

Article

# Ice Thickness Estimation from Geophysical Investigations on the Terminal Lobes of Belvedere Glacier (NW Italian Alps)

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**Abstract:** Alpine glaciers are key components of local and regional hydrogeological cycles and real-time indicators of climate change. Volume variations are primary targets of investigation for the understanding of ongoing modifications and the forecast of possible future scenarios. These fluctuations can be traced from time-lapse monitoring of the glacier topography. A detailed reconstruction of the ice bottom morphology is however needed to provide total volume and reliable mass balance estimations. Non-destructive geophysical techniques can support these investigations. With the aim of characterizing ice bottom depth, ground-penetrating radar (GPR) profiles and single-station passive seismic measurements were acquired on the terminal lobes of Belvedere Glacier (NW Italian Alps). The glacier is covered by blocks and debris and its rough topography is rapidly evolving in last years, with opening and relocation of crevasses and diffuse instabilities in the frontal sectors. Despite the challenging working environment, ground-based GPR surveys were performed in the period 2016–2018, using 70-MHz and 40-MHz antennas. The 3D ice bottom morphology was reconstructed for both frontal lobes and a detailed ice thickness map was obtained. GPR results also suggested some information on ice bottom properties. The glacier was found to probably lay on a thick sequence (more than 40 m) of subglacial deposits, rather than on stiff bedrock. Weak deeper reflectors were identified only in the frontal portion of the northern lobe. These interfaces may indicate the bedrock presence at a depth of around 80 m from the topographic surface, rapidly deepening upstream. Single-station passive seismic measurements, processed with the horizontal-to-vertical spectral ratio (HVSR) method, pointed out the absence of sharp vertical contrast in acoustic impedance between ice and bottom materials, globally confirming the hypotheses made on GPR results. The obtained results have been compared with previous independent geophysical investigations, performed in 1961 and 1985, with the same aim of ice thickness estimation. The comparison allowed us to validate the results obtained in the different surveys, supply a reference base map for the glacier bottom morphology and potentially study ice thickness variations over time.

**Keywords:** Alpine glaciers; Belvedere Glacier; ice thickness estimation; ice bottom morphology and properties; ground-penetrating radar (GPR); single-station passive seismic measurements; horizontal-to-vertical spectral ratio (HVSR)

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## 1. Introduction

Mountain glaciers are visible indicators of climate change, providing some of the clearest evidence of global warming, perturbation in the atmospheric flow pattern and consequent precipitation regime.

Due to their relatively small size and high mass turnover rates, these glacial bodies demonstrate extremely sensitive to temperature and precipitation modifications [1,2]. For the European continent, Alpine glaciers are a key component of local and regional hydrogeological cycles. The globally observed retreat of these ice masses over the last century has significant impacts on the surrounding environment, affecting both physical and socioeconomic systems [3–5]. The loss of freshwater storage and its consequent release into seas and oceans, modifications in resource availability for water consumption, irrigation and power generation, glacier-related natural hazards (e.g., landslides, avalanches and outburst of glacial lakes, causing floods and debris flows) are between the potential consequences of the general shrinkage trend.

Variations in glacier volume and mass are therefore primary targets of investigation for the understanding of ongoing modifications and the forecast of possible future scenarios. Remote sensing techniques (e.g., geodetic surveys, satellite images, GNSS or LiDAR surveys) can help to monitor these fluctuations [6–9] from accurate time-lapse reconstructions of the topographic surface of the glacier. Comprehensive knowledge of the ice bottom depth and morphology is however needed to provide a total volume estimate and reliable mass balance evaluations [10–12]. Ice thickness characterization and monitoring are also of primary importance for the modeling of future glacier dynamics [13], hydrological projections [14], glacier-related natural hazards [15] and ice core analyses [16].

Traditional glaciological measurements, i.e., local probe deployment for snow and firn/ice thickness variations or density measurements, are usually limited to the shallowest part of the glacier and do not extensively cover wide areas of investigations. Despite their relevance, ice bottom depth and morphology are often poorly known, mainly due to inadequate characterization methods and logistical issues. Geophysical methods can overcome these limitations, mitigating the operational efforts and enlarging the depth of investigation and data density of traditional techniques.

In the last decades, the ground-penetrating radar (GPR) technique has assumed an increasingly important role in the glacial exploration for the imaging of subsurface conditions [17]. The non-magnetic and low-conductive snow/ice column is indeed generally favorable for the efficient propagation of electromagnetic (EM) pulses, enabling a successful mapping of bottom morphology. In addition, GPR can also help in the evaluation of the glacier bottom properties, the search for internal water floods or underground channels and the recognition of internal glacial structures (as snow layering and crevasses detection). Several GPR applications are reported in the literature on Arctic and Antarctic ice caps and high-elevation icefields of the Tibetan Plateau [18–21]. Growing applications are also recorded in the Alpine context. Del Longo et al. [22] acquired GPR profiles on a Dolomitic glacier to identify the ice bottom depth. Binder et al. [23] investigated two glaciers in the Austrian Alps, for determination of total ice volume and ice-thickness distribution. Merz et al. [24] acquired a dense grid of helicopter-borne GPR, combined with ground-based seismic and geoelectric profiles, on a rock glacier of western Swiss Alps to reconstruct the 3D bedrock topography. Airborne GPR surveying generally overcomes problems in accessibility of the steeper glacier sectors and wave scattering on large boulders in close vicinity of the antenna, which are particularly disturbing in case of debris-cover and rock glaciers. Dossi et al. [25] performed quantitative 3D GPR analysis to estimate the total volume and water content of a glacier in Eastern Alps.

Techniques complementary to GPR surveys have also been applied. Maurer and Hauck [26] reviewed possible additional methods and proposed the joint interpretation of GPR, geoelectric and seismic surveys for analyzing the subsurface conditions of two rock glaciers in the Eastern Swiss Alps, with a special focus on the distribution of ice and water, the occurrence of shear horizons and the bedrock topography. However, geoelectric and reflection seismic methods require long arrays to reach considerable investigation depths and high-resolution imaging of the glacier subsurface, thus complicating field operations. Single-station passive seismic measurements may offer an effective and logistically affordable method to mitigate the problems of multi-channel active surveys, thanks to the use of portable and compact broadband seismometers and no need of energetic active sources. Picotti et al. [27] presented a pioneer study on the application of single-station passive measurements

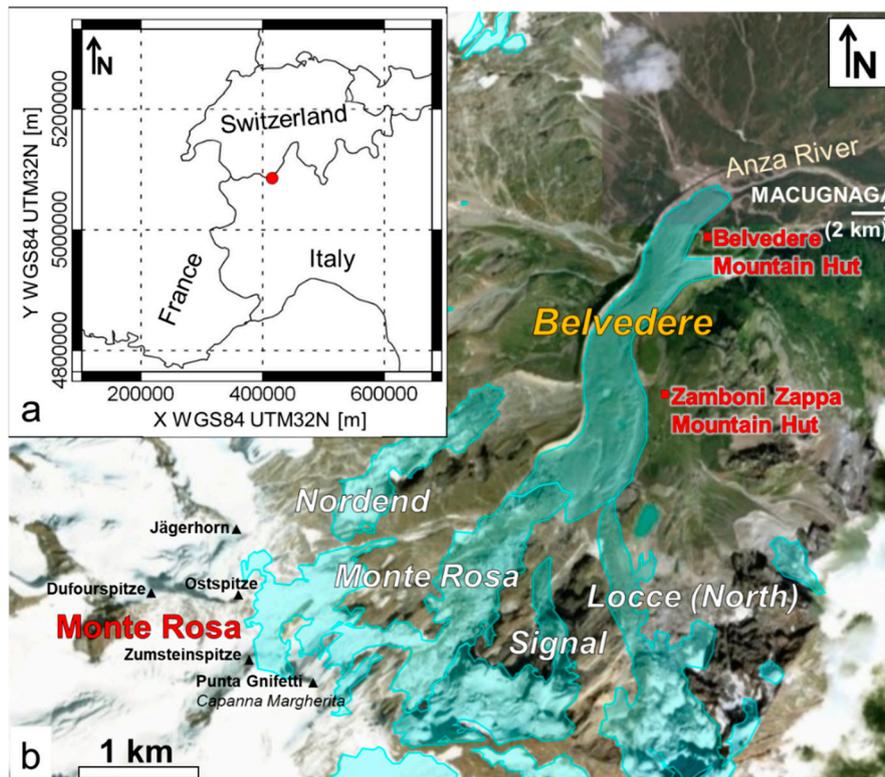
to determine ice thickness on five Alpine glaciers. Data were processed with the horizontal-to-vertical spectral ratio (HVSR, [28,29]) technique and validated using GPR, geoelectric and active seismic profiling methods. The HVSR method is based on the computation of the ratio between the spectra of the horizontal and vertical components of a triaxial seismic station, to retrieve the fundamental resonance frequency of a site [30,31]. Generally, the resonance originates from the trapping of seismic waves in sites with sufficiently high S-wave impedance contrast (e.g., soft sediments overlying a stiff bedrock). For these sites, a clear peak is found in the HVSR curve. The frequency of this peak is related to the depth of the interface between the two materials [32]. The origin of the HVSR peak is still debated and generally related to a superposition of Rayleigh-, Love- and/or shear-wave resonances [33].

