



Investigation of a Resonant dc–dc Converter for Light Rail Transportation Applications

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Article

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Abstract: A high efficiency dc–dc converter is studied for light rail transportation applications on DC microgrid systems. The adopted structure includes two series-connected resonant circuits with single isolated transformer from input 750 V to output 48 V. Two half-bridge resonant circuits and one voltage balance capacitor are used to reduce voltage rating of active devices and to realize split voltages balance. Two series resonant circuits are connected with input-series by single transformer to reduce primary root-mean-square currents. Therefore, power devices with low voltage rating are selected in studied circuit to reduce power loss on sower devices and transformer winding of the isolated transformer. Frequency control approach is adopted to adjust load voltage under different voltage condition and current variations. Since the equivalent resonant tank of the studied circuit is activated under inductive load, active devices are easily operated at zero-voltage switching over wide voltage and current operation range. The feasibility of the studied circuit has been verified with a 1 kW prototype.

Keywords: resonant circuit; zero-voltage switching; light rail transportation

1. Introduction

Renewable clean energy sources, wind energy, and solar photovoltaic (PV) energy, have been developed and researched to produce the clean energy to overcome the exhaustion of fossil fuels and electric vehicles and hybrid electric vehicles are developing to reduce environmental pollution and climbing temperature issues. Direct current (dc) microgrid systems have developed in order to incorporate energy storage systems, PV power, wind power, utility systems, local residential homes, and industrial factories with a common dc voltage. The dc bus voltage on the dc microgrid system can be 1500, 750, or 380 V for traction system, light rail transit, or residential building applications. Power transformers are widely employed to provide electrical isolation and voltage conversion levels. However, line frequency transformer [1,2] has a bulky size especially at traction and light rail applications. A high-performance dc-dc converter with high frequency and galvanic isolation is demanded as the interface between dc bus voltage and output voltage in light rail transportation vehicles. To prevent using low frequency transformer in traction and light rail applications, one possible solution is the transformerless converters [3–6] with series-parallel combination to reduce semiconductor blocking-voltage capability and current rating. The high frequency transformers are used in transformerless topologies to achieve electrical insulation demand. Conventional full-bridge dc-dc circuits use the insulated gate bipolar transistors (IGBT) devices with 1200 V voltage rating for high input voltage applications. Three-level converters [7–9] based on high frequency Metal-Oxide-Semiconductor Field-Effect Transistor (MOSFET) power semiconductors were widely used in modern power converters to overcome low frequency problem of IGBT-based full-bridge converters. Soft switching dc-dc converters [10-13] have been studied and presented to realize high efficiency power circuits. Phase-shift duty-cycle controls have been successfully used in

full-bridge dc-dc converters to have the benefits of no switching loss at heavy load and low switching losses at light load. However, the low circuit efficiency and high circulating current loss at light load are the main disadvantages. Half-bridge resonant converters have the benefits of no switching loss for all power active devices and low reverse recovery loss for fast recovery diodes. However, half-bridge resonant converters are difficult to apply in high voltage input products. Full-bridge multilevel resonant circuit [13] was proposed to lessen voltage rating of power semiconductors and realize high efficiency converter. However, the control strategy is very difficult to implement using the general commercial integrated circuit with cost issue.

This paper studies a cascade resonant dc–dc circuit with a transformer for dc transportation vehicles. Due to series connection of two resonant circuits at input side, power semiconductors with low blocking-voltage and low turn-on resistance MOSFETs instead of Insulated Gate Bipolar Transistors (IGBTs) can be adopted to decrease conduction losses and lessen voltage rating of power active devices. Two half-bridge circuits are controlled with frequency modulation. The adopted series-connected resonant converter is operated under inductive load. Therefore, power active devices can be easily turned on under zero-voltage and fast recovery diodes are turned off under zero-current without reverse recovery current loss. Two half-bridge resonant circuits use the sane isolated transformer to lessen primary root-mean-square currents and conduction losses on active devices. The circuit schematic and system analysis are discussed in Section 2. The converter characteristics in steady state, design procedure and test results are discussed and presented in Section 3, followed by the conclusions.

