

*Article*

## **Experimental and Numerical Analysis of Thermal and Hygrometric Characteristics of Building Structures Employing Recycled Plastic Aggregates and Geopolymer Concrete**

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**Abstract:** The correct estimation of building energy consumptions is assuming an always increasing importance, and a detailed reproduction of building structures, with all the single components involved, is necessary to achieve this aim. In addition, the current ecological development tries to limit the use of natural raw materials as building components, in favor of alternative (waste) materials, which ensure significant advantages from the economic, energetic and environmental point of views. In this work, dynamic heat and vapor transport in a typical three-dimensional (3D) building structure, involving different types of environmental-friendly concrete mixtures, have been simulated by using finite elements. In particular, the authors propose to substitute part of the aggregates with plastic waste and to use a fly ash based geopolymeric binder for the production of low conductivity concrete, to be employed in eco-efficient buildings. Concrete produced with natural limestone aggregates has been considered as the reference benchmark. The whole characterization of the different types of concrete tested in the present work has been obtained through laboratory experiments. The structure taken into account in the simulations is a 3D thermal bridge, typical of building envelopes. The thermal and hygrometric transient behavior of this structure, employing plastic waste in different percentages and geopolymer concrete, has been analyzed by the authors.

**Keywords:** geopolymer; lightweight concrete; thermal transmittance; thermal conductivity; heat transfer; temperature contours; vapor permeability; numerical modeling; recycled plastic waste aggregate

### Nomenclature:

$c$	= specific heat capacity ( $\text{J}/(\text{kg} \cdot \text{K})$ )
$C_{0-30}$	= concrete mixture (numbers from 0 to 30 indicate the percentage of recycled plastic)
$G$	= geopolymeric concrete
$h_c$	= convective heat transfer coefficient ( $\text{J}/(\text{kg} \cdot \text{K})$ )
$p_v$	= partial pressure of vapor (Pa)
$p_{sat}(T)$	= saturation pressure of water at temperature $T$ (Pa)
$\dot{q}$	= heat flux ( $\text{W}/\text{m}^2$ )
$s$	= thickness (m)
$T$	= temperature (K)
$T_p$	= surface temperature (K)
$T_\infty$	= environment temperature (K)

### Greek Symbols

$\delta$	= water vapor permeability ( $\text{kg}/(\text{m} \cdot \text{s} \cdot \text{Pa})$ )
$\lambda$	= thermal conductivity ( $\text{W}/(\text{m} \cdot \text{K})$ )
$\phi$	= relative humidity
$\rho$	= density ( $\text{kg}/\text{m}^3$ )
$\vartheta$	= time (s)

### Subscripts

0	= initial
$b$	= bricks
$co$	= concrete
$e$	= exterior
$eq$	= equivalent
$i$	= interior
$s$	= steel
$v$	= vapor
$w$	= water

## 1. Introduction

The always increasing attention given to the concepts of sustainable development and energy saving makes it necessary to adopt proper solutions to protect the environment and at the same time

reduce the overall energy consumption needed for the human activities. The building process involves high energy consumption and has significant effects on the environment. Therefore, the sustainable development concept tries to limit the use of natural raw materials in building applications and to increase the adoption of alternative materials, such as plastic wastes obtained from other industrial production processes. In this way, recycled plastic waste can be used as aggregate for concrete, offering significant advantages from the economic, energetic and environmental point of views.

These aspects assume a significant role, since plastic is used worldwide and an increase of plastic consumption has been registered in all countries, with a consequent increase of plastic waste production. For example, in 1996, about 12% in terms of weight of all municipal solid waste (MSW) in the United States was composed of plastics [1]. The world's annual consumption of plastic materials increased from around 5 million tons in the 50s to nearly 100 million tons in 2001 [1]. Therefore, it is evident that managing plastic waste is one of the most important problems of waste management, also because this kind of waste is non-biodegradable and it is composed by many toxic chemicals (especially cadmium and lead) that would produce significant pollution if not properly managed. Moreover, the Italian Legislative Decree n. 152/2006 [2] encourages the recovery of solid waste as an alternative to landfill disposal.

It is worth noting that a number of studies have dealt with the tuning of chemical-physics properties of plastic materials in order to obtain eco-friendly materials and reduce energy requirements, for example in the realization of OLED, PLED or FET [3–5].

Research is being conducted on the utilization of waste products in concrete. These waste products include discarded tires, plastic, glass, steel, burnt foundry and sand [1]. Plastic could be used in various applications, and efforts have been done to explore its use in concrete and asphalt. A review on waste and recycled plastics, waste management options, and the effects of recycled plastic on the fresh and hardened properties of concrete is available in [1,6].

A number of papers dealing with the experimental characterization of concrete mixtures employing different kinds of recycled aggregates have been published in the last few years [7–20]. In fact, Behiry [13] showed that by mixing recycled concrete aggregate (RCA) with traditional limestone aggregate (LSA), the mechanical properties of the mixture can be improved, taking the unconfined compressive strength as a quality indicator. Variables influencing the unconfined compressive strength such as cement content, curing time and dry density play important roles to determine the performance of the mixture. Specific treatments by using low concentration acid, aimed at producing high quality RCA for structural concrete applications, are under investigation [14]. Waste polyethylene terephthalate (PET) is deemed promising by the scientific community as an alternate binding material in place of the commonly used ordinary Portland cement, and it is also studied together with composite structures [15–19]. Furthermore, experimental data are often accompanied by numerical analysis in order to investigate the mechanical behavior of RCA structures [17,20].

It is possible to further reduce the concrete carbon footprint by substituting the traditional cement binder with a novel geopolymeric binder. The term “geopolymer” was introduced by Davidovits in the late 1970s, and nowadays identifies a family of amorphous alkali or alkali-silicate activated aluminosilicate binders of composition  $M_2O \cdot mAl_2O_3 \cdot nSiO_2$  usually with  $m \approx 1$  and  $2 \leq n \leq 6$  (where M usually is Na or K) [21]. Setting and hardening mechanisms of geopolymeric binders are quite different from those of cement based binders. In fact, the preparation of geopolymeric

binders is carried out by mixing reactive silico-aluminate materials with strongly alkaline solutions such as alkali metal (Na, K) hydroxides or silicates. In this environment, the silico-aluminate reactive materials are rapidly dissolved. A complex reaction mechanism follows, in which solubilized silica and alumina condense with the ultimate formation of a three-dimensional network [21]. The synthesis of geopolymers has been carried out starting from a wide variety of virgin raw materials, such as metakaolin [22–24], natural clays [25] and other natural silico-aluminates [26], as well as industrial process wastes such as coal fly ash [27–29] and metallurgical slag [30]. Geopolymer-based materials are attractive because excellent mechanical properties, high early strength, high durability, freeze-thaw resistance, low chloride diffusion rate, abrasion resistance, thermal stability and fire resistance, can be achieved [31–33]. Due to their lower Ca content, they are also more resistant to acid attack than Portland cement-based materials [34].

In addition, geopolymer-based materials are of great interest thanks to the reduced energy resources needed for their manufacture, due to the reaction pathways involved, with consequent mitigation of greenhouse gas (CO<sub>2</sub>) emissions. In fact, the production of kaolin-based or fly ash-based geopolymeric cement generates an amount of CO<sub>2</sub> up to six times or nine times less than Portland cement, respectively. The result is a reduction of greenhouse gas emissions up to about 90% [35,36]. On the other hand, a great deal of attention is given today to the issue of energy efficiency in buildings as demonstrated by international and national directives [37–42], that require member states to ensure minimum energy performance requirements for new and existing buildings. In particular, building envelopes must have good insulation properties, attenuation and phase-shift capacity of the external loads. Therefore, maximum values of the thermal transmittance and of the periodic thermal transmittance of building components must be ensured [40,42]. In particular, vertical walls, horizontal walls and windows must respect the limiting values of the thermal transmittance imposed by the National Legislative Decree n. 311/2006 [42], depending on the climatic zones defined in the National Legislative Decree n. 192/2005 [41]. Instead, the limiting value for the module of the periodic thermal transmittance of opaque walls assumes the fixed value of  $0.20 \text{ W}/(\text{m}^2 \cdot \text{K})$  [40]. In the case of upgrading the energy efficiency of existing buildings, the interventions can cause an increase of the structures weight, with possible problems of the static equilibrium. As a consequence, there is a need in the building sector to employ innovative and eco-efficient materials, that allow at the same time to reduce thermal dispersions, temperature oscillations and structures' weights.

Therefore, the use of structural and non-structural alternative materials with lower thermal conductivity and specific heat capacity than the traditional ones can contribute to reduce heat losses and temperature oscillations of the building envelopes, with consequent reduction of energy consumptions and related emissions. Moreover, the choice of recycled materials as alternative would have a positive impact on both construction and recycling sectors, with consequent increase of energetic efficiency on broad scale.

