

## Article

# Optimal Charging Schedule Planning and Economic Analysis for Electric Bus Charging Stations

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**Abstract:** The battery capacity of electric buses (EB) used for public transportation is greater than that of electric cars, and the charging power is also several times greater than that used in electric cars; this can result in high energy consumption and negatively impact power distribution networks. This paper proposes a framework to determine the optimal contracted power capacity and charging schedule of an EB charging station in such a way that energy costs can be reduced. A mathematical model of controlled charging, which includes the capacity and energy charges of the station, was developed to minimize costs. The constraints of the model include the charging characteristics of an EB and the operational guidelines of the bus company. A practical EB charging station was used to verify the proposed model. The financial viability of this EB charging station is also studied in this paper. The economic analysis model for this charging station considers investment and operational costs, and the operational revenue. Sensitivity analyses with respect to some key parameters are also performed in this paper. Based on actual operational routes and EB charging schemes, test results indicate that the EB charging station investment is feasible, and the planning model proposed can be used to determine optimal station power capacity and minimize energy costs.

**Keywords:** contracted capacity; controlled charging; charging schedule; electric bus; economic analysis

## 1. Introduction

While electricity from power plants is a tightly regulated source, electric vehicles (EVs) could bring more transportation-related emissions under stricter regulation. With emission caps in place for key pollutants, displacement of gasoline or diesel in favor of electricity will reduce overall emissions. Regional public transportation offers a good opportunity for the introduction of battery-powered vehicles. In order to reduce greenhouse gas emissions and improve air quality, 10,000 electric buses (EBs) are planned to be in operation in the next decade in Taiwan.

EBs are characterized by fixed running routes, fixed charging sites, near-identical charging capacity and a carbon-reducing means of transport worthy of extensive popularization. However, configuring an overall EB system is challenging; this would include possible battery recharge and exchange concepts, choice of battery technology, battery sizing, positioning and dimensioning of charging and exchange stations, and the respective bus line's characteristics and topography [1].

The energy consumed in charging an EB is several times that of charging an electric car for private use. The electrical energy consumption and the impact on the power system are greater. Therefore, to accommodate transportation electrification, the energy costs of charging stations and their impact on the distribution network should be well planned. The impact on power grids of charging EVs, including the use of smart charging methods to reduce energy costs and guarantee system security and integration with renewable energy, is discussed in [2–14]. While these analytical techniques presented and reviewed [2–14] could be extended to include EB charging, there are presently only a few studies which discuss the planning of EB charging stations and their impact on the distribution network.

In [15], the authors present optimal planning of EV charging stations with the use of capacitors to maintain voltage and improve the amount of power loss in electrical distribution networks. Simultaneous optimal planning of charging stations and distributed generation is presented in [16] by the same authors. Investment costs, system reliability, power loss, voltage profile and CO<sub>2</sub> emission issues are considered in an objective function. The financial viability of investing in EV charging stations located in the parking lots of commercial/industrial workplaces is proposed in [17]. Level II charging installations are examined and the internal rate of return and the net present value method are used to measure the investment's profitability.

The authors of [18] focus on the design optimization of the plug-in hybrid electric vehicle (PHEV) charging station with battery storage units, and examine the charging trend of PHEVs. An optimized operation for the battery storage schedule and a strategy of power trading in order to minimize the costs of the charging stations were proposed. An algorithm for optimally managing a large number of PHEVs (e.g., 3000) charging at a municipal parking station was presented in [19]. A mathematical framework for maximizing the average state-of-charge at the next step was established in this paper. A decision model to implement direct load control on battery-charging processes at EV charging points located in parking areas is presented in [20]. The objective function maximizes the net energy supplied to batteries while simultaneously minimizing the global energy cost. The use of an EB charging station, and its impact on the power grid, was studied in [21]. In order to improve power load characteristics and increase power sales, a consumption pattern of routine night-time charging, coupled with day use to balance the peaks and valleys of power use, was considered. The possibility of using energy storage systems to balance peak power demands using fast charging stations, as well as using such storage to optimize renewable energy sources, was investigated in [22].