2. Proposed Circuit and System Operation

The simplified circuit blocks in a dc microgrid system are shown in Figure 1 to combine clean energy sources, energy storage systems, utility systems, residential loads, and industrial applications. Ac–dc converters with bidirectional power flow are adopted between utility power and dc microgrid. Bidirectional dc–dc converter is adopted between dc microgrid and energy/power storage systems. For residential or commercial loads, unidirectional dc–dc converter or dc to ac converter is adopted to supply low dc voltage output or ac voltage output. The dc bus voltage in dc microgrid systems supplies 1500 V or 750 V for dc transportation systems and 380 V for local residential houses and industry factories. This study focused on dc-dc power converters for light rail transit systems. The dc microgrid for light rail applications is shown in Figure 2a. The input voltage 750 V_{dc} is supplied from dc microgrid to conductor rail for power demand in each transportation vehicle. The simplified circuit diagrams of the distributed power in conventional transportation vehicles and trams. A dc- ac inverter is first used to convert input dc voltage into three-phase ac voltage. Second, an ac-dc converter converts ac voltage into low dc voltage for auxiliary power demand and an ac-dc-ac converter is adopted for ac motor drive. Figure 2c shows the distributed power in the studied light rail transportation system. In this system, a dc–dc converter is directly converting 750 V voltage to supply auxiliary power in transportation vehicles. The dc-ac converters are adopted to drive AC motor and air and refrigerant compressors. In this way, the ac–dc converters are not necessary.

The circuit schematic of the developed converter for auxiliary circuit in light rail transportation system is given in Figure 3. Two half-bridge circuits by input-series output-parallel connected transformer is used in the studied converter. Since two resonant circuits are series connection, the voltage rating of power devices $Q_1 \sim Q_4$ is reduced. The low turn-on resistance and high frequency operation of power semiconductors such as MOSFETs are selected to decrease conduction losses and reduce converter size. A voltage balance capacitor C_f is adopted in order to balance V_{C1} and V_{C2} . The resonant tanks (L_{r1} , C_{r1} , and L_{m1}) and (L_{r2} , C_{r2} , and L_{m2}) are resonant to help power active devices with zero-voltage switching and fast recovery diodes with zero-current switching. Thus, the power losses are reduced in the studied circuit. The driving signals of half-bridge circuits are based on frequency modulation to adjust AC voltage gain and to operate at inductive load. Figure 4 illustrates the main current and voltage signals in the studied circuit. The converter operation are based on the assumptions: (1) output capacitors C_{o1} and C_{o2} are larger enough to treat as the constant voltages; (2) $Q_1 \sim Q_4$, D_1 and D_2 are all ideal; (3) $C_{r1} = C_{r2}$, $L_{r1} = L_{r2}$, and $L_{m1} = L_{m2}$; (4) $V_{C1} = V_{C2}$; and (5) the resonant tanks are operated at inductive load. Figure 5 demonstrates the topological circuits according to the conducting states of power devices under f_{sw} (switching frequency) $< f_r$ (series resonant frequency). If $f_{sw} > f_r$, then only modes 1, 3, 4, and 6 are operated in this region.

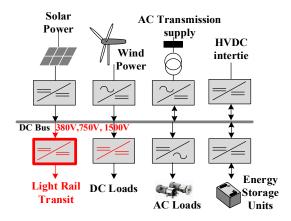


Figure 1. Simplified circuit schematic of a dc microgrid system.

