Temperature Estimation for Photovoltaic Array Using an Adaptive Neuro Fuzzy Inference System

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Abstract: Module temperature is an important parameter of photovoltaic energy systems since their performance is affected by its variation. Several cooling controllers require a precise estimation of module temperature to reduce excessive heating and power losses. In this work, an adaptive neuro fuzzy inference system technique is developed for temperature estimation of photovoltaic systems. For the learning process, experimental measurements comprising six environmental variables (temperature, irradiance, wind velocity, wind direction, relative humidity, and atmospheric pressure) and one operational variable (photovoltaic power output) were used as training parameters. The proposed predictive model comprises a zero-order Sugeno neuro fuzzy system with two generalized bell-shaped membership functions per input and 128 fuzzy rules. The model is validated with experimental information from an instrumented photovoltaic system with a fitness correlation parameter of $R = 95\%$. The obtained results indicate that the proposed methodology provides a reliable tool for estimation of modules temperature based on environmental variables. The developed algorithm can be implemented as part of a cooling control system of photovoltaic modules to reduce the efficiency losses.

Keywords: solar energy; temperature photovoltaic cell; photovoltaic performance; sensitivity analysis; artificial intelligence modeling

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1. Introduction

Solar energy has become one of the most attractive renewable energy sources since it is abundant, environmentally friendly, and safe. These characteristics have led many countries to pay attention on the design policies, strategies, and technology for its use [1–4]. In this context, photovoltaic (PV) systems are one of the most mature solar technologies, and it is constantly increasing its competitiveness and decreasing its production costs [5]. For these reasons, PV installations have been considered as a promising alternative to meet the growing demand for electrical energy by the industrial and residential sector [5,6].

On PV systems, the energy conversion process is highly dependent on irradiance. However, irradiance in peak hours produces adverse effects increasing PV module temperature and reducing the module’s performance [7]. A high module temperature produces a reduction of PV efficiency due to the consequent low values of open circuit voltage, fill factor, and power output [8].

Several cooling techniques have been implemented to reduce PV module operating temperature and the consequent efficiency losses [1,9,10]. Nevertheless, in most cases, their implementation...
requires measurement of the PV temperature using sensors that are usually imprecise. Moreover, the measurement system requires maintenance and calibration, and they are sensitive to climate variations. These factors make them unreliable when the measurement systems are used on a long-term basis [11,12]. An alternative to solve this issue is the use of mathematical and computational models to indirectly estimate the system variables.

Several expressions that correlate PV module temperature as a function of diode PV model electronic parameters (resistance, current, voltage, band gap, etc.) [13], material, and system-dependent properties (glazing-cover transmittance, plate absorptance, etc.) [14], can be found in the relevant literature. In practice, it is complicated to know or obtain the majority of these parameters under long periods of operation. Moreover, it is widely documented that external weather parameters such as environmental temperature, wind speed, wind direction, atmospheric pressure, and relative humidity [15–18], influence the behavior of PV temperature with high complexity. Therefore, the aim of the present work is the development of an adaptive mathematical model of the PV temperature considering the variability and nonlinear behavior of the environmental parameters [19,20].

In recent years, artificial intelligence (AI) methods have proven to be a powerful tool for nonlinear complex engineering applications. The main advantages of these computational tools are their versatility, robustness, fast computing process, and optimization achieved through learning processes [21,22]. AI methods have been successfully applied in many renewable energy problems [23–29]. In [23] artificial neural networks (ANN) and genetic algorithms (GA) have been used to predict the thermal efficiency of steam generation plants. Yaïci et al. employed ANN and adaptive neuro fuzzy inference system (ANFIS) for modeling the performance of solar thermal systems [24,25]. Wind speed and wind direction have been forecasted using artificial intelligence algorithms as particle swarm optimization (PSO) and GA [26,27]. Bassam et al. [28] used ANN to estimate the static formation temperatures in geothermal wells. Fuzzy logic algorithms have been employed to design strategies for wind farm efficiency estimation [29].

