A Fast Solution for the Lagrange Multiplier-Based Electric Power Network Parameter Error Identification Model

Ye Guo, Wenchuan Wu *, Boming Zhang and Hongbin Sun

Department of Electrical Engineering, Tsinghua University, Beijing 100084, China; E-Mails: guoye@mail.tsinghua.edu.cn (Y.G.); zhangbm@tsinghua.edu.cn (B.Z.); shb@tsinghua.edu.cn (H.S.)

* Author to whom correspondence should be addressed: E-Mail: wuwench@tsinghua.edu.cn; Tel./Fax: +86-10-6278-3086 (ext. 805).

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Abstract: The Lagrange multiplier-based method is an effective network parameter error identification method. However, two full matrices with high-dimensions are involved in the calculation procedure; these create huge computational burdens for large-scale power systems. To solve this problem, a fast solution is proposed in this paper, where special treatment techniques for full matrices are used to dramatically improve the calculation efficiency. A practical parameter error identification program has been developed and used in many electric power control centers. In this paper, the results for test systems and on-site applications are given, which show that the proposed approach is very efficient.

Keywords: state estimation; parameter error identification; Lagrange multiplier

1. Introduction

Identifying network parameter errors is important because they can seriously diminish the accuracy of various kinds of power system analyses. State estimation (SE) is very helpful for parameter error identification (PEI) [1], since the measurement residuals may directly indicate the parameter errors. Most existing PEI methods are based on SE results.

There are two types of traditional PEI methods. The first type is based on sensitivity analysis [2–8]. These methods use sensitivity factors between measurements and parameters, along with the measurement residuals to find the most suspicious network parameters. An important advantage of these methods is
that they are directly based on the SE results; therefore, current SE software can be used without any modification. However, the results of sensitivity factor-based PEI methods may be affected by artificial threshold values and random measurement errors. An offline application has been recently reported in [9]. The second type of PEI methods is based on augmented state estimation (ASE) [10–13]. ASE methods augment the parameter errors to the state variables and obtain their estimated values through SE calculation. The suspicious parameter set is limited by the numerical condition problem and should be obtained before calculation. This type of method is more appropriate for parameter estimation (PE) rather than PEI.

The recently proposed Lagrange multiplier (LM)-based method [14–16] is an effective PEI approach, but two high-dimension full matrices are involved during its calculation procedure. This represents a very heavy computational burden and requires huge memory. Furthermore, it is well known that network parameter error identifications should use multiple measurement scans to increase accuracy; the iterative usage of the LM-based PEI method requires a faster calculation speed, even for off-line applications.

The main contribution of this paper is the development of a fast approach for the Lagrange Multiplier (LM)-based PEI model. Specifically, the development concerns a treatment technique for full matrices. Based on the proposed approach, an efficient PEI program has been implemented, which has been used in several power system control centers. Extensive numerical tests on test systems and practical systems have been done to verify the performance of the developed PEI program.

2. Lagrange Multiplier-Based PEI

The LM-based network PEI procedure is based on the weighted least square (WLS) estimator. The procedure was proposed in [14]. The Lagrange Multiplier vector \( \lambda \) for equality constraints on network parameter errors can be calculated from:

\[
\lambda = H_p^TWr = H_p^TW\Delta z
\]

where \( H_p \) is the \( m \times p \) Jacobian matrix between measurements and parameters; \( r \) and \( z \) are \( m \times 1 \) residual vectors considering parameter errors and not considering parameter errors; \( m \) and \( p \) are the numbers of measurements and parameters, respectively; and \( W \) is the diagonal measurement weight matrix.

To normalize the Lagrange Multiplier vector \( \lambda \), its covariance matrix \( \Lambda = \text{cov}(\lambda) \) should be computed first:

\[
\Lambda = H_p^TWSWH_p
\]

\[
S = W^{-1} - H_s^T\left(H_s^TWH_s\right)^{-1}H_s^T = W^{-1} - H_s\Sigma H_s^T
\]

where \( H_s \) is the \( m \times n \) Jacobian matrix between measurements and state variables; \( n \) is the number of state variables; and \( \Sigma \) is the inverse of the information matrix, \( \Sigma = \left(H_s^TWH_s\right)^{-1} \).

