



Article

Improving Performance of Far Users in Cognitive Radio: Exploiting NOMA and Wireless Power Transfer

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Abstract: In this paper, we examine non-orthogonal multiple access (NOMA) and relay selection strategy to benefit extra advantage from traditional cognitive radio (CR) relaying systems. The most important requirement to prolong lifetime of such network is employing energy harvesting in the relay to address network with limited power constraint. In particular, we study such energy harvesting CR-NOMA using amplify-and-forward (AF) scheme to improve performance far NOMA users. To further address such problem, two schemes are investigated in term of number of selected relays. To further examine system performance, the outage performance needs to be studied for such wireless powered CR-NOMA network over Rayleigh channels. The accurate expressions for the outage probability are derived to perform outage comparison of primary network and secondary network. The analytical results show clearly that position of these nodes, transmit signal to noise ratio (SNR) and power allocation coefficients result in varying outage performance. As main observation, performance gap between primary and secondary destination is decided by both power allocation factors and selection mode of single relay or multiple relays. Numerical studies were conducted to verify our derivations.

Keywords: non-orthogonal multiple access; cognitive radio; outage probability; relay selection; throughput

1. Introduction

This is an era of explosive growth of mobile devices and broadband wireless services. It requires deployment of advanced communication techniques to meet demand of huge connections and enhance the spectral efficiency. The non-orthogonal multiple access (NOMA) and cognitive radio (CR) are considered to be two of the most effective methods to achieve spectral efficiency as in [1,2]. After the combination of both NOMA and CR definitions, the authors studied the spectrum efficiency and secrecy energy efficiency in the proposed CR-NOMA scheme as in [3]. Many other studies focus on facilitating the application of NOMA to CR and investigating the performance of CR with NOMA. In CR-NOMA, occasionally, the unlicensed secondary users (SU) can be served the same quality of service (QoS) conditions as the licensed primary users (PU). Therefore, the transfer energy distributed to the SU is limited by the immediate signal-to-interference-plus noise ratio (SINR) of the PU. This is the advantage of CR-NOMA compared to conventional CR systems. It can achieve higher spectral effect because both PU and SU can work well using the same spectrum at the same time.

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Recent studies in [4–6] have used a number of transmission systems to form energy harvesting (EH) assisted cooperative networks. In [4], the authors used relays to benefit EH in the first time in collaborative communication. In [5,6], the authors introduced numerous system models to allocate energy to power constraint devices with assuming a EH model which is defined according to time allocated for EH and the amount of harvested energy known before transmission. However, because both the energy arrival time and the amount of energy harvested are random, the predefined EH model seems unsuitable. Therefore, the authors of [7,8] introduced some transmission approaches to enable EH in networks in terms of using the general EH configurations. In particular, co-channel interference contributes to increase harvested energy for relays because more sources feed energy to dedicated device [8]. Further research on some effects in relaying network, such as imperfect channel state information or relay selection mode, is presented in [9–11].

In other trends of research, NOMA together with EH is one of the promising techniques that will help improve the number of served users who have limited power [12,13]. The important advantage of NOMA technology over traditional orthogonal multiple access (OMA) techniques is to allow multiple users to access the network simultaneously and at the same frequency by using non-orthogonal sources, such as different power levels or low density spreading codes. There have been many studies and discussions on the pros and cons of different NOMA schemes. Various NOMA system models have been applied and described. NOMA techniques have special advantages in non-orthogonality manner. They exhibit spectral efficiency, massive connectivity and low transmission latency regardless of the complexity of the interfering situation and the performance of the receiver. In [12], the implementation of NOMA in the CR transmission is examined and the performance of CR-NOMA is also described. The authors of [13] introduced NOMA based on the amplify and forward (AF) relaying procedure through Nakagami-m fading channels and it showed superiority to conventional NOMA. In [14], the collaborative EH NOMA protocol is introduced, in which the NOMA-strong users act as EH based relays to further assist the NOMA-weak users. In [15], the authors proposed closed-form expressions for total throughput and outage probability with static powers for different users as considering the uplink NOMA system.

Recent studies in [16–18] have demonstrated the superiority of the combination of CR and NOMA compared with CR with OMA for achieving a remarkable increase in spectrum efficiency. In addition, the NOMA techniques presented in [19–21] are extra solutions that contribute to improve spectrum access opportunities in CR network. We can improve the performance of SU and PU at the same time by designing a suitable cooperation model between CRs and NOMA as in [19–21]. Moreover, CRs' energy efficiency (EE) with NOMA may be higher than that of CRs with OMA as interesting work in [22]. In [23], a general optimization algorithm is presented to solve the spectrum resource optimization problem for CR NOMA. Nevertheless many challenges need to be addressed for its extensive use [24–26]. If these challenges are not fully understood and solved, spectrum efficiency of CRs may be reduced or even the designed CR may not work. For example, due to the non-orthogonal nature of NOMA, system model includes the primary source and the secondary receiving nodes following Rayleigh distribution as in [26]. In such paper, an exact closed-form of the outage probability for each secondary destination is derived. They further provided asymptotic expressions related to the outage probability [26]. Despite the extensive and individual studies, there are not much related works focused on combining EH with CR-NOMA.

In fact, integrating EH into CR-NOMA is only at an early stage. Thus, it is of great importance to understand the challenges and benefits of EH to implement green communication in such CR-NOMA. Therefore, we conducted research and analyzed the outage probability and throughput performance in such system. We directly obtained the closed-form expressions of the outage probability by studying the signal to interference and noise ratios (SINRs) at users. Up to now, no research work has focused on the EH assisted CR-NOMA scheme by exploiting performance gap between primary destination and secondary destination. In this paper, we aim to fill this open problem. From the above analysis,

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outage performance gap exists in such CR NOMA network where NOMA and relay selection strategy are applied for primary and secondary networks.

