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Abstract: The clearances in the slide guide system of a hydraulic press are one of the significant factors affecting its accuracy. These clearances also affect the energy consumption of the press. An energy loss model that considers the oil leaks and friction associated with these clearances was proposed, and the size of clearances was optimized based on the model. The maximum allowable eccentric load and the energy loss on the wedge clearance condition were calculated to ensure the slide and guide pillars function properly. The stiffness of pillars and wear of guide rails were checked under an eccentric load condition. A case for rapid sheet metal forming with a 20 MN hydraulic press was examined. For this case, the optimum fit clearances were found to be approximately 0.4 mm. The energy loss under an eccentric load condition was increased by approximately 83% compared to a non-eccentric load condition. The pillars were optimized by reducing excessive stiffness, which served to decrease the pillar weight by nearly 20%.

Keywords: hydraulic press; energy loss; design optimization; eccentric loads; stiffness

1. Introduction

It is often said that manufacturing is the engine for economic development; in many countries, manufacturing also represents the largest energy end-use. In 2010, China’s manufacturing sector accounted for about 60% of the total energy consumption [1]. A large portion of the energy consumption in this sector is associated with production processes, which is attributable to production equipment. Hydraulic presses are a mainstay in metal forming processes, owing to their ability to deliver high forming pressures; however, they are also large energy consumers [2,3]. In 2013, China produced about 2 million metal forming presses. If the average power demand of one of these presses is 40 kWh, more than 280 billion kWh will be consumed per year, which is comparable to the total energy consumed by Spain in 2014 [4]. Over the past several decades, much research has been performed on the efficiency and energy consumption of hydraulic presses [5,6]. This has shown that the slide, as the principal element of the press system, consumes most of the energy in the forming process. The slide guide system has a tremendous effect on the kinematic behavior of the slide and the associated forming accuracy, and affects the oil leakage from clearances associated with the working cylinder, wear of the guide rails [7], and life of the forming dies.

The slide guide system of a hydraulic press is composed of a slide and four guide pillars. The orientation of the slide, and its function, depends on the fit between the guide rails on pillars and the adjustable guide plates on the slide. The clearances are the gaps between the flat surfaces of the guide rails and the adjustable guide plates, as shown in Figure 1. An oil film exists within the clearances that separate the surfaces of rails on pillars and the adjustment plates on the slide. This film is used to
avoid metal-on-metal rubbing. As the lubricating oil film migrates or leaks from the clearance gaps, a reservoir replaces the lost fluid. A small clearance means less leakage, but it also means larger friction. A large gap serves to reduce the friction but may compromise forming accuracy and produce more oil losses. It is evident the total energy is dependent on the sizes of the clearances, and that it is important to consider the fit of adjustable guide plates on the slide and the guide rails on pillars from an overall systems perspective.

Figure 1. A hydraulic press. The inset shows the clearance between the slide and one of the pillars.

When a hydraulic press is used to deform a workpiece, the asymmetric geometry of the workpiece, positioning errors, and uneven heating of dies may lead to an asymmetric resistance force that acts on the slide. This eccentric load produces a complex stress state [8]. Much research has been performed to analyze and solve this problem. Osakada et al. indicated that crank presses with two connecting rods could increase the power and maintain parallelism of the slide under an off-center load [9]. Wagener et al. focused on determining the angular deflection, lateral offset, and angular spring constant of the die guidance system under central and eccentric loading. They reported that heel blocks with brass plates produce optimal improvement with regard to die and slide tilting and lateral offset, and a combination of heel block guides and pillar guides produces only a small increase in angular stiffness [10]. Peipei and Haibin put forward the concept and operating principle for a moment leveling and position control system to find the required correcting moment [11]. Jimma, Sekine, and Tozawa proposed an analytical method to select a suitable press for a given die set and eccentric load [12].

As expected, the stiffness of the principal elements in a hydraulic press plays an important role in realizing forming accuracy. Finite element simulation has been widely used in the design, analysis, and optimization of presses (Chval et al. [13], Socrate et al. [14], and Zhao et al. [15]). Such efforts have been employed to predict the maximum safe stress beyond which defects and wear will occur, the optimal cross-sectional area of structural elements, etc. However, the stress distributions from simulations do not always compare well with the results of experiments. Other methods have been used to analyze the stiffness of presses. For example, Arentoft et al. proposed a new procedure for measuring press stiffness, including separated horizontal and vertical loading of the press frame. The load can be eccentrically positioned for measuring rotational stiffness [16].

