

Article



Control-Loop-Based Impedance Enhancement of Grid-Tied Inverters for Harmonic Suppression: Principle and Implementation

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Abstract: To understand different control loops that have been proposed to improve the quality of current into grid from the perspective of output impedance, control-loop-based output impedance enhancement of grid-tied inverters for harmonic suppression is proposed in this paper. The principle and generalized control loop deduction are presented for reshaping the output impedance. Taking a traditional LCL (Inductor-Capacitor-Inductor)-type inverter with dual-loop control as an example, different kinds of control loop topologies are derived step by step and further optimized for the implementation of the proposed principle. Consequently, the improved control consists of a filtering-capacitor voltage loop, and a grid current loop is found which can remove the existing inner capacitor current loop and therefore simplify the control. Finally, the effectiveness of the proposed control method is compared with the existing method and both are verified by simulations and experiments.

Keywords: grid-tied inverter; harmonic suppression; impedance enhancement; output impedance

1. Introduction

This paper considers the suppression of current harmonics from the perspective of output impedance reshaping. In this section, the background of harmonic suppression, literature review, formulation of the problem of interest for this investigation, scope and contribution of this study, and organization of the paper are provided.

1.1. Background and Significance

With the wide application of power-electronics-based distributed generator equipment, the quality of current into grid is partly polluted with the harmonics caused by the process of switching and the distorted grid voltage [1]. The loss on the cables will increase and some sensitive loads will work abnormally or even break if large harmonic contents of current exist, leading to the low economy of a power system. Therefore, to suppress the current harmonics as well as to achieve the goal of grid-tied requirements for inverters, different kinds of schemes for harmonic suppression have been proposed, including different regulators, topologies, and control loops [2].

1.2. Literature Review

Originally, the L-type grid-tied inverter is usually employed in a distributed generation system with a single grid-current feedback control loop. To satisfy the grid-tied requirements on the harmonics current, a large inductor is generally adopted to mainly suppress the harmonics at the switching frequency. However, the scale of the inverters is large and the effect of harmonic suppression is not

sufficient. Therefore, to reduce the scale of inverters as well as achieve a better effect on suppressing current harmonics, an LCL filter is employed [3]. However, as the LCL filter has a resonance peak, the inverter will become unstable if the grid voltage or the inverter has an excitation source at the resonant frequency. To damp the resonant peak, the dual-loop control strategy with capacitor current and grid current has been proposed [4]. The positive resonance peak is compensated by a negative resonance peak which is introduced though an additional compensator [5,6]. However, since the capacitor current contains a large amount of high-frequency harmonics, it is difficult to compensate them accurately. Therefore, instead of using a capacitor current, the weighted average current flowing through the two inductors of an LCL filter is used. This method is a split formation of capacitor current for an LCL filter [7,8].

Besides the harmonics caused by switches, the background harmonics of grid voltage also affect the grid current [9,10]. To compensate the harmonics in the grid voltage, the grid voltage is directly feedforward (FF), i.e., an equivalent voltage source which has the same magnitude and phase with grid voltage is generated to attenuate the impact of grid voltage disturbance. This method is called the partial feedforward control strategy. It is more suitable for the L-type structure, although for the LCL-type structure, due to the role of the capacitor, partial feedforward control cannot fully compensate the background harmonics of grid voltage [11,12]. The magnitude and phase of the generated equivalent voltage will not be equal to the grid voltage through an LCL filter if partial feedforward control strategy is used. Therefore, the coefficient of feedforward should be modified to get full compensation, that is, a full feedforward control strategy [13]. Other control loops, such as in [14,15], which employ the combination of current feedback and grid voltage feedforward also achieve the effect of suppressing the current harmonics. In addition, some advanced control algorithms such as repetitive control and the adjoint method can be taken into consideration for harmonic suppression [16,17].

1.3. Formulation of the Problem of Interest for This Study

It is necessary that the guideline of harmonic suppression from the perspective of reshaping output impedance should be summarized since the different kinds of control loops which have been proposed in previous literatures are intrinsically enhancing the output impedance. Generally, the equivalent model of grid-tied inverter systems is equal to a current source in parallel with an output impedance [18]. If the output impedance is large enough within the control bandwidth, the current source will become as ideal as possible. Therefore, based on the idea of infinite output impedance enhancement, this paper investigates the principle regarding reshaping the output impedance and optimizing the control loops.

1.4. Scope and Contribution of This Paper

In this paper, through summarizing the prior different control loops, the concept of output impedance enhancement is put forward, thus providing an understanding of different control loops. An optimized control loop is derived from the grid voltage feedforward control strategy, which can remove the existing inner capacitor current loop and therefore simplify the control loop. Meanwhile, the capability of output impedance enhancement is identical to the grid voltage feedforward control strategy. Besides, the cost of the system is reduced and its practical implementation is more convenient.