The following is a summary of the main contributions of this study:

- Reliable transmission of AF relaying scheme required in such CR-NOMA system with a common relay and EH policy was studied. This implementation of two schemes is designed to satisfy the users' condition in terms of channel quality with respect to the more reliable transmitted information. We intend to analyze the system performance of EH assisted CR-NOMA networks through the Rayleigh fading channels.
- The exact expressions of outage probability is presented and then throughput is further examined.
 From the achieved results, we analyze the effects of a number of factors including power allocation factors, transmit SNR, and the number of relays to prove the superiority of such CR NOMA model.
- As extended model, multiple relay selection in Scheme 2 is introduced in EH assisted CR NOMA to increase data rate and reliability of transmission compared to singe relay systems reported in Scheme 1. Moreover, the EH assisted CR-NOMA systems illustrate an improved performance as increasing the number of selected relays.

The remaining sections are organized as follows. Section 2 describes the system model of EH assisted CR-NOMA. Section 3 analyzes the outage probability and throughput performance with fixed power allocation factors assigned for NOMA users in Scheme 1 and Section 4 presents Scheme 2. Next, numerical results are provided in Section 5. The conclusion is presented in Section 6.

2. System Model

To begin with describing the structure of considered system, we design the EH assisted CR-NOMA network to simultaneous supply energy and information transmission. At transmit side, the primary network is designed with one primary user (PUtx) and a secondary network containing one secondary transmitter (SUtx) while *PUrx*1, *PUrx*2, and *SUrx* are considered as destinations at the receiver side (in which only *PUrx*2 is located near the relay). This paper intends to evaluate performance of distant users (*PUrx*1 and *SUrx*) as in Figure 1. We consider the case that PUtx and SUtx want to send information to relay (R) in the uplink NOMA and then R transfers the signal to the main *PUrx*1 user and the secondary user *SUrx* in the downlink NOMA. We assume *PUrx*1 is not within the transmission line of PUtx and needs a relay node to support the communication process. Assume a secondary user R plays the role of intermediate node, which is able to harvest energy to support further transmission. It can be seen that the first hop in such network is operated in the model of energy harvesting. In particular, both secondary nodes R are capable of scavenging the energy from received signals (RF bearing signal). Moreover, all nodes are the half-duplex mode and are equipped with only one antenna.

There are two phases in the operation of CR NOMA. The PUtx and SUtx transfer their information to R in Phase 1. Then, the relay node R takes advantage of the harvested power from the part of received signals from the sources to forward the obtained signals to SUrx and PUrx1 in Phase 2.

It is assumed that the main user PUtx has a fixed power supply, i.e., P_S , while there is dynamic energy supply for the relay node R and hence R needs to collect power from the received signals in Phase 1. All channels experience the quasi-static Rayleigh fading channels. Let g_1 and g_2 be the channel coefficients at first hop, while h_i , i=1,2 are channels in second hop to SUrx and PUrx1, and h_0 is channel to PUrx2. Then, we denote channel gains as $g_i \sim CN\left(0,\Omega_{gi}\right)$ and $h_i \sim CN\left(0,\Omega_{i}\right)$ for i=1,2,3.

Figure 1 shows that the energy harvesting and information transfer protocol comprises two phases. In Phase 1, the PUtx transfers the superposition signal to relay, where x_1 and x_2 are the information that BS plans to transfer to PUrx1 and SUrx, respectively. a_i , (i=1,2) is the power allocation coefficient for two far NOMA users. It is assumed that $a_1^2 + a_2^2 = 1$ and $a_1^2 > a_2^2 > 0$. We also indicate the additive white Gaussian noise (AWGN) at all users in the network are $\omega_R \sim CN(0, \sigma_R^2)$ in this paper.

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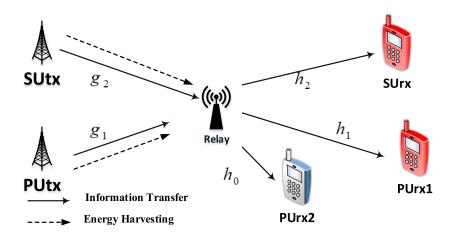


Figure 1. Scheme 1: System model of EH assisted CR-NOMA network.

In the second scenario in Figure 2, it is assumed that the k-th (k = 1, 2, ..., K) relay is selected to signal forwarding to destinations including SUrx, PUrx1, and PUrx2. Since the secondary network benefits from the sharing of licensed channel of the primary network, the user SUrx is able to receive its own signal. While the selected relay is willing to help the primary users to enhance their performance to serve both PUrx1 and PUrx2. This scheme further provides a chance to improve performance of far users by exploiting relay selection scheme. It is noted that, regarding these schemes, Schemes 1 and 2 are presented to exhibit performance gap among far users illustrated in Figures 1 and 2, respectively.

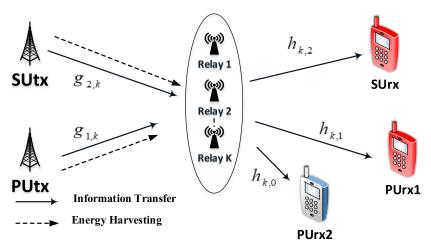


Figure 2. Scheme 2: Multiple relays in EH assisted CR-NOMA network.

We denote $g_{1,k}$, $g_{2,k}$ as channels of links PUtx to kth relay, and SUtx to kth relay, respectively, while channels from kth relay to PUrx2, PUrx1 and SUrx are $h_{k,0}$, $h_{k,1}$, $h_{k,2}$, respectively.

3. Performance Analysis in Scheme 1

3.1. Calculation of SNR

It is assumed that equal level of transmit power P_S is allocated for sources in primary and secondary network. With regard to evaluating system performance for Scheme 1 in Phase 1, the main PUtx transfers its information to relay node R following NOMA structure, and the received signal at R is given by

$$y_{R1} = \sqrt{P_S}g_1(a_1x_1 + a_2x_2) + \omega_R. \tag{1}$$

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The primary SUtx transmits its information to the relay node R following OMA scheme and such received signal in secondary link is given by

$$y_{R2} = \sqrt{P_S} g_2 x_3 + \omega_R. \tag{2}$$

The signal transmission in the system is separated into two phases. The first phase is deployed for transmission both information and energy from source to relay and relay forwards the received signal to destinations in the second phase.

