $g(t)$, in the population at age *t*. This is given by

$$d/dt \, g(t) = 1/K \, N(t) \quad (15)$$

where the proportionality constant is $1/K$ and $N(t)$ is the noise defined in Equation (14). The number of converted target genes, $g(t)$, in the population of *M* at age *t* is given by

$$g(t) = g_0 + M/K \left\{ N_0 t + \sum_{i=1}^m \left(\lambda_i / 2 \right) t^2 + \sum_{j=1}^m \left(\beta_j / 6 \right) t^3 \right\} \quad (16)$$

where g_0 is the number of converted genes in the population at $t = 0$. Phenotypic expression incidence, $E(t)$, in the population of age *t* would change at a rate, dE/dt , which is proportional to the total number of converted genes, $g(t)$, in the population. This relationship is expressed as

$$d/dt E(t) = 1/B g(t) \quad (17)$$

where $1/B$ is the proportionality constant. The incidence of phenotypic expression, $E(t)$, in the population at age t is given as

$$E(t) = E_0 + (g_0/B)t + M/2KB \{N_0 t^2 + \sum_{i=1}^m \left(\lambda_i/3\right) t^3 + \sum_{j=1}^m \left(\beta_j/12\right) t^4\} \quad (18)$$

where E_0 is the incidence at $t = 0$. Here time $t = 0$ when the egg is fertilized; so, at $t = 0$, $E_0 = 0$ and coherent states are absent. In this case, N_0 is the average number of inherited mutations per gene, including **ts** + **td**. However, coherent states would not be inherited, but accumulate with time. Initial conditions (observation) specify the value of g_0 . Phenotypic expression, $E(t)$, of cancer is a consequence of transcription ultimately yielding mutant disease protein, which can occur without replication [8,18]. Dix *et al.* [35] noted that differences between male and female incidence curves in Figure 7 are negligible and that both are proportional to t^4 . According to Equation (18), the time-dependence for populating “p53-type” genes with **ts** + **td** is described by quantum mechanical contributions, $\sum_{i=1}^m \left(\lambda_i/3\right) t^3 + \sum_{j=1}^m \left(\beta_j/12\right) t^4$, which simulate these average incidence of cancer

data. This analysis clearly implies that phenotypic expression of the 74 class 1 tumors (Figure 7) is *primarily a consequence* of quantum mechanical arrangements, *keto-amino* → *enol-imine*, yielding **ts** + **td** which originate consistent with evolutionary selection. Accordingly, the four substitutions—G'2 0 2 → T, *C2 0 2 → T, G'0 0 2 → C & *G0 2 0 → A (see Figure 2 for notation)—and two deletions, *A → deletion and *T → deletion, are the evolutionarily selected *stochastic* mutations that reveal “latent” genetic information contained in “p53-type” genes. As a consequence of an evolutionarily selected “genetic threshold” becoming populated to its allowed limit by **ts** + **td**, particular “latent” genetic information is expressed. In “p53-type” genes, this causes manifestation of cancer [15,42] and thus protects the gene pool against acquiring unsafe levels of mutation. This model of coherent states populating expanded (CAG)_n repeats inherited by human genomes [10,11] simulates data on phenotypic expression of Huntington’s disease and, therefore, may be generally applicable to expression of age-related disease, including Alzheimer’s.

5.2. Model Implications and Evolutionary Consequences

Certain “class 2” tumors (e.g., bone, lymphatic leukemia, testis and Hodgkin’s disease) exhibit high incidence peaks at age < 35 and a second peak at age > 50. Also several childhood cancers exhibit high incidence peaks at ages < 10 [35]. In situations where the inherited “p53-type” gene contained genetic sites previously populated by **ts** + **td**, the remaining “genetic space” for occupancy by **ts** + **td** would be reduced; so, high incidence peaks could be exhibited for ages < 10 or ages < 35 y. However if the “p53-type” gene were populated by **ts** + **td** to its threshold limit at time of conception, the model implies spontaneous abortion would be a consequence; so, $g_0 = 0$ in Equation (18). This argument implies the available “genetic space”, s , associated with a “p53-type” gene satisfies the inequality, *normal* ≥ s ≥ *threshold*. Thus an inherited “p53-type” genetic domain would contain a variable “genetic space”, s , for occupancy by **ts** + **td** before achieving the threshold limit. Since mean lifetimes, τ , for the metastable state are ~3000 year [9], at age

