Review

# A Review of Interferometric Synthetic Aperture RADAR (InSAR) Multi-Track Approaches for the Retrieval of Earth's Surface Displacements 

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#### Abstract

Featured Application: This review paper primarily aims to investigate the capabilities of the recently proposed multiple-satellite/multiple-angle Interferometric Synthetic Aperture RADAR (InSAR) combination techniques, which allow discriminating and monitoring the time evolution of three-dimensional (3-D) components of Earth's surface deformations. Such methods are nowadays being widely applied, mostly in areas characterized by the presence of significant deformation signals (for instance, due to massive volcanic or seismic episodes) and to less extent in regions with low-to-moderate deformation signals. This work intends to provide insights on theoretical aspects of multi-pass InSAR techniques and their applicability for the monitoring of a heterogeneous class of deformation phenomena.


#### Abstract

Synthetic Aperture RADAR Interferometry (InSAR) provides a unique tool for the quantitative measurement of the Earth's surface deformations induced by a variety of natural (such as volcanic eruptions, landslides and earthquakes) and anthropogenic (e.g., ground-water extraction in highly-urbanized areas, deterioration of buildings and public facilities) processes. In this framework, use of InSAR technology makes it possible the long-term monitoring of surface deformations and the analysis of relevant geodynamic phenomena. This review paper provides readers with a general overview of the InSAR principles and the recent development of the advanced multi-track InSAR combination methodologies, which allow to discriminate the 3-D components of deformation processes and to follow their temporal evolution. The increasing availability of SAR data collected by complementary illumination angles and from different RADAR instruments, which operate in various bands of the microwave spectrum ( X -, L - and C-band), makes the use of multi-track/multi-satellite InSAR techniques very promising for the characterization of deformation patterns. A few case studies will be presented, with a particular focus on the recently proposed multi-track InSAR method known as the Minimum Acceleration (MinA) combination approach. The presented results evidence the validity and the relevance of the investigated InSAR approaches for geospatial analyses.


Keywords: Synthetic Aperture RADAR Interferometry techniques; deformation; geodesy; multi-track; and satellite constellations

## 1. Introduction

Synthetic Aperture RADAR (SAR) is a coherent active microwave remote sensing instrument [1-3], whose capability to efficiently map the scattering properties of the Earth's surface is well documented [4-6]. A SAR sensor-which can be mounted on board an aircraft or satellite-has a side-looking illumination direction and can accurately retrieve the location of an object (target) relative
to the position of the platform where the sensor is mounted. Both the acquisition geometry and the physical characteristics of the imaged scene contribute to the formation of the received backscattered RADAR signal (echo) which, correctly processed, leads to the reconstruction of a complex-valued high-resolution microwave image of the observed area [2]. SAR is an active imaging sensor, i.e., it does not need an external energy source to work. Moreover, since it typically operates in the microwave region of the electromagnetic spectrum, it can be used efficiently in any meteorological condition (i.e., in the presence of a significant clouds' cover) and with a full day-and-night operational capability. As a consequence of its flexibility, SAR technology mostly improved over the last decades, thus developing further technologies based on the use of SAR data for the detection and monitoring of several geophysical phenomena [7-16]. Among these techniques, the SAR interferometry [13-16] plays a major role in the study of the dynamic of Earth's crust, thus permitting the monitoring of the surface movements. Deformations can be induced by several geophysical phenomena, such as the extensive fractures due to big earthquakes [17-19], pre-seismic deformations [20], slow-moving landslides [21-24], the eruptions of active volcanoes [25-28]. Human beings also severely contribute to the changes in the environment. In this framework, InSAR can monitor the modifications over time of highly urbanized zones by measuring the settlements of buildings, private and public facilities [29-31]. The results of these investigations are useful for city planners and local authorities to mitigate the urban risk and design effective plans of cities development.

This review paper will first address the fundamentals of InSAR technology and, then, will provide an overview of recently proposed multi-track/multi-satellite InSAR-based methodologies [32], which allow the detection and the continuous monitoring of the three-dimensional shape of deformation phenomena.

The paper is organized as follows. Section 2 illustrates the InSAR rationale, emphasizing key strengths and potential limitations. Section 3 provides an overview of the multi-pass InSAR techniques and Section 4 describes, with more details, the recently proposed minimum acceleration InSAR combination method [32]. The results of a few experiments will also be presented. Future perspectives on the use of InSAR and multi-satellite InSAR methodologies will be finally provided in Section 5.

## 2. Overview of InSAR Methodology

One of the principal applications of the SAR technology is represented by the SAR interferometry (InSAR) technique [13-16]. It relies on the measurement of the phase difference between two (or more) complex-valued SAR images, acquired from different orbital positions and/or at different times. In principle, different distributions of the receiving/transmitting antennas define distinctive interferometric configurations. In particular, conventional mono-static InSAR configurations involve the use of two antennas observing the investigated scene:
$>$ at the same time and from different positions, spaced in the across-track direction (across-track interferometry);
$>$ at different times and from the same position (along-track interferometry) [33,34];
$>\quad$ at different times and from different orbital positions (repeat-pass across-track interferometry).
Bi-static and multi-static InSAR interferometry configurations, where receiving and transmitting antennas are on board different moving platforms, have also been explored [35-37]. Such field of research, within InSAR framework, represents one of the most promising lines of development of InSAR technology.

### 2.1. InSAR Technique for the Estimation of Height Topography

In this review, we concentrate on the repeat-pass across interferometry. As earlier anticipated, such technology allows the measurement of geomorphological characteristics of the ground, such as the topography height and the modifications of the Earth's surface, due to earthquakes, volcano eruptions or other geophysical phenomena. Historically, InSAR has been mostly used for the measurement of
the ground topography [38-40]. To understand how InSAR works, let us refer to the imaging geometry depicted in Figure 1 and suppose the involved RADAR system acquires two SAR images over the same area. The first SAR image (i.e., commonly referred to as master image) is taken from the orbital position labelled to as $M$. The second image (i.e., the so-called slave image) is captured from the orbital position marked as $S$, located at a distance $b$ (referred to as baseline) from $M$. Notice that in the plane orthogonal to azimuth direction the two SAR antennas are separated by the baseline vector $\mathbf{b}$, which can be decomposed into either its parallel/perpendicular ( $b_{/ /,} b_{\perp}$ ) or horizontal/vertical ( $b_{h}, b_{v}$ ) components, respectively. Taking into account geometric considerations and by direct inspection of Figures 1 and 2, it is easy to demonstrate the validity of the following mathematical relationships:

$$
\left\{\begin{array}{c}
b_{\perp}=b \cos (\vartheta-\alpha)=b_{h} \cos \vartheta+b_{v} \sin \vartheta  \tag{1}\\
b_{/ /}=-b \sin (\vartheta-\alpha)=b_{h} \sin \vartheta-b_{v} \cos \vartheta \\
b_{h}=b \cos \alpha=b_{\perp} \cos \vartheta+b_{/ /} \sin \vartheta \\
b_{v}=b \sin \alpha=b_{\perp} \sin \vartheta-b_{/ /} \cos \vartheta
\end{array}\right.
$$

where $\vartheta$ and $\alpha$ are the satellite side-looking angle and the inclination angle of the baseline vector with respect to the horizontal plane, respectively. Equations (1) are fundamental to calculate the sensitivity of InSAR measurements to deformation measurements, as subsequently outlined in this Section. If we assume that the RADAR system has an infinite bandwidth, the master and slave complex-valued SAR images can be mathematically represented, pixel-by-pixel, as follows:

$$
\begin{gather*}
\hat{\gamma}_{1}=\gamma_{1} \exp \left[-j \frac{4 \pi}{\lambda} r\right]  \tag{2}\\
\hat{\gamma}_{2}=\gamma_{2} \exp \left[-j \frac{4 \pi}{\lambda}(r+\delta r)\right] \tag{3}
\end{gather*}
$$

where $\gamma_{1}$ and $\gamma_{2}$ are the complex reflectivity functions of the master and slave data, respectively and $\lambda$ denotes the effective RADAR wavelength. The interferometric phase map (called an interferogram) is formed, on a pixel-by-pixel basis, starting from the two co-registered (complex-valued) master and slave SAR images. Notice that the misalignment of the second image is precisely due to the path difference between the two RADAR signals.


Figure 1. SAR interferometric configuration.


Figure 2. Interferometric baseline geometry. The baseline vector can efficiently be decomposed in the perpendicular/parallel components (a) and the horizontal/vertical components (b), respectively.

Precisely for this reason, it is needed to properly co-register the images to represent the two SAR images in the same reference geometry [41,42]. In Equations (2) and (3), for the sake of simplicity, we have not considered the presence of any possible noise signals that corrupt the SAR signals. A comprehensive overview of the sources of noise associated with SAR images falls beyond the scopes of this review paper. Nonetheless, the Section 2.2 addresses the problem of noise corrupting interferometric SAR signal. Let us first discuss the rationale of the interferometry SAR technique. Taking into account Equations (2) and (3), we obtain, for each RADAR pixel, the phase difference between the two SAR images by merely multiplying the first image (master) by the complex conjugate of the second image (slave) and, then, by extracting its phase term:

$$
\begin{equation*}
C=\hat{\gamma}_{1} \hat{\gamma}_{2}^{*}=\left|\hat{\gamma}_{1} \hat{\gamma}_{2}\right| \exp \left[j\left(\frac{4 \pi}{\lambda} \delta r+\measuredangle \gamma_{1}-\measuredangle \gamma_{2}\right)\right] \tag{4}
\end{equation*}
$$

where the symbol $\left(^{*}\right)$ denotes the complex conjugate operation and the symbol $\measuredangle$ represents the phase extraction operation. From Equation (4), assuming that the electromagnetic-wave scattering mechanism on the ground has not changed between the two passages of the sensor over the illuminated area (this requirement could be directly accomplished if a single-pass configuration was considered), we get:

$$
\begin{equation*}
C=\hat{\gamma}_{1} \hat{\gamma}_{2}^{*}=|\hat{\gamma}|^{2} \exp \left[j \frac{4 \pi}{\lambda} \delta r\right] \tag{5}
\end{equation*}
$$

and its full phase term (i.e., not restricted to the $[-\pi, \pi]$ interval) represents the so-called interferometric phase:

$$
\begin{equation*}
\varphi=\frac{4 \pi}{\lambda} \delta r \tag{6}
\end{equation*}
$$