The impact of eccentric loads and the stiffness of components has been investigated with respect to the forming accuracy of hydraulic presses. However, it is still unknown how the clearances and guide geometry of the system affect the stiffness and accuracy of a hydraulic press. No research literature was found that discusses how the clearances and guide geometry affect the press energy consumption. Almost always, the clearances and guide length are determined based on experience [17,18]. This paper aims to optimize the clearances and guide length for a slide guide system; it is envisioned that
this solution will provide an excellent reference for the design of clearances and the adjustment of hydraulic presses.

The contents of this paper consist of four sections. The energy loss caused by the lubricating oil leakage and friction between the slide and guides (separated by clearances) under the conditions of centered and eccentric loading is analyzed in Section 2. Then, the maximum allowable lateral force is studied, and the stiffness of the pillars and wear of guide rails are examined under an eccentric load condition in Section 3. A case study is presented in Section 4. Finally, the paper presents a summary and conclusions.

2. Energy Loss Analysis in the Slide Guide System

During a metal forming process, the slide moves up and down, with its position constrained by the guides affixed to the pillars. lubrication in the slide guide system is provided by an oil film that fills the clearance gaps between the guide rails and the adjustable guide plates. The lubricating oil in the clearance gaps ensures that relative motion between the slide and pillars occurs without metal on metal contact. A consequence of the relative motion of the slide and the clearance gaps is that the lubricating oil will leak from the system (oil is made up from a reservoir). Frictional power losses are associated with the interfaces between the slide and the guide rails. Since lost oil in the system must be replaced, this will also consume power [19].

2.1. Energy Loss Model

Assuming that the guide surfaces are parallel to the plane of adjustable guide plates under central loading as shown in Figure 2, the amount of oil leakage $q$ for a single clearance gap can be described with Equation (1) [20]:

$$ q = \frac{b \delta \Delta p}{12 \mu L} - \frac{b \delta v}{2} $$

where $\delta$ is size of the clearance, $\Delta p$ is the differential oil pressure between the two ends of clearance (produced by oil leakage), $L$ is the length of adjustable oil pressure, $b$ is the width, $\mu$ is the dynamic viscosity of hydraulic oil, and $v$ is the velocity of slide.

Figure 2. The wedge oil-film clearances in hydraulic press between slide and pillars under eccentric loads.
Then, the leaking power loss $P_q$ is given by Equation (2):

$$P_q = \Delta pq = \Delta pb \left( \frac{\delta^3 \Delta p}{12 \mu L} - \frac{\delta v}{2} \right)$$

(2)

At the location of $z = \delta$, the friction force in the parallel clearances is:

$$F_f = \tau A = \mu \frac{du}{dz} A = bL \left( \frac{\Delta p \delta}{2L} + \frac{\mu v}{\delta} \right)$$

(3)

where $\tau$ is the shear stress of the oil at the moving surface. $A$ is the contact area which is equal to the area of adjustable guide plate. The energy loss per unit time caused by friction, namely the friction power loss $P_f$, is given by Equation (4):

$$P_f = F_f v = vbL \left( \frac{\Delta p \delta}{2L} + \frac{\mu v}{\delta} \right)$$

(4)

The total power loss is given by:

$$P_T = P_q + P_f = b \left( \frac{\Delta p^2 \delta^3}{12 \mu L} + \frac{\mu L v^2}{\delta} \right)$$

(5)

From the equations above, it is evident that the power loss due to oil leakage increases with increasing $\delta$, but the power loss due to friction decreases with increasing $\delta$. Therefore, there must be an optimum clearance $\delta$ that minimizes the total power loss. This is given as follows:

$$\frac{dP}{d\delta} = 0 \Rightarrow \delta = \sqrt{\frac{2\mu L v}{\Delta p}}$$

(6)

Since the relative velocity $v$, between the slide and guide pillars changes during the forming process, the energy loss for a working cycle (slide moving down to execute the process and then returning to the starting position) of time $T$ is given by Equation (7):

$$E = \int_0^T 16P_T dt = \frac{4}{3} \frac{b \Delta p^2 \delta^3 T}{\mu L} + \frac{16bL}{\delta} \int_0^t v(t)^2 dt$$

(7)

2.2. Energy Loss Considering Eccentric Load

The parallel oil-film clearances turn into wedge oil-film clearances in the slide guide systems under an eccentric load, as shown in Figure 2, in which the pillar moves with velocity $v$ and the slide is regarded as stationary. The amount of oil leakage in the wedge clearance may be expressed using Equation (8) [20]:

$$q^\prime = \frac{b \delta_1 \delta_2}{\delta_1 + \delta_2} \left( \frac{\delta_1 \delta_2}{6\mu L} \Delta p + v \right)$$