1.5. Organization of the Mauscript

The rest of this paper is organized as follows: by reshaping the output impedance based on the concept of output impedance enhancement, the grid voltage feedback and grid current feedback methods of reshaping output impedance are obtained in Section 2. The impact of two basic methods on output impedance enhancement is analyzed in detail in Section 3. To simplify the control loop for the convenience of realization, a method of splitting is adopted to optimize the grid voltage feedforward

control loop. Then, a novel control loop is proposed in Section 4. The correctness of the proposed control loop is verified in simulation and experiment in Section 5. Finally, a conclusion is made in Section 6.

2. Principle of Control-Loop-Based Impedance Enhancement

2.1. Reshaping Principle Based on Output Impedance Models

The LCL-type grid-tied inverter with dual loop of capacitor current and grid current is employed. The structure is shown in Figure 1a, where U_{dc} , u_{inv} , u_C , u_{PCC} , and u_g , represent DC voltage, voltage at inverter side, capacitor voltage, voltage at point of common coupling, and grid voltage, respectively. i_{inv} , i_C , i_g , i_{ref} , I_g , and i_{Cref} represent current at inverter side, capacitor current, grid current, reference current, the magnitude of the reference current, and the reference capacitor current, respectively. L_1 , L_2 , C_f , and Z_g represent the filter inductor at the inverter side, filter inductor at grid side, filter capacitor, and grid impedance, respectively. G_{ig} and G_{ic} represent the grid current regulator and the capacitor current regulator, respectively.



Figure 1. LCL (Inductor-Capacitor-Inductor)-type grid-tied inverter for single phase: (**a**) structure of main circuit; (**b**) structure of impedance model; (**c**) structure of equivalent circuit model.

 i_{ref} and i_o are satisfied with $i_o = i_{gref}G_o$, where G_o is a transfer function of current gain. Figure 1c shows the equivalent circuit model. It consists of a controlled current source in parallel with an output impedance and a voltage source in series with a grid impedance [6].

According to Figure 1c, i_g can be expressed as

$$i_{\rm g} = \frac{Z_{\rm o}}{Z_{\rm o} + Z_{\rm g}} i_{\rm o} - \frac{1}{Z_{\rm o} + Z_{\rm g}} u_{\rm g}.$$
 (1)

It is found in (1) that i_g is affected by i_o , u_g , Z_o , and Z_g . If Z_o is increased, the second item of (1) will be decreased. Therefore, the impact of u_g on i_g will be reduced by enhancing Z_o . If Z_o is increased to be much larger than Z_g , that is, $Z_o >> Z_g$, (1) will be simplified to

$$i_{\rm g} = i_{\rm o}.\tag{2}$$

It can be found that the impact of grid voltage disturbance on grid current can be reduced by increasing the output impedance, thereby improving the quality of current into grid. Therefore, i_g is approximately affected by i_0 but not affected by u_g and Z_g .

The methods of reshaping output impedance are listed in Figure 2. Take Figure 2a as an example: an extra impedance Z_{os} is in series with grid impedance. The output impedance will be enhanced if Z_{os} is designed properly. Other reshaping ways are shown in Figure 2b,h.



Figure 2. Methods of reshaping output impedance based on equivalent circuit: (**a**,**c**) series reshaping; (**b**) parallel reshaping; (**d**–**h**) combination of series and parallel reshaping.

2.2. Deduction Principle Based on Output Impedance Models

If an extra impedance Z_{os} is added to the grid side (shown in Figure 2a), the control structure will be changed into Figure 3a. Compared to Figure 1b, a grid current feedback loop is added to the control loop. To conveniently make a further control, the reference current i_{ref} is chosen, since a single point that has physical meaning is needed. Then, Figure 3a can be transferred to Figure 3b. It is obvious that the two structures are an equivalent formation. Similarly, the other reshaping ways shown in Figure 2b–h can be transferred to Figure 4b–h, respectively.



Figure 3. Block diagram of reshaping output impedance: (**a**) impedance model; (**b**) deformed impedance model.

Figure 4b,c,f,g, are grid voltage feedback control loops which feed grid voltage back to the reference current point. Figure 4a is a grid current feedback control loop which feeds the grid current back to the reference current, and Figure 4d,e,h are the combinations of grid voltage and grid current feedback control loops.





Figure 4. Methods of reshaping output impedance based on control loops: (**a**,**c**) series reshaping; (**b**) parallel reshaping; (**d**–**h**) combination of series and parallel reshaping.

From Figure 4a–h, two basic methods are obtained which can be employed to reshape output impedance: (a) grid voltage feedback control strategy and (b) grid current feedback control strategy. In the next section, the impact of output impedance based on two basic methods will be analyzed.

3. Analysis of Impact on Output Impedance of Various Control

3.1. Impact on Output Impedance Using Voltage Feedback Control

For convenience, K_u is adopted to uniformly represent the feedback coefficient when the grid voltage feedback control is employed. K_u can be expressed either as a constant value or a transfer function. Its control diagram is shown in Figure 5.