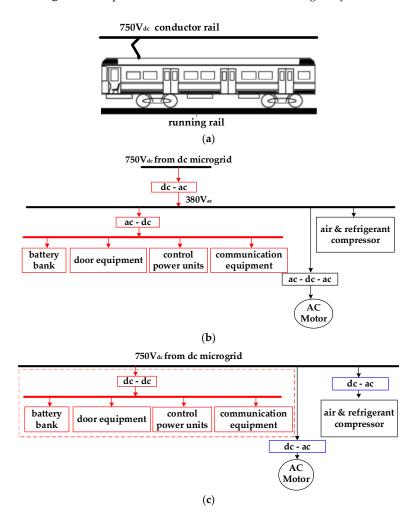


Figure 2. Basic blocks of light rail transportation vehicle (**a**) light rail vehicle; (**b**) distributed power in conventional vehicle; (**c**) distributed power in the studied case.

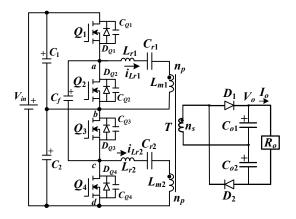


Figure 3. Proposed circuit schematic.

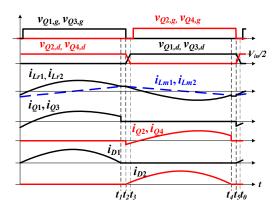


Figure 4. Basic circuit waveforms of the studied cascade resonant dc-dc converter.

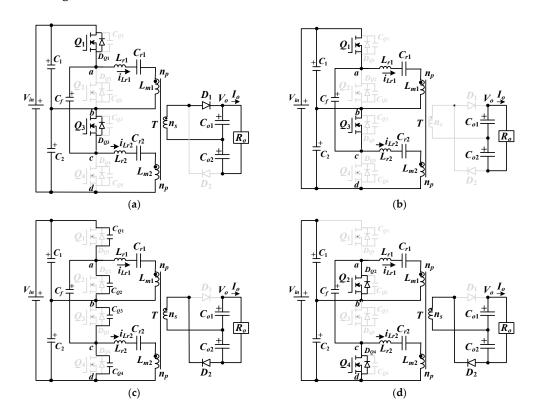


Figure 5. Cont.

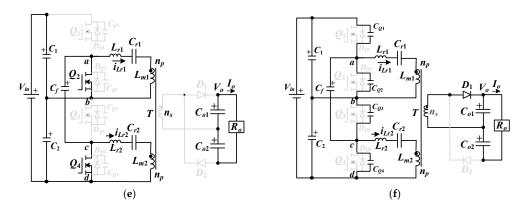


Figure 5. Equivalent circuits (a) mode 1; (b) mode 2; (c) mode 3; (d) mode 4; (e) mode 5; (f) mode 6.

Mode 1 [$t_0 \sim t_1$]: The voltages of C_{Q1} and C_{Q3} are reduced to zero at t_0 . Then, the body diodes D_{Q1} and D_{Q3} conduct. Thus, Q_1 and Q_3 can be turned on to achieve zero voltage. In mode 1, Q_1 , Q_3 , and D_1 conduct and $V_{C1} = V_{Cf}$. The primary voltages $v_{ns} = V_{Co1} = V_0/2$ and the primary voltages $v_{np} = (n_p/n_s)V_0/2 = nV_0/2$. Therefore, the slope of the magnetizing currents, di_{Lm1}/dt and di_{Lm2}/dt , increases with $nV_0/(2L_m)$, where $L_m = L_{m1} = L_{m2}$. The relationships of the primary currents and the secondary current are $n(i_{Lr1} + i_{Lr2} - i_{Lm1} - i_{Lm2}) = i_{D1}$. Since $C_{r1} = C_{r2}$, $L_{r1} = L_{r2}$, $L_{m1} = L_{m2}$ and $V_{C1} = V_{C2}$, it can obtain $i_{Lm1} = i_{Lm2}$ and $i_{Lr1} = i_{Lr2} = i_{D1}/(2n) + i_{Lm}$. In this mode, (L_{r1} and C_{r1}) and (L_{r2} and C_{r2}) are resonant with $C_r = C_{r1} = C_{r2}$ and $L_r = L_{r2}$.

