



Article An Intelligent Diagnostic Method for Wear Depth of Sliding Bearings Based on MGCNN

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Abstract: Sliding bearings are vital components in modern industry, exerting a crucial influence on equipment performance, with wear being one of their primary failure modes. In addressing the issue of wear diagnosis in sliding bearings, this paper proposes an intelligent diagnostic method based on a multiscale gated convolutional neural network (MGCNN). The proposed method allows for the quantitative inference of the maximum wear depth (MWD) of sliding bearings based on online vibration signals. The constructed model adopts a dual-path parallel structure in both the time and frequency domains to process bearing vibration signals, ensuring the integrity of information transmission through residual network connections. In particular, a multiscale gated convolution (MGC) module is constructed, which utilizes convolutional network layers to extract features from sample sequences. This module incorporates multiple scale channels, including long-term, medium-term, and short-term cycles, to fully extract information from vibration signals. Furthermore, gated units are employed to adaptively assign weights to feature vectors, enabling control of information flow direction. Experimental results demonstrate that the proposed method outperforms the traditional CNN model and shallow machine learning model, offering promising support for equipment condition monitoring and predictive maintenance.

Keywords: sliding bearing; wear depth; intelligent diagnosis; multiscale model

1. Introduction

Bearings are fundamental components of modern industry and are crucial for the development of a country's heavy industry, earning them the nickname the "joints" of mechanical equipment. Their primary function is to support rotating mechanical bodies, reducing the coefficient of friction during their motion, and thus, they are widely applied in rotary machinery. Bearings can be roughly divided into two types based on their working principles: rolling bearings and sliding bearings. Among these, sliding bearings are mechanical elements that support rotating components using the principle of sliding friction and allow for relative sliding between the loading surfaces [1]. Their advantages include a compact structure, requiring minimal installation space, and high rotational accuracy. Moreover, since they do not rely on rolling, they experience less inertial force at high rotational speeds, resulting in smoother and more reliable operation with lower noise compared with rolling bearings [2]. This makes them indispensable in applications where high precision is required, radial dimensions are small, and lubrication is difficult to apply. As a result, sliding bearings are extensively used in aerospace, shipbuilding, automotive, high-speed railway transportation, precision machine tools, agricultural machinery, and other fields, becoming one of the core components of modern mechanical equipment [3].

As modern machinery evolves towards complexity, precision, and high-speed operation, the conditions under which bearings operate have become more demanding [4,5]. Due to relative sliding between the loading surfaces, bearings may experience wear and degradation under radial loading, potentially leading to excessive shaft eccentricity, fluid



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Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). leaks, and interference between internal components [6]. Once a certain level of wear accumulates, it can result in the partial or complete loss of function of sliding bearings, affecting the safety and stability of the entire unit. For some heavy-duty equipment, the wear failure of sliding bearings can cause immeasurable economic losses and catastrophic events. Therefore, monitoring and predicting the wear state of sliding bearings during operation is of great significance [7].

There is currently a large amount of research on the state monitoring and prediction of components such as rolling bearings and machine tools, with numerous public datasets of mechanical product failures available worldwide for use [8–10]. Vencl et al. [11] systematically classified the wear failure of roller bearings, and established a fault tree for wear failure analysis. Li et al. [12] extracted a two-dimensional time-frequency image from the vibration signals of rolling bearings using a short-time Fourier transform and input it into a convolutional neural network for fault classification. Han et al. [13] proposed a rotary machinery fault diagnosis framework based on deep transfer learning. Wang et al. [14] used a relevance vector machine (RVM) to extract degradation features from the vibration signals of rolling bearings and fit an empirical exponential model to predict the remaining useful life (RUL) of rolling bearings. Zhu et al. [15] employed a superposed log-linear proportional intensity model to model and evaluate the reliability of incompletely maintained machine tools, quantitatively assessing the impact of maintenance activities on machine tool reliability. Wang et al. [16] conducted fault probability analysis on a disk-type tool magazine using Bayesian networks. SKF intelligent bearings are connected to external sensors to monitor and even control the entire operation of the bearings [17]. Alexander and Evgeny [18] studied the thermal analysis of bearing assemblies based on FEM and developed a methodological basis for implementing automatic diagnostics. Baron et al. [19] conducted diagnosis and analysis for bearings from the CNC machining center based on various vibrodiagnostic methods. In summary, existing intelligent diagnostic methods extract features from monitoring data and input them into classifiers or regressors for fault diagnosis or useful life prediction.

For sliding bearings, current research mainly focuses on issues such as rotor stability [20–27], calculation of oil film stiffness and damping [28–31], as well as material wear resistance performance [32–34], aiming to enhance the lubrication performance and wear resistance of bearings at the design stage. Although improving the lubrication performance and wear resistance of sliding bearings can effectively alleviate material wear problems, wear is inevitable during equipment startup, shutdown stages, and under the influence of some unexpected factors [35]. Some scholars use numerical models to simulate and predict the wear behavior of bearings. Jeon et al. [36] used a typical journal wear test to statically predict the wear of the joint bearing. König et al. [37] predicted the macroscopic wear amount of sliding bearings based on the Archard model and Fleischer model. Dai and Tian [38] introduced a sequential hybrid model of neural network and finite element for predicting wear in sliding bearings. In general, these methods simulate and predict bearing wear based on static conditions and cannot integrate with online data. Therefore, implementing real-time diagnosis and quantitative evaluation of the wear state during the operation of sliding bearings, and subsequently performing predictive maintenance, is of significant importance for enhancing equipment safety and reducing maintenance costs.

From a structural standpoint, sliding bearings and rolling bearings exhibit significant differences. The latter typically consists of components such as inner and outer rings, cages, and rollers, making their structure comparatively complex [39], while sliding bearings are characterized by a simpler structure, usually comprising a shaft journal and bearing, sometimes with coatings in certain scenarios. This disparity results in the vibration signals during the degradation process of sliding bearings being less pronounced compared with rolling bearings. Consequently, the data characteristics of status detection signals differ considerably between the two types of bearings. Currently, there is a scarcity of online diagnostic methods specifically tailored to sliding bearings, and there is also a lack of widely accepted data concerning the failure lifecycle of sliding bearings. Therefore, focusing on the

diagnosis and prognosis of sliding bearings, it is still necessary to conduct experiments on and analyses of monitoring data to develop practical and feasible wear diagnostic methods.

Since the maximum wear depth (MWD) of a sliding bearing is equivalent to the clearance of a shaft bearing, this paper uses MWD as a quantitative indicator for assessing the bearing's wear condition and proposes an intelligent diagnostic method based on a multiscale gated convolutional neural network (MGCNN), which can be trained and inferred based on online vibration signals of bearings and can quantitatively evaluate the MWD of bearings to characterize their current wear state. The contributions of this work are summarized as follows:

- 1. Different from the current research focus on the lubrication and antiwear performance of sliding bearings, this paper aims to dynamically diagnose and quantitatively evaluate the wear state during the operation of bearings. In typical situations, MWD directly impacts bearing performance, yet is often challenging to measure directly in real time. Conversely, vibration signals can be continuously collected through external sensors. Leveraging the vibration signals collected during the operation of sliding bearings, this paper proposes an end-to-end approach to infer the MWD affecting bearing performance, enabling the diagnosis of bearing conditions. This bridges a gap in the current research landscape of sliding bearings by providing an intelligent diagnostic method.
- 2. An MGCNN intelligent diagnostic model is constructed, with vibration signals as input and the bearing's MWD as output. Considering the periodic characteristics of rotating machinery, the established MGCNN model adopts a dual-path parallel structure in both time-domain and frequency-domain to fully extract valid information from bearing vibration signals, thereby enhancing the model's prior knowledge. The MGC module is designed, which utilizes three channels for long-term, mediumterm, and short-term cycles to extract multiscale information from vibration signals; meanwhile, gated units are designed to assign weights to feature vectors through non-linear mappings. By amplifying the weights of important features and disregarding unimportant ones, the control of information flow is achieved.
- 3. Building upon the diagnostic results of the proposed method, this paper further conducts predictive maintenance for sliding bearings. By setting a predefined wear threshold, this paper determines a bearing's remaining useful life, facilitating predictive maintenance for bearings and equipment.