Among AI modeling methods, adaptive neuro fuzzy inference system (ANFIS) is considered one of the most feasible tools to predict energy systems performance [25]. Several studies on PV technology have been developed using ANFIS. Mellit et al. [30] developed an ANFIS model to predict the optimal sizing coefficient of PV systems based only on geographical coordinates. The results obtained were compared and analyzed with artificial neural networks (ANN) proving that ANFIS model presents the most accurate results. Mohanty [31] generated an ANFIS model to predict monthly solar global radiation for PV system sizing using sunshine duration, ambient temperature, humidity, and clearness index as inputs. The model exhibited an absolute percentage error of 0.48, which yielded better results compared to other methods such as ANN and support vector machine (SVM). Mellit and Kalogirou [32] developed ANFIS models for different components of PV systems such as the generator, battery, and regulator. They designed a global model that combined different ANFIS models relative to each component of the PV system. The components of the global model were trained using various input data. The developed model predicts electrical variables of each component in the PV system using measurements of environmental temperature, irradiation, and clearness index. On the other hand, several studies related to PV maximum power point tracking (MPPT) using ANFIS have been reported in the literature [33–35]. These techniques improve the operation efficiency of the systems using input variables as short circuit current (I_{sc}), open circuit voltage (V_{oc}), environmental temperature, irradiation, and others.

In the present work, a new model based on ANFIS methodology to estimate the operation temperature of a PV array is proposed. The rest of this paper is organized as follows: the second section describes the environmental variables that influence the temperature of PV modules, the experimental PV array monitoring, and ANFIS theory. The third section develops the methodology employed in the modeling process by ANFIS technique. The fourth section presents the obtained results, and the last section contains the conclusions.
2. Materials and Methods

2.1. PV Module Performance

In PV industry, the performance of PV modules is evaluated by the standard test conditions (STC), the results of which are reported in the manufacturers’ PV module datasheet. In [13] the PV temperature \( T_{PV} \) is derived from \( I_o = B T_{PV}^3 e^{-E_g/(kT_{PV})} \), where \( I_o \) is the reverse saturation current of the diode PV model, \( E_g \) is the band gap of silicon, and \( B \) is a temperature-independent constant. Notton et al. [36] described a correlation between PV efficiency \( \eta \) and \( T_{PV} \) given by a linear relation \( \eta = \eta_{T_{ref}} \left[ 1 - \beta (T_{PV} - T_{ref}) + \gamma \log_{10} G_t \right] \), which depends of reference temperature \( T_{ref} \), temperature coefficient \( \beta \), radiation coefficient \( \gamma \), and direct irradiance \( G_t \). Chow et al. [37] establish a model to estimate the PV array power output \( P_{PV} \) as a function of \( T_{PV} \) given by \( P_{PV} = \eta A G_t p \tau_g \left[ 1 - \beta (T_{PV} - 25) \right] \) where \( p \) is a packing factor and \( \tau_g \) is the glazing transmissivity. Nevertheless, in practice, PV module efficiency is dependent on geographical location and its respective climatological conditions [38]. Several studies indicate that in tropical climates the power supplied by the module in the field can be 30% lower than expected [39]. Among environmental variables that affect the performance of PV module are: temperature \( T_a \), solar radiation \( G \), wind velocity \( W_v \), wind direction \( W_d \), relative humidity \( RH \), and atmospheric pressure \( P_{at} \).

- **Effect of environmental temperature.** Similar to other semiconductor devices, solar cells are sensitive to temperature. An increase in temperature reduces the band gap of a semiconductor, affecting most of the semiconductor material parameters. The decrease in the band gap of a semiconductor with increasing temperature can be viewed as an energy increase in the material’s electrons. Lower electronic energy is therefore needed to break the bond, yielding lower current values. In the bond model of a semiconductor band gap, reduction in the bond energy also reduces the band gap. Therefore, increasing the temperature reduces the band gap and consequently its performance. It has been proven that the conversion efficiency of PV modules drops progressively as dust is accumulated on its surface in the simultaneous presence of high temperature [15].

- **Effect of solar radiation.** Solar radiation is under constant changes throughout the day. It varies depending on geographical location, sun angle, cloudiness, month of the year, etc. An increment of solar radiation improves the module power output, but also increases its temperature, reducing the efficiency [40].

- **Effect of wind.** The wind lowers the module’s temperature, which helps to reduce the cell temperature, which is crucial to maintaining PV conversion efficiency [16].