In a glacial environment, the impedance contrast between ice and bedrock is expected to generate resonance phenomena and similar effects on the HVSR curves. Comparing HVSR data with other geophysical imaging results, Picotti et al. [27] showed that the resonance frequency depicted in the HVSR curves is correlated with the ice thickness at the site, in a wide range of ice bottom depths, from few tens of meters to more than 800 m. The reliability of the method mainly depends on the coupling of the sensor at the glacier surface and on the basal impedance contrast. However, beside the intrinsic limitation of the 1D approximation, very few Alpine glaciers lay directly on stiff bedrock for all their extent, while a basal layer of subglacial deposits and debris of significant thickness is generally present below the ablation zone [34], thus attenuating the vertical impedance contrast.

In this study, we acquired both GPR profiles and single-station passive seismic measurements on the terminal lobes of the debris-covered Belvedere Glacier (Macugnaga, NW Italian Alps), with the aim of ice thickness estimation and bottom morphology reconstruction. Very poor and conflicting reference information on ice thickness is indeed available for the glacier, from previous geophysical investigation attempts [35,36]. GPR data acquired in different seasons and with different antennas were processed and manual picking of the bottom surface was performed on the radargrams showing the clearest subsurface imaging. Retrieved ice depths were then spatially interpolated to reconstruct the 3D bottom morphology and compared with previous geophysical results [35,36]. Some single-station passive seismic tests were performed in the same area imaged with GPR profiles. Seismic recordings were processed with the HVSR method and interpreted in the light of the GPR results, for a combined evaluation attempt of the ice bottom morphology and properties.

## 2. Study Site

Belvedere Glacier is a debris-covered glacier located NE of the highest peaks of Monte Rosa Massif, in NW Italian Alps (Figure 1). Thanks to the debris cover and the favorable solar exposure, its frontal sectors reach considerably low altitudes and end approximately 2 km W of Macugnaga (VB). Belvedere Glacier represents the terminus of four higher-elevation glaciers (Nordend, Monte Rosa, Signal and Northern Locce Glaciers). Measurements of the Italian Glaciological Committee (CGI-CNR, <http://www.glaciologia.it/i-ghiacciai-italiani>) carried out in 2006 indicated a surface area of 1.46 km<sup>2</sup>, a maximum length of 3091 m, spanning in elevation from 2397 m to 1770 m above sea level (a.s.l.), with an average slope of 8°. The terminal portion of the glacier is bilobate. Both lobes are currently exhibiting a visible retreat. Nowadays, the bigger N lobe has an average length of 650 m, reaching a minimum elevation of about 1810 m a.s.l. (i.e., 40 m higher than measurements of 2006), while the S lobe has a length of 350 m, reaching an elevation of 1840 m a.s.l. at its front. The two lobes are separated by a median morainic relief, hosting the chair lift station and the Belvedere Mountain Hut (Figure 1).



**Figure 1.** (a) Geographical location and (b) aerial view of the north-eastern glaciers of the Monte Rosa Massif. The main glacial masses are delimited by light blue areas (modified from the Italian Glaciological Committee (CGI-CNR), <http://www.glaciologia.it/i-ghiacciai-italiani>).

Despite several glaciological studies were carried out on site since the beginning of the 20th century [37,38], the first attempt towards ice thickness characterization is reported by De Visintini [35]. P-wave reflection seismic measurements were indeed carried out on the glacier in 1957 for ice bottom contouring. Explosive sources were adopted, and the active shots were recorded with a 12-channel analog seismograph. Seven local areas of the glacier were surveyed with seismic profiling, from the vicinity of the Zamboni Zappa Mountain Hut (Figure 1), down to the confluence between the two lobes. A global contour map of ice bottom depth was achieved from the interpolation of these measurements, even if some glaciers parts (e.g., the two terminal lobes) were not investigated during this survey.

A later study by VAW-ETH [36] was performed using the GPR technique, with the aim of completing ice bottom characterization in unexplored compartments. A low-frequency GPR instrumentation (USGS Monopulse-radar, with variable central frequency in the range 1–5 MHz) was adopted, with 40 sparse measurements located along 9 transverse profiles covering almost all the glacier length. For each measurement, the time delays between the transmitted EM pulse and the received echoes were recorded. The highest-amplitudes echoes were referred to ice bottom reflections, their depth was estimated from the time delay (considering a constant velocity of the EM pulse in ice) and an interpretation of the bottom morphology was retrieved from data interpolation along the 9 cross-sections.

In the upper part of the glacier (W and SW of Zamboni Zappa Mountain Hut) both radar and seismic results seemed to locate the bedrock at depths of 200–250 m. Progressing northwards, major discrepancies in ice bottom determination arose between the two techniques. Particularly, radar bottom reflectors were found to be located approximately 100 m higher than the seismic reflectors in the central part of the glacier. The two techniques, sensitive to different physical changes in the subsurface, seemed therefore to identify different interfaces. This difference in ice bottom location was interpreted as the result of the presence of a layer of subglacial deposits with relevant thickness (up to

more than 100 m in the central part of the glacier) between ice and bedrock. Glacial deposits revealed transparent to the seismic reflection profiling, but were identified by the radar investigation, probably due to the significant contrast in electrical properties between these sediments and ice.

In a more recent work, Diolaiuti et al. [39] estimated the changes in ice volume between 1957 and 1991 and measured the debris thickness above the whole glacier area. The debris cover was indeed found to slow down the ablation rate of Belvedere Glacier, with respect to other similar glaciers of the same region lacking this peculiarity. A contour map of ice thickness was also presented. However, this map was based just on the results of reflection seismic [35] and did not consider the possible lower ice thicknesses, due to the presence of thick subglacial deposits, as highlighted by the later radar study [36].

In the last decades, geophysical prospection experienced greatly advanced in instrumentation, acquisition and processing techniques. Digital multi-channel recordings and high-sampling big data storage capacities allow for continuous radar profiling with respect to the study of VAW-ETH [36]. Passive seismic acquisitions require lighter instrumentation and no active sources with respect to the measurements of De Visintini [35]. At the light of these advances, new geophysical prospections at the site can therefore help in understanding the discrepancies between the previous works and provide new and more extensive information on the glacier bottom morphology and properties. Despite these considerations, the presence of blocks and debris with variable thickness and lateral distribution at the surface, the rough topography and heterogeneities inside the investigated glacial mass deeply complicate data acquisition and potentially affect the quality of the final results.

