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Abstract: Traditional sensor nodes are usually battery powered, and the limited battery power constrains the overall lifespan of the sensors. Recently, wireless power transmission technology has been applied in wireless sensor networks (WSNs) to transmit wireless power from the chargers to the sensor nodes and solve the limited battery power problem. The combination of wireless sensors and wireless chargers forms a new type of network called wireless rechargeable sensor networks (WRSNs). In this research, we focus on how to effectively deploy chargers to maximize the lifespan of a network. In WSNs, the sensor nodes near the sink consume more power than nodes far away from the sink because of frequent data forwarding. This important power unbalanced factor has not been considered, however, in previous charger deployment research. In this research, a power balance aware deployment (PBAD) method is proposed to address the power unbalance in WRSNs and to design the charger deployment with maximum charging efficiency. The proposed deployment method is effectively aware of the existence of the sink node that would cause unbalanced power consumption in WRSNs. The simulation results show that the proposed PBAD algorithm performs better than other deployment methods, and fewer chargers are deployed as a result.

Keywords: wireless rechargeable sensor networks; minimum dominating set; charging power

1. Introduction

In the past, due to the limitations of battery power, the lifetimes of sensors used in wireless sensor networks heavily depended on the energy provided by the batteries, which made the stability of the whole network greatly uncertain. Various scholars have put forward a range of studies in attempts to solve the problem of limited battery power, including the use of effective routing protocols [1], efforts to ensure efficient energy consumption [2], and so on. However, the above research did not succeed in solving the problem in a fundamental way. Although the advances they proposed can effectively extend the lifespan of the network, the network will still become unusable in the end when the sensors run out of battery power. In addition, if the sensors in a network rely on solar power provided by the sun, the sensors and the overall efficiency of the network will be affected by various environmental factors. In fact, a number of factors can make a sensor unable to operate effectively for extended periods of time. In order to overcome the power constraints of sensing devices, various discussions relating to the concept of wireless power transmission have been started in recent years [3], and the related studies have provided some solutions to the limited lifetimes of wireless sensor networks. Through chargers, electric power is transmitted to radio-frequency identification (RFID) tags [4], sensing devices [5], and terminal equipment. Due to the convenience and rapid development of wireless charging technology, it has attracted the attentions of both academic scholars and industrial professionals. According to
the annual growth rate of the global wireless charging market will be more than 33% in 2020—this shows that this field has great potential.

How to improve the survival time of wireless sensor networks using wireless power transmission technology is thus a topic that is currently widely discussed and studied [6,7]. These new types of networks, which enable the use of wireless charging to prolong the lifespan of the network sensors, are called wireless rechargeable sensor networks (WRSNs). In order to make the sensors within the sensing region maintain stable power, the deployment of the wireless chargers becomes the primary consideration. Due to cost considerations, the number of chargers in the region should be minimized to the greatest extent possible. On the other hand, the amount of power supplied to a sensor has an important influence on the performance of the sensor. Therefore, effectively minimizing the number of wireless chargers used in the deployment while also maximizing the charging ability of the wireless chargers is the goal of this research.

Although many studies relating to the deployment of wireless chargers have been published in recent years, these studies did not take into account some important factors. For example, previous research has solved the sensor coverage problem without calculating charging power and without considering the existence of the sink node. To overcome these limitations, this study aims to investigate how to set up X directional chargers in a given area. Previous studies assume a uniform power consumption of the sensor nodes, but this is not the case in a realistic setting. The data sink node collects sensing data from all the sensor nodes, and sensor nodes nearby the sink need to facilitate more data forwarding than sensor nodes far away from the sink, so the power consumption of the nodes close to the sink is larger and the area near the sink is called the hot zone [8]. The sensor nodes in the hot zone run out of battery power more quickly than sensor nodes outside the hot zone. When the sensor nodes in the hot zone run out of battery power, the sensor network fails to work properly and this phenomenon is the famous “energy hole problem” [9]. No matter in wireless sensor networks (WSNs) or WRSNs, multi-hop transmission is employed to forward data back to the sink node and the appearance of the energy hole will interrupt the communications. Figure 1 shows the concept of the multi-hop transmission and demonstrates how the sensor nodes in the hot zone take the responsibility of forwarding the data to the sink node.