As an EB charging station will consume large amounts of energy, to achieve a high return on investment it must be properly planned according to the operating guidelines of the bus company. The electricity bill will include both basic charges and energy charge. This paper proposes a controlled charging method to minimize the energy costs of an EB charging station. This model uses the charging power at each time interval and the contracted capacity as state variables, and considers the constraints of the bus company's operational policies and station-contracted capacity. This paper also examines the financial viability of investing in EB charging stations. An economic model considering subsidies from the government, investment costs, operational costs and revenues is proposed. An actual EB charging station is studied to demonstrate the effectiveness of the proposed method.

Due to the high charging power of EVs and EBs, system security concerning the integration of EVs and EBs is drawing a lot of attention. Therefore, most of the published papers focus on the impact analyses of them on the distribution network. They consider the objective functions concerning the operation at the system level, such as grid loss minimization [12], network security [7,11], and power market participation [23]. Few papers address the planning and operation of a charging station. To avoid EV charging during the peak hours, utilities can use a time-of-use pricing scheme to shift the charging time to the off-peak period. Therefore, it is necessary to present a planning model for the charging station to follow the time of use pricing scheme. Through the proposed model, the charging station not only can minimize the energy cost but also help the utilities mitigate the charging impacts on the distribution system.

The organization of the paper is as follows. A description of the studied EB charging station is provided in Section 2. Problem formulation and solution methods are described in Section 3. Section 4 introduces the economic analysis model for this charging station. Test results are offered in Section 5. Finally, concluding remarks are given.

## 2. Description of the EB Charging Station

In the actual EB system studied, an EB is able to seat 23 persons at most. At present, there are ten EBs providing transport service between the Qishan township and Kaohsiung City. The battery capacity is 250 kWh. The AC power source for EB charging is 380 V, and this is subsequently converted

into 300 to 450 V DC. The current rating of the charger is 120 A and the rated output power is 50 kW. Charging current is controllable. Figure 1 shows the wiring of the charging station. Figure 2 shows the measured three-phase charging power during the period of operation.



Figure 1. Actual wiring diagram of the charging station.

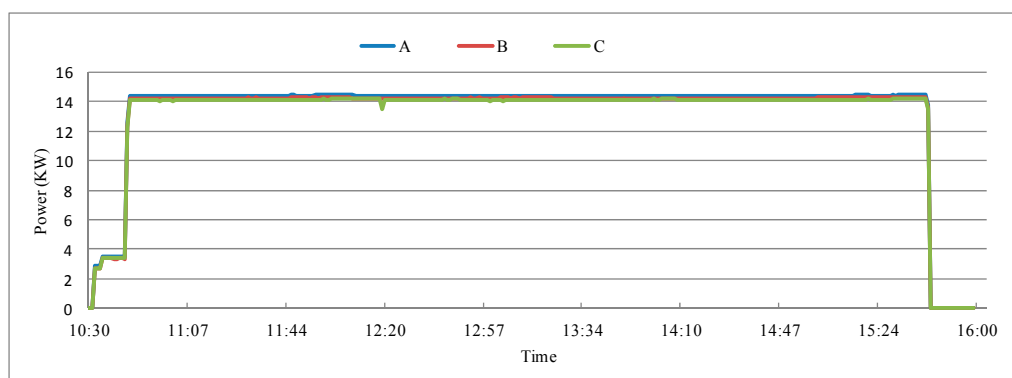


Figure 2. The measured three-phase charging power.

The EB charging station operates from 6:00 a.m. to 11:40 p.m. The EB route takes 160 min to complete one transport service, consisting of two round-trips between the Qishan Township and Kaohsiung City. The first departure is at 6:00 a.m. and the last trip returns to Qishan Station at 11:40 p.m. At present, the ten EBs are not charged immediately after service, but wait until the off-peak time (after 10:30 p.m.). Currently, the service is supplemented by diesel buses. In the long run, it is planned to have EBs take over all services. It is estimated that if EBs are used for all scheduled services, seven EBs will need to be charged during the service period in order to make another trip. An EB battery charging scheme is proposed to help the bus company reduce the EB operation cost by controlling the charging time and current required to provide the service. A network impact study will highlight the added value of the proposed charging scheme.

### 3. Problem Formulation and Solution Method

The Taiwan Power Company uses a time of use pricing scheme to stimulate the EV and EB charging during the off-peak hours and flatten the load profile. An optimal EB charging station planning model based on the time of use pricing scheme is proposed in this section. Issues about

the integration of renewable energy and implementation of the proposed model in the field are also addressed here.