- **Effect of relative humidity.** When water vapor interacts with solar radiation the light may be reflected, refracted or diffracted. This affects nonlinearity of the irradiance, and at the same time causes non-linear small variations in \( V_{oc} \) and large variations in \( I_{sc} \) [18,41].

- **Effect of atmospheric pressure.** Atmospheric pressure is a combination of air molecules with weight and movement. The change of air pressure causes the change of airflow on the surface of PV modules, which affects heat dissipation and causes module temperature fluctuation [17].

2.2. Experimental System Description

The experimental system consists of a static PV array located at the Engineering Faculty of the Autonomous University of Yucatan, in Merida, Yucatan, Mexico. It comprises a 4 \( \times \) 4 PV array built with Siemens SR100 PV monocrystalline modules. The PV modules are south oriented with a tilt angle of 21°. Table 1 summarizes the properties of the PV system. Experimental data sets were collected during three years in 1-min measurements and 30-min averages to obtain representative samples of several weather conditions. All data was stored using a CR1000 datalogger and the software LoggerNet from the American company Campbell Scientific. The data was filtered to include only measurements obtained between 09:00 and 17:00 hours,
corresponding to the location’s peak hours of sunshine. The experimental setup and data acquisition process are illustrated in Figure 1.

### Table 1. Properties of the experimental PV array system.

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Latitude (°)</td>
<td>20°56' N</td>
</tr>
<tr>
<td>Longitude (°)</td>
<td>89°36' W</td>
</tr>
<tr>
<td>Tilt angle (°)</td>
<td>21°00'</td>
</tr>
<tr>
<td>Incident area (m²)</td>
<td>14.16</td>
</tr>
<tr>
<td>Nominal output voltage (V) *</td>
<td>17.7</td>
</tr>
<tr>
<td>Nominal output current (A) *</td>
<td>5.6</td>
</tr>
</tbody>
</table>

* According to PV module datasheet.

Figure 1. Components of the experimental process.

Variables measured during the experimental operation were selected according to their influence on PV temperature array. To ensure the accuracy of the measurements, the standard deviations (SD) were computed for each 30-min series. Atmospheric variables, such as solar radiation \( G \), temperature \( T_a \), wind velocity \( W_v \), wind direction \( W_d \), relative humidity \( RH \), and atmospheric pressure \( P_{at} \), were measured by a weather station located immediately next to the PV installation. Solar radiation was converted to its equivalent plane-of-array (POA) irradiance to represent the interaction with the tilt of the modules [42]. The temperature of PV array \( T_{PV} \), was recorded as an average measured by infrared temperature sensors placed in contact with the backside center of the modules. On the other hand, the exposition to atmospheric variables causes a permanent degradation of the cells reducing their performance. Therefore, in the present study the use of PV power output \( P_{PV} \) as an operational variable for cell degradation assessment is proposed. PV voltage \( V_{PV} \) and PV current \( I_{PV} \) of the array were measured to estimate \( P_{PV} \), SD = ±0.4821 W. Table 2 contains the characteristics of employed sensors, which have low uncertainty and, therefore, guarantees data reliability.
Table 2. List of measurement devices.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Sensor</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>Solar radiation (G)</td>
<td>Campbell CS300-L Pyrometer</td>
<td>±5%</td>
</tr>
<tr>
<td>Environmental temperature (T_a)</td>
<td>Campbell CS215-L</td>
<td>±4%</td>
</tr>
<tr>
<td>Wind velocity (W_v)</td>
<td>WINDSONIC4-L</td>
<td>±2%</td>
</tr>
<tr>
<td>Wind direction (W_d)</td>
<td>WINDSONIC4-L</td>
<td>±3%</td>
</tr>
<tr>
<td>Relative humidity (RH)</td>
<td>Campbell CS215-L</td>
<td>±4%</td>
</tr>
<tr>
<td>Atmospheric pressure (P_a)</td>
<td>Campbell CS100</td>
<td>±1.0 mb</td>
</tr>
<tr>
<td>PV voltage (V_{PV})</td>
<td>TI LM747</td>
<td>±5%</td>
</tr>
<tr>
<td>PV current (I_{PV})</td>
<td>FW BELL NT-50</td>
<td>±0.30%</td>
</tr>
<tr>
<td>PV temperature module (T_{PV})</td>
<td>Sensor K-Type</td>
<td>±0.75%</td>
</tr>
</tbody>
</table>