![Figure 1. The power unbalanced phenomenon of wireless sensor networks (WSNs).](image)

Wireless charger deployment problems have attracted substantial attention in recent years. We review a number of the relevant previous studies. He et al. [10] focused on the omnidirectional wireless charger deployment problem and deployed charging devices in the sensing area of interest to provide enough charging power to maintain the operation of the network, but they explored the space with a more traditional triangle solution. Chiu et al. [11] divided the sensing areas into grids
and placed omnidirectional wireless chargers on various grid points. Their deployment also took into consideration the moving paths of mobile sensors. In a study by Liao [12], the coverage area of the chargers was conical, and the sleep schedule of the chargers was considered in order to reduce the power consumption. Compared with the aforementioned studies of omnidirectional wireless chargers, studies by Horster and Lienhart [13,14] considered the deployment of the directional chargers and defined the charging area of a directional charger as a sector with a given angle. In the Horster and Lienhart study [13], triangles were used to represent the charging area of directional chargers, so an integer linear programming solution was proposed in which each grid point represents a possible location of the deployment. The Han et al. study [14], meanwhile, minimized the number of deployed chargers while also considering the connections among chargers. The reviewed literature is organized in Table 1 below. Interestingly, these studies did not consider the unbalanced power consumption effect caused by forwarding data to the sink node. Such unbalanced power consumption can make the sensor nodes near the sink rapidly lose power.

Table 1. Literature comparisons.

<table>
<thead>
<tr>
<th>Name</th>
<th>Type</th>
<th>Contribution</th>
<th>Power Balance Aware</th>
</tr>
</thead>
<tbody>
<tr>
<td>Energy provisioning in wireless rechargeable sensor networks. [10]</td>
<td>Omnidirectional charger</td>
<td>Physical characteristics of wireless charging</td>
<td>No</td>
</tr>
<tr>
<td>Optimized charger deployment for wireless rechargeable sensor networks. [12]</td>
<td>Omnidirectional charger</td>
<td>Charger sleep scheduling</td>
<td>No</td>
</tr>
<tr>
<td>Minimizing charging delay in wireless rechargeable sensor networks. [15]</td>
<td>Omnidirectional charger</td>
<td>Robot stop locations in discrete areas</td>
<td>No</td>
</tr>
<tr>
<td>Approximating optimal visual sensor placement. [13]</td>
<td>Directional charger</td>
<td>Grid linear programming</td>
<td>No</td>
</tr>
<tr>
<td>Deploying directional sensor networks with guaranteed connectivity and coverage. [14]</td>
<td>Directional charger</td>
<td>Considers the fact that the sensors are connected to each other</td>
<td>No</td>
</tr>
</tbody>
</table>

2. Experimental Section

2.1. Problem Statement

First, we define the basic assumptions of the WRSN model. This is then followed by an introduction of the charger coverage Equation and the charging power Equation. The definition of charging demand and the effects of the data sink node are also given.

2.1.1. The WRSN Model

Given a two-dimensional region Z, assume that this space has X rechargeable sensors and make them a collection of \( S = \{s_1, s_2, \ldots, s_X\} \). The data sink node, which is labeled as Y, exists in Z. The locations of the sensors and data sink node are known. The objective is to deploy M directional chargers. Define M directional chargers as \( A = \{a_1, a_2, \ldots, a_M\} \). Each charger can be deployed anywhere in the region, and a given directional charger can be placed at any angle. Assume that the chargers must cover a subset of the sensors \( S \), regardless of the fact that all the chargers have the same charging efficiency. Past studies have failed to consider the existence of the data sink node and this defect can have significant impacts on the wireless charger deployment. In Section 2.1.3, we will explain the difference between charging efficiency and charging demand. According to the study by Garey and Johnson [16], the deployment of the chargers is a nonlinear programming problem, so it belongs to the category of non-deterministic polynomial-time hard (NP hard) problems and thus it is challenging to solve the charger deployment problem.
2.1.2. Coverage Area and Charging Power Model

In this section, we will illustrate the different types of chargers and why we have selected the directional chargers for deployment.

