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Anomalous Zenith Total Delays for an Insular Tropical Location: The Tahiti Island Case

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Abstract: The weighted mean temperature of the troposphere, T_m, is a key parameter in GNSS meteorology. It can be routinely derived based on meteorological data from radiosonde (RS) or numerical weather models. Alternatively, it can be also derived through a least-squares model of the ratio between the precipitable water vapor from RS data and the zenith wet delay estimates from GNSS measurement in the precise point positioning mode. In this last case, we found anomalous T_m values for the remote sub-tropical humid location of the Tahiti Island in the South Pacific Ocean and traced these anomalous values to anomalous zenith total delays (ZTD) that seem to have an accuracy poorer by one order of magnitude than the claimed accuracy of ZTD delays from worldwide databases. The possible causes of these discrepancies are discussed.

Keywords: GNSS; weighted mean temperature; zenith total delays; precise point positioning; precipitable water vapor; radiosonde

1. Introduction

The atmospheric water vapor plays a central role in all meteorology/climate processes, and at all temporal and spatial scales: micrometeorology, evapotranspiration, clouds, precipitations, and energy balance [1]. In addition, water vapor accounts for around three quarters of the greenhouse warming on Earth, and is therefore one of the main drivers of climate variability [2]. Precipitable water vapor (PWV/PW), the core quantity to model the water vapor contents of the troposphere, is defined as the equivalent amount of water that could be produced if all the water vapor in an atmospheric column rained down instantly [3].

Several techniques are commonly used to model the spatial and temporal variations of PW. These include radiosonde balloons (RS), water vapor radiometers, and sun photometers, but their low spatial and temporal resolution, and sometimes poor quality and high cost limit their use [4–7]. To overcome these drawbacks, the ground-based Global Positioning System (GPS) receivers, and now GLONASS, BDS, and Galileo (collectively known as Global Navigation Satellite Systems (GNSS)) have been extensively used since the early 1990s for the determination of PW with all-weather capability, high temporal sampling frequency (down to a few minutes), and widely different line-of-sight receiver-satellite geometries (from the near-horizon to zenith direction) [8]. Widely used techniques include relative positioning and precise point positioning (PPP). Compared to relative positioning, PPP is favored in GNSS meteorology because it uses a stand-alone receiver to obtain absolute atmospheric parameters [9]. The GNSS receivers are also relativity cheap, with the average cost of a GNSS receiver being roughly equivalent to 25 radiosonde balloon launches [10].

An extra atmospheric delay in the GNSS receiver-satellites radio-links is caused, at around a 10–20% level, by the wet refractivity variations in the troposphere, with the bending of the ray as a second order effect [11,12]. The wet refractivity is highly variable, both

horizontally and vertically. The total propagation delay, remapped along the vertical direction, is named zenith total delays (ZTD). It can be split as the sum of a zenith hydrostatic (also improperly called "dry") delay (ZHD) and a zenith wet (non-hydrostatic) delay (ZWD) [13]. The ZHD can be determined with a good accuracy by empirical models such as the Hopfield model [14], the Saastamoinen model [15], or the Black model [16]; all of them are constrained by surface meteorological measurements (temperature and pressure). Therefore, the ZWD can be defined by the relation ZWD = ZTD-ZHD, if we assume no other factors other than water vapor are involved. The PW itself can be derived from the ZWD by using a multiplicative conversion factor, a function of the so-called weighted mean temperature T_m [17,18]. Usually, values of T_m are derived by analyzing long time series of RS profile observations, but they can also be computed by ray tracing/vertical integration with respect to gridded numerical weather models (NWM) [19,20]. In 1992, Bevis et al. demonstrated that there is a linear relation between T_m and T_s ($T_m = a + b \cdot T_s$), with $T_m < T_s$. The surface temperature, T_s, can be easily obtained from GNSS collocated weather stations or nearby weather stations (for example, [21] for Europe, [22] for India, [23] for Turkey, and [24] for Tahiti). To improve the reliability of GNSS PWV, Huang et al. (2022) adopted three enhanced vertical correction models for temperature, pressure, and PWV, and developed four accurate T_m models suitable for four regions of China [25]. Ross and Rosenfeld (1997) noted that the coefficients of the linear relationship between T_m and T_s change as a function of locations and seasons [26]. In other words, PW estimates from GNSS data need three input values: ZTD, ZHD, and T_m, and a site-dependent tailored fit [27,28].

This study was prompted by the conclusions of a previous paper [24] about the determination of PW estimates in Tahiti from GPS data only, with stand-alone receivers used in the PPP mode. The linear fits $T_m - T_s$ pointed, in this tropical context, to overlarge values of T_m, sometimes larger than the surface temperature T_s. From its own definition (see Equation (14)), T_m should be lower than the maximum temperature in the troposphere, normally found at ground level (a small inversion layer due to the trade winds present in Tahiti but does not change this behavior). The determination of the linear fit was also complicated by the fact that the range of surface temperature in Tahiti is also quite limited, around 10 K, thanks to the South Pacific Ocean acting as a heat buffer. This problem is already apparent in the seminal paper of Bevis et al. (1992) [29], where the scatter around the linear relationship $T_m - T_s$ becomes larger and larger with increasing values of T_m and T_s. In this previous paper, two possible conclusions were made: (1) the underlying physics of the $T_m - T_s$ linear relationship break for some reasons for large atmospheric humidity contents, and/or (2) some systematic errors are present in the GNSS data processing software or in the determination of T_s. The purpose of this follow-on paper is to investigate these two points by examining all the links of the computation chain leading to the mean temperature estimate. Our breadcrumb trail will be the comparison between the $T_m - T_s$ relationship determined from in situ RS/meteorological data and the $T_m - T_s$ relationship determined from GNSS data.

The paper is organized as follows: Section 2 recalls the underlying physics of the derivation of ZTD, ZHD, ZWD, T_m and PW; Section 3 introduces the datasets; Section 4 analyses the results, including comparisons between our results and the references; Section 5 gives the discussion about the anomalous ZTD results; and Section 6 draws the conclusions.

2. Methodology

The total tropospheric delay along the zenith direction can be determined as the integration along the vertical of the atmospheric total refractivity N as:

$$ZTD = 10^{-6} \int N \, dz, \tag{1}$$

where z is the geometrical height of the observation site above the mean sea level. N and its subparts N_d (hydrostatic) and N_w (wet) can be written as:

$$N = k_1\left(\frac{P_d}{T}\right)Z_d^{-1} + k_2\left(\frac{P_v}{T}\right)Z_v^{-1} + k_3\left(\frac{P_v}{T^2}\right)Z_v^{-1} = N_d + N_w, \tag{2}$$

$$N_d = k_1\left(\frac{P}{T}\right)Z_d^{-1}, \tag{3}$$

$$N_w = [k_2'\left(\frac{P_v}{T}\right) + k_3\left(\frac{P_v}{T^2}\right)]Z_v^{-1}, \tag{4}$$

where T is the temperature in Kelvin, P_d is the dry air pressure in mbar, P_v the water vapor pressure in mbar [30], and $P = P_d + P_v$. Z_d^{-1} and Z_v^{-1} are the inverse compressibility factors for dry air and water vapor, respectively [31]. N_d is the refractivity of dry air and N_w is the refractivity of water vapor. k_1, k_2 and k_3 are refractivity constants, $k_2' = k_2 - k_1 \cdot (M_w/M_d) = 22.1$ (K/hPa), $M_w = 18.0152$ (kg/kmol) is the molar weight of wet air, and $M_d = 28.9644$ (kg/kmol) is the molar weight of dry air [19].