(8)

Since the tilt angle $\alpha$ caused by an eccentric load is very small, the following approximations may be made using the coordinate system of Figure 2: $tan \alpha = a, cosa \approx 1, ax = \delta_2, (a + l - L)a = \delta_2’; (l + a)x = \delta_1, (l + a)x = \delta_1’$; and $xa = \delta$. Based on these approximations, the leakage in up and down wedge clearance could be given by Equation (9):

$$q^\prime = \frac{ba \left( L + a \right) a}{(L + 2a)} \left( \frac{a \left( L + a \right) a^2}{6\mu L} \Delta p + v \right) + \frac{b \left( l - L + a \right) \left( l + a \right) a}{(2l + 2a - L)} \left( \frac{\left( l - L + a \right) \left( l + a \right) a^2}{6\mu L} \Delta p + v \right)$$

(9)
Then, the power loss due to leakage for the wedge clearances is given by Equation (10):

$$ P_q' = \Delta p \frac{b(L_a+L+x)}{(L+2a)} \left( \frac{(L_a+L+x)^2}{6L} \Delta p + v \right) + \Delta p \frac{b(l-L_a)(L+x)}{(2L+2a-L)} \left( \frac{(l-L_a)(L+x)^2}{6L} \Delta p + v \right) $$

(10)

The power loss caused by friction in an eccentric load state is:

$$ P_f' = F_f' v = \mu b \left[ \int_a^{a+L} \left. \frac{dv}{dz} \right|_{z=0} dx + \int_{l-a}^{l-a+L} \left. \frac{dv}{dz} \right|_{z=0} dx \right] $$

(11)

where: 

$$ F_f' = \tau A = \mu \left. \frac{dv}{dz} \right|_{z=0} A = \mu \left( \frac{\Delta p a^2(L+x)^2}{\mu(2L+2a)} + \frac{v}{\alpha} \right) A. $$

Additionally, the energy loss for a working cycle \( T \) under an eccentric load condition is:

$$ E' = \frac{T}{8} \left( P_q' + P_f' \right) dt = \frac{4}{3} \left( \frac{\Delta p^2 a^2(L+x)^2}{\mu(2L+2a)} + \frac{\Delta p^2 b(l-L_a)(L+x)^2}{\mu(2L+2a)} \right) $$

$$ + 16 \left( \frac{\Delta p b a(L+x)}{(L+2a)} + \frac{\Delta p b(l-L_a)(L+x)}{(2L+2a-L)} \right) \int_0^T \left( \frac{v}{a} + \frac{16\mu}{a} \left( \ln \frac{l-a+L}{l-a} + \ln \frac{l-a}{l-a} \right) \right) dt $$

(12)

As noted above, energy loss models have been established under the conditions of concentric and eccentric loading. Models for the energy loss are largely dependent on the size of the clearance \( \delta \) and the guidance length \( L \) in the slide guide system.

3. Optimization of the Slide Guide System

The proposed energy loss model described above may now be used to determine the optimum clearances in the slide guide system. The press must be designed so that during metal forming processes, the eccentric loading must be less than some maximum value to ensure proper slide and pillar function. Furthermore, the lateral forces on the hydraulic press must be within the allowable range.

Under eccentric load conditions, and in order to ensure adequate clearance (so that fluid lubrication is present between the slide and pillars), the proposed method employs a stiffness check for the pillars. If there is excessive stiffness in the pillars, then their dimensions may be altered so that they are less stiff. This will not only satisfy operational requirements but also reduce the amount of material in the press.

In order to ensure that sliding between the pillar does not result in excessive wear under working conditions, the proposed method utilizes a wear check method under ultimate conditions. The procedure for optimizing the system is shown in Figure 3.

**Figure 3.** Optimization flow of guidance for slide and pillar of hydraulic press.
3.1. Lateral Force Analysis

In order to ensure hydraulic press functionality and avoid the rail wear associated with excessive friction, some minimum level of oil-film thickness must be guaranteed by the slide guide system. Above some maximum allowable lateral load \( F_p \), the large pressure in the clearances will compromise the oil-film. Since the plunger of the hydraulic cylinder and slide represents a rigid joint, the structure of hydraulic press could be simplified to a space frame, and the lateral force \( F_{1x} \) on the pillars (produced by the eccentric moment \( F_e \)) may be expressed by Equation (13) [21]:

\[
F_{1x} = \frac{F_e}{4(Z + Y)h}
\]

where \( F_{1x} \) is the maximum eccentric load in the X direction, which is the component of the side thrust \( F_1 \) on the pillars, as shown in Figure 4a. Force analysis of space frame under the eccentric load is shown in Figure 4b. Under the action of the operational load, \( F_{\text{working}} \), the slide is acted on by the eccentric moment \( F_e \).

