Review

Fluctuating Asymmetry: Methods, Theory, and Applications

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Abstract: Fluctuating asymmetry consists of random deviations from perfect symmetry in populations of organisms. It is a measure of developmental noise, which reflects a population’s average state of adaptation and coadaptation. Moreover, it increases under both environmental and genetic stress, though responses are often inconsistent. Researchers base studies of fluctuating asymmetry upon deviations from bilateral, radial, rotational, dihedral, translational, helical, and fractal symmetries. Here, we review old and new methods of measuring fluctuating asymmetry, including measures of dispersion, landmark methods for shape asymmetry, and continuous symmetry measures. We also review the theory, developmental origins, and applications of fluctuating asymmetry, and attempt to explain conflicting results. In the process, we present examples from the literature, and from our own research at “Evolution Canyon” and elsewhere.

Keywords: continuous symmetry measures; developmental instability; Evolution Canyon; fitness; genomic coadaptation; landmark methods; stress
1. Introduction

Symmetry is ubiquitous in the living world [1]. Bilateral, radial, rotational, dihedral, and translational symmetries are present in all major groups of organisms. Even sponges, which are widely regarded as lacking symmetry, have fractal symmetry (i.e., symmetry of scale) [2]. These symmetries, however, are approximate and only large-sample averages approach the perfectly symmetrical objects of geometers. The extent to which the average individual departs from perfect symmetry is fluctuating asymmetry [3, 4], a measure of developmental noise and developmental instability [5-7]. Fluctuating asymmetry is important to population biologists because it reflects a population’s state of adaptation and coadaptation [8]. Consequently, it has numerous applications, theoretical and practical, in evolutionary biology, quantitative genetics, environmental biology, conservation biology, anthropology, agriculture, and medicine. Interest in fluctuating asymmetry has already spawned several book-length reviews [9-12]. In this paper, we review the methods, theory, and applications of fluctuating asymmetry.

Because all life forms are more or less symmetrical, one can demonstrate fluctuating asymmetry in all taxa [13, 14]. One can even demonstrate it in extinct life forms [15], bacteria [16], and viruses [17]. The ubiquity of symmetry is a major advantage of fluctuating asymmetry over other measures of developmental instability. One could conceivably compare developmental instabilities of vertebrates and viruses, and attempt to decipher the underlying causal stress.

From an initial emphasis on fluctuating bilateral asymmetry [18, 19, 5-7], research on fluctuating asymmetry now encompasses diverse symmetries (i.e., radial and dihedral symmetry, translational symmetry, etc.), shape asymmetry, and continuous symmetry measures [20-24]. Nevertheless, most practitioners are unaware of the diversity of approaches to the study of fluctuating asymmetry. Thus, we begin with an overview of symmetry in living organisms.

2. Symmetries

Living organisms display symmetries at every turn [1]. Vertebrates, for example, are bilaterally symmetrical, and adult echinoderms have dihedral symmetry. The flower of the periwinkle is rotationally symmetrical, and colonial flagellates, such as Volvox, are spherically symmetrical. Filamentous algae, on the other hand, are translationally symmetrical. Gastropods and nucleic acids have helical symmetry. Bacterial and fungal colonies exhibit various forms of symmetry, including fractal symmetry. All of these symmetries are potentially the basis for studies of fluctuating asymmetry.

2.1. Types of Symmetry

Belousov [25] proposed a taxonomy of symmetries, related to one another by a series of invariant transformations. These transformations are rotation, reflection, and translation, as well as all possible combinations of these three operations. Rotation moves an object in a circular motion. Reflection transforms it to its mirror image. Translation slides it to a new location.
A sphere is the most symmetrical object in three dimensions. It has neither dorso-ventral, nor right-left axes. An infinity of rotational and reflective axes pass through the center of a sphere. Oocytes, blastulas, and colonial algae, such as *Volvox*, have spherical symmetry (Figure 1A). Flattened disk-shaped organisms (e.g., centric diatoms, mushroom caps, and bacterial colonies) are a special case of radial symmetry—circular symmetry (Figure 1B-C). These also have an infinity of rotational and reflective axes, but only in two dimensions.

**Figure 1.** Spherical and circular symmetries. A. *Volvox* (© www.micrographia.com). B. Cap of a mushroom. C. Centric diatom. (© www.micrographia.com).

Rotational symmetry involves rotation around one or more axes of symmetry (Figure 2). If an object also has mirror symmetry, it has dihedral symmetry [26], which is a property of regular polygons. Most echinoderms, including adult starfish (Figure 2A), have five-fold dihedral symmetry. Moreover, most flowers and inflorescences have three-fold, four-fold, or five-fold dihedral symmetries (Figure 2B). Some flowers, such as the periwinkle, *Vinca major* (Apocynaceae: Angiospermae), which resembles a pinwheel, are rotationally symmetrical (Figure 2C). Breaking dihedral symmetry produces a bilaterally symmetrical object having just one reflective axis of symmetry.

**Figure 2.** Dihedral and rotational symmetries. A. Starfish (Bill Davin, Department of Biology, Berry College). B. Aster inflorescence. C. Periwinkle flower.
Bilateral, or mirror, symmetry involves reflection across an axis of symmetry (Figure 3). Left and right sides are mirror images of one another. It is the most common form of symmetry in the animal kingdom (Figure 3A), and is the rule in the leaves of plants (Figure 3B) and in the flowers of orchids and legumes, such as Clitoria (Figure 3C). Vertebrates, flatworms, and arthropods are bilaterally symmetrical. Even some sand dollars (Clypeasteroida: Echinodermata) display bilateral symmetry, though it verges on dihedral symmetry (Figure 3D). Breaking bilateral symmetry produces an object having handedness (or chirality). If most individuals in a population have handedness in the same direction, the asymmetry is directional asymmetry. If the population is a mixture of random left- and right-handed individuals, the asymmetry is antisymmetry. The mammalian heart and brain are directionally asymmetric, and the claws of male lobsters and fiddler crabs are antisymmetric.

**Figure 3.** Bilateral symmetry. A. Skull of a turtle. B. Leaf of *Quercus calliprinos*. C. Flower of Clitoria. D. Sand dollar.

Translational symmetry involves translation, a rigid movement (or sliding) of an object in one direction. Filamentous cyanobacteria, such as *Nostoc* (Figure 4A), have translational symmetry of individual cells, and annelid worms, such as *Glycera* (Figure 4C), have translational symmetry of metameres (Figure 4). The breaking of translational symmetry in many arthropods produces structurally distinct segments, as in the lobster. The internodes of vascular plants, such as *Equisetum* (Figure 4B), usually have broken translational symmetry as well.

Helical symmetry involves rotation, along with translation along the axis of rotation. Snails, spirochetes, tobacco mosaic virus particles, and deoxyribonucleic acid molecules have helical symmetry (Figure 5). Breaking of helical symmetry in gastropods produces the oddly shaped terrestrial snail *Opisthostoma* (Diplommatinidae: Gastropoda).

Fractal symmetry is symmetry of scale. Fractals are self-similar. For example, a mathematical fractal, such as the Sierpinski gasket, looks the same at all scales. Fractals in the living world, however, are finite, random fractals. Examples of such fractals include skull sutures and branching corals (Figure 6). Fractals having more than one scaling property are called multifractals. The time series of human heartbeat is a multifractal.
Figure 4. Translational symmetry. A. Filament of a cyanobacterium, Nostoc (Ashwani K. Rai, Department of Botany, Banaras Hindu University). B. Internodes of a horsetail, Equisetum arvense (Eric Guinther, public domain). C. Metameres of the polychaete Glycera (NOAA Photo Library).

2.2. Symmetry Groups

An $n$-dimensional object is mirror (i.e., bilaterally) symmetric if it is invariant under a reflection about a hyperplane of dimension $(n - 1)$ passing through the object’s center of mass. Thus a 2-dimensional object is mirror symmetric if it is invariant under a reflection about a line (the mirror-symmetry axis) (Figure 7b), and a 3-dimensional object is mirror symmetric if it is invariant under a reflection about a plane \cite{1, 26}. A 2-dimensional object has rotational symmetry of order $n$ if it is invariant under rotation of $\frac{2\pi}{n}$ radians about the symmetry center of the object (Figure 7a). A 3-dimensional object has rotational symmetry of order $n$ if it is invariant under rotation of $\frac{2\pi}{n}$ radians about an axis passing through the center of the object. This axis is the rotational symmetry axis. Rotational symmetry of order $n$ is denoted $C_n$-symmetry. Dihedral symmetry is the symmetry of a 2-dimensional object having both mirror symmetry and $C_n$-symmetry (such objects have $2n$ axes of mirror symmetry) (Figure 7c). Dihedral symmetry of order $n$ is denoted $D_n$-symmetry. Radial symmetry is $C_\infty$-symmetry (see Figure 7d). It differs from rotational and dihedral symmetries because the number of rotational and reflective axes of symmetry is infinite. An object displays translational symmetry if each of its segments is equal to the other segments of the object located at equal translational distances \cite{1}.
Symmetry is a major trait of life, partly because it requires less free energy than asymmetric alternatives. Oocytes, for example, are invariably spherical, because a sphere has the smallest surface to volume ratio, and hence the least free energy, of any membrane-enclosed object suspended in a fluid (air or another liquid). A sphere is the most symmetrical of objects, with symmetry order \( \infty/\infty \cdot m \), where \( \infty/\infty \) indicates the order of rotational symmetries (i.e., the number of rotations) and \( m \) indicates the presence of mirror symmetry. Other kinds of symmetry arise by breaking spherical symmetry. In sea urchins [25], a spherical oocyte transforms into a directionally asymmetrical larva. The change involves a gradual reduction in the symmetry order of the entire embryo (\( \infty/\infty \cdot m \) [oocyte] \( \rightarrow \infty \cdot m \) [fertilized egg] \( \rightarrow 2 \cdot m \) [2-cell stage] \( \rightarrow 4 \cdot m \) [4-cell stage] \( \rightarrow 8 \cdot m \) [8-cell stage] \( \rightarrow \infty \cdot m \) [blastula] \( \rightarrow 1 \cdot m \) [early bilaterally symmetrical larva] \( \rightarrow 1 \) [mature directionally asymmetrical larva]).

Symmetry is often adaptive. Bilateral symmetry, for example, usually occurs in actively moving organisms, such as most animals, where efficient locomotion is important [27, 28]. It influences flight efficiency of birds [29, 30] and improves internal circulation [31]. Radial, dihedral, and rotational symmetries occur in sedentary organisms, such as adult echinoderms, which interact with the environment from all directions [27]. Translational symmetry occurs in filamentous algae and bacteria, plants, and fungi, which require large surface to volume ratios. Metamerism, a form of translational symmetry, is an easy way to build a multicellular organism from serially repeated parts [32, 33]. Finally, fractal symmetry is an energetically efficient way for an organism to fill space [34-37], as well as an efficient design for conduits to distribute nutrients and gases to all cells of a multicellular organism [38].

2.3. Types of Objects

Symmetrical objects may be consistent, partially consistent, or inconsistent. One can apply asymmetry measures to all three categories.

Consistently symmetrical objects have a consistent topology of specific landmarks displaying some form of symmetry. The position of the corresponding landmarks, and the distances among them, may vary (Figure 8A), but their number is maintained. The methods of geometric morphometrics [21, 39] are suitable for quantifying asymmetry of consistent objects. A detailed review is given in section 3.2. Studies using this approach have been done with Drosophila wings [21], mite exoskeletons [40], honey bee wings [41], and house mouse mandibles [42].
Partially consistent objects have consistent topology, but the number of homologous landmarks varies among specimens (Figure 8B). The landmark method is suitable here as well, although characteristics of specific landmarks cannot be quantified. An example of partial consistency would be the wild carrot, *Daucus carota* (Apiaceae: Angiospermae), where individual leaves differ in the number of secondary veins.

Inconsistent objects have no homologous landmarks, no consistent topology, no quantitative consistency, and sometimes no matching points (Figure 8C). Besides the continuous symmetry measure (CSM) and its applications (detailed review is given in section 3.3), there are no general methods for quantifying asymmetry of inconsistently symmetrical objects. An example would be leaves of the white oak, *Quercus alba* (Fagaceae: Angiospermae), which often have different numbers of lobes and sinuses on left and right sides.

To quantify asymmetry of inconsistently symmetrical objects, Milner et al. [23, 24] determined anchor points (in contrast to landmarks) on left and right sides of a bilateral structure, and used these as matching points. Since no geometric or structural consistency could be assumed, they introduced the idea of defining matching points, based on biological growth models, for Palestine oak (*Quercus calliprinos*) [24].

Figure 8. Three types of objects for quantifying metric asymmetry. A. Structures having consistent topology and number of landmarks (*Drosophila melanogaster* wings). B. Structures having consistent topology, but varying number of corresponding landmarks among specimens (the secondary veins of *Daucus carota* leaves). C. Variable structures having no consistent topology, no quantitative consistency, and sometimes no matching points (lobes and sinuses on the leaves of *Quercus alba*).

3. Measuring Deviations from Perfect Symmetry

Deviations from perfect symmetry may be measured as variances (or related measures of dispersion) of linear dimensions, shape variation involving landmarks, or as continuous symmetry measures. We begin by applying these approaches to bilaterally symmetrical structures.
The first step in measuring the asymmetry of bilaterally symmetrical structures is determining matching points on left and right sides. In perfectly symmetrical objects, these points will be mirror images of one another. Using mathematical notation, these points form an orbit of the given symmetry group. When there are no matching points, artificial points can be created, for example, by choosing points where the margin of an object intersects a line that (1) crosses the axis of symmetry at its midpoint, and (2) is orthogonal to the axis of symmetry [43-45]. Other alternatives include sampling along the contour of an object [46] or comparing the width of corresponding elements [47].

The second step in measuring asymmetry is selecting a function that returns a measure of asymmetry. This measure may be applied to Procrustes, Hausdorff, or Euclidian distances (e.g., width, distance to origin, absolute distance, etc.).

Before proceeding further, one should verify that the asymmetry is fluctuating asymmetry, and not a broken symmetry, such as directional asymmetry or antisymmetry [48, 49]. Ordinarily, fluctuating bilateral asymmetry is symmetrically distributed about a mean of zero. Directionally asymmetric traits will have a mean other than zero, and antisymmetric traits will have either a platykurtic or bimodal distribution about a mean of zero. Directionally asymmetric and antisymmetric traits should be studied separately [50, 51]. In fact, Graham et al. [52] and Van Dongen [53] have developed methods for either removing the directional component or decomposing a mixture distribution into fluctuating, directional, and antisymmetric components.

Asymmetry measurements are made on individuals, or repeated parts of individuals (leaves, flowers, etc.). Nevertheless, fluctuating asymmetry is largely a population parameter [4, 6]. It has been applied to individuals [54], but with only limited success. Finally, studies of fluctuating asymmetry can be based upon single [48] or multiple traits [55, 49].

3.1. Measures of Dispersion

The classic measure of fluctuating bilateral asymmetry is the variance (or standard deviation) of the difference between the value of a trait on left and right sides [19, 5]. If \( d_i = l_i - r_i \), where \( d_i \) is the left-right asymmetry of individual \( i \), \( l_i \) is the value of the trait on the left side, and \( r_i \) is the value of the same trait on the right side, then a measure of fluctuating asymmetry is \( \text{Var}(d_i) \), or its square root (standard deviation). Trait values \((l, r)\) can be either continuous or discrete.

An alternative to the variance is the mean absolute deviation [56]. This is the expectation \( E \) of \(|x_i - \mu|\), where \( x_i \) is an individual observation and \( \mu \) is the population mean. Assuming \( \mu = 0 \), which is routine in studies of fluctuating asymmetry, the mean absolute value of \( d \) is \( E|d_i| \). It is less sensitive to outliers than the variance [57], and \( |d_i| \) lends itself to analysis of variance [58, 59, 49]. If \( d_i \) is normally distributed, then \( |d_i| \) has a half-normal distribution. One can normalize \( |d_i| \) with a power transform: \((|d_i| + 0.00005)^{0.33} [54]. The value of the mean absolute deviation is approximately 0.8 of the standard deviation [60].