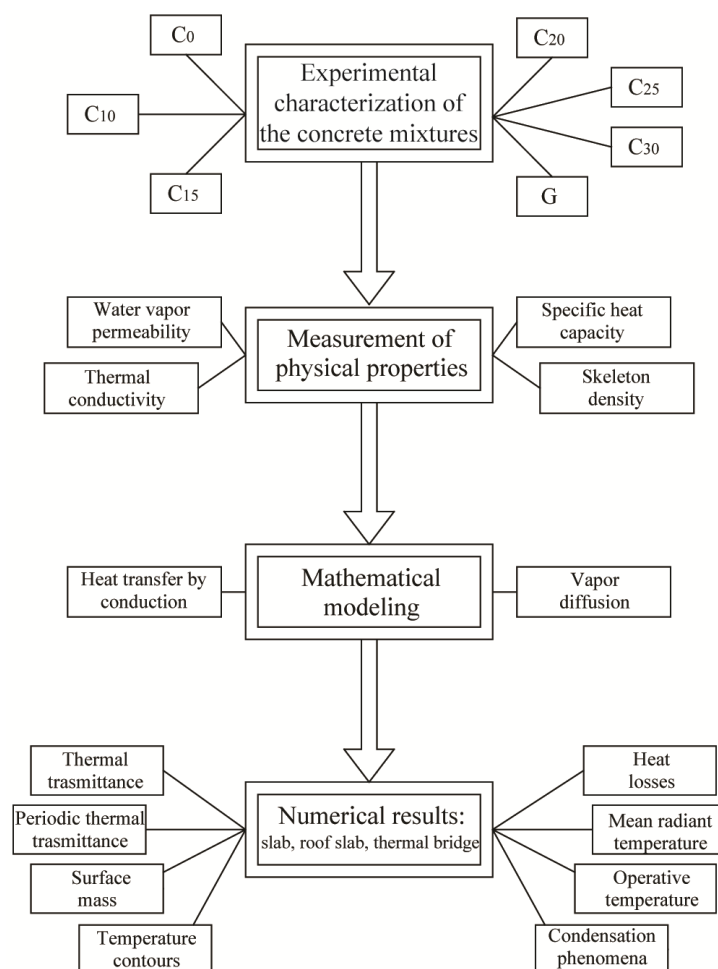
In the authors' opinion, the development of new construction materials employing recycled plastics assumes a crucial role in both the construction and the plastic recycling industries. These materials could be used for building applications, as structural and non-structural parts of the envelope, ensuring at the same time good thermal, hygrometric and mechanical properties, economic savings and energetic advantages. Furthermore, the present eco-efficient concrete mixtures can contribute to reduce

the weight of building structures, given their reduced density, that is an important aspect to take into account, especially with regards to seismic forces.

To the authors' knowledge, numerical investigations of heat and mass transfer in three-dimensional (3D) building structures employing concrete with recycled plastic aggregates or geopolymer as binder are not available in the literature. Therefore, the authors have carried out laboratory experiments in order to characterize different concrete mixtures in terms of mechanical, thermal and hygrometric properties. In particular, the values of the following properties are reported in the present paper: density, vapor permeability, thermal conductivity, specific heat capacity. These experimental data have then been used in a numerical simulation code, based on finite elements, in order to reproduce the transient behavior of a typical building structure, characterized by a 3D field of the quantities of interest, defined as thermal bridge. This novel paper integrates the experiences of the authors belonging to research groups, working in two research areas: materials sciences [7–10,23,25,29,33] and thermal sciences [43–48].

The present paper is structured as follows: the next section describes the materials employed in the experiments. Section 3 describes the experimental procedures used to measure the thermo-hygrometric properties. In Section 4, the mathematical model employed is introduced. The fifth section presents the main obtained results, while some conclusions are drawn in the last section. A flow-chart of the structure of the present work is reported in Figure 1.

**Figure 1.** Flow-chart of the work carried out by the authors.



## 2. Materials Employed in the Experiments

This work proposes the use of plastic waste aggregate supplied by the company Ri.genera s.r.l. (Marigliano (NA), Italy) for the production of low conductivity concrete for eco-efficient building applications. A natural limestone aggregate has been used as reference benchmark. The cement used was CEM II/A-L 42,5 R, according to European Standards EN-197-1 [49], produced by the Italcementi factory (Matera, Italy).

The fine and coarse aggregates were crushed limestone, with density values of 2351 and 2372 kg/m<sup>3</sup>, and water absorption capacity of 2.05% and 0.63%, respectively. They were separated into different size fractions that were then recombined to a specific grading. The fly ash employed was supplied by ENEL S.p.A. (Brindisi, Italy). The respective chemical compositions are reported in Table 1.

**Table 1.** Chemical composition of materials (wt%).

Oxides	CEM	Fly ash	Marble sludge
CaO	60.84	4.32	53.76
SiO <sub>2</sub>	20.66	53.75	2.13
Al <sub>2</sub> O <sub>3</sub>	4.89	28.12	0.12
Fe <sub>2</sub> O <sub>3</sub>	3.24	6.99	0.69
MgO	1.94	1.59	0.15
SO <sub>3</sub>	2.95	-	-
Na <sub>2</sub> O	0.12	0.87	-
K <sub>2</sub> O	0.84	1.89	-
Cl <sup>-</sup>	0.94	-	-
LoI *	5.76	6.01	42.74

\* Loss on ignition.

The superplasticizer used was an acrylic one with 40% solid content and a specific gravity of 1.2 kg/dm<sup>3</sup>. The water content of the superplasticizer was considered during the mix-design phase. Six conventional concrete mixtures have been designed in addition to a geopolymeric concrete characterized by S5 consistency class [50]. The workability was kept constant for all the mixtures. Table 2 shows mixture proportions for all the concrete specimens.

**Table 2.** Mixture proportions of concrete samples.

Mixture	G	C <sub>0</sub>	C <sub>10</sub>	C <sub>15</sub>	C <sub>20</sub>	C <sub>25</sub>	C <sub>30</sub>
Cement (kg/m <sup>3</sup> )	-	300	300	300	300	300	300
Natural aggregate (kg/m <sup>3</sup> )	854	1648	1351	1293	1227	1203	1101
Plastic aggregate (kg/m <sup>3</sup> )	-	0	70	105	140	175	210
Fly ash (kg/m <sup>3</sup> )	208	90	90	90	90	90	90
Marble sludge (kg/m <sup>3</sup> )	-	146	152	163	171	176	183
Activating solution (kg/m <sup>3</sup> )	138	-	-	-	-	-	-
Acrylic admixture (L/m <sup>3</sup> )	-	6.86	7.26	8.05	8.91	8.75	9.95
Water/cement	N.A.	0.5	0.5	0.5	0.5	0.5	0.5

The activating solution employed to prepare the geopolymer concrete has the following composition: Na<sub>2</sub>O · 0.90SiO<sub>2</sub> · 14.7H<sub>2</sub>O and was prepared starting from a commercial sodium silicate

solution ( $\text{SiO}_2 / \text{Na}_2\text{O}=3.3$ ) supplied by Prochin Italia s.r.l. (Marcianise (CE), Italy) and a 10 M NaOH solution prepared by using NaOH in pellets (analytical R grade, Baker, Milan, Italy). Geopolymer specimens have been cured at room temperature, completely wrapped in a PVC film, in order to prevent any early water evaporation.

The mix proportions of the concrete mixtures are reported in Table 2. In this table, the first part of the mixture code gives information on the kind of concrete (C indicate conventional concrete, G geopolymeric concrete), while the second part indicates the percentage of waste plastic employed as aggregate (from 0% to 30 %). The mixtures used in the present work have similar mixture proportions in terms of the aggregate to cement ratio. The water to cement ratio was kept constant at 0.5 for all the cement based concrete mixtures.