The remainder of this paper is organized as follows. Section 2 describes the bearing wear problem and introduces the related deep learning theories and foundations; Section 3 introduces the proposed MGCNN model; Section 4 presents the bearing wear test and validates, analyzes, and discusses the proposed model; Section 5 provides the conclusions of this work and discussions on future work.

2. Bearing Vibration Signals and Deep Neural Networks

2.1. Wear State and Diagnosis of Sliding Bearing

As shown in Figure 1a, the common assembly form of sliding bearings is the rotor– bearing fit, where the rotor rotates under the support of sliding bearings. The surface of the shaft contacts and slides relative to the inner surface of the bearing. Since the rotor is often subjected to a radial load F and shaft rotation, the inner surface of the bearing is prone to wear in a fixed direction. The wear of the bearing's inner surface results in an abnormal clearance D between the shaft and the bearing. As shown in Figure 1b, the rotor is considered as an eccentric mass block and the sliding bearing as a spring-damping support, and the abnormal clearance caused by bearing wear leads to abnormal vibration during rotor rotation. Moreover, the vibration signal is directly related to the size of the clearance D. It is worth noting that because the bearing load-bearing surface is an arc, the wear depth at each node is not uniform, and the clearance D is equal to the maximum wear depth (MWD). In actual systems, vibration signals can be collected by deploying sensors on the equipment surface, while the bearing wear depth is difficult to measure online. Therefore, this paper focuses on the research of sliding bearing wear diagnosis, establishes an intelligent diagnostic model, and infers the current maximum wear depth of the bearing based on the vibration signals collected from the worn sliding bearing.

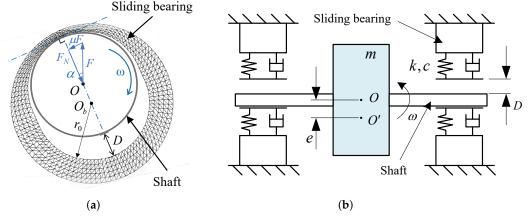


Figure 1. (a) Rotor–bearing contact, where ω is the rotational speed, O_b is the center of the bearing, O is the geometric center of rotor, μ is the surface friction coefficient, r_0 is the original radius of bearing inner surface, and F_n is the normal pressure; (b) dynamic system of the rotor–bearing, where *m* is the mass of rotor and O is the geometric center of the rotor, while O' is the center of mass, e = |OO'| represents the eccentricity, and *k* and *c* are the equivalent stiffness and damping, respectively.

2.2. Sample Cutting and Preprocessing

When the vibration signal x of a bearing is collected over a period of time, data preprocessing is performed first, as shown in Figure 2. The purpose of data augmentation is to increase the diversity of the dataset [40], allowing the model to better learn the various variations and complexities of the data during training, thereby enhancing the model's generalization ability and robustness.

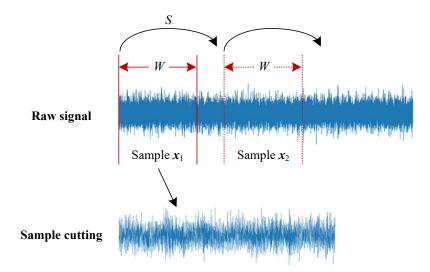


Figure 2. The process of sample cutting.

In practical applications, data augmentation is commonly regarded as an effective strategy to improve the performance of deep learning models. For the original vibration signal $x_t = [x_1 \ x_2 \ \cdots \ x_L]$, specifying a sample length W and a stride S, we obtain several shorter samples x_1, x_2, \cdots, x_n by slicing the raw signal. By reducing the sample length and increasing the number of samples, we provide more comprehensive training for

the neural network, where the number of samples is n = mod(len(x) - L, S), and $mod(\cdot)$ represents the modulo operator. The obtained new samples are as follows:

$$\mathbf{x}_i = \left[\begin{array}{ccc} x_{1+(i-1)S} & x_{2+(i-1)S} & \cdots & x_{W+(i-1)S} \end{array} \right]$$
(1)

Additionally, this paper involves the deliberate addition of noise to the raw data, enabling the model to learn features that more accurately represent bearing degradation information. Related experiments and discussions are conducted in Section 4.4. The process of adding noise is as follows:

$$=x_i+\epsilon$$
 (2)

where x_i is the raw sample, and ϵ is the noise. This paper employs Gaussian white noise $\epsilon \sim \mathcal{N}(0, \sigma^2)$, where ϵ follows a normal distribution with a mean of 0 and a variance of σ^2 . The hyperparameter σ determines the intensity of the noise.

 \hat{x}_i

It is worth mentioning that in time series analysis problems, multiscale entropy (MSE) is commonly used to quantify the complexity of time series [41]. Ref. [42] explored the linear correlation between multiscale permutation entropy (MPE) and multiscale weighted permutation entropy (MWPE) using the slope of linear regression as a discriminant statistic. Building on this, Ref. [43] investigated the effects of the optimal parameters of nonuniform embedding. In this paper, the diagnostic task is abstracted as a regression problem rather than a pure time series prediction problem, meaning it focuses on outputting evaluation metrics based on input vectors. Therefore, the current work does not delve deeply into the complexity of vibration signal time series. Integrating time series analysis techniques will be a potential research point in future work.

2.3. Convolutional Neural Network

After obtaining samples through data preprocessing, this paper uses convolutional neural network layers to extract features from sample sequences, where convolutional kernels are used to perform convolution operations on local regions of the input signal [44], obtaining the corresponding features, as shown in Figure 3. For bearing condition data, taking vibration signals as an example, they are one-dimensional vectors containing several elements. The weight sharing in the convolutional layer allows a single convolutional kernel to traverse the entire input vector, effectively reducing the scale of network parameters. Generally, the size of a convolutional kernel is the depth $c_{\text{conv}} *$ width $l_{\text{conv}} *$ height h_{conv} , where the depth is consistent with the number of channels of the input data; for one-dimensional vibration signals, the height h_{conv} is 1, so the size is $c_{\text{conv}} \times l_{\text{conv}}$. Therefore, a convolutional kernel can be represented as follows:

$$\mathbf{K} = \begin{bmatrix} k_1^{(1)} & k_2^{(1)} & \cdots & k_l^{(1)} \\ k_1^{(2)} & k_2^{(2)} & \cdots & k_l^{(2)} \\ \vdots & \vdots & \ddots & \vdots \\ k_1^{(c)} & k_2^{(c)} & \cdots & k_l^{(c)} \end{bmatrix}$$
(3)

Using the convolutional kernel K to perform a sliding convolution over the sequence samples, the feature y obtained from a single channel in a single convolution is as follows [44]:

$$y_i = \sum_{m=1}^c \sum_{n=1}^l k_n^{(m)} x_n^{(m)}$$
(4)

where $x_n^{(m)}$ is the *n*th element of the *m*th channel in the current convolutional region.