Figure 5. The structure of grid voltage feedback control.

The new output impedance Z_{ou} is

$$Z_{\rm ou} = \left. \frac{u_{\rm PCC}}{(-i_{\rm g})} \right|_{i_{\rm gref}=0} = Z_{\rm o} - \frac{Z_{\rm o}}{K_{\rm u}G_{\rm o}Z_{\rm o} - 1} K_{\rm u}G_{\rm o}Z_{\rm o} = \frac{Z_{\rm o}}{1 - K_{\rm u}G_{\rm o}Z_{\rm o}}.$$
(3)

Considering G_0 is positive in general within the control bandwidth, Z_{ou} can be enhanced when K_u is positive.

3.2. Impact on Output Impedance Using Current Feedback Control

 K_i represents the feedback coefficient when the grid current feedback control is employed. The control diagram is shown in Figure 6.



Figure 6. The structure of grid current feedback control.

The new output impedance Z_{oi} is

$$Z_{\rm oi} = \left. \frac{u_{\rm PCC}}{(-i_{\rm g})} \right|_{i_{\rm gref}=0} = Z_{\rm o} - K_{\rm i}G_{\rm o}Z_{\rm o}.$$
(4)

As indicated in (4), Z_{oi} will be enhanced when K_i is negative. If (5) is satisfied, the two basic methods will have an identical ability to enhance output impedance. Bode plots are given in Figure 7 to verify the enhancement effectiveness of the output impedance.

$$Z_{\rm ou} = Z_{\rm oi} \to K_{\rm i} = \frac{K_{\rm u} Z_{\rm o}}{K_{\rm u} G_{\rm o} Z_{\rm o} - 1}.$$
(5)



Figure 7. Bode plots of output impedance with two basic impedance reshaped methods.

(a). As indicated in (4), Z_{oi} will be enhanced when K_i is negative. If (5) is satisfied, the two basic methods will have an identical ability to enhance output impedance. Bode plots are given in Figure 7 to verify the enhancement effectiveness of the output impedance. The output impedance will be enhanced when K_u is positive for voltage feedback control, while K_i is negative for current feedback control.

(b). The capacity of the two basic methods to reshape the output impedance is identical and they are equivalent when (5) is satisfied except in one circumstance, that is, when K_u is equal to $1/G_oZ_o$, K_i will trend to be infinite.

To obtain the largest gain of output impedance in order to prove that the basic impedance reshaped methods have the instructive significance for the enhancement of output impedance, a specific example is illustrated.

3.3. Impedance Enhancement Control Loop Based on Basic Impedance Reshaped Methods

Take the dual loop with capacitor current and grid current feedback as an example. When a grid voltage feedback control loop is added to the reference current, as shown in Figure 8a, the control diagram can be obtained (Figure 8b).





Figure 8. LCL-type grid-tied inverter for single-phase: (**a**) the main circuit structure with grid voltage feedback control loop; (**b**) control loop.

According to Figure 8b, the original output impedance without grid voltage feedback control loop is

$$Z_{\rm o} = \frac{s^3 L_1 L_2 C_{\rm f} + s^2 G_{\rm iC} G_{\rm inv} L_2 C_{\rm f} + s L_1 + s L_2 + G_{\rm ig} G_{\rm iC} G_{\rm inv}}{s^2 L_1 C_{\rm f} + s G_{\rm iC} G_{\rm inv} C_{\rm f} + 1}.$$
(6)

 G_0 can be calculated as

$$G_{\rm o} = \frac{i_{\rm g}}{i_{\rm ref}} |_{u_{\rm PCC}=0} = \frac{G_{\rm ig}G_{\rm iC}G_{\rm inv}}{s^3 L_1 L_2 C_{\rm f} + s^2 G_{\rm iC}G_{\rm inv} L_2 C_{\rm f} + sL_1 + sL_2 + G_{\rm ig}G_{\rm iC}G_{\rm inv}}.$$
(7)

The reshaped output impedance can be calculated according to

$$Z_{\rm ou} = \frac{Z_{\rm o}}{1 - K_{\rm u}G_{\rm o}Z_{\rm o}} = \frac{s^3 L_1 L_2 C_{\rm f} + s^2 G_{\rm iC} G_{\rm inv} L_2 C_{\rm f} + s L_1 + s L_2 + G_{\rm ig} G_{\rm iC} G_{\rm inv}}{s^2 L_1 C_{\rm f} + s G_{\rm iC} G_{\rm inv} C_{\rm f} + 1 - K_{\rm u} G_{\rm ig} G_{\rm iC} G_{\rm inv}}.$$
(8)

If the denominator of (8) is zero, the output impedance can be enhanced as much as possible. Then, K_u is

$$K_{\rm u} = \frac{s^2 L_1 C_{\rm f} + s G_{\rm iC} G_{\rm inv} C_{\rm f} + 1}{G_{\rm ig} G_{\rm iC} G_{\rm inv}}.$$
(9)