As ZTD is, by its own definition, equal to the sum of ZHD and ZWD [29], then:

$$ZHD = 10^{-6}\int N_d\, dz = 10^{-6}k_1\int\left(\frac{P}{T}\right)Z_d^{-1}\, dz, \tag{5}$$

and

$$ZWD = 10^{-6}\int N_w\, dz = 10^{-6}k_2'\int\left(\frac{P_v}{T}\right)Z_v^{-1}\, dz + 10^{-6}k_3\int\left(\frac{P_v}{T^2}\right)Z_v^{-1}\, dz, \tag{6}$$

From an observational point of view, P_v is measured as

$$P_v = RH \cdot e_s/100, \tag{7}$$

where RH is the sensor relative humidity, and e_s is the saturation water vapor pressure that depends on the surface temperature T_s [32,33], that can be calculated by

$$e_s = 6.11 \times 10^{\frac{7.5 \times T_s}{237.3 + T_s}}. \tag{8}$$

The ZHD must always be calculated from empirical models as the signature of the water vapor in the ZTD cannot be distinguished, from a practical point of view, from the signature in the hydrostatic delay (ZHD) [34]. The Saastamoinen model is the most common model, with an accuracy that is claimed to be at the millimeter-level [15]:

$$ZHD = 2.2779\, P_s/f(\lambda,\ H), \tag{9}$$

The model of [17] has the same form as the Saastamoinen model, but with a slightly different constant:

$$ZHD = 2.2768\, P_s/f(\lambda,\ H), \tag{10}$$

where, for both, $f(\lambda,H) = 1 - 0.00266 \cdot \cos(2\lambda) - 0.00028 \cdot H$, $H(km)$ is the geometrical height of the receiver above the ellipsoid, $\lambda(rad)$ is the station latitude, and P_s is the surface pressure in hPa.

As already stated, ZWD is defined as the Equation (11):

$$ZWD = ZTD - ZHD, \tag{11}$$

with ZWD converted into PW by [19]:

$$PW = \Pi \cdot ZWD, \tag{12}$$

and with the ratio Π defined as [35]:

$$\Pi = 10^6 / (\rho \cdot R_v(\frac{k_3}{T_m} + k_2')), \tag{13}$$

where ρ = 1000 (kg/m^3) is the density of liquid water (kg/m^3), and R_v = 461.495 (J/kg·K) is the specific water vapor constant. T_m, the vertically weighted mean temperature of the atmosphere with respect to its water vapor contents, is defined as [17]:

$$T_m = \int (P_v/T)dz / \int \left(P_v/T^2\right)dz, \tag{14}$$

As it is clear from Equation (14), time series of T_m for a particular site can be derived from the knowledge of the vertical values of T and P_v from RS profiles or numerical weather models [20]. It is also clear from Equation (14) that T_m is the mean temperature defined with the water vapor pressure P_v as weight. It should be also emphasized that this definition ignores any orographic effect, with the exception of the initial altitude of the vertical profiles.

RS profiles and gridded weather models also allow a direct computation of *PW* as:

$$PW = \frac{1}{\rho} \int \rho_w dz, \tag{15}$$

$$\rho_w = P_v/(R_v \cdot T), \tag{16}$$

where ρ_w is the density of water vapor.

3. Datasets

Two International GNSS Service (IGS) stations are operating on the South Pacific Ocean Island of Tahiti: FAA1 is located at almost sea level on the premises of the Tahiti international airport; THTI is located inland at a horizontal distance of 2.56 km and with an altitude difference of 86.14 m with respect to FAA1. Although they are close (Figure 1), their surroundings are quite different. FAA1, managed by Météo-France, is located at near sea-level, under the premises of the international airport, on a very large area that was flattened to host the airstrip. THTI is located on the main campus of the University of French Polynesia, a little bit more inland, on a ridge crest with a slope of about 8%, at a distance from the sea of about 1.5 km. They belong to two distinct valleys, each one with its own micro-climate [10,36].
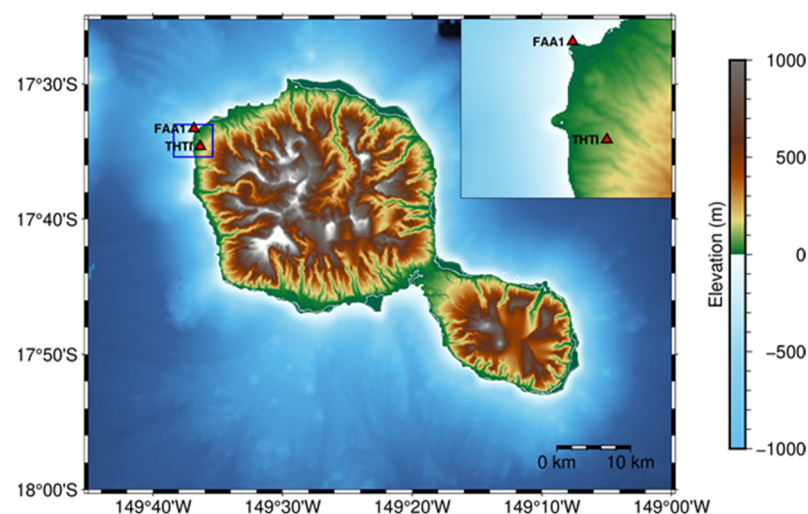
Figure 1. Location of the THTI site (149.61°W, 17.58°S, ellipsoidal altitude 98.49 m) and FAA1 site (149.62°W, 17.56°S, ellipsoidal altitude 12.35 m) on Tahiti Island.

A precise analysis of the differences between their ZTD time series showed that the difference in insulation (and so evapotranspiration), and not the altitude difference, is the leading actor in these differences. For this study, we processed GNSS data for the whole year of 2017 on a daily basis, and obtained one-year ZTD results using the Bernese Software Version 5.2 in the static post-processing PPP mode [37,38]. To validate the accuracy of our ZTD estimates, we compared our estimates with the Center for Determination in Europe (CODE) tropospheric products and the IGS final tropospheric products. Their ZTD products, with a claimed accuracy of 4 mm, are presented in the literature [39,40] as highly reliable products. Details of these data processing strategies are described in Table 1.

Table 1. Data processing strategies of our ZTD estimates and IGS/CODE tropospheric products.