100 year approximately 3% of the G-C + A-T sites would be occupied by *ts* + *td*. This implies a relationship between *normal* and *threshold*. If *normal* is identified as 100% free of *ts* + *td*, then the *threshold* can be approximated by $threshold = normal - 3\%$. The genetic space inequality can thus be rewritten as $1 \geq s \geq 0.97$. As the available inherited genetic space, *s*, approaches the threshold limit in subsequent generations, smaller times are required for *ts* + *td* to populate *s* such that the threshold limit is achieved, $s \approx 0.97 + \varepsilon$. In this situation, future generations would exhibit high incidence peaks at early ages, e.g., ages < 39 year [45]. The pre-35 high incidence peaks are considered consequences of individuals inheriting sensitive “p53-type” genes that had been previously populated by *ts* + *td* beyond the normal limit. Perturbations that introduced larger β values into Equation (18) would contribute to enhanced background “genetic noise”, responsible for additional *ts* + *td*. The observed ~70% increase in stomach cancer among white males, ages 25 to 39 year, over three decades, 1977 to 2006 [45], implies these genetic thresholds were populated by *ts* + *td* to their allowed limit at early ages. This could be a consequence of avoidable, but “additional”, external perturbations. For example, consumption of excessive carbonated beverages could cause increases in energy density of “local” DNA, thereby enhancing rates of populating a “genetic space”, *s*, with *ts* + *td*. Cancers that exhibit high incidence peaks for ages < 39 year can be reevaluated for their origin in terms of the particular “p53-type” gene and contributions by N_0t^2 , λt^3 and βt^4 terms in Equation (18). Application of Equation (18) appears to provide an additional “tool” for assessing origins of specific cancers. This could assist in identifying and implementing “new” cancer prevention strategies, for example, including protocols for avoiding increases in energy density of DNA. Consistent with Equations (13) to (18) and Figure 7, the model implies the development of new software for predicting probabilistic times required for a particular “genetic space”, *s*, to become populated by *ts* + *td* to its evolutionarily allowed limit, which is manifested as phenotypic expression.

Based on observations [46,47], a restricted “genetic space”, *s*, inequality, $0.976 \geq s \geq 0.970$, is inherited by the human pygmy genome. The normal human pygmy exhibits puberty at age 5, menopause at age 11 and age-related degenerative diseases at age ≥ 16 , where lifespan is ≤ 26 year [46,47]. The “genetic space” quantum model implies that sensitive “genetic switches” responsible for human puberty, menopause and age-related degenerative diseases are *all* operated by evolutionarily selected *keto-amino* $\rightarrow$ *enol-imine* arrangements populating a particular “genetic space” to its evolutionarily defined threshold. At age 5 year, *stochastic* mutations would have populated a particular “genetic space” to its threshold limit which initiates puberty; so, growth in pygmy height ceases by age 7. The “compressed” pygmy lifecycle implies that the human pygmy “genetic space”, *s*, is (a) ~80% occupied at conception, or (b) the “space” presents a larger cross section of metastable G-C + A-T sites, which would allow coherent states to populate the relevant space in a smaller time interval. DNA sequence evaluations of genes, e.g., *p53* and *K-ras*, from *Homo sapien* and human pygmy genomes could distinguish these possibilities and provide insight into conditions responsible for time-dependent genotypic origin of cancer. When the inherited “genetic space”, *s*, becomes the order of $s \approx 0.970 + 2\varepsilon$, evolutionary extinction is implied. The model appears to be applicable to *Homo sapien* and human pygmy genomes and offers an explanation for the disappearance of Neandertals after existing for ~350,000 y [48].