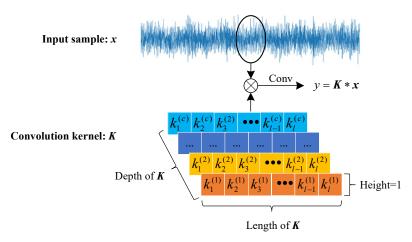


Figure 3. The process of convolution. The symbol (*) represents convolution operation, and the different colors represent parameters at different depths of the convolution kernel.

After convolution, the samples typically undergo pooling processing, which serves to suppress noise, reduce computational complexity, and prevent overfitting, among other functions. Common pooling operations include max pooling and average pooling, which use the mean and maximum values within the pooling filter region as the pooling output, respectively. Due to the symmetry typically found in vibration signals in the time domain, using average pooling might result in features close to zero after pooling, leading to ineffective features. Therefore, this paper employs max pooling [44], which is defined as follows:

$$y_{ij} = \max_{x_k \in R_{ii}} x_k \tag{5}$$

where R_{ij} represents the region of influence of the pooling filter. Figure 4 illustrates the max pooling process for one-dimensional samples, with a pooling filter size of 2 × 1 and a stride of 2.

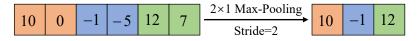


Figure 4. The process of max pooling. The different colors represent different pooling regions.

After the samples have undergone convolution or pooling, an activation function is applied to the convolutional output to perform a nonlinear transformation. According to reference [45], commonly used activation functions include the Sigmoid function (Equation (6)), the Tanh function (Equation (7)), and the ReLU function (Equation (8)):

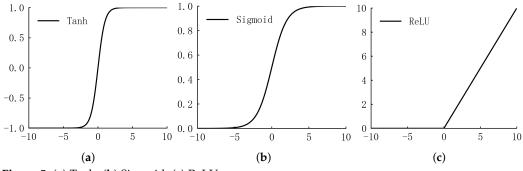
$$f_{\text{Sigmoid}}(y) = \frac{1}{1 + e^{-y}} \tag{6}$$

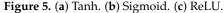
$$f_{\text{Tanh}}(y) = \frac{e^{y} - e^{-y}}{e^{y} + e^{-y}}$$
(7)

$$f_{\text{ReLU}}(y) = \max(y, 0) \tag{8}$$

The curves corresponding to the three activation functions are shown in Figure 5. Due to the fact that deep neural networks update network weights through the backpropagation algorithm by transferring gradients layer by layer, for the Sigmoid and Tanh functions, when the absolute value of the input is large, the curve will saturate, and the gradient will approach 0. As the number of layers in the neural network increases, these smaller gradients will gradually propagate through each layer, eventually leading to slow or stagnant parameter updates in the deep network. This prevents the network from fully learning complex features, thus affecting the convergence and output performance of

the model, a phenomenon known as gradient vanishing [46,47]. Therefore, this paper adopts the ReLU activation function, which has a gradient of 1 for positive inputs, helping to alleviate the gradient vanishing problem and allowing the proposed neural network structure to be trained more effectively.





2.4. Fully Connected Neural Network

The Universal Approximation Theorem [48,49] states that a feedforward neural network with a linear output layer and at least one hidden layer with any kind of "squashing" activation function can approximate any Borel measurable function from one finitedimensional space to another with arbitrary precision, provided that the network has enough hidden units. Therefore, this paper selects the fully connected neural network as the output module of the proposed method model, also named Multilayer Perceptron (MLP).

The basic structure of a fully connected neural network is shown in Figure 6, where each neuron in the *i*th layer is connected to every neuron in the (i + 1)th layer. The mathematical expression for this is [45]

$$x^{[i+1]} = f_{\text{act}}(\sum_{j} w_{j}^{[i]} x_{j}^{[i]} + b^{[i+1]})$$
(9)

where f_{act} is a nonlinear activation function. If no activation function is added, the fully connected neural network can only express linear models. Here, the ReLU function shown in Equation (8) is also adopted.

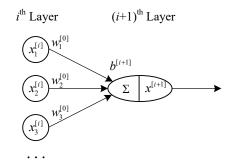


Figure 6. Structure of the neuron.

In terms of model training, neural networks use the error backpropagation algorithm to calculate the derivatives of the loss function concerning the model parameters and update the parameters to minimize the loss function. For cases where the dataset is small or the model parameter space is limited, Stochastic Gradient Descent (SGD) [50] can converge to the global optimum. However, in high-dimensional parameter spaces and with complex loss functions, the Adam optimizer (Adaptive Moment Estimation) [51] often requires fewer hyperparameter adjustments and exhibits better convergence performance. Considering the multimodule coupling of the proposed intelligent diagnostic method and

the complexity of the network units, this paper uses the Adam method to optimize the established deep learning model, as shown in Algorithm 1.

Algorithm 1 Adam [51]

Require: Stepsize: α ; exponential decay rates for the moment estimates: $\beta_1, \beta_2 \in [0, 1)$; constant $\epsilon = 10^{-8}$; model parameters: θ ;

Initialize 1st moment vector: $m_0 = 0$; 2nd moment vector: $v_0 = 0$, and timestep: t = 0**Ensure:** Optimised parameters: θ_t

1: while θ_t not converged **do**

- 2: $t \leftarrow t + 1$
- 3: $g_t \leftarrow \nabla_{\theta} L(\theta_{t-1})$, where $L(\theta)$ is the objective function with parameters θ

4: $m_t \leftarrow \beta_1 \cdot m_{t-1} + (1-\beta_1) \cdot g_t$

5: $v_t \leftarrow \beta_2 \cdot v_{t-1} + (1 - \beta_2) \cdot g_t \odot g_t$, where \odot represents element-wise multiplication of vectors.