Measures of dispersion are easily generalized to other kinds of symmetry as well. For a pentameric starfish, for example, one can measure within-individual variation in arm length as a variance: \( \text{Var}(x_i) \), where \( x_i \) is the length of arm \( i \). Because all starfish have five arms, this would be a population variance, rather than a sample variance (if all five arms were measured). Used in this way, \( \text{Var}(x_i) \) is analogous to \( d_i \), and is a measure of individual asymmetry. The mean of \( \text{Var}(x_i) \) (or the standard deviation) would
be the actual measure of fluctuating asymmetry for a sample of starfish. In addition to the variance, the mean absolute deviation can be applied to other kinds of symmetry. For the starfish mentioned earlier, individual asymmetry would be $E|x_i - \mu|$, where $x_i$ is the length of arm $i$ and $\mu$ is the mean of all five arms. Similar approaches can be taken with translational symmetry. For reasons discussed previously, we prefer the mean absolute deviation.

On the other hand, traditional measures of dispersion completely ignore the shape of a structure (e.g., rotations, translations, etc.), but refer only to linear distances of morphometric traits or counts of meristic traits. Landmark methods give the appropriate attention to consistent and partially consistent objects, and continuous symmetry measures extend that attention to inconsistent objects.

3.2. Landmark Methods for Shape Asymmetry

Landmark methods for the analysis of bilateral shape asymmetry were developed by Bookstein [61] and first used by Auffray et al. [42] and Smith et al. [41]. These approaches have been reviewed by Auffray et al. [62].

Bilateral symmetry can be either matching symmetry or object symmetry [63]. With matching symmetry, a structure is present in two separate copies, located on the left and right sides as mirror images of one another (e.g., *Drosophila* wings). The symmetry axis does not pass through matching symmetries. With object symmetry, in contrast, the structure itself is symmetric (e.g., human face), and the symmetry axis passes through the object. By using developmentally homologous points (i.e., landmarks), rather than conventional measurements of distance, it is possible to quantify asymmetry in complex structures using matching symmetry [21] or object symmetry [39].

Klingenberg and McIntyre [21] suggest the following procedure for quantifying matching asymmetry via landmarks.

1. Select morphological landmarks and digitize their $x$ and $y$ coordinates (Figure 9). Klingenberg and McIntyre [21] used wing vein intersections for their landmarks, but this approach can be applied to many other situations, such as the mouse mandible [64] and the ventral face of the mite exoskeleton [40].

**Figure 9**. The right wing of *Drosophila melanogaster*. The arrowheads point to the landmarks.
2. Reflect the landmarks on one side of the body to their mirror image (left wing in the example) to align corresponding landmarks on both sides (Figure 10).

**Figure 10.** Left wing reflected to its mirror image.

3. Scale both configurations on left and right sides to have the same unit centroid size (Figure 11). The centroid size is the square root of the sum of the squared distances from the landmarks to the common centroid (*i.e.*, the geometric center).

**Figure 11.** Scale both wings to the same unit centroid size.

4. Superimpose the wings (configurations of landmarks) by shifting the left and right centroids to a common set of $x$ and $y$ coordinates [0, 0] (Figure 12).

**Figure 12.** Superimpose the two wings.
5. Rotate both configurations around their centroids to achieve the optimal fit of corresponding landmarks (Figure 13). This is a least-squares approach. The optimal fit minimizes the sum of the squared deviations between the paired landmarks.

**Figure 13.** Rotate the wings to achieve an optimal fit of the landmarks [adapted from 21].

6. The difference between homologous landmarks on right and left sides of a specimen is calculated as $x_{y_{l}} - x_{y_{r}}$. The total difference between landmarks within an individual is calculated as $\sum (x_{y_{l}} - x_{y_{r}}) / k$, where $k =$ the number of landmarks. Palmer and Strobeck [49] pointed out that $x_{y_{l}} - x_{y_{r}}$ is conceptually the same as $(l_{i} - r_{i}) / [(l_{i} + r_{i}) / 2]$, the most common index of asymmetry for a single trait. Normalization for unit centroid size eliminates size differences in much the same way as normalizing asymmetry by trait size does (e.g., $(l_{i} + r_{i}) / 2$).

Klingenberg and colleagues [39] have suggested a measurement for quantifying object symmetry via landmarks. We illustrate their approach with ten landmarks (Figure 14, vertices). The vertical line defines the single axis of symmetry, whereas the remaining eight vertices are in four pairs on right and left sides. The diagram shows the original configuration (solid black line). The procedure consists of three steps:

1. Generate a reflected copy of each landmark by reversing the side of its $x$-coordinate. Then the paired landmarks of the reflected copies are re-labeled so that each paired landmark obtains the label of its counterpart (dotted black line).

2. The Procrustes average is then defined (dashed-dotted red line) as the middle of the line passing between the original landmark and the reflected copy of the corresponding landmark. The new shape created by connecting these average landmarks is perfectly symmetrical.

3. The asymmetry of the entire object is then the difference between the original and the mirror configurations, or equivalently, the landmark deviations of the original configuration from the average landmarks.
Figure 14. Asymmetry of eight landmarks. The diagram shows the original configuration (solid black) and its reflected and relabeled copy (dotted black), after least-squares Procrustes superimposition. The Procrustes average (dashed-dotted red) is perfectly symmetrical. (Adapted from [39]).

Landmark methods are suitable for analyzing bilateral asymmetry in either 2- or 3-dimensions. Unfortunately, they are restricted to objects having homologous left and right landmarks. In the next section, we present an overview of the continuous symmetry measure (CSM), defined for all symmetry groups in all dimensions, regardless of whether or not there are homologous landmarks.

3.3. Continuous Symmetry Measures (CSM)

Continuous symmetry measures (CSM) are a flexible alternative to measures of dispersion and landmark methods of shape asymmetry [65]. Moreover, they are the only suitable approach for inconsistent objects having variable structural elements. Hence, they encompass the landmark methods.

The continuous symmetry measure (CSM) was developed for the computer vision and computer graphics community [66]. Its novelty for this community is treating symmetry as a continuous feature rather than a binary feature (i.e., whether it exists or not). Developmental instability is a continuous property of organisms. Thus, the amount of asymmetry should provide information about the level of developmental instability. CSM can do this as well. Moreover, because the CSM quantifies asymmetry in all dimensions and for all types of symmetry, it is an efficient tool for analyzing deviations from symmetry in living organisms.

The underlying mathematics of symmetry relies on the concept of symmetry groups, groups of symmetry-preserving operations [67, 1]. We define a symmetric object as a set of points invariant under the actions of any element of a symmetry group (e.g., bilateral, translational, rotational, dihedral, or a mixture of all of these). A point $x$ of an object, and all its transformations under the group members, is called an orbit. This implies that an object is symmetric if one can partition it into orbits invariant under the operations of the symmetry group. For example, an equilateral triangle in 2-dimensions is rotationally symmetric (order 3) and one can partition it into orbits containing three points each. The vertices of the triangle form one such orbit. Consequently, given a point $x$, every point
in its orbit is naturally associated with an element of the symmetry group. For example, in Figure 15d, the orbit of point \( P_0 \) consists of the points \( P'_0, P'_1, P'_2 \), which are associated with \( R_1^0, R_3^1, R_5^2 \) (rotations of \( \frac{2\pi}{n} \) for \( i = 0, 1, 2 \)), respectively.

The continuous symmetry measure (CSM) involves the amount of 'effort' required to transform a given shape (composed of orbits) into a symmetric shape. This 'effort' is the mean of the squared distances each point must move from its original position to one of perfect symmetry. Note that we assume no a priori symmetric reference shape. Denote by \( \Omega \) the space of all shapes of a given dimension, where each shape \( P \) is represented by a sequence of \( n \) points \( \{P_i\}_{i=0}^{n-1} \). A metric \( d \) is defined on this space as follows:

\[
d : \Omega \times \Omega \rightarrow R
\]

\[
d(P, Q) = d(\{P_i\}, \{Q_i\}) = \frac{1}{n} \sum_{i=0}^{n-1} \|P_i - Q_i\|^2
\]

**Figure 15**. The folding-unfolding algorithm applied to a single orbit (from [26]). CSM with respect to rotational symmetry of order 3 is calculated. The points \( P_0, P_1, P_2 \) are associated with the rotations \( R_3^0, R_3^1, R_3^2 \), respectively: a) Original 3 points \( \{P_i^2\}_{i=0}^{2} \). b) Fold – apply the inverse symmetry element to each point (i.e., rotate \( P_i \) by \( R_3^{-i} \)). Points \( \{P_i^2\}_{i=0}^{2} \) are obtained. c) Average – points \( \{P_i^2\}_{i=0}^{2} \) are averaged, obtaining \( \bar{P} = \frac{1}{3} \sum_{i=0}^{2} P_i \). d) Unfold – apply the symmetry elements to average point \( \bar{P} \) (i.e., rotate by \( R_3^{i} \)), obtaining points \( \{P_i^2\}_{i=0}^{2} \). CSM is calculated: CSM = \( \frac{1}{3} \left( \|P_0^2 - \bar{P}\|^2 + \|P_1^2 - \bar{P}\|^2 + \|P_2^2 - \bar{P}\|^2 \right) \).

This metric defines a distance function between any two shapes in \( \Omega \). We define the symmetry transform of a shape \( P \) as the symmetric shape \( \hat{P} \), closest to \( P \) in terms of metric \( d \). The continuous symmetry measure (CSM) of a shape \( P \) is the distance between \( P \) and its symmetry transform:

\[
CSM = d(P, \hat{P})
\]
Thus, the CSM explicitly implies invariance to rotation and translation. Normalizing the original shape prior to the transformation also allows the invariance to scale. An additional feature of the CSM is that we obtain the symmetric shape 'closest' to the given one, enabling visual evaluation (Figure 15d).

Zabrodsky et al. [26] developed a geometric algorithm for deriving the symmetry transform of a shape and, accordingly, the CSM value. For a specific symmetry group, the process of evaluating the CSM involves two steps.

1. **Partitioning the object into orbits**, i.e. determining the points or features of the input that will form each orbit and associating an element of the symmetry group with each point.

2. **Evaluating the symmetry transform and CSM value given the orbits**. Typically, there are numerous possibilities for partitioning the input points into orbits. We seek the partition providing the minimal distance between the original set and its symmetry transform. The algorithm implementing step 2 is referred to as the folding-unfolding method because of its geometric visualization. Given an orbit of points \( \{P_i\}_{i=0}^k \), with associated symmetry group members \( \{g_i\}_{i=0}^k \), the folding-unfolding method involves the following steps:

   1) **Fold**—apply the inverse symmetry element to each point, i.e., apply \( g_i^{-1} \) to \( P_i \) for \( i = 0, \ldots, k-1 \). The folded points \( \{\tilde{P}_i\}_{i=0}^k \) are obtained.

   2) **Average**—if the original points were perfectly symmetrical, then (by definition) they would converge onto a single point. In general, however, they do not. Thus, we average the points \( \{\tilde{P}_i\}_{i=0}^k \), obtaining \( \hat{P}_0 = \frac{1}{k} \sum_{i=0}^{k-1} \tilde{P}_i \).

   3) **Unfold** the average point \( \hat{P}_0 \) by applying back the symmetry element \( g_i \). We obtain the unfolded points \( \{\tilde{P}_i\}_{i=0}^k \), where \( \tilde{P}_i = g_i \hat{P}_0 \).

   4) The first three steps are applied independently to each orbit. The CSM is calculated by averaging the deviation of each orbit from perfect symmetry \( \frac{1}{n} \sum_{i=0}^{n-1} \|P_i - \hat{P}\|^2 \).

An example of the algorithm is shown in Figure 15, for a single orbit of the C3 symmetry group, namely, the rotational symmetry group of order 3. For a set of orbits, we calculate the CSM independently for every orbit, with the appropriate symmetry operation applied about the center of mass of all points rather than about the origin. This algorithm can be implemented for all symmetry groups in any dimension. Proof and details can be found in [65, 68, 26]. An example of a hexagon and its CSM value and symmetry transform for various symmetry groups is given in Figure 16.
Figure 16. Hexagon and its CSM value and symmetry transform for various symmetry groups (from [26]).

3.3.1. CSM in Physics and Chemistry

Symmetry is closely associated with the chemical and physical characteristics of materials, whether natural or man-made [69]. The study of symmetry is important in chemistry and physics, where the symmetry of a molecule correlates with its chemical and physical properties [68, 70, 71]. The CSM has been used in the study of structures ranging from single molecules [65, 68, 70, 72, 73], through clusters [74], and up to crystals [75]. Correlations have been shown between CSM values and nuclear-magnetic resonance values [76], energy changes accompanying molecular isomerization [77], optical rotations [75], pressure and temperature structural effects [78], as well as enzymatic activity [79] and more [80].

3.3.2. Measuring Asymmetry in the Absence of Landmarks

Symmetry measures based upon landmarks are limited to single, relatively rigid, elements (e.g., vertebrate bones, arthropod limb segments and wings, and body outlines of fish) [49]. The CSM can quantify asymmetry when there are no landmarks, no consistent topology, no quantitative consistency, and sometimes no matching points (Figure 8C). Hence, CSM is not limited to rigid elements.

3.3.3. Analysis of Asymmetry Using Anchor Points

One approach to evaluating symmetry of partially consistent and inconsistent objects (see section 2.3) is the use of anchor points. In contrast to landmarks, anchor points are features selected on a specimen-by-specimen basis. They may vary in number, relative location, form, and characteristics among individuals. A classic example is the leaf venation pattern. Typically, the middle and secondary veins of leaves display planar, tree-like (i.e., bifurcating) geometry. The general layout of the veins consists of a central main vein, the symmetry axis from which secondary veins bifurcate on both sides.
Individual leaves may vary in the number of secondary veins, their bifurcation points along the main vein, their lengths, and their angles.

To apply anchor points, we first define a bifurcating structure as a set of points interconnected by line segments (see Figure 17A). The approach requires matching pairs of points to be deformed into symmetric pairs. With our bifurcating structure, this pairing of points reduces to a pairing of secondary veins. Figure 17B shows an example where points on paired veins have been matched (point $P_k$ matches point $Q_k$). When a secondary vein is ‘missing’, we insert a new zero-length vein, marked as two endpoints located at the bifurcation point. Figure 17C shows the paired points, where $P_1$ and $P_2$ are the endpoints of the new vein inserted as a match for $Q_1$ and $Q_2$, respectively. One can estimate the optimal pairing of points with a dynamic programming algorithm [23, 24].

Figure 17. A bifurcating structure consisting of a main vein and secondary veins branching off the main vein. A. The bifurcating structure is a set of points interconnected by segments. B. Points $P_k$ and $Q_k$ on paired veins have been matched. C. A new vein is inserted as points $P_1$ and $P_2$ (matching $Q_1$ and $Q_2$), the endpoints of the new vein. Points $P_1$, $P_2$, and $Q_2$ coincide.

Given a set of paired anchor points, one can use the CSM approach (section 3.3) to evaluate the bilateral symmetry of the structure. Given a paired set of veins (whether two existing veins or an inserted missing vein), the CSM of a pair of veins is computed using the folding-unfolding method [26] (see section 3.3). The CSM value of the entire leaf’s venation pattern is the average CSM value of both sets of matching veins (i.e., matching secondary veins). See Figure 18 for an example of the folding-unfolding method used on a matched pair of secondary veins. Note that the symmetric bifurcating structure closest to the original is a byproduct of the CSM method (Figure 18D). The unfolded points form a symmetric configuration ‘closest’ to the original in terms of the average mean squared distance (see Zabrodsky et al. [26] for further details and proofs). One can easily see the CSM calculations (and the folding-unfolding method) applied to all the veins simultaneously (independently). The CSM value of the whole structure is the average CSM value of each pair of matching veins.
The CSM approach constrains the bifurcating end-points of the secondary veins to remain positioned along the main vein. The approach allows veins to change length, translate bifurcation points, and add additional veins to the structure. Thus, the deformation applied by the CSM (and the folding-unfolding method) maintains the structure within the bifurcating structure class defined earlier.