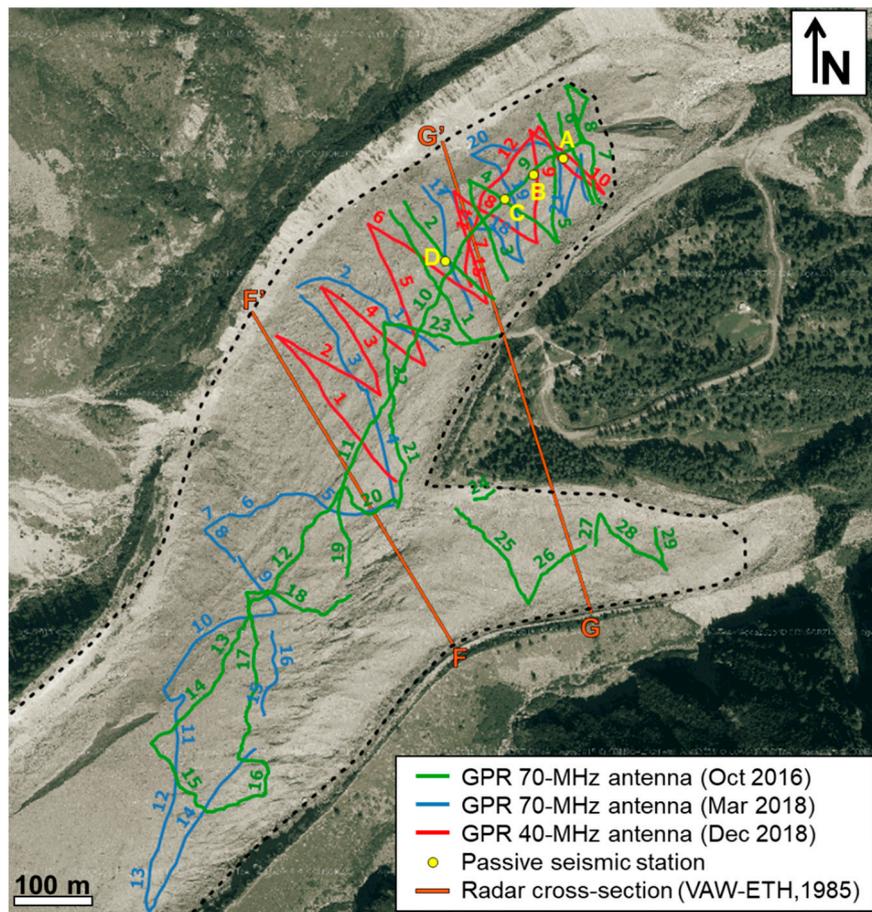
### 3. Methods

#### 3.1. Ground-Penetrating Radar

Several GPR campaigns were carried out at the Belvedere Glacier between 2016 and 2018. In October 2016, 29 GPR profiles were acquired with an air-coupled 70-MHz GPR monostatic antenna (Subecho-70, Radarteam), for a total surveyed length of 2169 m (blue traces in Figure 2). The antenna was connected to an IDS K2 TR200 acquisition unit and manually transported above the ground surface. Traces were recorded for a total length of 1000 ns, with a sampling of 1024 samples/trace, and georeferenced by means of a GPS Ublox EVK-5T system.

In March 2018, 22 radar profiles were acquired with the same air-coupled 70-MHz antenna (green traces in Figure 2) transported on skis, for a total length of 2696 m of acquisitions (trace length = 2000 ns, 2048 samples/trace).

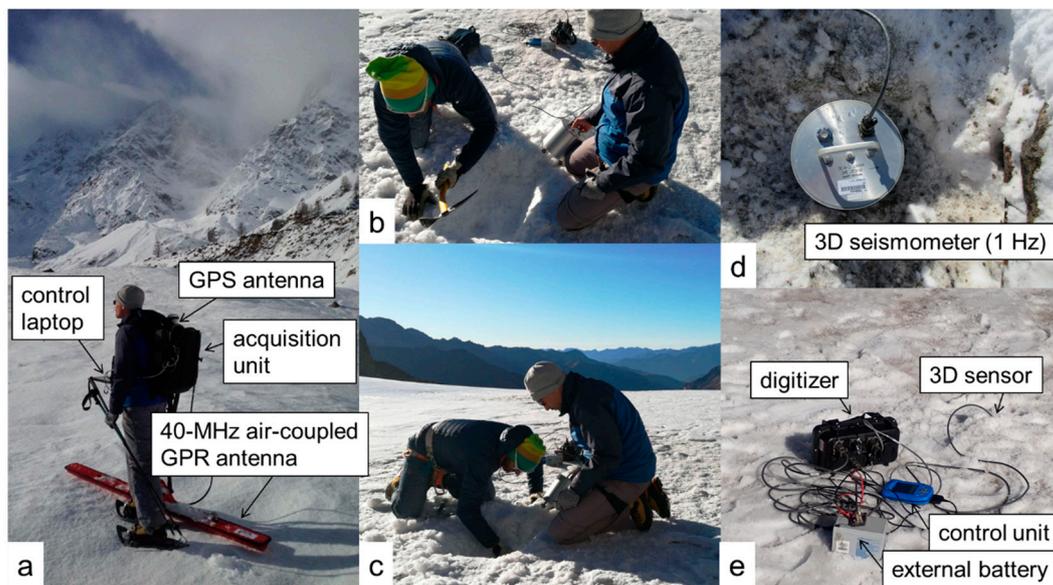
Finally, in December 2018 a lower frequency (40 MHz, Subecho-40, Radarteam) air-coupled antenna was manually moved along 15 profiles (red traces in Figure 2) focused on the terminal sector of the northern lobe of the glacier, for a total length of 2169 m of acquisitions (total recorded trace length = 1200 ns, 1024 samples/trace). The acquisition setup is shown in Figure 3a. The same acquisition unit and georeferencing instruments of October 2016 were adopted in all the later campaigns. In all surveys, the snow cover on site was limited (from absent to a few tens of centimeters on the debris cover). Unfortunately, due to the rough and rapidly evolving topography of the glacier along the years, the opening and/or relocation of crevasses and diffuse instabilities in the frontal sectors, it was not possible to follow the same profiles in each survey operating in safe conditions. In addition, due to the shape of both low-frequency antennas and the encountered topographic conditions, it was not possible to direct drag the instruments on the glacier surface to maximize the coupling. In each survey, the antenna was consequently maintained a few centimeters above the thin layer of snow partially hiding the cover of blocks and debris of the glacier (Figure 3a).



**Figure 2.** Geophysical surveys carried out at the Belvedere Glacier. Green lines: 70-MHz ground-penetrating radar (GPR) profiles acquired on October 2016; blue lines: 70-MHz GPR profiles acquired on March 2018; red lines: 40-MHz GPR profiles acquired on December 2018. GPR profiles are labelled with a progressive number for each survey. Yellow dots (A–D): Single-station passive seismic measurements (HVSr method). Orange lines (FF' and GG'): Past cross-sections of the glacier interpreted from radar measurements, from VAW-ETH [36]. The background orthophoto was acquired during summer 2015 (AGEA 2015, RGB orthophoto, WMS service at [www.geoportale.piemonte.it](http://www.geoportale.piemonte.it)). The black dashed line highlights the approximate glacier perimeter in October 2016 (first GPR campaign).

Data processing was performed in ReflexW software. A basic processing procedure was adopted: (i) Start time of each trace was shifted to delete samples before the main bang and obtain exact zero time; (ii) low-frequency components were removed (dewow); (iii) high-pass horizontal filtering was applied to remove horizontally coherent components (background removal); (iv) geometrical spreading correction was applied, to gain signal amplitude with depth (divergence compensation).

Manual picking of the ice bottom reflections was finally performed on the processed time sections. Due to the reduced snow cover during the surveys, the picking of the reference glacier topography (corresponding to the top of the debris cover) was neglected. A uniform ice velocity of 0.17 m/ns was considered for a time to depth conversion, disregarding the top debris cover. The latter is expected to have significant lateral and vertical variations, from a few centimeters up to a metric thickness in correspondence of boulders and blocks.