![Figure 4. Lateral force analysis: (a) eccentric moment acting on the slide, and (b) eccentric loads force acting on hydraulic press.](image)

The pressure in the wedge clearances caused by the compression of the lubricating oil is given by Equation (14) [20]:

\[
p = p_1 \left[ \left( \frac{L+a}{x} \right)^2 - 1 \right] \frac{\Delta p}{(L+a)^2} + \frac{6\mu \omega}{\alpha^2(L+2a)} \frac{(x-a)[L-(x-a)]}{x^2}
\]

\[
p' = p'_1 \left[ \left( \frac{L+a}{x} \right)^2 - 1 \right] \frac{\Delta p}{(L+a)^2} + \frac{6\mu \omega}{\alpha^2(2a-L)} \frac{(l+a-x)[x-(l+a-L)]}{x^2}
\]

Then the allowable lateral loads on the slide are given by Equation (15):

\[
F_p = b \left( \int_a^{a+L} pdx + \int_{l+a}^{l+a-L} p'dx \right)
\]
Since \( p' \approx p \), Equation (15) can be expressed as:

\[
F_p = 2p_1Lb - \Delta pLb \left( \frac{a}{L+2a} + \frac{(l+a-L)}{2L+2a-L} \right) + \frac{2q \rho h}{\pi} \left( \ln \frac{L+a}{a} + \ln \frac{l+a}{L+a-L} \right) - \frac{2L}{2L+L} - \frac{2l}{2a+2a-L} 
\]

(16)

It is to be noted that the eccentric load condition must be met, i.e., \( F_{1x} \leq [F_p] \), where \( F_p \) is the allowable lateral force under the condition of minimum oil-film thickness, \( \delta_1 \).

### 3.2. Stiffness Check of Guide Pillars

The stiffness of the guide pillars must be checked under the maximum eccentric load condition to ensure the stability of the press. This check is performed with an applied force on the slide equal to the maximum allowable force and an offset distance, \( e \), of half the dimension of the workbench. The axial forces acting on the pillars include the axial force \( F_e \) caused by working force \( F_{\text{working}} \) and the axial force caused by eccentric moment \( F_e \) (see reference [21]):

\[
F_0 = \frac{F}{4} + \frac{F_e}{2d} \left( 1 - \frac{0.5Y^2}{Z + Y} \right)
\]

(17)

In the stiffness check, the pillars may be regarded as compression bars with both ends under the action of axial force \( F_0 \), and a lateral force \( F_{1x} \). The differential equations for the deflection are given by [22]:

\[
\begin{align*}
EI \frac{d^2x}{dx^2} &= \frac{F_{1x}(h-Yh-Zh)}{h} - F_0 \delta (0 \leq x \leq (Yh + Zh)) \\
EI \frac{d^2x}{dx^2} &= \frac{F_{1x}(Yh+Zh)(l-x)}{h} - F_0 \delta ((Yh + Zh) \leq x \leq l)
\end{align*}
\]

(18)

The solution is given by:

\[
\begin{align*}
\delta &= \frac{F_{1x} \sin k(h-Yh-Zh)}{F_{0h} \sin kh} \sin k(h-x) + \frac{F_{1x}(h-Yh-Zh)}{F_{0h}} (h-x) \\
M &= \frac{F_{1x}k \sin k(h-Yh-Zh)}{F_{0h} \sin kh} \sin k(h-x)
\end{align*}
\]

(19)

where the parameter

\[
k^2 = F_0 / (EI)
\]

(20)

At the midpoint on the pillar where the lateral force, \( F_{1x} \), is applied, the maximum deflection and bending moment are given by:

\[
\delta_{\text{max}} = -\frac{F_{1x}}{2F_0 k} \tan \frac{kh}{4} + \frac{F_{1x}h}{8F_0}
\]

\[
M_{\text{max}} = \frac{EF_{1x}k}{2F_0} \tan \frac{kh}{4}
\]

(21)

(22)

In order to ensure the demanded oil-film thickness between the slide and pillars, some clearance between the pillars and slide is needed. The stiffness of the pillar should satisfy the limitation:

\[
\delta_{\text{max}} < 11 \delta_1 - \delta_2\]

Meanwhile, the strength should also satisfy:

\[
\sigma_{\text{max}} = \frac{F_0}{A} + \frac{M_{\text{max}}}{W} \leq [\sigma]
\]

(23)

The dimensions of the pillar should be revisited if the stiffness of the pillars does not meet the required stiffness under the maximum eccentric load condition.