The normalized LM \( \lambda^N \) can be calculated as:

\[
\lambda^N = \lambda / \sqrt{\Lambda_{ii}}
\]
In the LM-based network PEI method, the normalized LM vector $\lambda^N$ can then be used as the index for identifying suspicious network parameters. To identify errors in network parameters (along with those of measurements), the LM-based PEI procedure proceeds as follows:

1. Perform SE, and obtain the normalized measurement residual vector $r^N$.
2. Calculate $\lambda^N$ using Equations (1)–(4).
3. If the $\max |\lambda^N, r^N| < \alpha$, where $\alpha$ is a threshold value that can be taken as 3.0, proceed to step 4.
   Otherwise:
   - If the $\max |\lambda^N| \leq \max |r^N|$, the measurement corresponding to $\max |r^N|$ should be considered as erroneous and be removed from the active measurement set. Return to step 1.
   - If the $\max |\lambda^N| > \max |r^N|$, the parameter corresponding to $\max |\lambda^N|$ should be considered as erroneous; modify the corresponding parameter by PE and return to step 1.
4. Output the PEI and SE results.

Calculating the normalized LM vector $\lambda^N$ is critical for the LM-based network PEI method; such calculations involve determining $\Lambda$. However, two full matrices, $S$ and $\Sigma$, are involved in the calculation procedure for the covariance matrix $\Lambda$. The dimensions of $S$ and $\Sigma$ are $m$ and $2n-1$; respectively. For large scale practical power systems, their dimensions may exceed 10,000 or more; this necessitates a prohibitive amount of calculation time and memory storage.

3. Solution

This section will provide an efficient method for calculating $\Lambda_{(i,j)}$. To simplify the presentation, the discussions in this section are based on the decoupled SE method. Similarly, the uncoupled form can be derived. In $H$, if $H_{\alpha(i,j)} \neq 0$, measurement $i$ is said to be relative to state variable $j$. In $H_p$, if $H_{p(i,c)} \neq 0$, then measurement $i$ is said to be relative to parameter $c$. All the measurements relative to parameter $c$ form the relative measurement set of parameter $c$ (expressed by $\varphi_c$). The symmetric production of $\varphi_c$ is called the relative dual measurement set for parameter $c$, and is expressed as $\psi_c$. For an arbitrary set $\varphi_c = \{a, b, d, e\}$, its symmetric production $\psi_c$ is defined as:

$$\psi_c = \{(a,b),(a,d),(a,e),(b,d),(b,e),(d,e)\}$$ (5)

If one assumes $\tilde{H} = WH_p$, then Equation (2) can be expressed as:

$$\Lambda = \tilde{H}^T SH\tilde{H}$$ (6)

The $c$-th diagonal elements $\Lambda_{(c,c)}$ can be calculated by:

$$\Lambda_{(c,c)} = (\tilde{H}_{(1,c)} S_{(1,1)} + \ldots + \tilde{H}_{(m,c)} S_{(m,1)}) \tilde{H}_{(1,c)} + (\tilde{H}_{(1,c)} S_{(1,2)} + \ldots + \tilde{H}_{(m,c)} S_{(m,2)}) \tilde{H}_{(2,c)} + \ldots + (\tilde{H}_{(1,c)} S_{(1,m)} + \ldots + \tilde{H}_{(m,c)} S_{(m,m)}) \tilde{H}_{(m,c)}$$ (7)

Since $\tilde{H}$ is a sparse matrix, only the following elements in the full matrix $S$ have to be calculated to determine $\Lambda_{(c,c)}$:

$$\{S_{(k,q)} | \tilde{H}_{(k,c)} \neq 0, \tilde{H}_{(q,c)} \neq 0\}$$ (8)
Therefore, the subscripted set of the necessary elements in $S$ is exactly the relative dual measurement set $\psi_c$ for parameter $c$. Assume that parameter $c$ belongs to branch $l$; according to the measurement functions, the relative measurement set $\varphi_c$ is formed by the branch power and the terminal node injection power measurements of branch $l$. The relative dual measurement set $\psi_c$ can also be derived easily according to $\varphi_c$.