**Figure 3.** On-site operations for GPR and passive seismic acquisitions. (a) GPR instrumentation and acquisition setup. Note that the GPR antenna is not ground-coupled, but maintained a few centimeters above the ground surface during acquisition. (b–e) Installation of the broadband triaxial seismometer and passive seismic instrumentation details.

### 3.2. Single-Station Passive Seismic Measurements

Four single-station passive seismic measurements were carried out on the N lobe of the Belvedere Glacier (A to D, in Figure 2). A 3-D 1-Hz broadband seismometer (L-4-3D, Sercel Inc.) connected to a 24-bit 3-channel digitizer was adopted for the acquisitions. To obtain the best coupling between sensor and ice, the surface layers of snow, ice, and debris were removed. The 3D seismometer was placed in direct contact with compact ice and then buried with the excavated materials to minimize external noise (Figure 3b–e). At each station, noise recording lasted from 30 to 45 min, with a sampling frequency of 100 Hz.

Details on the theoretical formulation and assumption underling the application of the HVSR methods in a glacial environment can be found in Picotti et al. [27]. If the width of the glacier is considerably larger than the ice thickness, the subsurface conditions can be approximated with a 1D model for which:

$$f_0 = \frac{V_S}{4H}, \quad (1)$$

where  $f_0$  is the resonance frequency depicted from the HVSR curve,  $V_S$  is the average S-wave velocity of ice and  $H$  is the ice thickness. If 2D effects are present at the station,  $f_0$  value should be multiplied by correcting factors accounting for the shape of the basin [27,40]. Station locations along the axial position of the N lobe were chosen to minimize 2D lateral effects, due to the valley sides.

HVSR computation was carried out in Geopsy software. The original recordings (30–45 min) were divided into 120-s non-overlapping windows. An anti-triggering STA/LTA (short time average over long time average) algorithm was applied to each time window. This filtering procedure is based on the computation of the average signal amplitude over short (STA = 1 s) and long (LTA = 30 s) moving windows. If the STA/LTA ratio exceeds user-defined thresholds (STA/LTA < 0.2 or STA/LTA > 2.5, in this study), the window is filtered out from further computations. Otherwise, amplitude spectra of the horizontal components are combined using vector summation and the horizontal to vertical spectral ratio is computed. A smoothing function, with a 10% cosine taper and a bandwidth coefficient of 30 [32], was then applied to the resulting HVSR curve to ensure a constant number of points at low and high frequencies. This computation was repeated for all the 120-s windows passing

the anti-triggering filter. The average curve and the standard deviation over the accepted HVSR curves were finally obtained. The spatial directivity of the HVSR peaks was computed using the same processing parameters, to check for the absence of 2D effects on the detected resonance frequencies.

The results were analyzed to search for HVSR peaks clearly indicating the presence of sharp subsurface contrasts in acoustic impedance and potentially estimate their embedment depth. Since no clear peaks were detected, further processing attempts, including inverse [41] or forward modeling [42,43] of the measured HVSR curves were not undertaken.

## 4. Results

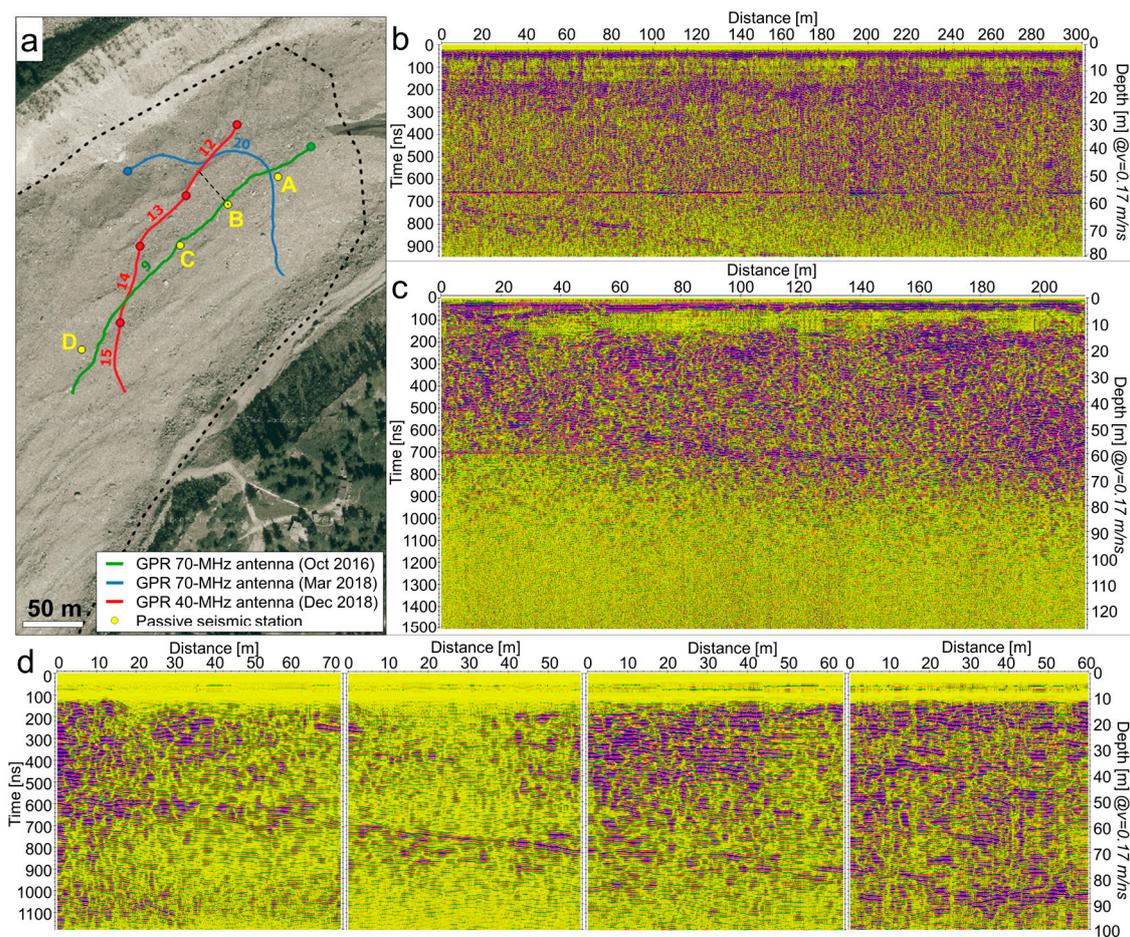
### 4.1. Ground-Penetrating Radar

Representative radargrams obtained from the three GPR campaigns are shown in Figure 4. Some clear artifacts, due to electromagnetic noise are still visible in the data, even after the described processing sequence, e.g., the horizontal events at 650 ns and 700 ns in Figure 4b,c. The overall data quality is very poor if compared with the typical S/N ratio of GPR data acquired on other glaciers. High scattering is noticed along the profiles, with extremely high attenuation of the EM signals with depth. Not always clear readability in the processed profiles was observed for the 70-MHz surveys. Even increasing the total recording time (Figure 4c compared to Figure 4b), no reflections were observable in the data below 900 ns. Better results were obtained with the 40-MHz antenna (Figure 4d). In these radargrams, reflections appear more clearly and can be spatially followed and correlated between adjacent profiles. An exemplificative marked interpretation of the ice bottom morphology on the radargrams of Figure 4 is reported in Figure 5. Similar interpretations have been performed on the remaining profiles of the different campaigns for which ice bottom picking was clear and reliable.

The ice bottom appears as a discontinuous reflecting horizon in all the surveys. Layering with different orientations is noticed in some parts of the radargrams at the ice bottom location (e.g., distance = 38 m, time = 1000 ns in profile 15 of Figures 4d and 5d). A low-amplitude reflector deeper than the ice bottom is depicted in profile 12 of Figures 4d and 5d. This interface is characterized by a steeper dipping with respect to the ice bottom, in dip direction opposite to the glacier movement, reaching times higher than 1150 ns (depth > 100 m) in the center of the profile, at a distance of approximately 120 m from the glacier front.