A. Omnidirectional Chargers

According to previous studies by He et al. and Chiu et al. [7,8], in the past, the coverage area of the omnidirectional charging model assumed the same charging ability and the equal charging distances. In fact, however, the received power attenuates when the distance increases and eventually the received power will be decreased to zero when a critical distance is reached. The charging coverage area of an omnidirectional charger is assumed to be a disk and the charger is assumed to be at the center of the charging area.

B. Directional Chargers

According to previous studies by Liao [12,13], the coverage area of the charging model is a sector, and products from different companies have charging angles with different ranges. Due to their relatively stable power coverage and low cost, directional chargers are often used in wireless rechargeable sensor networks.

Figure 2 is a schematic diagram of the coverage area of a directional charger. As shown in Figure 2, the directional charger $a_i$ with angle $\theta$ charges the sensor $s_j$, and the radius is $r$. The arrow is directed out from the face of the charger. $\vec{v}$ is a unit vector of the charger face, and $\vec{u}$ is the vector formed by the charger and the sensor. According to Ai and Abouzeid [15], the following Equation can be used to determine whether the sensor $s_j$ is in the coverage area.

$$
D(a_i, \vec{v}, s_j) = \begin{cases} 
1, & \text{if } \vec{v} \cdot \vec{u} - ||\vec{u}||_2\cos(\frac{\theta}{2}) \geq 0 \\
0, & \text{if } \vec{v} \cdot \vec{u} - ||\vec{u}||_2\cos(\frac{\theta}{2}) < 0
\end{cases} 
$$

(1)

Figure 2. Coverage area of a directional charger.

Equation (1) determines whether the sensors are in the coverage area, and when the value is 1, the charger’s charging power is calculated according to Equation (2).

$$
E(\text{dist}(a_i, s_j)) = \begin{cases} 
\frac{a}{(\text{dist}(a_i, s_j) + \beta)^2}, & \text{dist}(a_i, s_j) \leq r \\
0, & \text{dist}(a_i, s_j) > r
\end{cases} 
$$

(2)

In Equation (2), we define $\text{dist}(a_i, s_j)$ as the Euclidean distance between the location of charger $a_i$ and the location of sensor $s_j$, and $a = \frac{\delta W_0 G_0 G_s}{\zeta t_\lambda}$ where $\lambda$ is the wavelength, and $\zeta$ is the efficiency of the rectifier. $G_0$ and $G_s$ are the antenna gain of the charger and the sensor, respectively. $W_0$ is the charging power, $C_{\alpha}$ is the antenna polarization loss, and $\beta$ is the compensation parameter for short range transmission [17]. When the distance is larger than the charging radius $r$, the charging power
is 0. According to Dai et al. [18], although the total power may not be precise, the total power can still be expressed as a function of the following Equation (3).

\[
W(j) = \sum_{i \in M} D(a_i, \vec{v}, s_j) E(dist(a_i, s_j))
\] (3)