6. Discussion

Consistent with experimental [8,18] and theoretical [9-14] evidence, this report implies that the classical double helix of duplex DNA contains an embedded microphysical subset of hydrogen bonded protons and electron lone pairs that (a) obeys quantum probability laws and (b) governs time-dependent specificity of DNA information. An evolutionarily designed “quantum reader”, the transcriptase, deciphers information contained within coherent states occupying this microphysical subset. Data [8,14-18] and the model [9-13] provide evidence that evolutionary pressures have selected quantum probability laws over laws of classical kinetics for (i) introducing time-dependent “point” genetic alterations, (ii) transcription of coherent states occupying decoherence-free subspaces and (iii) subsequent replication-substitution or deletion of selected decohered isomers. This provides a rationale for the selection of metastable keto-amino complementary pairs as the initial state of duplex DNA. In particular, quantum uncertainty limits operate on amino DNA protons to drive the *keto-amino* $\rightarrow$ *enol-imine* arrangement at a rate consistent with DNA evolution [8,14,16-18], thereby populating accessible enol-imine coherent states of reduced energy. Product enol-imine protons are entangled and participate in coupled quantum oscillation at frequencies of $\sim 10^{13} \text{ s}^{-1}$ between two indistinguishable sets of electron lone-pairs. Before decoherence, genetic specificities of each superposition duplex DNA state are measured by the transcriptase within an interval, $\Delta t \ll 10^{-13} \text{ s}$. This quantum measurement creates an additional entanglement between coherent protons and transcriptase components, which prevents immediate reequilibration and ultimately yields an ensemble of decohered enol and imine isomers that participate in Topal-Fresco substitution-replication, *i.e.*, $G'2\ 0\ 2 \rightarrow T$, $G'0\ 0\ 2 \rightarrow C$, $*G0\ 2\ 0^0 \rightarrow A$ & $C2\ 0\ 2^2 \rightarrow T$. However, coherent states within $*A$ - $*T$ sites (Figure 3) are deleted. These time-dependent substitutions, *ts*, and deletions, *td*, contribute to the spectrum of *stochastic* mutations [15,43].

The transcriptase is a ‘quantum reader’ that can identify the relative distribution of coherent states measured at a duplex G' - C' site. Just before transcriptase measurement, the distribution of quantum G' - C' states is described by Equation (8), $|\psi\rangle = \alpha |+-+> + \beta |+-+> + \gamma |--+> + \delta |--+>$. As a result of transcriptase measurement on the G' - C' superposition, three of the four G' - C' states yield a corresponding decohered molecular genetic observable. For example, the probability of G' - C' being in state $G'2\ 0\ 2$ - $C'0\ 2\ 0$ is given by $|\langle --+ | \psi \rangle|^2 = |\delta|^2$ where $|\delta|^2$ is determined from transcriptase measurement yielding the particular molecular genetic observable, $G'2\ 0\ 2 \rightarrow T$. Agreement between observation and Figure 6 provides the relation, $|\delta|^2 = 3|\beta|^2 = 3|\gamma|^2$, which yields $\alpha = \frac{\pm i\sqrt{2}}{3}$. Consequently, the expression for the four coupled coherent protons, Equation (8), cannot be written as a tensor product, illustrated by Equation (7), which is indicative of enol-imine proton entanglement. Evidently this entanglement originated from quantum uncertainty interactions, $\Delta x \Delta p_x \geq \frac{1}{2}\hbar$, evolutionarily imposed on amino ($-\text{NH}_2$) DNA protons, which is responsible for rates of *keto-amino* $\rightarrow$ *enol-imine* arrangement. However as a consequence of the transcriptase deciphering quantum information within a G' - C' superposition, an additional entanglement is created between coherent protons and transcriptase components. This entanglement state plays a significant role in bestowing a well defined three-dimensional structure on decohered isomers— G' , C' , $*G$, $*C$ (Table 1)—which is a requirement for reproducible Topal-Fresco substitution-replication.

Since experimental lifetimes of metastable keto-amino states at 37°C are $\geq \sim 3,000$ year [9], approximate quantum methods for small times, $t < \sim 100$ year, yield the probability, $P(t)$, of *keto-amino* $\rightarrow$ *enol-imine* arrangement as $P_p(t) = \frac{1}{2} (\gamma_p / \hbar)^2 t^2$ (Appendix). This model for time-dependent alteration of genetic

specificity implies a quantum Darwinian evolution model (QDEM), which expresses *stochastic* mutations in terms of $ts + td$. Data and the QDEM imply existence of an inherited genetic space, s , inequality, $1 \geq s \geq 0.97$, for *Homo sapiens*. When $ts + td$ populate s such that $s \approx 0.97 + \varepsilon$, an age-related degenerative disease is manifested. The QDEM allows predictive consequences of reduced energy coherent states populating “genetic space”, s , in “p53-type” genes, thereby expressing “latent” genetic information. The quantum mechanical terms in Equation (18), $\sum_j \beta_j t^4$, express the consequences of $ts + td$ populating sensitive genetic spaces, s , within a “p53-type” gene, which simulate data on incidence of cancer as a function of age exhibited in Figure 7. These evolutionarily acquired quantum mechanisms for operating microphysical genetic processes imply gains in evolutionary advantages. Enhanced advantages include (A) possibilities of favorable population responses to changing environmental conditions and, concomitantly, (B) mechanisms of protecting the gene pool against acquiring unsafe levels of mutation. This analysis clearly implies that phenotypic expression of the 74 class 1 tumors (Figure 7) is *primarily a consequence* of quantum mechanical arrangements, *keto-amino* $\rightarrow$ *enol-imine*, generating genotypic $ts + td$ which are consistent with evolutionary design. Agreement between Equation (18) and Figure 7 implies age-related increased incidence of cancer is an example evolutionary mechanism of protecting the gene pool against acquiring unsafe levels of mutation.