In Figure 5c,d, the approximate locations (A' to D' and A'' to D'') of the single-station passive seismic measurements (A to D) are projected on the GPR sections, for further comparisons between the two geophysical methods.

The results of ice bottom picking along GPR profiles are summarized in Figure 6. All the 40-MHz radargrams provided quite clear imaging of the subsurface conditions. Conversely, only 12 radargrams acquired on October 2016 (70 MHz) supplied information on ice thickness, close to the front of the N lobe, on the S lobe and at the confluence. These areas correspond to generally lower ice thicknesses with respect to the surrounding zones. Analogously, the 70-MHz GPR campaign of March 2018 resulted in only 5 radargrams for which ice bottom picking was clearly interpretable. No information on ice thickness was recovered from the GPR data for the glacier main body, upstream the terminal bifurcation (Figure 6a). Ice thickness retrieved from ice bottom picking is shown in Figure 6b. A traditional U-shaped bottom morphology seems to be reconstructed for the N lobe, with considerable ice depths in the axial part (100–110 m) despite the proximity to the terminus. The S lobe is conversely characterized by significantly shallower ice depths and a probably flatter morphology.

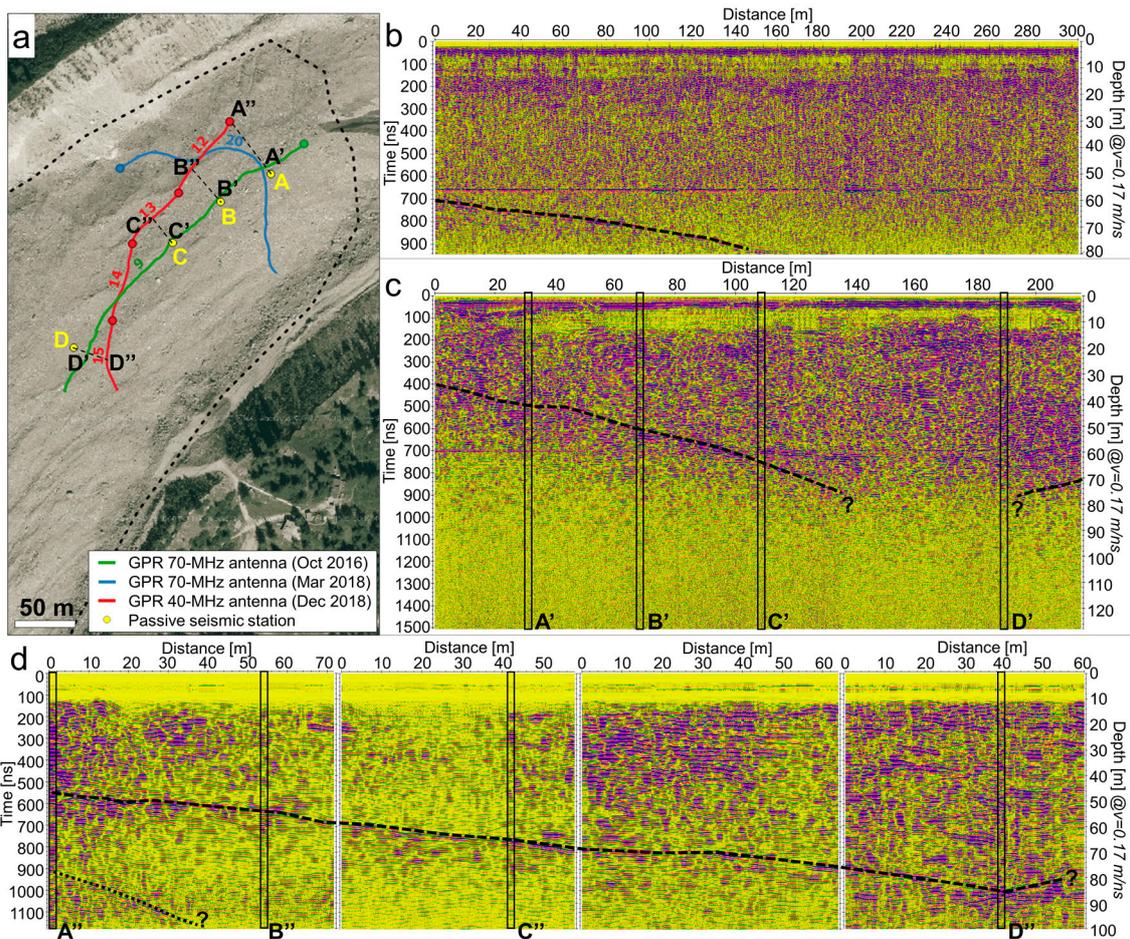


**Figure 4.** GPR results. (a) Location of the GPR profiles are shown in the right and bottom sections. The starting point of each profile is highlighted with a dot. (b) Profile 9 (70-MHz antenna, October 2016). (c) Profile 20 (70-MHz antenna, March 2018). (d) Profile 12 to 15 (left to right, 40-MHz antenna, December 2018). The vertical scale of some radargram is cut (no reflections for higher recorded times).

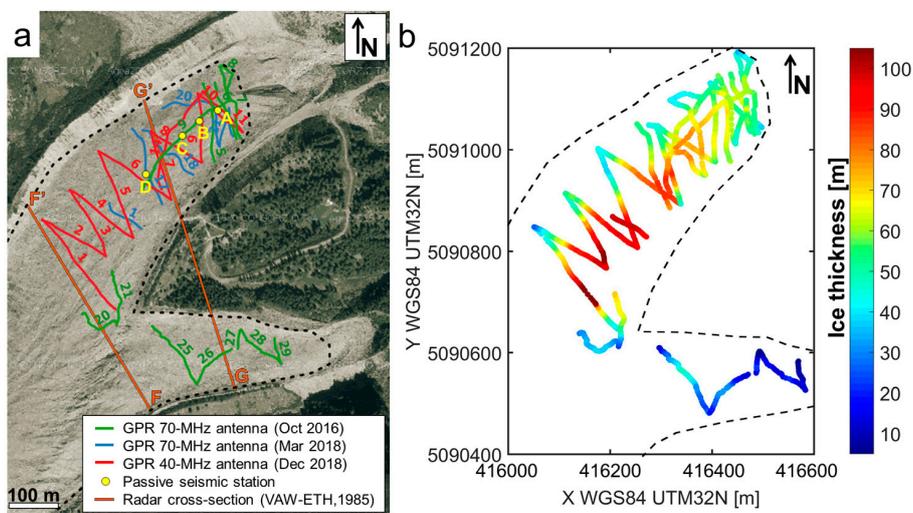
#### 4.2. Single-Station Passive Seismic Measurements

The results of HVSR processing are shown in Figure 7. No clear single peaks are found in the results, at least two to three HVSR minor peaks can be depicted for each station. HVSR amplification is low ( $<2$ ) for all the measured points. For the first three stations, the peak with the highest amplitude ( $f_0$ ) is located at similar frequency values, progressively decreasing from A to C. A higher frequency peak is noticed at station D.