2.3. Adaptive Neuro-Fuzzy Inference System (ANFIS)

An adaptive neuro-fuzzy inference system (ANFIS) is a computational technique of the AI family, developed by Jang [43]. ANFIS is a multilayer network combination of ANN learning algorithms and a fuzzy inference system (FIS) to map specific input parameters to an output value. It consists of conventional FIS components (rule base, database, and reasoning mechanism). The neural network’s learning capacity is provided to enhance the system knowledge [25,44]. Computations at each stage are performed by a layer of hidden neurons. There are two FIS types employed in ANFIS modeling called Mamdami and Sugeno, with Sugeno being the most used since it is more computationally efficient and works well with optimization and adaptive techniques [19]. The consequent parameters in Sugeno FIS can be a constant coefficient or a linear equation, called zero-order Sugeno and first-order Sugeno, respectively. Figure 2 illustrates a simple two-rule Sugeno ANFIS architecture with two inputs (x and y) and a single output (F), where A1, A2, B1, and B2 are the input membership functions.

The Sugeno ANFIS model uses fuzzy if-then rules. Equations (1) and (2) express the rules used for the architecture of Figure 2:

\[
\text{IF } x \text{ is } A1 \text{ and } y \text{ is } B1 \text{ THEN } f_1 = \begin{cases} 
  s_1 \text{ (zero-order Sugeno)} \\
  p_1x + q_1y + r_1 \text{ (first-order Sugeno)}
\end{cases} 
\]

\[
\text{IF } x \text{ is } A2 \text{ and } y \text{ is } B2 \text{ THEN } f_2 = \begin{cases} 
  s_2 \text{ (zero-order Sugeno)} \\
  p_2x + q_2y + r_2 \text{ (first-order Sugeno)}
\end{cases} 
\]

where \( s_i \) is the zero-order Sugeno consequent parameter, and \( p_i, q_i, \) and \( r_i \) are the first-order Sugeno consequent parameters. ANFIS model is composed by a five-layer architecture (Figure 2), where all the nodes in the same layer have a similar function [45]. Layer 1 is composed of membership function nodes. This layer converts the crisp input in fuzzy values, providing the inputs to the following layers. The output of this layer is given by:

\[
\sum \overline{w}_f_i f_i
\]
\[ O_{1,1} = \mu A_i(x) \]  
\[ O_{1,2} = \mu B_i(y) \]  
where \( \mu \) is the membership function, \( O_{1,i} \) is the membership value for the crisp inputs \( x \) and \( y \), and the subscripts 1 and \( i \) represent the layer number and node number, respectively.

Layer 2 contains the rule nodes. The nodes in this layer calculate the firing strength of a rule \( w_i \) as:

\[ O_{2,i} = w_i = \mu A_i(x) \mu B_i(y) \]  

In layer 3, each node calculates the ratio of the \( i \)-th rule’s firing strength to the sum of all rule firing strength (\( \bar{w} \)):

\[ O_{3,i} = \frac{w_i}{\sum w_i} \]  

Layer 4 calculates the rule outputs based on the consequent parameters (Equations (1) and (2)) and the output of the previous layer:

\[ O_{4,i} = \bar{w}_i f_i = \begin{cases} 
\bar{w}_i s_i \text{ (zero – order Sugeno)} \\
\bar{w}_i (p_i x + q_i y + r_i) \text{ (first – order Sugeno)} 
\end{cases} \]  

Finally, layer 5 computes the overall output adding all the inputs signals to get the output model value:

\[ O_{5,i} = \sum_i w_i f_i = \frac{\sum_i w_i f_i}{\sum w_i} \]  

3. ANFIS PV Module Modeling

A methodology comprising four steps is employed to estimate the temperature of the PV array considering the influence of atmospheric variables. Figure 3 illustrates a flowchart of the methodology employed.