2.1.3. Charging Efficiency and Charging Demand

The data sink node is an important piece of equipment in wireless sensor networks. Sensors within the sensing area can collect data and send data back to the data sink node by multi-hops. If a sensor is close to the data sink node, then it will facilitate other sensors to forward data to the sink frequently, thus incurring more power consumption. The charging efficiency defines the charging ability of a charger, and different manufacturers have different charging efficiencies. The charging efficiency can be defined as the following Equation (4):

\[
P(W(j)) = \begin{cases} 
\sigma \cdot W(j), & W(j) \leq W_{\text{max}} \\
\sigma \cdot W_{\text{max}}, & W(j) > W_{\text{max}} 
\end{cases}
\] (4)

\[H(dist(a_i, Y)) = \begin{cases} 
\gamma + \mu, & \text{dist}(a_i, Y) < f \\
\gamma, & \text{dist}(a_i, Y) = f \\
\gamma - \mu, & \text{dist}(a_i, Y) > f
\end{cases}
\] (5)

Due to the charging power being a continuous value, deployed positions will have infinite points. Without discretization, a large amount of computation time is unavoidable. In order to design an efficient algorithm, we will further elaborate the discretization in the fourth chapter. Table 2 briefly explains all the symbols used in this study.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Corresponding Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z</td>
<td>Selected 2D region</td>
</tr>
<tr>
<td>x</td>
<td>Number of sensors</td>
</tr>
<tr>
<td>s_j</td>
<td>The sensor j</td>
</tr>
<tr>
<td>m</td>
<td>The number of chargers</td>
</tr>
<tr>
<td>a_i</td>
<td>The charger i</td>
</tr>
<tr>
<td>Y</td>
<td>The data sink node</td>
</tr>
<tr>
<td>\theta</td>
<td>Charging angle</td>
</tr>
<tr>
<td>r</td>
<td>Charger radius</td>
</tr>
<tr>
<td>\vec{v}</td>
<td>Direction vector of a charger</td>
</tr>
<tr>
<td>\vec{u}</td>
<td>The vector of the charger and sensor</td>
</tr>
<tr>
<td>\sigma</td>
<td>The factor affecting charging effect</td>
</tr>
<tr>
<td>W_{\text{max}}</td>
<td>Upper bound value of charging power</td>
</tr>
<tr>
<td>\gamma</td>
<td>The average charging demand</td>
</tr>
<tr>
<td>\mu</td>
<td>The charging demand adjustment coefficient</td>
</tr>
<tr>
<td>f</td>
<td>The specific distance which influences the charging demand</td>
</tr>
</tbody>
</table>
2.2. Method

This paper deploys directional chargers to cover the sensors in the sensing region. Moreover, a greedy algorithm is adopted to calculate the coverage and consideration of the influence of the data sink node is the premise utilized to obtain full coverage and to maximize the charging power. The proposed method called power balance aware deployment (PBAD) can be divided into two steps. First, the selected area is divided into a number of sub-regions, so that each sub-region can have a constant degree of charging power and charging demand. Then each sub-region is further analyzed to discover the minimum dominating sets (MDSs), and then the charging power is taken into consideration to select the optimal dominating set.

2.2.1. Area Discretization of Charging Power and Charging Demand

In a real environment, the chargers can be deployed in an infinite number of positions and give the sensors different charging effects. In order to be able to effectively deal with the problem, Fu et al. [15] suggested that the selected area should be discretized into finite sub-regions, so that the number of candidate points can be limited to a finite number of points. Due to different charging powers for sensors in different ranges, as shown in Figure 3, the charger can generate a certain charging power to sensors in each area. The charging power in the interval \([S(X-1), (X)]\) is approximated to \(W(S(X))\).

![Figure 3. Schematic diagram of the discretization of charging power.](image)

Figure 4 shows that the whole area is divided by eight homocentric circles into 15 sub-regions (including the area where the power is 0). The sensors placed in the same area will receive the same charging power.

