Fabrication and Simulation of Self-Focusing Field Emission X-ray Tubes

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Abstract: A self-focusing field emission (FE) X-ray tube with a large-area cathode design was simulated and fabricated. The designed X-ray tube had a cylindrically symmetric geometry; the diameter of the cathode and the anode was 15 mm, and the cathode-anode distance was 20 mm. Owing to the unique cup-shaped design of the cathode, the electron beam emitted from the large-area cathode was focused onto the anode without using magnetic lenses or extra biased electrodes. Carbon nanocoils, which were grown on the bottom of the circular cup-shaped cathode, were used as electron emitters because of their excellent FE properties. A simulation of the electron trajectories for various cup heights revealed that the optimal focal spot size (0.1 mm) was obtained at a cup height of 5 mm.
when a voltage of 50 kV was applied. To verify this result, an X-ray tube was fabricated and tested. An X-ray photograph of the tested tooth and electric circuits showed good resolution and X-ray intensity. The large cathode area effectively reduces the current density and thereby improves the lifetime of the cathode.

**Keywords:** X-ray tubes; field emission; carbon nanocoils

1. Introduction

X-ray radiation has long been used in various fields, such as medical diagnosis, industrial applications, material characterization, and scientific research. A traditional X-ray tube comprises a metal filament (hot cathode) and a metal target (anode), which are enclosed in an evacuated glass envelope. The metal filament is heated to over 1000 °C to emit electrons, which are accelerated by an applied electric field to bombard the metal target, generating X-rays [1]. These thermionic emission (TE) X-ray tubes have many limitations. Metal filaments must be heated to a high temperature to boil off electrons, so the response time is long. Moreover, the energy distribution of the emitted electrons from the heated cathode is wide, inhibiting their focusing and the X-ray imaging resolution. Also, the high temperature may lead to evaporation of the filament material or its oxidation by residual gases, reducing its lifetime. The typical lifetime of a TE X-ray tube is less than a year and a large portion of their failures thereof is filament-related.

Field emission (FE) of electrons from the surface of a conductor was proposed by Fowler and Nordheim in 1928 [2]. In FE, electrons are drawn from high-aspect-ratio or low-work-function cathode materials to the vacuum under a high electric field. This phenomenon is used in a variety of applications such as FE display panels [3], backlight units [4], field emission lamps (FELs) [5], and X-ray tubes [6]. FE-type X-ray tubes have many desirable properties. Electrons are extracted from the metal cathode by an applied electric field while the temperature of the emitters is significantly lower than that of the TE filaments. A colder cathode has the benefits of a longer lifetime and a much faster response. The FE current depends on the applied voltage, and the X-ray intensity depends on the FE current. Thus, the X-ray intensity can be conveniently and very rapidly controlled by varying the cathode voltage. Many researchers have worked on the design and fabrication of FE X-ray tubes [7,8].

The typical FE X-ray tubes may comprise three parts, which are an FE cathode grown with electron emitters, an anode (metal target), and a gate electrode. Also, magnetic lenses or extra biased focusing electrodes can be used to focus the electrons onto the anode. Since nano-materials were discovered, carbon nanotubes (CNTs) [9–11], carbon nano-coils (CNCs) [12–15], and CNTs decorated with nanodiamonds [16] have been identified as excellent FE cathode materials because of their high aspect ratio, good thermal stability, and good mechanical strength. The extremely high aspect ratios of CNTs and CNCs give rise to a large field enhancement factor, β [17], which makes them excellent field emitters with low turn-on fields. Researchers have found that CNCs exhibit several advantages over CNTs, including better long-term current emission stability, higher current density, and longer operation lifetime [18,19].
The resolution of an X-ray image depends on the spot size of the electron beam on the anode. To minimize the spot size, a focusing electrode [20] is commonly used, but its use requires an extra bias circuit and results in a more complicated tube design. In this research, a simple diode-type FE X-ray tube is designed and focusing is achieved without resorting to magnetic lenses or active focusing electrodes.

2. Simulation Methodology, Material, and the Experiments

This section will firstly introduce the simulation methodology, and then describe the material properties of CNCs and the process of their fabrication.

2.1. Finite Element Method (FEM)

The FEM was employed in the simulation to calculate the electric field strength. The FEM is a numerical technique for finding approximate solutions to boundary value problems for differential equations. First, the problem domain is divided into finite elements, as shown in Figure 1, and each element is represented by a set of element equations to the original problem. To make the final calculation, all element equations are systematically recombined into a global system of equations, which can be numerically solved by known techniques from the initial values in the original problem.