### 3.1. Optimal EB Charging Station Planning Model

A 3-stage time-of-use (TOU) rate schedule shown in Figure 3 is available from the utility company. The monthly bill includes the basic capacity charge and energy charge. The basic capacity charge expressed in Equation (1) is based on the contracted capacities from the power company. A detailed description about the contracted capacities is shown in Appendix A. As shown in Equation (2), the energy charge is calculated by multiplying the power consumption of the charging station during each time interval by the electric rate of the interval. The mathematical model, as proposed in this paper, uses the charging power of an EB during each time interval, and the usual contracted capacity, half-peak contracted capacity, and off-peak contracted capacity, as variables. The objective function minimizes the sum of the basic capacity charge and energy charge. The constraints enable the EB to complete the charging process before performing transport service according to the operating guidelines of the bus company, while avoiding power consumption exceeding the contracted capacity during each time interval. The problem formulation is shown in Equation (3). As the contracted capacity of Taiwan Power Co., Ltd. is calculated based on 15 min, the model uses 15 min as the time unit. Although the proposed model is built based on the time of use pricing scheme performed in Taiwan, it can be modified to the other pricing scheme by changing the electricity price at each time interval in Equation (2).

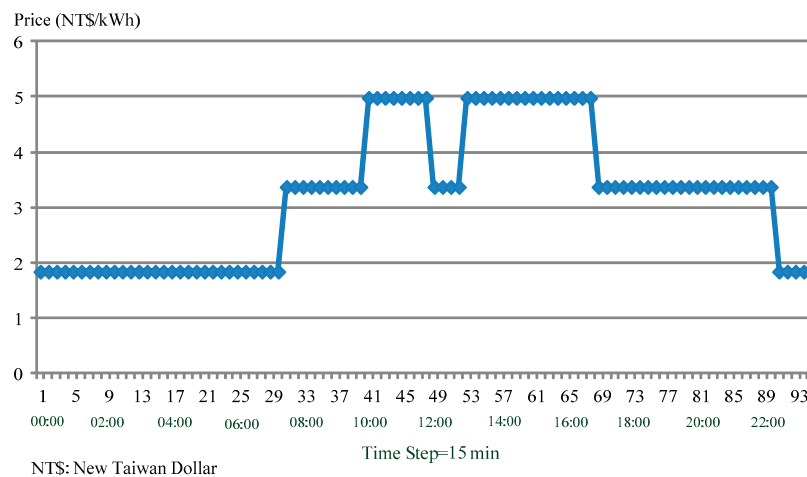


Figure 3. Time-of-use rate schedule.

$$\text{Basic capacity charge} = \text{har} \times \text{CP} + \text{CHP} \times \text{CH} + \text{COP} \times \text{Max}((\text{CO} - (\text{CP} + \text{CH})/2), 0) \quad (1)$$

where CP, CH, and CO are the usual, half-peak and off-peak contracted capacities that cost CPP, CHP, and COP (NT\$) per kW, respectively.

$$\text{Energy charge} = \left( \begin{array}{l} P_{pp} \times \sum_{i=1}^{\text{BusNo}} \sum_{t \in \{t_p\}} \text{BusChg}_{i,t} + \\ HP \times \sum_{i=1}^{\text{BusNo}} \sum_{t \in \{t_h\}} \text{BusChg}_{i,t} + \\ OP \times \sum_{i=1}^{\text{BusNo}} \sum_{t \in \{t_o\}} \text{BusChg}_{i,t} \end{array} \right) \times 0.25 \times \text{DayNo} \quad (2)$$

where  $\text{BusChg}_{i,t}$  is the charging power of bus  $i$  at time  $t$ , and PP, HP, and OP are the electricity price of every 1 kWh at peak, half-peak, and off-peak periods, respectively. DayNo is the number of days of a billing cycle.  $\{t_p\}$ ,  $\{t_h\}$  and  $\{t_o\}$  are peak, half-peak, and off-peak hours, respectively, as defined in Table 1. The contracted capacities CP, CH, and CO and the charging power of each bus  $i$  at time  $t$   $\text{BusChg}_{i,t}$  are the state variables to be determined.