Convergence of biological data and arguments from physics, chemistry and evolution support the model that age-related incidence of cancer [35] is a consequence of evolutionarily selected arrangements, *keto-amino* $\rightarrow$ *enol-imine*, populating a particular genetic space to its threshold limit, $s \approx 0.97 + \varepsilon$, in a “p53-type” gene. Similar arguments are applicable to phenotypic expression of Huntington’s disease resulting from $ts + td$ populating an unstable (CAG)_n tract to its evolutionary allowed limit [10,13]. These manifestations of quantum “genetic switches” imply that evolutionarily selected life-cycle alterations, e.g., the initiation of puberty and subsequent initiation of menopause [46], may be governed by “genetic switches” that are operated by time-dependent coherent states populating a particular “genetic space” to an evolutionarily determined threshold. Based on an accumulation of *stochastic* mutations, $ts + td$, within particular inherited genetic spaces, s , natural selection has employed quantum mechanisms to reveal “latent” genetic information which ultimately disallows further contributions to the gene pool. Compared to *Homo sapiens*, the life-cycle of the “normal” human pygmy is “compressed” in that puberty, menopause and onset of age-related degenerative disease are all exhibited at comparatively early ages [46,47]. This implies that $ts + td$ populate the relevant genetic space to its “threshold limit” at early ages, thereby activating age-related “genetic switches” at relatively young ages in the human pygmy life-cycle. In this case, the genetic space, s , inequality would be approximated by $0.98 \geq s \geq 0.97$ for the “normal” human pygmy genome. Accordingly, these human pygmy populations [46] are closer to their evolutionary extinction limit, i.e., $s \approx 0.97 + 2\varepsilon$, than are *Homo sapiens*.

Quantum information processing exhibited by T4 phage DNA systems and by human genomes, e.g., references 10 & 13 and Figure 7 in terms of Equation (18), imply that quantum uncertainty limits on amino DNA protons have been operational since the primordial pool of primitive duplex DNA components [49]. This quantum law has been selected to drive a probabilistic yield of *keto-amino* $\rightarrow$ *enol-imine* arrangements, thereby introducing reduced energy enol-imine coherent states. However, particular decohered isomers are selected for substitution-replication or deletion. These are substitutions—G’2 0 2 $\rightarrow$ T, *C2 0 2² $\rightarrow$ T, G’0 0 2 $\rightarrow$ C, *G0 2 0⁰ $\rightarrow$ A – and *A-*T $\rightarrow$ deletion. The fact that mutation frequencies, G’2 0 2 $\rightarrow$ T & *C2 0 2² $\rightarrow$ T, phenotypically expressed via quantum transcription—before replication—are identical to