### 3.3. Wear Check in the Slide Guide System

Under eccentric load conditions, when the length of the guide is too short the pressure in the clearances will be too large and the slide may become jammed due to friction. In this case, the wear between the guide rail and guide plate will be intensified. As shown in Figure 5, under the action of
the force \( F_{1x} \), the stresses \( \sigma_1 \) and \( \sigma_2 \) are generated due to the elastic deformation of the rail. The length of each adjustable guide plate is \( L = L_1 + L_2 \). Due to the stress triangle similarity, the relation is given by Equation (24) [23].

\[
\begin{align*}
\frac{L_1^2}{L_2^2} &= \frac{N_1}{N_2} \\
(N_2 - N_1) \times (S + \frac{L_2}{3}) &= \frac{2L}{3} N_1
\end{align*}
\]

Solving these equations results in:

\[
L_1 = \frac{L^2 + 3SL}{3L + 6S} \quad L_2 = \frac{2L^2 + 3SL}{3L + 6S}
\]

The friction forces \( F_1' \) and \( F_2' \), associated with the lateral forces \( N_1 \) and \( N_2 \) between the guide plate and the sliding rail, are:

\[
F_1' = N_1 f, \quad F_2' = N_2 f
\]

Based on these expressions, the mechanical equilibrium equations are given by Equation (27):

\[
\begin{align*}
F_{1x} h + N_1 \left( S + L - \frac{L_2}{3} \right) + M_e &= M_a + N_2 \left( S + \frac{L_2}{3} \right) \\
F_0 &= F_1' + F_2' \\
F_{1x} + N_1 &= N_2 \\
M_d &= \frac{y(2-y)}{8(Z+Y)} Fe, \quad M_e = -\frac{y^2}{8(Z+Y)} Fe
\end{align*}
\]

Solving Equation (27), we obtain:

\[
N_1 = \frac{3 \left( Yh + S + \frac{L_2}{3} - h \right)}{8 (Z+Y) hL} Fe, \quad N_2 = \frac{2L + 3 \left( Yh + S + \frac{L_2}{3} - h \right)}{8 (Z+Y) hL} Fe
\]

The equivalent forces \( N_1 \) and \( N_2 \) approximately act along the flat surface of the sliding rails. The following constraints should be satisfied in order to avoid failure of the sliding pair:
\[
\max \left( \frac{N_1}{b L_1}, \frac{N_2}{b L_2} \right) \leq [P] \tag{29}
\]

The wear and associated pressure may be calculated using the work of Archard [24,25], and are given by Equation (30):

\[
h' = \frac{K_c P \dot{v} t}{H} \Rightarrow [P] = \frac{h' H}{K_c \dot{v} t} \tag{30}
\]

If the pressure calculated in the guide clearances does not satisfy the requirement according to Equation (28), the critical pressure \([P]\) may be used to calculate the side force \(N_1\) and \(N_2\) according to Equation (27), and the slide guide length \(L\) is then calculated based on the wear check method. The corresponding optimum clearances \(\delta\) of the guides can then be calculated based on Equation (6).

4. Case Study

A hydraulic press (RZU2000HM) (Hefei Metriforming Intelligent Maunfacturing Co., Ltd.: Hefei, China) was investigated as a case study. This press is a sheet metal drawing machine for the front door panel of an automobile. Based on the actual processing parameters, the models and calculation method presented above were used to optimize its slide guide system.

4.1. The Clearances Optimization Based on Energy Loss

The processing parameters for the case study are given in Table 1. ISO 46 hydraulic oil was used in the hydraulic press. The variation of displacement of the slide in a work cycle, \(T\), is shown in Figure 6. At 20 °C, the kinematic viscosity of the hydraulic oil, \(\nu\), is 128 mm²/s, and for an oil proportion \(S'\) of 0.8741, the dynamic viscosity is: \(\mu = S' \nu \times 10^{-9} \approx 1.119 \times 10^{-7}\) MPa s. The clearance \(\delta\) was calculated using Equation (6) as \(\delta = 0.4338\) mm.

\[\text{Figure 6. The displacement of the slide in the forming process of the automobile front door panel.}\]

\[\text{Table 1. The data used in the case.}\]