Employing the method of power splitting based EH protocol [7–11], the received information can be separated into two parts by R, one for energy harvesting and another for information processing. The received signal with respect to EH at relay for primary link is given by

$$\sqrt{\lambda_1} y_{R1} = \sqrt{P_s \lambda_1} g_1 \left(a_1 x_1 + a_2 x_2 \right) + \sqrt{\lambda_1} \omega_R. \tag{3}$$

Here, $0 < \lambda_1 < 1$ is the part of information splitting for EH of R for two considered links. It is important that R takes advantage of all the collected power to forward the received signal to PUrx1 and SUrx yielding $\lambda_1 = 0$ or $\lambda_1 = 1$. Therefore, the transmitted power of the relay node for primary link and secondary link can be calculated, respectively, as

$$P_{R1} = \eta \lambda_1 P_S |g_1|^2 \tag{4}$$

and

$$P_{R2} = \eta \lambda_1 P_S |g_2|^2. \tag{5}$$

Here, $0 \le \eta \le 1$ indicates the energy conversion efficiency. In Phase 2, the relay node R then forwards $\sqrt{1-\lambda_1}y_R$ together with the secondary information x_2 based on the AF scheme and the superposition coding. The relay node harvests total power of $P_R = P_{R1} + P_{R2}$ and then R can split its power into two parts: $P_R = \lambda_3 P_R + (1-\lambda_3) P_R$. More specifically, $\lambda_3 P_R$ is used to forward the main information transmitted from PUtx to the primary destination PUrx1 and PUrx2, while $(1-\lambda_3) P_R$ is used to transfer the secondary information to the secondary destination SUrx.

The power amplify factor G_i of relay is given by

$$G_{i} = \frac{1}{\sqrt{(1 - \lambda_{1}) \left(P_{S}|g_{i}|^{2} + \sigma_{R}^{2}\right) + \sigma_{b1}^{2}}}$$

$$\approx \frac{1}{\sqrt{(1 - \lambda_{1}) \left(P_{S}|g_{i}|^{2}\right)^{2}}},$$
(6)

where the approximation is tight at high SNR.

The received signal at the relay node R for primary link and secondary link are given by

$$x_{R1} = G_1 \sqrt{\lambda_3 P_R} \left(\sqrt{1 - \lambda_1} y_{R1} + \omega_{b1} \right) \tag{7}$$

and

$$x_{R2} = G_2 \sqrt{(1 - \lambda_3) P_R} \left(\sqrt{1 - \lambda_1} y_{R2} + \omega_{b1} \right),$$
 (8)

where all signals are considered as the unit-power transmitted information. $\omega_{b1} \sim CN\left(0, \sigma_{b1}^2\right)$ denotes the white Gaussian noise demonstrated by the signal conversion from passband to baseband at R.

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In this step, the received signal at user *PUrx*1 and *SUrx* can be expressed, respectively, as

$$y_{PUrx1} = h_1 x_{R1} + n_3$$

$$= \sqrt{(1 - \lambda_1) \lambda_3 P_R P_S} G_1 g_1 h_1 a_1 x_1 + \sqrt{(1 - \lambda_1) \lambda_3 P_R P_S} G_1 g_1 h_1 a_2 x_2$$

$$+ \sqrt{(1 - \lambda_1) \lambda_3 P_R} G_1 h_1 n_R + \sqrt{\lambda_3 P_R} h_1 G_1 n_{b1} + n_3,$$
(9)

$$y_{SUrx} = h_2 x_{R2} + n_3 = \sqrt{(1 - \lambda_1)(1 - \lambda_3)} P_R P_S G_2 g_2 h_2 a_1 x_3 + \sqrt{(1 - \lambda_1)(1 - \lambda_3)} P_R G_2 h_2 n_R + \sqrt{(1 - \lambda_3)} P_R h_2 G_2 n_{b1} + n_3,$$
 (10)

where $n_3 \sim CN(0, \sigma_3^2)$ denotes the additive noise at PUrx1 and SUrx. The primary user PUrx1 tries to recover from y_{PUrx1} in the existence of the interference from the PUrx2. The signal-to-interference-plus-noise ratio (SINR) of PUrx1 to detect x_1 is thus given by

$$\gamma_{x1} = \frac{\eta \lambda_1 \lambda_3 P_S |g_1|^2 |h_1|^2 a_1^2}{\eta \lambda_1 \lambda_3 |h_1|^2 \left(P_S |g_1|^2 a_2^2 + \sigma_R^2\right) + \frac{\eta \lambda_1 \lambda_3}{(1 - \lambda_1)} |h_1|^2 \sigma_{b1}^2 + \sigma_3^2}.$$
(11)

After performing successive interference cancellation (SIC) applied in the NOMA, system decodes the signal x_2 of user PUrx2. Regarding OMA, x_2 is decoded at the SUrx via expected SINR as

$$\gamma_{x3} = \frac{\eta \lambda_1 \lambda_3 P_S |g_2|^2 |h_2|^2}{\eta \lambda_1 \lambda_3 |h_2|^2 \sigma_{b1}^2 + \frac{\eta \lambda_1 \lambda_3}{(1 - \lambda_1)} |h_2|^2 \sigma_{b1}^2 + \sigma_3^2}.$$
 (12)

Consequently, the data rates gained at the primary user *PUrx*1 and the secondary user *SUrx* can be expressed, respectively, by

$$\tau_{PUrx1} = \frac{1}{2}\log_2(1+\gamma_{x1}),$$
(13)

and

$$\tau_{SUrx} = \frac{1}{2} \log_2 (1 + \gamma_{x3}).$$
(14)

3.2. Outage and Throughput Performance Analysis

This section provides an analysis of the outage probability and throughput in delay-limited mode for *PUrx*1 and *SUrx*. In addition, an investigation is conducted about harvested energy for power transfer at the secondary user.