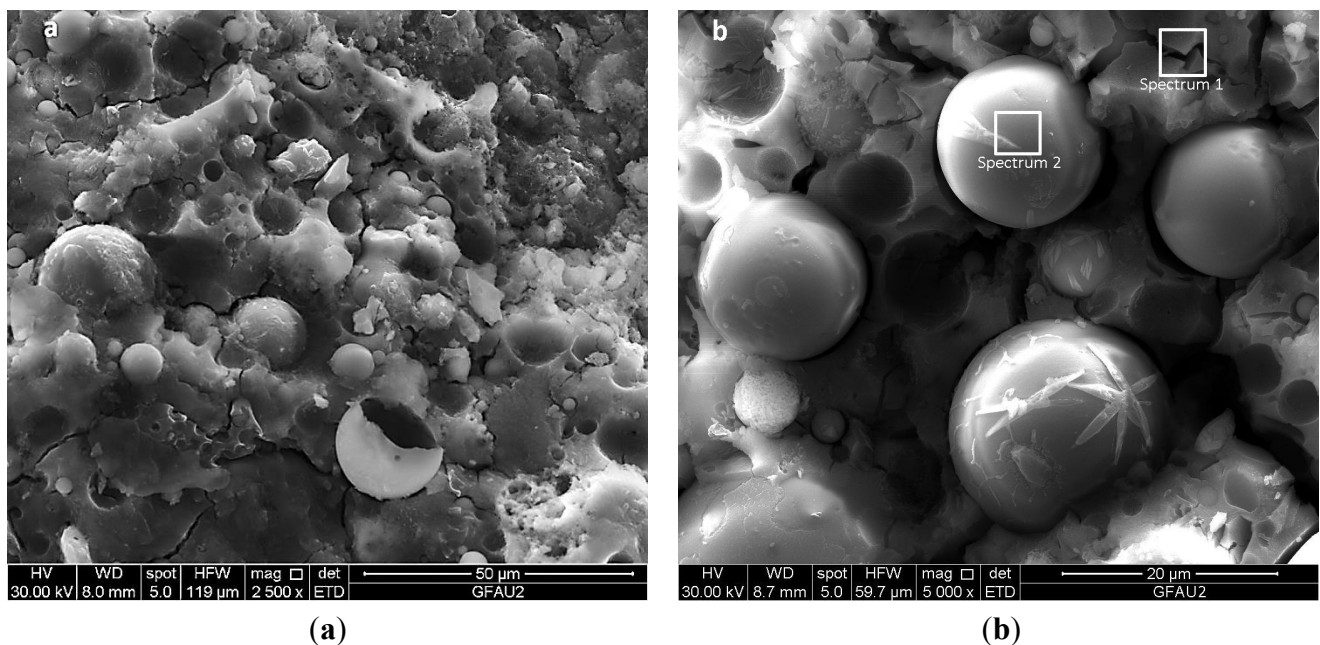
In order to assess the correct development of the geopolymerization process, 28 days cured specimens were analyzed by Scanning Electron Microscopy (SEM) and Energy Dispersive Spectroscopy (EDS) elemental analysis. SEM micrographs reported in Figure 2 refer to the binder matrix and show a typical fly ash based geopolymer microstructure [51]. A cementitious matrix constituted by the reaction products between the sodium silicate solution and the alumino-silicate precursors can be observed from the figure, and its chemical composition, as derived from the elemental analysis, is reported in Table 3. Several unreacted fly ash particles are observed to coexist with reaction products and with a few particles attacked by the alkaline solution but which maintain their spherical shape. The chemical composition of the spherical fly ash particles, as derived from the elemental analysis, is reported in Table 4. It may be noticed the higher percentage of sodium in the spectrum 1, arising from the polycondensation reaction involving fly ash and sodium silicate solution.

**Table 3.** Spectrum 1, elemental analysis performed on the area delimited by the white square.

Element	Weight %	Atomic %
C K	4.69	7.52
O K	51.83	62.46
Na K	9.64	8.08
Mg K	0.38	0.30
Al K	7.04	5.03
Si K	20.41	14.01
P K	0.15	0.09
S K	0.21	0.13
K K	1.25	0.62
Ca K	1.31	0.63
Ti K	0.40	0.16
Cr K	1.20	0.45
Fe K	1.49	0.51
Totals	100.00	-

**Table 4.** Spectrum 2, elemental analysis performed on the area delimited by the white square.

Element	Weight %	Atomic %
O K	54.82	68.60
Na K	1.60	1.40
Mg K	0.22	0.18
Al K	12.99	9.64
Si K	25.05	17.85
K K	2.14	1.09
Ca K	0.17	0.09
Ti K	0.76	0.32
Cr K	1.02	0.39
Fe K	1.23	0.44
Totals	100.00	-

**Figure 2.** SEM micrographs of the geopolymers binder at (a) 2500 $\times$  and (b) at 5000 $\times$ .

### 3. Measurement of Vapor Permeability and of Thermal Properties

Water vapor permeability was measured according to the UNI EN 1015-19 [52]. Appropriate boxes were filled with a saturated solution of potassium nitrate. Concrete cylindrical specimens (22 cm diameter, 3 cm height) were used to close the upper part of the box, producing an internal atmosphere of the container with 93% relative humidity at 20 °C.

Then, the boxes were put into a climatic chamber with a controlled temperature ( $20 \pm 2$  °C) and relative humidity ( $50\% \pm 5\%$ ), in order to obtain a difference of relative humidity between the two disc surfaces. The weight of the boxes was measured at constant intervals of time and the water vapor transmission rate was determined by the change in mass of the system at steady state.

This test was carried out until the required stability in the specimens weight was obtained and allowed to measure the water vapor permeability and the water vapor resistance, which is related to the



material's reluctance to let water vapor to pass through. High water vapor resistance values indicate high resistance to water vapor transmission.

The thermal conductivity and the specific heat capacity of the six concrete mixtures and the geopolymer were measured by using the TPS 1500 Thermal Conductivity System (ThermTest Inc., Fredericton, NB, Canada). This instrument has the following characteristics declared by the manufacturer: thermal conductivity measurement range 0.001 to 20 W/(m·K), specific heat capacity measurement up to 5 MJ/(m<sup>3</sup>K), reproducibility typically better than 1%, accuracy better than 5%.

#### 4. The Mathematical Model

The mathematical model employed in the present work for the simulation of heat and mass transfer through a three-dimensional (3D) thermal bridge, characterized by the presence of the materials described in the previous sections, consists in the unsteady equations for heat and vapor transport through homogenous permeable media. The following governing equations are written for each isotropic homogeneous material that is found in a typical building envelope:

*Heat transfer by conduction:*

$$\rho c \frac{\partial T}{\partial \vartheta} = \lambda \nabla^2 T \quad (1)$$

*Vapor diffusion:*

$$\frac{\partial p_v}{\partial \vartheta} = \delta \nabla^2 p_v \quad (2)$$

The partial differential Equations (1) and (2) are solved with the following boundary and initial conditions:

$$\begin{aligned} T(x, y, z, \vartheta = 0) &= T_0; \quad p_v(x, y, z, \vartheta = 0) = p_{v,0} \quad \text{in the whole computational domain} \\ h_{c,i} [T_{\infty,i} - T_{P,i}(x, y, z, \vartheta)] &= -\lambda \frac{\partial T(x, y, z, \vartheta)}{\partial n} \Big|_{P,i}; \quad p_v = p_{v,i} \quad \text{on the interior surfaces} \\ h_{c,e} [T_{\infty,e} - T_{P,e}(x, y, z, \vartheta)] &= -\lambda \frac{\partial T(x, y, z, \vartheta)}{\partial n} \Big|_{P,e}; \quad p_v = p_{v,e} \quad \text{on the exterior surfaces} \\ \frac{\partial T(x, y, z, \vartheta)}{\partial n} \Big|_P &= 0; \quad \frac{\partial p_v(x, y, z, \vartheta)}{\partial n} \Big|_P = 0 \quad \text{on the remaining (lateral) surfaces} \end{aligned} \quad (3)$$

where  $T_0$  and  $p_{v,0}$  are the initial temperature and partial pressure of vapor, respectively,  $h_{c,i}$  and  $h_{c,e}$  are the convective heat transfer coefficients of the interior and exterior environment, respectively,  $T_{\infty,i}$  and  $T_{\infty,e}$  are the interior and exterior environment temperatures, respectively,  $T_{P,i}$  and  $T_{P,e}$  are the temperatures of the interior and exterior surfaces, respectively,  $p_{v,i}$  and  $p_{v,e}$  are the partial pressures of vapor in the interior and exterior environment, respectively. The simple mathematical model described above is solved by using the well known Finite Element Method [53,54].

In order to avoid interstitial and superficial water condensation, the following condition must be satisfied in each point of the structure [55]:

$$p_v < p_{sat}(T) \quad (4)$$

where  $p_{sat}(T)$  is the saturation pressure of water calculated at temperature  $T$ .

The relation between temperature and saturation pressure of water is [55]:

$$p_{sat}(T) = 610.5 e^{\left(\frac{17.269 \cdot T}{237.3 + T}\right)} \quad \text{for } T \geq 0^\circ\text{C} \quad (5)$$

$$p_{sat}(T) = 610.5 e^{\left(\frac{21.875 \cdot T}{265.5 + T}\right)} \quad \text{for } T < 0^\circ\text{C}$$

where the temperature must be expressed in Celsius degrees ( $^\circ\text{C}$ ).

In common practice, the conditions characterized by a partial pressure of vapor,  $p_v$ , larger than saturation pressure of water at a prescribed temperature,  $p_{sat}(T)$ , are not physical, since the saturation pressure is the maximum pressure compatible at that prescribed temperature value. Therefore, inside the computational domain, wherever  $[p_v - p_{sat}(T)] \geq 0$ , condensation is occurring.