$$v_{Cr1}(t) = v_{Cr2}(t) = v_{Cr}(t) = [V_{in}/2 - nV_o/2][1 - \cos\omega_r(t - t_0)] + v_{Cr}(t_0)\cos\omega_r(t - t_0) + i_{Lr}(t_0)Z_r\sin\omega_r(t - t_0)$$
(1)

$$i_{Lr1}(t) = i_{Lr2}(t) = i_{Lr}(t) = \frac{[V_{in}/2 - nV_o/2 - v_{Cr}(t_0)]\sin\omega_r(t - t_0)}{Z_r} + i_{Lr}(t_0)\cos\omega_r(t - t_0)$$
(2)

where $f_r = 1/2\pi\sqrt{L_rC_r}$, $Z_r = \sqrt{L_r/C_r}$, $v_{Cr} = v_{Cr1} = v_{Cr2}$ and $i_{Lr} = i_{Lr1} = i_{Lr2}$. When the magnetizing currents i_{Lm1} and i_{Lm2} increase and equal i_{Lr1} and i_{Lr2} at time t_1 . Diode D_1 becomes reverse biased.

Mode 2 $[t_1 \sim t_2]$: At t_1 , $i_{D1} = 0$ and D_1 is reverse biased. i_{Lr1} flows through C_1 , Q_1 , L_{r1} , C_{r1} , and L_{m1} , and i_{Lr2} flows through C_2 , Q_3 , L_{r2} , C_{r2} , and L_{m2} . Since $C_1 \gg C_{r1}$ and $C_2 \gg C_{r2}$, L_{r1} , C_{r1} and L_{m1} are resonant, and L_{r2} , C_{r2} , and L_{m2} are resonant.

$$v_{Cr1}(t) = v_{Cr2}(t) = v_{Cr}(t) = V_{in} [1 - \cos \omega_p (t - t_1)] / 2 + v_{Cr}(t_1) \cos \omega_p (t - t_1) + i_{Lr}(t_1) Z_p \sin \omega_p (t - t_1)$$
(3)

$$i_{Lr1}(t) = i_{Lr2}(t) = i_{Lr}(t) = \frac{[V_{in}/2 - v_{Cr}(t_1)]\sin\omega_p(t - t_1)}{Z_p} + i_{Lr}(t_1)\cos\omega_p(t - t_1)$$
(4)

where $Z_p = \sqrt{(L_m + L_r)/C_r}$ and $\omega_p = 1/\sqrt{(L_m + L_r)C_r}$.

Mode 3 [$t_2 \sim t_3$]: At t_3 , active devices Q_1 and Q_3 turn off. $i_{Lr1}(t_2)$ will charge C_{Q1} and discharge C_{Q2} , and $i_{Lr1}(t_2)$ will charge C_{Q3} and discharge C_{Q4} . During this time interval, D_2 conducts and $v_{Lm1} = v_{Lm2} = -nV_0/2$. Since $C_{Q1} \sim C_{Q4}$ are so small, the time interval is neglected and i_{Lr1} and i_{Lr2} are considered constant.

Mode 4 [$t_3 \sim t_4$]: This mode starts at t_3 if $v_{CQ1} = v_{C1}$, $v_{CQ3} = v_{C2}$ and $v_{CQ2} = v_{CQ4} = 0$. Due to $i_{Lr1}(t_3) > 0$ and $i_{Lr2}(t_3) > 0$, D_{Q2} and D_{Q4} conduct. Therefore, active devices Q_2 and Q_4 turn on after t_3 to have the characteristic of zero voltage turn-on operation. In this mode, $v_{Cf} = V_{C2}$. Since D_2 is forward biased, $v_{Lm1} = v_{Lm2} = -nV_0/2$ so that i_{Lm1} and i_{Lm2} decreases. v_{Cr1} , v_{Cr2} , i_{Lr1} , and i_{Lr2} in mode 4 are calculated in (5) and (6).

$$v_{Cr1}(t) = v_{Cr2}(t) = v_{Cr}(t) = nV_o[1 - \cos\omega_r(t - t_3)] + v_{Cr}(t_3)\cos\omega_r(t - t_3) + i_{Lr}(t_3)Z_r\sin\omega_r(t - t_3)$$
(5)

$$i_{Lr1}(t) = i_{Lr2}(t) = i_{Lr}(t) = \frac{[nV_o - v_{Cr}(t_3)]\sin\omega_r(t - t_3)}{Z_r} + i_{Lr}(t_3)\cos\omega_r(t - t_3)$$
(6)

When $i_{Lm1} = i_{Lr1}$ and $i_{Lr2} = i_{Lm2}$ at time t_4 . Diode D_2 is reverse biased.