![Figure 4. Schematic diagram of regional discretization.](image)
As illustrated in Section 3, due to the existence of a data sink node in the real environment, each sensing power charging demand will vary. Because of the multi-hop characteristics in data transmission, sensors close to the data sink node will be used more frequently. In order to be able to find the minimum dominating set needed to meet this requirement, the sensing area must first be discretized, and the sensors are clustered according to the distances to the data sink node, as shown in Figure 5 below. The blue points represent the sensors. Two parameters, $\gamma$ and $\mu$, are used to cluster the sensors into three groups. The parameter $\gamma$ is the threshold of the average charging demand and the parameter $\mu$ is the adjustment coefficient. According to different charging demands, the charger deployment locations are calculated.

![Figure 5. The distribution of the charging demands of the sensors.](image)

### 2.2.2. Searching for Minimal Dominating Set

In the previous section, the discretization of the region is elaborated and the next step is to discover the minimal dominating set from all the dominating sets. Therefore, this section mainly discusses the minimal dominating set. Two definitions are given first.

**Definition 1.** Given two sets of sensors under coverage, $S_i$ and $S_j$, if $S_i \subseteq S_j$, then $S_j$ dominates $S_i$.

**Definition 2.** If there is no other set dominating $S_j$ in the region, then $S_j$ will be determined to be the optimal dominating set in the region.

In order to find the optimal dominating set, we first assume that a charger is placed on a fixed point in the region. It is then rotated through different directions in order to determine all the coverage dominating sets, after which the best dominating set is selected. The minimal dominating set in the region is the optimal dominating set of the directional chargers. There is no need to calculate all of the coverage sets, because the target area has already been separated, so the charging powers in the same area are the same.

The above Algorithm 1 can be regarded as one kind of greedy algorithm. The coverage dominating sets are obtained through continuous rotations of the directional chargers, and then the optimal dominating set is selected from the calculated coverage dominating sets, as such, the region can be covered with the least amount of chargers. Steps 1 to 3 initialize the angles and Steps 4 to 7 rotate the angles and discover the angle that can cover the maximum number of sensors and label the sensors as a coverage dominating set. Step 8 removes the sensor with the smallest angle until the current set can be covered again. Figure 6 shows an example of finding the coverage dominating sets through rotations. The algorithm starts from the first coverage dominating set $\{s_2, s_3\}$ and then discovers three more dominating sets, $\{s_3, s_4\}$, $\{s_4, s_5, s_6\}$, and $\{s_5, s_6, s_7, s_8\}$. 

\[
\text{Input: } \theta_j \text{; } \text{Add } s_j \text{ to } S_t \text{; } j = (j + 1) \mod X \text{; } \\
\text{Step 6. Add the current } S_t \text{ to the cover dominating sets } CDSs; \\
\text{Output: } \text{optimal dominating set.}
\]
Algorithm 1: Calculate the Coverage Dominating Sets of Given Sensors

Input: Directional charger $a_i$, angle $\theta$ and the sensor set $S_i$ with the locations of all the sensors
Output: Coverage Dominating Sets CDSs

Step 1. Calculate the included angle between the sensor and the charger;
Step 2. Sort sensors using angles, from small to large, $\theta_1 \leq \theta_2 \leq \ldots \leq \theta_X$ with respect to sensors $s_1$, $s_2$, $\ldots$, $s_X$;
Step 3. Set a parameter $S_t$ to record the current coverage set. Two parameters, $\theta_{\text{min}}$ and $\theta_{\text{max}}$, record the minimum and maximum of the current coverage set. Initialize $\theta_{\text{min}} = \theta_1$, $\theta_{\text{max}} = \theta_1$; $S_t = \{s_1\}$;
Step 4. Starting from second sensors, $j = 2$;
Step 5. Rotate the chargers until no more sensors can be covered.
While ($\theta_j - \theta_{\text{min}} \leq \theta$){
  $\theta_{\text{max}} = \theta_j$;
  Add $s_j$ to $S_t$;
  $j = (j + 1) \mod X$;
}
Step 6. Add the current $S_t$ to the cover dominating sets CDSs;
Step 7. Let $\theta_{\text{max}} = \theta_j$ and add $s_j$ to $S_t$;
Step 8. Remove the sensor from the smallest angle until the current set can be covered again
While($\theta_{\text{max}} - \theta_{\text{min}} > \theta$){
  From the $S_t$ to remove the minimum angle sensor, and $\theta_{\text{min}}$ update into the current minimum angle value;
  If($\theta_{\text{min}} = \theta_1$){
    End;
  }
}
Go to Step 5.