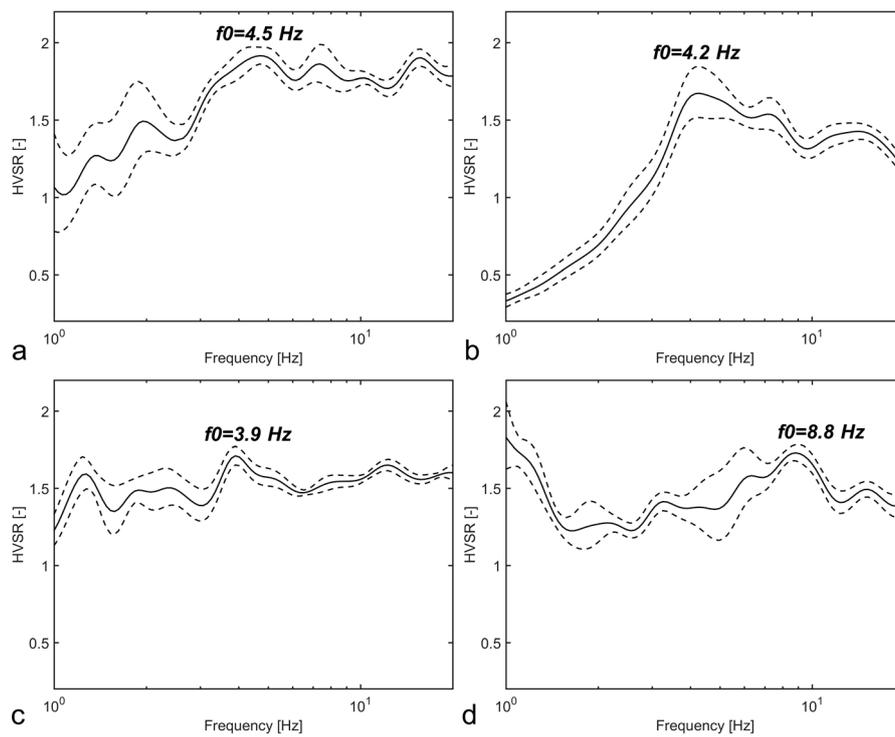
Figure 8 shows HVSR directivity, as a function of frequency and azimuth ( $0^\circ = N$ ,  $90^\circ = E$ ), measured at the four stations. These results clearly highlight that  $f_0$  spectral peaks spread over a wide azimuthal range, covering from  $100^\circ$  to  $180^\circ$ . These resonance frequencies seem therefore almost azimuth independent, denoting the absence of 2-D effects. The secondary peaks located at frequencies lower than 3 Hz conversely showed more focused directivities.



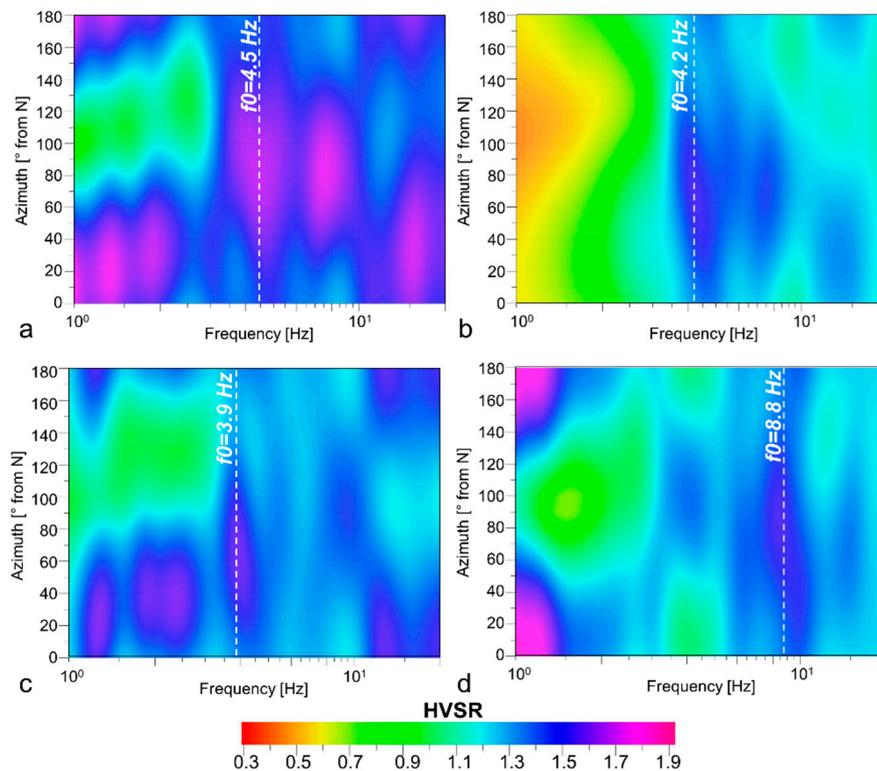
**Figure 5.** GPR results (same as Figure 4) with glacier bottom interpretation. The ice bottom morphology is highlighted in the radargrams with the dashed black lines. The possible bedrock top is underlined in (d) with the dotted black line. The approximate location of single-station passive measurements projected on the GPR profiles is shown in (a) with letters A' to D' (on 70-MHz profile 9) and A'' to D'' (on 40-MHz profiles 12 to 15), and in (c,d) with the black rectangles, for further comparison between GPR and HVSR results.



**Figure 6.** (a) Summary of the GPR profiles for which ice bottom picking was retrieved. (b) Map of the resulting ice bottom picks.



**Figure 7.** HVSR results on stations (a) A, (b) B, (c) C and (d) D (location in Figure 2). In each panel, the black bold and dashed curves are the average and standard deviation obtained from all the accepted 120-s window curves for each station.



**Figure 8.** Directional HVSR azimuth (in degrees from N direction) on stations (a) A, (b) B, (c) C and (d) D. In each panel, the white dashed lines highlight the location of the highest spectral peaks ( $f_0$ ) identified in Figure 7.

## 5. Discussion

Geophysical characterization of rock glaciers and debris-covered glaciers is usually complicated by several factors: Logistically challenging and expensive transport of equipment and personnel on site, extremely rugged topographic conditions inhibiting antenna dragging on the surface, and inaccessibility of some areas, due to safety concerns [44]. In addition, despite the advances in geophysical prospection and instrumentation of the last decades with respect to the previous reference ice bottom investigations carried out on the Belvedere Glacier, recent surveys are not free of interpretation issues. Widespread scattering and high attenuation of the EM signals, often referred to as clutter, are noticed in all the 70-MHz GPR profiles. Slightly better results are obtained with a lower frequency of the GPR antenna (40 MHz vs. 70 MHz). No information is however retrieved for depths higher than 100–150 m below the glacier surface.

Many causes may have contributed to the poor quality of GPR imaging on this glacier. The absence of direct coupling with the ground, with possible centimetric variations in the height of the antenna, limits the amount of EM energy inserted in the subsurface, resulting in rapidly decreasing energy to image the reflectors with depth and laterally variable trace amplitudes. In addition, the presence of the top debris cover, characterized by extreme variability in grain size, thickness and lateral distribution, generates diffuse scattering and attenuation of the EM pulses transmitted to the underlying ice column, with respect to GPR prospections in glaciers lacking this surface layer. Pecci et al. [45] discussed the negative clutter effects on GPR data quality caused by the surface debris cover with a highly variable thickness of Calderone Glacier (Central Apennines, Italy). Intense clutter phenomena were observed also at a depth of few meters from the surface and were related to the presence of ice layers containing a high concentration of debris. As a consequence, the reflectors corresponding to the ice-bedrock interface could not be clearly and continuously detected.

Similar results were obtained on a debris-covered glacier of Italian Dolomites [22]. Most of the GPR scans pointed out the presence of intense clutter effects, due to the presence of heterometric debris at the surface. Authors were able to detect the ice-bedrock only with an acquisition adopting bistatic antennas in parallel-polarized modality. This arrangement was observed to be more sensitive to buried targets oriented parallel to the main axes of the antennas and relatively insensitive to depolarized scattered fields. However, moving this configuration on a rugged topography could be a logistical issue, especially when low-frequency antennas with long dipoles are adopted.