Simplify (9) and the deformed feedback coefficient K'_{u} is

$$K'_{\rm u} = \frac{s^2 L_1 C_{\rm f} + s G_{\rm iC} G_{\rm inv} C_{\rm f} + 1}{G_{\rm inv}}.$$
(10)

In order to reduce high-frequency noise introduced by the second-order differential item K'_{u} , a first-order low pass filter is employed. The output impedance will turn into

$$Z'_{ou} = \frac{Z_{o}}{1 - \frac{K'_{u}}{T_{LFF}s + 1} \times G_{o}Z_{o}} = \frac{s^{3}L_{1}L_{2}C_{f} + s^{2}G_{iC}G_{inv}L_{2}C_{f} + sL_{1} + sL_{2} + G_{ig}G_{iC}G_{inv}}{s^{2}L_{1}C_{f} + sG_{iC}G_{inv}C_{f} + 1 - \frac{K'_{u}}{T_{LFF}s + 1} \times G_{ig}G_{iC}G_{inv}}$$
(11)

where T_{LPF} is the time constant of the low-pass filter. The voltage harmonics are mainly considered about less than 40th, and the cut-off frequency of the low-pass filter should be larger than 2 kHz in order to enhance output impedance as much as possible. So, $T_{\text{LPF}} = 40 \ \mu\text{s}$. (Cut-off frequency is 3980 Hz, approximately).

The parameters of an LCL inverter system are given in Table 1. According to (8), (11), and Table 2, the original output impedance and reshaped output impedance can be obtained, as shown in Figure 9. Figure 9 shows that the reshaped output impedance is obviously enhanced under the cut-off frequency, and the highest gain is about 1000 times greater than before.