## 5. Results

In the present work, the authors have simulated both unsteady conduction heat transfer and vapor diffusion in a typical building structure, characterized by a three dimensional (3D) field of the quantities of interest, defined as thermal bridge [56]. The type of thermal bridge considered in the present simulations is the one proposed in the technical standard [56], modified with the insertion of structures employed in actual constructions. In particular, a steel-concrete column ( $0.3 \times 0.3 \times 2.3 \text{ m}^3$ ), a brick concrete slab ( $0.25 \times 0.86 \times 1.8 \text{ m}^3$ ), screed, tiles, interior and exterior plasters have been inserted in the simulated geometry. A sketch of this geometry is reported in Figure 3.

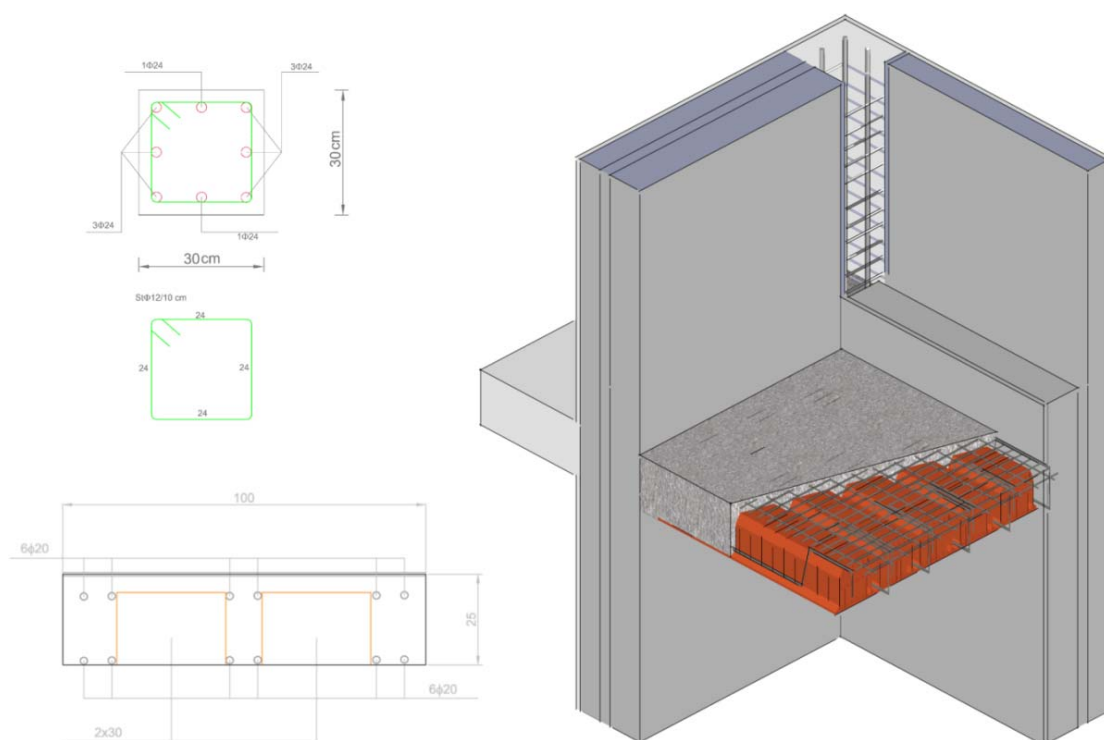
The thermal and hygrometric properties of the concrete used in the calculations have been measured through laboratory tests, while the physical properties of the other materials have been taken from the technical standards [57–59]. Six different concrete mixtures and a geopolymeric concrete have been characterized experimentally, in order to use the obtained data within the numerical model. The properties of the analyzed concrete mixtures and the other materials are reported in Tables 5 and 6, respectively.

**Table 5.** Properties of the concrete mixtures measured experimentally.

Concrete mixture	Thermal conductivity $\lambda$ (W/(m·K))	Vapor permeability $\delta \cdot 10^{12}$ (kg/(m·s·Pa))	Skeleton density $\rho$ (kg/m <sup>3</sup> )	Specific heat capacity $c$ (J/(kg·K))
C <sub>0</sub>	1.42	7.97	2094	722
C <sub>10</sub>	1.18	40.1	1914	743
C <sub>15</sub>	1.07	34.9	1835	756
C <sub>20</sub>	0.94	30.4	1762	766
C <sub>25</sub>	0.82	27.8	1661	779
C <sub>30</sub>	0.71	25.1	1518	789
G	1.01	32.8	1811	751

**Table 6.** Properties of the materials taken from the technical standards [57–59].

Material	Reference	Thermal conductivity $\lambda$ (W/(m·K))	Vapor permeability $\delta \cdot 10^{12}$ (kg/(m·s·Pa))	Density $\rho$ (kg/m <sup>3</sup> )	Specific heat capacity $c$ (J/(kg·K))	Thickness $s$ (m)
Exterior plaster	n.1 in Figure 6	1.4	9.0	2000	1000	0.02
Exterior Brick	n.2 in Figure 6	0.50	27	1400	840	0.10
Insulation	n.3 in Figure 6	0.050	5.0	15	1250	0.05
Interior Brick	n.4 in Figure 6	0.50	27	1400	840	0.15
Interior plaster	n.5 in Figure 6	0.40	18	1000	1000	0.02
Tiles	n.6 in Figure 6	1.30	9.0	2000	800	0.015
Screed	n.7 in Figure 6	Table 5	Table 5	Table 5	Table 5	0.10
Slab	n.8 in Figure 6; Figure 3	Table 5	Table 5	Table 5	Table 5	0.25
Column	Figure 3	Table 5	Table 5	Table 5	Table 5	0.30
Steel-framework	Figure 3	50	0	7500	385	Figure 3

**Figure 3.** Geometry considered in the simulations, with column and slab sections.

The concrete mixtures with percentage of recycled plastic up to 15% ( $C_0$ ,  $C_{10}$  and  $C_{15}$ ) have been used for structural (column and joists) and non-structural (screed) purposes. Instead, the concrete mixtures with percentage of recycled plastic larger than 15% ( $C_{20}$ ,  $C_{25}$  and  $C_{30}$ ) have been used only for the screed. In fact, when these mixtures have been considered in the calculations, the mixture employed for column and joints has been fixed to  $C_{15}$ . The geopolymer concrete (G) has been used for both structural and non-structural purposes.

Before presenting the results obtained by using the 3D numerical model, some considerations on thermal transmittance, periodic thermal transmittance and weight reduction for slabs employing the present innovative concrete mixtures have been reported in the following section.

### 5.1. Reduction of Thermal Transmittance, Periodic Thermal Transmittance and Weight

The authors have analyzed the thermal transmittance of the slab considered in the simulations. A typical slab presents values of this parameter around  $2.48 \text{ W}/(\text{m}^2 \cdot \text{K})$ , that is significantly larger than the values obtainable by using innovative concrete mixtures. Table 7 reports the values of the thermal transmittance and of the periodic thermal transmittance, parameters defined in the technical standards [60,61], obtained employing the different concrete mixtures in the slab reported in Figure 3. Concrete mixtures with 30% ( $C_{30}$ ) of recycled plastic can ensure about 15% and 20% reduction of thermal transmittance and periodic thermal transmittance of the slab with respect to the traditional concrete ( $C_0$ ), respectively. This reduction assumes an important role, given the limiting values imposed by the Italian ministry [40,42]. In particular, the maximum values of the thermal transmittance of vertical walls, horizontal walls and windows, reported in reference [42], depend on the climatic zones defined in reference [41]. Instead, the decree [40] imposes  $0.20 \text{ W}/(\text{m}^2 \cdot \text{K})$  as maximum permissible value of the module of the periodic thermal transmittance for all the horizontal and vertical opaque walls, that separate interior and exterior environments. Therefore, in order to respect these limits, the slab considered in the present work could be employed as roof slab only with the insertion of an insulation panel. In any case, the use of the present innovative and eco-efficient concrete mixtures would ensure up to 15% reduction of thermal transmittance and also good properties of phase shift and attenuation, obtaining up to 20% reduction of periodic thermal transmittance, as reported in Table 7, and in Figure 4.