	Our ZTD Estimates	IGS	CODE
Precise satellite orbits and clocks	CODE Final products	IGS Final products	CODE Final products
Approach	PPP	PPP	Relative positioning
Elevation angle cutoff	3 degrees	7 degrees	3 degrees
Mapping function	VMF1 (Vienna Mapping Function 1)	GMF (Global Mapping Function)	VMF1
A priori troposphere estimate	Dry VMF model	Dry Niell model	Dry VMF model
Ionosphere correction	Ionosphere-free linear combination of L1 and L2	Ionosphere-free linear combination of L1 and L2	Ionosphere-free linear combination of L1 and L2
Temporal resolution	1 h	5 min	2 h
Ocean tidal loading	FES 2004	FES 2004	FES 2014b
Atmospheric tidal loading	Ray and Ponte (2003) [41]	Ray and Ponte (2003) [41]	S1 + S2 tidal corrections from the Vienna atmospheric pressure model

The Integrated Global Radiosonde Archive (IGRA) is maintained by the National Oceanic and Atmospheric Administration (NOAA) and consists of radiosonde observations over 2700 globally distributed stations since 1905 [42]. A IGRA radio sounding balloon station is collocated with the FAA1 GNSS receiver at a few meters distance. The RS balloons are launched twice a day at 00:00 and 12:00 UTC and provide approximately vertical profiles (depending on the wind) of the atmospheric key variables including pressure, temperature, relative humidity, wind speed and direction, dew point temperature, and elapsed time since launch, until the balloon blows up under overpressure of its envelope at around 30 km [43].

The meteorological parameters from the site-wise VMF1 files (using the 40 years reanalysis (ERA-40) NWM data of the ECMWF, https://vmf.geo.tuwien.ac.at/, accessed on 9 November 2022) were also used in this study. The values are interpolated from a 2.0° × 2.5° grid, with a six-hour temporal resolution, and include the so-called hydrostatic/wet "a" coefficient of the VMF1 mapping function continuous fraction, the hydrostatic/wet zenith delays, an estimation of the atmosphere mean temperature above the site, the pressure, temperature and water vapor pressure at the site, and the orthometric altitude of the station (geoid model EGM96) [39]. Here, all site-wise products are generated based on the coordinates and altitude of IGS stations [44].

In addition, to compute tropospheric delays, we converted the geopotential heights recorded on RS data to orthometric heights [45]. The 1976 US Standard atmosphere [46] at waterless high altitudes was used to complement the RS troposphere delay models. This standard atmosphere model, up to 100 km altitude, assumes that air is a clean, dry (no water vapor present) gas, obeying the perfect gas law and the hydrostatic equation. It is roughly representative of year-round, mid-latitude conditions [47].

4. Results

In this section, to analyze and discuss our results calculated by using the above methodology and datasets, we make some comparisons between our results and the

references that will be provided, including our ZTD estimates versus CODE and IGS products in Section 4.1, surface temperature from ground station versus that from site-wise VMF1 files in Section 4.2, weighted mean temperature estimated from RS measurements versus that from site-wise VMF1 files in Section 4.3, ZWD results estimated from RS measurements versus that from site-wise VMF1 files in Section 4.4, ZHD estimates based on the original Saastamoinen model versus that based on Davis' adapted Saastamoinen model in Section 4.5, and Section 4.6 includes ZHD estimates based on Davis' adapted Saastamoinen model versus that calculated by using RS data and standard atmosphere, and GPS ZTD estimates versus ZTD derived from RS data and standard atmosphere. The detailed comparisons are presented in the following.
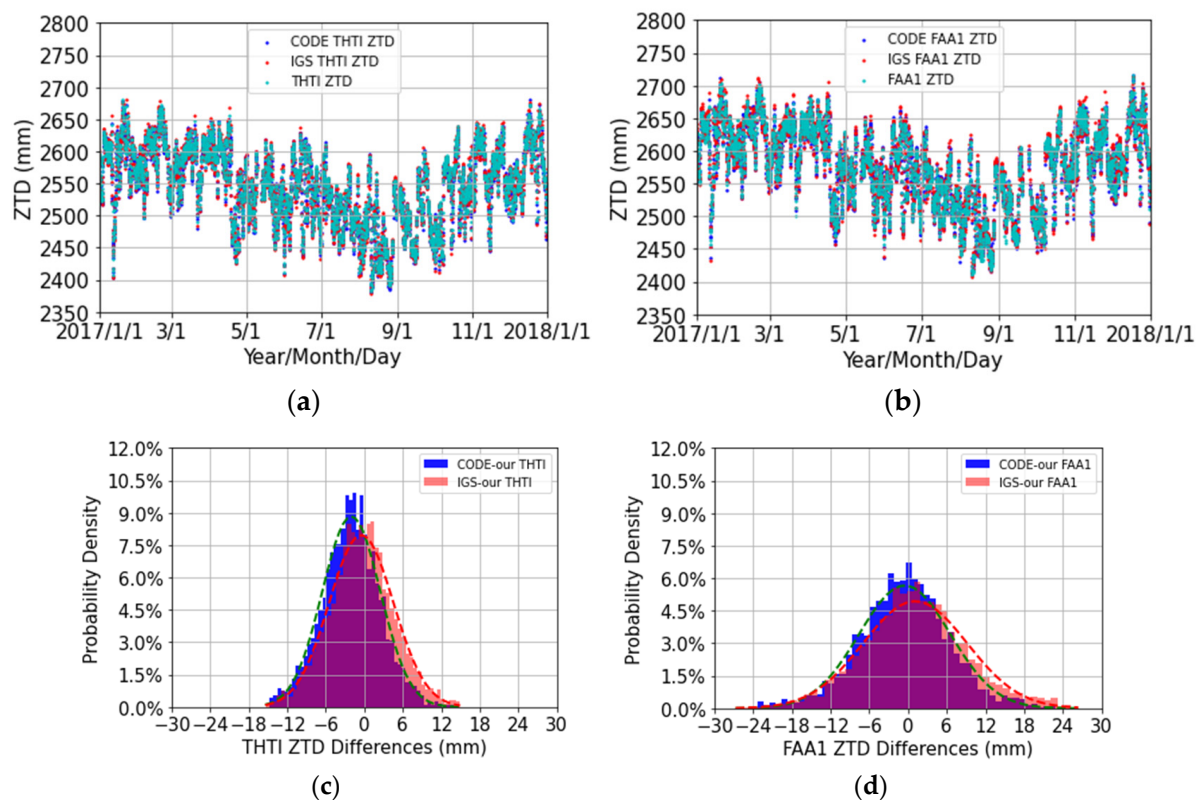
4.1. Comparisons of Our ZTD Estimates with CODE and IGS ZTD Estimates

To validate the effectiveness of our data processing strategies and the accuracy of our ZTD estimates, we compare, in this subsection, our ZTD to CODE/IGS ZTD products. The different settings between our processing and CODE/IGS products are summarized in Table 1. Our processing and the IGS final ZTD products both use the so-called PPP post-processing mode [48,49]. IGS lists four PPP providers at the time of the writing of these lines (https://igs.org/products-access/#gps-orbits-clocks, accessed on 9 November 2022). Our Bernese 5.2 software uses the PPP-CODE final product (https://www.aiub. unibe.ch/research/code___analysis_center/, accessed on 9 November 2022) and the IGS data analysis centers use the PPP-IGS final product [50]. Details about what are exactly the differences in processing strategies between the currently available PPP products are arcane. We refer to [48,51,52] for recent assessments of the PPP models for several constellations. All these PPP products claim a few centimeter-level accuracy on the GPS satellite orbits. CODE ZTD products use the relative positioning approach [39].