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6: \hat{m}_t \leftarrow m_t / (1 - \beta_1^t)
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7: \hat{v}_t \leftarrow v_t / (1 - \boldsymbol{\beta}_2^t)
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8: \boldsymbol{\theta}_t \leftarrow \boldsymbol{\theta}_{t-1} - \alpha \cdot \boldsymbol{\theta}_t / (\hat{\boldsymbol{v}}_t + \boldsymbol{\epsilon})
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```
9: end while
```

3. Multiscale Gated Convolutional Neural Network

3.1. Overall Structure of the MGCNN

The proposed method for sliding bearing wear diagnosis based on the multiscale gated convolutional neural network (MGCNN) is shown in Figure 7. The original vibration signals are subjected to data augmentation, and after sample cutting, they are input into MGCNN for feature extraction and regression fitting. Due to the rotational periodicity of rotating machinery, the vibration signals also contain rich degradation fault information in the frequency domain. Therefore, in addition to directly extracting features from the time-domain signals, a Fourier transform [52] is applied to the time-domain signals to obtain the frequency-domain signals:

$$x_{\mathbf{f},j} = \left\| \sum_{k=1}^{m} x_{\mathbf{t},k} e^{-i\frac{2\pi}{m}j(k-1)} \right\|, \quad k = 1, 2, \cdots m$$
(10)

Features are extracted from the frequency-domain signals using neural networks to capture the frequency-domain information. Consequently, the structure of the training data is $\{(x_t, x_f), D_{label}\}$, where D_{label} represents the true value of maximum wear depth, which is the data label.

The MGCNN includes time-domain and frequency-domain pathways, each with two levels of multiscale gated convolution (MGC) modules to extract features from their respective domains. The feature maps obtained from the MGC modules are concatenated along the channel direction, and the output of the 1st-MGC passes through a ReLU activation function before entering the 2nd-MGC. Since the original vibration signal is a one-dimensional vector, the input channel number for the 1st-MGC module is 1, while the input channel number for the 2nd-MGC module equals the output channel number of 1st-MGC. Every time the data pass through an MGC, the feature length is reduced to 1/8 of its original size. Since the signal undergoes a Fourier transformation at the outset on the frequency domain path, the feature length is always half that of the corresponding position on the time–frequency path. Finally, the feature maps are flattened and input into the MLP for regression fitting to obtain the maximum wear depth.

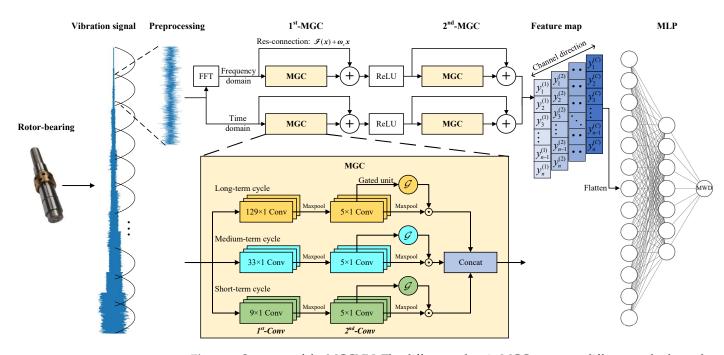


Figure 7. Structure of the MGCNN. The different colors in MGC represent different cycle channels.

In theory, if a neural network with fewer layers has already achieved a high level of accuracy, then adding more layers should result in a network that is at least as accurate as the original. This is because, if the added layers are identity transformations, the output accuracy of the network before and after the addition should be the same; moreover, the additional layers should, in principle, be trainable to perform even better. However, in practice, deep neural networks exhibit a phenomenon known as "degradation", where, as the network depth increases beyond a certain point, the model's accuracy unexpectedly and significantly decreases [53].

A qualitative analysis of the reasons behind this phenomenon reveals significant differences between deep learning and traditional machine learning, particularly in terms of deeper network structures, the application of nonlinear activation functions, and the automated process of feature extraction and transformation. In deep learning, the introduction of nonlinear activation functions is crucial as it allows data to be mapped into higher-dimensional spaces, facilitating better classification and regression. However, as the number of network layers increases, so does the number of introduced nonlinear activation functions, leading to the mapping of data into more complex nonlinear spaces. Due to the complexity of this mapping, it becomes very difficult to restore the data to their original space (i.e., to perform an identity transformation). In other words, the neural network requires a considerable amount of computation to remap the data back to their original space, which may exceed the computational capabilities supported by the current data and hardware resources.

To address this issue, the MGCNN adopts a residual neural network structure [54]. In the constructed neural network model, residual connections are placed at both ends of each MGC module to ensure the integrity of data information transmission. By introducing residual connections between the input and output of the neural layers, the output of the neural layer is no longer a direct feature mapping but a residual of the input, i.e., the difference between the layer's input and output. This type of connection allows the network to more easily learn identity mappings, thereby simplifying the optimization of deep networks. For a stacked-layer neural network, the output of layer *l* is $x_l = F(x_{l-1})$; however, the output of a residual unit is

$$\mathbf{x}_l = \mathscr{F}(\mathbf{x}_{l-1}) + \boldsymbol{\omega}_s \mathbf{x}_{l-1} \tag{11}$$

where ω_s represents the transformation parameters to maintain the same shape between $w_s x_{l-1}$ and $F(x_{l-1})$; specifically, in this paper, ω_s is achieved using 1×1 convolutional kernels with certain strides. This allows the stacked layer to act as an identity transformation when $F(x_{l-1}) = 0$, ensuring that the network's performance does not decrease with the addition of this stacking layer.

In this paper, the Dropout technique is used in MLP to improve the model's generalization ability [55]. During the network training process, Dropout randomly sets the output of neurons to zero with a certain probability to prevent certain parts of the network from being overly dependent on specific samples. This reduces the coupling between neurons in the neural network, making the network sparser and thereby reducing overfitting.

3.2. Structure of the MGC Module

To fully extract the multiscale periodic information from bearing vibration signals, the MGC module sets up three channels in parallel: a long-term cycle, a medium-term cycle, and a short-term cycle. These channels achieve multiscale periodic feature extraction through convolutional kernels of different lengths. For machine learning models, more complex models often have stronger feature representation capabilities. Traditional stacked networks mainly increase model complexity by stacking network layers, which simultaneously brings about the issues of vanishing/gradients explosion; whereas the parallel convolutional layer structure increases the "width" of the network rather than its "depth", enhancing the model's capability to represent complex features while somewhat mitigating the vanishing/gradients explosion phenomena [56]. In the MGC module, after the first convolution operation is completed, max pooling is applied, followed by a further feature abstraction using a small convolution kernel, and then pooling again. Each scale channel has a gated unit $\mathcal{G}(\cdot)$, and the output after the gated unit is as follows:

$$y = x \odot \mathcal{G}(x) \tag{12}$$