**Figure 18.** Computing the CSM using the folding-unfolding method applied to two paired secondary veins, each represented by 2 points. A. Original bifurcating structure with matching points marked. B. Fold – Vein Q is reflected across the symmetry axis, obtaining the folded points $\tilde{Q}_1$ and $\tilde{Q}_2$. C. Average – The folded points are averaged with their matching points, obtaining the points $\hat{P}_1$ and $\hat{P}_2$. D. Unfold – The average points are reflected back across the symmetry axis, obtaining the unfolded points $\hat{Q}_1$ and $\hat{Q}_2$. The CSM value is the average distance squared between the original points and the corresponding unfolded points:

$$\frac{1}{4}[|P_1 - \hat{P}_1|^2 + |P_2 - \hat{P}_2|^2 + |Q_1 - \hat{Q}_1|^2 + |Q_2 - \hat{Q}_2|^2]$$

The CSM global approach has been extended to more complex bifurcating structures having 3rd and 4th order veins [81]. These structures are inherently hierarchical, where every sub-structure is itself a bifurcating structure, as can be seen in Figure 19.

**Figure 19.** An example of a bifurcating structure. Sub-structures and ranks are marked.
In bifurcating structures with three or more ranks, a distinction can be made between *Global Mirror Symmetry*, with the whole structure symmetric with respect to the main vein (the rank-1 vein) (Figure 20a), and *Local Mirror Symmetry*, with every substructure symmetric with respect to its respective main vein (a high-ranking vein) (Figure 20b). Thus, Frid, Raz, and Hel-Or [81] defined *Complete Symmetry*, which has both Global and Local Symmetry (Figure 20c). They then extended the CSM approach to Complete Symmetry of complex bifurcating structures.

**Figure 20.** Symmetry of bifurcating structures. a) Global Symmetry. b) Local Symmetry. c) Complete Symmetry.

To evaluate Complete Symmetry, the algorithm must simultaneously account for both local and global perspectives. The structure is traversed recursively, and the symmetry of the sub-structures is evaluated. These symmetry values are then combined into a single complete symmetry value. The algorithm combines both top-down and bottom-up approaches. The top-down part of the algorithm incorporates local symmetry, and the bottom-up part incorporates global symmetry. Figure 21 shows a flow chart of these two parts of the Complete CSM algorithm applied on a 4-ranked structure (Figure 21.1). The top-down part of the algorithm recursively selects sub-structures (marked in blue) and the bottom-up part of the algorithm imposes local symmetry, recursively up the structure (marked in green), resulting in Global Symmetry. The result of the Complete CSM algorithm is a CSM value as well as a Complete Symmetric structure (closest to the original in terms of CSM), as shown in Figure 22.
Figure 21. An example of the Complete CSM algorithm.
Figure 22. Resulting symmetric structure after applying the Complete CSM algorithm.

We used the Complete CSM approach on the leaves of fringed rue, *Ruta chalepensis* (Sapindales: Angiospermae), growing on the opposite slopes of "Evolution Canyon II," in Nahal Kziv, Israel. This is part of the "Evolution Canyon" project (see section 10). Using the Complete CSM, we demonstrated that leaves on the south-facing slope were significantly more asymmetrical, on average, than those on the north-facing slope, and those differences were stronger when using the 3rd and 4th order veins than when using only the 2nd order veins [81].

3.3.4. CSM-Developmental Stability Measurement

Fluctuating asymmetry (*i.e.*, symmetrical distribution around a mean of zero) is the most reliable measure of developmental instability. Fortunately, the CSM can absorb the standard statistics of fluctuating asymmetry. As with the landmark method [49], the CSM approach incorporates estimates of measurement error, to obtain an unbiased estimate of fluctuating asymmetry. In either approach, the $x$ and $y$ coordinates of the anchor points, or landmarks, contain information about measurement error (the difference in locations between replicate sets of digitized landmarks). The asymmetry is the true difference between the locations of the reflected landmarks on right and left sides; the variance components for both fluctuating asymmetry and measurement error may be estimated by using a modification of the standard mixed-model ANOVA [48]. In the next section, we present a method for quantifying measurement error based on fuzzy analysis.

The average right-left differences among all of the aligned landmarks yield a single, multivariate estimate of an individual’s deviation from perfect symmetry. A sample of these estimates can then be analyzed using the standard tests for fluctuating asymmetry. Moreover, it is easy to verify that the distribution is indeed fluctuating asymmetry (symmetrical right-left distribution around a mean of zero), and not a broken symmetry (directional asymmetry or antisymmetry).

Unlike bilateral structures, rotationally, dihedrally, or radially symmetrical structures do not have directionality. Thus, one cannot easily verify that asymmetry has been broken (and hence is not fluctuating asymmetry). We suggest adding two statistics (variance and entropy) to the CSM measurement. The CSM procedure already includes folding, finding the average of the folded points, and quantifying the distance from this average. Variance and entropy describe the distribution around the average, and are conceptually similar to the moments of a normal asymmetry distribution.
4. Measurement Error

Measurement error inflates variances, mean absolute deviations, and continuous symmetry measures. It is especially harmful in its effect on asymmetry distributions, generating mixed distributions that can generate spurious associations [82]. Thus, there is a need for replicate measurements in all studies of fluctuating asymmetry.

To obtain a true estimate of developmental instability, one must estimate measurement error and subtract it from the asymmetry mean square. The most widely used, but not exclusive, technique for performing this is a mixed-model ANOVA introduced by Leamy [83], and expanded and advocated by Palmer and Strobeck [48]. Nested ANOVA may also be used, but the advantage of the mixed-model design is that one can estimate directional asymmetry and measurement error simultaneously. A similar approach is available for landmark methods, and fuzzy analysis can be used for continuous symmetry measures.

4.1. Mixed-Model ANOVA

The ANOVA used most frequently for fluctuating asymmetry is a two-way, mixed-model ANOVA with replication. The main fixed effect is \( \text{sides} (S) \), which has two levels (left and right). The block effect is \( \text{individuals} (I) \), which is a random sample of individuals from a population. The \( S \times I \) interaction is a mixed effect. Finally, an error term \( (m) \) represents measurement error (replications within \( S \times I \)). Although individuals are randomly sampled from a population, this is not a randomized block design. Left and right sides cannot be assigned at random; individuals come with left and right sides already determined. The design is thus a nonrandomized observational design that incorporates blocking [84]. From the standpoint of fluctuating asymmetry, the nice aspect of this design is that one can simultaneously test for directional asymmetry and partition the total phenotypic variance into three random components.

Statisticians debate the expected mean squares and tests of significance in two-way mixed-model ANOVAs (see Samuels [84, 85] and commentary [86-88]). The main controversy is over whether \( \sigma^2_{S \times I} \) should appear in the expected mean square for individuals. The model used by Palmer and Strobeck [48], Samuels’ Model 2, includes \( \sigma^2_{S \times I} \). Her Model 1, however, excludes it. Although Samuels [84] favors Model 1, the best model for studies of fluctuating asymmetry is still unclear. According to Samuels, Model 1 is more appropriate for nonrandomized observational designs like those represented by fluctuating asymmetry. Indeed, her example of such a design is density of neurons in right and left hemispheres of the brain. Nevertheless, Model 2 is more appropriate when the goal of a mixed-model ANOVA is estimating components of variance. This is because all of the random terms in Model 2 are uncorrelated [84].

Table 1 shows an ANOVA table with expected mean squares for a mixed-model ANOVA. This is like the table given by Palmer and Strobeck [48]. In particular, we treat the number of sides as a constant, rather than as a variable. As with Palmer and Strobeck [48], we use expected mean squares associated with Model 2. The expected mean squares consist of variance components for each effect, and the appropriate coefficients. The effect called \( \text{sides} \) is the variation between the two sides; it is a measure of directional asymmetry. The effect called \( \text{individuals} \) is the variation among individual
genotypes; the *individuals* mean square is a measure of total phenotypic variation and it is random. The *individual by sides interaction* is the failure of the effect of individuals to be the same from side to side; it is a measure of fluctuating asymmetry and antisymmetry. It is a mixed effect. The error term is the measurement error; it is a random effect.

**Table 1.** Variance components $\sigma^2$ in a mixed-model ANOVA (after [55]). $N$ is the number of individuals and $R$ is the number of replicate measurements per individual. $<\sigma^2_S>$ is not a true variance component, since sides are fixed. $\sigma^2_m$ is a random component due to measurement error.

<table>
<thead>
<tr>
<th>Source</th>
<th>df</th>
<th>$MS$</th>
<th>Expected mean squares</th>
<th>Interpretation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sides</td>
<td>1</td>
<td>$MS_S$</td>
<td>$\sigma^2_m + R(\sigma^2_{SxI} + N&lt;\sigma^2_S&gt;)$</td>
<td>Directional asymmetry</td>
</tr>
<tr>
<td>Individuals</td>
<td>$N-1$</td>
<td>$MS_I$</td>
<td>$\sigma^2_m + R(\sigma^2_{SxI} + 2\sigma^2_i)$</td>
<td>Size/shape variation</td>
</tr>
<tr>
<td>Sides x Individuals</td>
<td>$N-1$</td>
<td>$MS_{SxI}$</td>
<td>$\sigma^2_m + R \sigma^2_{SxI}$</td>
<td>FA and antisymmetry</td>
</tr>
<tr>
<td>Replicates ($S x I$)</td>
<td>$N(R-1)$</td>
<td>$MS_{error}$</td>
<td>$\sigma^2_m$</td>
<td>Measurement error</td>
</tr>
</tbody>
</table>

The similarity between this design and Kozhara’s [89, 90] partitioning of total phenotypic variance into two components, factorial and stochastic, is evident. Total phenotypic variance (assuming no directional asymmetry) is the mean square for individuals

$$MS_I = \frac{1}{2}\text{Var}(l + r)$$

and the stochastic component (including measurement error) is equal to the interaction mean square

$$MS_{SxI} = \frac{1}{2}\text{Var}(l - r).$$

Kozhara’s factorial component is the total phenotypic variance minus the stochastic component ($MS_I - MS_{SxI}$). It is the variation among individuals; the stochastic component is the variation within individuals.

Although many researchers test for a significant interaction (and individuals) effect, it is superfluous to do so. Tests of significance in ANOVA are primarily reserved for fixed effects. A fixed effect is one whose levels the researcher has an interest in comparing (e.g., left and right sides) of the factor. For fixed effects, we compare the means. Thus, it is perfectly legitimate to test the significance of sides, since the null hypothesis is that the mean of the left side equals the mean of the right side ($H_0$: $\mu_l = \mu_r$). The two means are tested by comparing variances (the mean squares). For random effects, however, one does not (cannot) compare levels. For a random effect, the levels of the effect are a random sample from a large population. It is more meaningful to estimate variance components.
While it is possible to entertain the hypothesis that a particular variance associated with a random effect is not significantly different from zero (say $H_0: \sigma^2_{S \times I} = 0$, under Model 2), it does not make much sense to do so. For metric traits, no two individuals are identical, no two sides in an otherwise symmetrical individual are ever identical, and no two measurements of the same object are ever identical. Variation is pervasive. One can always find a difference, no matter how small. Thus, we know beforehand that the null hypothesis for a random effect is not true; it cannot be true. The only reason one might consider testing the null hypothesis that fluctuating asymmetry is not significantly greater than zero would be during trait selection. Traits having small amounts of asymmetry may not be worth the effort.

Instead of testing the significance of the random effects, researchers should estimate the three estimable variance components ($\sigma^2_m, \sigma^2_{S \times I}, \sigma^2_I$), and test only for differences between sides. The variance component for individuals ($\sigma^2_I$) is an estimate of the shape and size variation among individuals. The variance component for the interaction effect ($\sigma^2_{S \times I}$) is an estimate of the non-directional asymmetry (fluctuating asymmetry and antisymmetry). The variance component for replicates ($\sigma^2_m$) is an estimate of measurement error. Provided that the sides effect is insignificant, and that there is no obvious antisymmetry, one can interpret $\sigma^2_I$ and $\sigma^2_{S \times I}$ as factorial and stochastic variances. Their sum is the total phenotypic variance, minus measurement error.

If the sides effect is significant (i.e., $H_0: \mu_l \neq \mu_r$), the variance component estimate for the interaction (i.e., fluctuating asymmetry) may be biased, depending upon how directional asymmetry is manifested [52]. This is because the ANOVA’s additivity assumption may be violated. Nothing more can be done with the mixed-model ANOVA. Alternate methods of partitioning out directional asymmetry have been proposed by Graham et al. [52] and Van Dongen et al. [53]. The mixed-model ANOVA should be viewed then as the beginning, not the end of an asymmetry analysis.

An additional problem for most studies of fluctuating asymmetry is that the error models for size and asymmetry usually differ from those for measurement error. Size and asymmetry usually fit a multiplicative error model (see section 5.1). But measurement error is usually additive. This creates a problem because the additivity assumption is violated, even if the data are transformed. If measurement error is small, then it is best to use a log transform. If measurement error is large, however, it may be best not to transform the data. Either way is a compromise. A better solution is to take multiple replicate measurements, average them, and then at some later (random) time take several more and average them. This reduces the measurement error so that it does not seriously influence the analysis.

Nevertheless, the mixed-model ANOVA is widely misused [91]. Our main objection is that many researchers focus exclusively on tests of hypotheses rather than on estimating variance components [92, 93]. In reality, the one important test is for sides. Moreover, some researchers confuse mean squares and variance components. Just because measurement error ($\sigma^2_m$) is equal to or greater than fluctuating asymmetry ($\sigma^2_{S \times I}$) does not mean fluctuating asymmetry is insignificant. Finally, it is always best to express measurement error ($MS_{error}$ or $\sigma^2_m$) as a percentage of either the total phenotypic variation ($MS_I$) or the asymmetry variance ($\sigma^2_{S \times I}$).
4.2. Fuzzy Analysis for Quantifying Measurement Error

The CSM for fuzzy data [94] considers input points of imprecise location. Specifically, the locations of the input points are a probability distribution. For example, Figure 23a shows a point configuration whose locations are given by a normal-distribution function. The dots represent the point locations, and the rectangles represent their uncertainty (i.e., measurement error). The widths and lengths of the rectangles are proportional to their standard deviations. The CSM approach for fuzzy data [94] provides the most probable symmetric configuration represented by the fuzzy-input points and the probability distribution of the symmetry distance values for those points.

A variant of the folding method (presented in 3.3 for $C_n$-symmetry) is used to evaluate the most probable symmetric shape under the maximum likelihood criterion. This variant considers the fuzzy-input points as $n$ measurements, $Q_i \sim (P_i; A_i)$, where $P_i$ is the mean and $A_i$ is the covariance of the point-location distribution. The folding-unfolding method is applied to these $n$ measurements. (See Figure 23, which shows the method applied to a rotationally symmetrical object of order $n$. The approach for mirror symmetry, or any other symmetry, is similar.)

**Figure 23.** Folding a set of $n$ measurements: a) A configuration of 6 measurement points: $Q_0 \ldots Q_5$. b) Each measurement $Q_i$ is rotated by $2\pi/6$ radians about the centroid of the expected point location (marked as +), obtaining measurements $Q_0 \ldots Q_5$ (from [26]).

When given $m = qn$ measurements, they are divided into $q$ interlaced sets of $n$ points (each forming an orbit), and the folding method is applied separately to each set of measurements. Derivations and proof can be found in [94]. The folding-unfolding method results in the most probable symmetric shape, as well as a probability distribution of CSM values for the given set of measurements. Figure 24 displays distributions of the CSM value for various measurements. As expected, the distribution becomes broader as the uncertainties (the variance of the distribution) of the measurements increase.
Figure 24. Probability distribution of CSM values depends on measurement error. a-d) Measurement error of the points increases from left to right. e) Probability density and symmetry values (C$_6$-symmetry) for configurations a-d (from [26]).

5. Error Models and Size Scaling

Positive size scaling is a common problem. It occurs when asymmetry increases with size. If left uncorrected, it can easily generate spurious differences among populations. Larger individuals may be mistakenly judged more developmentally unstable than smaller individuals. Positive size scaling arises when growth is active (i.e., old tissue contributes to the production of new tissue), and errors are multiplicative [82]. Negative size scaling is also a potential problem, especially if measurement error is significant. It can generate spurious differences as well.