Mode 5 [$t_4 \le t < t_5$]: After t_4 , D_2 is reverse biased and $v_{Cf} = V_{C2}$. i_{Lr1} flows through Q_2 , L_{r1} , C_{r1} , and L_{m1} , and i_{Lr2} flows through Q_4 , L_{r2} , C_{r2} ; L_{m2} . L_{r1} , C_{r1} , and L_{m1} are resonant; and L_{r2} , C_{r2} , and L_{m2} are resonant.

Mode 6 [$t_5 \le t < t_0$]: Q_2 and Q_4 turn off at time t_5 . $i_{Lr1}(t_5)$ will charge C_{Q2} and discharge C_{Q1} , and $i_{Lr1}(t_5)$ will charge C_{Q4} and discharge C_{Q3} . Since D_1 is forward biased, $v_{Lm1} = v_{Lm2} = nV_o/2$. At t_0 , $v_{CQ1} = v_{CQ3} = 0$.

3. Circuit Characteristics, Design Example, and Test Results

If active devices Q_1 and Q_3 conduct as shown in Figure 6a, it obtains $v_{Cf} = V_{C1}$. If V_{C1} is greater (or less) than V_{C2} , then C_1 will charge (or discharge) C_f via active devices Q_1 and Q_3 . In a similar way, v_{Cf} is equal to V_{C2} if active devices Q_2 and Q_4 conduct as shown in Figure 6b. If V_{C1} is greater (or less) then V_{C2} , C_f will charge (or discharge) C_2 via active devices Q_2 and Q_4 . Therefore, V_{C1} and V_{C2} are controlled to be balanced at $V_{in}/2$. Fundamental frequency analysis is selected to analyze the transfer function of the studied circuit. The primary inductor voltages $v_{Lm1} = v_{Lm2} = nV_o/2$. According to fundamental harmonic frequency analysis, the equivalent ac resistance is calculated in (7).

$$R_{ac} = R_{ac,1} = R_{ac,2} = \frac{4n^2}{\pi^2} R_o \tag{7}$$

Based on the voltage divider of the resonant tank by C_{r1} , L_{r1} , L_{m1} , and R_{ac1} , the voltage gain of the resonant circuit is calculated in (8).

$$|G_{ac}(f)| = \frac{1}{\sqrt{\left[1 + \frac{1}{m}\left(1 - \frac{f_r^2}{f_{sw}^2}\right)\right]^2 + Q^2 \left(\frac{f_{sw}}{f_r} - \frac{f_r}{f_{sw}}\right)^2}}$$
(8)

where $m = L_m/L_r$ and $Q = \sqrt{L_r/C_r}/R_{ac}$.

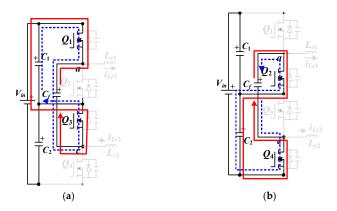


Figure 6. Voltage-balancing by flying capacitor (a) Q1 and Q3 on (b) Q2 and Q4 on.