Taking into account the acquisition geometry illustrated in Figures 1 and 2 and in the application of the cosine's rule to the MST triangle depicted in Figure 1 [41], it is straightforward to demonstrate that:

$$
\begin{equation*}
r+\delta r=\sqrt{b^{2}+r^{2}-2 b r \sin (\vartheta-\alpha)} \simeq r^{\prime}-b \sin (\vartheta-\alpha) \tag{7}
\end{equation*}
$$

Accordingly, the interferometric phase, see (6), can be written as:

$$
\begin{equation*}
\varphi \simeq-\frac{4 \pi}{\lambda} b \sin (\vartheta-\alpha)=\frac{4 \pi}{\lambda} b_{/ /} \tag{8}
\end{equation*}
$$

where $b_{/ /}$is the parallel baseline component, see Equation (1).
At this stage, the problem to be addressed is the recognition of the interferometric phase dependency upon the surface topography and the subsequent estimation of the error budget of the InSAR-based topographic measurements. To this aim, let us refer again to the geometry of the problem sketched in Figure 1 and we expand Equation (8) around the angular position $\vartheta=\vartheta_{0}$, which represents the side-looking angle that corresponds to the case when Earth's surface is flat (i.e., $z=0$ ). Therefore:

$$
\begin{equation*}
\varphi \simeq-\frac{4 \pi}{\lambda} b\left[\sin \left(\vartheta_{0}-\alpha\right)+\cos \left(\vartheta_{0}-\alpha\right)\left(\vartheta-\vartheta_{0}\right)\right] \tag{9}
\end{equation*}
$$

The target height, namely $z$, is related to the side-looking angle $\vartheta$ and to the satellite height $H$ as $z=H-r \cos \vartheta$.

Hence:

$$
\begin{equation*}
\frac{\partial z}{\partial \vartheta}=r \sin \vartheta \rightarrow \frac{\partial \vartheta}{\partial z}=\frac{1}{r \sin \vartheta} \rightarrow \vartheta-\vartheta_{0}=\frac{z}{r \sin \vartheta} \tag{10}
\end{equation*}
$$

Finally, the interferometric phase can be seen as composed of two distinctive terms, as follows:

$$
\begin{equation*}
\varphi \simeq-\frac{4 \pi}{\lambda} b \sin \left(\vartheta_{0}-\alpha\right)-\frac{4 \pi}{\lambda} \frac{b_{\perp}}{r \sin \vartheta} z \tag{11}
\end{equation*}
$$

where the mathematical relation $b_{\perp}=b \cos (\vartheta-\alpha)$ (see (1)) has been used.
The first term on the right-end side of Equation (11) represents the so-called flat-Earth phase contribution, i.e., the phase that is obtained when the topographic profile is entirely flat $(z=0)$. The second term relates the interferometric phase to the surface height $z$. By Equation (11), it is simple to understand that the interferometric phase is proportional to the height through the value of the perpendicular baseline of the interferometric data pair. Accordingly, the larger the perpendicular baseline, the more accurate the estimate of the topography, as clarified by the following Equation (12) that relates the standard deviation of the phase measurement (i.e., the error of the InSAR phase measurement)—namely $\sigma_{\varphi}$-to the standard deviation of the InSAR-driven height measurements, namely $\sigma_{z}$ :

$$
\begin{equation*}
\sigma_{z}=-\frac{\lambda}{4 \pi} \frac{r \sin \vartheta}{b_{\perp}} \sigma_{\varphi} \tag{12}
\end{equation*}
$$

By using the parameters of the C-band ASAR RADAR instrument mounted on board the ENVISAT satellite of the European Space Agency (ESA), we have evaluated the accuracy of the height measurement in a real context. Note that the ENVISAT/ASAR instrument operated from 2002 to 2010 with a wavelength of 5.6 cm , the scenes were imaged with an average side-looking angle of about $23^{\circ}$ and the sensor-to-target distance, namely $r$, was approximately 800 km . Figures 3 and 4 depict the plot of the standard deviation of the height measurement (as calculated by Equation (12)) vs. the perpendicular baseline and the standard deviation of the interferometric phase, respectively. The accuracy of InSAR phase, however, depends on the perpendicular baseline of the interferogram. Unfortunately, an increase in the perpendicular baseline, which would be beneficial for reducing the standard deviation of the height measurement by Equation (12), is responsible for increasingly severe decorrelation noise artefacts [41,43-45] (see Section 2.2 for details) in the generated map of the interferometric phase. Accordingly, the use of very large baseline interferograms limits the efficacy of InSAR-based height measurement. For this reason, in practice, a compromise arises for establishing a criterion for the selection of the optimal baseline separation between orbits for InSAR applications. Height accuracy can also be calculated with respect to the components of the baseline vector. To do
that, we observe that, by using Equations (7) and (11) (neglecting the flat-Earth term contribution), the topography can be expressed as a function of the parallel baseline component as:

$$
\begin{equation*}
z=\frac{r \sin \vartheta}{b_{\perp}} b_{/ /} \tag{13}
\end{equation*}
$$

and, making use of Equations (1), we get:

$$
\begin{equation*}
z=\frac{r \sin ^{2} \vartheta}{b_{\perp}} b_{h}-\frac{r \sin (2 \vartheta)}{2 b_{\perp}} b_{\vartheta} \tag{14}
\end{equation*}
$$

Therefore, the standard deviation of the topography can also be expressed as follows:

$$
\begin{gather*}
\sigma_{z}=\frac{r \sin ^{2} \vartheta}{b_{\perp}} \sigma_{b_{h}}  \tag{15}\\
\sigma_{z}=\frac{r \sin (2 \vartheta)}{2 b_{\perp}} \sigma_{b_{v}}
\end{gather*}
$$

Finally, another frequently-used measure of the interferometric performance for the estimation of height topography is the so-called height ambiguity, which represents the amount of height change leading to a $2 \pi$-change of the interferometric phase, which can be easily derived from Equation (12) by imposing $\sigma_{\varphi}=2 \pi$, as:

$$
\begin{equation*}
z_{2 \pi}=\left|-\frac{\lambda r \sin \vartheta}{2 b_{\perp}}\right| \tag{16}
\end{equation*}
$$



Figure 3. (a) Standard Deviation of the height measurement vs. the perpendicular baseline of the used interferometric data pairs for different values of the phase noise standard deviation $(\pi / 16, \pi / 8, \pi / 4$, $\pi / 2$ and $\pi$ ). (b) Standard Deviation of the height measurement vs. the phase noise standard deviation for different values of the InSAR perpendicular baseline (i.e., $125 \mathrm{~m}, 250 \mathrm{~m}, 500 \mathrm{~m}, 750 \mathrm{~m}$ and 1000 m ). Plots refer to technical parameters of ENVISAT/ASAR radar sensor.

### 2.2. Noise Signals Corrupting SAR Interferograms

This subsection shortly addresses the issue of characterizing the noise that corrupts the interferometric SAR signal. The focus is mostly on the noise signals that characterize the interferometric
phase. Accordingly, we neglect the effect of additional noise signals corrupting the complex-valued SAR signals that are ascribable to inaccurate pre-processing of SAR data. To this class belong the errors due to an incorrect focusing of SAR raw data [41,46-48], the presence of uncompensated radio frequency interference (RFI) signatures in the focused SAR imagery [49-51], or other possible causes of disturbances in the complex SAR signal. These effects globally increase the level of noise in the generated interferograms but their full characterization is outside the aim of this review paper. Here, we only spend a few words about the effect of uncompensated RFI signals in the two interfering master and slave SAR acquisitions. RFI artefacts are due to electromagnetic interference signals emitted by civil and military communication systems at the operational radar frequency in many areas of the world $[49,50]$. These artefacts are known to be more prominent at low frequency (L-band). For instance, SAR raw data collected by the Japanese L-band PALSAR systems are affected by such mistakes, which are mostly compensated during pre-processing and focusing of SAR data at ground stations before the delivering to users. At higher frequencies, RFI events have occurred but they are somewhat limited. ESA has reported some limited RFI events at C-band (although there is evidence they are increasing), whereas at X-band they have not been reported so frequently to represent a real problem [50]. Uncompensated RFI artefacts appear as various kinds of bright linear features in the azimuth-time range frequency domain [51]. Incoherent RFI is filtered out (at most) by the matched-filter used for focusing the SAR images. However, high-power RFI signals might be filtered during focusing step and they require proper RFI filters to be implemented [52-54]. Uncompensated RFI can increase the noise level in the phase signature of SAR images at L-band [55]. As said, however, the characterization of the RFI effects falls outside the limits of our investigation. Interested readers can find details on the RFI sources and the developed algorithms for their mitigation in SAR images, in [51] and the references listed therein.

This subsection aims to get an estimate of the error-budget associated to the InSAR measurement of the terrain height topography. As said, the standard deviation of the height is linked to the standard deviation of the $\operatorname{InSAR}$ phase $\sigma_{\varphi}$ by Equation (12). Our analysis moves from the basic observation that, in the interferometric processing, the conjugate multiplication of the two co-registered master and slave SAR images yields the complex interferogram:

$$
\begin{equation*}
I=\hat{\gamma}_{1} \cdot \hat{\gamma}_{2}^{*}=\left|\hat{\gamma}_{1} \cdot \hat{\gamma}_{2}^{*}\right| \exp [j \varphi] \tag{17}
\end{equation*}
$$

where $\varphi$ is the interferometric phase. To further reduce the phase noise corrupting the interferometric phase, a multi-look operation [56] is usually carried out on the generated SAR interferograms, at the expenses of a worse spatial resolution of InSAR products. The multi-looking operation consists in the calculation, pixel-by-pixel, of the statistical expectation value of the complex interferogram, namely $E[I]$. Mathematically, under the hypothesis that SAR processes are stationary, jointly stationary and ergodic (in mean), the ensemble value can be substituted with spatial averages, thus resulting in the so-called sample co-variance:

$$
\begin{equation*}
Z_{n}=E[I]=E\left[\hat{\gamma}_{1} \cdot \hat{\gamma}_{2}^{*}\right]=\left\langle\hat{\gamma}_{1} \cdot \hat{\gamma}_{2}^{*}\right\rangle_{n}=\frac{1}{n} \sum_{i=1}^{n} \hat{\gamma}_{1} \cdot \hat{\gamma}_{2}^{*}=I_{n} \exp \left[j \varphi_{n}\right] \tag{18}
\end{equation*}
$$