$\begin{array}{cccc} u_{\rm g} & {\rm Grid} \ {\rm voltage} & 220 \ {\rm V} \\ f_{\rm g} & {\rm Frequency} & 50 \ {\rm Hz} \\ U_{\rm dc} & {\rm DC} \ {\rm voltage} & 400 \ {\rm V} \\ L_1 & {\rm Filter} \ {\rm inductor} \ {\rm at} \ {\rm inverter} \ {\rm side} & 2.4 \ {\rm mH} \\ L_2 & {\rm Filter} \ {\rm inductor} \ {\rm at} \ {\rm grid} \ {\rm side} & 2.4 \ {\rm mH} \\ Z_{\rm g} & {\rm Grid} \ {\rm impedance} & 0.2 \ \Omega/0.08 \ {\rm mH} \\ C_f & {\rm Filter} \ {\rm capacitor} & 4 \ {\rm \mu F} \\ f_{\rm s} & {\rm Switch} \ {\rm frequency} & 16 \ {\rm kHz} \\ G_{\rm ic} & {\rm Capacitor} \ {\rm current} \ {\rm regulator} & 30 \\ G_{\rm inv} & {\rm Gain} \ {\rm of} \ {\rm the} \ {\rm inverter} & 1 \\ K_{\rm p} & {\rm Proportional} \ {\rm coefficient} & 1 \\ K_{\rm R} & {\rm Resonance} \ {\rm regulator} \ {\rm coefficient} & 50 \\ \omega_{\rm c} & {\rm Band} \ {\rm frequency} & 10 \ {\rm rad} \ {\rm s}^{-1} \\ T_{\rm LPF} & {\rm Time} \ {\rm constant} \ {\rm of} \ {\rm low} \ {\rm pass} \ {\rm filter} & 40 \ {\rm \mu s} \\ i_{\rm ref} & {\rm Reference} \ {\rm current} & 10 \ {\rm A} \\ \end{array}$	Symbol	Quantity	Value
$ \begin{array}{ccccc} f_{g} & Frequency & 50 \ \text{Hz} \\ U_{dc} & DC \ \text{voltage} & 400 \ \text{V} \\ L_{1} & Filter \ \text{inductor at inverter side} & 2.4 \ \text{mH} \\ L_{2} & Filter \ \text{inductor at grid side} & 2.4 \ \text{mH} \\ Z_{g} & Grid \ \text{impedance} & 0.2 \ \Omega/0.08 \ \text{mH} \\ C_{f} & Filter \ \text{capacitor} & 4 \ \mu\text{F} \\ f_{s} & Switch \ frequency & 16 \ \text{kHz} \\ G_{ic} & Capacitor \ \text{current regulator} & 30 \\ G_{inv} & Gain \ \text{of the inverter} & 1 \\ K_{p} & Proportional \ \text{coefficient} & 1 \\ K_{R} & Resonance \ \text{regulator coefficient} & 50 \\ \omega_{c} & Band \ frequency & 10 \ \text{rad s}^{-1} \\ T_{LPF} & Time \ \text{constant of low pass filter} & 40 \ \mu\text{s} \\ i_{ref} & Reference \ \text{current} & 10 \ \text{A} \\ \end{array} $	Иg	Grid voltage	220 V
$\begin{array}{ccccc} U_{\rm dc} & {\rm DC \ voltage} & 400 \ V \\ L_1 & {\rm Filter \ inductor \ at \ inverter \ side} & 2.4 \ mH \\ L_2 & {\rm Filter \ inductor \ at \ grid \ side} & 2.4 \ mH \\ Z_g & {\rm Grid \ impedance} & 0.2 \ \Omega/0.08 \ mH \\ C_f & {\rm Filter \ capacitor} & 4 \ \mu {\rm F} \\ f_{\rm s} & {\rm Switch \ frequency} & 16 \ kHz \\ G_{\rm ic} & {\rm Capacitor \ current \ regulator} & 30 \\ G_{\rm inv} & {\rm Gain \ of \ the \ inverter} & 1 \\ K_p & {\rm Proportional \ coefficient} & 1 \\ K_R & {\rm Resonance \ regulator \ coefficient} & 50 \\ \omega_c & {\rm Band \ frequency} & 10 \ rad \ {\rm s}^{-1} \\ T_{\rm LPF} & {\rm Time \ constant \ of \ low \ pass \ filter} & 40 \ \mu {\rm s} \\ i_{\rm ref} & {\rm Reference \ current} & 10 \ {\rm A} \end{array}$	f_{g}^{o}	Frequency	50 Hz
$\begin{array}{ccccc} L_1 & \mbox{Filter inductor at inverter side} & 2.4 \mbox{ mH} \\ L_2 & \mbox{Filter inductor at grid side} & 2.4 \mbox{ mH} \\ Z_g & \mbox{Grid impedance} & 0.2 \Omega/0.08 \mbox{ mH} \\ C_f & \mbox{Filter capacitor} & 4 \mu \mbox{F} \\ f_s & \mbox{Switch frequency} & 16 \mbox{Hz} \\ G_{ic} & \mbox{Capacitor current regulator} & 30 \\ G_{inv} & \mbox{Gain of the inverter} & 1 \\ K_p & \mbox{Proportional coefficient} & 1 \\ K_R & \mbox{Resonance regulator coefficient} & 50 \\ \omega_c & \mbox{Band frequency} & 10 \mbox{ rad s}^{-1} \\ T_{LPF} & \mbox{Time constant of low pass filter} & 40 \mbox{µs} \\ i_{ref} & \mbox{Reference current} & 10 \mbox{ A} \\ \end{array}$	$U_{\rm dc}$	DC voltage	400 V
$\begin{array}{cccc} L_2 & \mbox{Filter inductor at grid side} & 2.4 \mbox{ mH} \\ Z_g & \mbox{Grid impedance} & 0.2 \ \Omega/0.08 \mbox{ mH} \\ C_f & \mbox{Filter capacitor} & 4 \ \mu \mbox{F} \\ f_s & \mbox{Switch frequency} & 16 \mbox{ kHz} \\ G_{ic} & \mbox{Capacitor current regulator} & 30 \\ G_{inv} & \mbox{Gain of the inverter} & 1 \\ K_p & \mbox{Proportional coefficient} & 1 \\ K_R & \mbox{Resonance regulator coefficient} & 50 \\ \omega_c & \mbox{Band frequency} & 10 \mbox{ rad s}^{-1} \\ T_{LPF} & \mbox{Time constant of low pass filter} & 40 \ \mu \mbox{s} \\ i_{ref} & \mbox{Reference current} & 10 \ \mbox{A} \end{array}$	L_1	Filter inductor at inverter side	2.4 mH