(I) Database generation using experimental system measurement: The experimental database consists of datasets measured during the experimental system operation described in Section 2. Variables that integrate the database are solar radiation (\( G \), 1367–100 W/m²), temperature (\( T_a \), 39.53–9.56 °C), wind velocity (\( W_v \), 9.80–0.30 m/s), wind direction (\( W_d \), 360–0°), relative humidity (\( RH \), 97–25%), atmospheric pressure (\( P_{at} \), 103.2–100 Bar), temperature of PV array (\( T_{PV} \), 62.8–9.97 °C), and the PV array output power (\( P_{PV} \), 356–1.5 W). The SD of the variables were included in the database to consider the uncertainty of the measurements. Table 3 enlists the parameters that are part of the database (minimum, nominal and maximum values) and the SD average measurement.

Table 3. Parameters employed for mathematic modeling.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Minimum</th>
<th>Nominal</th>
<th>Maximum</th>
<th>±SD</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inputs:</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Solar radiation *</td>
<td>(G)</td>
<td>100</td>
<td>987</td>
<td>1367</td>
<td>10.130</td>
</tr>
<tr>
<td>Temperature</td>
<td>(T_a)</td>
<td>9.56</td>
<td>28.73</td>
<td>39.53</td>
<td>5.1000</td>
</tr>
<tr>
<td>Wind velocity</td>
<td>(W_v)</td>
<td>0.30</td>
<td>4.20</td>
<td>9.80</td>
<td>0.0572</td>
</tr>
<tr>
<td>Wind direction</td>
<td>(W_d)</td>
<td>0</td>
<td>133</td>
<td>360</td>
<td>21.12</td>
</tr>
<tr>
<td>Relative humidity</td>
<td>(RH)</td>
<td>25</td>
<td>57</td>
<td>97</td>
<td>1.7288</td>
</tr>
<tr>
<td>Atmospheric pressure</td>
<td>(P_{at})</td>
<td>100</td>
<td>101.4</td>
<td>103.2</td>
<td>0.5370</td>
</tr>
<tr>
<td>PV output power **</td>
<td>(P_{PV})</td>
<td>17.07</td>
<td>326.2</td>
<td>356</td>
<td>0.4821</td>
</tr>
<tr>
<td>Output:</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>PV temperature modules</td>
<td>(T_{PV})</td>
<td>9.97</td>
<td>37.6</td>
<td>62.8</td>
<td>4.3000</td>
</tr>
</tbody>
</table>

* Represent the POA irradiation. ** \( P_{PV} \) is obtained by the product of \( V_{PV} \) and \( I_{PV} \).
The database was divided randomly into two parts by a systematic sampling to yield an unbiased representation of data set. The first one \((m\%)\) was designed for the training process and the second one \((n\%)\) was employed for testing and validation. Initial random division starts by assigning half of the database for both processes \((m = 50\% \text{ and } n = 50\%)\). To find the better ratio, \(m\%\) and \(n\%\) values were increased and decreased, respectively, in steps of 5%. For the current data base, it was found that optimum ratio was presented with \(m\%\) and \(n\%\) values of 85\% and 15\%, respectively.

**II) Generation of best approximation by ANFIS modeling:** An initial ANFIS structure is generated from the seven input variables enlisted in Table 3 to yield the optimum model for temperature prediction of the PV array. The inference system type is defined for the output model behavior, where a zero-order Sugeno model was employed in the modeling process due to the complex nature of PV temperature. Thereby, the evaluation of several combinations of membership functions in the zero-order Sugeno ANFIS structure generated was suggested as a suitable strategy to find the optimum modeling results. On the other hand, the membership function number corresponding to each input variable is chosen heuristically. However, due to the exponential dependency between the total number of rules and the number of input variables membership, the number of functions per input is limited to reduce computational lag.

**III) Computational methodology:** To validate the obtained results from ANFIS model, they were compared to the experimental data considering two important aspects: the statistical agreement and the computing performance. Statistical agreement was carried out by a comparison using the three different test parameters illustrated in Table 4, where \(T_{PV,Exp}\) is the module temperature, \(T_{PV,Sim}\) is the predicted temperature, \(T_{PV,Exp}\) is the average experimental temperature, \(T_{PV,Sim}\) is the average simulated temperature, and \(N\) indicates the data size. The root mean square error (RMSE) determines the accuracy of the model comparing the deviation of simulated and experimental values. The mean absolute error (MAE) indicates the average quantity of total absolute bias error between estimated and actual values. The coefficient of correlation \((R)\) determines the linear relationship of the predicted data with the measured data [46]. Knowledge of these criteria is relevant to evaluate whether the prediction is sub-estimated or over-estimated with respect to real data.