where $n$ epresents the number of average neighbouring samples, the symbol $\langle\cdot\rangle_{n}$ denotes the spatial average operation and $I_{n}$ and $\varphi_{n}$ represent the amplitude and the phase of the $n$-multi-looked SAR interferogram, respectively. Therefore, the multi-looking procedure leads to a worsening of the spatial resolution of InSAR measurements of factor $n$. Nevertheless, this does not represent a serious drawback because, as a counterpart, the average operation leads to a reduction of the phase noise standard deviation, as outlined hereinafter. Statistics of the multi-looked interferometric phase have been investigated in several papers [6,57-60]. In particular, the InSAR phase has been modelled as characterized by an additive noise [60]:

$$
\begin{equation*}
\varphi_{n}=\varphi_{n}+v_{n} \tag{19}
\end{equation*}
$$

with $\varphi_{x}$ being the true phase and $v_{n}$ denotes a zero-mean additive noise the variance of which is independent of $\varphi_{x}$. The InSAR multi-looked phase is described by the following pdf:

$$
\begin{equation*}
p_{\varphi_{n}}\left(\varphi_{n}\right)=\frac{\beta \sqrt{n}}{2 \sqrt{\pi}} \cdot \frac{\left(1-|k|^{2}\right)^{n}}{\left(1-\beta^{2}\right)^{n+0.5}}, \quad k \cos \left(\varphi_{n}\right) \neq 0 \tag{20}
\end{equation*}
$$

where $\beta=k \cos \left(\varphi_{n}-\varphi_{x}\right)$ and the term $k$ denotes the spatial coherence, which represents the amplitude of the cross-correlation factor $\chi$ between $\hat{\gamma}_{1}$ and $\hat{\gamma}_{2}$ defined as follows:

$$
\begin{equation*}
x=\frac{\left\langle\hat{\gamma}_{1} \cdot \hat{\gamma}_{2}^{*}\right\rangle_{n}}{\sqrt{\left.\left.\left.\langle | \hat{\gamma}_{1}\right|^{2}\right\rangle\left._{n} \cdot\langle | \hat{\gamma}_{2}\right|^{2}\right\rangle_{n}}} \tag{21}
\end{equation*}
$$



Figure 4. Pdf of the interferometric phase for different values of the (a) multi-look factor (with a fixed, given value of spatial coherence that is equal to 0.5 ) and for different values of the (b) spatial coherence (with a fixed value $n=50$ ).

Figure $4 \mathrm{a}, \mathrm{b}$ sketches the pdf in Equation (20) for different values of the number of looks (with a given value of the spatial coherence equal to 0.5 ) and for different values of the spatial coherence (for a fixed value of the number of looks equal to 50), respectively. Plots depicted in Figure 4 are obtained by imposing $\varphi_{x}=0$. It is straightforward to note that the pdf distribution of the multi-look phase (see Equation (20)) is symmetrical with respect to its mean value (i.e., $\varphi_{x}$ ). This is in agreement with the additive model of Equation (19). It is worth noting that the validity of the model (19) is restricted to the $\left[\varphi_{x}-\pi, \varphi_{x}+\pi\right]$ interval. A closed-form for the standard deviation of the interferometric phase is hard to investigate, unless in the limit of Cramer-Rao, which is valid for high values of the spatial coherence $k$, where it assumes the asymptotic value [60]:

$$
\begin{equation*}
\sigma_{\varphi_{n}}=\frac{1}{\sqrt{2 n}} \cdot \frac{\sqrt{1-k^{2}}}{k} \tag{22}
\end{equation*}
$$

Figure 5 plots the standard deviation of the multi-looked phase vs. the spatial coherence for different values of $n$.


Figure 5. Phase standard deviation vs. spatial coherence for different values of the number of independent looks.

For example, if we consider a SAR pixel with given spatial coherence $k=0.35$ and we assume $n=80$, we obtain the height estimate has a standard deviation of about 1.5 m (by assuming a perpendicular baseline of the interferogram of 200 m ). In the calculations, we took into account asymptotical formulations in Equations (12) and (21) and we used the parameters of ASAR/ENVISAT sensor. Note that the obtained value represents a lower bound for the height measurement accuracy.

Generalized models for the multi-looked interferometric noise have also been proposed in [60]. They are based on the observation that a restriction $\varphi_{n} \in\left[\varphi_{x}-\pi, \varphi_{x}+\pi\right]$ does not apply when the phase is considered in the complex plane instead of the real plane. These models describe the real and imaginary parts of the complex phasor $\exp \left[j \varphi_{n}\right]$ as:

$$
\begin{align*}
& \operatorname{Re}\left\{\exp \left[j \varphi_{n}\right]\right\}=\mathrm{N}_{c} \cos \left(\varphi_{x}\right)+v_{n 1}^{\prime} \cos \left(\varphi_{x}\right)-v_{n 2}^{\prime} \sin \left(\varphi_{x}\right)  \tag{23}\\
& \operatorname{Im}\left\{\exp \left[j \varphi_{n}\right]\right\}=\mathrm{N}_{c} \sin \left(\varphi_{x}\right)+v_{n 1}^{\prime} \sin \left(\varphi_{x}\right)+v_{n 2}^{\prime} \cos \left(\varphi_{x}\right) \tag{24}
\end{align*}
$$

where $\mathrm{N}_{c}$ is the expected value of $\cos \left(v_{n}\right)$ and ${v^{\prime}}_{n 1}$ and ${\nu^{\prime}}_{n 2}$ are two zero-mean random variables. $\operatorname{Re}\{\cdot\}$ and $\operatorname{Im}\{\cdot\}$ denote the extraction of the real and imaginary parts operations, respectively. The combination of Equations (23) and (24) in the complex plane results in the following noise model for the complex phasor $\exp \left[j \varphi_{n}\right]$ :

$$
\begin{equation*}
\exp \left[j \varphi_{n}\right]=\left(N_{c}+v_{n 1}^{\prime}+j v_{n 2}^{\prime}\right) \exp \left[j \varphi_{x}\right] \tag{25}
\end{equation*}
$$

It can be demonstrated that, for large values of the multi-look factor $n$ (and in the case $k \neq 0$ ):

$$
\begin{equation*}
N_{c}=1-\frac{1}{8 n} \tag{26}
\end{equation*}
$$

and the standard deviation of the two zero-mean random variables ${v^{\prime}}_{n 1}$ and ${v^{\prime}}^{n}$ are:

$$
\begin{equation*}
v_{n 1 \sigma}^{\prime}{ }_{\sigma}^{2}=\sigma_{v_{n 2}^{\prime}}^{2} \simeq \frac{1}{2}\left(1-k^{2}\right)^{\alpha n} \tag{27}
\end{equation*}
$$

where $\alpha$ is a constant value [60]. Interested readers can also find a comprehensive derivation of the noise model for multi-looked multi-dimensional SAR data in [60].

As earlier anticipated, the InSAR height measurement accuracy strictly depends on the InSAR phase measurement accuracy. InSAR phase can be modelled with the pdf function in Equation (20), which depends on the spatial coherence $k$ of the given SAR pixel. Therefore, it is worth to discuss the sources of noise decorrelation that may impact on the value of the measured spatial coherence. It is known in the literature that the cross-correlation factor (see Equation (21)) can be profitably factorized to make it evident the single sources of decorrelation as follows [41]:

$$
\begin{equation*}
\chi=\chi_{\text {thermal }} \cdot \chi_{\text {spatial }} \cdot \chi_{\text {Doppler }} \cdot \chi_{\text {misreg }} \cdot \chi_{\text {temp }} \tag{28}
\end{equation*}
$$

where $\chi_{\text {thermal }}$ depends on RADAR thermal noise, $\chi_{\text {spatial }}$ depends on geometric relations between the two SAR acquisitions, $\chi_{\text {Doppler }}$ takes account of reduced azimuth spectral overlap of the two interfering SAR images due to their difference of the Doppler Centroid (DC) frequencies, $\chi_{\text {misreg }}$ accounts for possible misregistration errors and, finally, $\chi_{\text {temp }}$ takes into account temporal decorrelation effects, also including the changes over time of the scattering centres location within a volume.

A few additional observations on the decorrelation noise sources are now in order.
(i) The loss of correlation due to thermal noise is given by:

$$
\begin{equation*}
k_{\text {thermal }}=\left|\chi_{\text {thermal }}\right|=\frac{1}{1+S N R^{-1}} \tag{29}
\end{equation*}
$$

where SNR denotes the signal-to-noise ratio.
(ii) The spatial decorrelation arises from the fact that the same ground resolution cell is imaged from slightly different illumination angles, while the master and slave images are collected. It can be modelled as [6]:

$$
\begin{equation*}
k_{\text {spatial }}=\left|\chi_{\text {spatial }}\right|=1-\frac{2 b_{\perp}}{\lambda} \cdot \frac{\Delta r}{r \tan (\vartheta-\Omega)}=1-\frac{b_{\perp}}{b_{\perp c}} \tag{30}
\end{equation*}
$$

where $b_{\perp}$ is the interferometric perpendicular baseline, $\lambda$ is the operational wavelength, $\vartheta$ is the side-looking angle, $b_{\perp}$ is the slant-range distance from the sensor to target, $r$ is the range resolution and $\Delta r$ is the (average) terrain slope angle. From Equation (30), we can easily note how complete decorrelation occurs when the perpendicular baseline is larger than the critical value, defined as: $b_{\perp c}=(\lambda / 2) \cdot \frac{r \tan (\vartheta-\Omega)}{\Delta r}$.
(iii) The Doppler Centroid (DC) decorrelation accounts for the loss of coherence due to a non-perfect overlap of the azimuth spectra for the master and slave SAR acquisitions. The loss of coherence is modelled as follows:

$$
\begin{equation*}
k_{\text {Doppler }}=\left|\chi_{\text {Doppler }}\right|=1-\frac{f_{D C_{\text {Master }}}-f_{D C_{\text {Slave }}}}{4 \pi} \cdot \frac{L}{v} \tag{31}
\end{equation*}
$$

where $f_{D C_{\text {Master }}}$ and $f_{D C_{\text {Slave }}}$ are the $D C$ frequencies of the master and slave SAR images, $L$ is the real antenna aperture and $v$ is the velocity of the platform.
(iv) Mis-registration decorrelation is due to co-registration mistakes [41].
(v) Temporal decorrelation occurs in repeat-pass interferometry. It is very difficult to be modelled from a statistical point of view. Nonetheless, a quantification of temporal decorrelation is available [6]. The volumetric change of a resolution element is measured by considering the influence of horizontal $\sigma_{x}$ and height $\sigma_{z}$ random changes, respectively. Then, by assuming those changes are unrelated to the initial position and are characterized by independent Gaussian probability distributions, the temporal decorrelation is given by:

$$
\begin{equation*}
k_{\text {temp }}=\left|\chi_{\text {temp }}\right|=\exp \left[-\frac{1}{2}\left(\frac{4 \pi}{\lambda}\right)^{2}\left(\sigma_{x}^{2} \sin ^{2} \vartheta+\sigma_{z}^{2} \cos ^{2} \vartheta\right)\right] \tag{32}
\end{equation*}
$$

Temporal decorrelation is one of the main limitations of InSAR technology and particularly over vegetated areas, where decorrelation increases with the amount of vegetation cover because the scatterers of the plants sensibly change over time. From Equation (32), it is clear that volumetric decorrelation is more significant at the lower frequencies (C-band) than at the higher frequencies (L-band). For this reason, use of L-band SAR data, provided (for instance) by the ALOS-1/2 Japanese RADAR instrument, is advantageous for the monitoring of surface height and the changes over time of terrain covered by vegetation [61].