$\begin{array}{cccc} Z_{\rm g} & {\rm Grid\ impedance} & 0.2\ \Omega/0.08\ {\rm mH} \\ C_f & {\rm Filter\ capacitor} & 4\ \mu{\rm F} \\ f_{\rm s} & {\rm Switch\ frequency} & 16\ {\rm kHz} \\ G_{\rm ic} & {\rm Capacitor\ current\ regulator} & 30 \\ G_{\rm inv} & {\rm Gain\ of\ the\ inverter} & 1 \\ K_{\rm p} & {\rm Proportional\ coefficient} & 1 \\ K_{\rm R} & {\rm Resonance\ regulator\ coefficient} & 50 \\ \omega_{\rm c} & {\rm Band\ frequency} & 10\ {\rm rad\ s^{-1}} \\ T_{\rm LPF} & {\rm Time\ constant\ of\ low\ pass\ filter} & 40\ \mu {\rm s} \\ i_{\rm ref} & {\rm Reference\ current} & 10\ {\rm A} \\ \end{array}$	L_2	Filter inductor at grid side	2.4 mH
$\begin{array}{cccc} C_f & \mbox{Filter capacitor} & 4 \ \mu \mbox{F} \\ f_{\rm s} & \mbox{Switch frequency} & 16 \ \mbox{Hz} \\ G_{\rm ic} & \mbox{Capacitor current regulator} & 30 \\ G_{\rm inv} & \mbox{Gain of the inverter} & 1 \\ K_{\rm p} & \mbox{Proportional coefficient} & 1 \\ K_{\rm R} & \mbox{Resonance regulator coefficient} & 50 \\ \omega_{\rm c} & \mbox{Band frequency} & 10 \ \mbox{rad s}^{-1} \\ T_{\rm LPF} & \mbox{Time constant of low pass filter} & 40 \ \mbox{\mu s} \\ i_{\rm ref} & \mbox{Reference current} & 10 \ \mbox{A} \end{array}$	Z_{g}	Grid impedance	$0.2 \Omega/0.08 \text{ mH}$
$f_{\rm s}$ Switch frequency16 kHz $G_{\rm ic}$ Capacitor current regulator30 $G_{\rm inv}$ Gain of the inverter1 $K_{\rm p}$ Proportional coefficient1 $K_{\rm R}$ Resonance regulator coefficient50 $\omega_{\rm c}$ Band frequency10 rad s ⁻¹ $T_{\rm LPF}$ Time constant of low pass filter40 μ s $i_{\rm ref}$ Reference current10 A	C_{f}	Filter capacitor	4 μF
$\begin{array}{cccc} G_{\rm ic} & {\rm Capacitor\ current\ regulator} & 30 \\ G_{\rm inv} & {\rm Gain\ of\ the\ inverter} & 1 \\ K_{\rm p} & {\rm Proportional\ coefficient} & 1 \\ K_{\rm R} & {\rm Resonance\ regulator\ coefficient} & 50 \\ \omega_{\rm c} & {\rm Band\ frequency} & 10\ {\rm rad\ s^{-1}} \\ T_{\rm LPF} & {\rm Time\ constant\ of\ low\ pass\ filter} & 40\ \mu {\rm s} \\ i_{\rm ref} & {\rm Reference\ current} & 10\ {\rm A} \end{array}$	f_{s}	Switch frequency	16 kHz
$\begin{array}{cccc} G_{\rm inv} & {\rm Gain \ of \ the \ inverter} & 1 \\ K_{\rm p} & {\rm Proportional \ coefficient} & 1 \\ K_{\rm R} & {\rm Resonance \ regulator \ coefficient} & 50 \\ \omega_{\rm c} & {\rm Band \ frequency} & 10 \ {\rm rad \ s^{-1}} \\ T_{\rm LPF} & {\rm Time \ constant \ of \ low \ pass \ filter} & 40 \ \mu {\rm s} \\ i_{\rm ref} & {\rm Reference \ current} & 10 \ {\rm A} \end{array}$	G _{ic}	Capacitor current regulator	30
$\begin{array}{ccc} K_{\rm p} & {\rm Proportional coefficient} & 1 \\ K_{\rm R} & {\rm Resonance regulator coefficient} & 50 \\ \omega_{\rm c} & {\rm Band frequency} & 10 {\rm rad s^{-1}} \\ T_{\rm LPF} & {\rm Time constant of low pass filter} & 40 \mu {\rm s} \\ i_{\rm ref} & {\rm Reference current} & 10 {\rm A} \end{array}$	G_{inv}	Gain of the inverter	1
$K_{\rm R}$ Resonance regulator coefficient50 $\omega_{\rm c}$ Band frequency10 rad s^{-1} $T_{\rm LPF}$ Time constant of low pass filter40 μ s $i_{\rm ref}$ Reference current10 A	Kp	Proportional coefficient	1
$\omega_{\rm c}$ Band frequency10 rad s^{-1} $T_{\rm LPF}$ Time constant of low pass filter40 $\mu {\rm s}$ $i_{\rm ref}$ Reference current10 A	$K_{\rm R}^{\rm I}$	Resonance regulator coefficient	50
$ \begin{array}{ccc} T_{\rm LPF} & {\rm Time \ constant \ of \ low \ pass \ filter} & 40 \ \mu s \\ i_{\rm ref} & {\rm Reference \ current} & 10 \ {\rm A} \end{array} $	ω _c	Band frequency	10 rad s^{-1}
<i>i</i> _{ref} Reference current 10 A	$T_{\rm LPF}$	Time constant of low pass filter	$40 \ \mu s$
	i _{ref}	Reference current	10 A