**Table 7.** Thermal transmittance and periodic thermal transmittance of the slab reported in Figure 3.

Concrete mixture	Thermal transmittance $\text{W}/(\text{m}^2 \cdot \text{K})$	Percentage reduction (%)	Periodic thermal transmittance $\text{W}/(\text{m}^2 \cdot \text{K})$	Percentage reduction (%)
$C_0$	2.48	-	0.570	-
$C_{10}$	2.40	3.23	0.544	4.56
$C_{15}$	2.35	5.24	0.528	7.37
$C_{20}$	2.29	7.67	0.504	11.6
$C_{25}$	2.20	11.3	0.480	15.8
$C_{30}$	2.11	14.9	0.457	19.8
G	2.32	6.45	0.519	8.94

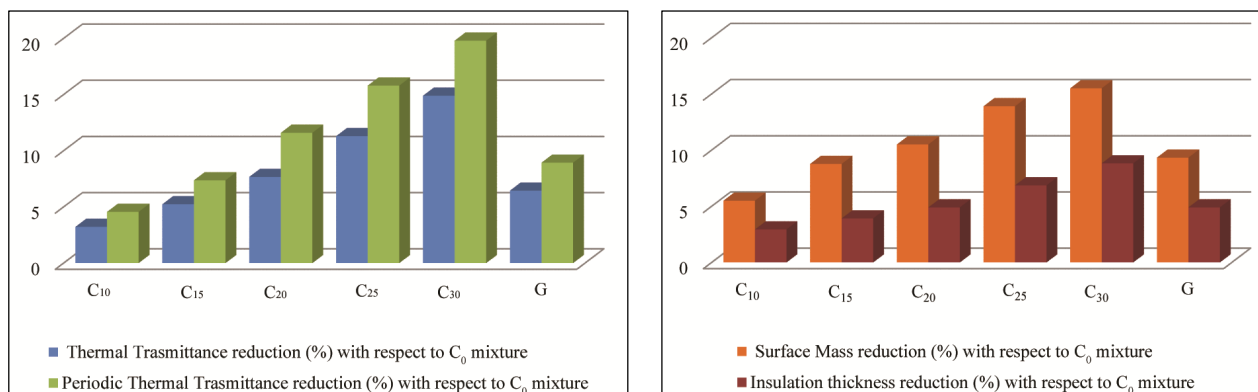
Another advantage of the present concrete mixtures is related to their reduced density, as reported in Table 5. In fact, the weight of building structures can be decreased by using the present materials, with positive effects on seismic forces and stability. The decree [42] imposes the limiting values for the thermal transmittance of roof slabs depending on the climatic zones. The authors have calculated the weight reduction of slabs that respect the limit of  $0.32 \text{ W}/(\text{m}^2 \cdot \text{K})$  imposed for climatic zone D (center Italy, *i.e.*, Rome), obtainable by using the present eco-efficient concrete mixtures. In particular,

fixing the value of the thermal transmittance to the above limit, 16% lighter structures can be obtained employing the present plastic aggregates, as reported in Table 8 and Figure 4. Besides surface mass, Table 8 and Figure 4 report the thickness of insulation material that must be employed in a slab in order to respect the limit value of thermal transmittance. About 9% reduction of insulation thickness can be achieved by using the present concrete mixtures in the slab, with consequent cost saving.

**Table 8.** Surface mass and insulation thickness of a roof slab with the thermal transmittance equal to the limit value of  $0.32 \text{ W}/(\text{m}^2 \cdot \text{K})$  for climatic zone D.

Concrete mixture	Surface mass ( $\text{kg}/\text{m}^2$ )	Percentage reduction (%)	Insulation thickness (m)	Percentage reduction (%)
C <sub>10</sub>	1185	5.50	0.099	2.94
C <sub>15</sub>	1144	8.77	0.098	3.92
C <sub>20</sub>	1123	10.5	0.097	4.90
C <sub>25</sub>	1080	13.9	0.095	6.86
C <sub>30</sub>	1060	15.5	0.093	8.82
G	1137	9.33	0.097	4.90

**Figure 4.** Percentage reductions of the quantities of interest obtainable with the present concrete mixtures.

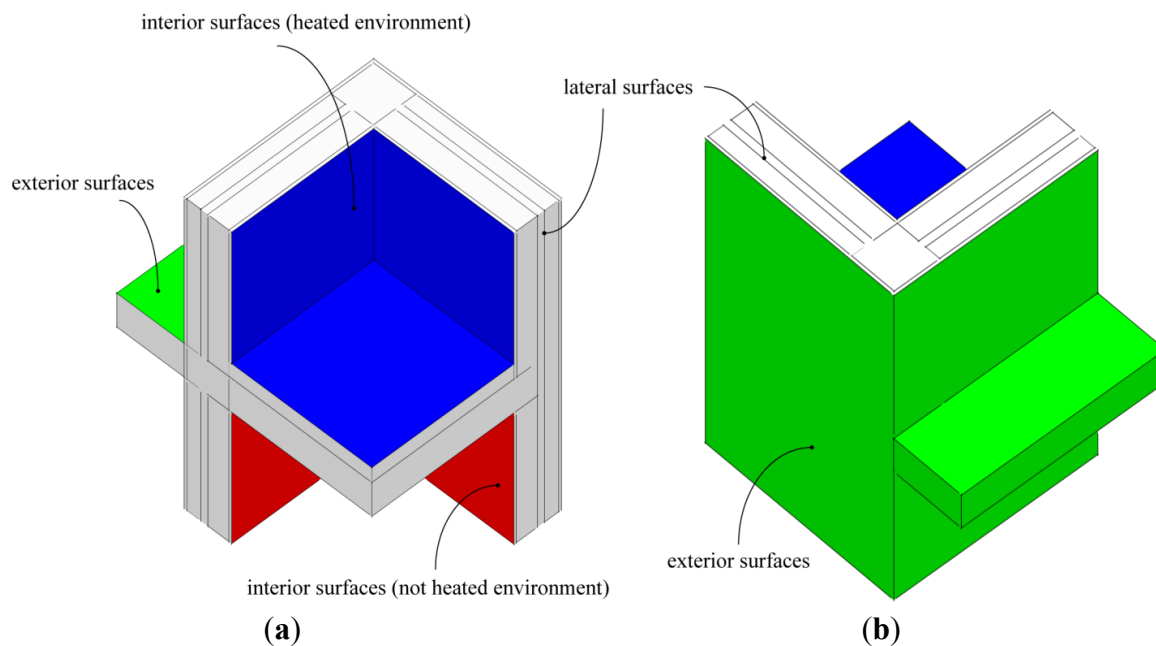


## 5.2. Dynamic Heat and Mass Transfer in a 3D Structure

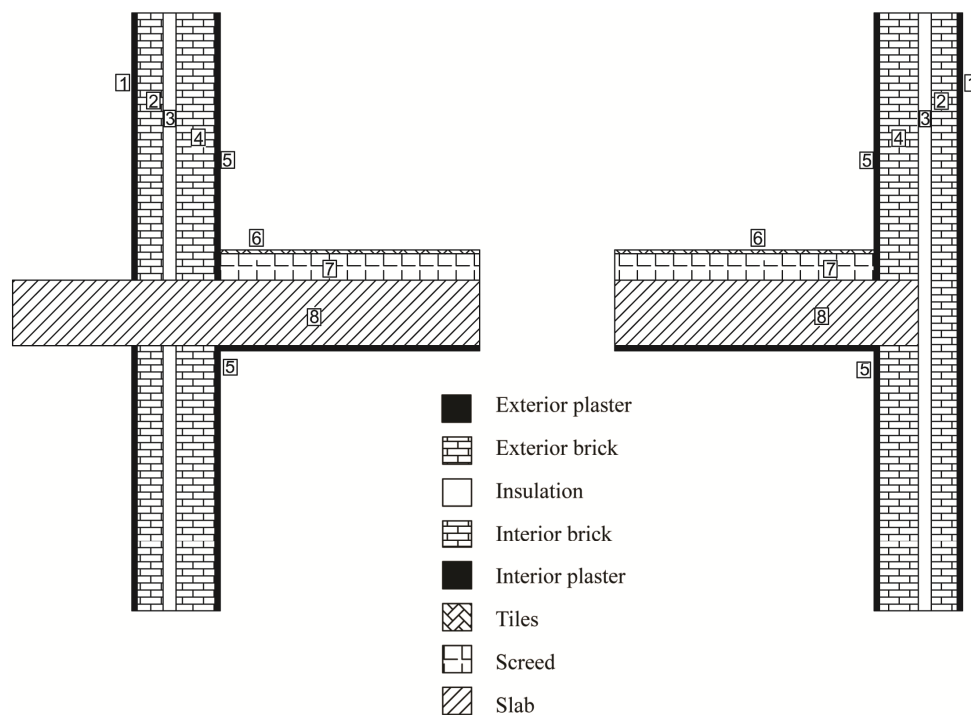
Dynamic heat conduction and vapor diffusion through the 3D building structure reported in Figure 3 have been simulated by using the Equations (1) and (2) with the boundary and initial conditions (3). As initial conditions for both dynamic heat transfer and vapor diffusion, the solution obtained from the steady state simulations has been employed. The values of time-dependent exterior temperature,  $T_{\infty,e}(\vartheta)$ , and time-dependent exterior relative humidity,  $\phi_e(\vartheta)$ , are calculated for the city of Bolzano in northern Italy on the basis of the technical standard [62], that reports the methodology to be employed for the definition of the reference year to be used to reproduce the climatic conditions. The temperature of the heated environment (reported in Figure 5) is  $20^\circ\text{C}$ , while the temperature of the not-heated environment is  $10^\circ\text{C}$ . For both these environments, the relative humidity has been taken equal to 50%. The convective heat transfer coefficients used in the simulations are  $25 \text{ W}/(\text{m}^2 \cdot \text{K})$  for the exterior environment, and  $7.7 \text{ W}/(\text{m}^2 \cdot \text{K})$  for both the heated and not-heated environments [60]. The

partial pressure of vapor has been calculated on the basis of time-dependent relative humidity and time-dependent saturation pressure of water, as  $p_v(\vartheta) = \phi(\vartheta) \cdot p_{sat}(T(\vartheta))$ . Figure 7 reports the front and rear view of the computational grid employed in the simulations, which is made of 74,771 nodes and 403,175 tetrahedral elements.