The optimization problem solved is as follows:

$$\begin{aligned}
 & \text{Min Basic capacity charge} + \text{Energy charge} \\
 & \text{S.T.} \\
 & \sum_{t=A_i}^{L_i} \text{BusChg}_{i,t} \times 0.25 \times \text{eff}_i \geq \text{ChgCap}_i \quad \forall \text{Bus } i \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq \text{CP} \quad t \in \{t_p\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq (\text{CP} + \text{CH}) \quad t \in \{t_h\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq (\text{CP} + \text{CH} + \text{CO}) \quad t \in \{t_o\} \\
 & 0 \leq \text{BusChg}_{i,t} \leq \text{MaxChg}_i \quad \forall i, \forall t
 \end{aligned} \tag{3}$$

where  $\text{BusChg}_{i,t}$  is the charging power of bus  $i$  at time  $t$ ,  $A_i$  and  $L_i$  are the start charging time and leaving time of bus  $i$ ,  $\text{eff}_i$  is the efficiency of charging pole  $i$ , and  $\text{ChgCap}_i$  is the electric energy (kWh) that bus  $i$  must have in order to complete a route transport service.

**Table 1.** Time intervals of applicable rate schedule.

Peak	Half-Peak	Off-Peak
10:00~12:00	07:30~10:00	22:30~24:00
13:00~17:00	12:00~13:00	00:00~07:30
	17:00~22:30	

The first constraint of Equation (3) is to ensure that each EB has sufficient energy to provide high quality services. Constraints 2~4 are to avoid power consumption exceeding the contracted capacity at each time interval.

The third term of the basic capacity charge in Equation (1) is to encourage users to use electricity during off-peak hours as much as possible. If the contracted capacity in the off-peak time interval does not exceed half the sum of the usual contracted capacity and half-peak contracted capacity, it is free of charge, i.e., if  $\text{CO} - (\text{CP} + \text{CH})/2 \leq 0$ , then the basic capacity charge =  $\text{CPP} \times \text{CP} + \text{CHP} \times \text{CH}$ . On the other hand, if  $\text{CO} - (\text{CP} + \text{CH})/2 > 0$ , then the basic capacity charge =  $\text{CPP} \times \text{CP} + \text{CHP} \times \text{CH} + \text{COP} \times (\text{CO} - (\text{CP} + \text{CH})/2)$ ; only the part exceeding half the sum of the usual contracted capacity and half-peak contracted capacity is charged. Figure 4 shows the solving procedure to deal with this particular condition. Two sub-problems (6) and (7) are formulated and solved respectively. Formulation (6) optimizes the energy cost under the constraint of  $\text{CO} - (\text{CP} + \text{CH})/2 \leq 0$ . Thus, the basic capacity charge =  $\text{CPP} \times \text{CP} + \text{CHP} \times \text{CH}$ , and the constraint of  $\text{CO} - (\text{CP} + \text{CH})/2 \leq 0$  is added to Formulation (6). Formulation (7) minimizes the energy cost considering the constraint of  $\text{CO} - (\text{CP} + \text{CH})/2 > 0$ . Therefore, the basic capacity charge =  $\text{CPP} \times \text{CP} + \text{CHP} \times \text{CH} + \text{COP} \times (\text{CO} - (\text{CP} + \text{CH})/2)$ , and the constraint of  $\text{CO} - (\text{CP} + \text{CH})/2 > 0$  is added to Formulation (7). By comparing the objective functions of (6) and (7), the smaller one is chosen as the optimal solution.

$$\text{Basic capacity charge 1} = \text{CPP} \times \text{CP} + \text{CHP} \times \text{CH} \tag{4}$$

$$\text{Basic capacity charge 2} = \text{CP} \times \text{CP} + \text{CHP} \times \text{CH} + \text{COP} \times (\text{CO} - (\text{CP} + \text{CH})/2) \tag{5}$$

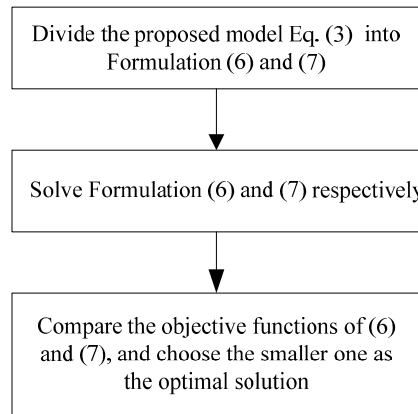


Figure 4. Solving procedure.