From a practical point of view, our ZTD estimates are very close to the CODE/IGS final ZTD products (Figure 2a,b and Table 2), with a mean bias at the mm level over one year, probably caused by some different settings between our GPS data processing and the CODE/IGS final products (Figure 2c,d): PPP/relative positioning models, mapping functions, a priori ZTD models, cut-off angles, and oceanic/Earth tides models (see Table 1). Such a small bias does not validate our processing versus CODE/IGS products. It just indicates that if systematic effects are present, they are present in both these computations, possibly disappearing in the ZTD differences.

Table 2. Statistical summary for the comparison between our THTI/FAA1 ZTD estimates and CODE/IGS THTI/FAA1 ZTD estimates (CODE/IGS values minus our ZTD values, Figure 2a,b) in terms of maximum (max), minimum (min), bias, root mean squares (RMS), and standard deviation (STD). The exact definitions of bias, RMS and STD, are shown in Appendix A.

| Differences		Max (mm)	Min (mm)	Bias (mm)	RMS (mm)	STD (mm)	Data Points
THTI	CODE-our	14.53	−14.72	−2.02	4.96	4.52	4244
	IGS-our	14.93	−15.42	−0.47	5.03	5.01	4244
FAA1	CODE-our	22.89	−23.39	−0.51	7.06	7.04	4149
	IGS-our	26.36	−26.71	1.09	8.15	8.08	4149

Figure 2. Comparisons of our THTI ZTD estimates (cyan dots) with CODE/IGS THTI ZTD estimates (blue and red dots) (**a**), and FAA1 ZTD estimates (cyan dots), with CODE/IGS FAA1 ZTD estimates (blue and red dots) (**b**). See Table 2 for a statistical summary; (**c**) histograms of the ZTD differences between our THTI ZTD estimates and CODE/IGS THTI ZTD estimates; (**d**) histograms of the ZTD differences between our FAA1 ZTD estimates and CODE/IGS FAA1 ZTD estimates.

According to Table 2, RMS values for the FAA1 site are larger than that for the THTI site, by around 3 mm. This difference is mainly driven by insolation differences, and the differences in altitude and the wind are secondary factors, as presented by Zhang et al. (2019) [10].

4.2. Comparison of the Surface Temperature from the FAA1 Ground Weather Station and the Site-Wise VMF1 Files

To assess from a metrological point of view, the linear relationship between the mean temperature, T_m, and surface temperature, T_s, we need to examine the accuracy of T_s values. For this purpose, we compared the surface temperature records (T1) from the FAA1 ground weather station with the time series of the surface temperature (T2) from the site-wise VMF1 files (Figure 3a). The histogram of the temperature differences between T1 and T2 is shown in Figure 3b. From time series of T2, we find that surface temperature over Tahiti is relatively stable with variations less than 8 K through one year, reaching the lowest values in August. T1 generally follows the trend of T2 but exhibits larger noises. According to Figure 3b, the noises of T1 roughly obey a Gaussian distribution with a small bias. A statistical summary provided in Table 3 shows that these two temperature records are coherent with a bias of 1 K and an RMS of 2 K. We should emphasize that ground temperatures are influenced by micro-scale variations, both in time and space, of turbulence and insolation at the air-soil interface, so the concept of "surface temperature" is a blurry one. These micro-scale variations are certainly the main contributor to the RMS value of 2 K.

(**a**)   (**b**)
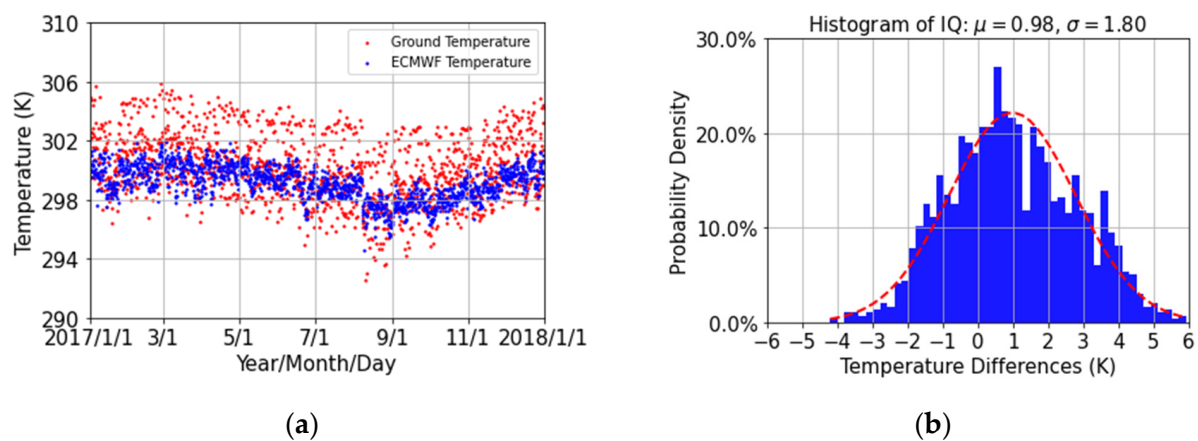
Figure 3. FAA1 station: (**a**) comparison between the surface temperature from the ground weather station (T1, red dots) and from the site-wise VMF1/ECMWF files (T2, blue dots); (**b**) histograms of the temperature differences between the surface temperature from the ground weather station (T1) and from the site-wise VMF1/ECMWF files (T2).

Table 3. Statistical summary for the comparisons (Figure 3) between the surface temperature from the ground weather station (T1) and from the site-wise VMF1/ECMWF files (T2) (T1 minus T2) in terms of max, min, bias, STD, and RMS.

Differences	Max (K)	Min (K)	Bias (K)	RMS (K)	STD (K)	Data Points
T1-T2	5.93	−4.20	0.98	2.04	1.80	1458

*4.3. Comparison of T_m Estimates from RS Measurements and Site-Wise VMF1 Files*

In this section we derive mean temperature, T_m, estimates built only from the RS balloon measurements (noted $RS - T_m$) made at the FAA1 weather station in 2017. We calculated the T_m estimates by directly considering its definition (Equation (14)), with the flight of the balloon assumed to be vertical up to its maximum altitude. Its lateral drift can reach up to 20 to 50 km, depending on the direction and intensity of the wind [24].