**Figure 1.** X-ray tube divided into finite elements for electric field calculations. Red and blue parts are anode and cathode, respectively.

The FEM is the preferred method in structural mechanical analysis. In this study, the FEM is a suitable tool for obtaining a numerical solution for the spatial distribution of the electric field between the cathode and the anode.

2.2. Field Emission Theory

FE refers to the quantum-mechanical phenomenon of electron tunneling from a conductor into the vacuum through a surface potential barrier whose width is significantly reduced by a high local electric field [21–25]. The tunneling probability depends very strongly on the width of the potential barrier and decreases exponentially with increasing barrier width. The local electric field can be orders
of magnitude greater than the applied macroscopic field, owing to the enhancement effect at sharp tips or edges.

The FE current \( I \) can be calculated from the quantum-mechanical tunneling probability of electrons through a triangular potential barrier, and the result is the well-known Fowler-Nordheim (F-N) equation:

\[
I = \alpha A (\beta^2 E^2 / \phi) \exp(-b\phi^{3/2} / \beta E)
\]

where \( \alpha \) and \( b \) are constants; \( A \) is the effective FE area; \( E, \phi, \) and \( \beta \) are the applied macroscopic electric field (without the local microscopic geometrical effect that causes enhancement), the material work function, and the field enhancement factor, respectively. The value of \( \beta \) depends on the microscopic geometry of the emitters and is the most important factor that affects the FE performance. Nanomaterials with enormously high aspect ratios, such as CNCs and CNTs, are known to have very high \( \beta \), and have been demonstrated to be excellent field emitters with low turn-on \( E \) fields \([21–25]\).

The value of \( \beta \) can be extracted from the experimentally obtained slope of the F-N plot.

To obtain the macroscopic electric field \( E \), which determines the FE current density, Poisson’s equation was firstly solved numerically for the potential distribution \( V(x, y, z) \) using the FEM. The electric field distribution is then calculated by differentiation:

\[
\vec{E} = -\nabla V
\]

In this work, three different kinds of software packages were used in the simulation; they were (1) SolidWorks® (Dassault Systèmes SolidWorks Corp., Waltham, MA, USA), which was used to define a precise device geometry; (2) Comsol Multiphysics (Comsol Inc., Stockholm, Sweden), which was used to calculate the distribution of the electric field on the designed cathode surface; and (3) Simion 8.0 (Scientific Instrument Services, Inc., Ringoes, NJ, USA), which simulated the trajectory of the emitted electrons that were accelerated by the electric field between the cathode and the anode.

2.3. CNCs as Electron Emitting Nanomaterial

The unique properties of carbon nanomaterials, such as their high thermal conductivity, low work function, and excellent electron migration rate, make them promising FE emitters. CNTs have received much attention since their discovery by Iijima \([26–32]\). An advantage of CNTs in FE is that they are natural field-enhancing objects because of their high aspect ratio.

CNCs \([13–16,33–37]\) are nanocarbon materials with a coiled structure and are composed of nanometer-scale fibers. Compared with CNTs, CNCs have considerably more electron emission sites—not only at the tips but also at the numerous nanocrystallites embedded in the amorphous carbon body. Additionally, CNCs are more robust than CNTs because the former are much thicker and thus can withstand a higher current density. Owing to their much larger diameter and higher FE site density, CNCs exhibit better long-term current emission stability, current density, FE efficiency, and lifetime than CNTs \([18,19]\), and so they have already found application in FE lighting \([38–41]\). Consequently, CNCs are used as the emitter material in the X-ray tube in this work.

CNCs are generally synthesized by catalytic thermal chemical vapor deposition (TCVD) or arc discharge. Since CVD can be used in the low-cost, large-scale commercial synthesis of CNCs, it was utilized to synthesize the CNCs herein.
The substrates that were used herein for the synthesis of CNC cathodes were 304 stainless steel circular disks with a diameter of 15 mm. Each substrate was firstly cleaned with acetone, ultrasonicated for 10 min, and subsequently washed in deionized water. To expose the bare metal surface, each stainless steel substrate was then immersed in 10%–37% HCl for 3–10 min and rinsed again with deionized water. Before TCVD, Pd catalysts were deposited onto the substrates through chemical displacement in a 100–800 ppm PdCl₂ solution of pH 1.6–1.8 at 80 °C for 10 min. After the reaction was complete, the cathodes were rinsed with deionized water and dried with N₂ gas. The prepared cathodes were placed in a TCVD furnace and the pressure was pumped down to 10⁻² Torr. The temperature was gradually increased to 600 °C at a rate of 20 °C/min in an atmosphere of H₂ and Ar. The flow rates for H₂ and Ar were 10 and 100 sccm, respectively. When the temperature reached 600 °C, the Ar gas was evacuated and the H₂ flow rate was increased to 20 sccm to pretreat the Pd catalysts for 5 min. Next, to grow the CNCs, C₂H₂ gas was fed at a flow rate of 5 sccm for 20 min while the furnace temperature was maintained at 600 °C.