There is an outage event if the data rates of PUrx1 and SUrx are lower than the given target rates. Thus, the outage probability for a given target rate R_j , j = PUrx1, SUrx are computed by

$$OP_{out}^{j}(\tau_{j} < R_{j}) = OP_{out}^{j}(\gamma_{j} < \varepsilon_{j}).$$
 (15)

Here, we use $\varepsilon_j = 2^{2R_j} - 1$. To further proceed system performance analysis, we have the following propositions.

Proposition 1. The outage probability for the primary user PUrx1 in the cognitive relay network is then expressed by

• If
$$\varepsilon_{PUrx1} \ge \frac{l_D}{m_D}$$

$$OP_{out}^{PUrx1} = 1. \tag{16}$$

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• If $\varepsilon_{PUrx1} < \frac{l_D}{m_D}$

$$OP_{out}^{PUrx1} = \Pr\left(\gamma_{x1} < \varepsilon_{D}\right)$$

$$= 1 - \exp\left(-\frac{\varepsilon_{PUrx1}k_{D}}{\Omega_{g1}\left(l_{D} - m_{D}\varepsilon_{PUrx1}\right)}\right)\sqrt{\frac{4\varepsilon_{PUrx1}}{\Omega_{1}\Omega_{g1}\left(l_{D} - m_{D}\varepsilon_{D}\right)}}K_{1}\left(\frac{4\varepsilon_{PUrx1}}{\Omega_{1}\Omega_{g1}\left(l_{D} - m_{D}\varepsilon_{PUrx1}\right)}\right), \quad (17)$$

where $l_D=\frac{\eta\lambda_1\lambda_3P_Sa_1^2}{\sigma^2}$, $m_D=\frac{\eta\lambda_1\lambda_3P_Sa_2^2}{\sigma^2}$, $k_D=\eta\lambda_1\lambda_3\left(1+\frac{1}{(1-\lambda_1)}\right)$. K_1 (.) is the modified Bessel function of the second kind with first order defined in [27].

Proof. See Appendix A. \square

Proposition 2. The outage probability of the secondary user SUrx in OMA mode can be expressed as

• If
$$|g_2|^2 < \frac{\varepsilon_{SUrx1}k_C}{l_C}$$

$$OP_{out}^{SUrx} = 1. \tag{18}$$

• If $|g_2|^2 > \frac{\varepsilon_{SUrx1}k_C}{l_C}$

$$OP_{out}^{SUrx} = \Pr\left(\gamma_{x3} < \varepsilon_{SUrx1}\right)$$

$$= 1 - \exp\left(-\frac{\varepsilon_{SUrx1}k_C}{l_C\Omega_{g2}}\right) \sqrt{\frac{4\varepsilon_{SUrx1}}{\Omega_{g2}\Omega_{g2}l_C}} K_1\left(\sqrt{\frac{4\varepsilon_{SUrx1}}{\Omega_{g2}\Omega_{g2}l_C}}\right),$$
(19)

where
$$l_c = \frac{\eta \lambda_1 \lambda_3 P_S}{\sigma^2}$$
, $k_c = \eta \lambda_1 (1 - \lambda_3) \left(1 + \frac{1}{1 - \lambda_1} \right)$.

Proof. Similar derivations can be found in Appendix A. Therefore, it can be omitted it here. \Box

3.3. Consideration on Overall Performance in Terms of Outage Behavior and Throughput

In this paper, we only examine performance of far users who are under poor channel condition, then the overall outage probability can be formulated by

$$OP_{out,I} = 1 - \left(1 - OP_{out,I}^{PUrx1}\right) \left(1 - OP_{out,I}^{SUrx}\right). \tag{20}$$

Therefore, it can be obtained partial throughput at PUrx1 and SUrx for scheme I as

$$\psi_{j,I} = \left(1 - OP_{out,I}^{j}\right) R_{j} \frac{(1 - \lambda_{3}) T/2}{T} = \frac{\left(1 - OP_{out,I}^{j}\right) R_{j} (1 - \lambda_{3})}{2}, j = (PUrx1, SUrx). \tag{21}$$

In this case, the overall throughput performance can be further written by

$$\psi_{\text{System }I} = \psi_{\text{PIIrx1}I} + \psi_{\text{SIIrx}I}. \tag{22}$$

4. Performance Analysis in Scheme 2

In Phase 1, the main PUtx transfers its information to the relay node. The received signal can be calculated in secondary link as

$$y_{R1,k} = \sqrt{P_S} g_{1,k} (a_1 x_1 + a_2 x_2) + \omega_R, \tag{23}$$

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and the primary SUtx transmits its information to the relay node and received signal at relay for secondary link is given by

$$y_{R2,k} = \sqrt{P_S} g_{2,k} (a_1 x_3 + a_2 x_4) + \omega_R.$$
 (24)

It is thus assumed that $\sigma^2 = \sigma_{b1}^2 = \sigma_{b1}^2 = \sigma_3^2$. The SINR of *PUrx*1 to detect x_1 is then formulated by

$$\gamma_{x1,k} = \frac{\eta \lambda_1 \lambda_3 P_S |g_{1,k}|^2 |h_{k,1}|^2 a_1^2}{\eta \lambda_1 \lambda_3 |h_{k,1}|^2 (P_S |g_{1,k}|^2 a_2^2 + \sigma^2) + \frac{\eta \lambda_1 \lambda_3}{(1 - \lambda_1)} |h_{k,1}|^2 \sigma^2 + \sigma^2}.$$
 (25)

Similarly, the SINR need be calculated to decode the signal x_3 of user SUrx as

$$\gamma_{x3,k} = \frac{\eta \lambda_1 \lambda_3 P_S |g_{2,k}|^2 |h_{k,2}|^2}{\eta \lambda_1 \lambda_3 |h_{k,2}|^2 \sigma^2 + \frac{\eta \lambda_1 \lambda_3}{(1-\lambda_1)} |h_{k,2}|^2 \sigma^2 + \sigma^2}.$$
 (26)