<table>
<thead>
<tr>
<th>Statistical Criteria</th>
<th>Function</th>
</tr>
</thead>
<tbody>
<tr>
<td>Root Mean Square Error</td>
<td>( RMSE = \sqrt{\frac{\sum_{i=1}^{N} (T_{PV,Exp} - T_{PV,Sim})^2}{N}} )</td>
</tr>
<tr>
<td>Mean Absolute Error</td>
<td>( MAE = \frac{\sum_{i=1}^{N}</td>
</tr>
<tr>
<td>Coefficient of Correlation</td>
<td>( R = \frac{\sum_{i=1}^{N} (T_{PV,Exp} - T_{PV,Sim})(T_{PV,Sim} - T_{PV,Exp})}{\sqrt{\sum_{i=1}^{N} (T_{PV,Exp} - T_{PV,Exp})^2} \sqrt{\sum_{i=1}^{N} (T_{PV,Sim} - T_{PV,Sim})^2}} )</td>
</tr>
</tbody>
</table>

On the other hand, the computing performance was evaluated considering the optimal epoch and computing time. Optimal epoch is the minimum number of iterations for minimizing the differences between experimental data and the simulated output. Computing time is the one to complete the number of epochs.

**IV) Sensitivity analysis:** A sensitivity analysis was performed to determine how the variation of input variables affects the output of ANFIS model. Sensitivity analysis is based on the idea of varying one uncertain parameter to know the response of the model [47]. The analyzed variable is evaluated in the ANFIS model at its maximum and minimum values and maintaining the other input variables in their nominal values. The difference of the output model between the maximum \((Q(P_{max}))\) and minimum \((Q(P_{min}))\) evaluated variable indicates the uncertainly sensitivity range \((S)\):

\[
S = Q(P_{max}) - Q(P_{min})
\]
A larger difference $S$ indicates a larger model sensitivity to the evaluated variable.

Figure 3. ANFIS methodology flowchart.

4. Results and Discussion

4.1. ANFIS Simulation Results

Training of the ANFIS model is accomplished through a series of epochs performing an optimization process to minimize the differences between experimental data and simulated output. The hybrid learning algorithm (which consists of a combination of the gradient descent method and least squares) was used for the developed model. $RMSE$ results, calculated with experimental data
and ANFIS predictions, were used as an optimization criterion for adequacy modeling. Furthermore, ANFIS architecture with two input membership functions was used (generating 128 number of rules) to avoid unnecessary computational load. MATLAB software with its Fuzzy Logic Toolbox [48] was employed to perform the training numerical computations.

Different input membership functions (trimf, trapmf, psigmf, pimf, gaussmf, gauss2mf, and gbellmf) were tested to determine the best ANFIS model. A preliminary training with 550 epochs was carried out to find the number of epochs with the minimum error for each membership function (Figure 4). As it can be appreciated, the best performance is obtained by the bell-shaped membership function (gbellmf).

![Figure 4. Evaluation of the seven input membership functions during 550 training epochs.](image)

Table 5 provides the results of computational and statistical criteria for estimation of $T_{PV}$ according to the minimum number of epochs for the membership functions tested. As it can be seen from Table 5, bell-shaped membership function presents the best statistical results (gbellmf, MAE = 0.06729, RMSE = 3.4553, and R = 95.56%), and a low computational time (45.122 s) with the second smallest number of epochs (115).

<table>
<thead>
<tr>
<th>Membership Function</th>
<th>Computational Parameter Criteria</th>
<th>Statistical Analysis</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Epochs</td>
<td>Time (s)</td>
</tr>
<tr>
<td>Trifm</td>
<td>001</td>
<td>0.65000</td>
</tr>
<tr>
<td>Trapmf</td>
<td>187</td>
<td>93.4484</td>
</tr>
<tr>
<td>Psigmf</td>
<td>550</td>
<td>386.149</td>
</tr>
<tr>
<td>Pimf</td>
<td>550</td>
<td>386.950</td>
</tr>
<tr>
<td>Gaussmf</td>
<td>437</td>
<td>84.2374</td>
</tr>
<tr>
<td>Gauss2mf</td>
<td>142</td>
<td>69.9605</td>
</tr>
<tr>
<td>Gbellmf</td>
<td>115</td>
<td>55.7117</td>
</tr>
</tbody>
</table>