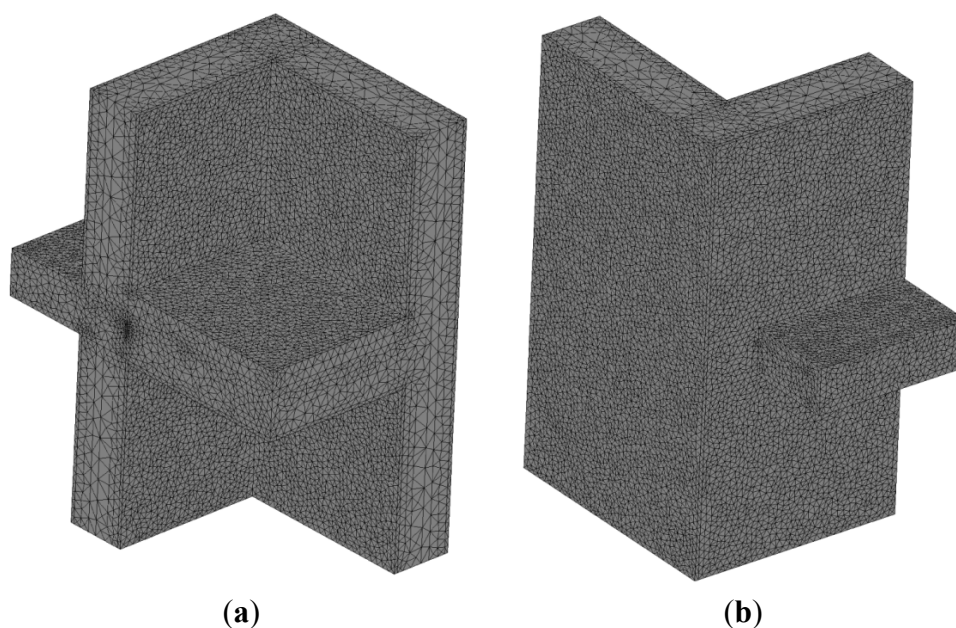
**Figure 5.** Computational domain considered: interior view (a) and exterior view (b).



**Figure 6.** Longitudinal and transverse sections of the geometry.

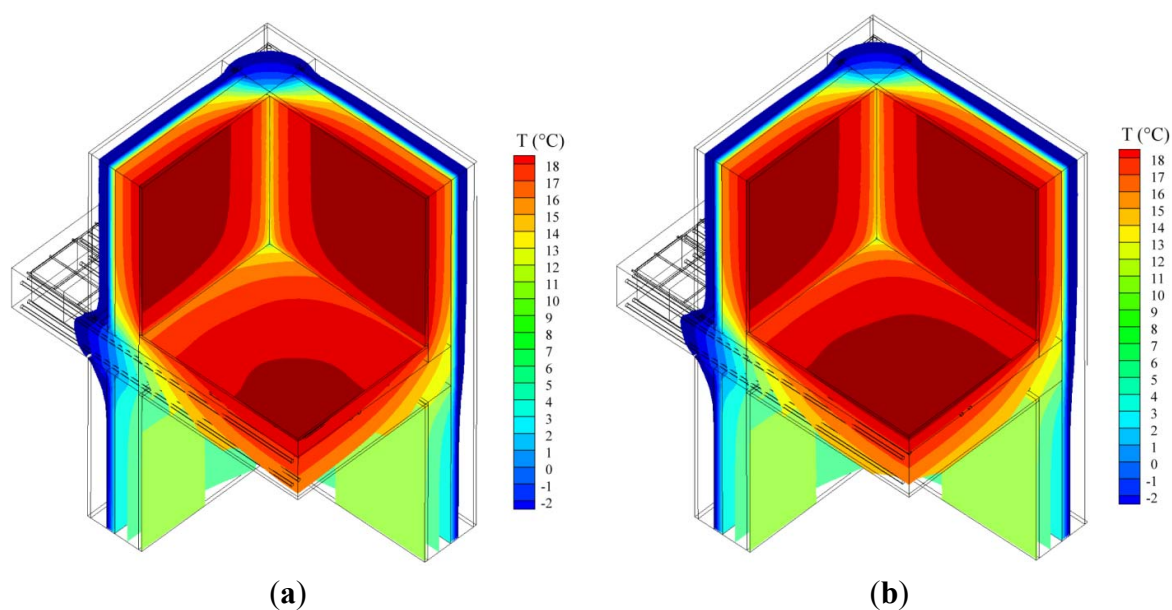


**Figure 7.** Computational grid employed (74,771 nodes and 403,175 tetrahedral elements): front view (a) and rear view (b).



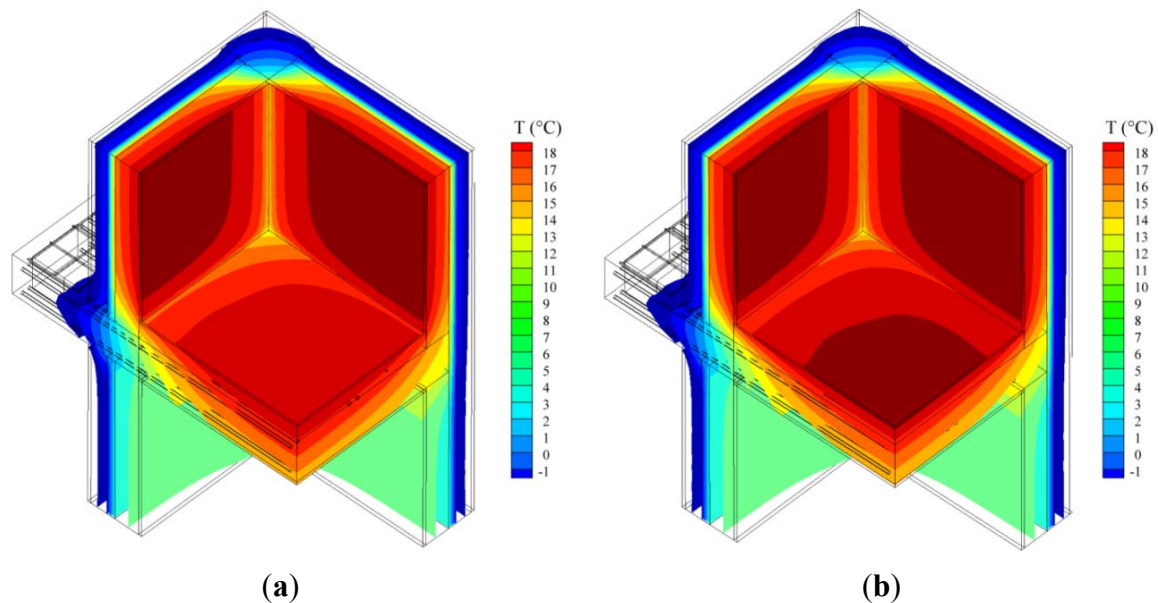
Figures 8 and 9 show the temperature contours obtained after three and seven days, respectively, employing two different concrete mixtures ( $C_0$  and  $C_{30}$ ). From the analysis of these figures, it can be noticed that the temperature distribution in the structure is significantly different when different kind of concretes are used for column, slab and screed. In particular, if the  $C_{30}$  mixture is employed in the structure, the slab is maintained at higher temperature for all the instances considered. These effects are appreciable also in correspondence of the corner between the two vertical walls, but it is less marked because of the presence of the insulation layer inside the walls.

**Figure 8.** Temperature contours obtained after three days (72 h) employing two different concrete mixtures:  $C_0$  (a) and  $C_{30}$  (b).