The electrical specifications of the proposed circuit in a laboratory prototype are: $V_{in} = 750 \text{ V} \sim 800 \text{ V}$, $V_o = 48 \text{ V}$, $I_{o,max} = 21 \text{ A}$, and series resonant frequency $f_r = 100 \text{ kHz}$. The unity DC gain of resonant circuit is designed at $V_{in} = 800 \text{ V}$. The turn-ratio of *T* is expressed in (9).

$$n = \frac{V_{in,\max}}{2V_o} = \frac{800}{2 \times 48} \approx 8.33$$
 (9)

The magnetic core TDK EER-42 (TDK Corporation, Tokyo, Japan) with $A_e = 1.94 \text{ cm}^2$ is selected for transformer with $n_p = 25$ turns and $n_s = 3$ turns. Then the maximum DC voltage gain at $V_{in} = 750 \text{ V}$ is obtained in (10). Energies 2018, 11, 1078

$$G_{dc,\max} = \frac{2nV_o}{V_{in,\min}} = \frac{2 \times 8.33 \times 48}{750} \approx 1.066$$
(10)

From (7), R_{ac} under full load is derived in (11).

$$R_{ac} = \frac{4n^2}{\pi^2} R_{o,rated} = \frac{4 \times 8.33^2}{\pi^2} \times \frac{48}{21} \approx 64.28\Omega$$
(11)

The selected inductor ratio $m = L_m/L_r = 10$ and quality factor Q = 0.3. From the given Q = 0.3 at full load and $f_r = 100$ kHz, the series resonant inductors and resonant capacitors are obtained in (12) and (13).

$$L_{r1} = L_{r2} = \frac{R_{ac}Q}{2\pi f_r} = \frac{64.28 \times 0.3}{2\pi \times 100,000} \approx 31\mu H$$
(12)

$$C_{r1} = C_{r2} = \frac{1}{4\pi^2 L_r f_r^2} = \frac{1}{4\pi^2 \times 57 \times 10^{-6} \times (100,000)^2} \approx 82nF$$
(13)

The magnetizing inductances L_{m1} and L_{m2} are obtained in (14).

$$L_{m1} = L_{m2} = m \times L_r = 10 \times 31 = 310 \mu H \tag{14}$$

The current and voltage ratings of C_{r1} and C_{r2} are obtained in (15) and (16).

$$i_{Cr1,rms} = i_{Cr2,rms} = \sqrt{\left(\frac{\pi I_{o,max}}{2n\sqrt{2}}\right)^2 + \left(\frac{nV_o/2}{4\sqrt{3}L_{m1}f_r}\right)^2} \approx 2.95A$$
(15)

$$v_{Cr1,\max} = v_{Cr2,\max} = V_{in,\max}/2 + \sqrt{2}i_{Cr,rms}/(2\pi f_r C_r) \approx 281V$$
(16)

The average current and voltage ratings of fast recovery diodes are expressed in (17) and (18).

$$i_{D1,av} = i_{D2,av} = I_0 / 2 = 10.5A \tag{17}$$

$$v_{D1,stress} = v_{D2,stress} = V_o = 48V \tag{18}$$

Diodes MBR40200PT are selected for D_1 and D_2 in the studied converter. The voltage rating of $Q_1 \sim Q_4$ equals $V_{in}/2 = 400$ V. MOSFETs G20N50C (Vishay Dale Electronics Inc., Pennsylvania, USA) with 500 V voltage stress instead of 1200 V IGBT are used for $Q_1 \sim Q_4$. The other capacitors $C_1 = C_2 = 220 \ \mu$ F, $C_f = 2.2 \ \mu$ F, and $C_{o1} = C_{o2} = 2200 \ \mu$ F. A type 2 voltage controller with a shunt voltage regulator based on the TL431 and a photocoupler based on PC817 are used to achieve output voltage control. The frequency control IC with Texas Instruments UCC25600 is selected to control $Q_1 \sim Q_4$.