subsequent substitution frequencies, $G'2\ 0\ 2 \rightarrow T$ & $*C2\ 0\ 2^2 \rightarrow T$, expressed as a consequence of Topal-Fresco replication of decohered isomers indicates that consequences of coherent states are “hard wired” into the DNA code. In these cases of the transcriptase reading quantum states $G'2\ 0\ 2$ and $*C2\ 0\ 2^2$ as normal $T2^2\ 0\ 2^2$, the transcriptase receives quantum instructions which are precisely communicated and executed for forming the particular complementary mispairs, $G'2\ 0\ 2$ -syn- $A0^0\ 2\ \#$ and $*C2\ 0\ 2^2$ - $A0^0\ 2\ \#$ (Table 1; Figure 5). These decohered mispairs are subsequently “replicated” to complete the prescribed substitutions, $G'2\ 0\ 2 \rightarrow T$ and $*C2\ 0\ 2^2 \rightarrow T$, at the particular G' and $*C$ genetic sites. This apparently involves “seamless” collaboration between transcriptase and replicase systems. In the absence of entanglement, one cannot explain how ~100% of the coherent state population identified by quantum transcription, e.g., $G'2\ 0\ 2$, is subsequently decohered to form the complementary mispair, $G'2\ 0\ 2$ -syn- $A0^0\ 2\ \#$ (Figure 5b), all of which participate in the $G'2\ 0\ 2 \rightarrow T$ substitution at replication [8,18]. This observation implies evolutionarily implemented quantum entanglement prevents immediate reequilibration and preserves the 3-deminsional molecular structure of particular decohered enol and imine isomers for purposes of efficient substitution-replication. Note that coherent state $G'0\ 0\ 2$ is not a transcription analog of any base; so, expression of the substitution $G'0\ 0\ 2 \rightarrow C$ at this G' - C' site is a consequence of the complementary mispair, $G'0\ 0\ 2$ -syn- $G2^2\ 2\ \#$, completing its replication-substitution prescribed by transcriptase quantum processing. Interestingly, qualitative agreement between biologically expressed decohered data and Figure 6 suggests a field-theoretic mechanism for transcriptase quantum processing, subsequent entanglement and the observation that $G'2\ 0\ 2 \rightarrow T$ substitutions are ~3-fold (rather than 2-fold) $> G'0\ 0\ 2 \rightarrow C$ substitutions at the particular G' - C' genetic site. The QDEM also predicts an inaccurate molecular clock [13]. Inexactness exhibited by observable molecular clocks [14,16] is attributed to *ts* introducing additional initiation codons—UUG, CUG, AUG, GUG—which can manifest dynamic mutation expansion [13,34]. Additionally, DNA microsatellite contractions can be consequences of (a) *ts* introducing stop codons—UAA, UAG, UGA—or (b) *td* at $*A$ - $*T$ sites. The QDEM thus implies that improved models for calculating genetic distance between species could result from an inclusion of information responsible for this “clock inexactness”, i.e., include *all* consequences of *ts* + *td*.

Hwang and Green [14] have clearly shown that mammalian DNA exhibits time-dependent, molecular clock events, CpG $\rightarrow$ TpG substitutions, at the DNA level. The terminology, “CpG substitutions”, indicates C $\rightarrow$ T and/or G $\rightarrow$ A substitutions at a CpG site. Time-dependent CpG substitutions are the most frequent point mutation observed in the human genome and the rate is ~15-fold greater when cytosine is methylated [16]. A consequence of a methyl group occupying carbon-5 cytosine is an increased proton-proton interaction, i.e., $-NH_2 - - H_3C-$, which would increase the probability of confining cytosine amino protons to too small of space, Δx . This would enhance rates of *keto-amino* $\rightarrow$ *enol-imine* arrangement via the asymmetric channel (Figure 1b), as observed. Although the assumed mechanism for CpG $\rightarrow$ TpG mutation is hydrolytic deamination of cytosine [14,16,48], the extensive molecular genetic investigation by Ripley [17] could not identify evidence supporting deamination of cytosine as the mechanism responsible for time-dependent CpG $\rightarrow$ TpG. Also after a CpG $\rightarrow$ TpG event, deaminated cytosine could not reacquire an $-NH_2$ group and return to its original state, $C0^0\ 2\ 2^2$, in the next round of growth. However this “reequilibration recovery” of cytosine is routinely exhibited by T4 phage DNA systems that have expressed CpG $\rightarrow$ TpG [8]. Elango *et al.* [16] have noted that this deamination explanation for time-dependent CpG $\rightarrow$ TpG requires invoking a vague mechanism for inserting H_2O between DNA strands. Since a hydrolytic deamination of cytosine mechanism would not include the βt term in Equation (13), this

mechanism is inconsistent with a model that satisfies incidence of cancer data in terms of *stochastic* mutations, $ts + td$ [15]. Based on evidence discussed here and the QDEM, the present report implies that most time-dependent CpG $\rightarrow$ TpG substitutions are a consequence of the asymmetric channel illustrated in Figure 1b. Also the fact that specific experimental designs are required to observe nontrivial quantum effects in biological systems [7,8] has played a role in obscuring mechanism of mutation illustrated by Equation (18).