Figure 6. A coverage dominating set finding example.
After discovering all the coverage dominating sets CDSs, the total power $P$, charging efficiency $W$ and charging demand $H$ are then calculated. The coverage dominating set with minimum $H-W$ is selected as the best dominating set. The following algorithm II illustrates the procedures of finding the best dominating set. Figure 7 shows a best dominating set example obtained using the power balance aware deployment (PBAD) algorithm.

![Figure 7. A best dominating set example.](image_url)

**Algorithm 2: Search for the Best Dominating Set**

| Input: Coverage Dominating Sets CDSs |
| Output: The Best Dominating Set BDS |
| Step 1: Calculate the total power $P$ and the charging efficiency $W$ of all Coverage Dominating Sets CDSs using Equations (3) and (4) |
| Step 2: Calculate the charging demand $H$ of all Coverage Dominating Sets CDSs using Equation (5) |
| Step 3: Select the best dominating set $BDS$ with minimum $H-W$ |

### 3. Results

In this section, the simulations are conducted to verify the performance of the proposed approach. We compare the proposed power balance aware deployment (PBAD) algorithm with the location merging design (LMD) proposed by Fu et al. [15] and random deployment.

#### 3.1. Description of Parameter Setting and Comparisons

We use the following parameters to set up the experiment: sensors are placed in a two-dimensional space measuring 100 m × 100 m. The number of sensors is 20 ($X = 20$), and the charging power model parameters of the chargers are $\alpha_1 = 80$, $\beta_1 = 40$, $d_1 = 16$, and $\theta_1 = 90$. The upper bound value of the average charge demand $f_{up} = 30$ m and $f_{low} = 10$ m. $W_{max} = 40$ mW, $\sigma = 1$, $\mu = 4$ mW, and $\gamma = 28$ mW.

The proposed PBAD method is compared with the random position and random orientation (RPRO) approach and the aforementioned LMD. The following data are the values resulting from the respective implementations of our method, the RPRO, and the LMD for 300 simulations. Because LMD uses omnidirectional chargers for the deployment, it also uses different parameters. Specifically, those parameters are $\alpha_2 = 70$, $\beta_2 = 50$, $d_2 = 10$, and $\theta_2 = 360$. 

We demonstrate the results using different numbers of chargers, the proposed PBAD method is compared with the random position and random orientation (RPRO) approach and the aforementioned LMD. For such a location merging design (LMD) proposed by Fu et al. [15] and random deployment.

The upper bound value of the average charge demand $f_{up} = 30$ m and $f_{low} = 10$ m. $W_{max} = 40$ mW, $\sigma = 1$, $\mu = 4$ mW, and $\gamma = 28$ mW.
3.2. Experimental Results

We demonstrate the results using different numbers of chargers, different numbers of sensors, and different charging demands to show that the proposed PBAD algorithm achieves better coverage and has better charging power. The performance of the charging efficiency of each sensor is also given.

Satisfying all the charging demand for the deployment of the chargers is our main purpose. As can be seen from Figure 8 above, our method uses eight chargers to achieve this purpose. Compared with the RPRO and LMD approaches, the deployment generated by our approach is better. While the LMD approach only takes the power of charging into consideration, it does not consider the existence of the data sink node. Also, the charging power of an omnidirectional charger is poor, so the effect is poor. Without a doubt, the RPRO is the worst among the three algorithms.

![Figure 8](image)

**Figure 8.** (a) The deployment of PBAD (power balance aware deployment) approach; (b) The deployment of the RPRO (random position and random orientation) approach; (c) The deployment of the LMD (location merging design) approach.