A 1 kW circuit was built and the test results are demonstrated to show the performance of the studied converter. The circuit components of the proposed circuit are obtained from previous section. Figure 7a gives the photograph of the proposed prototype and Figure 7b gives the block diagram of the experimental circuit model. The test waveforms shown in Figures 8–13 of the converter is supplying 1 kW of output power under $V_{in} = 750$ V. The PWM signals of $Q_1 \sim Q_4$ of 50% load and 100% load are shown in Figure 8. The switching frequency at 100% load is less than the frequency at 50% load. Figure 9 demonstrates the measured waveforms of V_{C1} , V_{C2} , and V_{Cf} at 50% load and 100% load. The test experimental waveforms of V_{C1} , V_{C2} , and V_{Cf} are balanced. Figure 10 gives the test waveforms of v_{C1} , v_{C2} , int v_{C1} , v_{C2} , int v_{C1} and v_{Cr1} are balanced and i_{Lr1} and i_{Lr2} are balanced. Figure 11 demonstrates the measured i_{D1} , i_{D2} , i_{D1} + i_{D2} and V_o at 50% and 100% loads. It is observed that the zero-current turn-off of D_1 and D_2 are realized. Figure 12 demonstrates the measured voltage and current of $Q_1 \sim Q_4$ at 20% load. It can observe that C_Q is discharged to zero voltage before switch Q is active. It can also observe that the voltage stress of each active devices is equal to $V_{in}/2 = 375$ V instead of $V_{in} = 750$ V. Since power devices with low voltage stress are used in the studied converter, the conduction losses due to turn-on resistance of MOSFETs are

reduced. Therefore, the power losses on power devices are improved. Figure 13a the measured circuit efficiencies of the proposed converter and the conventional three-level phase-shift PWM converter with the same power devices, capacitors, and core size as the proposed converter. This three-level PWM converter have been built in the laboratory for many years to study high input voltage applications. The circuit efficiencies of the proposed converter from 92.3% (at 20% load) to 95.4% (at 75% load) under 750 V input. The measured circuit efficiencies of the conventional three-level PWM converter are from 90% (at 20% load) to 92% (at 75% load). It is clear that the proposed converter has better circuit efficiency. The main reasons of the low circuit efficiency of the conventional three-level PWM converter are high duty loss on heavy load (75% load and 100% load) and high switching frequency at light load (20% load). However, the switching loss on the proposed converter from low load to full load can be removed due to resonant behavior. Figure 13b gives the measured circuit efficiencies and the frequency range is from 62 kHz to 78 kHz at 750 V input and from 95 kHz to 123 kHz at 800 V input case.

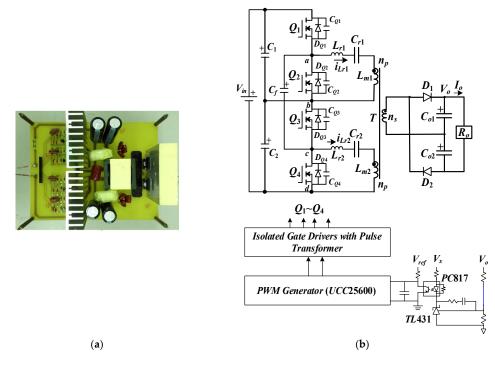


Figure 7. Proposed prototype circuit (a) photograph and (b) block diagram.

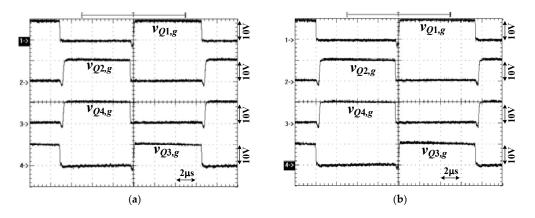


Figure 8. Test results of $v_{Q1,g} \sim v_{Q4,g}$ at (**a**) 50% power and (**b**) rated power.

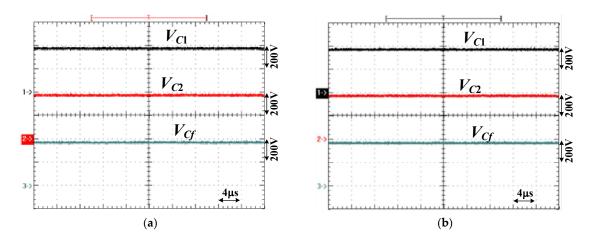


Figure 9. Experimental waveforms of V_{C1} , V_{C2} , and V_{Cf} (**a**) at 50% power and (**b**) rated power.