To reduce the decorrelation noise in single InSAR interferograms, several noise-filtering methods have been developed over the last three decades [12,57,62-64]. More recently, some new hybrid multi-temporal InSAR noise-filtering approaches, based on the joint exploitation of sequences of InSAR interferograms, have also been proposed [65-68].

### 2.3. InSAR Technique for the Estimation of Surface Displacements

SAR interferometry nowadays is mostly used for the detection/monitoring of surface changes occurring between passages of the RADAR sensor over the same scene. In such a case, as a slight change across the two SAR acquisition times happens in the imaged scene, an additive term in the interferometric phase associated with the RADAR line of sight (LOS) component of the surface displacement arises, in addition to the phase dependency on the topography. By the inspection of the imaging geometry depicted in Figure 6, we get:

$$
\begin{equation*}
\Delta \varphi=-\frac{4 \pi}{\lambda} \cdot \frac{b_{\perp}}{r \sin \vartheta} z+\frac{4 \pi}{\lambda} d_{L O S} \tag{33}
\end{equation*}
$$

where $d_{\text {LOS }}$ represents the projection of the occurred deformation with respect to sensor LOS direction. For the sake of convenience, we neglected the presence of the flat earth phase contribution.


Figure 6. InSAR geometry for the estimation of the displacement of Earth's surface.

To measure the interferometric phase term associated with the displacement, the interferometric phase contribution pertinent to the underlying topography in Equation (33) has to be removed. Precisely, the differential SAR interferometry (DInSAR) mainly consists in the synthesis of a simulated topographic phase screen from an available Digital Elevation Model (DEM) of the area and to subtract, pixel-by-pixel, these synthetic fringes, leaving only the term associated with the displacement. Computed differential SAR interferograms, however, contain, in addition to the deformation component, some (unwanted) phase terms arising from certain inaccuracies on the knowledge of the actual topographic pattern and of the orbital parameters. In particular, the variation of the interferometric phase can be expressed, more in general, in the form:

$$
\begin{equation*}
\Delta \varphi=\Delta \varphi_{\text {displ }}+\Delta \varphi_{\text {topo }}+\Delta \varphi_{\text {orb }}+\Delta \varphi_{\text {atmo }}+\Delta \varphi_{\text {scatt }}+\Delta \varphi_{\text {noise }} \tag{34}
\end{equation*}
$$

where:
$\Delta \varphi_{\text {displ }}=\frac{4 \pi}{\lambda} d_{\text {LOS }}$ accounts for a possible displacement of the scatterer on the ground between observations, where $d_{\text {LOS }}$ denotes the projection of the relevant displacement vector on the LOS;
$\Delta \varphi_{\text {topo }}=-\frac{4 \pi}{\lambda} \cdot \frac{b_{\perp}}{r \sin \vartheta} \Delta z$ represents the residual-topography-induced phase due to a non-perfect knowledge of the actual height profile (i.e., the DEM errors $\Delta z$ );
$\Delta \varphi_{\text {orb }}$ accounts for residual fringes due to the use of inaccurate orbital information in the synthesis of the topographic phase;
$\Delta \varphi_{a t m}$ denotes the phase components due to the variation of propagation conditions (pertinent to the change in the atmospheric and ionospheric dielectric constant) between the two master/slave acquisitions;
$\Delta \varphi_{\text {scatt }}$ denotes the phase components due to changes in scattering behaviour;
$\Delta \varphi_{\text {noise }}$ includes all the phase noise contributions (see Section 2.2).
Finally, another source of misinterpretation about the (wanted) deformation signal is the presence of phase unwrapping errors, due to an incorrect estimate of $2 \pi$-multiple integers to be added to the (measured) InSAR phase to recover the full (unrestricted) phase [69]. Additional information on the phase unwrapping procedures is provided in Section 2.3.

Overall, limits and potential of InSAR technique are addressed in [44].
Some additional remarks on the error budget of DInSAR measurements are now in order. First of all, we remark that for DInSAR applications, the (wanted) signal to be recovered is the terrain displacement $d_{\text {LOS }}$ (see Equations (33) and (34)), whereas the additional phase terms that appear on the right-hand side of Equation (34) evidently represent error sources, namely $\Delta \varphi_{\text {artifacts }}$. Hence, we can rewrite Equation (34) as:

$$
\begin{equation*}
\Delta \varphi=\frac{4 \pi}{\lambda} d_{\text {LOS }}+\Delta \varphi_{\text {artifacts }} \tag{35}
\end{equation*}
$$

Accordingly, by assuming the (actual) signal and the additive phase artefacts are uncorrelated, the variance of the DInSAR phase signal $\sigma_{\Delta \varphi}^{2}$ can be modelled as:

$$
\begin{equation*}
\sigma_{\Delta \varphi}^{2}=\left(\frac{4 \pi}{\lambda}\right)^{2} \sigma_{d_{L O S}}^{2}+\sigma_{\Delta \varphi_{\text {artefacts }}}^{2} \tag{36}
\end{equation*}
$$

As a consequence, long-wavelength RADAR systems (e.g., operating at L-band) are characterized by less accurate measurements of the LOS deformation through SAR interferometry. At the same time, as earlier said, temporal decorrelation is less severe at L-band, thus leading to a reduced standard deviation of the noise. Hence, there is a balance between these two distinctive effects. In particular, the authors of [70] have demonstrated that LOS range precision of ALOS is globally 1.5 times worse than the corresponding measurements obtained using the C-band ERS RADAR system.

As far as residual topographic artefacts are concerned, they are due to inaccurate knowledge of height topography by the used DEM of the area used for interferogram flattening. The residual topographic phase $\Delta \varphi_{\text {topo }}$ depends on RADAR parameters as well as on the perpendicular baseline of
the considered interferogram. Note that multi-pass interferometry techniques (which are addressed in the following Section 2.3) permit to recover and compensate for such artefacts. The exploited strategy consists in correlating the residual topographic phase terms of a long-lasting sequence of InSAR interferograms with their relevant perpendicular baselines (for instance, see [71]).

As far as orbit errors are concerned, the critical information is the separation between the two acquisition tracks. The estimation and correction of satellite orbit errors that corrupt the computed differential SAR interferograms have already been the matter of previous studies [72-76]. In many cases, the phase artefacts induced by orbit errors are merely approximated with their linear (or quasi-linear) components, often referred to as "orbital ramps," and then compensated. Moreover, other techniques exploit the pixel offsets between the interferometric image pairs to estimate the baseline components [77,78]. The main drawback of this class of algorithms is their limited estimation accuracy that confines their use to preliminary coarse orbit estimation. Accordingly, an additional baseline refinement step is necessary, typically performed by solving for the baseline components that minimize the phase difference between the unwrapped interferometric phase and the corresponding synthetic interferogram. A multi-orbit correction method has recently been proposed in [79] to align the achieved precision of the corrected RADARSAT-1 orbits to that of the precise orbits of the other first-generation C-band spaceborne SAR sensors (e.g., the ERS, ENVISAT sensors of ESA). In particular, the algorithm in [79] investigates the differential phase gradient directly computed from the wrapped interferograms and is focused on the estimation of the perpendicular baseline and of the parallel baseline azimuth rate components, separately performed along the range and azimuth directions, respectively. Starting from the estimates carried out on the interferograms, the orbit correction associated with each SAR acquisition is retrieved by solving a system of linear equations via the Singular Value Decomposition (SVD) method [80].

Finally, for what attains the Atmospheric Phase Screen (APS), the phase artefact is due to the heterogeneity of the medium crossed by the transmitted electromagnetic signal. Studies have shown that APS is correlated over space but uncorrelated in time [81]. In fact, the dominant contribution to the path delay component of phase error is from the spatial heterogeneity of the wet component of the atmospheric refractivity [81-85], which primarily depends on local temperature, pressure and humidity. The APS varies gradually over space and is modelled as a long-wavelength component in the unwrapped phase [83]. Experiments also showed that changes in the tropospheric thickness are responsible for additional phase error contributions that are correlated with the terrain topography [85]. They are due to heterogeneities of the troposphere that appear on interferograms with large topographic variations. Accordingly, because these contributions to APS are highly correlated with the topography, they can be extracted and compensated in sequences of interferograms by searching for those residual phases that are highly correlated with the terrain height, as synthesized from a DEM of the area [83,86].

Furthermore, an additional contribution to the path delay is related to ionospheric heterogeneities, which can significantly differ from the tropospheric artefacts [87-90]. Simple models that describe the APS phase statistics in single interferograms and a noise co-variance model for InSAR time-series is provided in [91].

Figures 7-10 show a selection of DInSAR interferograms generated from SAR data acquired from RADAR instruments mounted on board the first- and second-generation of SAR missions. In particular, Figure 7a,b shows two differential SAR interferograms relevant to the Big Island of the Hawaii, U.S., which is dominated by the deformation due to the Kilauea volcano eruptions. The first interferogram (left side) was produced by processing two SAR images collected by the ASAR instrument on board the ESA ENVISAT satellite [92] on 3 September 2007 and 8 October 2007, with a VV polarization and a perpendicular baseline of 240 m . The second interferogram was obtained starting from two RADARSAT-1 images collected on 28 July 2001 and 25 March 2002, respectively: RADARSAT-1 was an Earth Observation satellite working at C-band managed by the Canadian Space Agency, operational from November 1995 to March 2013 [93].