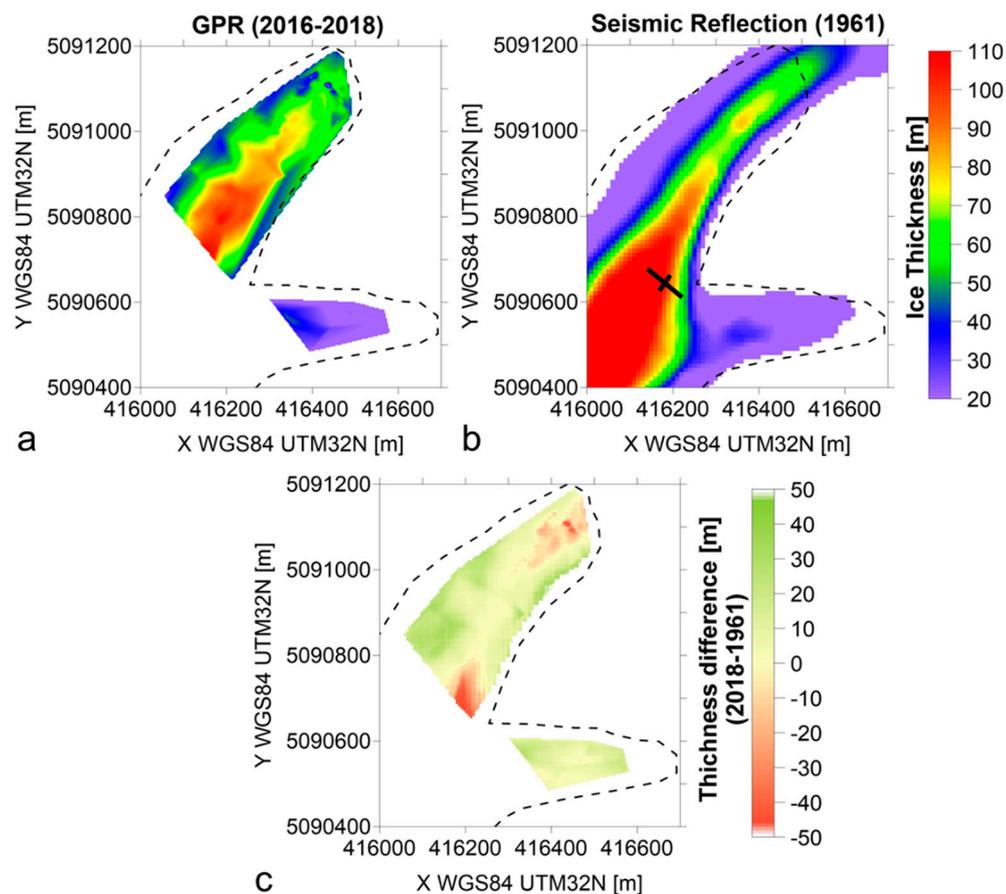
Despite these considerations, the presence of debris at the surface and the use of air-coupled antennas are common to other GPR surveys in debris-covered glaciers and rock glaciers (e.g., [24,26]) which led to satisfactory data quality. As a consequence, we hypothesize that widespread internal heterogeneities in the glacier mass may have had an additional and primary role in scattering and attenuation of the GPR signals. Beside the possible widespread presence of solid rock debris within the ice body [45], enhanced radar scattering, due to water englacial inhomogeneities is reported by several authors. Bamber [46] performed a numerical analysis to quantify the back scattering of water-filled cavities on the scale of decimeters affecting GPR results on several glaciers in Svalbard Islands. Numerical results illustrated the difficulties that may be encountered while sounding temperate glaciers possessing widespread englacial water bodies and explained the absence of bed echoes in the accumulation zone of these glaciers. GPR profiles collected by Murray et al. [47] in the ablation zone of Tsanfleuron Glacier (Swiss Alps) and Bakaninbreen Glacier (Svalbard) showed a two-layered structure, with an upper layer characterized by low returned GPR power and a lower layer of strong scattering. The thickness of these layers was observed to rapidly change along the profiles at both sites. At Tsanfleuron Glacier, the two layers were interpreted as dry ice, with a water content of 1.18%, overlapping ice containing small water bodies, up to decimeter in size, occupying 3.90% by volume. At Bakaninbreen Glacier, the upper radar layer was interpreted as cold ice with no measurable water-content and the lower layer as warm ice with a water content of 1.29%. Barrett et al. [48] modeled layers of randomly distributed scatters of decimeter-scale dimensions with an undulating upper boundary or confined to obliquely dipping planes to reproduce the scattering effects noticed on

the radargrams acquired on Bakaninbreen Glacier. Numerical results supported the hypothesis that scattering originates from multiple planar sets of water-filled cavities. These features are expected to be common in glaciers surging by a thermally regulated soft bed mechanism, both at the end of the surge and into early quiescence phases. The presence of surge-type movements at the Belvedere Glacier, supporting the hypothesis of abundant water presence within the glacial mass, is well-documented in the literature [49].

As a consequence of the poor GPR data quality, ice thickness estimation was possible only in the glacier sectors characterized by the lowest ice thickness. Layering with different orientations, probably indicating the overlap of lateral morainic deposits on the bottom materials, was found to locally emphasize the bottom morphology. Only close to the terminus of the N lobe, deeper and steeper reflectors were imaged below the ice bottom. These observations suggest that the glacier bottom is not characterized by stiff bedrock, but by a thick sequence of fine-grained glacial deposits, as already hypothesized in the study of VAW-ETH [36]. If this hypothesis is valid, the glacial deposits have an average thickness of 40 m close to the glacier front and bedrock is located at a depth of approximately 80 m (e.g., rectangle A'' in Figure 5d). The thickness of the bottom deposits rapidly increases upstream if the steep dipping of bedrock is constant.

Single-station passive seismic measurements confirmed the absence of sharp acoustic impedance contrasts in the glacier subsurface. The lack of a single clear peaks with high HVSR amplification values are a key piece of evidence for the absence of ice in direct contact with stiff bedrock. The occurrence of a multi-layered subsurface, with several weak contrasts in acoustic impedance at depth, can conversely help to explain the obtained HVSR results. The progressive lowering in the frequency of  $f_0$  peak from station A to C (Figure 7) is coherent with the presence of interfaces which are progressively deeper upstream, as highlighted in the GPR results (Figure 5d). HVSR complex results are however difficult to interpret with single simplified equations (e.g., Equation (1)), due to the existence of multiple interfaces whose resonance phenomena are superimposed. The stratigraphic condition appearing from all the above considerations is also at the limit of validity of the assumptions underlying further processing and interpretation of the measured curves. Despite the challenging working environment and investigated ice mass, a comparison between past and present geophysical surveys at the Belvedere Glacier is worthy of investigation. The ice-thickness map obtained from triangulation with linear interpolation of the GPR bottom peaks (Figure 6b) is shown in Figure 9a. The map confirms the previous observations of a traditional U-shaped bottom morphology for the N lobe and of shallow ice depths and flatter bottom surface for the S lobe. A digitized version of the ice thickness map of De Visintini [35], reported in Diolaiuti et al. [39], is shown for the same area of the glacier in Figure 9b. It must be noticed that the only reflection seismic measurements on this area were performed at the confluence of the two lobes (black bold lines in Figure 9b) and no data coverage was directly available on the lobes. As a consequence, this map is the result of a more approximated data interpretation with respect to the continuous GPR profiling from which Figure 9a is derived. Despite these considerations, Figure 9c shows the difference in ice thickness between the present and past maps.

A general agreement in ice thickness estimation is found along the axial position of the N lobe and on a wide area of the south lobe. Visible negative values (reduction in ice thickness) are found close to the northern front, underlying the accelerating retreat and shrinkage of the glacier in recent times. A visible decrease in ice thickness is also noticed close to the confluence between the lobes. This result can be considered quite reliable given the good data coverage of both present and previous surveys close to this point. By contrast, the unrealistic increases in ice thickness close to the glacier sides are more likely due to an erroneous approximation of ice thickness in the past study, rather than to a significant increase in ice volume in these marginal sectors.