Table 1. Parameters of single phase inverters with LCL filter.



Figure 9. Bode plot of output impedance based on voltage feedback control.

Control Strategy	THD of Grid Current/%
Dual-loop control strategy	13.17 5.78
Proposed control strategy	5.75

Table 2. THD of grid current under different harmonic suppression schemes.

Actually, this method is also called the full feedforward control strategy [9]. The principle of reshaped output impedance is elaborately described in previous sections. Based on the impedance model, two basic methods of reshaping output impedance are obtained, and a specific example is illustrated to prove the effectiveness of the basic methods. Further, it is necessary to apply the methods to engineering implementation.

4. Implementation and Optimization of Control-Loop-Based Impedance Enhancement

According to the Kirchhoff voltage law, grid voltage is equal to the difference between capacitor voltage and grid-side inductor voltage, and the expression of the feedback branch can be transformed to

$$K'_{\rm u} = \frac{s^2 L_1 C_{\rm f} + s G_{\rm iC} G_{\rm inv} C_{\rm f} + 1}{G_{\rm inv}}.$$
(12)

The expression of the feedback branch turns from $u_{PCC}K_u$ to $(u_C - u_{L2}) K_u$, which means the control loop turns from a single loop of grid voltage to a dual loop of capacitor voltage and inductor voltage. If the feedback coefficient is equal to K_u , the capacity of reshaping output impedance is identical to the grid voltage feedforward control. The control structure is shown in Figure 10. K_Z is the feedback coefficient of the grid-side inductor voltage. A new control loop structure is created through a split. Similarly, the inductor voltage at grid side is also equal to the grid current multiplied by the inductor impedance, and then the grid voltage also can be transformed to

$$u_{\rm PCC}K_{\rm u} = \left(u_{\rm C} - i_{\rm g}Z_{\rm L_2}\right)K_{\rm u} \tag{13}$$

where Z_{L2} represents inductor impedance. The control structure is shown in Figure 11. K_{I} is the feedback coefficient of the grid current.



Figure 10. The structure of capacitor voltage and grid-side inductor voltage feedback control loop.



Figure 11. The structure of capacitor voltage and grid current feedback control loop.

To obtain a simpler control loop, continue to simplify to

$$u_{PCC}K_{u} = (u_{C} - i_{g}Z_{L2})K_{u} = u_{C}K_{u} - i_{g}Z_{L2}K_{u} = u_{C}\left(\frac{s^{2}L_{1}C_{f} + sG_{iC}G_{inv}C_{f} + 1}{G_{ig}G_{iC}G_{inv}}\right) - i_{g}sL_{2}\left(\frac{s^{2}L_{1}C_{f} + sG_{iC}G_{inv}C_{f} + 1}{G_{ig}G_{iC}G_{inv}}\right) \\ = u_{C}\frac{s^{2}L_{1}C_{f} + 1}{G_{ig}G_{iC}G_{inv}} + u_{C}\frac{sC_{f}}{G_{ig}} - i_{g}\left(\frac{s^{3}L_{1}L_{2}C_{f} + s^{2}G_{iC}G_{inv}C_{f}L_{2} + sL_{2}}{G_{ig}G_{iC}G_{inv}}\right) \\ = u_{C}\frac{s^{2}L_{1}C_{f} + 1}{G_{ig}G_{iC}G_{inv}} + i_{C}\frac{1}{G_{ig}} - i_{g}\left(\frac{s^{3}L_{1}L_{2}C_{f} + s^{2}G_{iC}G_{inv}C_{f}L_{2} + sL_{2}}{G_{ig}G_{iC}G_{inv}}\right)$$
(14)

Compared to the FF control strategy, the capacitor voltage, capacitor current, and grid current feedback control loops are employed instead of the grid voltage feedback control loop as shown in Figure 12a. The control structure in Figure 12a can be optimized to Figure 12b through simplifying the control loops where the new controller G'_{ig} equals $G_{ig}G_{iC}$. G'_{ig} is a proportional-resonant controller similar to G_{ig} in the FF control strategy. Otherwise, the proposed control method is derived from the FF control strategy, and the capability of enhancing output impedance regarding the two methods is identical, as is the control bandwidth. The specific control structure of the proposed method is shown in Figure 12c. It shows that the inner capacitor current loop is eliminated and the capacitor current is no longer needed compared to the FF control strategy. Therefore, the cost will be reduced and the implementation in practice will be convenient.



Figure 12. Proposed control loop of capacitor voltage and grid current feedback. (**a**) Optimization step I; (**b**) optimization step II; (**c**) proposed control structure, respectively.

To deal with harmonic influences of the grid voltage on the grid current, the capacitor feedforward control loop is proposed from the perspective of enhancing output impedance. The output impedance is enhanced in the full bandwidth compared to the multiple PR (Proportional Resonance) controller which enhances the output impedance only at the selected frequency, as shown in Figure 13. As mentioned in [18], the repetitive control is equivalent to a combination of a proportional controller and multiple parallel resonant controller. The effectiveness of enhancing output impedance is similar to the multiple PR controller. Meanwhile, the repetitive control is a relative complex for implementation. Therefore,

the proposed control strategy with the capacitor feedforward control loop is convenient to enhance the output impedance.



Figure 13. Comparison of the output impedance with the proposed method and multiple PR (Proportional Resonance) controller.

The stability of the proposed control strategy can be determined by the ratio of the grid impedance and output impedance, that is, Z_g/Z'_{ou} should be satisfied with the Nyquist criterion [18]. Here, the grid impedance is 0.2 $\Omega/0.08$ mH, and Z'_{ou} is shown in (11).