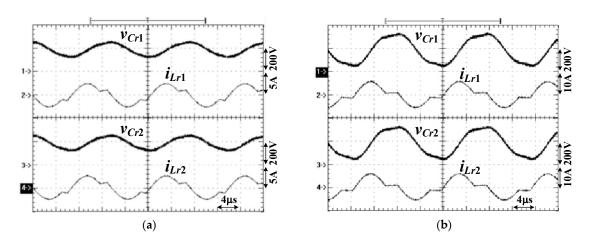


Figure 10. Experimental waveforms of v_{Cr1} , v_{Cr2} , i_{Lr1} , and i_{Lr2} (**a**) at 50% power and (**b**) rated power.

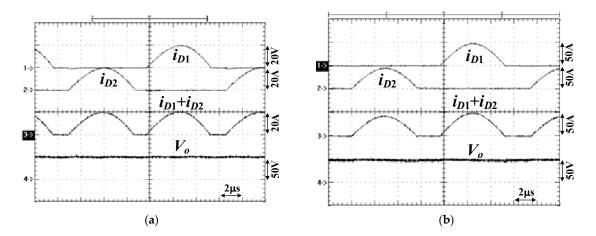


Figure 11. Test waveforms of diode currents and output voltage (a) at 50% power and (b) rated power.

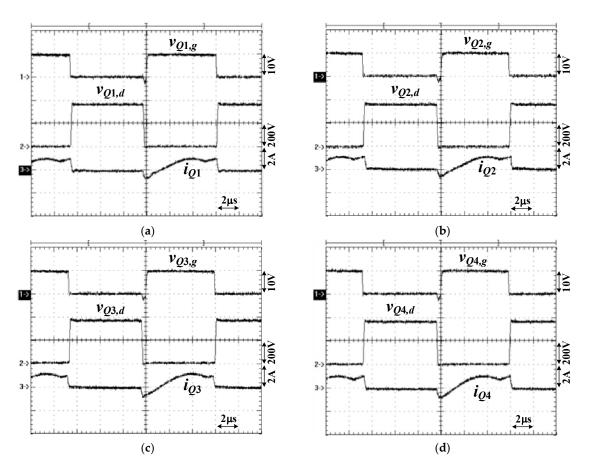


Figure 12. Commutation of switches $Q_1 \sim Q_4$ under 20% load (a) Q_1 ; (b) Q_2 ; (c) Q_3 ; (d) Q_4 .

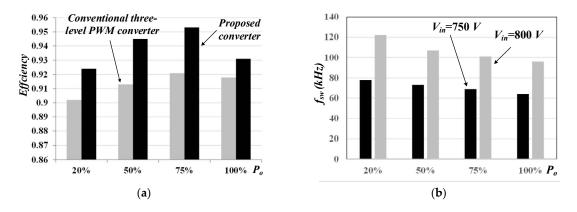


Figure 13. Test results (**a**) circuit efficiency compared to the conventional three-level PWM converter; (**b**) switching frequency.

4. Conclusions

A cascade resonant circuit with a single isolated transformer feasible to transportation vehicle applications is studied and presented in this paper. The circuit schematic, principles of operation and design procedure of the developed circuit are provided and discussed. Although the high voltage 1200 V SiC (Silicon Carbide) MOSFETs can be used on phase-shift full-bridge converter, the narrow ZVS range of lagging-leg switches will result in low circuit efficiency at low load. The cost of 1200 V SiC MOSFETs is main drawback to implement power products with low cost and high quality power supply. Therefore, lots of three-level circuit topologies are still developing to overcome the high voltage input issue. The benefits of the adopted circuit are low voltage rating of power semiconductor devices,

less power loss, and better efficiency. Finally, the practicability of the adopted power converter are demonstrated from a laboratory circuit under 1 kW rated power.

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Conflicts of Interest: The author declares no potential conflict of interest.

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