where *x* is the output after convolution and max pooling, serving as the input to the gated unit; $\mathcal{G}(\cdot)$ is the gating function that maps *x* to the interval (0, 1); and the \odot operator denotes element-wise multiplication of vectors/matrices of the same size, as shown in Figure 8.

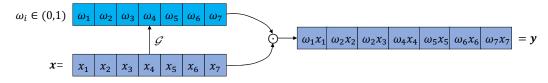


Figure 8. The process of the gated unit.

In this paper, the gated unit uses a Sigmoid function (as shown in Equation (6)), so the gating mapping relationship is fixed and does not change with the model. The following represents the feature maps processed by the gated unit in matrix form:

$$\mathbf{Y} = \begin{bmatrix} \mathcal{G}(x_1^{(1)})x_1^{(1)} & \mathcal{G}(x_2^{(1)})x_2^{(1)} & \cdots & \mathcal{G}(x_m^{(1)})x_m^{(1)} \\ \mathcal{G}(x_1^{(2)})x_1^{(2)} & \mathcal{G}(x_2^{(2)})x_2^{(2)} & \cdots & \mathcal{G}(x_m^{(2)})x_m^{(2)} \\ \vdots & \vdots & \ddots & \vdots \\ \mathcal{G}(x_1^{(c)})x_1^{(c)} & \mathcal{G}(x_2^{(c)})x_2^{(c)} & \cdots & \mathcal{G}(x_m^{(c)})x_m^{(c)} \end{bmatrix}$$
(13)

where x_i^j represents the features after convolution mapping, and $\mathcal{G}(x_i^j)$ is the weight value of after being processed by the gated unit, so $\mathcal{G}(x_i^j) \cdot x_i^j$ forms the final features, making up the feature map Y. Each element in matrix Y represents a feature in a certain dimension,

but not all features reflect information about bearing wear and degradation. Qualitatively, the feature map Y is divided into two parts:

$$Y = \mathcal{G}(x^+) \odot x^+ + \mathcal{G}(x^-) \odot x^-$$
(14)

where x^+ represents features related to degradation information, while x^- represents irrelevant features. Because x^- does not provide effective features and may even interfere with the model's judgment, we assign smaller weights to these features through the gated unit to minimize their impact on the model's regression inference. The specific process is achieved through the optimization of model parameters. It is worth mentioning that since this paper uses the Sigmoid function as the gated unit, which is a fixed function, the weights assigned to x by the gating unit are actually determined by x itself. We know that x is the feature obtained from convolution. Therefore, from the perspective of model training, the gated unit affects the optimization process that makes it easier for parameters to converge to the global optimum. Additionally, the gated unit could be set as an independent function, also based on training sets for parameter optimization, but this approach would place further demands on the scale and quality of the dataset, which we do not discuss further here.

Equation (14) shows that by introducing a nonlinear function \mathcal{G} to map the output of the current layer and multiplying it with the original output as a weight, the adaptive enhancement of the importance of important information and the ignoring of unimportant information are achieved, thereby regulating the flow of information and serving as a "gate". This operation based on the gated unit has several advantages. Firstly, the introduction of the gated unit allows the neural network to adaptively regulate the importance of each feature in the information transmission. In traditional neural networks, all features are treated equally, whereas the gated unit, through learning weight adjustments, allows the network to handle the contributions of different features to the task more flexibly. This mechanism is similar to the processing of information in the human brain and can better simulate human cognitive processes, thereby enhancing the representation and generalization capabilities of the neural network. Secondly, the gated unit can help the neural network better deal with noise and redundant information in the data. Due to external interference and factors such as assembly clearance, bearing vibration signals often contain a large amount of irrelevant information. The gated unit can adjust weights to selectively transmit features meaningful to the task and suppress the transmission of useless information, thereby improving the robustness and anti-interference ability of the model. Additionally, the gated unit can mitigate issues such as gradient disappearance and gradient explosion to some extent. By introducing a nonlinear function, the gated unit can effectively clip and adjust gradients, avoiding excessive growth or disappearance of gradients during backpropagation, which is conducive to accelerating the convergence speed of the network and improving training efficiency and stability. Therefore, the introduction of the gated unit provides a flexible and efficient information processing method for the network, which helps to enhance the performance and application scope of the model.

It is worth noting that Equation (3) shows that the one-dimensional convolution kernel has a depth direction, equal to the number of channels of the input sample. In the two levels of MGC modules in the constructed network structure, the input to the first-level MGC is the time–frequency domain vibration signal with one channel; the input to the second-level MGC is the output of the first-level MGC, and the number of channels at this point is a predefined hyperparameter, determined by the network structure. The multiscale convolution kernels are set with a stride of 1, and to maintain the same feature length before and after convolution, the zero-padding length is designed according to the following rules:

$$N_{\text{padding}} = \left\lfloor \frac{l_{\text{conv}} - 1}{2} \right\rfloor \tag{15}$$

where l_{conv} is the length of the convolution kernel, and $\lfloor \cdot \rfloor$ denotes the floor function.

3.3. Detailed Model Parameters

The detailed parameters of the designed network model are shown in Table 1. The number of zero-padding in the convolution and pooling layers is calculated according to Equation (15), which is not given in the table. The depth of the convolution kernel is equal to the number of input channels.

	LayerI		r of Channels	s Convolution Kernel		Max	Pooling	- Gated Unit	
			Output	Size	Stride	Size	Stride	Gated Offic	
	Long-term cycle	1	16	129 × 1	1				
	1st-Conv Medium-term cycle	1	16	33×1	1	4×1	2	Sigmoid	
1st-MGC	Short-term cycle	1	16	9×1	1		_		
(time-domain)	2nd-Conv	16	16	5×1	2	4×1	2	/	
	Res-connection	1	48	1×1	8	/	/	/	
	Long-term cycle	48	16	129 × 1	1				
	1st-Conv Medium-term cycle	48	16	33×1	1	4×1	2	Sigmoid	
2nd-MGC	Short-term cycle	48	16	9×1	1	1/1	-	orginora	
(time-domain)	2nd-MGC in time-domain	16	16	5×1	2	4×1	2	/	
	Res-connection	48	48	1×1	8	/	/	/	
	Long-term cycle	1	16	129 × 1	1				
	1st-Conv Medium-term cycle	1	16	33×1	1	4×1	2	Sigmoid	
1st-MGC	Short-term cycle	1	16	9×1	1	1 / 1		orginoid	
(frequency-domain)	2nd-Conv	16	16	5×1	2	4×1	2	/	
	Res-connection	1	48	1×1	8	/	/	/	
	Long-term cycle	48	16	129 × 1	1				
	1st-Conv Medium-term cycle	48	16	33×1	1	4×1	2	Sigmoid	
2nd-MGC	Short-term cycle	48	16	9×1	1	1/1	-	Signola	
(frequency-domain)	2nd-Conv	16	16	5×1	2	4×1	2	/	
	Res-connection	48	48	1×1	8	/	/	/	
	Flatten		Channels: 48–	→1; activatio	on function:	ReLU; D	ropout =	0.5	
MLP	1st layer	L	ength of feature	e vectors: 2	304→20; acti	vation f	unction: I	ReLU	
	2nd layer		Length of featu	are vectors:	$20 \rightarrow 1$; activa	ation fui	nction: Re	eLU	

Table 1. Parameters of MGCNN.

4. Experiment and Discussion

4.1. Wear and Vibration Test of Sliding Bearings