5.1. Error Models and Probability Distributions

Multiplicative errors are ubiquitous, whenever tissue at time t – 1 actively participates in the production of tissue at time t [95]. The tissue generating the structure is growing continuously. If the size of a structure $X_t$ at time $t$ is a random proportion of its size $X_{t-1}$ at a previous time $t-1$, such that $X_t = X_{t-1} + e_t X_{t-1}$, then $X_t$ is asymptotically lognormally distributed [96, 97]. Thus, multiplicative error generates a lognormal distribution (but see [98]). Examples of such active growth include leaves, petals and stems of plants, and bones and soft tissues of animals (Figure 25A).
Additive error occurs whenever tissue at time $t - 1$ does not actively participate in the production of tissue at time $t$. The tissue generating the inert structure does not grow. If the size of a structure $X_t$ at time $t$ is independent of its size $X_{t-1}$ at a previous time $t - 1$, such that $X_t = X_{t-1} + \varepsilon_t$, then $X_t$ is asymptotically normally distributed. Additive error generates a normal distribution. Examples of such inert growth include nails, scales, bristles, feathers, teeth, and exoskeletons. Measurement error is additive as well.

Errors, however, are rarely just multiplicative or just additive. Researchers usually deal with mixed error models and mixture distributions. A mixture of lognormal and normal distributions is most commonly encountered and has appeared in every study of leaf asymmetry we have undertaken [99-101].

**Figure 25.** Frequency distributions of lobe lengths of 300 fig leaves, *Ficus carica* (from [82]). A. Lognormal distribution of lobe length. B. Normal distribution of the same data after logarithmic transformation.

5.2. Transformations for Size Scaling

The most commonly used transformation for positive size scaling is essentially a coefficient of variation (Table 2). Either $(l - r)/(l + r)/2$ or $(l - r)/(l + r)$ are commonly employed [49]. Logarithmic transforms (Figure 25B), however, have better statistical properties if trait values fit a lognormal distribution. We suggest $\log l - \log r$ [82] (Figure 26), which is identical to Palmer and Strobeck’s [49] $\log(l/r)$. To evaluate the success of a log transform, $|\log l - \log r|$ should be regressed on $(\log l + \log r)$. 
Figure 26. Size-scaling of asymmetry (from [82]). \( l \) and \( r \) are lognormally distributed and correlated. A. Size-scaling of asymmetry \( l - r \) plotted against size \((l + r)/2\). B. Lack of size-scaling of asymmetry \( \log l - \log r \) plotted against size \((\log l + \log r)/2\).

A logarithmic transform of \( l \) and \( r \) may also remedy some leptokurtic asymmetry distributions [82], because the difference between two lognormal distributions is leptokurtic, and the difference between two normal distributions is normal. Consequently, a transformation changing a lognormal distribution of \((l + r)\) into a normal distribution, will likely change a leptokurtic distribution of \((l - r)\) into a normal distribution of \((\log l - \log r)\).

Problems can arise when log (or other) transformations are applied uncritically to correct size scaling (Figure 27A-B). It often occurs that a positive slope of \(|l - r|\) regressed on \((l + r)\) is replaced by a negative slope when \(|\log l - \log r|\) is regressed on \((\log l + \log r)\). This is usually, in our experience, caused by a mixture of lognormal and normal distributions. When the normally distributed part of the mixture is measurement error, one may simply average the replicates and use the averages. Measurement error decreases by \(\sigma^2 - ((\sigma^2/n)/\sigma^2)100\) with each replicate averaged.

Power transforms (Table 2) are useful when one cannot eliminate the additive error in a mixture distribution (Figure 27C). This might occur when there are not enough (or no) replicate measurements to work with, or when other sources of additive error are present.

One should not apply these transformations to methods that adjust landmarks to a unit centroid size. Doing so will amount to transforming the data twice. Moreover, mixture distributions are a likely problem with landmark methods, just as they are with conventional methods. If negative size scaling is a problem, we suggest averaging replicate \(x, y\) coordinates before proceeding with a landmark analysis.
**Figure 27.** Positive and negative size scaling of leaf asymmetry in *Olea europaea* from the “African” slope of “Evolution Canyon” I. A. Untransformed data showing positive size scaling. B. Log transformation generates negative size scaling. C. Power transformation ($\lambda = 0.6$) removes all size scaling. $R'$ and $L'$ are transformed variates.

**Table 2.** Common transformations for fluctuating asymmetry studies.

<table>
<thead>
<tr>
<th>Transformation</th>
<th>Equation</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Division by the mean</td>
<td>$d$ or $</td>
<td>d</td>
</tr>
<tr>
<td>Log transform</td>
<td>$\log l - \log r$</td>
<td>[99, 52, 82, 49]</td>
</tr>
<tr>
<td>Power transform</td>
<td>$[(l^\lambda - 1)/\lambda] - [(r^\lambda - 1)/\lambda]$ for $\lambda \neq 0$ $\log l - \log r$ for $\lambda = 0$</td>
<td></td>
</tr>
<tr>
<td>Half-normal transform</td>
<td>$(</td>
<td>d + 0.00005</td>
</tr>
</tbody>
</table>

5.3. **Recommended Approaches**

Sample sizes in studies of fluctuating asymmetry should be as large as practical. Moreover, replicate measurements are essential, for the reasons discussed previously. If necessary, two or three replicates are not too much. Before deciding how many replicates to measure, it is worthwhile
estimating how much of the observed asymmetry variance is measurement error. Finally, combining more than one trait in a composite index of fluctuating asymmetry helps to maximize the power to reject the null hypothesis.

Composite indices of fluctuating asymmetry, combining data from more than one independent trait, are considerably more powerful than indices based on single traits [102]. According to Leung et al. [102], the simplest composite index involves computing a standardized, summed asymmetry value for each individual, and using Levene’s test to compare composite asymmetries of different groups. The asymmetry values are standardized to insure equal weight for different traits. Leung and colleagues standardize \( |d_i| \) by the average of that trait for the population. An alternative for highly leptokurtic data is to total the ranks of the asymmetry values.

The choice of traits to study is often dictated by convenience. Nevertheless, some traits may have greater inherent variation than others. In plants, for example, leaves seem to be more variable than flowers [103]. This has been attributed to the functional importance of flower symmetry in attracting pollinators. In animals, functionally important traits, such as those involved in locomotion, are less variable than functionally unimportant traits, such as foramina [104]. In general, functionally unimportant traits, including sexually-selected ornaments, may be more sensitive to stress than functionally important traits [105].

In addition to morphometric characters, meristic (i.e., countable) characters are useful. In fact, they are often more variable and less canalized than morphometric characters [106]. Nevertheless, they have a built-in bias caused by thresholds in the continuous morphogen distribution underlying the discrete trait. Young [107] has developed an unbiased maximum likelihood metric for meristic traits, and established a general method to remove bias caused by counting errors.

Fluctuating asymmetry must be distinguished from directional asymmetry and antisymmetry [6, 48]. These two broken symmetries are, nevertheless, interesting [50, 51], and may increase under stress. They should, however, be treated separately from fluctuating asymmetry. Occasionally, an asymmetry distribution may be partitioned into fluctuating, directional, and antisymmetric components [52, 53].

In addition to reporting the first and second moments of \( d_i \) (location and variance), one should also report the third and fourth moments of the distribution (i.e., skew and kurtosis). Moreover, for the sake of future meta-analyses, one should report both signed and unsigned asymmetries. For a full discussion of sampling and statistical considerations, see Palmer and Strobeck [49].

Finally, researchers will want to compare fluctuating asymmetries among populations. This is most often accomplished using analysis of variance. Levene’s test, a one-way ANOVA on \( |l - r| \), is often recommended [49]. If the assumptions of the analysis of variance are violated, nonparametric approaches are also an option. In addition to these frequentist approaches, Bayesian approaches are also available [108].

6. Developmental Homeostasis, Canalization, and Developmental Stability

The stability of development is one of its most general characteristics [109]. Consider the remarkable similarity of identical (monozygotic) twins, or the symmetrical wings of a butterfly. To explain this stability, Waddington [110] proposed the concept of developmental homeostasis (or
homeorhesis), the stabilized flow of a developmental trajectory. Schmalhausen [111] arrived independently at the same concept, which he called autoregulation. Moreover, today’s systems biologists use the term robustness in more or less the same way [112].

Developmental homeostasis has two independent components: canalization and stability [110, 13, 14]. Canalization is the stability of development under different environmental and genetic conditions. Developmental stability, on the other hand, is the stability of development under constant environmental and genetic conditions.

Canalization is assessed either by raising individuals having the same genotype in different environments (environmental canalization) or by raising individuals having different genotypes in the same environment (genetic canalization). The converse of environmental canalization is developmental plasticity [113]. To demonstrate environmental canalization, Waddington [114] raised Bar mutants of Drosophila melanogaster at two different temperatures. At 18°C, flies had more than 150 facets in both eyes, but at 25°C they had fewer than 60. By selecting for increased canalization, he was able to reduce the difference to fewer than six facets in some lines. Consequently, canalization is heritable.

Stability is the ability of a system to correct minor fluctuations. Doing so requires feedback and the ability to detect fluctuations (or perturbations). Development is stable if a developmental trajectory returns to its original course after having been perturbed. But stability is not the whole story. Homeostasis also involves buffering (i.e., resilience). Buffering refers to the ability of a system to minimize, or soften, perturbations. It is analogous to C. S. Holling’s [115, p. 17] concept of resilience, which he defined as “the ability to absorb changes of state variables, driving variables, and parameters, and still persist.”

To understand developmental instability, one must distinguish fluctuations and perturbations. Fluctuations are intrinsic deviations spontaneously generated by the system [116]. Perturbations, on the other hand, are local changes communicated from the environment [116]. Perturbations can obviously generate fluctuations, but the two concepts are nevertheless independent. Small perturbations, for example, can generate large fluctuations, and large perturbations can generate small fluctuations. Fluctuations are intrinsic; perturbations are extrinsic.

Developmental stability, then, involves stability, resilience, fluctuation, and perturbation. To use an analogy, consider an automobile and driver trying to maintain a stable trajectory on a highway. Feedback between driver and steering system represents the stability of the system, the integrity of the shocks and tires represents its resilience, the roughness of the road and the velocity and direction of the wind are perturbations, and the vehicle’s random variation around its trajectory represents fluctuation. Stability, resilience, and perturbation influence the roughness of the ride, which is analogous to developmental noise. If we assume perturbations are small and constant, or nearly so, then we can estimate the stability and resilience of the system by examining its fluctuations.

One can estimate developmental instability, the converse of developmental stability, by raising genetically identical individuals in a common environment. Because genotype and environment are controlled, the residual variation (except for measurement error) must be random developmental variation (developmental noise). A second way of measuring developmental instability is to examine random variation between right and left sides of traits that are, on average, bilaterally symmetrical. Both sides of a symmetrical structure are genetically identical. Moreover, they have had a similar
history of gene activity. Finally, they have experienced the same environment. This is fluctuating asymmetry.

7. Random Developmental Variation

Fluctuating asymmetry measures stochastic variation and deterministic variation indistinguishable from stochastic variation [51]. As mentioned previously, both developmental stability (including resilience) and perturbation influence the stochastic variation one observes. The influence of perturbation, however, is usually small, so the observed variation is largely developmental instability. (We discuss the distinctions between stress and perturbation later in this paper.)

7.1. Nature, Nurture, and Noise

Fluctuating asymmetry is a stochastic component of phenotypic variation [117]. When one partitions total phenotypic variation ($\sigma^2_p$) into genetic ($\sigma^2_g$) and environmental ($\sigma^2_e$) components, fluctuating asymmetry is part of the environmental component [118]. But the stochastic component is often as large as, or larger than, the genetic and true environmental components. Consequently, several authors have argued that it should stand on an equal footing [119, 120, 117, 121]. Kozhara [89, 90], as mentioned previously, decomposes $\sigma^2_p$ into factorial ($\sigma^2_f$) and stochastic ($\sigma^2_s$) components. The factorial component is the variation among individuals, and the stochastic component is the variation within individuals. For symmetrical traits, $\sigma^2_p = \frac{1}{2}\text{Var}(l + r)$, and $\sigma^2_f = \frac{1}{2}\text{Var}(l + r) - \frac{1}{2}\text{Var}(l - r)$. The factorial component combines genetic and environmental variation.

Developmental noise arises at multiple levels: molecular, cellular, tissue, and organ-levels. At the molecular level, for example, gene expression is inherently noisy [122-124]. Elowitz et al. [125] showed that random variation in the expression of identical promoters in *Escherichia coli* influences numbers of cyan and yellow fluorescent proteins in each bacterial cell. This variation at the molecular level generates visible color variation at the cellular level. Random variation may also arise at the cellular level. Random cell-cell interactions, for example, may contribute to variation within a three-dimensional matrix [126]. Moreover, cell migration has a random component partly under genetic control [127]. At the tissue level, the induction of one tissue by a neighboring tissue contains stochastic elements. During embryonic development in vertebrates, for example, diffusible signals induce ectodermal cells overlying the notochord to develop into the neural plate. Diffusion is a stochastic process: the net transport of matter from a region of higher concentration to one of lower concentration by random molecular motion [128]. In *Drosophila*, random variation in morphogen gradients is minimized by a network of extracellular proteins [129].

7.2. Deterministic Chaos

In addition to noise, deterministic chaos contributes to some of the stochastic variation. It resembles noise, and has its origins in nonlinear feedback [51, 130]. Moreover, delays in feedback loops may interact with noise to generate oscillations in gene expression [131]. In our view, much of the variation regarded as stochastic may include deterministic components.
7.3. Population and Individual Fluctuating Asymmetry

Population estimates of fluctuating asymmetry are usually far more useful and reliable than individual estimates. For bilateral fluctuating asymmetry, only one degree of freedom is associated with the estimate of individual asymmetry. In contrast, population estimates have \( n - 1 \) degrees of freedom, where \( n \) is the sample size. One simply cannot say much about the developmental instability of a single individual from a single measurement.

This admonition against individual fluctuating asymmetry applies only to non-modular organisms. One can reliably estimate individual fluctuating asymmetry (and consequently developmental instability) in modular organisms having many repeated parts. Plants, for example, have tens to hundreds of leaves, flowers, and branches. Cowart and Graham [99] sampled 60 leaves from each of five fig plants, *Ficus carica* L. (Moraceae: Angiospermae), and concluded there were significant differences in leaf asymmetry among the five individuals; the smallest of the five plants had the most symmetrical leaves. Other studies have sampled up to 10 flowers to estimate individual developmental instability [132].

Individual fluctuating asymmetry has been applied, with much controversy, to studies of sexual selection and individual fitness. In this review, we mostly refer to population estimates of fluctuating asymmetry.

8. Origins of Developmental Homeostasis

The most fundamental adaptation is the harmonious physiological and developmental functioning of an organism [133, 134]. Consequently, both physiological and developmental homeostasis should be important components of fitness [135]. Physiological homeostasis, for example, maintains an organism’s internal environment, permitting it to function under a range of external conditions. Developmental homeostasis produces consistent phenotypes for a particular genotype and environment.

8.1. Adaptation, Coadaptation, and Heterozygosity

The genetic basis of fitness and, by association, developmental stability, has been controversial for nearly 60 years [136]. The roles of heterozygosity and genomic coadaptation have been especially contentious. Dobzhansky [137, p. 301], in an influential paper, attributed the higher fitness of inversion heterozygotes in *Drosophila pseudoobscura* to polygenic complexes that “have become mutually adjusted, or coadapted, by natural selection in the course of the evolutionary process.” Because the inversions hinder crossing over, they maintain high levels of heterozygosity. Nevertheless, Dobzhansky’s [138] emphasis was clearly on coadapted gene complexes rather than allelic heterozygosity per se. In contrast, Lerner [134, p. 6], in his classic *Genetic Homeostasis*, suggested that coadapted heterozygosity was important: “ontogenetic self-regulation (developmental homeostasis) is based on the greater ability of the heterozygote to stay within the norms of canalized development.” His emphasis was clearly on the greater fitness of allelic heterozygotes (overdominance). In the ensuing years, the overdominance hypothesis has fallen into disfavor [139, 140] (but see [141]).
Nevertheless, there are several good examples of fitness overdominance [142-144]. Invariably, they involve genes for respiratory enzymes and cellular energy homeostasis, such as phosphoglucomutase and isocitrate dehydrogenase in rainbow trout [143] and adenylate kinase, phosphoglucomutase, octopine dehydrogenase, and glutamate-oxaloacetate transaminase in the deep-sea scallop Placopecten [142].