We compared our $RS - T_m$ estimates with the T_m estimates from the site-wise VMF1/ECMWF files, that considers an atmospheric column up to 47 km [39]. Time series, histogram of their differences, and a statistical summary are given in Figure 4a,b and Table 4, respectively. According to Figure 4a, $RS - T_m$ values are consistent with the VMF1 ones, displaying a periodical pattern with peak-to-peak values of around 8 K. From Table 4, the bias and RMS values of the differences between $RS - T_m$ and T_m from VMF1/ECMWF are 0.56 K and 1.05 K, respectively.

Table 4. Statistical summary for the comparison between $RS - T_m$ and T_m from VMF1/ECMWF (vmf1 minus RS) in terms of max, min, bias, STD and RMS.

Differences	Max (K)	Min (K)	Bias (K)	RMS (K)	STD (K)	Data Points
ECMWF—RS	4.55	−2.69	0.56	1.05	0.88	724
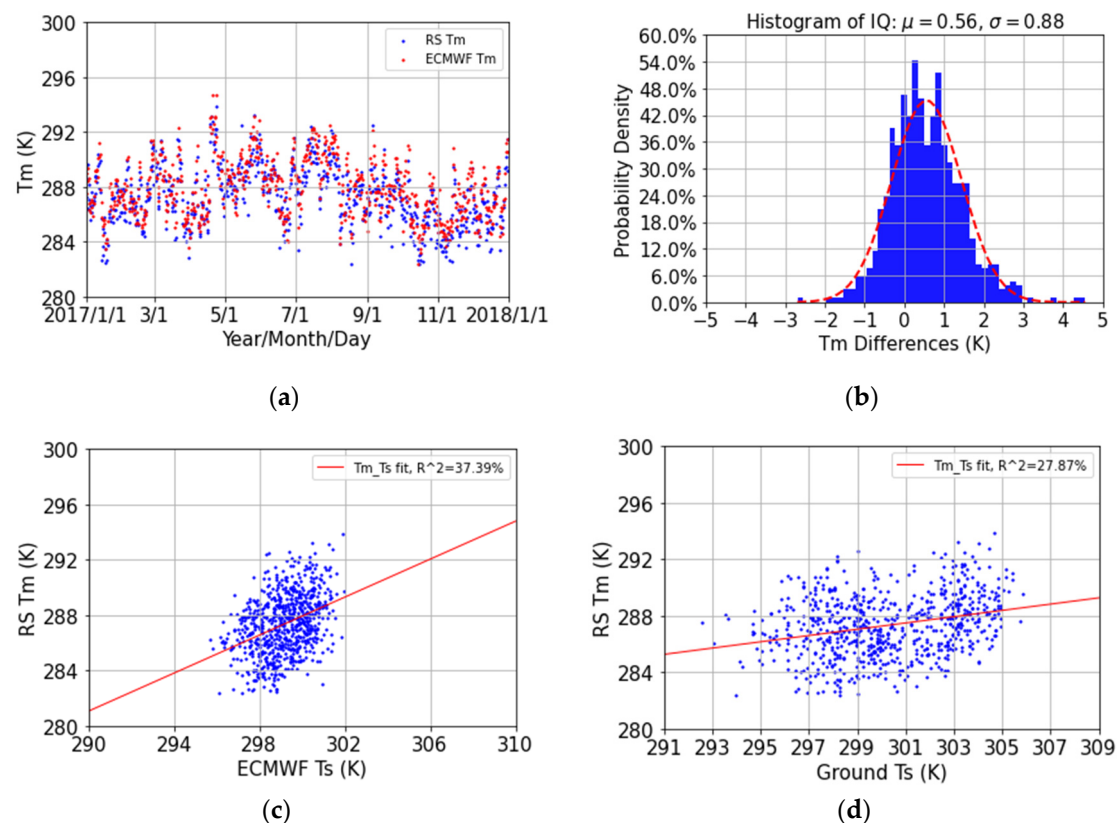
Figure 4. (**a**) FAA1 station: comparison between the $RS - T_m$ values computed from Equation (14) (blue dots) and the VMF1/ECMWF $- T_m$ values (red dots), and (**b**) histogram of the differences between the $RS - T_m$ values and the VMF1/ECMWF $- T_m$ values, and (**c**) linear fit between the $RS - T_m$ and the VMF1/ECMWF $- T_s$, and (**d**) linear fit between the $RS - T_m$ and the surface temperature measurements, T_s, from the FAA1 ground weather station.

We can now try to check a possible linear relationship noted $T_m - T_s$, based on the FAA1 surface temperature estimates, T_s, from the site-wise VMF1/ECMWF files (Figure 4c) or the FAA1 ground weather station (Figure 4d) and our weighted mean temperature, T_m, from RS measurements. In Figure 4c, the linear relationship between T_m and T_s is shown based on 724 RS profiles as $T_m = 0.69 \times T_s + 81.99$, with $R^2 = 37.39\%$ and an error bar of 6.01 K. In Figure 4d, the linear relationship between T_m and T_s is shown based on 724 RS profiles as $T_m = 0.22 \times T_s + 220.56$, with $R^2 = 27.879\%$ and an error bar of 6.22 K. Clearly, these fits are not good. We think that the main culprit is the small range of surface temperature, T_s, (10 K) in Tahiti over the year [24] that impairs a reliable estimation of the fit line, probably linked with instrumental difficulties for the balloon humidity sensor to measure accurately the high levels of water vapor present in the tropical location of Tahiti (Equation (7), see [53]).

4.4. Comparison of the ZWD Estimates from RS Data with the ZWD Estimates from VMF1/ECMWF Files

The next step is to compare our ZWD estimates from RS data (RS-ZWD) with ZWD estimates from VMF1/ECMWF records (VMF1/ECMWF-ZWD) for the FAA1 site. Our RS-ZWD estimates at the FAA1 station were calculated by using Equation (6). In our case, we did not consider the extension of the atmospheric column by the standard atmosphere, as it is void by construction of any water vapor. In Figure 5a, the consistency between the RS-ZWD and the VMF1/ECMWF-ZWD is also not very good, with an obvious bias of 28.43 mm (Table 5). In addition, the RMS between our RS-ZWD and VMF1/ECMWF-ZWD is also very large at about 34.57 mm (Table 5). Indicated by [39,54], the ZWD differences between ZWD estimates obtained from the VMF1/ECMWF files and ZWD derived by GPS data processing are very

large in terms of bias and STD up to a 2-cm level for the Kokee Park station (Kaua'i Island, Hawaii), with a climatic environment close to the one found in Tahiti.