The morphologies of the CNCs were examined using a transmission electron microscope (TEM, model: Tecnai F30, FEI, Hillsboro, OR, USA) and a field emission scanning electron microscope (FE-SEM, model: JEOL JSM-7600F, Japan Electron Optic Laboratory Co., Ltd., Tokyo, Japan). Their graphite crystallinity was analyzed using Raman spectroscopy.

3. Results and Discussion

3.1. Simulation of the Self-Focusing Cathode Design

Figure 2 displays the geometry of the X-ray tube for simulation. The red part is the anode, which has a diameter of 15 mm and is biased at an applied voltage of 50 kV; the blue part is the metallic cup for electrostatic focusing which has a diameter of 15 mm with a 12-mm-diameter aperture on the top to focus the emitted electrons. The CNC FE cathode disk (not shown) was situated at the bottom of the metallic cup. The whole cathode (CNC FE disk and cup) was grounded. The distance from the electron emitters to the anode was fixed at 20 mm, and the cup height was varied to minimize the size of the focal spot on the anode.

Figure 2. Geometry of the X-ray tube in SolidWorks. Red and blue parts are anode and cup-shaped cathode, respectively. CNC FE disk (diameter = 15 mm) is at the bottom of focusing cup; a 12-mm-diameter aperture is at the top of cup.
In the design herein, the electron-emitting area was quite large. This was advantageous because it would greatly reduce the average current density if the total FE current was fixed, resulting in a longer lifetime of the CNC emitters.

The electrostatic potential distribution and, hence, the electric field distribution were then calculated using Comsol Multiphysics. Finally, the trajectories of the emitted electrons accelerated by the Coulomb force were simulated using Simion 8.0. The calculated trajectories are shown in Figure 3.

![Figure 3. Trajectories of emitted electrons (a) without and (b) with focusing cup design. Vertical axis in (b) represents electric potential $V$.](image)

Figure 3a presents the simulation results for an X-ray tube without the focusing cup; electrons are dragged by the applied voltage in straight trajectories to bombard the anode. In contrast, in Figure 3b, the trajectories of the electrons emitted from a cup-shaped cathode clearly converged onto a small focal spot. After testing with various heights of the cup-shaped cathode, the optimal cup height was about 5 mm, which yielded the smallest focal spot size of 0.1 mm (diameter). Figure 4 shows the three-dimensional (3D) electron trajectories in the X-ray tube with a 5-mm-high focusing cup.

![Figure 4. Three-dimensional (3D) diagram of electron trajectories in the X-ray tube with a 5-mm-high focusing cup.](image)

Note that the focusing cup is maintained at the same voltage as the CNC FE disk. Thus, no extra bias circuit is needed, and the structure and fabrication of such an X-ray tube are simple.
To understand why this simple design offered such a good focusing effect for a large-area cathode, Figure 5 shows the electric field distribution on the CNC FE disk (a) without and (b) with the focusing cup design. Comparing Figure 5a with b, the metallic cup wall clearly has a strong shielding effect: the electric field strength near the disk edge was reduced from $9.5 \times 10^5$ V/m (center) to below $1.2 \times 10^5$ V/m. In contrast, the electric field without the focusing cup was nearly constant everywhere on the CNC FE disk. This shielding effect forced the electric field lines within the cup to converge towards the central axis, so the electrons were guided by this field distribution and focused onto the anode.

![Electric field distribution](image)

**Figure 5.** Calculated electric field strength on the surface of CNC FE disk (a) without and (b) with focusing cup design.

### 3.2. Characterization of the Synthesized CNCs

Figure 6 (secondary electron image) displays a scanning electron micrograph (SEM) of the CNCs grown on the stainless steel disk. The pitch and diameter of the CNCs are both approximately 0.1–0.2 μm.