Parsons [145, p. 592] has argued that energetic efficiency is “a measure of fitness in a stressed world.” Thus, the best examples of fitness overdominance are those involving energy efficiency [146]. Nevertheless, the actual mechanism whereby such allelic variation is adaptive remains elusive. Heterozygotes can produce \( n + 1 \) versions of the same enzyme, where \( n \) is the number of protein subunits. They can produce two different versions of the same monomeric enzyme, three different versions of the same dimeric enzyme, and five different versions of the same tetrameric enzyme. As we suggest later in this review, the superiority of heterozygotes may be related to the distributed robustness of metabolic networks (i.e., their topology). Because these enzymes are involved in the synthesis of ATP and NADPH, they are linked to every reaction in the cell requiring energy. Thus, even a small advantage may be multiplied across the metabolome by the number of links.

Overdominance, however, is only one advantage of heterozygosity. Heterogeneous habitats can maintain multiple allelic systems [147], especially in the presence of stress, across Israel [148-152] and across the globe [153]. Consequently, the hypothesis that heterozygosity modulates fitness has been demonstrated locally, regionally, and globally.

In contrast to heterozygosity, genomic coadaptation has received much more attention from those studying fluctuating asymmetry [154-157]. Genomic coadaptation refers to the coadapted, harmonious interactions among gene loci. Selection at one locus influences selection at other loci, in a system of mutual interaction. Inbreeding and hybridization disturb these interactions, and both have been associated with increased developmental instability [157, 158].

Hybrid zones, though, are especially enlightening. Under the overdominance hypothesis, both fitness and developmental stability should be greater in hybrid zones between species and subspecies, because hybrids have greater heterozygosity. Under the coadaptation hypothesis, however, fitness and developmental stability should be reduced, because the genomes of hybrids have been disturbed. Most natural hybrid zones support the coadaptation hypothesis [157]. For example, in the blind mole rat, Spalax, selection against hybrids in narrow hybrid zones may rise to 90% [159]. Several hybrid zones, however, including those between subspecies of Mus musculus, Artemisia tridentata, Hyla spp., Sceloporus grammaticus, and Lepomis macrochirus, have hybrids more developmentally stable than their parental subspecies [157]. The situation in big sagebrush, A. tridentata, is interesting because the hybrids have higher fitness and stability, but only in the center of a narrow hybrid zone [160, 161]. They have lower fitness and stability elsewhere.

Directional selection should also increase fluctuating asymmetry [7] by disrupting coadapted genomes, but there is virtually no evidence it does so, at least in Drosophila [162, 163].

An additional consequence of the relationship between genetic variation (heterozygosity and homozygosity) and fluctuating asymmetry is that small island populations [7] and populations on the edge of a species range [164] should have greater asymmetry. There are several good examples of both in the literature [7, 165, 166].
The genetic architecture of fluctuating asymmetry is still largely unknown [158]. In general, narrow-sense heritabilities ($h^2$) for fluctuating asymmetry are small, but not zero [158, 167]. Nevertheless, estimates of heritability require large sample sizes, and most are not large enough to distinguish between heritabilities $h^2$ of 0.1 and 0.5 [168, 169]. In contrast, epistatic interactions account for much of the genetic variation in fluctuating asymmetry within laboratory populations of Mus musculus [170, 158].

The search for specific genes modulating phenotypic variation, and influencing developmental stability, has focused on those coding for molecular chaperones, such as Hsp90. Some studies find that its role, and that of Hsp83, is minimal [171-173], while others find a significant role [174]. Other research supports the hypothesis that environmental canalization and developmental stability share underlying regulatory mechanisms, but environmental and genetic canalization do not [175]. Moreover, fluctuating asymmetry and phenodeviants in Drosophila bipectinata share a common buffering system [176]. Understanding the underlying basis of developmental instability is critically important to the future development of the field [105]. There is still much work to do.

8.2. Distributed Robustness

The robustness of living organisms arises from redundancy and distributed robustness [112, 177]. Redundancy involves duplicate parts: genes, cells, etc. If there are two or more identical copies of a particular gene, inactivating one of them will have minimal impact on fitness. Distributed robustness, in contrast, involves the complexity of genetic and metabolic networks. If a link in a network is broken, it may often be bypassed. Wagner and colleagues [177, 178] believe distributed robustness is more important than redundancy.

If distributed robustness is the main contributor to developmental stability, then the topology of genomic and metabolic networks should be critically important. These networks are termed small-world networks [179-181], and they are robust to perturbation [182, 183]. But a metabolic pathway’s Achilles’ heel is the highly connected nodes in the network. Error tolerance comes at a price [184]. Knock out a highly connected node and the system fails.

Networks consist of nodes and links [185]. In a metabolic network, the nodes are chemical intermediates (substrates), and the links are enzymatically mediated reactions (enzymes). A highly connected node is a hub. In a small-world network, the connectivity $P(k)$ of nodes follows a power-law, $P(k) \approx k^{-\gamma}$, distribution. Most nodes have few links, but a few hubs may have hundreds or thousands of links. The hubs connect the less connected nodes to the system. These systems are typically scale-free [179] and hierarchical [186].

In yeast, Saccharomyces cerevisiae, hubs buffer phenotypic variation. Working with 4,718 strains of haploid single-gene knockouts, Levy and Siegal [187] estimated the overall phenotypic variance resulting from single deleted genes. They called this the phenotypic potential, which is equivalent to the variation among clone mates in a common environment, an alternate estimator of developmental instability. Most deletions have almost no effect on phenotypic variation because they are not hubs.

What are the implications of distributed robustness and the network topologies for fluctuating asymmetry? At first glance, one might expect negative power-law (i.e., Pareto) distributions of fluctuating asymmetry because that is how the links are distributed. (This is not the distribution of $d = l$...
- \( r \), but the distribution of \( \text{Var}(d) \) or \( E|\xi - \mu| \) among different populations or genotypes.) If the response to a specific, local perturbation to a node or link is proportional to the connectedness of the node, then fluctuating asymmetry should also be distributed as a negative power-law. Clearly, this does not occur, because a small amount of noise is necessary for normal development and gene regulation [122, 123]. We have never seen a continuous trait that did not have some asymmetry. Thus, one would expect a skewed distribution with fat tails. The Double Pareto lognormal distribution is such a distribution; it is a mixture of lognormal and Pareto distributions. Babbitt and colleagues [188-190] have fit the double Pareto lognormal distribution to asymmetry data (though the data appear to contain artifactual antisymmetries). Nevertheless, the distribution may still be useful in testing the hypothesis that distributed robustness mediates developmental instability.

Under our model, most perturbations should have little effect on organism-wide developmental instability, unless they perturb a hub. These perturbations are probably responsible for most of the minor developmental noise. Stress, on the other hand, lessens energy efficiency, consequently involving several important hubs (metabolic intermediates). For example, stress-related decreases in ATP or NADH production should influence thousands of linked metabolic reactions. This hypothesis has important implications for fluctuating asymmetry as an indicator of stress: organisms should be far more robust to perturbations than scientists have imagined, but the effects of stress are more likely to manifest themselves at hubs, not nodes.

8.3. Environmental Stress

Stress and perturbation are distinct concepts. Whereas perturbation is energy or mass communicated from the environment, stress is anything (physical, chemical, genetic, psychological, etc.) dissipating energy away from growth and production [191-194, 145]. By doing so, stress usually limits productivity [195]. Nutrient loading, however, can increase productivity, but qualifies as a stress if it simultaneously causes a decrease in the efficiency of energy metabolism [145]. Stress also interferes with stability and resilience of development, though we have a poor understanding of the mechanisms.

According to Escós et al. [196, p. 331], “defining stress exclusively in terms of production decline may be misleading.” They define stress as “any environmental factor that causes a reduction in the efficient use of energy, causing a reduction in developmental homeostasis, and finally reducing long-term, total inclusive fitness.”

Stress might lessen developmental stability by dissipating energy away from feedback loops, either by changing gene-expression patterns [197] or by changing the flux through metabolic pathways [145]. Expression of heat-shock (stress) proteins, for example, has negative effects on growth and development [198]. Stress might also change the topology of genetic and metabolic networks. Salt-tolerant varieties of rice maintain the expression of homeostatic genes involved in energy supply, transcription, cell transport, cell wall synthesis, and DNA synthesis in the face of salt stress; salt-sensitive varieties down-regulate these same genes prior to death [199].
9. Applications

Fluctuating asymmetry has numerous applications. Most notably, it is an (albeit controversial) index of environmental and genetic stress. Furthermore, developmental instability, which it measures, may be correlated with individual fitness, and is widely viewed as an index of adaptation and coadaptation. Recently, a few scientists have used fluctuating asymmetry to study developmental integration, under the assumption that parts sharing asymmetries must share a common developmental basis. Finally, we explore several applications beyond the usual fluctuating bilateral asymmetry, such as fluctuating translational asymmetry. Throughout this section, we present “Evolution Canyon,” at Mount Carmel, Israel, and other “Evolution Canyons” as important model systems for fluctuating asymmetry.

9.1. Stress

Fluctuating asymmetry is an indicator of environmental (Table 3) and genetic (Table 4) stress. Nevertheless, it is not without its detractors and skeptics. Presumed stressors often have no effect on asymmetry, even while decreasing growth and increasing mortality [200]. Moreover, fluctuating asymmetry can be a poor indicator of both stress and individual fitness [201]. Such findings, however, do not invalidate fluctuating asymmetry as an indicator of stress. Here, we discuss both sides of the controversy and argue that fluctuating asymmetry is indeed a valuable indicator, if it is put in perspective.

To begin with, fluctuating asymmetry seems a less sensitive indicator of stress than specific physiological and morphological modifications. These modifications will have evolved to minimize even minor stress. Consequently, they should be exquisitely sensitive to it, providing the stress is a normal part of the organism’s evolutionary history. Nevertheless, this is also an advantage for fluctuating asymmetry, because adaptive modifications contribute to the resiliency of development. They buffer stress. According to West-Eberhard [202, p. 507], “an environmental condition that was originally stressful or extreme, and disadvantageous to the organism, eventually, if recurrent, may become part of normal development and would no longer be regarded as a ‘stress’.” Fluctuating asymmetry, on the other hand, is never (or rarely) adaptive, and it does not contribute to the resiliency of development.

Some small amount of random variation, however, is necessary for normal development. Some developmental decisions at the cellular level are best left to chance [203]. Moreover, when Mather [5] selected for decreased asymmetry of sternopleural bristles in Drosophila melanogaster, the result was a dramatic decline in fitness, which is contrary to the common notion that zero asymmetry is optimal. When selection was relaxed, fitness returned to normal. Elena and Sanjuán [204] discuss similar trade-offs between robustness and fitness in viruses.

Decreased growth is often a more sensitive indicator of stress than is fluctuating asymmetry [205, 206]. This is unsurprising because a decline in growth is simultaneously a direct indicator of stress (i.e., stress may dissipate energy away from growth [207]) and a likely adaptive modification maintaining lifetime fitness.
Stressed individuals not shunting energy away from growth may have lower lifetime fitness [208-210]. In plants, for example, the cost of reproduction often increases with size in a habitat-dependent way [211]. In other words, there should be an optimum size for reproduction, and it should vary with habitat. The optimum size is usually smaller under stressful conditions. Consequently, it is difficult to say with certainty whether smaller size indicates stress, or is simply a way of avoiding stress.

Excessive nutrients, beyond the adaptive norm, are an exception to the generalization that small size indicates stress. Excess nutrients can simultaneously increase both growth and asymmetry [212, 22, 213, 214], and growth and mortality [215]. Saline solutions, on the other hand, can stop plant growth completely, with no increase in fluctuating asymmetry [216, 207, 22].

There may also be a trade off between rapid growth and developmental stability. In some studies, faster growth is associated with greater asymmetry (but see Pélabon et al. [217]). Martel et al. [218], for example, stimulated faster leaf growth in the birch Betula pubescens by breaking apical dominance. Those treated leaves reached the same size as the control leaves, but did so in a shorter time. They also had more asymmetrical leaves. Wells et al. [219] found that Brazilian boys with the fastest early growth were more asymmetrical at age nine, even though both groups attained the same average size. Wells and colleagues attributed the effect to greater compensatory growth in small newborns.

Leaf size of 12 plant species at “Evolution Canyon,” Israel (see sections 10.2 and 10.3), demonstrates how phenotypic modifications are more sensitive to stress than fluctuating asymmetry [220, 101]. The main stresses for plants at “Evolution Canyon” are water availability and evapotranspiration on the south-facing “African” slope and light availability on the north-facing “European” slope. To minimize water loss on the south-facing slope, all 12 species there have smaller leaves. Moreover, larger leaves on the north-facing slope maximize light interception, and consequently photosynthesis. Besides leaf size, plants on the opposing slopes differ in leaf thickness [220]. In contrast to these phenotypic modifications, our preliminary results suggest less dramatic differences in leaf asymmetry between the 12 populations on the two slopes [101].

The leaf size example at “Evolution Canyon” begs the question: was stress still present after the modification? It was obviously present before the modification, and undoubtedly triggered the modification, but was it present for the development of each leaf? Adaptive modifications are not easily reversed [202], so they can indicate only that stress occurred sometime during the development of the leaf.

In a similar study, Escós et al. [196] examined fluctuating asymmetry of Anthyllis cytisoides (Fabaceae: Angiospermae), on north- and south-facing slopes of Rambla Honda Valley, near Tabernas, Spain. Unlike “Evolution Canyon,” which is Mediterranean and mesic, this microsite is arid (218 mm rainfall per year), with most rain falling in the winter. Plants on the north-facing slope had larger leaves, longer shoots, allocated more resources to reproduction, and had greater fractal dimension (a measure of how much the plant fills space). The plants maintained developmental stability at the expense of productivity. The less productive plants on the more arid south-facing slope, however, had lower fluctuating asymmetry than those on the north-facing slope during an extreme drought. The authors attributed the difference to the burden of extra biomass in the plants on the north-facing slope. As additional evidence, grazed plants on both slopes had a lower water deficit, better survival, and increased developmental stability, presumably because grazing removed the burden of extra biomass.
Besides aridity, other environmental stresses have been associated with higher fluctuating asymmetry (Table 3). For example, dental asymmetry of the Middle East blind mole rat, *Spalax ehrenbergi* (Spalacidae: Mammalia), in Israel is unrelated to aridity. Asymmetry, however, increases with altitude, minimum January temperature, and the amount of indurated (*i.e.*, compacted) soil [221].

**Table 3.** Natural environmental stress and fluctuating asymmetry: a small sampling of studies and stressors. All studies are of fluctuating bilateral asymmetry.