The selected relay index and its respective SNR are given as [28]

$$k* = arg \max_{k=1,\dots,K} (\gamma_{ii,k}), ii = x1, x3.$$
 (27)

Proposition 3. The outage probability for the primary user PUrx1 in the EH-enabled CR-NOMA is then expressed by

• If
$$\varepsilon_{PUrx1} \ge \frac{l_D}{m_D}$$

$$OP_{out,II}^{PUrx1} = 1. \tag{28}$$

• If $\varepsilon_{PUrx1} < \frac{l_D}{m_D}$

$$OP_{out,II}^{PUrx1,k} = 1 - \sum_{k=1}^{K} {K \choose k} (-1)^{k-1} \exp\left(-\frac{k\varepsilon_{PUrx1}k_{D}}{\Omega_{g1,k} (l_{D} - \varepsilon_{PUrx1}m_{D})}\right) \times \sqrt{\frac{4k\varepsilon_{PUrx1}}{\Omega_{k,1}\Omega_{g1,k} (l_{D} - \varepsilon_{PUrx1}m_{D})}} K_{1} \left(\frac{4k\varepsilon_{PUrx1}}{\Omega_{k,1}\Omega_{g1,k} (l_{D} - \varepsilon_{PUrx1}m_{D})}\right).$$

$$(29)$$

Proof. See in Appendix B. \square

Proposition 4. The outage probability of the secondary user SUrx in NOMA mode can be expressed in two cases as

• If
$$|g_{2,k}|^2 < \frac{\varepsilon_{SUrx}k_C}{l_C}$$

$$OP_{out,II}^{SUrx,k} = 1.$$
(30)

• If $|g_{2,k}|^2 > \frac{\varepsilon_{SUrx}k_C}{l_C}$

$$OP_{out,II}^{SUrx,k} = \Pr\left(\gamma_{x3,k} < \varepsilon_{SUrx}\right)$$

$$= 1 - \sum_{k=1}^{K} {K \choose i} (-1)^{k-1} \exp\left(-\frac{k\varepsilon_{SUrx}k_{C}}{l_{C}\Omega_{g2,k}}\right) \sqrt{\frac{4k\varepsilon_{SUrx}}{\Omega_{g2,k}\Omega_{2,k}l_{C}}} K_{1}\left(\sqrt{\frac{4k\varepsilon_{SUrx}}{\Omega_{g2,k}\Omega_{2,k}l_{C}}}\right). \tag{31}$$

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Proof. It can be recalled such outage event as

$$OP_{out,II}^{SUrx,k} = \Pr\left(\gamma_{x3,k*} < \varepsilon_{SUrx}\right)$$

$$= 1 - \Pr\left(\frac{\frac{\eta \lambda_{1} \lambda_{3} P_{S} a_{2}^{2}}{\sigma^{2}} \left|g_{2,k*}\right|^{2} \left|h_{k*,2}\right|^{2}}{\eta \lambda_{1} \lambda_{3} \left(1 + \frac{1}{(1 - \lambda_{1})}\right) \left|h_{k*,2}\right|^{2} + 1} \ge \varepsilon_{SUrx}\right)$$

$$= 1 - \Pr\left(\left|g_{2,k*}\right|^{2} \ge \frac{\varepsilon_{SUrx} k_{C} \left|h_{k*,2}\right|^{2} + \varepsilon_{SUrx}}{l_{C} \left|h_{k*,2}\right|^{2}}\right).$$
(32)

Using characterizations of probability of random variables, it can be rewritten as

$$OP_{out,II}^{SUrx,k} = 1 - \int_{0}^{\infty} \left[\sum_{k=1}^{K} {K \choose k} (-1)^{k-1} \exp\left(-\frac{\varepsilon_{SUrx}kk_{C}x + k\varepsilon_{SUrx}}{l_{C}\Omega_{g2,k}x}\right) \right] \frac{1}{\Omega_{k,2}} \exp\left(-\frac{x}{\Omega_{k,2}}\right) dx$$

$$= 1 - \frac{1}{\Omega_{k,2}} \sum_{k=1}^{K} {K \choose k} (-1)^{k-1} \exp\left(-\frac{\varepsilon_{SUrx}kk_{C}}{l_{C}\Omega_{g2,k}}\right) \int_{0}^{\infty} \exp\left(-\frac{k\varepsilon_{SUrx}}{l_{C}\Omega_{g2,k}x} - \frac{x}{\Omega_{k,2}}\right) dx \quad (33)$$

$$= 1 - \sum_{k=1}^{K} {K \choose k} (-1)^{k-1} \exp\left(-\frac{\varepsilon_{SUrx}kk_{C}}{l_{C}\Omega_{g2,k}}\right) \sqrt{\frac{4k\varepsilon_{SUrx}}{l_{C}\Omega_{g2,k}\Omega_{k,2}}} K_{1} \left(\frac{4k\varepsilon_{SUrx}}{l_{C}\Omega_{g2,k}\Omega_{k,2}}\right).$$

The proof is completed. \Box

The overall outage performance in Scheme 2 can be given as

$$OP_{out,II}^{k} = 1 - \left(1 - OP_{out,II}^{PUrx1,k}\right) \left(1 - OP_{out,II}^{SUrx,k}\right). \tag{34}$$

From Propositions 3 and 4, the outage probability at both PUrx1 and SUrx can be achieved. We concentrate on throughput for both primary network and secondary in this paper, i.e., ψ_j^k . $(1 - \lambda_3) T/2$ is time constant and where T (second) is time epoch to transmit signal from source to destination. Therefore, it can be obtained partial throughput at PUrx1 and SUrx as

$$\psi_{j,II}^{k} = \left(1 - OP_{out,II}^{j,k}\right) R_{j} \frac{\left(1 - \lambda_{3}\right) T/2}{T} = \frac{\left(1 - OP_{out,II}^{j,k}\right) R_{j} \left(1 - \lambda_{3}\right)}{2}, j = (PUrx1, SUrx). \tag{35}$$