It should be noted that the experiments and validations in this paper consider vibrations originating solely from bearings, without interference from degradation of other components. When lubrication is insufficient in sliding bearings, wear behavior is prone to occur on the load-bearing surface, and a certain degree of wear depth can accumulate, leading to excessive clearance between the journal and the bearing, which in turn causes abnormal vibration of the rotor. To quantitatively study the relationship between the vibration signals under bearing wear conditions and the depth of bearing wear, a sliding bearing wear test platform was designed and set up in our related work [57]. The wear test is divided into two parts:

1. During the sliding bearing wear test stage, the inner surface of the bearing contacts the middle section of the shaft, and the bearing remains stationary in the circumferential direction while being subjected to a fixed direction and amplitude load radially. The two ends of the shaft are supported by cylindrical roller bearings, which are constrained axially and radially, and maintain a constant speed rotation in the circumferential direction, as shown in Figure 9a. In this stage, the test bearing transitions from a healthy state to a worn state.

2. In the vibration measurement stage of the worn bearing, the worn test bearing is fixed in a bearing housing as a support for one end of the shaft, while the other end of the shaft is connected to an electric motor through a spring coupling. An eccentric mass block *m* is attached to the shaft, with an eccentricity e, and the shaft rotates at a constant speed in the circumferential direction. As shown in Figure 9b, *D* is the clearance between the journal and the bearing, which is also the maximum wear depth of the bearing.

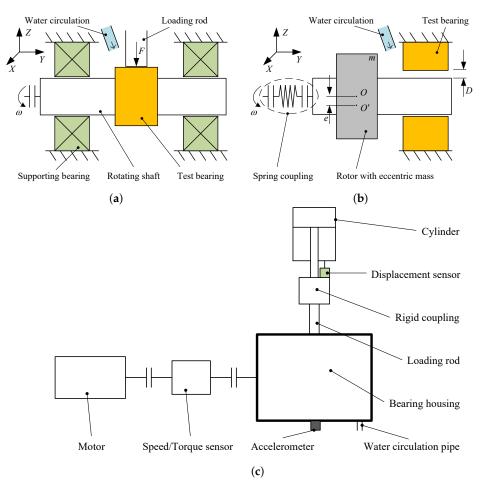


Figure 9. (a) Bearing housing assembly in wear test; (b) bearing housing assembly in vibration test; (c) overall structure of the test platform [57].

The established sliding bearing wear test platform is shown in Figure 10. A selflubricating brass bushing with graphite was used as the test bearing, and the shaft material was a modulated steel. A cylinder, through a loading rod, applies a radial load on the surface of the test bearing, and a displacement sensor measures the displacement of the loading rod, which is used to characterize the bearing wear depth during the test process. A single-axis accelerometer was deployed on the surface of the bearing housing to collect bearing vibration signals. Additionally, the test platform collects motor torque and bearing surface temperature. A worn bearing is shown in Figure 11.

According to various scenarios, sliding bearings operate at specific rotational speeds, ranging from several hundred to several thousand revolutions per minute. In our experiments, the motor speed was set to 3500 r/min, which is a relatively common moderate speed. Multiple test specimens were used for wear tests of different durations to obtain several sliding bearings with different wear depths, and vibration tests were conducted.

The vibration signals under different wear depths are shown in Figure 12, and the wear depths (μ m) included are as follows:

$$\boldsymbol{D}_{\text{label}} = [0, 70, 240, 270, 410, 420, 530, 690, 740, 760, 900, 950, 1060, 1160]$$
(16)

It is worth mentioning that in the experiment, each wear depth value was actually sampled for several segments, and Figure 12 only shows the vibration signals of 1 s in length corresponding to each wear depth.

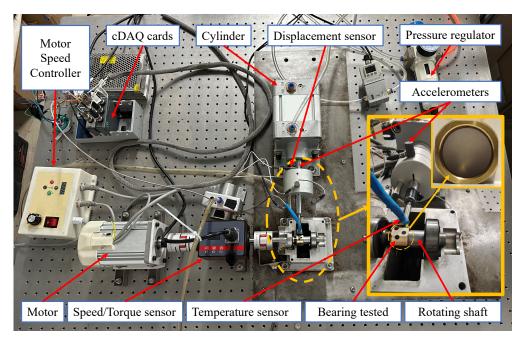


Figure 10. Sliding bearing test platform [57].



Figure 11. The worn bearing.

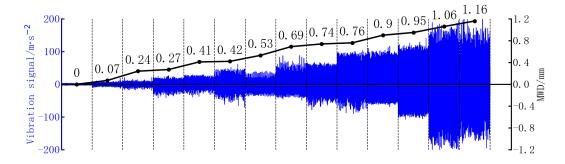


Figure 12. The measured vibration signals at different maximum wear depths.

4.2. Wear Depth Diagnosis

The set sample length W = 2048, and the stride S = 512. Data augmentation is applied to the samples with overlapping cuts. The original sample length is 25,600, with a quantity of 621. After cutting, the number of samples increases to 29,187, with each sample now having a length of 2048.

The mean squared error (MSE) is used as the loss function:

(

$$e_{\text{MSE}} = \frac{1}{N} \sum_{i=1}^{N} \left(\hat{D}_i - D_{\text{label},i} \right)^2$$
 (17)

where \hat{D}_i represents the output of the model, and $D_{\text{label},i}$ is the true value.

The set batch size $n_{\text{batch}} = 512$, the learning rate $\alpha = 5 \times 10^{-4}$, and the number of training epochs $n_{\text{epoch}} = 50$. There are 14 different wear depths, which correspond to 14 classes of labels, and each label has several samples. Since the samples are generated from the original data through overlapping cutting, to avoid data leakage between the test set and the training set, the first 100 samples from each label are taken as the test set, and the remaining data are used for training and validation. This means that at most 3 samples in each label's 100 test samples may overlap with the training data, which is negligible. The test set contains a total of 1400 samples. The remaining 27,787 samples are divided into the training set and the validation set according to *k*-fold cross-validation method (k = 5).

As shown in the validation loss function curve of the training process in Figure 13, it can be seen that the model's loss function on the validation set exhibits a stable downward trend as training progresses, and it can reach a stable convergence state around epoch $n_{\text{epoch}} = 15$.

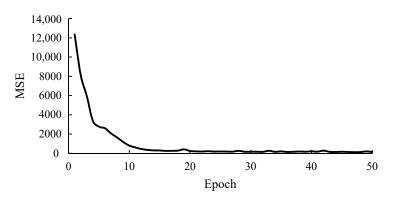


Figure 13. The curve of validation set loss function during training.

As described, the method undergoes 5 rounds of training, and the best model on the validation set for each round is used for testing. The average output of the 5 models on the test set is taken as the final result. This paper compares the proposed method with traditional diagnostic methods, including a single-scale CNN network, as illustrated in Figure 14, and a shallow machine learning model, support vector regression (SVR),

which extracts 11 time-domain features and 12 frequency-domain features referring to reference [58]. It should be noted that since the SVR training process does not involve batching and random reading of samples, and k-fold cross-validation was not adopted.

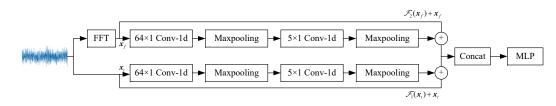


Figure 14. The CNN model used for comparison.

The wear diagnosis results of the models are shown in Table 2. It is worth mentioning that the SVR diagnostic error using time–frequency domain features is too large, so an SVR model using only time–frequency features was added as a control. To evaluate the performance of the models on the entire test set, the mean absolute error (MAE) was calculated by taking the absolute value mean of the test errors under each label. The calculation results are MAE_{MGCNN} = 11.7, MAE_{CNN} = 22.9, MAE_{SVR-1} = 287.1, and MAE_{SVR-2} = 62.8. Figure 15 shows the error curves of MGCNN, CNN, and time-domain feature SVR. From the results of the tables and figures, it can be seen that the proposed MGCNN model has higher accuracy than the traditional CNN and the shallow machine learning SVR, proving the effectiveness of the proposed method. Among them, the performance of the MGCNN and the traditional CNN is better than that of the shallow machine learning SVR model, which verifies the advantages and necessity of deep learning methods in diagnostic tasks with large sample sizes.

	MGC	MGCNN		CNN		SVR-1		R-2
True Value/µm	Output	Error	Output	Error	Output	Error	Output	Error
0	0.7	0.7	15.8	15.8	322.5	322.5	148.7	148.7