<table>
<thead>
<tr>
<th>Stressor</th>
<th>Taxa</th>
<th>Traits</th>
<th>Result ¹</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water limitation/drought</td>
<td><em>Quercus ilex</em>, wet site</td>
<td>leaf</td>
<td>↑FA</td>
<td>[222]</td>
</tr>
<tr>
<td></td>
<td><em>Quercus ilex</em>, dry site</td>
<td>leaf</td>
<td>0</td>
<td>[222]</td>
</tr>
<tr>
<td></td>
<td><em>Phaseolus vulgaris</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[223]</td>
</tr>
<tr>
<td></td>
<td><em>Salix sericea</em></td>
<td>leaf</td>
<td>0</td>
<td>[224]</td>
</tr>
<tr>
<td></td>
<td><em>Salix eriocephala</em></td>
<td>leaf</td>
<td>0</td>
<td>[224]</td>
</tr>
<tr>
<td>Flooding</td>
<td><em>Betula pubescens</em></td>
<td>leaf</td>
<td>0</td>
<td>[218]</td>
</tr>
<tr>
<td>High salinity</td>
<td><em>Glycine max</em></td>
<td>leaf</td>
<td>0</td>
<td>[216]</td>
</tr>
<tr>
<td>UV-B radiation</td>
<td><em>Dimorphotheca sinuate</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[225]</td>
</tr>
<tr>
<td>Heat shock</td>
<td><em>Bicyclus anynana</em></td>
<td>eyespots</td>
<td>0</td>
<td>[226]</td>
</tr>
<tr>
<td></td>
<td><em>Scaphophaga stercoraria</em></td>
<td>tibia and wing</td>
<td>↑FA</td>
<td>[227]</td>
</tr>
<tr>
<td>High elevation/cold</td>
<td><em>Betula pubescens</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[228]</td>
</tr>
<tr>
<td>Food limitation</td>
<td><em>Sternus vulgaris</em></td>
<td>primary feathers</td>
<td>↑FA</td>
<td>[229]</td>
</tr>
<tr>
<td></td>
<td><em>Scaphophaga stercoraria</em></td>
<td>tibia and wing</td>
<td>0</td>
<td>[227]</td>
</tr>
<tr>
<td></td>
<td><em>Coenagrion puella</em></td>
<td>femurs, wings</td>
<td>0 ²</td>
<td>[230]</td>
</tr>
<tr>
<td></td>
<td><em>Cyrtodiopsis dalmanni</em></td>
<td>eye stalks, wings</td>
<td>0</td>
<td>[200]</td>
</tr>
<tr>
<td>Nutrient limitation</td>
<td><em>Acer platanoides</em></td>
<td>leaf</td>
<td>0</td>
<td>[205]</td>
</tr>
<tr>
<td></td>
<td><em>Betula pendula</em></td>
<td>leaf</td>
<td>0</td>
<td>[205]</td>
</tr>
<tr>
<td>Nitrogen enrichment</td>
<td><em>Betula pubescens</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[213]</td>
</tr>
<tr>
<td></td>
<td><em>Lythrum salicaria</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[214]</td>
</tr>
<tr>
<td>Competition</td>
<td><em>Salix sericea</em></td>
<td>leaf</td>
<td>0</td>
<td>[224]</td>
</tr>
<tr>
<td></td>
<td><em>Salix eriocephala</em></td>
<td>leaf</td>
<td>0</td>
<td>[224]</td>
</tr>
<tr>
<td>Insect attack</td>
<td><em>Betula pubescens</em></td>
<td>leaf</td>
<td>0</td>
<td>[228]</td>
</tr>
<tr>
<td>Grazing/browsing</td>
<td><em>Betula pubescens</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[218]</td>
</tr>
<tr>
<td>Infection</td>
<td><em>Salix sericea</em></td>
<td>leaf</td>
<td>0</td>
<td>[224]</td>
</tr>
<tr>
<td></td>
<td><em>Salix eriocephala</em></td>
<td>leaf</td>
<td>0</td>
<td>[224]</td>
</tr>
<tr>
<td>Natural disaster</td>
<td><em>Peromyscus leucopus</em></td>
<td>femur length</td>
<td>↑FA</td>
<td>[231]</td>
</tr>
<tr>
<td></td>
<td><em>P. maniculatus</em></td>
<td>femur length</td>
<td>↓FA</td>
<td>[231]</td>
</tr>
</tbody>
</table>

¹↑FA indicates a significant increase in fluctuating asymmetry. ↓FA indicates a significant decrease in fluctuating asymmetry. 0 indicates no significant change.

²Food limitation facilitated the effect of pesticides, increasing fluctuating asymmetry before the molt.
Fluctuating asymmetry is also an indicator of genetic stresses, such as inbreeding and outbreeding [232]. As with environmental stress, many unresolved questions remain. Several meta-analyses, for example, have failed to find significant associations between heterozygosity and developmental instability [233].

Hochwender and Fritz [224], though, designed an especially elegant experiment comparing the effects of genetic and environmental stress on two species of willow (Salix sericea, S. eriocephala, and their F₁ and F₂ hybrids (Salicaceae: Angiospermae)). Although they sampled only one leaf from each plant, they sampled leaves from 2359 plants. Genetic stress was more important than environmental stress. F₂ hybrids had the greatest leaf asymmetry, but water stress, pathogen attack, and competition had no effect on leaf asymmetry. Fluctuating asymmetry also decreased with plant size.

Fluctuating asymmetry increases when adaptive modifications fail to buffer stress. Therefore, even if fluctuating asymmetry is less sensitive than adaptive modification, it indicates more severe stress, and it indicates when stress has exceeded an organism’s homeostatic abilities. In particular, it indicates when stress has influenced developmental stability.

Table 4. Genetic stress and fluctuating asymmetry: a small sampling of studies and stressors.

<table>
<thead>
<tr>
<th>Stressor</th>
<th>Species</th>
<th>Traits</th>
<th>Result¹</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inbreeding</td>
<td>Scathophaga stercoraria</td>
<td>tibia and wing</td>
<td>0</td>
<td>[227]</td>
</tr>
<tr>
<td>Hybridization</td>
<td>Dalechampia scandens</td>
<td>leaf</td>
<td>0</td>
<td>[234]</td>
</tr>
<tr>
<td></td>
<td>Piriqueta caroliniana</td>
<td>leaf</td>
<td>↑FA</td>
<td>[235]</td>
</tr>
<tr>
<td></td>
<td>Salix spp.</td>
<td>leaf</td>
<td>↑FA</td>
<td>[224]</td>
</tr>
<tr>
<td></td>
<td>Enneacanthus spp.</td>
<td>meristic</td>
<td>↑FA</td>
<td>[154]</td>
</tr>
<tr>
<td>Directional selection</td>
<td>Drosophila melanogaster</td>
<td>wing shape</td>
<td>0</td>
<td>[217]</td>
</tr>
<tr>
<td>Heterozygosity</td>
<td>Alectoris chukar</td>
<td>toe length</td>
<td>0</td>
<td>[236]</td>
</tr>
<tr>
<td>Molecular chaperones</td>
<td>Drosophila melanogaster</td>
<td>bristles, wings</td>
<td>0</td>
<td>[171]</td>
</tr>
<tr>
<td></td>
<td>(Hsp90, Hsp83)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Drosophila melanogaster</td>
<td>wing shape</td>
<td>0 and ↑FA²</td>
<td>[173]</td>
</tr>
<tr>
<td></td>
<td>Arabidopsis thaliana</td>
<td>hypocotyl</td>
<td>↑Vₚ³</td>
<td>[174]</td>
</tr>
<tr>
<td>DNA damage</td>
<td>Dimorphotheca sinuate</td>
<td>leaf</td>
<td>↑FA</td>
<td>[225]</td>
</tr>
<tr>
<td>Transposons</td>
<td>Drosophila melanogaster</td>
<td>bristles</td>
<td>0</td>
<td>[237]</td>
</tr>
</tbody>
</table>

¹↑FA indicates a significant increase in fluctuating asymmetry. ↓FA indicates a significant decrease in fluctuating asymmetry. 0 indicates no significant change.
² Increase in fluctuating asymmetry only for Hsp83 allele introgressed into a control line. No effect of Hps90 inhibition.
³ Developmental instability was estimated as phenotypic variation (Vₚ) of hypocotyl length among clone mates. Because the plants were inbred, and the environment was standardized, Vₚ is measuring developmental noise.
9.2. Fitness

Evolutionary biologists sometimes use fluctuating asymmetry as an indicator of individual fitness, but they have done so with varying degrees of success [140, 161]. The promise of an easily measured component of fitness has not borne out. The initial optimism has been replaced with skepticism, and the belief that fluctuating asymmetry is a weak measure of developmental instability, and consequently a poor measure of individual fitness [238, 239, 201, 240]. The main problem is that with only two sides to a bilaterally symmetrical trait, only one degree of freedom is available to estimate a variance and a sample size $n = 2$ to estimate a mean absolute deviation. Given such small samples, the estimate of the underlying developmental instability is apt to be imprecise [241-243]. Estimates of the repeatability ($R$) of fluctuating asymmetry (i.e., proportion of the asymmetry variance due to developmental instability) average a low 0.08 [244].

The difference between left and right sides, the individual asymmetry, is actually an estimate of variation, too. In fact, the unsigned asymmetry, $|d| = |l - r|$, is exactly twice the mean absolute deviation of a sample $(l, r)$ of size $n = 2$. The mean absolute deviation is the mean of $|x_i - \mu|$, where the $x_i$s are the individual observations on left and right sides and $\mu$ is the mean. Consequently, the mean deviation is $\Sigma|x_i - \mu|/n$, and with $n = 2$, it may be reduced to $|x_l - x_r|/2$.

Of course, this criticism is irrelevant if one is working with a modular organism having multiple symmetrical parts (e.g., leaves, flowers, and branches of plants), because one can sample more than one repeated part. In fact, only the number of repeated parts limits the sample size. Consequently, one can estimate developmental instability of a single individual (or clone mate) with much greater precision.

Unfortunately, few studies have taken advantage of the potentially larger samples available with plants. Andalo et al. [245], for example, sampled three leaves and flowers from each plant, and Pélabon et al. [234] and Handy et al. [235] sampled one leaf from each plant. Unsurprisingly, these studies found no relationship between fluctuating asymmetry and individual fitness. Samples of modular parts from individuals should be at least 30-40, as they are in comparisons of fluctuating asymmetry at the population level.

To our knowledge, only one study in the literature [161] has attempted to establish a link between fluctuating asymmetry (a composite of three measurements on each leaf) and overall fitness (itself a composite of juvenile survival, numbers of seeds, and their germination rate) in a long-term (4-year) study. Leaves of big sagebrush *Artemisia tridentata* (Asteraceae: Angiospermae) were measured in a common-garden experiment involving three gardens, two subspecies, and three categories of hybrids. The common gardens were in the actual hybrid zone. Five leaves were sampled from each plant. In general, plants not native to a garden had lower fitness and higher leaf asymmetry. Fluctuating asymmetry was negatively correlated with fitness ($r = -0.495$, $P < 0.005$).

Further work is essential if fluctuating asymmetry is to be a trustworthy indicator of individual fitness [246]. In particular, we need to sample more traits on non-modular organisms, and we need larger sample sizes of repeated parts on modular organisms. We also need to eliminate, or reduce, measurement error by making replicate measurements, and we need to take size scaling and mixed-error distributions into account. Far too many studies use only one or two traits, use inadequate sample sizes, apply scaling uncritically, and disregard replicate measurements and mixed-error distributions.
9.3. Developmental Integration

Fluctuating asymmetry is a useful tool for evolutionary developmental biology because it reveals direct interactions among modular parts of organisms [247-255]. In particular, covariation of fluctuating asymmetries among traits is evidence they share developmental pathways [251]. Klingenberg and Zaklan [248], for example, studied morphological integration between developmental compartments of the *Drosophila* wing. Earlier studies had suggested that anterior and posterior compartments of the wing were distinct developmental modules; but landmarks spanning the entire wing show evidence of persistent covariation. The *Drosophila* wing is, therefore, a single developmental unit.

9.4. Diverse Fluctuating Asymmetries

Although most applications have dealt with fluctuating bilateral asymmetry, there are numerous examples of other kinds of asymmetry in the literature. We summarize some notable examples.

9.4.1. Fluctuating Rotational, Dihedral, and Radial Asymmetries

A 2-dimensional object has rotational symmetry of order \( n \) if it is invariant when rotated \( \frac{2\pi}{n} \) radians about the symmetry center of the object. This axis is the axis of rotational symmetry. Dihedral symmetry is the symmetry of a 2-dimensional object having both mirror symmetry and rotational symmetry. Radial symmetry is rotational symmetry with an infinite number of rotations.

Despite their potential application, no published models for fluctuating rotational, dihedral, and radial asymmetry take into account two- and three-dimensional geometry and shape [256, 22]. Nevertheless, Raz, Lefel, Hel-Or, Graham, and Nevo [257] are working on a novel model for quantifying fluctuating radial asymmetry. They are now applying it to bacterial and fungal colonies growing on plate culture.

As demonstrated earlier (see 3.1), measures of dispersion are easily generalized to many kinds of fluctuating asymmetry. \( \text{Var}(x_i) \), for example, is analogous to \( |l - r| \), and is a measure of individual dihedral and rotational asymmetry. The mean of \( \text{Var}(x_i) \) (or the standard deviation) is the actual measure of fluctuating asymmetry for a sample. Unfortunately, this method completely ignores shape and rotation. Therefore, it is usually a poor measure of fluctuating rotational, dihedral, and radial asymmetries. Occasionally, as in the lengths of ray flowers in the inflorescence of a sunflower, it may be the best approach.

A few studies have looked at fluctuating asymmetry of flowers displaying dihedral symmetry. Møller and Eriksson [256], for example, measured flower asymmetry as either the difference between two randomly chosen petals, or the difference between the longest and the shortest petals. The deviations from dihedral symmetry were reduced to one-dimensional measurements of length and the problem was approached in terms of bilateral asymmetry (i.e., only two measurements were made on each flower or inflorescence, and the statistics of bilateral fluctuating asymmetry were applied).
9.4.2. Fluctuating Translational Asymmetry

Translational symmetry occurs in the internode lengths of plants and algae [22] and in the bristle counts of metameres (segments) in arthropods [3]. When this symmetry has not been broken, the analysis is straightforward; the within-individual variance is a measure of individual asymmetry. The mean of the within-individual variances is then an estimate of fluctuating translational asymmetry at the population level. Tracy et al. [258], for example, studied within-plant variation in internode length of the aquatic macrophyte *Elodea canadensis* (Hydrocharitaceae: Angiospermae) in polluted and unpolluted streams in Michigan, USA. Internode lengths of *Elodea* in the Clinton River, polluted with heavy metals, PCBs, grease, and pesticides, were more variable than those of plants in an unpolluted tributary. In contrast to *Elodea*, *Ceratophyllum demersum* (Ceratophyllaceae: Angiospermae) showed no significant differences in translational fluctuating asymmetry of internode lengths between these sites. Unlike *Elodea*, which is rooted in the sediments, *Ceratophyllum* is an unrooted macrophyte. Most of the pollutants were sequestered in the sediments.

To use this approach, though, one must first verify that the trait value (i.e., internode length in *Elodea*) is unrelated to its order. We recommend regressing the trait value on its order and examining the residuals before accepting the null hypothesis. If trait value changes with order, then translational symmetry has been broken. This is analogous to handedness of bilateral traits, and specialized methods are required to estimate fluctuating translational asymmetry.

More often than not, translational symmetry is broken. In arthropods, segment (metamere) length and width, as well as numbers of bristles, show consistent variation from anterior to posterior ends. By modeling this relationship, one can estimate individual asymmetry as a lack of fit to the model. Astaurov [3], for example, studied variation in bristle count in the millipede *Geophilus ferrugineus* (Geophilidae: Myriapoda). For the first 15 segments, beginning at the anterior end, the number of bristles on each side averaged about 19. Between segments 15 and 30, the number of bristles declined to about 16, and remained unchanged to segment 46. In segment 47, the number of bristles decreased to 13 on each side. In general, the number of bristles declined from anterior to posterior ends of *Geophilus*. This variation was strictly deterministic, but the number of bristles varied in a random fashion, both within segments and between neighboring segments. This corresponds to fluctuating bilateral and translational asymmetry. Astaurov [3] used deviations from a moving average as a measure of random translational variation. Paxman [259] used a similar approach with variation in leaf length of *Nicotiana rustica* (Solanaceae: Angiospermae). In contrast to Astaurov’s [3] moving average, Paxman used the standard error of the estimate $S_{y|x}$ of leaf length on leaf order as a measure of developmental instability. The standard error of the estimate, however, varies with the mean $\bar{y}$ of the dependent variable. Zar [260] prefers $S_{y|x}/\bar{y}$ as a measure of variation around the regression.