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
<th>Unit</th>
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<tbody>
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<td>(b)</td>
<td>185</td>
<td>mm</td>
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<tr>
<td>(L)</td>
<td>560</td>
<td>mm</td>
</tr>
<tr>
<td>(v)</td>
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<td>mm</td>
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<td>(\Delta p)</td>
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<tr>
<td>(B)</td>
<td>670</td>
<td>mm</td>
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</table>
The energy loss, $E$, in the cycle $T$ may be found using Equation (7):

$$E = \frac{2}{3} b \Delta p^2 \frac{\delta T}{\mu L} + \frac{8 b H}{L} \int_0^T v(t)^2 \, dt = 5.243 \times 10^3 \delta^3 + \frac{91.40}{\delta}$$

(31)

The relation between $\delta$ and $E$ is shown in Figure 7. It is a nonlinear relationship between the energy loss $E$ and clearances $\delta$. There is an optimum $\delta$ corresponding to the minimum $E$. For the variable velocity in a forming work cycle, the optimal clearances altered. The clearances were optimized based on the designed maximum velocity of the slide, and smaller clearances mean heavy assembly and debugging tasks. According to Equation (7), the minimum energy loss is about $6.39 \times 10^2$ J when $\delta$ is about 0.4 mm.

![Figure 7. The energy loss changing with the fit clearances in a work cycle.](image)

Under the eccentric load condition, the energy loss in a cycle due to leakage and friction, based on Equations (8)–(12), is about $E = 1.17 \times 10^3$ J. For the reason that leakage and friction were increased in the clearance with the eccentric load according to the established model. The energy loss under this eccentric load condition increases by approximately 83% when compared to the non-eccentric load condition.

4.2. The Pillars Optimization in Slide Guide System

In order to ensure that the surfaces of the guide rails and adjustable guide plates in the slide guide system will not be badly worn by eccentric loading, the minimum thickness of the oil film must be guaranteed. For $\delta_2 = 0.03$ mm [18], the tile angle of the slide is $\alpha = (\delta - \delta_2)/(l/2) = 4.038 \times 10^{-4}$ rad. According to Equation (16), the maximum allowable lateral force acting on the guide rails was calculated, and $[F_p]$ is $1.94 \times 10^5$ N. Then, the maximum eccentricity, $e$, in the X direction is 100 mm. According to Equation (13), the eccentric force on the pillar is $F_{1x} = 1.83 \times 10^5$ N $< [F_p]$. Thus, the designed clearances meet the requirements under eccentric loading conditions.

4.2.1. Optimization Based on Stiffness Check

The pillars are made of S45C, and the material constants and key pillar variables are provided in Tables 2 and 3. Under the maximum eccentric load condition in the X direction, according to Equations (13) and (17), the lateral force acting on the pillar $F_{1x_{\text{max}}}$ is $4.2125 \times 10^6$ N, axial forces acting on the pillars $F_0$ is $9.0846 \times 10^6$ N, and the inertia moment $I_x = BH^3/12 = 3.0785 \times 10^{10}$ mm$^4$. Parameter $k$ may be calculated using: $k = [F_0/(EI)]^{1/2} = 3.8412 \times 10^5$ mm$^{-1}$. According to Equations (21)–(23), we obtain:
\[
|\delta_{\text{max}}| = \frac{F_{1x}}{2F_{0}k} \tan \left(\frac{kh}{4} + \frac{F_{1x}h}{8F_{0}}\right) = 0.2903 \text{ mm} \leq |\delta_{1} - \delta_{2}| = 0.4038 \text{ mm}
\]

\[
\sigma_{\text{max}} = 54.8607 \text{ MPa} \leq [\sigma]
\]

(32)

(33)

Table 2. The pillar material constants.

<table>
<thead>
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<th>Ranges</th>
<th>Values</th>
<th>Unit</th>
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<td>GPa</td>
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<td>0.27</td>
<td>-</td>
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<tr>
<td>Yield Strength (\sigma_y)</td>
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<td>-</td>
<td>MPa</td>
</tr>
<tr>
<td>The Allowable Stress ([\sigma])</td>
<td>-</td>
<td>150</td>
<td>MPa</td>
</tr>
</tbody>
</table>