Figure 7. Hawaii Big Island InSAR experiments: (a) ENVISAT/ASAR differential interferogram relevant to the SAR data-pair 3 September-8 October 2007. (b) RADARSAT-1 differential interferograms generated from the two SAR data acquired on 28 July 2001 and 25 March 2002.


Figure 8. Mt. Etna volcano, Italy InSAR experiments: (a) ALOS-1 differential (wrapped) interferogram computed from the SAR acquisitions collected on 22 March and 7 May 2010, i.e., one repeat cycle (46 days) covering the seismic event. (b) LOS ground deformation map corresponding to the interferogram in (a). (Adapted with permission from [94], Elsevier, 2012).

Figure 8a shows an Advanced Land Observation Satellite (ALOS)-1 differential interferogram relevant to Mt. Etna volcano, Italy, superimposed on amplitude SAR image of the area. Acquisition dates are 22 March and 7 May 2010. Figure 8 b shows the map of ground deformation (in LOS) corresponding to the interferogram shown in Figure 8a. The maximum detectable deformation along the satellite LOS direction was about 23 cm , corresponding approximately to the two fringes that are apparently visible in the interferogram. Note that ALOS-1, managed by the Japanese Aerospace Exploration Agency (JAXA), was operational from January 2006 to May 2011 and worked at L-band
(23.6 cm-wavelength) [95]. As a representative of the use of COSMO-SkyMed SAR data for InSAR applications, Figure 9 shows one differential interferogram (in radar coordinates) relevant to the coastal area of Shanghai produced by SAR images collected on 8 January and 9 February 2014. COSMO-SkyMed is a constellation of four satellites for Earth Observation managed by the Italian Space Agency and operating at X-band (3-cm-wavelength) [96].


Figure 9. COSMO-SkyMed differential interferogram (in radar coordinates) computed from SAR acquisitions collected over Shanghai megacity on 8 January and 9 February 2014.

Finally, two differential interferograms showing the deformation induced by 16 September 2015, Mw 7.7 Chile earthquake [97] are reported in Figure 10. The interferograms are generated from two SAR data pairs acquired on 26 August-19 September 2015 (Figure 10a) and on 31 July-17 September 2015 (Figure 10b) by the Sentinel-1 mission [98].

### 2.4. Multi-Pass InSAR Techniques for the Retrieval of Surface Displacement Time-Series

In this section, we provide a short overview of advanced multi-pass InSAR techniques [71,99-109], allowing to retrieve the temporal evolution of deformation by properly combining sequences of differential SAR interferograms. Two main categories of advanced DInSAR techniques for deformation time-series generation have been proposed. They are often referred to as persistent scatterer (PS) [99-102] and small baseline (SB) [71,103-106] techniques, respectively, although a solution that incorporates both PS and SB approaches has also recently been proposed [107]. Furthermore, more recently, the SqueeSAR method [108], which operates on interferograms computed at the same spacing of the full resolution ones but following an ad-hoc Low-Pass filtering step, has been introduced. SqueeSAR implements a statistical approach, which exploits both phase and amplitude information, to directly retrieve from all the possible interferograms, i.e., without imposing baseline constraints, the noise-filtered phase values associated with the SAR acquisitions. To this aim, the phase triangulation method [108] is applied. The reconstructed phase maps related to each SAR acquisitions, properly post-processed, lead to the generation of surface displacement time-series.

More precisely, PS algorithms select all the interferometric data pairs about a single common master image, without imposing any constraint on the temporal and spatial separation (baseline) among the orbits. In this case, the analysis is carried out at the full spatial resolution scale and is focused on the pixels containing a single dominant scatterer. Conversely, for what concerns the SB techniques, the differential SAR interferograms are generated by considering multiple-master images, in order to have interferometric data pairs with small temporal and spatial baselines. Accordingly,
distributed targets can also be investigated and the analysis may exploit both single-look and multi-look interferograms. Among the SB techniques, a popular approach is the one referred to as Small BAseline Subset (SBAS) [71] that allows producing LOS-projected mean deformation velocity maps and corresponding displacement time-series. The SBAS technique has been initially developed to analyse multi-look (complex average) interferograms [71] and it has subsequently been extended to work with full-resolution interferograms [109], with the aim to analyse localized deformation signals affecting, for instance, single buildings or artificial structures.


Figure 10. Sentinel-1 differential (wrapped) interferograms relevant to the 16 September 2015, Mw 7.7 Chile earthquake, superimposed on a Google Earth image and computed by using the SAR pairs: (left) 26 August-19 September 2015 (ascending orbit, Track 18); (right) 31 July-17 September 2015 (descending orbit, Track 156). The red star is the main shock epicentre. (Adapted with permission from [97], MDPI, 2017).

As previously said, the SBAS approach relies on imposing constraints on the spatial and temporal baselines of SAR data pairs used to produce the interferograms. Accordingly, the selected SAR data pairs may be arranged in (few) subsets that are separated by large baselines. These subsets turn out to be independent of each other (since no suitable interferogram that connects SAR images belonging to different subsets exists). The presence of subsets gives rise to an underdetermined problem for the time-series inversion, which can be solved by searching for a minimum norm least squares solution via the SVD method [80].

In 2015, an improved SBAS processing chain, which complements the Extended Minimum Cost Flow (EMCF) [110] space-time phase unwrapping operations with an innovative space-time noise-filtered approach and an optimized selection of InSAR data to be inverted, has also been proposed [68]. To provide an example of the effectiveness of the noise-filtered approach implemented in [68], we show in Figure 11 a comparison between conventional and noise-filtered ASAR/ENVISAT differential SAR interferograms detecting the 6 April 2009, Mw. 6.3 L'Aquila (Italy) earthquake.


Figure 11. Comparison between the unfiltered (left column) and noise-filtered (right column) multi-look ASAR/ENVISAT interferograms relevant to the area of the Abruzzi region, Italy. (a-c) interferograms relevant to 30 October 2005-8 November 2009, 21 August 2005-6 June 2010 and 1 August 2004-12 April 2009 SAR data-pairs, characterized by perpendicular baseline values of 192,145 and 395 m , respectively. (d-f) Noise-filtered multi-look interferograms corresponding to the ones in (a-c), respectively. (Adapted with permission from [68], IEEE, 2015).

Hereinafter, a few additional details about the rationale of the Small BAseline Subset (SBAS) approach will be provided.

The starting point is the availability of a sequence of, say M, differential SAR interferograms. Measured interferometric phases are restricted to the $[-\pi, \pi]$ interval. However, to produce deformation time-series, the information conceived in the phase must be unrestricted. Phase Unwrapping (PhU) operations, essentially consisting in recovering the absolute phase field from the observed wrapped measurements, are employed to accomplish this task. Over the years, much work has been done on two-dimensional (space) PhU, which has resulted in many algorithms. They may be arranged in three main categories: minimum-norm [111,112], branch-cut [113] and minimum cost flow (MCF) network [69] methods. More recently, the need for analysing long sequences of multi-temporal interferograms for (advanced) DInSAR applications has also promoted the development of new PhU approaches, based on the joint exploitation of the spatial and temporal relationships among the produced DInSAR interferograms [110,114,115]. Among them, a technique that is very well integrated within the SBAS procedure is the one proposed in [110], which is referred to as extended MCF (EMCF) and represents the space-time extension of the conventional MCF approach [69].

The sequence of unwrapped interferograms can be expressed, pixel-by-pixel, as follows:

$$
\begin{equation*}
\Delta \varphi_{k}=\frac{4 \pi}{\lambda} d_{k}-\frac{4 \pi}{\lambda} \frac{b_{\perp k}}{r \sin \vartheta} \Delta z+\Delta \varphi_{o r b, k}+\Delta \varphi_{a t m o, k}+\Delta \varphi_{s c a t t, k} k=1, \ldots, M \tag{37}
\end{equation*}
$$

where $d_{k}$ and $b_{\perp k}$ are the LOS deformation and the perpendicular baseline values of the $k$-th interferogram. $\Delta z$ is the error of the used DEM and $\Delta \varphi_{o r b, k}, \Delta \varphi_{a t m o, k}$ and $\Delta \varphi_{s c a t t, k}$ are the orbital inaccuracies, the APS and the scattering phase contributions relevant to the k-th interferogram. For the sake of simplicity, we have included in $\Delta \varphi_{\text {scatt }, k}$ also the phase noise signal that corrupt the measure of the phase measurement.

The system of Equations (37) can be reorganized using the matrix formalism as follows [71]:

$$
\begin{equation*}
\mathbf{A} \cdot \boldsymbol{\Phi}=\Delta \boldsymbol{\Phi} \tag{38}
\end{equation*}
$$

where $\mathbf{A}$ is an incidence-like matrix, related to the identified set of SB InSAR data-pair and $\Delta \boldsymbol{\Phi}$ is the vector of unwrapped phases. The elements of matrix A are defined as follows:

$$
\left\{\begin{array}{c}
A\left(j, I M_{j}\right)=1 I M_{j} \neq 0  \tag{39}\\
A\left(j, I S_{j}\right)=-1 I S_{j} \neq 0 \\
\text { Ootherwhise }
\end{array}\right.
$$

where IM and IS are the indices vectors of the master and slave time acquisitions concerning the $N+1$ ordered times $\left[t_{0}, t_{1}, t_{2}, \ldots, t_{N}\right]^{T}$. The system of Equation (38) can be solved in the Least Squares (LS) sense:

$$
\begin{equation*}
\boldsymbol{\Phi}=\mathbf{A}^{+} \cdot \Delta \boldsymbol{\Phi}=\left(\left(\mathbf{A}^{T} \cdot \mathbf{A}\right)^{-1} \cdot \mathbf{A}^{T}\right) \cdot \Delta \boldsymbol{\Phi} \tag{40}
\end{equation*}
$$

where $\mathbf{A}^{+}$is the left inverse matrix. However, generally speaking, the matrix $\mathbf{A}$ can also be rank deficient: This happens when SB InSAR data pairs lead to the presence of several independent subsets of SB interferograms separated by large baselines [71]. In this case, the matrix $\mathbf{A}^{T} \cdot \mathbf{A}$ is rank-deficient and does not admit an inverse matrix, that is to say the number of LS solutions of the problem (38) is infinite. Among the infinite LS solutions, one solution is selected by applying the SVD method to matrix $\mathbf{A}$.