Although cancer has been modeled in terms of classical Darwinian *stochastic* mutations [50], agreement between Figure 7 data and Equation (18) implies that coherent state contributions to the genotypic origin of tumors, $\sum_j \beta_j t^4$, have been significantly underestimated [9,10,13] and, concomitantly, the role of classical *stochastic* mutations has apparently been over estimated. Unlike the QDEM, classical models [50] do not: (a) simulate Figure 7 data in terms of intrinsic physical properties of cells [9,10]; (b) explain molecular origins of *stochastic* mutations, $ts + td$; (c) provide internally consistent explanations for “early” cancer incidence peaks, e.g., ages < 39 [35,45]; (d) identify the evolutionary advantage of protecting the gene pool against acquiring unsafe levels of haploid *stochastic* mutation. The latter is a consequence of diploid “p53-type” genes manifesting age-related degenerative disease [15,42] due to an inherited “genetic space”, s , becoming populated by *stochastic* mutations to its threshold limit, $s \approx 0.97 + \epsilon$. The QDEM further provides testable explanations for different lifecycle manifestations exhibited by *Homo sapien* and human pygmy genomes, e.g., ages at puberty [46], menopause, *etc.* The model also predicts a modest time-dependent evolutionary shift favoring A-T richness, which may play a role in evolutionary extinction. In addition to observable transcriptase quantum processing [8,9], recent studies [51] have shown that light-harvesting by certain marine algae photosynthetic proteins involves long-lived quantum superposition states that transfer energy, thereby exhibiting nontrivial quantum phenomena by a biological system.

When viewed through the lens of quantum theory, consequences of transcriptase quantum processing not only provide insight into quantum processing and entanglements, but also identify evolutionary origins of age-related degenerative disease. This article reviews the origin of coherent states exhibited by enol-imine proton bonds in duplex DNA and outlines their role in communicating quantum information genetic specificity, which is ultimately exhibited as contributions to a quantum molecular clock. Data on enzymatic quantum measurements of genetic specificities within intervals, $\Delta t \ll 10^{-13}$ s, imply quantum entanglement between coherent protons and enzyme components. Transcriptase quantum processing, subsequent entanglement states and enzyme catalyzed decoherence reactions require additional theoretical refinements [52,53] to describe enzyme functions. Also, evidence of coherent states occupying decoherence-free subspaces at biological temperatures implies an opportunity for implementing carefully designed interdisciplinary experiments [7]. These recent studies [8-13,51] also identify areas in biology where quantum coherence is required for proper biological insight into microscopic molecular mechanisms and explanations of macroscopic biological consequences, Figure 7.

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Appendix

Probability of Hydrogen Bond Arrangement, keto-amino $\rightarrow$ enol-imine, Using Approximate Quantum Methods

For purposes of discussing consequences of coherent states populating duplex G'-C' and *G-*C sites, an expression is obtained for the quantum mechanical "rate constant" associated with hydrogen bond arrangement, *keto-amino* $\rightarrow$ *enol-imine* via symmetric and asymmetric channels (Figure 2). This allows the development of a polynomial expression for time-dependent alterations (classical + quantum) in genetic specificities at a DNA base pair, which can be generalized to express an altered gene function. Time-dependence for the reactive five proton system of metastable G-C to populate complementary enol-imine states is modeled in terms of a composite proton, of mass equal two protons, in an appropriate asymmetric three-well potential illustrated in Figure A-1. Here the motion of two tunneling-exchange protons, using the symmetric and asymmetric channels (Figure 2), is simulated in terms of a composite proton model. Secondary contributions by the 2nd asymmetric pathway (unlabeled) are neglected. At $t = 0$ the composite proton is replicated into the metastable state $|3\rangle$ at energy E_3 which, according to data [8,18] and shown in Figure A-1, is separated from the enol-imine ground state, $|1\rangle$, and hybrid state, $|2\rangle$, by approximately equal energy barriers. The relationship $E_1 < E_2 < E_3$ for the ground state, hybrid state and metastable state, respectively, is displayed in Figure A-1. Enol-imine product states are designated by a general arrangement state $|\rho\rangle$ where the energy E_ρ would equal E_1 or E_2 as appropriate. Time-dependence of an eigenstate, $|\Psi\rangle$, is expressed by $|\Psi\rangle = |\phi_1\rangle \exp(-i E_1 t / \hbar)$, so $|\Psi\rangle = |\phi_1\rangle$ at $t = 0$ [38]. The relationship $|\Psi\rangle = \sum_i |i\rangle \langle i|\Psi\rangle$ is used to express an eigenstate $|\Psi\rangle$ in terms of base states $|i\rangle$ and amplitudes C_i as

$$|\Psi\rangle = |1\rangle \langle 1|\Psi\rangle + |2\rangle \langle 2|\Psi\rangle = |1\rangle C_1 + |2\rangle C_2 \quad (1-A)$$

where base states satisfy $\langle i | j \rangle = \delta_{ij}$. The eigenstate is normalized, $\langle \Psi | \Psi \rangle = 1$, and an eigenstate and eigenvalue E are related to the Hamiltonian matrix, $\sum_j \langle i | H | j \rangle \langle j | \Psi \rangle = E \langle i | \Psi \rangle$, which can be rewritten as

$$\sum_j (H_{ij} - E \delta_{ij}) C_j = 0 \quad (2-A)$$

for an expression to solve for amplitudes, $\{C_j | i=1,2; j=1,2\}$. A nonzero solution to Equation (2-A) is available if the determinant of $\sum_j (H_{ij} - E \delta_{ij}) = 0$.