The necessary subscript set $\Sigma_\psi$ for calculating all of the diagonal elements in $\Lambda$ is:

$$\Sigma_\psi = \psi_1 \cup \psi_2 \cup \ldots \cup \psi_p$$  \hspace{1cm} (9)

Therefore, only a few elements in the full matrix $S$ have to be calculated. This significantly reduces the calculation burden. However, the calculation of $S$ in Equation (2) still involves a full matrix $\Sigma$. According to Equation (2), $S_{(k,q)}$ is calculated by:

$$S_{(k,q)} = \left( H_{x(k,l)\Sigma_{(l,1)}^T} + H_{x(k,l)\Sigma_{(l,2)}^T} + \ldots + H_{x(k,l)\Sigma_{(l,n)}^T} \right) H_{x(l,q)}^T + \left( H_{x(l,l)\Sigma_{(l,1)}^T} + H_{x(l,l)\Sigma_{(l,2)}^T} + \ldots + H_{x(l,l)\Sigma_{(l,n)}^T} \right) H_{x(l,q)}^T$$

$$+ \ldots + \left( H_{x(k,n)\Sigma_{(l,n)}^T} + H_{x(k,n)\Sigma_{(l,n)}^T} \right) H_{x(l,q)}^T$$ \hspace{1cm} (10)

Using the same idea, by calculating the required $S_{(k,q)}$, the necessary elements in $\Sigma$ can be expressed as:

$$\{ \Sigma_{i,j} | H_{x(k,l)} \neq 0, H_{x(q,l)} \neq 0, (k,q) \in \Sigma_\psi \}$$ \hspace{1cm} (11)

For a specified branch $l$, its relative measurements, $k$ and $q$, include both its branch power and its power injection measurements (of $l$’s terminal nodes). For branch power measurements, the relative nodes will only include the terminal nodes of $l$. For power injection measurements, the relative nodes will include their neighbor nodes. In summary, the node indices, $i, j$, for the elements in $\Sigma$ necessary to calculate $\Lambda_{(c,c)}$ can be obtained from the symmetric production of the node set formed by the terminal node of branch $l$ and their neighbor nodes (if the terminal node has injection measurement).

Taking the simple branch shown in Figure 1 as an example, the arrows numbered 1 through 5 stand for measurements, and $B_1$-$B_6$ represent the six nodes. The necessary element set in matrix $S$ is the symmetric production of the measurement set $\{1, 2, 5\}$, which can be expressed as $\{(1, 2), (1, 5), (2, 5)\}$. The necessary element set in matrix $\Sigma$ is the symmetric production of nodes $B_1, B_2$ (terminal nodes), and $B_3, B_4$ (neighbor nodes of $B_1$, since $B_1$ has injection measurements). The elements with rows or columns corresponding to nodes $B_3$ and $B_6$ are unnecessary to calculate, since no injection measurements exist in node $B_2$. The necessary element set in matrix $\Sigma$ is $\{(B_1, B_2), (B_1, B_3), (B_1, B_4), (B_2, B_3), (B_2, B_4), (B_3, B_4)\}$.

**Figure 1.** An example branch.

In summary, the necessary elements in $S$, as well as in $\Sigma$, can be conveniently selected according to the node-branch relationship, and the calculation burden of the diagonal elements of matrix $\Lambda$ can be greatly reduced.
After the necessary elements in $\Sigma$ and $S$ are known, we can use Equations (7) and (10) to calculate these elements. Furthermore, it can be concluded that if the branches with small measurement residuals can be pre-filtered, only a part of the branch parameters will participate in the PEI calculation, and the necessary elements of $S$ and $\Sigma$ can be decreased even more significantly, thereby increasing the calculation efficiency even more.

4. Numerical Tests

4.1. Measurement Pre-Processing

Gross errors in measurements can deteriorate the results of any PEI method. An SE program with a bad data identification function will distinguish all measurements into two groups: good data ($G$) and bad data ($B$). Notably, some measurements are surely erroneous in the set $B$, while the other measurements may be correct, but are infected by parameter errors. Distinguishing between erroneous measurements and measurements infected by parameter errors is very important. The former will deteriorate the PEI results and should be excluded in PEI calculations while the latter is very important evidence of parameter errors.

To maintain calculation efficiency, a simplified method of consistency checking is used. A simple branch is shown in Figure 1 as an example.

1. For a branch power measurement in set $B$ (such as measurement 1 in Figure 1): if $|z_1 - z_2| < c \max (|z_1|, |z_2|)$, it is justified that measurement 1 is correct but infected by parameter errors. Otherwise, it is justified that measurement 1 is erroneous. Here, $c$ is a constant that equals 0.1 in this paper.
2. For an injection measurement in set $B$ (such as measurement 5 in Figure 1): if $|z_1 + z_2 + z_3| < c \max (|z_1|, |z_2|, |z_3|)$, it is justified that measurement 5 is correct but infected by parameter errors. Otherwise, it is justified that measurement 5 is erroneous.