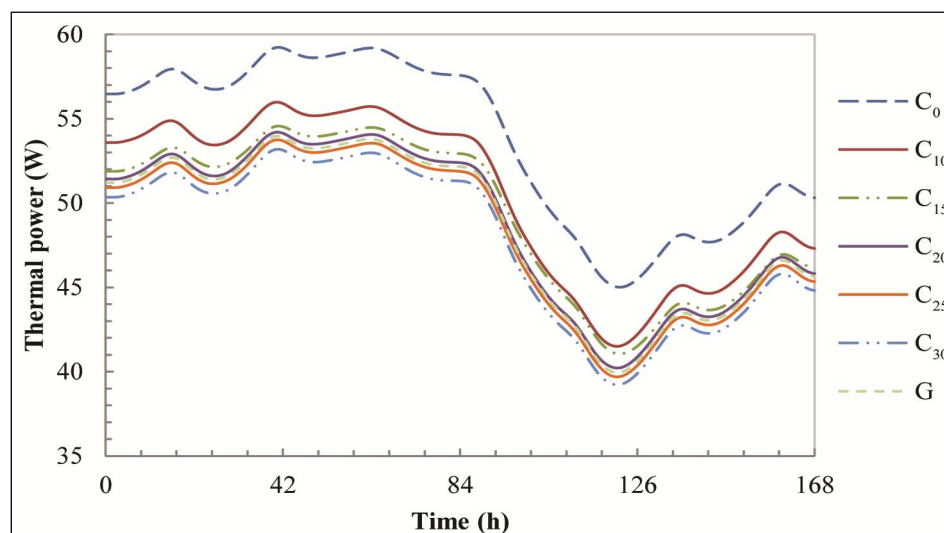


**Figure 9.** Temperature contours obtained after seven days (168 h) employing two different concrete mixtures:  $C_0$  (a) and  $C_{30}$  (b).



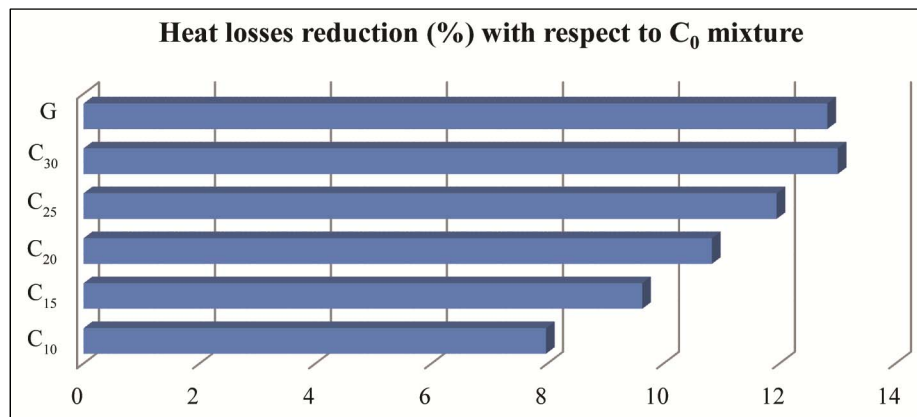
In order to analyze the reduction of heat dispersions through the structure, obtainable by employing the present eco-efficient concrete mixtures, the authors report in Figure 10 the thermal power transferred by the surfaces of the heated environment (sketched in Figure 5) during the coldest week of the year. It is evident that the use of the present innovative concretes with low thermal conductivity allows to reduce heat losses from the heated environment. The percentage reduction of thermal power, with respect to the use of the classic concrete ( $C_0$ ), is reported in Figure 11. The use of a geopolymeric concrete (G) or 30% recycled plastic aggregates ( $C_{30}$ ) allows one to obtain about a 13% reduction of heat dispersion, with consequent advantages in terms of reduced emissions and cost savings related to building heating.

**Figure 10.** Thermal power transferred from the heated environment when the present concrete mixtures are used.



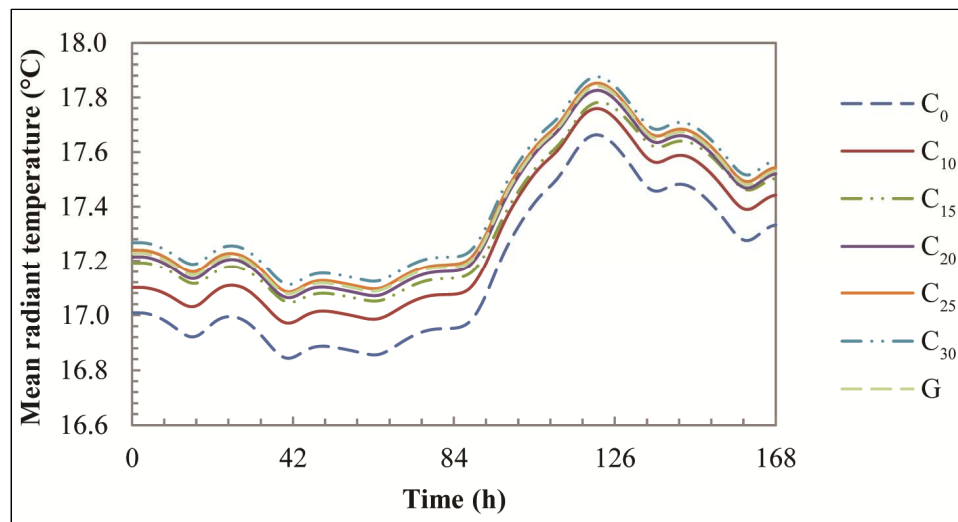


**Figure 11.** Heat losses reduction (%) obtainable by using the present concrete mixtures, with respect to  $C_0$  mixture.



The authors have calculated a parameter commonly employed to evaluate the thermo-hygrometric comfort, the mean radiant temperature, defined as the uniform temperature of the walls of the interior environment, considered as black body exchanging radiant energy with the human body, also considered as black body [63,64]. This parameter influences the radiative heat transfer between human body and the surrounding environment. Therefore, in order to ensure thermo-hygrometric comfort conditions for occupants, the value of the mean radiant temperature should be near to the temperature of the heated environment. Figure 12 reports the behavior of this parameter over time, for the different concrete mixtures considered.

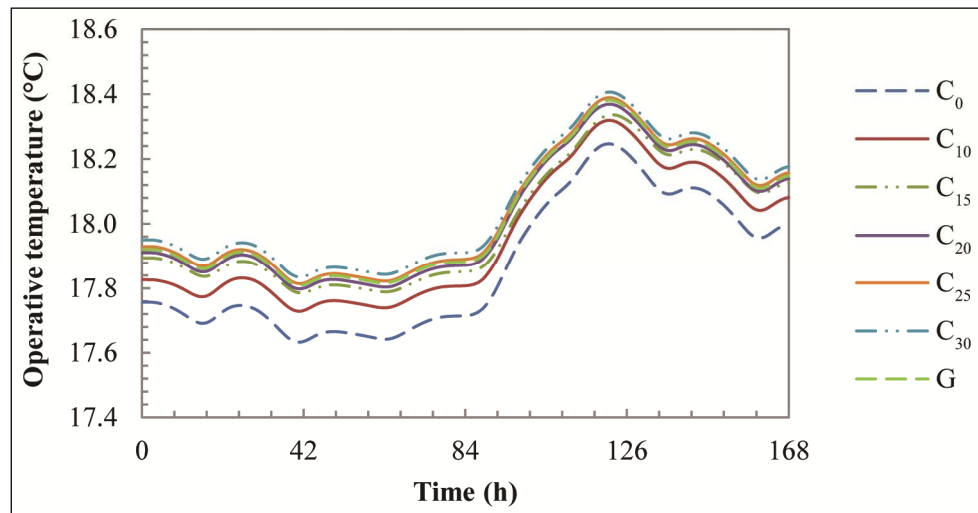
**Figure 12.** Mean radiant temperature calculated by using the different concrete mixtures.



Thanks to the higher thermal storage capacity of the present innovative concretes, the superficial temperatures assume larger values, therefore the mean radiant temperature increases, as shown in Figure 12. The thermo-hygrometric comfort also depends on air temperature inside buildings. In order to take into account both parameters, the operative temperature, defined as the uniform temperature of an enclosure in which an occupant would exchange the same amount of heat by radiation plus convection as in the existing non-uniform environment [64], is introduced. In common practice, this parameter is

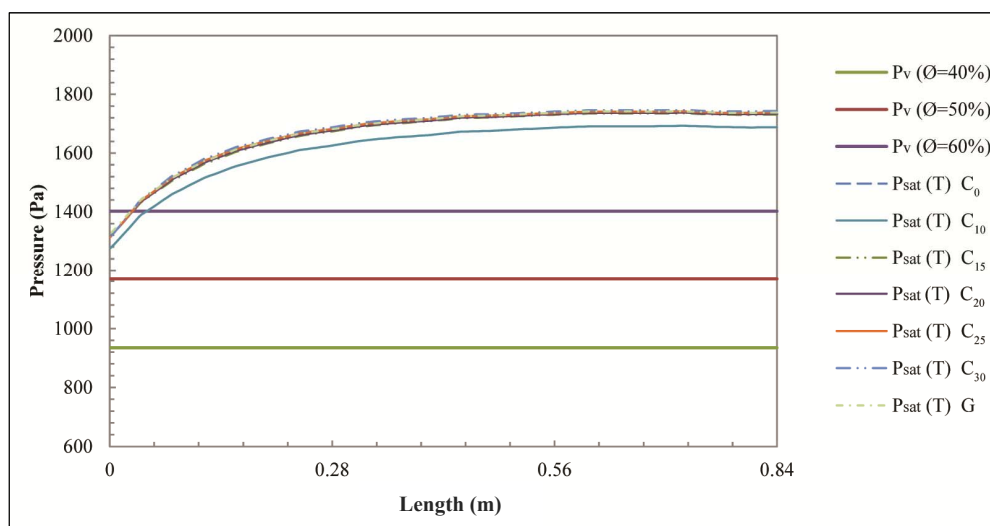
approximated to the arithmetic mean of air temperature and mean radiant temperature [63,64]. Figure 13 shows the variation over time of this parameter for the different concrete mixtures considered by the authors. Larger values of the operative temperature, obtainable by using the present eco-efficient concretes, allow one to reduce heating requirements for buildings.