More specifically, the solution of the problem is the one that minimizes the norm of the residuals of the system of Equation (38) and, at the same time, the norm of the phase vector $\boldsymbol{\Phi}$ (i.e., $\|\boldsymbol{\Phi}\|_{2}$ ). However, such a solution may introduce large discontinuities in the obtained results, thus leading to a non-physical sound solution (see Figure 12). A strategy to overcome this problem is at the base of the SBAS algorithm [71]: it consists in manipulating the system of Equations (38) in such a way to
replace the phase unknowns $\boldsymbol{\Phi}_{i}, i=0, \ldots, N$ with the mean phase velocity between time-adjacent acquisitions $V_{i}, i=0, \ldots, N-1$, which are defined as follows:

$$
\begin{equation*}
\mathbf{V}=\left[V_{0}=\frac{\Phi_{1}-\Phi_{0}}{t_{1}-t_{0}}, V_{1}=\frac{\Phi_{2}-\Phi_{1}}{t_{2}-t_{1}}, \ldots, V_{N-1}=\frac{\Phi_{N}-\Phi_{N-1}}{t_{N}-t_{N-1}}\right]^{T} \tag{41}
\end{equation*}
$$

Accordingly, the system of Equation (38) becomes:

$$
\begin{equation*}
\mathbf{B} \cdot \mathbf{V}=\Delta \boldsymbol{\Phi} \tag{42}
\end{equation*}
$$

which is solved in the LS sense by applying the SVD method to the matrix $\mathbf{B}$.


Figure 12. An example describing how SBAS works with two subsets identified by blue and orange dots. Dotted line refers to the actual deformation time-series, red and orange lines refer to the estimated minimum-norm-velocity and minimum-norm phase deformation time-series, respectively.

Once the phase associated with each SAR acquisition, as well as the residual topography, are estimated, the phases are converted to deformation and the APS is computed and filtered out from the obtained deformation time-series. APS removal is achieved by exploiting the assumption that APS is correlated in space and uncorrelated in time. Thus, the processing of the atmospheric corrupted time-series is performed with a spatial low-pass (LP) filter and a time high-pass (HP) filter [71,109].

The quality of retrieved LOS time-series is finally evaluated pixel-by-pixel by calculating the values of the temporal coherence factor, originally proposed in [110]. Residual orbital fringes are also estimated and filtered out in the SBAS processing chain by searching for (in each interferogram) any possible phase ramp, which can be directly related to errors in the knowledge of sensor position along its orbit. Such residual phase ramps are jointly analysed to correct the orbits state vectors. Finally, for pixels with high temporal coherence, the map of LOS mean deformation rate over the analysed period is computed.

The accuracy of the displacement time-series retrieval by the SBAS algorithm in different geophysical contexts has been assessed and the results have been the subject of several investigations (see, for instance, [107,116-118]). Experiments, based on the comparison between DInSAR deformation time-series and independent GPS/levelling measurements, show that the SBAS technique provides an estimate of the mean deformation velocity with a standard deviation of about $1 \mathrm{~mm} /$ year for a typical data set composed by 40 to 60 SAR images [117]. Moreover, the single displacement measurements, computed with respect to a reference point of known motion, show a sub-centimetric accuracy, with a standard deviation of about 5 mm , consistently in both the SAR/levelling and SAR/GPS comparisons. Different SB multi-pass DInSAR tools have been developed in the recent years for the reconstruction of ground deformation [119-121]. A cross-comparison analysis between different SB approaches is provided in [121]. To illustrate the capability of the SBAS methodology, we present the results
of experiments conducted for three different applications (Figures 13-15). The first investigation concerns the study of urban deformations within the metropolitan area of Istanbul, Turkey. The second experiment is relevant to the Mt. Etna volcano area, Sicily Island, Italy, while the third one pertains to the analysis of landslide deformations in the city of Assisi, Italy. Figure 13 shows the SBAS-DInSAR results achieved over Istanbul by processing 43 TerraSAR-X data ( $3 \mathrm{~m} \times 3 \mathrm{~m}$ spatial resolution) collected during the 2010-2012 period. In particular, the produced spatially-dense deformation velocity map and time-series associated to points affected by land subsidence, have been reported, pointing out the relevance of DInSAR techniques as tools for supporting sustainable urban planning and management [122].


Figure 13. SBAS-DInSAR products for Istanbul megacity, Turkey (Adapted with permission from [122], MDPI, 2017). (a) Deformation velocity map generated by processing TerraSAR-X data acquired from 2010 to 2012. (b) Zoomed view of the deformation velocity map over the Golden Horn heritage district. (c,d) Displacement time-series for two SAR points located in Miniaturk and Yenikap areas.


Figure 14. SBAS-DInSAR products for the Mt. Etna volcano (Italy), during the 2009-2010 period. (a) Mean deformation velocity map of the area obtained by using X-band COSMO-SkyMed data. (b) Mean deformation velocity map of the same area obtained by using L-band ALOS-1 data. (c) Mean deformation velocity map of the same area obtained by using C-band ERS/ENVISAT data. (d) COSMO-SkyMed time series of deformations across the Pernicana Fault trace: the plot shows the displacement of the point labelled as a red star in (a) with respect to the one marked with a red circle in (a). (e) Same as (d) for ALOS. (f) Same as (d) for ERS/ENVISAT. The vertical red line identifies the occurrence of the 3 April $2010 \mathrm{M}=4.3$ seismic event. (Adapted with permission from [123], Elsevier, 2014).

Figure $14 \mathrm{a}-\mathrm{c}$ show the LOS mean deformation velocity maps obtained by processing COSMO-SkyMed, ALOS and ERS/ENVISAT data, respectively, for the north-eastern flank of Mt. Etna volcano, Sicily, which corresponds to the area of the well-known Pernicana Fault [123]. An increased spatial coverage of the COSMO-SkyMed measurements, with respect to the C-band case, is clearly observed. On the other hand, a denser spatial coverage achieved by ALOS data shown in Figure 14b is visible, especially for areas closer to the fault. In this case, the coherence improvement due to the longer L-band wavelength is predominant over the effect of the different spatial resolution. On 3 April 2010, a $\mathrm{Mw}=4.3$ earthquake occurred in the Pernicana area, thus making this region particularly interesting for a time series analysis. When discontinuous seismic signals are expected, the choice of the SBAS approach is particularly appropriate since no temporal model is required. A comparison of the three datasets regarding their temporal features is shown in Figure 14d-f wherein the time series of the relative displacement across the Pernicana Fault are reported.

$\begin{array}{lllllll}<-7.5 & -4.5 & -3.0 & -1.5 & 1.5 & 3.0 & >4.5\end{array}$
Figure 15. Deformation velocity map for the city of Assisi, Italy, generated by processing COSMO-SkyMed data acquired from 2009 to 2012, superimposed on the Landslide Inventory map. Shades of blue show ancient and relict landslides; shades of red show recent landslides (Adapted with permission from [24], Elsevier, 2014).

The SBAS-DInSAR technique has been successfully applied also to investigate mass movements, as the Ivancich landslide affecting the city of Assisi, Central Italy. In particular, a dataset of 39 COSMO-SkyMed images collected in the 2009-2012 time interval, along descending orbits with a $3 \mathrm{~m} \times 3 \mathrm{~m}$ spatial resolution has been used. The analysis resulted in a very significant density of SAR measure points (in average, about 15,000 points $/ \mathrm{km}^{2}$ ), showing the improved capability of the high spatial resolution SAR sensors in detecting and assessing ground deformations induced by active landslides in urban and sub-urban areas [24].

## 3. Multi-Track/Multi-Satellite InSAR Methodologies

Nowadays there is an increasing availability of large archives of SAR data collected by several RADAR instruments mounted on board space-borne platforms, which operate at different wavelengths and with distinctive looking angle geometries (and also possibly through different acquisition modes). This poses the issue of how to effectively combine the complementary pieces of information embedded by the different SAR datasets. In particular, the combination of multi-platform (multi-angle) LOS displacement time series can improve our ability to retrieve the 3-D, i.e., East-West (E-W), North-South (N-S), Up-Down (U-D) components of the measured surface displacement; thus, overcoming the main limitation of DInSAR to measure only the satellite LOS projection of the displacement. Such a problem has already been faced in the literature and a few technical solutions capable of combining multiple-orbit/multiple-angle DInSAR-based measurements, as well as merging DInSAR data products with other external information (such as the one derived from GPS stations), have been
proposed [124-135]. Let us first consider the combination of InSAR data acquired from two satellites flying along ascending and descending orbits with $\vartheta_{1}$ and $\vartheta_{2}$ side-looking angles, respectively (see Figure 16). Note that, for the sake of convenience, the N-S deformation components have been considered negligible. This is due to the consideration that almost all modern space-borne satellites move along near-polar orbits (i.e., satellite azimuthal direction is approximately parallel to N-S) and, thus, there is no diversity in the viewing geometries to accurately measure N-S displacements.


Figure 16. Multi-angle InSAR observations. Deformation is discriminated with respect to its horizontal East-West $\left(d_{H}\right)$ and vertical Up-Down $\left(d_{V}\right)$ components.

The LOS components of the deformation $\mathbf{d}$ can be related to the E-W, namely $d_{H}$ and U-D, namely $d_{V}$, components through the following equations [136]:

$$
\left\{\begin{array}{c}
d_{L O S_{1}}=\mathbf{d} \cdot \hat{\mathbf{i}}_{\mathrm{LOS}_{1}}=d_{H} \sin \vartheta_{1}+d_{V} \cos \vartheta_{1}  \tag{43}\\
d_{\text {LOS }_{2}}=\mathbf{d} \cdot \hat{\mathbf{i}}_{\mathrm{LOS}_{2}}=-d_{H} \sin \vartheta_{2}+d_{V} \cos \vartheta_{2}
\end{array}\right.
$$

The system of Equation (43) can be expressed using matrix formalism as:

$$
\left(\begin{array}{cc}
\sin \vartheta_{1} & \cos \vartheta_{1}  \tag{44}\\
-\sin \vartheta_{2} & \cos \vartheta_{2}
\end{array}\right) \cdot\binom{d_{H}}{d_{V}}=\binom{d_{L O S_{1}}}{d_{L O S_{2}}}
$$

In this simplified case, a direct solution can be formally achieved as follows:

$$
\binom{d_{H}}{d_{V}}=\left(\begin{array}{cc}
\sin \vartheta_{1} & \cos \vartheta_{1}  \tag{45}\\
-\sin \vartheta_{2} & \cos \vartheta_{2}
\end{array}\right)^{-1} \cdot\binom{d_{L O S_{1}}}{d_{L O S_{2}}}=\frac{\binom{d_{L O S_{1}} \cos \vartheta_{2}-d_{L O S_{2}} \cos \vartheta_{1}}{d_{L O S_{1}} \sin \vartheta_{2}+d_{L O S_{2}} \sin \vartheta_{1}}}{\sin \left(\vartheta_{1}+\vartheta_{2}\right)}
$$