This method is based on a physical concept: when measurement errors occur simultaneously with high relative and consistent values, it is more reasonable that they originate from parameter errors (rather than from bad measurements). Then, a simplified PEI procedure can be obtained:

1. SE with bad data identification function. All measurements will be divided into the groups $G$ and $B$.
2. Distinguish between erroneous measurements and measurements infected by parameter errors.
3. Pre-filter the branches with small measurement residuals that will not take part in the PEI. In this paper, the branches are excluded from the PEI when the largest residual is smaller than 0.01 p.u.
4. Calculate the LM using normal measurements and measurements infected by parameter errors.
5. Calculate the diagonal elements in $\Lambda$ based on the method proposed in Section 3.
6. Calculate the normalized LM.

This simplified PEI procedure no longer needs iterative SE, PEI or PE, and is thus very efficient. The PEI can be carried out based on the SE results directly, and the existing SE codes can be kept unchanged. A PEI program has been developed based on this simplified procedure and the efficient
calculation method concerning the diagonal elements in the covariance matrix. This program is very efficient. Its performances on test systems and on-site test results are introduced as follows.

4.2. 9-Node System

Figure 2 shows the 9-node system in which the PEI procedure is illustrated. The SE is carried out based on commercial decoupled SE software and no modification has been made to the existing code. A single measurement scan is used in this example.

![Diagram of 9-node system](image)

Figure 2. 9-node system.

White noise, based on the real-load flow distribution of the 9-node system, is added to generate the measurement values. The standard deviations of the errors are taken as 0.01 for the power and 0.001 for the voltage measurements, respectively. The reactance of branch 9-8 has been changed manually from 0.1008 p.u. to 0.2016 p.u. as a parameter error, and the active power measurement of branch 4-6 has been changed manually from $-30.57$ MW to $-60.57$ MW to create a gross error. The PEI can be carried out step by step as described in subsection 4.1:

1. Perform SE: the suspicious measurements identified by bad data identification function are listed in Table 1, and the gross errors are in bold.

<table>
<thead>
<tr>
<th>Index</th>
<th>Measurement name</th>
<th>Measurement value (MW/MVar)</th>
<th>Estimation value (MW/MVar)</th>
<th>Residual (MW/MVar)</th>
<th>Normalized residual</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$P_{9,8}$</td>
<td>24.16</td>
<td>20.28</td>
<td>3.88</td>
<td>3.88</td>
</tr>
<tr>
<td>2</td>
<td>$P_{8,9}$</td>
<td>$-24.10$</td>
<td>$-20.21$</td>
<td>$-3.89$</td>
<td>3.88</td>
</tr>
<tr>
<td>3</td>
<td>$P_{4,6}$</td>
<td>$-60.57$</td>
<td>$-27.42$</td>
<td>$-33.15$</td>
<td>32.28</td>
</tr>
</tbody>
</table>

2. From Table 1, it can be concluded that the first two measurements are infected by parameter errors, as their measurement values are consistent (24.16 MW & $-24.10$ MW). In contrast, the measurement $P_{4,6}$ is an erroneous measurement, since its measurement value significantly mismatches with the measurement $P_{6,4}$. 
3. Pre-filter the branch with small measurement residuals. In this example, branches 9-8, 9-6, and 4-6 should take part in the PEI calculation. In fact, as the measurement and parameter errors are manually set, it can be concluded that the branch 8-9 has erroneous parameters; the branch 4-6 has no erroneous parameters but gross error measurement; and the branch 9-6 is infected by erroneous parameters and measurements.