All of these approaches assume a simple linear or nonlinear relationship between the trait and the segment (or internode) order. A more complex model, such as a higher-order polynomial, can always be made to fit the data more and more closely. Some judgement is necessary, and the residuals should be examined before $S_{y|x}/\bar{y}$ is used to estimate fluctuating translational asymmetry. $S_{y|x}/\bar{y}$ is estimated on a per individual basis, and the mean of $S_{y|x}/\bar{y}$ across the sample is the estimate of fluctuating translational asymmetry.
In plants, internode lengths and widths show consistent variation from older to newer internodes. This relationship is a consequence of allometry and inhibition \[261\]. Alados et al. \[262\] studied fluctuating translational asymmetry in *Anthyllis cytisoides* L. (Fabaceae: Angiospermae). The relation between internode length and internode order fits the general equation 
\[L = kN^a e^{bN},\]
where \(L\) is internode length, \(N\) is internode order starting from the base of the shoot, \(e\) is the base of natural logarithms, and \(k\), \(a\), and \(b\) are fitted constants \[263\]. The \(kN^a\) reflects the allometric relationship between internode length and node order, and \(e^{bN}\) reflects apical inhibition. Stress presumably decreases the accuracy of the curve fitting. The standard error of the estimate \((S_{y·x}/\bar{y})\), the statistical noise in the allometric relation, is a measure of individual asymmetry.

Under controlled laboratory conditions involving a known stressor (cadmium), fluctuating translational asymmetry has proven a more reliable indicator of stress than fluctuating bilateral asymmetry, and more sensitive than either growth or reproduction \[264\]. It was used to assess environmental stress associated with water pollution \[258, 265, 266\], soil cadmium \[264\], and soil salinity \[47, 267\].

9.4.3. Fluctuating Helical Asymmetry

Certain snails have a spiral shell approximating an equiangular spiral. Graham et al. \[20\] studied deviations from a perfect equiangular spiral in three populations of the terrestrial snail *Cepaea nemoralis* (Helicidae: Gastropoda) in the Ukraine.

The equation for an equiangular spiral is

\[r = ae^{\theta \cot \Phi},\]

where \(r\) is the radius from apex to curve, \(a\) is a constant, \(e\) is the base of natural logarithms, \(\theta\) is the angle made with a reference line passing through the apex, and \(\Phi\) is the constant angle at which the radius vector cuts the curve. Graham et al. \[20\] regressed \(\log_e r\) on \(\log_e a + \theta \cot \Phi\) for each individual snail and used the standard error of the estimate, divided by the mean of the dependent variable, \((S_{y·x}/\bar{y})\) as an estimate of individual asymmetry. Populations exposed to ammonia emissions and pesticides showed higher levels of asymmetry. Individuals in the population having the greatest helical asymmetry also showed erosion of their periostracum, which was not evident in the other two populations.

9.4.4. Fractal Dimension

Fractals are objects invariant with respect to scaling \[268, 269\]. They represent a form of symmetry, appearing the same at both high and low magnification. The fractal dimension \((D)\) of an object is a measure of its complexity. While lines, planes, and solids have discrete dimensions (1, 2, and 3, respectively), fractals have fractional dimensions. A skull suture or a time series has a dimension between one and two \((1 < D < 2)\). Clouds and bushes have dimensions between two and three \((2 < D < 3)\).
3). Indeed, fractal is short for fractional dimension. A skull suture having \( D = 1.7 \) fills more of a plane than one having \( D = 1.2 \). A bush having \( D = 2.8 \) fills more space than one having \( D = 2.3 \).

Graham et al. [20] first suggested that fractals might be useful in studies of developmental instability, though it was unclear at the time how the fractal dimension of an object might respond to stress. Theory suggested it might decrease under stress, under the assumption that stress dissipates energy away from the development of space-filling fractals [270]. Work on the fractal dynamics of human heartbeat had also suggested that nonlinear complexity declined with aging and disease [271]. Nevertheless, we found fractal dimension usually decreasing under stress, though it could increase as well [258, 22].

Fractal dimension decreases under stress in the roots of nitrogen-starved corn [272], in the pulmonary arteries of hypertensive individuals [273], in the crown of shrubs exposed to grazing [274, 261, 196], in the sagittal sutures of inbred Damas gazelles [275], in the branching complexity of virally infected pepper [276], in the behavioral time series of Spanish ibex parasitized with scabies [276, 277], in time series associated with heart disease and Huntington’s disease [271] (but see [278]), and in the vasculature of pituitary tumors [279]. Shandorff [280], however, found no difference in the fractal dimension of skull sutures in Harbor Seals before and after the advent of pollution in the Baltic Sea, but the left-right fractal asymmetry of these sutures was greater during the period of greatest pollution. The fractal dimension of skull sutures in Harbor Seals was only slightly larger than 1.0, so they were never complex to begin with. Indeed, if they were not significantly greater than 1.0, one would have difficulty calling them fractal sutures.

Examples of fractal dimension increasing under stress are more difficult to find. The rockweed *Fucus* sp. (Fucaceae: Phaeophyceae) shows greater fractal dimension at polluted sites in Puget Sound, near Seattle, Washington [258]. The increased fractal dimension is associated with increased irregularity of rockweed’s surface.

Clearly, changes in the fractal dimension of a trait have more in common with phenotypic modifications (i.e., decrease in growth rate) than they do with developmental instability. Because the fractal dimension of an object is usually estimated as the slope of a regression line, Graham et al. [20] also suggested the standard error of the estimate \( S_{y|x}/\sqrt{\hat{y}} \) be used as an index of developmental instability. There are, however, many methodological problems associated with such estimates [281]. For example, if techniques devised to estimate monofractals are blindly applied to multifractals, then \( D \) will be biased and \( S_{y|x}/\sqrt{\hat{y}} \) will be inflated, because multifractals are more complex than monofractals [282, 271]. More research is needed.

9.5. Fluctuating Asymmetry and Developmental Instability of Diverse Taxonomic Groups

9.5.1. Viruses

There have been few studies of developmental instability (and environmental robustness) in viruses. Moreover, many of the studies of genetic robustness address canalization, not stability. Nevertheless, some studies have examined within-genotype variation. Commoner [283] and colleagues, including Symington et al. [284], examined variation in length of the Tobacco Mosaic Virus, a helical RNA virus. The rods vary greatly in length, from 50-600 μm. The modal length is 300 μm. Rods longer than
300 μm arise by polymerization during preparation, but most of the rods measuring less than 300 μm are due to natural biosynthetic variation, not in vivo breakage during preparation for electron microscopy [284]. The short rods probably represent aborted forms of the virus [283], and they make up much of the population. Assuming all of these rods are genetically identical (they came from the same purified strain), this work suggests biosynthesis of Tobacco Mosaic Virus is inherently unstable.

According to Elena and Sanjuán [204], viral thermostability is a form of environmental robustness, and hence a measure of developmental stability. It is also an essential characteristic of vaccines [285]. RNA viruses are also less robust to mutation than comparable DNA viruses or RNA products in bacteria and eukaryotes [204]. This is largely a consequence of their compact genome, high mutation rate, and large population size [286]. Nevertheless, such hypersensitive RNA viruses often induce, and then take advantage of, their host’s molecular chaperones. Moreover, co-infection by different genotypes introduces an element of distributional robustness. Therefore, while mutational robustness is low for individuals, it may be large for populations within a host.

Bacteriophage plaques could be a useful model system for the study of developmental stability. Phenotypic variation among plaques of a single haplotype, and fluctuating radial asymmetry of individual plaques, could be used to study response to environmental or genetic stresses. Nevertheless, we are unaware of studies examining plaque variation and asymmetry in bacteriophage.

9.5.2. Archaea and Eubacteria

To our knowledge, there is only one study of developmental instability of eubacteria [16], and none of Archaea, in the literature. For the most part, measuring asymmetry of individual bacteria is impractical. Nevertheless, random variation in gene expression within a genetically homogeneous population is developmental instability [125].

Costas and Lopez-Rodas [16] found copper sulphate and DCMU-herbicide both increasing asymmetry between sister cells in the cyanobacterium Microcystis aeruginosa. The sister cells are analogous to bilateral symmetry, though there is no way to specify right and left.

Despite the difficulty of measuring asymmetry of individual bacteria, bacterial colonies are large enough for asymmetry estimates. Moreover, microbiologists often see bacterial colonies as multicellular organisms [287], albeit simple ones. Many bacteria produce disk-like colonies on agar medium, and the shape of these colonies may change under stress [288].

Many bacterial colonies produce branching fractal patterns, a product of cell-cell interactions [289]. The fractal dimension of these colonies can change under stress. According to Ben-Jacob [288], colonies of Paenibacillus dendritiformis, a lubricating bacterium, can shift from compact, to tip-splitting, to bushy fractal, to dihedral branches as peptone concentration is lowered in its medium.

In studies of colony asymmetry, one needs to distinguish asymmetric sectors caused by mutation from those caused by random variation [288]. Because cell numbers are enormous, mutations early in the development of a colony can generate significant variation at the level of the colony itself.

By using continuous symmetry measures, one can estimate fluctuating radial asymmetry of bacterial colonies even in the absence of landmarks. We are preparing a study of colony asymmetry of soil bacteria and their phages from north- and south-facing slopes of “Evolution Canyon,” Israel.
9.5.3. Fungi

As with bacteria, fluctuating asymmetry studies of fungal species are rare. Levy and Siegel’s [187] study of _Saccharomyces cerevisiae_, however, is an excellent example of work with unicellular fungi. They found 300 gene products that, when absent in single-gene knockouts, caused an increase in morphological variation among cells. The 300 gene products included proteins influencing or mediating chromosome organization and DNA integrity, RNA elongation, protein modification, cell cycle, and response to stress. These proteins were also among the most highly connected hubs in _Saccharomyces_’ metabolic network.

Fungi are excellent subjects for studies of fluctuating asymmetry. The fruiting bodies of several fungal groups, including the basidiomycota and ascomycota, often exhibit radial symmetry. Moreover, clones usually produce several fruiting bodies, so one can compare clones. Finally, the prevalence of haploidy in fungi suggests genetic and environmental robustness may be low. Haploid fungi should, theoretically, have greater developmental instability than diploid organisms, such as plants and animals.

Fungal colonies on agar medium are also amenable to studies of fluctuating radial asymmetry. We have begun a study of colony asymmetry in the soil fungus _Aspergillus niger_ (Trichocomaceae: Ascomycota) from “Evolution Canyon.” The conidia of populations on the south-facing slope have greater melanin content than do those on the north-facing slope [290]. This is presumably an adaptation to UV-stress on the exposed south-facing slope.

9.5.4. Plants

Plants are excellent subjects for studies of fluctuating asymmetry [212, 22]. Their modular design is a distinct advantage, allowing researchers to estimate individual fluctuating asymmetry. One disadvantage of plants is that they are immobile, which means environmental stress may vary among a plant’s different parts [291]. Cowart and Graham [99], for example, found outer leaves in the crown of _Ficus carica_ more asymmetrical than inner leaves. If leaf location is included as a source of variation, however, one can account for it statistically.

Studies of fluctuating asymmetry in plants have addressed leaf asymmetry of angiosperms [292], needle asymmetry of conifers [293], flower asymmetry [256], dichotomous branching [23, 24], fractal branching [20, 261, 274], and fractal time series [20, 277].

Plants also lend themselves to experimental manipulation [224].

9.5.5. Animals

Most studies of fluctuating asymmetry have been done with animals (see references mentioned throughout this review), including arthropods (insects, millipedes, arachnids), molluscs, and vertebrates (fish, reptiles, birds, and mammals). Nevertheless, there have been, to our knowledge, no comparative studies of different taxonomic groups, and no studies of the parazoa or radiata.
9.6. Fossil Material

There have been few studies of fluctuating asymmetry among fossil populations [15]. There are serious limitations, of course; specimens are compressed, deformed, and fragmented during fossilization. Nevertheless, some meristic traits, such as the number of facets in left and right eyes of trilobites, or the arrangement of foramina in vertebrate skulls, might permit reliable evaluation of asymmetry. In addition, one can study objects resistant to deformation, such as teeth. Unfortunately, it is difficult to assign teeth to individuals if the skull is fragmented.

Despite these challenges, the study of fluctuating asymmetry in fossil populations is the only way of testing some important evolutionary questions. Palmer [294], for example, suggested that comparisons of fluctuating asymmetry among prehistoric populations, or between prehistoric and extant populations, might be the only means of inferring genetic and environmental stress in the fossil record. Moreover, fluctuating asymmetry might reveal changes in morphological integration over evolutionary time [255]. To date, however, few studies of this sort have been published.

Van Valen [6] conducted the earliest study of fluctuating asymmetry on fossil material: dental asymmetry of the Pliocene horse *Griphippus gratus* (Equidae: Mammalia). The difficulties of working with *Griphippus* are typical. Of 400 specimens, only 36 had complete upper jaws with teeth on both sides. Van Valen reported the existence of random variation, but made no attempt to compare populations.

Smith [295] studied asymmetry in nine genera of early Paleozoic (lower Cambrian through Silurian) trilobites (Trilobita: Arthropoda). The idea that the Cambrian Explosion was due, in part, to lax developmental constraints suggested that fluctuating asymmetry might decline through the Paleozoic. Smith, however, found no evidence of a decline in fluctuating asymmetry of five bilateral traits measured on the cranidium (part of the head shield) over the nearly 100 million years.

Palmqvist *et al.* [296] attributed bilateral asymmetry and dental anomalies in a single complete skull of the large lower-Pleistocene canid *Canis (Xenocyon) falconeri* to possible isolation and small population size. Of 66 skeletal remains of this species, all but this one skull were fragmented and scattered; most teeth could not be assigned to particular individuals.

9.7. Molecular Robustness

Both genetic and environmental robustness can be studied at the molecular level, and these studies address basic questions regarding the evolution of robustness. Szöllösi and Derényi [297], for example, examined the robustness of miRNA precursors to thermal fluctuations. They concluded that the genetic robustness of miRNA sequences is a byproduct of selection for environmental robustness (but see [298]). See also the section 9.5.1, on viruses.

9.8. Specific Disciplines

Here we present a brief sampling of the literature on fluctuating asymmetry in different disciplines. For many of these disciplines, this is a small fraction of the literature.
9.8.1. Ecotoxicology

Fluctuating asymmetry has been widely used as an indicator of anthropogenic stress, including air and water pollution, elevated carbon dioxide, pesticides, and heavy metals (Table 5). A comparison of Table 5 with the small sample of studies in Tables 3 and 4 reveals proportionately more anthropogenic stressors showing positive results. Novel stressors, such as pesticides, are more likely to interfere with development simply because populations have not had time to adapt (but see [299]). But elevated carbon dioxide, a greenhouse gas, actually decreased the amount of leaf asymmetry in two oaks [300]. Nevertheless, unnatural toxins tend, in general, to increase fluctuating asymmetry.

Table 5. Anthropogenic stress and fluctuating asymmetry; a small sampling of studies and stressors.