A two-level Hamiltonian that will allow a composite proton to tunnel from the metastable state $|3\rangle$ at energy E_3 to an arrangement state $|\rho\rangle$ at energy E_ρ can be written as

$$H = \begin{pmatrix} E & -\alpha_\rho \\ \alpha_\rho & E_\rho \end{pmatrix} \begin{pmatrix} H_{11} & H_{12} \\ H_{21} & H_{22} \end{pmatrix} \quad (3-A)$$

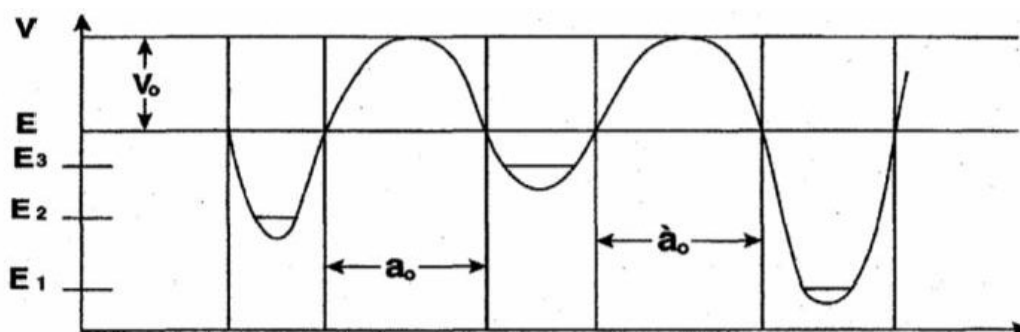
where α_ρ is the quantum mechanical coupling between states $|3\rangle$ and $|\rho\rangle$. The resulting upper and lower eigenvalues, $E_{A\rho}$ and $E_{B\rho}$, are found as

$$E_{Ap} = \xi_p + \gamma_p \quad (4-A)$$

and

$$E_{Bp} = \xi_p - \gamma_p \quad (5-A)$$

Figure A-1. Qualitative energy surface for a composite DNA proton system occupying the metastable, hybrid and ground states.



(Asymmetric three-well potential to simulate metastable keto-amino protons populating accessible enol-imine states in terms of a “composite” proton originating in the metastable E_3 energy well at $t = 0$ where $E_1 < E_2 < E_3$).

where $\xi_p = (E_3 + E_p)/2$, $\gamma_p = [(E_3 - E_p)^2/4 + \alpha_p^2]^{1/2}$ and $p = 1, 2$ for the symmetric and asymmetric channels, respectively. The time-dependent wave function $|\Psi(t)\rangle$ of the composite proton in the asymmetric three well potential can be expressed in terms of the corresponding eigenstates as

$$|\Psi(t)\rangle = |\Psi_{A1}\rangle \exp(-i E_{A1} t/\hbar) + |\Psi_{A2}\rangle \exp(-i E_{A2} t/\hbar) + |\Psi_{B1}\rangle \exp(-i E_{B1} t/\hbar) + |\Psi_{B2}\rangle \exp(-i E_{B2} t/\hbar) \quad (6-A)$$

which can be expressed in terms of physical base states $|3\rangle$, $|2\rangle$, $|1\rangle$ as [10]

$$|\Psi(t)\rangle = \exp(-i \xi_1 t/\hbar) \{ |3\rangle \exp(-i \gamma_1 t/\hbar) + |1'\rangle \exp[-i (\gamma_1 t/\hbar + \delta)] \} + \exp(-i \xi_1 t/\hbar) \{ |3\rangle \exp(+i \gamma_1 t/\hbar) + |1'\rangle \exp[+i (\gamma_1 t/\hbar + \delta)] \} + \exp(-i \xi_2 t/\hbar) \{ |3\rangle \exp(-i \gamma_2 t/\hbar) + |2'\rangle \exp[-i (\gamma_2 t/\hbar + \delta)] \} + \exp(-i \xi_2 t/\hbar) \{ |3\rangle \exp(+i \gamma_2 t/\hbar) + |2'\rangle \exp[+i (\gamma_2 t/\hbar + \delta)] \} \quad (7-A)$$