In this regard, the overall throughput is computed by

$$\psi_{system,II}^k = \psi_{PUrx1,II}^k + \psi_{SUrx,II}^k. \tag{36}$$

5. Simulation Results

Numerical results were examined to compare the performance of primary/secondary network obtained by using these considered schemes. The outage behavior of the proposed EH assisted CR NOMA was also evaluated in the simulations. The simulation settings were based on similar parameters as in [13,14]; the common parameters related to average channel gains were $\Omega_{g1}=\Omega_{g2}=\Omega_1=\Omega_2=1, \lambda_1=\lambda_3=0.1$, and power efficiency was $\eta=1$. All channels are assumed to be Rayleigh flat fading. In following figures, we denote "ana." to illustrate for simulations corresponding to mathematical results, "System ana." indicates overall system performance, and "sim." stands for Monte-Carlo simulation.

In Figure 3, we illustrate outage probability of primary and secondary networks. We set $d_1 = 1/2$ as distance from PUtx/SUtx to relay, $d_2 = 1 - d_1$ as distance from relay to PUrx1, $d_3 = 1/4$ as distance from relay to SUrx, and $\lambda_1 = \lambda_3 = 0.1$. It can be seen clearly that higher SNR leads to enhanced outage performance. Furthermore, higher acquired requirement on target rates results in the worse outage performance of both main users. This phenomenon can be explained as follows: target rates limit

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outage performance, as confirmed by Equation (15). Figure 3 indicated that higher data rates threshold is main reason to decreasing outage performance. Changing power allocation factors results in outage performance gap, as shown in Figure 4. This situation can be clarified as follows: higher value a_1 contributes to worse SINR and hence degraded outage performance occurred.

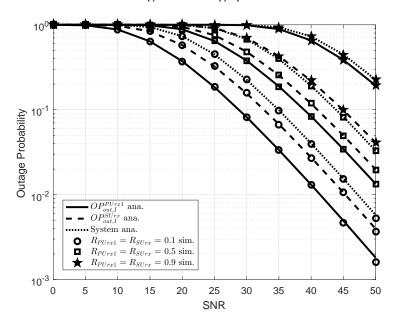


Figure 3. Scheme 1: Outage performance of *PUrx*1 and *SUrx* versus transmit SNR at source when $R_{PUrx1} = R_{SUrx}$ ($a_1 = 0.85$, $\eta = 1$).

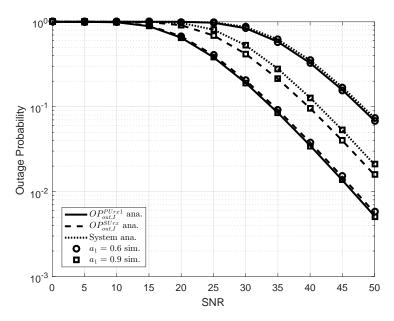


Figure 4. Scheme 1: PUrx1 and SUrx and overall outage of system comparison with respect to varying both SNR and a_1 ($R_{PUrx1} = R_{SUrx} = 0.3$).

In Figure 5, we highlight different trend of PUrx1 and SUrx as varying a_1^2 . In this simulation, we set $d_1=1/2$ as distance from PUtx to relay, $d_2=1-d_1$ as distance from relay to PUrx1, $d_3=1/4$ as distance from relay to SUrx, $\lambda_1=\lambda_3=0.1$, and $R_{PUrx1}=R_{SUrx}=0.5$. It can be observed clearly that different trends in term of outage behavior for PUrx1 and SUrx can be raised. The lower outage performance can be seen at PUrx1 as increasing a_1^2 from 0.2 to 0.9 and the opposite trend can be raised for SUrx. The main reason is that a_1^2 is contained in the expressions of SINR and such value make

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direct impact of SINR and then outage performance will be changed. Interestingly, overall outage system is certainly at middle point of considered range of a_1^2 . This situation can be explained by a_1^2 must be satisfied fairness between SU and PU.

Figure 6 shows similar trend of outage performance in three values of target rate $R_{PUrx1} = R_{SUrx} = 0.1, 0.5, 0.9$. In this case, we set $R_{PUrx1} = R_{SUrx}$ ($a_1 = 0.85, \eta = 1, K = 2$). It is worth noting that outage performance of PUrx1, k is worst case as $R_{PUrx1} = R_{SUrx} = 0.9$ and it leads to worse overall performance as well. Figure 7 illustrates impact of power allocation factors on outage performance. The similar performance of Scheme 2 can be achieved in such figure. In this case, we set $d_3 = 1/4$ as the distance from relay to SUrx, and $R_{PUrx1} = R_{SUrx} = 0.3, K = 2$.

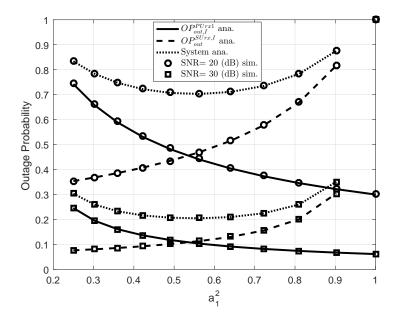


Figure 5. Scheme 1: Outage performance of *PUrx*1 and *SUrx* under changing of a_1^2 and SNR ($R_{PUrx1} = R_{SUrx} = 0.1$).

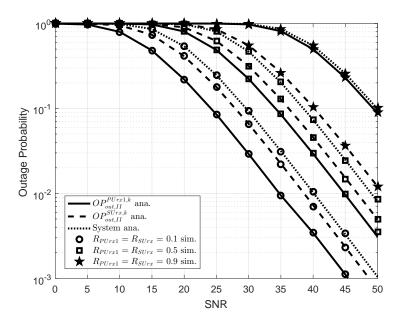


Figure 6. Scheme 2: Outage comparison of PUrx1 and SUrx versus SNR.