We conclude that for the FAA1 station (and Kokee Park station), with a very high humidity, the large biases of Table 5 are mainly the result of a mismodeling of the wet contents of the atmosphere from the underlying numerical weather models, probably due to micro-local effects, as the resolution of the site-wise VMF1/ECMWF files (more than 200 km) is much larger than the dimensions of the Tahiti Island (30 km in diameter) or Kaua'i Island (35 km in diameter).
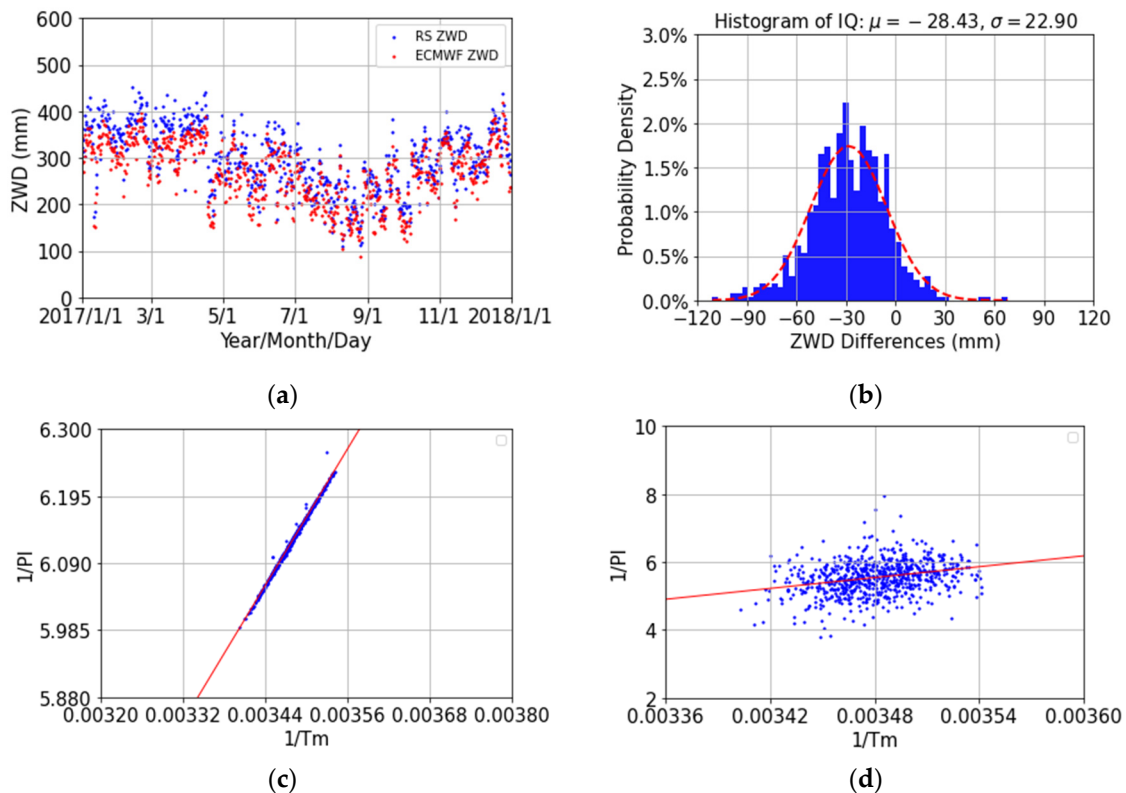
Figure 5. (**a**) FAA1 station: comparison between our RS-ZWD estimates (blue dots) with the ZWD estimates from VMF1/ECMWF (red dots); (**b**) histogram of the ZWD differences between the RS-ZWD values and the VMF1/ECMWF-ZWD values; (**c**) relationship between $1/\Pi$ ($1/P1$ for the y-axis, RS-ZWD/RS-PW) and $1/T_m$ (for the x-axis, RS $- T_m$), and their least-squares linear fit: $1/\Pi = 1779.61 * 1/T_m - 0.07$, with $R^2 = 99.78\%$ (red line); (**d**) relationship between $1/\Pi$ ($1/P2$ for the y-axis, GPS-ZWD (VMF1/ECMWF)/RS-PW) and $1/T_m$ (for the x-axis, RS $- T_m$), and their least-squares linear fit: $1/\Pi = 5322.56 * 1/T_m - 12.98$, with $R^2 = 28.38\%$ (red line).

Table 5. Statistical summary for the comparison between RS-ZWD and VMF1/ECMWF-ZWD (VMF1/ECMWF minus RS-ZWD) in terms of max, min, bias, STD, and RMS.

ZWD Differences	Max (mm)	Min (mm)	Bias (mm)	RMS (mm)	STD (mm)	Data Points
VMF1-RS	68.01	−111.01	−28.43	36.51	22.90	724

We then tested if the computation of the Π factor through Equation (13) is valid. For this purpose, we plotted, for the FAA1 station, the relation between $1/\Pi$ and $1/T_m$ that should be linear according to this equation. Based on Equation (12), the $1/\Pi$ factor can be estimated using a ZWD estimate divided by the corresponding PW estimate. This is indeed the case with a very high accuracy with RS $-$ ZWD and RS $-$ PW calculated through Equation (15) (Figure 5c, with $1/\Pi$ noted $1/\Pi1$). The linear relationship between $1/\Pi1$

and $1/T_m$ (T_m values are also from the RS measurements) is shown based on 724 RS profiles as $1/\Pi 1 = 1779.61 \times 1/T_m - 0.07$, with $R^2 = 99.78\%$ and an error bar of 0.01 K. Besides, we estimated $1/\Pi$ using GPS (VMF1/ECMWF)-ZWD divided by RS – PW (Figure 5d, with $1/\Pi$ noted $1/\Pi 2$). We have $1/\Pi 2 = 5322.56 \times 1/T_m - 12.98$, with $R^2 = 28.38\%$ and an error bar of 1.41 K.

The conclusion is straightforward; the underlying physics for the $T_m - T_s$ relationship is confirmed, even for the high levels of humidity found in Tahiti. We have to look at other possible causes for the violation of $T_m < T_s$.

4.5. Comparison of ZHD Estimates Based on the Saastamoinen Model with ZHD Estimates Based on Davis' Adapted Saastamoinen Model

The two most used empirical models, with an accuracy that is claimed to be at the mm-level for the determination of ZHD estimates, the Saastamoinen model (1972, Equation (9), noted here old-SAAS) and the Davis-Saastamoinen model, as modified by Davis et al. (1985, Equation (10), noted here new-SAAS), are analyzed in this section.

We used the VMF1/ECMWF pressure time-series for the FAA1 (Figure 6a,c) and THTI (Figure 6b,d) IGS stations, that are separated by a 2.56 km horizontal distance and an altitude difference of 86.14 m [10], to calculate ZHD estimates with respect to the two kinds of Saastamoinen models. A statistical summary is given in Table 6. For both stations, the ZHD estimates from the two kinds of Saastamoinen models are consistent with the ZHD VMF1/ECMWF estimates at the mm level.