It can be found that in Figure 14, there is no pole at the right side of the s plane, and its Nyquist curve does not circle the point -1 + i0. According to the Nyquist criterion, this system is stable.



Figure 14. Pole-zero plot and Nyquist curve of Z_g/Z'_{ou} . (a) Pole-zero plot; (b) Nyquist curve, respectively.

5. Simulations and Experimental Verifications

To verify the proposed control strategy, a single-phase grid-tied inverter with an LCL filter was established in PSIM (Power Simulation), and the parameters are shown in Table 1. The 3rd, 5th, 7th, 9th, 11th, and 13th harmonics were injected into grid voltage, and the magnitude of each harmonic was 5%, 6%, 1%, 1.5%, 3.5%, and 3%, respectively.

In order to be more realistic, a 0.5 Ω resistor was concatenated on the DC side to simulate the true DC voltage source in this paper. Figure 15a shows the simulation results of a dual-loop control strategy with capacitor current and grid current. It can be seen that both the voltage and current are heavily distorted. The THD (total harmonic distorted) of the grid current was 7.4%, as shown in Figure 15b. (i_g *20)/A in Figures 15a, 16a and 17a indicates that the grid current is 20 times greater than the original value.



Figure 15. Simulation results of dual-loop control strategy. (**a**) Waveforms of grid voltage and current. (**b**) FFT (Fast Fourier Transformation) analysis of grid current (THD = 7.4%).



Figure 16. Simulation results of grid voltage feedforward control strategy. (**a**) Waveforms of grid voltage and current. (**b**) FFT analysis of grid current (THD = 3.3%).



Figure 17. Simulation results of the proposed control strategy. (**a**) Waveforms of grid voltage and current. (**b**) FFT analysis of grid current (THD = 2.8%).

By introducing the grid voltage feedforward control loop, the impact of distorted grid voltage on the grid current is smaller. The current wave in Figure 16a is approximately sinusoidal and the THD of

the grid current reduces to 3.3% in Figure 16b. It is suggested that by enhancing the output impedance, the current harmonics are suppressed, and the grid voltage feedforward control strategy is effective at suppressing the grid voltage disturbance.

The simulation results in Figure 17a indicate that the proposed control strategy employing the capacitor voltage and grid current is also effective at suppressing current harmonics. It is suggested that the proposed control strategy also has an identical ability of enhancing output impedance with the grid voltage feedforward control strategy. The THD of the grid current is 2.8% in Figure 17b and it achieves the requirements of grid connectedness.

In order to further verify the proposed control strategy, a prototype was designed and established in the laboratory, as shown in Figure 18. The parameters were identical to the simulation as shown in Table 2. The experimental results of the dual-loop control strategy with the capacitor current and grid current feedback, the grid voltage feedforward control, the proposed control strategy of capacitor voltage, and the grid current are shown in Figures 19–21 respectively.



Figure 18. Platform of the grid-tied inverter for single phase.



Figure 19. The experimental results of conventional dual-loop control strategy. (**a**) Waveforms of grid voltage and current. (**b**) The FFT analysis of grid current (THD = 13.17%).



Figure 20. The experimental results of the FF (Feed Forward) strategy. (**a**) Waveforms of grid voltage and current, and (**b**) the FFT analysis of grid current (THD = 5.78%).



Figure 21. The experimental results of the proposed control strategy. (**a**) Waveforms of grid voltage and current, and (**b**) the FFT analysis of grid current (THD = 5.75%).

The current harmonics are well suppressed when the grid voltage feedforward control is employed, as shown in Figures 19 and 20. The proposed control strategy achieves the same ability of suppressing current harmonics with the FF as shown in Figure 21. The THDs of the grid current with different harmonic suppression schemes are shown in Table 2.

To show the good transient performances, dynamic experiments were carried out in which the reference current was given from 2 to 4 A at t_1 and from 4 to 2 A at t_2 , respectively. The experimental results are shown in Figure 22 and indicate that dynamic performance can be guaranteed when the proposed control method is adopted.



Figure 22. Dynamic performances when the proposed control strategy is employed.

6. Conclusions

The principle and implementation of control-loop-based impedance enhancement of grid-tied inverters for harmonic suppression was proposed in this paper in detail. Based on the idea of reshaping output impedance, two basic methods of impedance reshaping were obtained. It was found that the grid voltage feedback control has an infinite impedance enhancement ability which can eliminate the influences of the distorted grid voltage in theory. A specific example was illustrated to prove the effectiveness of the basic methods of reshaping impedance. Based on the idea of infinite impedance reshaping, the implementation of control loops was made step by step. To find an optimized control loop, a novel control loop that can eliminate the inner capacitor current loop and reduce the number of sensors was proposed through splitting the grid voltage. Finally, the simulation and experimental results were illustrated to verify the effectiveness of the proposed control strategy.

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