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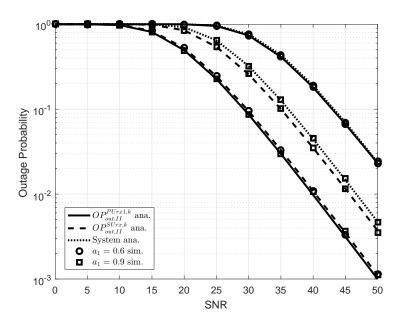


Figure 7. Scheme 2: Outage performance of PUrx1 and SUrx versus SNR as varying a_1 .

Figure 8 also indicates similar performance of Scheme 2 under varying power allocation factor a_1 . Especially, more relays contribute to improve outage performance of Scheme 2, as shown in Figure 9, i.e., K = 3 is the better one. The simulation parameters in Figure 9 are $a_1 = 0.85$, $R_{PUrx1} = R_{SUrx} = 0.1$.

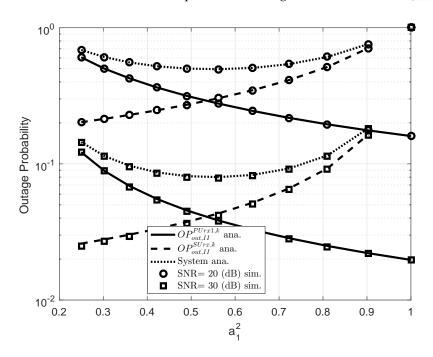


Figure 8. Scheme 2: Performance of *PUrx*1 and *SUrx* with a_1 as varying SNR ($R_{PUrx1} = R_{SUrx} = 0.1$, K = 2).

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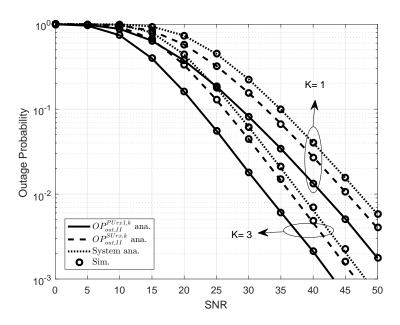


Figure 9. Scheme 2: Impact of *K* on outage comparison of *PUrx*1 and *SUrx* versus SNR.

It can be confirmed that Scheme 2 exhibits the best performance corresponding to K=3 considering outage performance and throughput, as shown in Figures 10 and 11. In these case, we set $a_1=0.85$, $R_{PUrx1}=R_{SUrx}=0.1$. Regarding the comparison scenario shown in Figure 10, the related parameters of model in [14] were aligned as $a_1=0.85$, R=0.1, $\Omega_1=\Omega_2=1$, $\alpha=\beta=0.1$, $\eta=1$, $d=d_1=2$, and m=3. It can be observed that outage performance in the proposed two schemes is better than exact outage reported in [14].

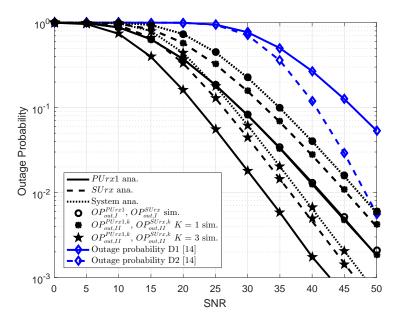


Figure 10. Comparison of two schemes and work in [14] in terms of outage performance.

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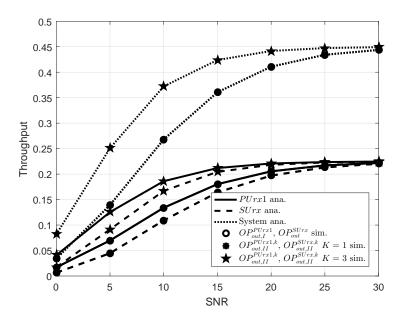


Figure 11. Scheme 2: Throughput performance of Schemes 1 and 2 versus SNR (K = 1,3 for Scheme 2).

6. Conclusions

This study investigated a new spectrum efficiency as deploy EH in such CR-NOMA. In this model, both the primary and the secondary receivers who are located far way benefit from EH based relay. Such wireless powered relay intends to serve both primary and secondary networks. To examine the performance of EH-enabled CR-NOMA, expressions for the outage probability and throughput for each user and the entire NOMA network were analyzed. In addition, we demonstrated that the effect of transmit SNR, power allocation factors, and target rates are main factors affecting on performance of EH assisted CR-NOMA. In future work, multiple users of the such CR-NOMA model should be studied.

Author Contributions: D.-T.D. designed the algorithm, performed the theoretical analysis, checked the results and wrote the manuscript. M.-S.V.N. implemented the simulation and contributed to the manuscript preparation. M.V. was responsible for formulating the research issues, and revised the paper.

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Appendix A. Proof of Proposition 1

Based on Equation (10), the outage probability for the primary user *PUrx*1 in the EH-enabled CR-NOMA can be obtained as follows

$$OP_{out,I}^{PUrx1} = \Pr\left(\gamma_{x1} < \varepsilon_{PUrx1}\right)$$

$$= 1 - \Pr\left(\frac{l_D|g_1|^2|h_1|^2}{m_D|g_1|^2|h_1|^2 + k_D|h_1|^2 + 1} \ge \varepsilon_{PUrx1}\right)$$

$$= 1 - \Pr\left(|g_1|^2 \ge \frac{\varepsilon_{PUrx1}\left(k_D|h_1|^2 + 1\right)}{(l_D - \varepsilon_{PUrx1}m_D)|h_1|^2}\right).$$
(A1)