![SEM micrographs](image)

**Figure 6.** SEM micrographs of carbon-nanocoils at (a) low magnification and (b) high magnification.
A TEM image of the CNCs synthesized at 600 °C is shown in the inset of Figure 7. The CNCs synthesized at this temperature had a diameter of around 100 nm and an amorphous structure. A Pd catalyst particle was observed in the micrograph (the red circle). Also shown in Figure 7 is the energy dispersive X-ray (EDX) spectrum that was obtained within the red circle to reveal the chemical composition of the catalyst particle (The Cu signal came from the Cu grid supporting the CNC samples for TEM analysis).

![TEM image of CNCs and EDX spectrum](image1)

**Figure 7.** TEM image of CNCs (inset) and EDX spectrum taken within the red circle, which contained one Pd catalyst particle.

Figure 8 shows the Raman spectrum of the synthesized CNCs. The D-band at around 1350 cm\(^{-1}\) and the G-band at 1580 cm\(^{-1}\) are clearly seen; they are related to the structural defects and the graphite lattice, respectively, in carbonaceous materials. The intensity ratio \(I_D/I_G\), which is an indicator of the crystallinity of carbon materials, is 0.78. This number is similar to those obtained for the CNCs in previous studies [39,42].

![Raman spectrum](image2)

**Figure 8.** Raman spectrum of as-grown CNC film.
3.3. Test of X-Ray Tube

To validate the device simulation herein, an X-ray tube with the designated geometry and dimensions (a 20 mm cathode-anode separation; a 15 mm diameter; a 5 mm focusing cup height; and a Cu anode) was constructed and tested. The focal spot size was estimated experimentally to be roughly \( \leq 0.8 \) mm. The deviation from the optimal simulation result might be attributed to the slightly different electric field distribution in the real device with the tilted anode, as shown in Figure 9, or to the non-ideal alignment of the anode relative to the cathode. The most important applications of X-rays are the nondestructive inspection of electronic devices and medical diagnosis. To demonstrate the good resolution of the cathode design herein, X-ray images of a fine test circuit board and a human tooth (Figure 10) were obtained using our X-ray tube at 50 kV. The FE current was 0.076 mA at 50 kV. The image was taken using a film placed behind the objects, which were irradiated by the X-ray tube. The sample to be analyzed was placed in the direction perpendicular to the cathode-anode axis (i.e., to the right side of the anode in Figure 9). The source-to-sample and sample-to-film distances were 10 and 20 cm, respectively. The film used for the imaging was Kodak Dental Intraoral D-Speed (Kodak, Rochester, NY, USA), and the exposure time was determined by adjusting the mAs for a gross optical density of about 1.5 on a portion of the film that was not covered by the test pattern. As shown in Figure 10, the fine structures of the test circuit board and the tooth were clearly resolved using our X-ray tube. The image quality is likely to be similar to that achieved by the conventional X-ray imaging technique, as judged by the fine details in the image of the reference phantom.

Figure 9. Photograph of the anode and cathode geometry in our X-ray tube; the anode material is Cu.

Figure 10. X-ray image of a circuit board and a tooth captured using the self-focusing X-ray tube.
4. Conclusions

A self-focusing cathode with an auxiliary metallic cup was developed for use in an X-ray tube. The design was both simulated and fabricated. CNCs were chosen as electron emitters because they have a higher long-term stability, longer lifetime, higher FE currents, and more emission sites than CNTs. A disk-shaped stainless steel substrate was deposited with CNCs and placed at the bottom of the cup as the electron source. A planar copper anode was also used. The diameters for the anode and the CNC FE disk were both 15 mm, and the aperture on the top of the cup had a diameter of 12 mm. The primary advantages of the cup-shaped cathode were the large emitting area, the self-focusing of emitting electrons, the simplicity of the structure and the bias circuit, and the ease of fabrication. The simulation results revealed that at a cup height of 5 mm, the optimum focal spot size was about 0.1 mm. An X-ray tube with the designed geometry and dimensions was constructed and tested. The experimental results verified the good imaging performance of this design. The good resolution of the captured image of a fine test circuit and a tooth suggested the practical usefulness of the design.

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Author Contributions

Yih-Ming Liu and Ming-Der Ger conceived and designed the experiments; Kevin Cheng performed the experiments; Yi-Ping Chou and Kung-Hsu Hou analyzed the data; Meng-Jey Youh contributed reagents/materials/analysis tools; Nen-Wen Pu wrote the paper.

Conflicts of Interest

The authors declare no conflict of interest.

References


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