A comparison between ANFIS model and a multivariate regression model was performed to demonstrate the accuracy of the developed model under the same type and number of input variables. Figure 5 illustrates the evaluation of experimental ($T_{PV,Exp}$) and simulated ($T_{PV,Sim}$) values for both AI and non-AI modes through a linear regression. The results indicate that the ANFIS model has a significant agreement with the experimental data, obtaining a coefficient $R = 0.95563$, given by:
A sensitivity analysis was performed to determine the influence of each input variable to $T_{PV}$.

Moreover, it aims the identification of the positive or negative importance level for the model for each variable. Figure 7 illustrates a tornado chart with the sensitivity analysis results according to the description of Section 3 (IV: Sensitivity analysis). The central value of the graph indicates the $T_{PV}$ at each variable. Figure 7 illustrates a tornado chart with the sensitivity analysis results according to the

\[ T_{PV, Sim} = 2.40622 + 0.9142 T_{PV, Exp} \]  \hspace{1cm} (10)
nominal values of input variables (Table 3). On the other hand, the extreme values of Figure 7 represent the $T_{PV}$ variation when evaluating the maximum and minimum values of each input variable. As can be seen, the highest result of the analysis was generated by the environmental temperature, indicating that it is the most influential variable. The second most influential variable according to the sensitivity analysis was the solar radiation, followed by wind velocity, and relative humidity. On the other hand, the wind direction, PV power output, and atmospheric pressure were the variables with less influence.

Even though the wind direction ($W_d$), PV power output ($P_{PV}$) and atmospheric pressure ($P_{atm}$) present a low contribution according to sensitivity analysis, these variables still improve the performance of ANFIS algorithm.

4.3. Evaluation of the ANFIS Model

A comparison between experimental and simulated curves of the PV temperature system was performed to validate the developed ANFIS model, employing data not included in the training and testing phases. The comparison criteria employed was the error percentage given by:

$$EP = 100 \times \frac{T_{PV,Sim} - T_{PV,Exp}}{T_{PV,Exp}}$$  \hspace{1cm} (11)$$

The results of the $EP$ evaluation describe an error with a normal distribution behavior, illustrated in the normalized histogram presented in Figure 8. Applying the equation for standard distribution ($Z$) to histogram results [49] it is possible to establish a correlation between the standard normal distribution and $EP$. Correlation results indicate that 94% of the $EP$ is in the error percentage range between $-5\%$ and $5\%$ (Figure 8), which is an acceptable error for this estimation process according to literature [17,19,42].

The results in Figure 8 indicate that the developed model can estimate the behavior in the temperature of the PV array for different atmospheric conditions. Therefore, the model generates a feasible estimation of the PV array temperature that can be used in monitoring processes and for maximum power control.
we can see that abrupt fluctuations in solar radiation significantly affect the accuracy of the estimated 
which is a favorable condition for the performance of the PV system. It can be observed that at low 
variables described by the sensitivity analysis. As can be observed, the estimation of the model presents 
errors related to abrupt changes in solar radiation. 
Figure 9 illustrates the validation of the ANFIS model for four different cases corresponding to 
each season of the year. For the validation process, we also included the two most influential variables 
according to the sensitivity analysis ($T_a$ and $G$). Case 1, displayed in Figure 9a, describes measurements 
performed during a clear day with good $G$ levels above 980 W/m$^2$. On the other hand, $T_{PV,Exp}$ curve 
illustrates high temperature values (above 55 °C between 12:00 and 15:00 hours), which are detrimental 
to the photovoltaic module performance. These high temperatures are due to the influence of the high 
levels of $G$ and the $T_a$ that reaches values between 35 °C and 40 °C, being the highest reported in the 
database. As can be seen in Figure 9a), the estimates of the ANFIS model are able to adapt adequately 
to the experimental data under clear conditions and gradual changes of $T_a$.