70	85.8	15.8	100.1	30.1	371.3	301.3	178	108
240	230.4	-9.6	219.5	-20.5	385.0	145.0	226.6	-13.4
270	302.8	32.8	338.6	68.6	408.6	138.6	321.3	51.3
410	427.6	17.6	397.2	-12.8	417.8	7.8	332.8	-77.2
420	404.9	-15.1	410.5	-9.5	428.6	8.6	452.6	32.6
530	514.2	-15.8	544.5	14.5	435.1	-94.9	431.7	-98.3
690	682.8	-7.2	654.4	-35.6	441.8	-248.2	586.7	-103.3
740	738.0	-2.0	736.3	-3.7	448.6	-291.4	734.8	-5.2
760	759.1	-0.9	779.4	19.4	449.2	-310.8	778.6	18.6
900	899.7	-0.3	911.1	11.1	473.8	-426.2	873.4	-26.6
950	968.6	18.6	973.6	23.6	478.5	-471.5	1011.6	61.6
1060	1072.4	12.4	1072.6	12.6	489.1	-570.9	1094.8	34.8
1160	1144.9	-15.1	1116.7	-43.3	478.0	-682	1060.8	-99.2
MAE			22.	9	282	7.1	62	.8

Table 2. Comparison of wear depth diagnosis results. Here, SVR-1 represents the SVR model using time–frequency domain features, while SVR-2 represents the SVR model using time-domain features.

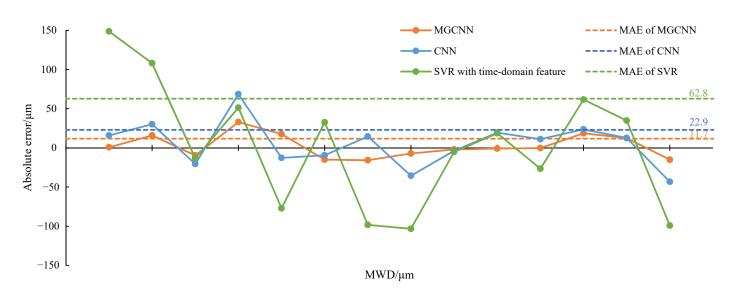


Figure 15. Comparison of diagnosis results from different models, where the abscissa corresponds to [0, 70, 240, 270, 410, 420, 530, 690, 740, 760, 900, 950, 1060, 1160] sequentially.

In addition, this paper selects three datasets with wear depth labels [240 µm, 530 µm, 760 µm] as the test set, and the remaining 11 wear depths data as the training set and validation set for the experiment. The results, as shown in Table 3, still show the smallest diagnosis error for the MGCNN. It can be observed that the error shown in Table 2 is larger than that in Table 3. The reason for this is that, although this paper abstracts the sliding bearing wear diagnosis as a regression problem and infers a continuous regression value from the vibration signal as the wear depth, during the supervised training process of the model, the training set labels are discrete, as described in this paper. As stated, the dataset contains 14 labels. This leads to more accurate diagnostic results at places where the model is "similar" to the training data. Therefore, in terms of data quality and completeness, vibration signals with richer and uniformly distributed depth labels help train more accurate diagnostic models; conversely, if the dataset is unbalanced, and the distribution of training set labels is uneven, the diagnostic error for data outside the training set range will be relatively large; that is, the model has poor generalization ability. In summary, for sliding bearing wear intelligent diagnostic methods, the rationality of the model structure and the balance of the data are two important aspects.

	MGCNN		CNN		SVR-1		SVR-2	
True Value/µm	Output	Error	Output	Error	Output	Error	Output	Error
240	176.9	-63.1	184.4	-55.6	390.1	150.1	131.5	-108.5
530	557.4	27.4	584.0	54.0	428.2	-101.8	363.2	-166.8
760	797.4	37.4	808.0	48.0	448.1	-311.9	846.3	86.3
MAE 42		5 52.4		4	187.9		120.5	

Table 3. The diagnosis results of MGCNN. The test set consists of data from three bearings with wear depths of $[240 \,\mu\text{m}, 530 \,\mu\text{m}, 760 \,\mu\text{m}]$, respectively.

4.3. Impact of Dataset Size on Model Performance

Next, the impact of the size of the training dataset on the model's diagnostic accuracy is analyzed. Based on the original dataset (containing 29,187 samples), the training set size is randomly reduced by 10% each time and model testing is conducted again. The size of the validation set is reduced synchronously with the test set, and *k*-fold cross-validation (k = 5) is still used to randomly divide the validation set. The size of the test set remains unchanged, always maintaining 1400 samples. The test results are shown in Table 4, and

Figure 16.

	Size of Training Set								
True Value	90%	80%	70%	60%	50%	40%	30%	20%	10%
0	1.1	5.1	4.7	2.4	6.6	8.2	9.9	33.2	66.1
70	91.8	84.6	86.7	93.4	86.3	97.3	111.3	108.5	131.9
240	237.1	234.5	231.7	235.3	231.7	233.0	218.5	202.8	199.4
270	302.4	307.7	302.8	306.3	311.4	311.2	327.1	327.7	331.6
410	421.3	422.1	428.4	430.2	428.8	410.5	405.1	406.7	369.3
420	402.0	404.4	403.1	403.5	402.1	408.1	420.4	420.1	453.6
530	520.6	516.2	517.4	518.5	519.6	517.1	520.3	527.8	529.3
690	678.8	685.8	682.5	683.1	683.0	684.4	673.9	664.5	651.1
740	735.4	733.2	733.9	731.6	732.8	734.2	734.6	731.5	741.4
760	760.7	763.6	761.3	763.5	763.1	769.2	778.5	788.1	817.1
900	903.5	905.2	904.5	905.4	907.8	908.9	919.8	918.4	939.1
950	973.1	975.9	979.1	976.1	970.3	977.1	981.9	996.9	999.6
1060	1067.1	1074.1	1075.7	1075.3	1075.7	1074.4	1081.8	1087.2	1105.7
1160	1147.7	1140.9	1138.8	1139.6	1139.5	1127.2	1123.9	1120.6	1121.9
MAE	11.4	13.1	14.0	14.4	14.4	15.2	21.0	26.1	41.1

the trend of MAE on the test set with respect to the size of the training set is shown in

Table 4. Diagnostic results of MGCNN with different sizes of training set.

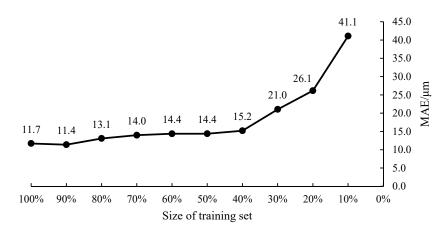


Figure 16. The variation in diagnosis error with training set size.

The MAE for 100% training set size is already given in Table 2. As the number of training set samples decreases, the error gradually increases, but the change trend is relatively slow between 100% and 40%, while between 40% and 10%, the diagnostic error increases significantly. From the results, it can be seen that for the established MGCNN model, a larger and more complete training set can better train the model. To ensure the generalization ability of the model, there is a roughly defined "lower limit" for the training set size. Taking Table 4 as an example, the model accuracy is similar above 40% data volume, while it significantly deteriorates below 40%. Considering the cost of data collection and processing, 40% data volume would be a suitable choice. Generally speaking, as the complexity of the model increases and the number of parameters to be trained increases, the demand for the scale of the dataset will also increase. Due to significant variations in data distribution across different environments, appropriately estimating the data volume based on specific conditions and requirements will aid in the deployment and application of the model.

4.4. Impact of Noise on Model Performance

This section analyzes the impact of noise on MGCNN by adding noise to datasets at various signal-to-noise ratio (SNR) levels. The definition of SNR is as follows [52]:

$$SNR = 10 \lg \frac{P_s}{P_n}$$
(18)

where P_s is the signal power, and P_n is the noise power. A lower SNR indicates a higher noise component. Five noise levels were chosen, specifically SNR = [8 dB, 6 dB, 4 dB, 2 dB, 0 dB], and Figure 17 shows the waveform of a signal after the addition of different noise levels.

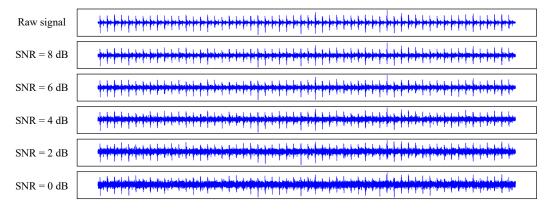


Figure 17. Signal with Gaussian white noise added at different SNRs, where $D = 420 \,\mu\text{m}$ and the signal length is 1 s.

It is worth noting that three specific noise strategies were implemented. Each strategy includes test results for five SNRs:

- Strategy 1: Noise at a specific SNR was not added to the training or validation sets but only to the test set. The test results are shown in Table 5.
- Strategy 2: Noise at a specific SNR was added to all training, validation, and test sets. The test results are shown in Table 6.
- Strategy 3: Noise at one specific SNR was added to the test set, while the remaining four SNRs were added to the training and validation sets. For example, the test set was subjected to 0 dB of noise, whereas the training and validation sets were exposed to noise levels of SNR = [8 dB, 6 dB, 4 dB, 2 dB], resulting in a quadrupling of the training set size. The test results are shown in Table 7.