4. Discussion

4.1. Effects of the Sensor Quantify on Charger Quantity

As can be seen from Figure 9, regardless of the number of sensors, the proposed PBAD method outperforms the other two algorithms and utilizes fewer amounts of chargers. It can be found that there is a slightly drop of the RPRO method at the number of 30 sensors, and this is due to the random nature of RPRO approach.

![Figure 9](image)

**Figure 9.** Comparison of charger quantity.

4.2. Effects of the Adjustment Coefficient of Charging Demand $\mu$

This section studies the impact of the charging demand adjustment coefficient on the number of chargers required. We use the results indicated in Section 3.2 as a precondition for the experiment and
assume that $\mu$ changes within the range of 2 and 10 mW. Figure 10 shows that the LMD algorithm is not affected by $\mu$. This is because the LMD approach does not take the data sink node into account in its deployment. The LMD deployment is meant to maximize the charging power without considering the power balance, so the required number of chargers is always 13. Our deployment method deploys fewer chargers when $\mu$ increases, and there is a negative correlation between the number of chargers and $\mu$. This is because the sensor charging demand becomes low. Nevertheless, our method requires less chargers than the LMD method for deployment.

![Figure 10. Effects of the charging demand adjustment coefficient $\mu$.](image)

### 4.3. Effects of the Charging Angle $\theta$

The effects of the charging angle $\theta$ on the number of required chargers are explored in this section. The charging angle $\theta$ is changed from 40 to 360 degrees. Since LMD can only be applied to the omnidirectional chargers, PBAD is compared with RPRO only in this section. Figure 11 shows that the number of required chargers and the charging angle $\theta$ are positive correlated. When the charging angle $\theta$ is set to 360 degrees, the deployment results of PBAD can be compared with the results of LMD in Section 3.2. The PBAD deploys 13 chargers less than LMD.

![Figure 11. Effects of the angle $\theta$.](image)

### 4.4. Charging Efficiency Performance in the Real Case of Each Sensor

In this section, numbers are assigned to the sensors. The closer a sensor is to the data sink node, the smaller the number that is assigned to it. In Figure 12, the effect of the charging efficiency of each sensor in the different algorithms is shown. We limit the number of deployed chargers to 10. The efficiency
of the RPRO charging method is very unbalanced; this is because the deployment method randomly picked the interested points. The strategy used by the LMD approach is to find the best charging efficiency for the sensors. In contrast, our method considered the charging demand instead of charging efficiency. The aim of our approach is to maintain the operation of the sensors instead of going after the best charging efficiency. In a realistic environment, our approach can effectively reduce the number of required chargers.

![Figure 12. (a) Optimal solution; (b) PABD method; (c) LMD method; (d) RPRO method.](image)

### 5. Conclusions

In this study, the influence of the data sink node on sensors is considered. Many studies have failed to pay attention to this important factor. This paper takes into account the effect of the data sink node and proposes a power balance aware deployment (PBAD) approach that can reduce the number of the required chargers and still maintain good charging effects. This study considers directional chargers which has been rarely considered among previous studies. The deployment given by the proposed PBAD method can reduce the required number of directional chargers and maintain the charging efficiency. The simulation results show that our approach outperforms the LMD and RPRO approaches by a significant degree and thus further demonstrate the usability of our algorithm.

In a realistic charger deployment, there are still many additional factors that need to be considered, such as charger recharging. It is expected that in the future, more factors can be considered to further optimize the algorithm, so that the charging power can be further improved.

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**Author Contributions:** Tu-Liang Lin and Sheng-Lin Li developed the concept and designed the experiments together. The experiments were conducted by Sheng-Lin Li. Tu-Liang Lin wrote the draft and Hong-Yi Chang revised the paper.

**Conflicts of Interest:** The authors declare no conflict of interest.

**References**