(a)

(b)

(c)

(d)
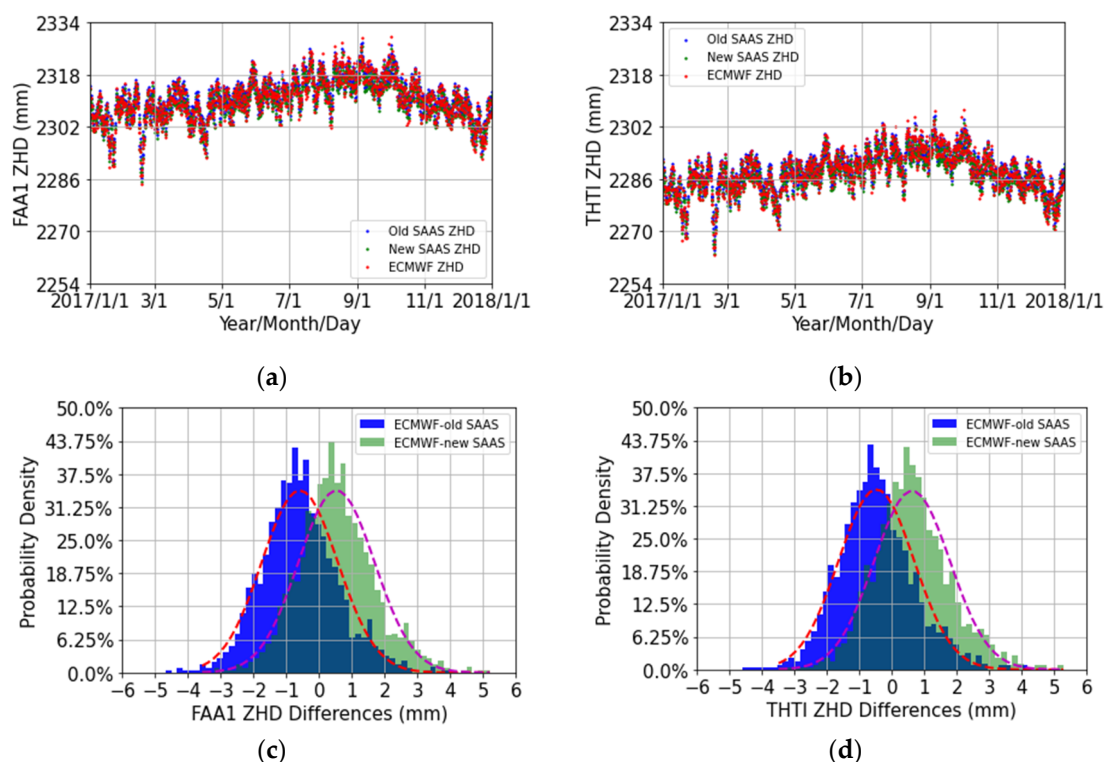
Figure 6. Comparisons of the new-SAAS ZHD estimates (green dots) and the old-SAAS ZHD estimates (blue dots) with the ZHD estimates from VMF1/ECMWF (red dots) for the FAA1 station (**a**), and the THTI station (**b**), and the histograms of their corresponding ZHD estimates differences at FAA1 station (**c**), and THTI station (**d**).

Table 6. Statistical summary for the comparison between the new/old SAAS ZHD estimates and the VMF1/ECMWF ZHD estimates (VMF1/ECMWF minus new/old) in terms of max, min, bias, STD, and RMS, for Figure 6c,d.

Differences	Max (mm)	Min (mm)	Bias (mm)	RMS (mm)	STD (mm)	Data Points
ECMWF-old FAA1	4.08	−4.68	−0.59	1.30	1.16	1461
ECMWF-new FAA1	5.20	−3.56	0.53	1.28	1.16	1461
ECMWF-old THTI	4.18	−4.60	−0.48	1.26	1.16	1461
ECMWF-new THTI	5.28	−3.49	0.62	1.32	1.17	1461

Zhang et al. (2016) [55] increased the numerator value in Equation (10) from 2.26768 to 2.2794 and claimed a global ZHD accuracy of less than 1 mm for this modified formula. This is certainly not true for our case, as this model is leading to a larger bias because of the large value in the numerator with respect to the Saastamoinen original and modified formulas.

4.6. Comparison of GPS ZTD Estimates with ZTD Estimates from RS Data and a Standard Atmosphere

In this section, based on Equation (5), we first calculate the ZHD estimates by using RS data from the surface of the Earth up to a balloon altitude of 30 km, and then we complement this value up to a 100 km altitude by using the vertical profiles from the U.S. Standard Atmosphere (SA) 1976 model [46].

Figure 7a shows that the comparison of ZHD estimates based on Davis-Saastamoinen model [17] with ZHD estimates derived from RS and SA. The consistency is obvious, with a bias of −3.00 mm and an RMS of 3.18 mm (Table 7).

(a)

(b)

(c)

(d)
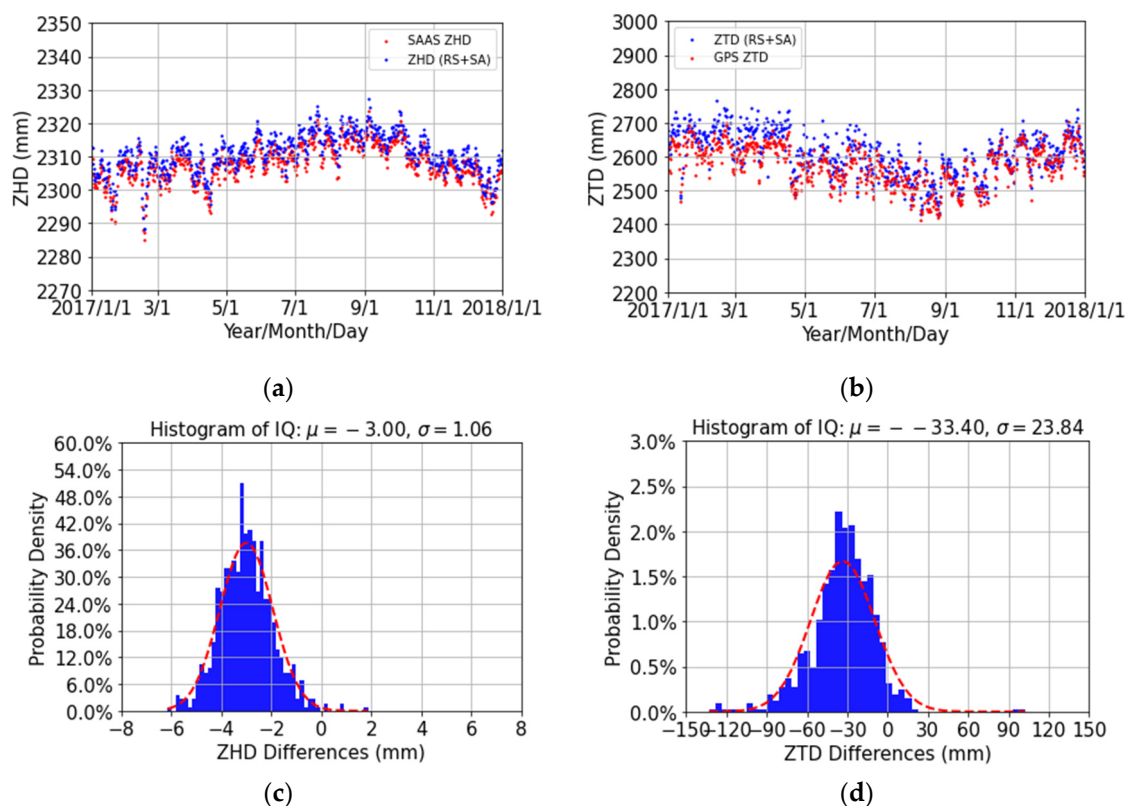
Figure 7. FAA1 station: (**a**) Comparison of ZHD estimates (RS + SA, ZHD1) (black dots) with ZHD estimates based on the new Saastamoinen model (ZHD2) (red dots); (**b**) Comparison of ZTD (RS + SA, ZTD1) (green dots) with GPS ZTD estimates (ZTD2) (red dots); (**c**) histograms of the ZHD differences between SAAS ZHD estimates and ZHD (RS + SA) estimates; (**d**) histograms of the ZTD differences between GPS ZTD estimates and ZTD (RS + SA) estimates.