<table>
<thead>
<tr>
<th>Stressor</th>
<th>Taxa</th>
<th>Traits</th>
<th>Result(^1)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heavy metals</td>
<td><em>Drosophila melanogaster</em></td>
<td>bristles</td>
<td>↑FA</td>
<td>[301]</td>
</tr>
<tr>
<td></td>
<td><em>Drosophila melanogaster</em></td>
<td>bristles</td>
<td>0</td>
<td>[302]</td>
</tr>
<tr>
<td></td>
<td><em>Sorex araneus</em></td>
<td>various</td>
<td>↑FA</td>
<td>[303]</td>
</tr>
<tr>
<td>Paper mill effluent</td>
<td><em>Gambusia holbrooki</em></td>
<td>various</td>
<td>↑FA</td>
<td>[304]</td>
</tr>
<tr>
<td>Urban air pollution</td>
<td><em>Platanus</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[305]</td>
</tr>
<tr>
<td>SO(^2) emissions</td>
<td><em>Betula spp.</em></td>
<td>leaf</td>
<td>↑FA(^2)</td>
<td>[45]</td>
</tr>
<tr>
<td></td>
<td><em>Pinus sylvestris</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[293, 306]</td>
</tr>
<tr>
<td>Acidification</td>
<td><em>Rana arvalis</em></td>
<td>skeleton</td>
<td>↑FA</td>
<td>[307]</td>
</tr>
<tr>
<td>Pesticides</td>
<td><em>Lucilia cuprina</em></td>
<td>bristle, wing</td>
<td>↑FA(^3)</td>
<td>[299]</td>
</tr>
<tr>
<td>Elevated CO(^2)</td>
<td><em>Quercus spp.</em></td>
<td>leaf</td>
<td>↓FA</td>
<td>[300]</td>
</tr>
<tr>
<td>Dioxin</td>
<td><em>Mus musculus</em></td>
<td>mandible</td>
<td>0(^4)</td>
<td>[308]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>teeth</td>
<td>↑FA</td>
<td>[309]</td>
</tr>
<tr>
<td>Magnetic fields</td>
<td><em>Drosophila melanogaster</em></td>
<td>bristles</td>
<td>0</td>
<td>[310]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>wing veins</td>
<td>↑↓FA(^5)</td>
<td>[310]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>phenodeviants</td>
<td>↑↓FA(^6)</td>
<td>[310]</td>
</tr>
<tr>
<td>Military training</td>
<td><em>Rhus copallinum</em></td>
<td>leaf</td>
<td>↓FA(^7)</td>
<td>[311]</td>
</tr>
<tr>
<td></td>
<td><em>Ipomoea pandurata</em></td>
<td>leaf</td>
<td>↓FA(^8)</td>
<td>[311]</td>
</tr>
<tr>
<td></td>
<td><em>Cnidoscolus stimulosus</em></td>
<td>leaf</td>
<td>↑FA</td>
<td>[312]</td>
</tr>
</tbody>
</table>

\(^1\)↑FA indicates a significant increase in fluctuating asymmetry. ↓FA indicates a significant decrease in fluctuating asymmetry. 0 indicates no significant change.

\(^2\) Treatment with lime alleviates the stress.

\(^3\) Fluctuating asymmetry returned to normal after several generations in the presence of the pesticide.

\(^4\) While FA did not increase, mandible size was smaller and its shape changed.

\(^5\) Wing asymmetry was greater at 80 \(\mu\)T than at 1.5 \(\mu\)T, but wing asymmetry was less at 1.5 \(\mu\)T than in the controls.

Abdominal phenodeviants paralleled the wing vein asymmetry.

\(^6\) Decreased asymmetry is a likely consequence of greater light availability in disturbed sites.
9.8.2. Conservation Biology

Threatened and endangered species often suffer from inbreeding and outbreeding depression. Inbreeding occurs because populations of rare species are small. Outbreeding occurs when rare species hybridize with more abundant related species. Both inbreeding and outbreeding depression sometimes increase fluctuating asymmetry [313].

In addition to inbreeding and outbreeding, anthropogenic stress, such as deforestation, habitat fragmentation, and urbanization, can increase fluctuating asymmetry of endangered species. Moreover, anthropogenic stress can exacerbate the effects of inbreeding depression. The Taita Thrush, *Turdus helleri* (Turdidae: Aves), for example, is a critically endangered species suffering from both inbreeding and forest fragmentation. Inbreeding has a greater effect on fluctuating asymmetry in more fragmented habitats than in less fragmented ones [314, 315].

One may combine data on fluctuating asymmetry with GIS data and map areas of disturbance. Teixeira *et al.* [316], for example, combined data on fluctuating asymmetry of *Didelphis albiventris*, a marsupial (Didelphinae: Mammalia), with GIS data on environmental composition. Though the sample sizes in this study were small, opossums in the least impacted natural environment had statistically lower levels of asymmetry.

9.8.3. Anthropology and Evolutionary Psychology

Anthropologists and evolutionary psychologists are doing some of the most interesting research involving fluctuating asymmetry. The literature, especially in anthropology, is large. We point out some of the highlights here. See Perzigian [317] for a review of the older literature on dental asymmetry in human populations.

Studies of human cranial asymmetry have produced surprising results. Modern humans, for example, have greater cranial asymmetry than Medieval from Cedyinia and Grózdek in Poland [318, 319]. Modern humans also have greater dental asymmetry than the great apes (*Pan, Gorilla, Pongo*) [320]. In contrast, Medieval Nubians (Sudanese Nubia) from the early Christian period display greater cranial asymmetry than those from the later Christian period [321]. Independent evidence suggests individuals from the early period were also less healthy.

Research on fluctuating asymmetry of fossil hominids is limited by the number of intact skeletons and the availability of complete left and right dental arches [322]. Even with limited sample sizes, *Homo habilis*, *H. neanderthalensis*, and *H. sapiens* (Hominidae: Mammalia) all seem to have greater dental asymmetry than the great apes [320]. Moreover, the small sample of *H. habilis* seems to have lower fluctuating dental asymmetry than either *Australopithecus africanus* or *Australopithecus (Paranthropus) robustus* [323, 322]. Larger samples will be necessary to distinguish between species of *Australopithecus, Paranthropus*, and the extinct species of *Homo*. As more material becomes available, researchers may be able to infer environmental and genetic stresses in our evolutionary past.

There has been much work on fluctuating asymmetry and sexual selection in humans. Women, for example, rate the dancing of symmetrical men more highly than that of asymmetrical men [324].

Finally, there are applications in psychology. Fluctuating asymmetry, for example, is associated with male, but not female, sexual orientation [325]. Moreover, it is positively associated with
schizophrenia [326, 327], human reactive aggression [328], and attention-deficit hyperactivity disorder [329, 330], but is unrelated to psychosis [331].

9.8.4. Medicine and Public Health

Other than the association between fractal dimension and disease states, which we reviewed in section 9.4.5, there have been few applications of fluctuating asymmetry to medicine and public health, despite Thornhill and Møller’s [332] “wake-up call” to the health professions. If fluctuating asymmetry is truly a marker of “good health,” as they argue, then it should be a useful tool. We agree, but feel it will be more useful as an indicator of community (i.e., population) health, than as an indicator of individual health.

As a recent example of a public-health application, high school students (especially males) from a slum in Ankara, Turkey had greater facial asymmetry than those from an upper-class neighborhood [333]. Moreover, the students from the slum were 9 kg lighter and 7 cm shorter than those from the upper-class neighborhood [334].

Van Dongen et al. [335] studied fluctuating asymmetry of human fetuses with severe developmental disorders. Surprisingly, skeletal asymmetry was significantly greater than that of controls for only four of 17 developmental disorders. The disorders having elevated fluctuating asymmetry were those associated with left–right patterning, limb defects, and problems of bronchopulmonary and urogenital systems. Moreover, even for these four kinds of disorders, levels of fluctuating asymmetry were smaller than expected.

For a review of the literature on symmetry and physical health, see [336].

9.8.5. Agriculture and Aquaculture

Fluctuating asymmetry is also a potentially useful indicator of animal [337] and plant [47, 267] health and welfare. Almeida et al. [338], for example, found higher fluctuating asymmetry in ornamental goldfish than in their wild relatives. Moreover, mortality of commercial oysters is related to shell asymmetry [339]. In contrast, stress does not increase fluctuating asymmetry of domestic chickens [340].

10. Fluctuating Asymmetry: Problems and Solutions

10.1. Inconsistencies among Studies of Fluctuating Asymmetry

The results of fluctuating asymmetry studies are inconsistent. In some studies, for example, fluctuating asymmetry increases under environmental and genetic stress [313, 11]. Conversely, fluctuating asymmetry does not increase under stress in other studies [158, 341]. Indeed, Leung and Forbes [342, p. 403] have stated that fluctuating asymmetry "may be a poor general predictor of either stress or fitness." Complex environments, adaptation to stress, and inadequate methodology may contribute to this inconsistency, at least in part. Here we examine some likely reasons for these inconsistencies, as well as partial solutions.
Various biotic and abiotic stressors impinge on individuals in natural populations. The biotic stressors include competition, predation, herbivory, parasitism, and disease. The abiotic stressors include high and low temperature, insufficient light, and inadequate water and nutrients. Together, they present a complex spatio-temporal pattern. One can control these variables in a lab or field experiment [224, 341], but studying fluctuating asymmetry of natural populations is problematic. At the outset, we usually have little information about the kinds and amounts of stress. Indeed, we usually take the opposite approach and try to infer stress through fluctuating asymmetry.

Extreme environments are stressful (or not) only when they interact with organisms, or more precisely, when they interact with the different parts of organisms. Some parts, such as the wings of a fruitfly, may respond to stress, and others, such as its sternopleural bristles, may not [49, 6]. Fluctuating asymmetry of one trait rarely correlates with fluctuating asymmetry of other traits [343]. This is especially true when one is looking at fluctuating asymmetry of several traits in a single individual [49, 6].

While individual-wide fluctuating asymmetry is rare, population-wide asymmetry is common. If one trait is more asymmetric in one population, other traits are likely more asymmetric as well. To estimate population-wide asymmetry, researchers sometimes use Kendall’s Coefficient of Concordance.

Responses to stress are trait-specific, and may remain undetected unless the appropriate traits are measured [341]. Consequently, particular environmental conditions will affect only some developmental pathways leading to specific responses [193]. In addition, individuals and populations may be well adapted to an environment appearing stressful to us, or may be able to avoid stress through behavioral modifications [303].

Measuring and comparing fluctuating asymmetry is not as easy and straightforward as it seems. The signal is small, and the chance of producing spurious results is high. If one is careless, one may miss a real signal (false negative) or find a false signal (false positive). Measurement error, size scaling, and the statistical distribution should be handled carefully (see [55], and section 5 in this review).

10.2. The “Evolution Canyon” Microsites

Controlling abiotic and biotic stressors in a controlled experiment may provide a partial solution to the inconsistency problem. One cannot, however, control these stressors in natural situations, though their number can be reduced. By using standardized sampling and measurement, as well as by collecting data from many species in a variety of taxa, we may be better able to evaluate developmental instability.

Divergent microsites provide an opportunity for reducing the number of environmental factors in studies of natural populations. We found this in the “Evolution Canyon” microsites (Figure 28), where south-facing "African" slopes abut north-facing "European" slopes. The “African” slopes, which are xeric and tropical, are (on average) 200 m from the “European” slopes, which are mesic and temperate.

The two slopes of the “Evolution Canyon” microsites provide a wonderful opportunity for studying developmental instability in a partly controlled natural experiment. The rocks, soils, and topography are similar on the opposing slopes. Microclimate alone is the major abiotic difference. The “African” slope is more stressful for many terrestrial organisms [344-347, 151, 348, 349], hence we know, in
part, the amount of stress on each slope, especially since microclimate on the opposite slopes is known
[350].

**Figure 28.** The four “Evolution Canyons” in Israel (EC I – EC IV). Note the interslope divergence in vegetation, even in EC III in the Negev Desert [151].

One consequence of the contrasting stressors is that terrestrial and aquatic communities respond differently to microclimate on the two slopes. There are more terrestrial species on the “African” slope, and more aquatic species on the “European” slope. Moreover, phenotypic and genetic variation differs between the two slopes. For example, nine of 14 model organisms (bacteria to vertebrates) have significantly greater genetic polymorphism on the more stressful “African” slope. Moreover, some species have greater rates of mutation, gene conversion, recombination, and DNA repair, as well as larger genome sizes and more small sequence repeats (SSRs), single nucleotide polymorphisms (SNPs), retrotransposons, transposons, candidate gene diversity, and genome-wide gene expression and regulation on the more stressful “African” slope (reviews in [344-347, 151]. Remarkably, incipient sympatric speciation is occurring across all taxa, from bacteria to mammals, on the two slopes.

10.3. Ongoing Research on Fluctuating Asymmetry at the “Evolution Canyon” Microsites

The interdisciplinary study of fluctuating asymmetry at the “Evolution Canyon” microsites includes the development and use of novel, trait-specific measures of fluctuating asymmetry, as well as the use of conventional indices. Some of the novel methods include measures of leaf asymmetry involving secondary [23, 24] and higher order [81] veins. We have used these approaches on leaves of *Quercus calliprinos* and *Salvia fruticosa* at “Evolution Canyon I,” as well as *Ruta chalepensis* at “Evolution Canyon II.” All of these studies have shown higher fluctuating asymmetry on the dry “African” slope.
We are currently conducting a study of leaf asymmetry of 12 plant species at “Evolution Canyon” I [101].

Previously, Auslander et al. [351] studied the developmental instability of *Pistacia lentiscus* on the opposite slopes of two “Evolution Canyons” in Israel (e.g., Nahal Keziv and Nahal Oren) and an additional canyon, Nahal Mearot. The average leaves at the three canyons were 20% larger on the “European” slope than on the “African” slope. In addition, leaf asymmetry (standardized by leaf size) was similar on “African” and “European” slopes of Nahal Mearot and Nahal Keziv, whereas it was two times higher on the “African” slope of Nahal Oren (*i.e.*, “Evolution Canyon” I). In contrast, we found no difference in leaf asymmetry of *P. lentiscus* at Nahal Oren, probably because the power transformation we used compensated for overcorrection almost certainly present in the Auslander study. Prior to the power transformation, our data also indicated greater asymmetry on the “African” slope [101].

One study of fluctuating asymmetry in an animal species has been completed at “Evolution Canyon” (though more are in progress). Derzhavets et al. [352] found greater fluctuating asymmetry of wing dimensions in *Drosophila melanogaster* on the “African” slope. Unlike the Auslander [351] study, five replicate measurements were averaged prior to the analysis, to minimize measurement error. Overcorrection was not a problem here. Low humidity on the “African” slope is a likely stressor for *D. melanogaster* [353].

In addition to this completed work, the group at the Institute of Evolution at the University of Haifa, as well as their collaborators elsewhere, is currently developing an image-processing-based CSM for fluctuating radial asymmetry, and is already using it with seven fungal species from the opposite slopes of “Evolution Canyon” I. Moreover, the group is developing a new CSM for 3-dimensional branches of plants. Finally, a study of the fluctuating asymmetry of beetles is in our immediate plans. Future studies will address fluctuating asymmetry of bacteria, additional arthropods, and mammals, to see if different taxa across life share a similar drought stress on the “African” slope and light stress on the “European” slope.

### 11. Conclusions

Fluctuating asymmetry is a useful indicator of stress, not because it is more sensitive to stress than phenotypic modification, but because it reveals the average individual’s robustness and stability in the face of stress. In this respect, it is the only indicator that addresses developmental homeostasis. Consequently, if fluctuating asymmetry remains unchanged in the face of a stressor that has influenced growth and reproduction (e.g., clutch size), it may simply mean that developmental homeostasis was not disturbed. Moreover, if one accepts the definition of stress advocated by Escós et al. [188] and Walter Cannon [133], then one might infer that, despite changes in growth and reproduction, the population was unstressed. In future work, researchers might compare indices of developmental and physiological homeostasis.

Fluctuating asymmetry may occasionally correlate with individual fitness. Nevertheless, we do not advocate using it as an index of individual fitness. Scientists should measure relative reproductive success, not symmetry. Nevertheless, it may be worthwhile to understand when and how fluctuating
asymmetry correlates with individual fitness. The best opportunity for doing so is with organisms having repeated modular elements, such as plants. Regardless of whether it is used as either an indicator of stress or a correlate of fitness, fluctuating asymmetry must be used with more care than has been typical in the literature. Sample sizes should be large, and replicate measurements are essential. Moreover, researchers must address mixed error distributions and size-scaling. Failure to do so can easily generate spurious associations.

Future work should focus on resolving the current controversies regarding developmental instability, stress, and fitness. These issues are too important to ignore, and the recent genomic revolution provides unlimited opportunity to dissect the genetic architecture of developmental instability. We also suggest that ecologically divergent microsites, such as “Evolution Canyon,” might serve as natural laboratories for the study of developmental instability across all of life. Consequently, we have initiated studies of fluctuating asymmetry in several species of plants, fungi, bacteria, and animals on both slopes of “Evolution Canyon,” sharing drought stress on the “African” slope and light stress on the “European” slope. We also plan to compare and contrast these taxa in at least two “Evolution Canyons,” one in the mountains of Carmel and the other in Upper Galilee (EC I and EC II).

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