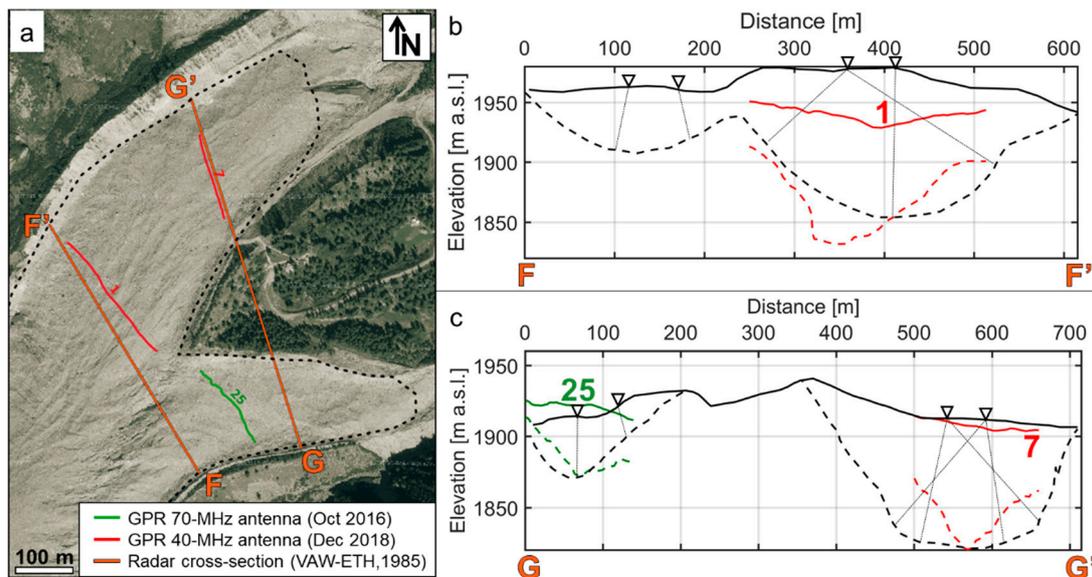


**Figure 9.** (a) Interpolated glacier bottom map from GPR results (2016–2018). (b) Reference glacier bottom map from De Visintini [35] and Diolaiuti et al. [39]. The black bold lines in (b) indicate the location of the only seismic reflection measurements in the area of interest. (c) Difference between (a) and (b) maps. The black dashed line highlights the approximate glacier perimeter in October 2016 (first GPR campaign).

An independent comparison between the glacier cross-sections obtained from the interpretation of the radar measurements of VAW-ETH [36] and the closest GPR profiles of the present study is presented in Figure 10. In this case, the adopted geophysical technique is the same, even if in different frequency bands. Both surveys should therefore have depicted the same interfaces. The ice bottom morphology presented in the previous work (black dashed lines in Figure 10b,c) is however the results of only two points of measure on each lobe (white triangles in Figure 10b,c), for both FF' and GG' sections [36] and not of continuous profiling.

Along the FF' cross-section, the 40-MHz profile 1 shows a depressed glacier topography with respect to the one of 1985. An acceptable discrepancy of around 15 m between the maximum ice bottom depth of the two surveys is noticed. Major differences in the morphology of the bottom surface are observed between the two campaigns. Recent GPR profiles outline a narrower and more asymmetric section of the N lobe, steeper on the side of the moraine hosting the Belvedere Mountain Hat. It is however interesting to notice that the reflection points related to the ray paths of two radar measurements performed on the N lobe well overlap with the recent bottom estimation from continuous GPR profiling. The lateral discrepancies can therefore be explained as the consequence of insufficient lateral data coverage of previous surveys. Similar results are found on GG' cross-section. Along this section, the topographic variations appear less marked on the N lobe. On the S lobe, profile 25 has higher topography than previous data, due to the fact that it is located almost 100 m upstream the reference GG' section trace. A good agreement between the present and past data is however

found for the S lobe bottom. On the N lobe, the maximum depth depicted in the two surveys is the same, but the GPR profile 7 defines again a narrower ice bottom section. A wider and smoother bottom morphology was considered during the interpretation of previous radar measurements and a clear mismatch is observed between the two surveys. Differently from the original data interpretation, past radar echoes (and related ray paths) were probably originated from the deepest and narrowest axial sector of the glacial valley rather than from the lateral moraines. This comparison definitely highlights the undeniable advantages of continuous GPR profiling in maximizing data coverage and improving bottom morphology reconstruction, with respect to previous sparse and local measurements.



**Figure 10.** Comparison between the radar cross-sections of VAW-ETH [36] and the closest GPR profiles of the present study with successful glacier bottom picking. (a) Location of the profiles. (b) Section FF'. (c) Section GG'. The original data interpretation is shown in black (white triangles and gray rays indicate the radar measurement points and the interpreted EM ray paths as reported in [36]), while recent GPR results are shown in red for Profiles 1 and 7 (40 MHz, December 2018) and in green for Profile 25 (70 MHz, October 2016). Bold line: Topography, dashed line: Estimated ice bottom location.

## 6. Conclusions

Geophysical surveys, including 40-MHz and 70-MHz GPR profiling and single-station passive seismic measurements, were acquired at the Belvedere Glacier with the aim of ice thickness reconstruction. The surveys were intended to fill a knowledge gap on the glacier bottom morphology, since the existing bottom information was only retrieved from sparse and local past geophysical measurements. Despite a dense GPR survey distribution, the ice bottom surface was detected only in radargrams acquired on the frontal lobes, while noisy and uninterpretable results were obtained upstream. The globally observed low data quality was attributed to the presence of a widespread debris cover, the absence of direct coupling between antenna and glacier surface and the probable widespread presence of debris and/or small-scale water bodies within the ice column. The concurrence of all these features probably caused the observed significant scattering and attenuation of the transmitted EM pulses. The lower frequency 40-MHz survey generally showed clearer results. Ice thickness estimations based on these results were interpolated to reconstruct a detailed ice thickness map that was compared with the previous study of De Visintini [35]. Some discrepancies between the two estimations arose, mainly due to different data coverage and acceleration in the glacier retreat over the last decades. A better fitting with the results of the radar measurements of VAW-ETH [36] was obtained. Also in this case, continuous GPR profiling provided denser data coverage with respect to previous local measurements, enabling for a better definition of the ice bottom morphology. Significant

ice thickness variations were detected in the upper part of the N lobe, with a transition from convex to concave glacier topography. Below the ice bottom, low-amplitude reflectors having steeper dip were identified only in the frontal portion of the N lobe. These elements may indicate the bedrock presence at a depth of around 80 m from the glacier surface close to the northern terminus and rapidly deepening upstream. Consequently, a thick layer (more than 40 m) of subglacial deposits may be present between ice and bedrock.

Single-station passive seismic measurements were processed following the HVSR method. The results showed the absence of a clear contrast in acoustic impedance (i.e., ice on bedrock) at depth, providing at least a general confirmation of the hypothesized subsurface conditions. However, without the reference GPR profiles, no information on the ice bottom could have been retrieved from HVSR curves. These tests highlighted the limitations of passive seismic measurements for glacier characterization, i.e., 1D approximation of the investigated subsurface, need to simultaneously have a dense grid of measurements but avoiding 2D effects, time-consuming acquisitions with respect to continuous GPR profiling, poor results in absence of a bottom ice-bedrock interface. Differently from GPR investigations, for which the denser data coverage of continuous profiling revealed the key point to improve the past knowledge about bottom morphology, due to the peculiar investigated conditions passive seismic methods did not succeed in improving past active seismic results, despite the lighter instrumentation, logistically easier acquisition and no need of active sources.

Future perspectives of the method may be addressed to glacier monitoring. Multi-station long-term passive seismic measurements can potentially be used for the investigation of the ongoing glacial processes (hydrogeological modifications, meltwater flow, seepage and accumulation) and of the glacier movements and stability conditions (e.g., icequakes, opening of crevasses, basal movements, serac falls and stability of the frontal compartments).

Further glaciological analyses are planned to understand the influence of the glacier subsurface conditions on the measured geophysical data. Future geophysical campaigns on site should be addressed to reach satisfactory imaging of the glacier bottom in the upstream sectors, and to monitor ice thickness variations over the investigated frontal areas. Alternative survey configurations, including the test of parallel-polarized antennas for data collection, will be tested to map the ice bottom, reducing the effect of clutter on GPR data quality.

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