Table 3. The parameters of movable crossbeam of the hydraulic press.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal Press</td>
<td>20,000</td>
<td>kN</td>
</tr>
<tr>
<td>The Size of Workbench and Slide Width in Left-Right Direction</td>
<td>4600</td>
<td>mm</td>
</tr>
<tr>
<td>Height of Slide</td>
<td>2000</td>
<td>mm</td>
</tr>
<tr>
<td>The Working Velocity of Slide Quickly Falls</td>
<td>(\geq 450)</td>
<td>mm/s</td>
</tr>
<tr>
<td>Slow Press</td>
<td>25–50</td>
<td>mm/s</td>
</tr>
<tr>
<td>Quickly Returns</td>
<td>(\geq 400)</td>
<td>mm/s</td>
</tr>
</tbody>
</table>

Under the ultimate eccentric load condition in the \(Y\) direction, we obtain:

\[
|\delta'_{\text{max}}| = 0.2365 \text{ mm} \leq |\delta_{1} - \delta_{2}|, \quad \sigma'^{\ast}_{\text{max}} = 41.3564 \text{ MPa} \leq [\sigma]
\]

(34)

Therefore, the stiffness and strength of the pillars used in this hydraulic press meet the operational requirements and avoid excessive stiffness. Assuming that the deformation of pillar reached the allowable amount of deformation, which is \(|\delta_{1} - \delta_{2}| = 0.4038 \text{ mm}\), then, according to Equations (20) and (21), the minimum inertia moments are \(I_{x} = 2.2149 \times 10^{10} \text{ mm}^4\) and \(I_{y} = 1.2048 \times 10^{10} \text{ mm}^4\), and the variation of sectional parameters \(B\) and \(H\) of the pillars, with respect to each other at the given minimum \(I_{x}\) and \(I_{y}\), is shown in Figure 8. In order to meet the minimum stiffness requirement in both the \(X\) and \(Y\) directions, the optimal section may be calculated, which is a rectangle with \(B\) of 572 mm and \(H\) of 775 mm. For these dimensions, the stress intensities in the two directions are:

\[
\sigma_{\text{max}} = 67.1512 \text{ MPa} \leq [\sigma], \quad \sigma'^{\ast}_{\text{max}} = 56.7040 \text{ MPa} \leq [\sigma]
\]

(35)

Figure 8. The sectional parameters \(B\) and \(H\) changing with each other for the minimum inertia moment \(I_{x}\) and \(I_{y}\).
As is evident, the strength of the pillars meet the working requirement, and the mass of each pillar is approximately 80.69% of the original mass; this saves about 5540.6 kg of steel for the four pillars.

4.2.2. Optimization Based on Wear Check

According to Equations (24)–(28), for the lengths: \( L_1 = 270.4274 \text{ mm} \) and \( L_2 = 289.5726 \text{ mm} \), the following forces are obtained: \( N_1 = 8.2309 \times 10^6 \text{ N} \), \( N_2 = 4.0185 \times 10^6 \text{ N} \). During the forming process of the inner panel of a car front door, the velocity is \( \bar{v} \approx 121.62 \text{ mm/s} \) based on Figure 6. The wear coefficient \( K_e \) of the bronze guides is \( 2 \times 10^{-10} \) under the condition of poor lubrication, and the surface hardness of guide plates on the pillar is \( H = 590 \text{ N/mm}^2 \) (HB). For this extreme working condition, the life (work time) of the hydraulic press will be less than 30 days and produce an average wear depth of \( h' = 0.03 \text{ mm} \). The contact pressure \([P]\) for these conditions is about 280.74 MPa. Based on Equation (29), the contact pressure calculated in the clearances is within the allowable \([P]\). Therefore, the length of the siding pair between the pillar and slide satisfies the operational requirement with the clearances satisfying the objective of minimum total power loss.

The length of the guide plane on a slide is another important factor influencing the guide accuracy, and the contact stresses on the guide surface affects the life of the hydraulic machine under eccentric loading. According to the Xinlu [21], the guide length \( L \) should be about 0.3 to 0.6 times of the slide height, \( l \). Giving different guide lengths \( 420 < L \leq 600, N_1 \) and \( N_2 \) were calculated, and are shown as in Figure 9. Given a minimum length of the guide plane of \( L = 420 \text{ mm} \), the calculated \( L_1 = 204.63 \text{ mm} \), and \( L_2 = 215.38 \text{ mm} \), so:

\[
\max \left( \frac{N_1}{bL_1}, \frac{N_2}{bL_2} \right) = \frac{1.0294 \times 10^7}{185 \times 204.6154} = 271.9277 \text{ MPa} \leq [P]
\]  

(36)

**Figure 9.** Max \( (N_1, N_2) \) and the fit clearances \( \delta \) calculated according to different \( L \) in the range of (420,600).