**Figure 13.** Operative temperature calculated by using the different concrete mixtures.

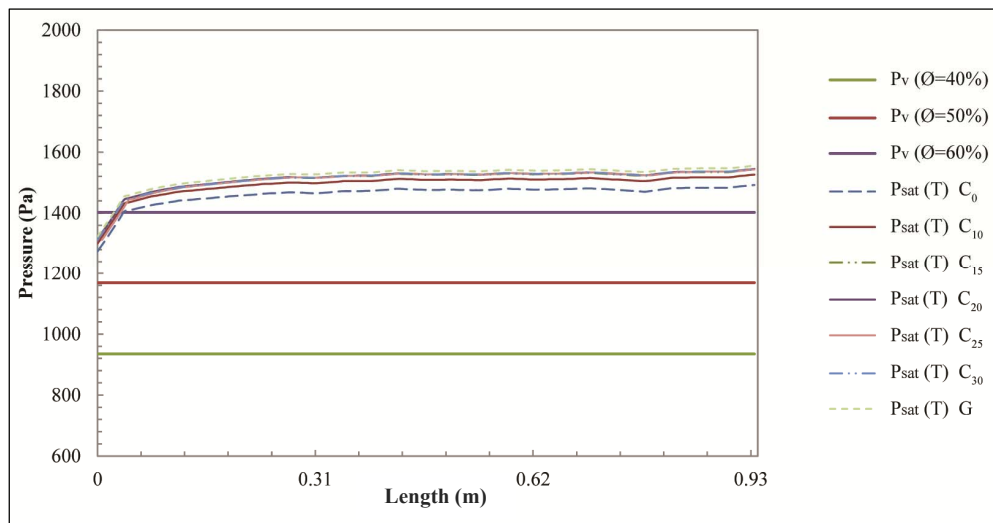


The presence of condensed water must be avoided in building structures. Therefore, the local distribution of partial pressure of vapor in critical zones of the structure, such as corners between walls or between columns and slabs, must be analyzed. Figures 14 and 15 report the values of the partial pressure of vapor and the saturation pressure of water at the end of the simulated week, calculated by using the different concretes, and for the relative humidity ranging between 40% and 60% [65], for the two corners shown in Figure 16. In the last day of the week, water condensation conditions are encountered in correspondence of the lower edge between column and slab, only if the relative humidity of the interior environment assumes the value of 60%.

**Figure 14.** Partial pressure of vapor and saturation pressure of water on the corner between wall and slab (corner “a” of Figure 16).



**Figure 15.** Partial pressure of vapor and saturation pressure of water on the corner between the two vertical walls (corner “b” of Figure 16).



**Figure 16.** Critical zones for condensation phenomena.

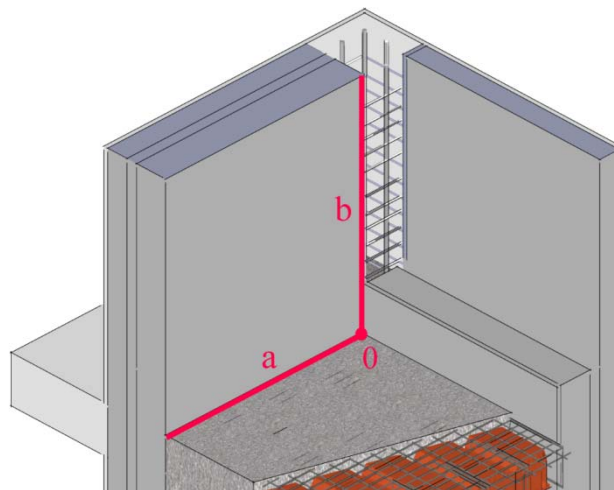
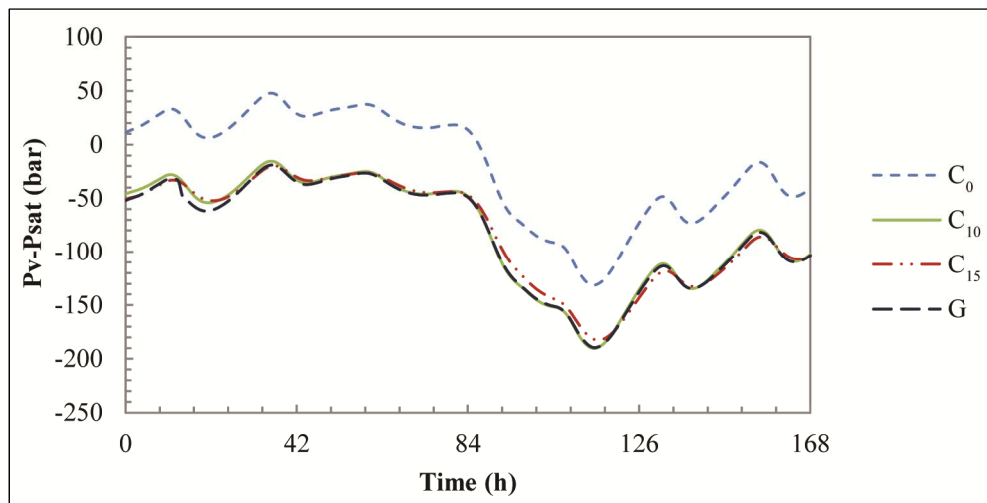


Figure 17 reports the dynamic behavior of pressure difference (partial pressure of vapor minus saturation pressure of water) calculated on the column surfaces, over the simulated week. The results for mixtures  $C_{20}$ ,  $C_{25}$  and  $C_{30}$  have not been reported since these concretes have not been used for structural purposes, as stated at the beginning of the sixth section. From the analysis of this figure, it can be noticed that interstitial condensation conditions are encountered in the first four days if concrete with natural limestone aggregates ( $C_0$ ) is used for the column. Instead, the present concrete mixtures with recycled plastic aggregates ( $C_{10}$ ,  $C_{15}$ ) and the geopolymeric concrete (G) allow one to avoid water condensation in correspondence of the column, for all the simulated days. These positive effects are due to the vapor permeability of the present innovative concretes, which is about one order of magnitude smaller than the reference concrete with limestone aggregates.

**Figure 17.** Partial pressure of vapor minus saturation pressure of water in correspondence of the column during the simulated week.



## 6. Conclusions

In this work, the authors have characterized experimentally six different concrete mixtures and a geopolymeric concrete, in order to use these data within a numerical model that reproduces dynamic conduction heat transfer and vapor diffusion in a typical building structure, characterized by a three-dimensional (3D) field of the quantities of interest. Different percentages of recycled plastic have been used as concrete aggregate, in order to analyze the effects on the thermal and hygrometric behavior of the 3D structure under investigation. These mixtures have been used for structural (column and joists) and non-structural (screed) purposes. To the authors' knowledge, a number of studies are available on the experimental characterization of concrete mixtures, but ones comparable to the present work integrating experimental activity with 3D numerical analysis of a typical building structure are not available in the literature.

The use of the properly developed geopolymeric concrete or recycled plastic aggregates for structural and non-structural applications allows to obtain about 13% reduction of heat dispersions from heated environments, with consequent advantages in terms of reduced emissions and cost savings related to building heating. The periodic thermal transmittance of a structure can be reduced of about 20% by employing the present concrete mixtures, with resulting advantages in terms of temperature oscillation reduction. The use of the present concretes in building structures can also produce positive effects in terms of thermo-hygrometric comfort, because of the larger values of mean radiant temperature and operative temperature. Furthermore, water condensation phenomena in correspondence of the column can be avoided by using the present innovative concretes for structural purposes. In general, the choice to use recycled plastic as concrete aggregate would have a positive impact on both construction and recycling sectors, with consequent increase of energetic efficiency on broad scale. Moreover, greenhouse gas emissions can be mitigated up to about 90% by using geopolymeric cement instead of Portland cement, due to the reduced energy resources needed for its manufacture.

The authors think that the coupling of experimental and numerical activity to study the present innovative and eco-efficient concrete mixtures for structural and non-structural applications in

buildings assumes an important role, in order to correctly characterize the transient behavior of 3D structures involving these new materials. The present 3D simulations together with the availability of experimental data, allowing one to obtain detailed local information in complex structures, could be integrated with the results obtained by using lumped parameter models reproducing the behavior of whole buildings.

## Conflicts of Interest

The authors declare no conflict of interest.

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