In the more simplified case that ascending and descending SAR data are acquired from the satellite with the same side-looking angle $\vartheta$, the results of the combination particularize as follows:

$$
\begin{equation*}
\binom{d_{H}}{d_{V}}=\frac{\binom{d_{L O S_{1}} \cos \vartheta-d_{L O S_{2}} \cos \vartheta}{d_{L O S_{1}} \sin \vartheta+d_{L O S_{2}} \sin \vartheta}}{\sin (2 \vartheta)}=\binom{\frac{d_{L O S_{1}}-d_{L O S_{2}}}{2 \sin \vartheta}}{\frac{d_{L O S_{1}}+d_{L O S_{2}}}{2 \cos \vartheta}} \tag{46}
\end{equation*}
$$

We may observe that the vertical displacement is associated with the sum of the two LOS deformation measurements whereas the E-W component is related to the difference between the two deformation measurements, respectively. Note that this method is beneficial if we are interested in merely combining the rate of deformations from ascending and descending orbits. More challenging is the generation of combined deformation time-series (see Section 4) because, apart from rare exceptions, ascending and descending orbits are not coeval over the same region (i.e., SAR data are not acquired simultaneously from the two complementary observation points). A way to overcome this problem is to interpolate LOS time-series acquired on ascending and descending orbits over the whole set of time acquisitions. However, such solution, in general, is of a low precision because of atmospheric, orbital, thermal and interpolation noise presented in original and recreated by the interpolation data.

To illustrate the results achieved through the basic combination technique described by Equations (43)-(46), we show in Figure 17a,b the E-W and U-D displacement maps obtained by combing ascending and descending COSMO-SkyMed DInSAR products related to the Mount Etna volcano area, Italy (see Table 1).


Figure 17. Estimated COSMO-SkyMed horizontal E-W (left side) and vertical U-D (right side) mean displacement velocity maps for the Mt. Etna volcano area, Italy, relevant to the 2011-2015 period.

Table 1. Data used for generating the E-W and U-D DInSAR maps shown in Figure 17.

| Mt. Etna Volcano |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sensor | Orbit | Start Time | End Time | Number of <br> Acquisitions | Number of <br> Interferograms |
| CSK | Descending | 23 July 2011 | 15 January 2015 | 87 | 198 |
| CSK | Ascending | 12 July 2009 | 10 January 2015 | 146 | 309 |

Let us now address the issue of combining multi-track InSAR data in a more general way, by referring to the achievements proposed in the literature.

In the work of Wright et al. [124], a global approach to recover 3-D displacements from the combination of ascending/descending and right/left looking SAR acquisitions was initially discussed. In particular, the authors combined five RADARSAT-1 interferograms generated from four right-looking ascending/descending passes and recovered the U-D and the E-W deformation field induced by the 23 October 2002, Nenana Mountain (Alaska) earthquake. In their investigation, they voluntarily neglected the N-S deformation, which is assumed to be very small. Resolving the N-S components of deformation, as said, is very critical, because space-borne satellites move along N-S oriented orbits. Such a limitation in recovering the N-S components was circumvented in the work of Gray [125] by combining LOS displacements derived from the extra-low and the extra-high beams of the RADARSAT-2 sensor to estimate the full 3-D movements of the Henrietta Nesmith Glacier. The whole 3-D deformation components were also inferred in [126,127] by complementing LOS displacements with GPS measurements.

To overcome the problem due to the low sensitivity of LOS measurements to N-S displacements, Pixel Offset (PO) tracking techniques have also been exploited. In particular, in [128,129], the 3-D co-seismic displacements were derived for the 1999 Hector Mine and 2001 Bam earthquakes, based on the combination of ascending/descending interferograms and Azimuth Pixel Offset (AZPO) measurements. The accuracy of estimating the azimuth offsets with amplitude matching can reach a fraction (i.e., $1 / 30$ th) of the pixel spacing; henceforth, it is greater than 10 cm [137-139]. Although PO methods have mostly been devoted to studying single deformation events, some efforts have also been made for extending these techniques to the generation of 3-D displacement time series, by combining the information derived from both sequences of multi-temporal DInSAR interferograms and amplitude maps. In particular, this is the case of the Pixel-Offset SBAS (PO-SBAS) technique [139]. The algorithm analyses the amplitudes of selected image pairs to calculate the relative across-track (range) and along-track (azimuth) pixel-offsets and inverts them through an SVD method for the retrieval of the range and the azimuthal displacement time-series. Experiments carried out using ENVISAT images collected over Sierra Negra Caldera have proved the capability of the PO-SBAS technique to investigate the temporal evolution of large or rapidly varying surface deformation phenomena, guaranteeing accuracy values of the order of $10-12 \mathrm{~cm}$. Very recently, a method for retrieving the 3-D components associated with massive deformation episodes, fully-based on the use of PO-SBAS measurements have been presented in [140]. The key idea of [140] is to combine the PO-SBAS time-series, which represent a direct measure of the deformation along the sensor-azimuthal direction (roughly parallel to $\mathrm{N}-\mathrm{S}$ ) and the LOS direction, taking into account the orbital flight parameters. To overcome the problem that orbitals are not coeval, the combination is performed by assuming that ascending and descending acquisitions are as close as possible in time (i.e., by considering them as acquired at the same time. A way to overcome this limitation has been studied in [32,136,141-143]. In particular, the Minimum Acceleration (MinA) combination algorithm has been developed in such a way to complement PO-SBAS, GPS and InSAR-based measurements in a single framework (see Section 4 for additional details). Very recently, innovative DInSAR-based combination approaches relying on the use of a Kalman filter have also been proposed [136]. More specifically, a method to combine overlapping segments of SAR images acquired at adjacent tracks to generate high spatiotemporal resolution maps of the (combined) LOS displacement field has been presented in [141]. Within this general context, in $[142,143]$, similar methods have been proposed for the combination of multi-track interferograms from various sensors and orbital positions; thus, obtaining time series of the U-D and E-W displacement. These approaches preserve the temporally variable components of the deformation field and, practically, assume the N-S deformation negligibility. In particular, the algorithm presented in [142], which is known in the literature to as Multiple-SBAS (MSBAS) consists of generating and simultaneously processing a considerable sequence of multiple-platform differential SAR interferograms. The latter are jointly inverted to recover (over the geocoded grid common to
all available SAR data tracks) 2-D (U-D and E-W) surface deformation time-series by solving an underdetermined system of linear equations. This latter relates the LOS displacements relevant to all the available unwrapped interferograms to the (unknown) 2-D deformation components and it is inverted through the LS approach by searching for a minimum-norm (MN)-velocity solution based on the use of the Tikhonov regularization [143,144].

## 4. Minimum Acceleration Combination Technique: Rationale and Applications

The potential of an alternative technique, known as minimum-acceleration (MinA) combination technique, which does not require the simultaneous process of very large archives of DInSAR interferograms has been proposed in [32]. It consists of a straightforward post-processing stage that involves the analysis of sequences of independently processed (potentially, also with different DInSAR toolboxes) multi-platform LOS displacement time series. Before their combination, LOS displacement time series are also depurated from atmospheric artefacts and residual topographic errors, as provided within the used DInSAR toolboxes. Following the lines of $[71,142]$, the preliminary-computed LOS displacement time-series are connected to the unknown 3-D velocities among consecutive time acquisitions. This leads to the writing of an underdetermined system of independent linear equations, which might be solved in the LS sense by using the SVD. The obtained system of linear equations is regularized by imposing the additional constraint that the 3-D displacement components are with minimum acceleration, which means that the difference between consecutive velocities is minimal. Once estimated, the unknown 3-D velocities are eventually (and independently) time integrated to recover the E-W, N-S and U-D deformation time series.

To introduce the right mathematical framework, let us assume the availability of K independent sets of multiple-platform SAR data collected at ordered times $t^{(j)}=\left[t_{0}^{(j)}, t_{1}^{(j)}, \ldots, t_{Q_{j}-1}^{(j)}\right]^{T} \forall j=1, \ldots, K$ over the same area on the ground, consisting of $Q_{j}$ distinctive time epochs, respectively. The MinA algorithm [32] requires the preliminary generation from each single SAR data-track of the original LOS-projected deformation time-series. This task can be achieved by independently applying either the SBAS technique [71] or other alternative multi-temporal DInSAR approaches to the available K SAR datasets. During this preliminary stage, the residual topography, as well as the APS artefacts corrupting differential SAR interferograms, might be estimated and successfully filtered out from the generated LOS-projected displacement time-series.

The obtained LOS-projected time-series of deformation are geocoded to a common spatial grid of points where the subsequent combination stage is applied. During this preliminary step, the location of high coherent targets is also identified. Henceforth, let $\mathbf{d}^{(j)}=\left[d_{0}^{(j)}, d_{1}^{(j)}, \ldots, d_{Q_{j}-1}^{(j)}\right]^{T} \forall j=1, \ldots, K$ be the geocoded LOS-projected deformation time-series relevant to a pixel $P$ that belongs to the group of high-coherent pixels common to all the available K SAR datasets. LOS-projected time-series of deformations are expressed with respect to the instants $t_{0}^{(j)}, \forall j=1, \ldots, K$, which are singularly taken as reference for each dataset, that is to say $d_{0}^{(j)}=0, \forall j=1, \ldots, K$. Let us now describe how the algorithm works and let $Q=\sum_{j=1}^{K} Q_{j}$ be the total number of the available SAR images collected at the "whole" ordered times $T=\cup_{j=1}^{K} t^{(j)}=\left[T_{0}, T_{1}, \ldots, T_{Q-1}\right]^{T}$. We observe that a generic LOS-projected deformation measurement, namely $d_{\text {LOS }}$, can be related to its inherent 3-D components, namely $\left[d_{E-W}, d_{U-D}, d_{N-S}\right]^{T}$, as [32]:

$$
\begin{equation*}
d_{\text {LOS }}=\mathbf{d} \cdot \hat{i}_{\text {LOS }}=\sin \vartheta \cos \varphi d_{\text {East-West }}-\cos \vartheta d_{\text {Up-Down }}+\sin \vartheta \sin \varphi d_{\text {North-South }} \tag{47}
\end{equation*}
$$

where $\hat{i}_{\text {LOS }}$ is the LOS-direction versor. Note that $\theta$ and $\varphi$ represent the RADAR side-looking and the satellite heading angles, respectively; the imaging geometries for ascending/descending data-tracks are shown in Figure 18. Extending to our case what initially proposed in [71], let us relate the available LOS deformations $d^{(j)}(P), j=1, \ldots, K$ (for each high coherent pixel) to their unknown