Therefore, the length \( L \) of the adjustable guide plates on the slide lies on the interval (420,600); thus, the wear constraints are met for the sliding pair in the slide guide system. The relations between \( \max (N_1,N_2) \) and \( L \) and between clearances \( \delta \) and \( L \) are shown in Figure 9. It shows the lateral forces \( N_1 \) and \( N_2 \) are reduced with an increase in the guide length. This means the abrasion of the guide rails are decreased with an increase in the guide length \( L \). Additionally, the guide length \( L \) is linear as a function of \( \delta \), and \( \delta \) increases with an increase in \( L \). As is evident, for a given guide length, the optimum clearances may be calculated based on the principle of minimum overall energy loss.

5. Summary and Conclusions

A mathematical model of total energy loss in a hydraulic press has been developed that considers the leakage and friction in a slide guide system. Based on the principle of minimum overall energy
loss, a method for calculation of optimum clearances was proposed, for which the maximum allowable lateral load may be calculated, which determines the maximum allowable side force that a hydraulic press may undergo.

A stiffness and wear check method for the system under eccentric loading was presented. This method allows for the redesign of the press pillars. Based on an allowable wear constraint associated with the movable crossbeam and pillars, a procedure for calculating of the minimum guide length was proposed.

A case study was considered for a hydraulic press (RZU2000HM). The methods proposed in this paper were used to determine optimum clearances of approximately 0.4 mm. The energy loss was estimated to increase by approximately 83% when subjected to an eccentric loading condition. Using the relations developed herein, the press’ four pillars were redesigned and their weight was reduced by nearly 20% to 80.69%. The length of the guide plates was shown to be reasonable through a wear check. It is believed that the methods developed in this paper may serve as an excellent reference for the optimization of the slide guide system for a hydraulic press.

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Author Contributions: For this article Mengdi Gao developed the models, data measurement for the case study and wrote the paper; Haihong Huang and Zhifeng Liu conceived and designed the verification method; Xinyu Li analyzed the data; John W. Sutherland contributed overall evaluation and revised the paper.

Conflicts of Interest: The authors declare no conflict of interest.

Abbreviations

The following abbreviations are used in this manuscript:

- $\delta$: clearances in slide guide system between slide and pillars
- $\Delta p$: differential pressure between the two ends of clearances
- $L$: length of adjustable guide plate on slide
- $b$: width of adjustable guide plate on slide
- $\mu$: dynamic viscosity of hydraulic oil
- $V(t)$: velocity of slide
- $q$: leakage through the parallel clearances
- $\tau$: liquid shear stress
- $F_f$: friction force caused by shearing oil in parallel clearances
- $P_p$: total power loss in parallel clearances
- $P_q$: power loss caused by leakage in parallel clearances
- $P_f$: power loss caused by friction force in parallel clearances
- $T$: working cycle
- $E$: energy loss in a working cycle $T$ in parallel clearances
- $\delta_1, \delta_1'$, $\delta_2, \delta_2'$: sizes of the upper end of the wedge clearances
- $p_{1}, p_{1}'$: pressure of inlet in wedge clearances
- $a$: intermediate parameter according to the coordinate system in Figure 2
- $l$: height of slide
- $p$: pressure distribution in wedge clearances
- $a$: tilt angle of slide
- $q'$: leaking caused by the up and down wedge clearances
- $F_f'$: friction force caused by shearing oil in wedge clearances
- $E'$: unit energy loss in a working cycle $T$ in wedge clearances
- $[F_p]$ maximum allowable lateral force under the condition of minimum thickness of oil-film $\delta_1$
- $F_{\text{working}}$: operational load
- $F_e$: eccentric moment
- $F_1$: side thrust
- $F_{1x}$: maximum eccentric load in the X direction
- $h$: distance from lower surface of upper crossbeam to top surface of bottom crossbeam
- $Zh$: distance from force bearing point on guide bush out of plunger in cylinder to the lower surface of upper crossbeam ($Z < 1$)
Yh  distance from bearing reaction force point on adjustable guide plates of slide to the bottom surface of top crossbeam (Y < 1)

$F_0$  total axial force

$\sigma_1, \sigma_2$  distribution stress

$L_1, L_2$  length of the distribution stress

$N_1, N_2$  resultant force of the distribution stress

f  friction coefficient

[P]  allowable pressure

Kc  coefficient of wear

P  contact pressure

t  wear time

H  contact surface hardness

$h'$  average wear depth

d  distance between two pillars

B, H  parameters of the section of pillar

References


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