Table 7. Statistical summary for Figure 7a,b for the comparison between ZHD1 and ZHD2 (ZHD2 minus ZHD1) and between ZTD1 and ZTD2 (ZTD2 minus ZTD1) in terms of max, min, bias, STD, and RMS.

Differences	Max (mm)	Min (mm)	Bias (mm)	RMS (mm)	STD (mm)	Data Points
ZHD2-ZHD1	1.87	−6.14	−3.00	3.18	1.06	724
ZTD2-ZTD1	102.61	−132.97	−33.40	41.04	23.84	689

It is very well known that the zenith tropospheric delay (ZTD) effect on GNSS signals is defined as the sum of a hydrostatic part (ZHD) and a wet part (ZWD), as ZTD = ZHD + ZWD. To justify this equation in our case, we build for the FAA1 station, ZTD (RS + SA) = ZHD (RS + SA) + ZWD (RS). As already stated, nearly all the water vapor is concentrated in the troposphere, so there is no need to complement the computation of ZWD by considering a continuation in altitude by the standard atmosphere. We made a comparison between ZTD (RS + SA) and ZTD derived from GPS in Figure 7b. There is a large bias of about 33.40 mm and a large RMS of about 41.04 mm.

Given the fact that the ZWD from RS is reliable (see Section 4.4), this large bias points to a culprit on the GPS side, probably linked with a common cause shared by both our local processing and the IGS processing. The common cause could be (see Table 1), but is certainly not limited to, the PPP approach and the Earth tide models (solid and oceanic) [56,57]. Considering the orbital period of one-half a sidereal day (approximately 11h 58m) for GPS satellites [58], and semidiurnal periods of tide effects [59], we assume all of them have effects on ZWD estimates with a common period of around 12 h, which may lead to an unfortunate addition of these possible errors.

5. Discussion

Through above analysis of all elements, we think that the reason for the large systematic error showing up in the last step of the previous comparisons (ZTD estimation) is related to external sources in the GNSS processing. Possible causes, and certainly intertwined causes, could be orbits/clocks errors in the PPP corrections [49,51,60] and errors in the tide models (Earth tides, oceanic tides and loading models) [61–63]. It should be also noted that the THTI and FAA1 receivers used in this study are IGS stations belonging to the network of reference stations used in the PPP corrections [64] and that GNSS orbits and tides share a common periodicity of 12 h. From a physical point of view, the tides are showing up at two places: (1) their gravitational pull on the GNSS satellites; (2) the modulation in the receiver position. It is far beyond the scope of this paper, and of the practical resources of the authors, to pinpoint the exact cause(s) of the ZTD mismodeling in Tahiti, but the first idea that comes to mind is the remoteness of the Tahiti Island in the central South Pacific, with degraded accuracies in some underlying physical models for this specific location.

6. Conclusions

This paper was motivated by the results of a previous study [24] that pointed to overlarge values of the mean temperature of the troposphere for the tropical location of the Tahiti Island. To understand the reason(s) of these overestimations, we examined all the links of the computation chain leading to the mean temperature estimate. We first evaluated the accuracy of the ZTD estimates derived from our GPS data processing, based on a comparison with the CODE/IGS final products at two local IGS sites, FAA1 and THTI. We found that our ZTD estimates and CODE/IGS ZTD estimates are coherent at a millimeter level. Secondly, we compared the surface temperature measurements and estimates at FAA1 from a ground weather station, from the IGRA RS balloons launched from the same site and from the VMF1/ECMWF site-wise records. They all are coherent at the 1 K level. Thirdly, the weighted mean temperature of the atmosphere was estimated from the RS measurements (temperature and humidity) taken from the FAA1 balloon launch site and compared with the T_m values

derived from the FAA1 site-wise VMF1/ECMWF records. We found that the T_m estimates from the RS data and the T_m estimates from VMF1/ECMWF are coherent within 0.56 K. This point also confirmed the underlying physical assumptions at the base of the $T_m - T_s$ linear relationship. Fourthly, ZWD estimates were calculated by using the RS data at the FAA1 site and were compared with the corresponding ZWD values computed from the corresponding site-wise VMF1/ECMWF records. We found a large bias of 28.43 mm, indicating that the VMF1/ECMWF model is not a reliable source for estimating the water vapor contents of the troposphere, probably because its resolution in space and time is not enough to capture the high variability of water vapor at our scale. Fifthly, we calculated the ZHD estimates for the FAA1 site from the RS balloon data completed up to 100 km altitude by the U.S. Standard Atmosphere 1976 model. We found a bias of 3.00 mm and an RMS of 3.18 mm between these ZHD estimates and the ZHD estimates computed from the Saastamoinen model. Finally, we compared our ZTD (RS + SA) estimates with the ZTD estimates derived from our GPS data processing. We found a large bias of 33.40 mm associated with a large RMS of 41.04 mm.

If we take these elements together, we find that anomalous T_m values for the Tahiti Island are traced to anomalous ZTD, leading to an accuracy poorer by one order of magnitude than the claimed accuracy of ZTD delays from worldwide databases. The reason for the large systematic errors of these ZTD estimates is assumed to be related to external sources in the GNSS data processing. Although it is not practical to pinpoint the exact causes of the ZTD mismodelling in Tahiti, the first idea coming to mind is that the remote Tahiti Island in the central South Pacific may suffer from degraded accuracies in some underlying physical models for this specific location.

Author Contributions: Conceptualization, F.Z. conceived and performed the experiments under the supervision of J.-P.B.; F.Z., P.F., G.X. and J.-P.B. analyzed the data; F.Z. wrote the paper. All authors have read and agreed to the published version of the manuscript.

Data Availability Statement: The data presented in this study are available on request from the corresponding author.

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Appendix A

The bias, RMS and STD, are used to quality the performances of the results with respect to the corresponding reference data. The formula is as follows [10]:

$$Bias = \frac{1}{n} \sum_{i=1}^{n} (G_i - R_i), \tag{A1}$$

$$RMS = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (G_i - R_i)^2}, \tag{A2}$$

$$STD = \sqrt{\frac{1}{n} \sum_{i=1}^{n} ((G_i - R_i) - Bias)^2}, \tag{A3}$$

where $i = 1, 2, 3, \ldots n$. n denotes the total number of data points. In this case, G denotes our results from GNSS data processing and R is the reference data.

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