3-D components. This leads to the writing of a system of Q-K independent linear equations with respect to the $M=3(Q-1)$ unknowns representing the East-West (E-W), Up-Down (U-D) and North-South (N-S) deformation velocities components between adjacent time-acquisitions, namely $\mathbf{V}_{\mathbf{E}}=\left[V_{E_{1}}, V_{E_{2}}, \ldots, V_{E_{Q-1}}\right], \mathbf{V}_{\mathbf{U}}=\left[V_{U_{1}}, V_{U_{2}}, \ldots, V_{U_{Q-1}}\right]$ and $\mathbf{V}_{\mathbf{N}}=\left[V_{N_{1}}, V_{N_{2}}, \ldots, V_{N_{Q-1}}\right]$. This system of linear equations can be expressed using matrix formalism as follows [71]:

$$
\mathbf{B} \cdot\left[\begin{array}{c}
\mathbf{V}_{\mathbf{E}}  \tag{48}\\
\mathbf{V}_{\mathbf{U}} \\
\mathbf{V}_{\mathbf{N}}
\end{array}\right]=\left[\begin{array}{c}
\Gamma^{1}\left(d^{(1)}-d_{0}^{(1)}\right) \\
\Gamma^{2}\left(d^{(2)}-d_{0}^{(2)}\right) \\
\cdots \\
\Gamma^{K}\left(d^{(K)}-d_{0}^{(K)}\right)
\end{array}\right]=\widetilde{\mathbf{d}}
$$

where $\Gamma^{j} j=1, \ldots, K$ are the values of temporal coherence [110] associated with the $K$ different datasets (representing a quality factor of the obtained LOS displacement time-series) and B is the incidence-like matrix of the linear transformation that converts LOS-projected measurements into their essential 3-D components (see [71], for further details).


Figure 18. SAR data acquisition geometries in the Up-East (a) and North-East (b) planes.

The system of Equations (47) and (48) has fewer linear independent equations (Q-K) than unknowns (M). Thus, it is an under-determined system that does not admit a unique solution. The matrix $\mathbf{B}$ has singular values that gradually decay to zero, thus rendering any solution much sensitive to noise level corrupting the vector $\widetilde{\mathbf{d}}$. It represents a canonical example of a linear discrete ill-posed problem whose meaningful solution can be obtained by replacing the "original" linear system (47) and (48) by a nearby system less sensitive to perturbations of the right-hand side of the system. This operation is known as regularization and can be performed using Tikhonov regularization [144], Truncated Singular Value Decomposition (TSVD) [145] and maximum entropy principle [146]. MinA algorithm accomplishes the regularization problem by adding to the original system (47) and (48) new equations that impose the condition the (unknown) 3-D (E-W, U-D, N-S) displacement time-series are with minimum curvature. That is to say, the velocity deformation differences (for all the 3-D components) between consecutive time intervals is minimal. Such conditions can formally be expressed by adding to $(2)$ the following set of $3(Q-2)$ additional equations:

$$
\begin{align*}
& \kappa\left(V_{E_{i+1}}-V_{E_{i}}\right) i=1, \ldots, Q-2 \\
& \kappa\left(V_{U_{i+1}}-V_{U_{i}}\right) i=1, \ldots, Q-2  \tag{49}\\
& \kappa\left(V_{N_{i+1}}-V_{N_{i}}\right) i=1, \ldots, Q-2
\end{align*}
$$

where k is a proper regularization factor. Accordingly, the regularized system of linear equations becomes:

$$
\left[\begin{array}{l}
\mathbf{B}  \tag{50}\\
\mathbf{C}
\end{array}\right] \cdot\left[\begin{array}{l}
\mathbf{V}_{\mathbf{E}} \\
\mathbf{V}_{\mathbf{U}} \\
\mathbf{V}_{\mathbf{N}}
\end{array}\right]=\left[\begin{array}{c}
\widetilde{\mathbf{d}} \\
\mathbf{0}
\end{array}\right]
$$

where $\mathbf{C}$ is the incidence-like matrix related to the minimum-acceleration-regularization linear transformation. The solution of (50) is finally obtained in the LS sense by applying Truncated SVD to the matrix $\Omega=\binom{\mathbf{B}}{\mathbf{C}}$.

Finally, once the problem in (40) is solved, the 3-D velocity deformation components are independently time-integrated to recover the relevant 3-D displacement time-series.

A simplified version of the MinA algorithm, which only computes the time-series of E-W and U-D components and estimates the rate of deformation along the N-S direction is detailed in [32]. Notice that in the areas where the expected N-S deformation is almost negligible the algorithm can be further simplified by only considering as unknowns the E-W and U-D displacement signals. MinA algorithm can be simply complemented, as a post-processing phase, with additional data, such as GPS, PO-based and levelling measurements, with no drastic modifications of the original algorithm. The general scheme of the MinA algorithm is shown in Figure 19.


Figure 19. MinA diagram block. $K$ independent sets of LOS measurements of the surface ground displacement, as obtained by processing data from K multi-angle/multi-sensor SAR systems, are combined (taking into account the associated quality reconstruction maps). The combination is based on the application of minimum-acceleration constraints on the achievable U-D, E-W and N-S time-series of deformation. (Adapted with permission from [32], IEEE, 2016).

An example, consisting of the application of the MinA algorithm to a data archive relevant to the Big Island of Hawaii (U.S.) was presented in [32]. Dataset was composed by 36 Stripmap and 13 ScanSAR images acquired on descending orbits (Track 200, Frame 3231) and 23 Stripmap and seven ScanSAR images collected on ascending orbits (Track 93, Frame 387) by the ASAR/ENVISAT satellite, spanning the overall time interval between 20 January 2003 and 22 September 2009. Figures 20-22 show the mean displacement velocity maps as well as a selection of E-W, U-D and N-S displacement time-series relevant to pixels located in areas with significant deformations.

Let us finally discuss the accuracy of the 3-D displacement time-series retrieved by applying the MinA technique by comparing time-series with continuous GPS measurements available over the Big Island area. The deformation time-series for the E-W, U-D and N-S components are shown
in Figures 20-22, where the combined time-series are represented with black triangles and the GPS measurement with red stars. Standard deviation values of the difference between DInSAR and GPS data are indicated in the presented plots. In this analysis, GPS measurements were assumed as a reference, thus neglecting any possible errors that may affect the data. As a result of the comparison, it was demonstrated that U-D and E-W time-series have an accuracy (on average) of about 8 and 9 mm , respectively.


Figure 20. U-D DinSAR results relevant to Big Island of Hawaii, U.S. (a) false colour mean displacement velocity map superimposed on a grey-scale SAR amplitude image of the area. ( $\mathbf{b}-\mathbf{g}$ ) Plots of the U-D time-series (black triangles) compared to GPS-driven U-D time-series of displacement (red stars). GPS locations are highlighted in (a). (Adapted with permission from [32], IEEE, 2016).

Conversely, N-S displacements estimates have accuracy of the order of 2.5 cm . Note that a simplified version of the MinA algorithm was applied in this case, allowing only the estimate of the N-S deformation rate. Accordingly, areas characterized by severe non-linear deformation signals (see for instance the deformation related to KTM GPS station) show worse accuracies (of about 8 cm in the case of KTM station). As expected, the N-S displacement time-series retrieval accuracy is on the order of a few centimetres, whereas for the E-W and U-D component it is on the order of some millimetres.


Figure 21. E-W DinSAR results relevant to Big Island of Hawaii, U.S. (a) false colour mean displacement velocity map superimposed on a grey-scale SAR amplitude image of the area. (b-g) Plots of the E-W time-series (black triangles) compared to GPS-driven E-W time-series of displacement (red stars). GPS locations are highlighted in (a). (Adapted with permission from [32], IEEE, 2016).

However, these values are better than ones expected by using Pixel-Offset [139] or Multiple-Aperture-Interferometry $[147,148]$ techniques, which are on the order of fractions of the image pixel dimension (on the order of 10 centimetres, or more). As an additional example, we also show in Figure 23 the results of another experiment performed by combining a set of COSMO-SkyMed and Sentinel-1A SAR data acquired over the coastal area of Shanghai. In particular, the COSMO-SkyMed dataset is the one exploited in [149], consisting of 61 SAR scenes (descending passes, HH polarization, with a side-looking angle of about $29^{\circ}$ and a satellite heading angle of about $8^{\circ}$ ) collected from December 2013 to March 2016. The second dataset, acquired through the Sentinel-1 mission from February 2015 to April 2017, consisted of 33 SAR scenes (ascending passes, VV polarization, with a side-looking angle of about $39^{\circ}$ and a satellite heading angle of about $12^{\circ}$ ). Sentinel- 1 data were available in the single-look-complex (SLC) format and acquired through the Interferometric Wide Swath (IW) mode by employing the Terrain Observation by Progressive Scans (TOPS) acquisition mode [150].


Figure 22. N-S DinSAR results relevant to Big Island of Hawaii, U.S. (a) false colour mean displacement velocity map superimposed on a grey-scale SAR amplitude image of the area. (b-e) Plots of the N-S time-series (black triangles) compared to GPS-driven N-S time-series of displacement (red stars). GPS locations are highlighted in (a). (Adapted with permission from [32], IEEE, 2016).


Figure 23. Maps of E-W (left) and U-D (right) mean displacement velocities in the Shanghai's ocean-reclaimed lands obtained using MinA algorithm. (Adapted with permission from [151], MDPI, 2017).

## 5. Conclusions

This review paper outlines the principal research lines developed over the last twenty years for the development of conventional and advanced InSAR techniques. The basic rationale of InSAR technique has first been provided to let readers have an understanding of the inherent mathematical framework and the state-of-the-art of InSAR methodologies. Emphasis has been put on recently-proposed multi-track InSAR combination methods. Current availability of large archives of SAR data collected by principal RADAR Earth Observation Missions makes the applicability of such integrated approaches largely encouraged. In particular, free of charge- and routinely-available SAR data collected by Sentinel-1A/B sensors' constellation represent a unique opportunity for applying these methods on a global scale. Use of additional data, such as GPS/levelling measurements, will be helpful for better constraining the solution of the multi-track combination methods presented in this work.

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