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Such outage event must be constrained by $\varepsilon_{PUrx1} < \frac{l_D}{m_D}$, and then $OP_{out,I}^{PUrx1}$ can be expressed by

$$OP_{out,I}^{PUrx1} = 1 - \int_{0}^{\infty} \exp\left(-\frac{\varepsilon_{PUrx1} (k_{D}x + 1)}{(l_{D} - \varepsilon_{PUrx1} m_{D}) x\Omega_{g1}}\right) \frac{1}{\Omega_{1}} \exp\left(-\frac{x}{\Omega_{1}}\right) dx$$

$$= 1 - \frac{1}{\Omega_{1}} \exp\left(-\frac{\varepsilon_{PUrx1} k_{D}}{\Omega_{g1} (l_{D} - \varepsilon_{PUrx1} m_{D})}\right) \int_{0}^{\infty} \exp\left(-\frac{\varepsilon_{PUrx1}}{\Omega_{g1} (l_{D} - \varepsilon_{PUrx1} m_{D}) x} - \frac{x}{\Omega_{1}}\right) dx$$
(A2)

To calculate the above integral, we put new variable as $t=\Omega_{g1}\left(l_D-\varepsilon_{PUrx1}m_D\right)x\to x=\frac{t}{\Omega_{g1}\left(l_D-\varepsilon_{PUrx1}m_D\right)}$, and then it can be expressed by

$$OP_{out,I}^{PUrx1} = 1 - \frac{1}{\Omega_{1}\Omega_{g1} (l_{D} - \varepsilon_{PUrx1}m_{D})} \exp\left(-\frac{\varepsilon_{PUrx1}k_{D}}{\Omega_{g1} (l_{D} - \varepsilon_{PUrx1}m_{D})}\right) \times \int_{0}^{\infty} \exp\left(-\frac{\varepsilon_{PUrx1}}{t} - \frac{t}{\Omega_{1}\Omega_{g1} (l_{D} - \varepsilon_{PUrx1}m_{D})}\right) dt$$
(A3)

Note that Equation (A3) can be calculated by applying $\int_0^\infty \exp\left(-\frac{\beta}{4x} - \gamma x\right) dx = \sqrt{\frac{\beta}{\gamma}} K_1\left(\sqrt{\beta\gamma}\right)$ in ([27], Equation (3.324)), and then we have Equation (16).

This completes the proof.

Appendix B. Proof of Proposition 3

By definition, we have such outage probability as

$$OP_{out,II}^{PUrx1,k} = \Pr\left(\gamma_{x1,k*} < \varepsilon_{D}\right)$$

$$= 1 - \Pr\left(\frac{l_{D}|g_{1,k*}|^{2}|h_{k*,1}|^{2}}{m_{D}|g_{1,k*}|^{2}|h_{k*,1}|^{2} + k_{D}|h_{k*,1}|^{2} + 1} \ge \varepsilon_{D}\right)$$

$$= 1 - \Pr\left(|g_{1,k*}|^{2} \ge \frac{\varepsilon_{D}\left(k_{D}|h_{k*,1}|^{2} + 1\right)}{(l_{D} - \varepsilon_{D}m_{D})|h_{k*,1}|^{2}}\right)$$
(A4)

In this case, the cumulative distribution function (CDF) related to selected channel are given respectively by [28]

$$F_{\left|g_{i,k^*}\right|^2}(x) = 1 - \sum_{k=1}^K \binom{K}{k} (-1)^{k-1} \exp\left(-\frac{kx}{\lambda_g}\right).$$
 (A5)

By using partial integration and the CDF of $\left|g_{i,k^*}\right|^2$, $OP_{out,II}^{PUrx1,k}$ is formulated as

$$OP_{out,II}^{PUrx1,k} = 1 - \int_{0}^{\infty} \left[1 - F_{|g_{1,k*}|^{2}} \left(\frac{\varepsilon_{D} (k_{D}x + 1)}{(l_{D} - \varepsilon_{D}m_{D}) x} \right) \right] f_{|h_{k*,1}|^{2}}(x) dx$$

$$= 1 - \int_{0}^{\infty} \left[\sum_{k=1}^{K} {K \choose i} (-1)^{k-1} \exp\left(-\frac{k\varepsilon_{D} (k_{D}x + 1)}{(l_{D} - \varepsilon_{D}m_{D}) \Omega_{g1,k}x} \right) \right] \frac{1}{\Omega_{k,1}} \exp\left(-\frac{x}{\Omega_{k,1}} \right) dx$$
(A6)

It can be rewritten as

$$OP_{out,II}^{PUrx1,k} = 1 - \frac{1}{\Omega_{k,1}} \sum_{k=1}^{K} {K \choose i} (-1)^{k-1} \exp\left(-\frac{k\varepsilon_{PUrx1}k_D}{\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D)}\right)$$

$$\times \int_{0}^{\infty} \exp\left(-\frac{k\varepsilon_{PUrx1}}{\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D) x} - \frac{x}{\Omega_{k,1}}\right) dx.$$
(A7)

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Let us change new variables as $t=\Omega_{g1,k}\left(l_D-\varepsilon_{PUrx1}m_D\right)x\to x=\frac{t}{\Omega_{g1,k}\left(l_D-\varepsilon_{PUrx1}m_D\right)}$ Hence, $OP_{out,II}^{PUrx1,k}$ can be formulated as below

$$OP_{out,II}^{PUrx1,k} = 1 - \frac{1}{\Omega_{k,1}\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D)} \sum_{k=1}^{K} {K \choose k} (-1)^{k-1} \exp\left(-\frac{k\varepsilon_{PUrx1}k_D}{\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D)}\right)$$

$$\int_{0}^{\infty} \exp\left(-\frac{k\varepsilon_{PUrx1}}{t} - \frac{t}{\Omega_{k,1}\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D)}\right) dt$$

$$= 1 - \sum_{k=1}^{K} {K \choose k} (-1)^{k-1} \exp\left(-\frac{k\varepsilon_{PUrx1}k_D}{\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D)}\right)$$

$$\times \sqrt{\frac{4k\varepsilon_{PUrx1}}{\Omega_{k,1}\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D)}} K_1 \left(\frac{4k\varepsilon_{PUrx1}}{\Omega_{k,1}\Omega_{g1,k} (l_D - \varepsilon_{PUrx1}m_D)}\right). \tag{A8}$$

This completes the proof.

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