Case 2 (Figure 9b) considers measurements on a clear day, with a maximum reported radiation 
rate of 1020 W/m$^2$ between 11:00 and 12:40 hours. However, although solar radiation is higher 
than in Case 1, $T_a$ has a lower range (20 °C–35 °C), which is due to convective effects of the wind. 
As illustrated in Figure 9b, $T_{PV,Exp}$ reaches a temperature up to 50 °C between 12:00 and 14:40 hours. 
These temperatures are lower than those illustrated in Figure 9a, which validate the results of the sensitivity analysis where $T_a$ is more influential on $T_{PV,Exp}$ than $G$. On the other hand, the estimation of 
the ANFIS model presents good results to the gradual changes of $G$ and $T_a$.

Case 3 (Figure 9c) describes a day with high clouds between 12:40 and 14:40 hours. Even though 
solar radiation and environmental temperature conditions are not adequate, the $T_{PV,Exp}$ reaches 
values between 40 °C and 62 °C as a result of latency in temperature increase and influence of other 
variables described by the sensitivity analysis. As can be observed, the estimation of the model presents 
errors related to abrupt changes in solar radiation.

Finally, Case 4 (Figure 9d) illustrates the behavior of the PV system temperature for a completely 
cloudy winter day with radiation ($G$) lower than 300 W/m$^2$. In the same way, $T_a$ is below 25 °C, 
which is a favorable condition for the performance of the PV system. It can be observed that at low 
temperatures (unlike Figure 9b), $G$ has a greater influence on $T_{PV,Exp}$ than $T_a$. On the other hand, 
we can see that abrupt fluctuations in solar radiation significantly affect the accuracy of the estimated 
model generated by ANFIS.

Results in Figure 9 indicate that the developed model is able to estimate the behavior in the 
temperature of PV array for different atmospheric conditions in a time interval from 09:00 to 17:00 
hours. Therefore, the model generates good estimation of the PV modules temperature. The model 
can be used in the monitoring process and for its implementation in cooling systems to obtain the 
maximum performance of PV systems.
was developed. The generated ANFIS model included seven input parameters: solar radiation, environmental temperature, wind velocity, wind direction, relative humidity, atmospheric pressure, and photovoltaic output power. The model was trained with three year experimental database and validated using data not included in the training and testing phase, obtaining a correlation coefficient of 95%. Validation results indicate that the ANFIS model generates good temperature estimations for the photovoltaic array at different atmospheric and operational conditions. Additionally, sensitivity analysis results determine that environmental temperature, solar radiation, wind velocity, and relative humidity are the parameters with the strongest influence on the temperature of the array according to the model.

The methodology and artificial intelligence technique employed proved to be a suitable tool for the estimation of photovoltaic array temperature. The developed ANFIS model provides an alternative to the estimation of photovoltaic temperature based on information generated by meteorological stations. Its use in large-scale photovoltaic installations can generate temperature estimation in a large number of modules, contributing to the reduction of operation, installation and instrumentation costs. In addition, the results of this work contribute to the development of algorithms that improve the photovoltaic systems performance. The implementation of this method in intelligent sensors for photovoltaic cooling systems can be also enhanced. Finally, the results open the door to future works aimed at the study of nonlinear behaviors presented individually in the modules to making reliable estimations that consider adverse situations.

Figure 9. Comparison of experimental temperature PV array curve and simulated results from the ANFIS model. (a) Model evaluation in a clear day. (b) Model evaluation in the maximum irradiation day reported. (c) Model evaluation in a day with high clouds. (d) Model evaluation in a cloudy winter day.

5. Conclusions

This paper proposed a method to estimate the operation temperature of a photovoltaic array in a specific place considering its power output and atmospheric values. An estimation model for the temperature of a photovoltaic array employing an adaptive neuro fuzzy inference system (ANFIS) was developed. The generated ANFIS model included seven input parameters: solar radiation, environmental temperature, wind velocity, wind direction, relative humidity, atmospheric pressure, and photovoltaic output power. The model was trained with three year experimental database and validated using data not included in the training and testing phase, obtaining a correlation coefficient of 95%. Validation results indicate that the ANFIS model generates good temperature estimations for the photovoltaic array at different atmospheric and operational conditions. Additionally, sensitivity analysis results determine that environmental temperature, solar radiation, wind velocity, and relative humidity are the parameters with the strongest influence on the temperature of the array according to the model.

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References


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