The comparison of errors for the three noise strategies is illustrated in Figure 18. As the SNR decreases, meaning the noise increases, the error in Strategy 1 shows a significant increasing trend, while in Strategy 2, since the noise level added to both the training and test sets is the same, meaning the data distribution is identical, the error only slightly increases with the addition of noise, remaining within an acceptable range. On the other hand, in Strategy 3, where the SNR in the training set differs from that in the test set, thus leading to different data distributions, the error trend is similar to that of Strategy 2. This indicates that data augmentation through the addition of varying levels of noise to the training set can effectively enhance the model's robustness. In practical applications, it is often difficult to know the noise distribution of the test targets a priori; therefore, Strategy 3 presents an effective method for data augmentation and holds certain practical value.

		SNR				
Models in k-Fold Cross-Validation	Raw Signal	8 dB	6 dB	4 dB	2 dB	0 dB
No.1	/	23.0	30.2	40.1	56.7	80.0
No.2	/	21.2	30.2	43.7	66.1	101.1
No.3	/	22.3	32.0	46.3	67.7	99.6
No.4	/	23.3	30.8	42.7	66.5	102.9
No.5	/	22.0	31.2	44.4	66.4	94.2
Mean	11.7	22.4	30.9	43.4	64.7	95.6

Table 5. Test results under Strategy 1.

Table 6. Test results under Strategy 2.

		SNR						
Models in k-Fold Cross-Validation	Raw Signal	8 dB	6 dB	4 dB	2 dB	0 dB		
No.1	/	11.6	10.0	14.0	14.6	16.4		
No.2	/	13.4	13.2	15.0	15.8	17.5		
No.3	/	12.7	12.1	13.8	14.2	17.5		
No.4	/	12.4	11.6	15.4	15.5	15.7		
No.5	/	10.8	11.8	12.9	14.8	17.4		
Mean	11.7	12.2	11.7	14.2	15.0	16.9		

Table 7. Test results under Strategy 3.

Models in k-Fold Cross-Validation	Raw Signal	8 dB	6 dB	4 dB	2 dB	0 dB
No.1	/	11.9	12.7	14.3	13.9	15.4
No.2	/	11.3	14.5	13.8	13.9	14.6
No.3	/	13.0	12.7	13.8	14.5	15.6
No.4	/	12.2	12.5	10.5	15.5	17.1
No.5	/	12.9	10.8	13.7	16.1	13.6
Mean	11.7	12.2	12.6	13.2	14.8	15.3

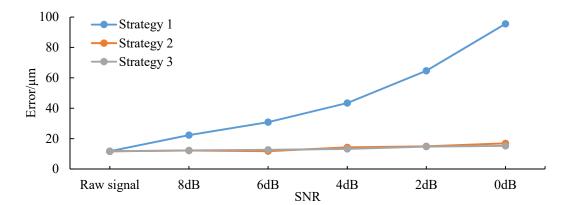


Figure 18. Comparison of errors for the three noise strategies.

4.5. Prognosis of Remaining Useful Life

Based on the diagnosis of MWD, this section theoretically predicts the remaining useful life (RUL) of sliding bearings. RUL is defined as the time interval from the current moment to the future failure moment [59]. We establish $D_{\text{threshold}}$ as the failure threshold for the sliding bearing; when MWD reaches $D_{\text{threshold}}$, the bearing is considered to have failed. We recorded the actual MWD change curve for a wear test, as illustrated in Figure 19. Setting $D_{\text{threshold}} = 1000 \,\mu\text{m}$, we use the diagnostic results at various depths and corresponding

times to fit an exponential function [60], as shown in Equation (19). The time at which this fitted curve reaches the failure threshold is taken as the predicted failure time.

$$D = a \cdot \exp(bt) - a \tag{19}$$

where *a* and *b* are parameters to be determined, obtained through least squares fitting. Then, the predicted RUL can be calculated:

$$RUL = \frac{1}{b} \ln(\frac{D_{\text{threshold}}}{a} - 1) - t_i$$
(20)

where t_i is the current time. When the MWD diagnostic result changes, the parameters *a* and *b* are updated, and the RUL prediction results are revised accordingly. The prediction results and errors of RUL are shown in Table 8.

In the early stages of prediction, due to the limited data available for fitting, the RUL predictions can exhibit significant errors. As the bearing continues to operate and diagnostic results are updated, the accuracy of the predictions improves, and the error tends to decrease towards zero. This indicates that the method is theoretically viable for predicting the RUL of sliding bearings. During the initial stages when prediction errors are large, it is advisable to make comprehensive judgments by integrating more conditions according to actual situations to avoid misjudgments. Meanwhile, it must be acknowledged that the validation experiments conducted in this study are relatively simplistic. Future research could involve using more accurate degradation models and developing failure conditions that are better suited to different practical scenarios.

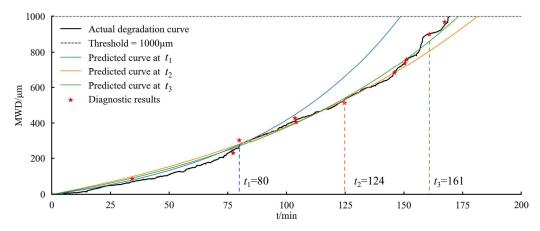


Figure 19. The actual degradation curve and the fitting curves at different times.

Current Time t_i (min)	Actual RUL (min)	Predicted RUL (min)	Error (min)
0	170	7	-163
34	136	14	-122
77	93	120	27
80	90	69	-21
104	66	52	-14
124	46	58	12
146	24	57	33
150	20	35	15
151	19	29	10
161	9	26	17
167	3	13	10
170	0	4	4

Table 8. Prognosis of RUL.

5. Conclusions

This paper addresses the quantitative diagnosis of wear in sliding bearings and proposes an intelligent diagnostic method based on an MGCNN. The proposed method utilizes dual-path parallel structures in the time and frequency domains to process time-domain and frequency-domain signals separately, ensuring the integrity of information transmission through residual network connections. Within the constructed MGC module, three parallel channels, including long-term, medium-term, and short-term cycles, are employed to extract multiscale cyclic information from bearing vibration signals. Additionally, nonlinear gated units are used to adaptively adjust the weights during the feature information transmission process, enhancing the model's representation and generalization capabilities. The experimental results demonstrate that the proposed MGCNN model surpasses traditional CNN models and shallow machine learning models like SVR in terms of diagnostic performance. The proposed method can achieve high-precision, real-time wear diagnostics based on vibration signals and has preliminarily realized the RUL prediction of sliding bearings, consistent with expectations. Additionally, our experiments analyzed the impact of noise and data volume on model performance and provided practical noise augmentation strategies.

This research provides new insights and perspectives into the problem of sliding bearing wear diagnosis, yet it also reveals several limitations and challenges that remain. In terms of data collection, the current validation was conducted under laboratory conditions, assuming that the vibration signals were primarily due to gaps caused by bearing wear; however, in real-world engineering applications, vibration signals from other components may overlap, necessitating the separation of bearing signals from overall machine signals. Moreover, this study was validated at a single rotational speed; future research could explore more complex operating conditions, including the transferability of models between different conditions. Additionally, the proposed method, as a diagnostic approach based on vibration signals, fundamentally involves extracting features from periodic time series signals and performing regression fitting. Therefore, it possesses a certain universality in rotating equipment, presenting a broader potential for application. However, it should be noted that we used MWD as a quantifiable indicator in our current experiments because it meets intuitive expectations and is easily verifiable; when applying this methodology to other rotating elements, defining an appropriate state quantification indicator will be crucial. In future work, we aim to continually refine this method to adapt to more complex environments and enhance its impact on equipment status diagnosis and predictive maintenance.

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