4. LM values are listed in the 3rd column of Table 2.

<table>
<thead>
<tr>
<th>Index</th>
<th>Parameter name</th>
<th>LM</th>
<th>Diagonal element of covariance matrix</th>
<th>Normalized LM</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>R_{9,8}</td>
<td>0.2464</td>
<td>532.0597</td>
<td>0.0106</td>
</tr>
<tr>
<td>2</td>
<td>X_{9,8}</td>
<td>-11.6343</td>
<td>577.0581</td>
<td>0.4843</td>
</tr>
<tr>
<td>3</td>
<td>R_{9,6}</td>
<td>18.3963</td>
<td>6832.8302</td>
<td>0.2225</td>
</tr>
<tr>
<td>4</td>
<td>X_{9,6}</td>
<td>26.3575</td>
<td>4000.9433</td>
<td>0.4167</td>
</tr>
<tr>
<td>5</td>
<td>R_{4,6}</td>
<td>-1.8738</td>
<td>4305.6817</td>
<td>0.0285</td>
</tr>
<tr>
<td>6</td>
<td>X_{4,6}</td>
<td>-8.0983</td>
<td>1703.2123</td>
<td>0.1962</td>
</tr>
</tbody>
</table>

5. The necessary elements in matrix $S$ are drawn in Equation (12), where the measurement index $M_{i,s}$ is a simplified expression of four measurements including P1-4, Q1-4, P4-1, and Q4-1, and $M_1$ is a simplified expression of P1 and Q1.

\[
S = \begin{bmatrix}
M_{1,4} & M_{2,4} & M_{3,4} & M_{4,4} & M_{5,4} & M_{6,4} & M_{7,4} & M_{8,4} & M_{9,4} & M_{1,5} & M_{1,6} & M_{1,7} & M_{1,8} & M_{1,9} \\
M_{2,5} & M_{2,6} & M_{2,7} & M_{2,8} & M_{2,9} & M_{3,5} & M_{3,6} & M_{3,7} & M_{3,8} & M_{3,9} & M_{4,5} & M_{4,6} & M_{4,7} & M_{4,8} & M_{4,9} & M_{5,6} & M_{5,7} & M_{5,8} & M_{5,9} & M_{6,7} & M_{6,8} & M_{6,9} & M_{7,8} & M_{7,9} & M_{8,9} & M_{9,9}
\end{bmatrix}
\]

6. The necessary elements in the calculation of diagonal elements in matrix $\Lambda$, which correspond to the parameters of branches 9-8, 9-6, and 4-6, are highlighted by signals “×”, “●” and “⊗”, respectively. The signal “.” is used to show the position of the necessary elements more clearly and has no physical meaning. Taking branch 9-8 as an example, its relative measurements include $M_{k,s}$ (branch power measurements), and $M_k$ and $M_s$ (injection power measurements for terminal nodes); the necessary measurements in $S$ are the diagonal and cross elements of these
Taking branch 9-8 as an example, the terminal nodes 9 and 8 both have injection measurements (node 9 has zero injection measurements), and the necessary elements in $\Sigma$ include the terminal nodes (8, 9) and their neighbor nodes (3, 6, 7). The diagonal and cross elements corresponding to these five nodes are necessary and highlighted by “$\times$”:

7. The normalized LM values are listed in the last column of Table 2. The reactance of branch 9-8 has the largest normalized LM, and has been correctly identified as a parameter error.

From the above example of the 9-node system, it can be concluded that only a few elements are necessary to the calculation. The simplified PEI procedure is very efficient, and is based directly on the SE results.

4.3. 118-Node System

To comprehensively evaluate the efficiency of the proposed method, extensive numerical tests have been done on the IEEE 118-node system. The measurements construction is same as the 9-node system tests’. To test the performance of the PEI program with different rates of gross errors, three classes of tests with 0, 1, and 2% bad measurement rates are produced, where the standard error of bad measurements is of 100 times that of normal measurements. In each class, 10 groups of tests with 1, 2, …, 10 parameter errors are produced. The error parameter fell between 2–10 times the true value 50% of the time, and between 0.1–0.5 times the true value the rest of the time. A total of 900 tests (with 30 samples each) have been selected. To evaluate the effectiveness of the proposed $\Lambda$ matrix calculation method, the following two indices were counted:

1. Average necessary element rates in $\mathbf{S}$: $\mathbf{S}$ is a 1098 × 1098 full matrix in this test. The necessary element rates are calculated in Figure 3; their values are all less than 0.1%.
2. Average necessary element rates in $\Sigma$: since decoupled SE software is used, $\Sigma$ is a 118 × 118 full matrix in both the P-sub and Q-sub iterations. The necessary element rates are calculated in Figure 4; their values are all less than 6.5%.

From Figures 3 and 4, it can be concluded that the proposed calculation method for the diagonal elements of $\Lambda$ is very effective. Less than 6.5% of the elements of $\Sigma$ and 0.1% of the elements of $\mathbf{S}$
need to be calculated. Therefore, the proposed method can significantly increase the efficiency of the PEI and can make practical the LM-based PEI for real-world applications.