This can be written more succinctly as

$$|\Psi(t)\rangle = (0.5)^{1/2} \exp(-i \xi_1 t/\hbar) \{ |3\rangle \cos(\gamma_1 t/\hbar) + |1'\rangle \sin(\gamma_1 t/\hbar) \} + (0.5)^{1/2} \exp(-i \xi_2 t/\hbar) \{ |3\rangle \cos(\gamma_2 t/\hbar) + |2'\rangle \sin(\gamma_2 t/\hbar) \} \quad (8-A)$$

where $|1\rangle = |1'\rangle e^{i\delta}$, $|2\rangle = |2'\rangle e^{i\delta}$ and δ of the arbitrary phase factor $e^{i\delta}$ is $-\pi/2$ and the relation $\cos(\theta - \pi/2) = \sin(\theta)$ is used. Data show that k_{ts} rates are approximately equal for transversions and transitions [32,33]; so, quantum mechanical “rate constants” for hydrogen bond arrangements, *keto-amino* $\rightarrow$ *enol-imine* via symmetric and asymmetric channels, are approximately equal (Figure 1-A). Since the

lifetimes, τ , for 37°C keto-amino G-C protons are the order of $\sim 3,200$ years [9], the wave function expression in Equation (8-A) would be applicable in the interval, $0 < t < \sim 3,200$ years.

At $t = 0$, the composite proton was in the metastable state $|3\rangle$ at energy E_3 . The probability, $P_1(t)$, that the proton is in the ground state $|1\rangle$ at a later time t is given by

$$P_1(t) = |\langle 1' | \Psi(t) \rangle|^2 = 0.5 \sin^2(\gamma_1 t / \hbar) \quad (9-A)$$

which identifies $P_1(t)$ in terms of contributions by the symmetric channel. The probability of the proton being in the hybrid state $|2\rangle$ at a later time is given as

$$P_2(t) = |\langle 2' | \Psi(t) \rangle|^2 = 0.5 \sin^2(\gamma_2 t / \hbar) \quad (10-A)$$

which is the contribution by the asymmetric channel. The probability that the proton is in metastable state $|3\rangle$ at time t is given by

$$P_3(t) = |\langle 3 | \Psi(t) \rangle|^2 = 0.5[\cos^2(\gamma_1 t / \hbar) + \cos^2(\gamma_2 t / \hbar)] \quad (11-A)$$

which is the sum of contributions for protons exiting state $|3\rangle$ by the symmetric and asymmetric channels. The sum of Equations (9-A to 11-A), given by

$$\sum_{i=1}^3 P_i(t) = (0.5) [\sin^2(r_1 t / \hbar) + \cos^2(r_1 t / \hbar)] + (0.5) [\sin^2(r_2 t / \hbar) + \cos^2(r_2 t / \hbar)] = 1 \quad (12-A)$$

is consistent with the requirement that the composite proton be confined to its set of base states, $|3\rangle$, $|2\rangle$, $|1\rangle$. The time derivative of $P_p(t)$, Equations (9-A & 10-A), can be expressed as

$$dP_p/dt = (\gamma_p/\hbar) \sin(\gamma_p t / \hbar) \cos(\gamma_p t / \hbar) \quad (13-A)$$

where $P_p(t)$ represents either $P_1(t)$ or $P_2(t)$ and the 0.5 normalization factor is omitted. A Taylor series expansion of Equation (13-A) is given by

$$dP_p/dt \approx (\gamma_p/\hbar)^2 t - 4/3 (\gamma_p/\hbar)^4 t^3 + 4/15 (\gamma_p/\hbar)^6 t^5 + \dots \quad (14-A)$$

where the first three terms are given. The experimental lifetime of metastable keto-amino hydrogen bonded G-C protons is the order of $\sim 3,200$ years, which is large compared to human lifetimes of, say, ~ 100 years. For times $t \ll 3,200$ years (e.g., $t < 100$ years), one could employ a small t approximation to express the probability of metastable protons populating enol-imine states $|1\rangle$ or $|2\rangle$ as

$$P_p(t) = \frac{1}{2} (\gamma_p/\hbar)^2 t^2, \quad (15-A)$$

indicating a *nonlinear* time dependence. This is consistent with exponential increases observed in base substitutions and deletions as a function of age in nonmitotic human mitochondria DNA [43]. Equation (15-A) is instrumental in developing the polynomial model in Section 5 for phenotypic expression of a “p53-type” gene, resulting from intrinsically altered genetic specificities.

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