**Figure 3.** Average necessary element rates in the $S$ matrix.

**Figure 4.** Average necessary element rates in the $\Sigma$ matrix.

### 4.4. Practical Application

In practical application, multiple measurement scans are used to increase the accuracy [16]. Employing LM for PEI and ASE for PE, this program has been used in several electric power control centers in China. As an example, the results of a provincial power system with 500 buses in Central China are shown. To this end, 96 continuous scans with 15-minutes intervals are realized and the results are presented in Table 3. The reactance of the “Luoanjia line” has the largest normalized (LM). The PE results also indicate that this parameter is erroneous (the estimated value of 1.3928 p.u. is far from its initial 3.2600 p.u.). The relative measurement residuals before and after parameter modification are listed in Table 4. Before parameter modification, the relative measurements have significant residuals (4th column), which indicates the existence of parameter errors. However, after modifying X of the Luoanjia line (from the initial value 3.2600 p.u. to the estimated value 1.3928 p.u.),
these measurement residuals decreased significantly (6th column), leading to the conclusion that these parameter identifications and estimation system results are reasonable.

**Table 3.** PEI and PE results for a provincial system.

<table>
<thead>
<tr>
<th>Index</th>
<th>Parameter name</th>
<th>Normalized multipliers</th>
<th>Initial parameter (p.u.)</th>
<th>Estimated parameter (p.u.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>X of Luoanjia line</td>
<td>2.4995</td>
<td>3.2600</td>
<td>1.3928</td>
</tr>
<tr>
<td>2</td>
<td>X of Luoanyi line</td>
<td>1.3589</td>
<td>1.3590</td>
<td>1.3613</td>
</tr>
<tr>
<td>3</td>
<td>X of Anquanjia line</td>
<td>1.2064</td>
<td>0.7880</td>
<td>0.8059</td>
</tr>
<tr>
<td>4</td>
<td>X of Anquanyi line</td>
<td>1.0687</td>
<td>1.0230</td>
<td>0.9523</td>
</tr>
<tr>
<td>5</td>
<td>R of Luoanjia line</td>
<td>0.8023</td>
<td>0.0960</td>
<td>0.1122</td>
</tr>
</tbody>
</table>

**Table 4.** Relative measurement residuals before and after modifying X of Luoanjia line.

<table>
<thead>
<tr>
<th>Measurement name</th>
<th>Measurement value (MW/MVar)</th>
<th>Before parameter modification</th>
<th>After parameter modification</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Estimated value (MW/MVar)</td>
<td>Residual (MW/MVar)</td>
<td>Estimated value (MW/MVar)</td>
</tr>
<tr>
<td>P on the head of Luoanjia line</td>
<td>204.1810</td>
<td>111.6740</td>
<td>204.1610</td>
</tr>
<tr>
<td>Q on the head of Luoanjia line</td>
<td>33.9729</td>
<td>41.3437</td>
<td>37.1494</td>
</tr>
<tr>
<td>P on the head of Luoanyi line</td>
<td>204.9290</td>
<td>271.3250</td>
<td>204.8880</td>
</tr>
<tr>
<td>Q on the head of Luoanyi line</td>
<td>33.7133</td>
<td>87.2995</td>
<td>36.8434</td>
</tr>
</tbody>
</table>

Figure 5 shows the computation times of PEI and decoupled SE. In this practical system, the computation time of the PEI procedure is less than 0.7 seconds for each measurement scan; this is only about twice SE’s computational time. The developed LM-based PEI program is very efficient and is absolutely acceptable for on-site application.

**Figure 5.** Comparison of calculation speeds between PEI and SE.
5. Conclusions

It is very important to maintain network parameter accuracy with high efficiency in power systems. In this paper, an efficient solution for the Lagrange multiplier-based parameter error identification method is proposed. A parameter error identification program based on the Lagrange multiplier has been developed and put into real practice at several electric power control centers in China. The results of test systems and practical systems demonstrate the effectiveness and efficiency of the proposed solution.

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Author Contribution

Ye Guo and Wenchuan Wu proposed the algorithm and prepared the manuscript, Ye Guo implement the software of the algorithm, Boming Zhang and Hongbin Sun revised the paper.

Conflicts of Interest

The authors declare no conflict of interest.

References


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