Min Basic capacity charge 1 + Energy charge

S.T.

$$\begin{aligned}
 & \sum_{t=A_i}^{L_i} \text{BusChg}_{i,t} \times 0.25 \times \text{eff}_i \geq \text{ChgCap}_i \quad \forall \text{Bus } i \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq \text{CP} \quad t \in \{t_p\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq (\text{CP} + \text{CH}) \quad t \in \{t_h\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq (\text{CP} + \text{CH} + \text{CO}) \quad t \in \{t_o\} \\
 & 0 \leq \text{BusChg}_{i,t} \leq \text{MaxChg}_i \quad \forall i, \forall t \\
 & \text{CO} - (\text{CP} + \text{CH})/2 \leq 0
 \end{aligned} \tag{6}$$

Min Basic capacity charge 2 + Energy charge

S.T.

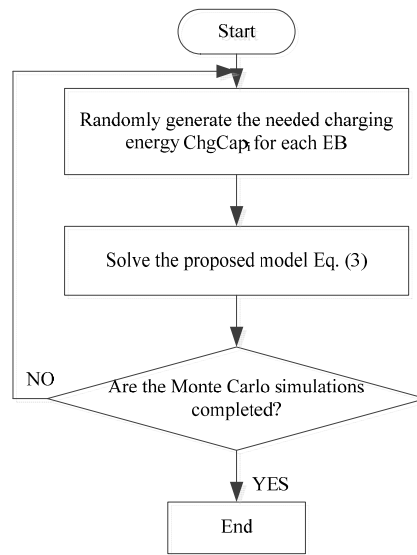
$$\begin{aligned}
 & \sum_{t=A_i}^{L_i} \text{BusChg}_{i,t} \times 0.25 \times \text{eff}_i \geq \text{ChgCap}_i \quad \forall \text{Bus } i \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq \text{CP} \quad t \in \{t_p\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq (\text{CP} + \text{CH}) \quad t \in \{t_h\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} \leq (\text{CP} + \text{CH} + \text{CO}) \quad t \in \{t_o\} \\
 & 0 \leq \text{BusChg}_{i,t} \leq \text{MaxChg}_i \quad \forall i, \forall t \\
 & \text{CO} - (\text{CP} + \text{CH})/2 \geq 0
 \end{aligned} \tag{7}$$

Due to driving habits, battery performance, the desired battery state of charge (SOC) etc., the  $\text{ChgCap}_i$  may change for each transport service. Based on the current SOC and the desired SOC, we can calculate the needed charging energy  $\text{ChgCap}_i$  in Equation (3), and maintain the battery SOC to work in the desired range. According to recorded battery-charging data, a normal distribution, as shown in Equation (8), is used to model the  $\text{ChgCap}_i$ . The mean value and standard deviation are 168 kWh and 13 kWh, respectively. The Monte Carlo Simulation is used to address the uncertainty of  $\text{ChgCap}_i$ . In each Monte Carlo simulation, a number between 0 and 1 is generated by a random number generator for each EB to determine the needed charging energy  $\text{ChgCap}_i$ . Figure 5 shows the proposed stochastic approach, which is described as follows.

$$f(\text{ChgCap}_i) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(\text{ChgCap}_i - \mu)^2 / (2\sigma^2)} \tag{8}$$

where  $\mu$  and  $\sigma$  are the mean value and standard deviation, respectively.

- 1 The randomness of the needed EBs' charging power is simulated based on Gaussian distributions with the mean values and standard deviations determined.
- 2 The solving procedure proposed in Figure 4 for the proposed model is used, as expressed in Equation (3).
- 3 Steps 1–2 are repeated until a predefined iteration number is reached. The coefficient of variance is often used as the stopping rule in the sampling. An alternative is to use a pre-specified number as the stopping rule. When the simulation process ends, the coefficient of variance is checked [24]. This paper adopts the coefficient of (standard deviation)/(mean value) being smaller than 0.01 as the criterion for convergence when the Monte Carlo simulation is completed.



**Figure 5.** Flow diagram of the proposed stochastic simulation.

### 3.2. Integration of the Renewable Energy

Due to the global energy crisis and environmental pollution, it is becoming a trend to integrate renewable energy into the power grid. The renewable energy can also be integrated into the proposed model as shown in Equation (9). A wind energy integration case is demonstrated in the test results section.

Min Basic capacity charge + Energy charge – RenewEng revenue

S.T.

$$\begin{aligned}
 & \sum_{t=A_i}^{L_i} \text{BusChg}_{i,t} \times 0.25 \times \text{eff}_i \geq \text{ChgCap}_i \quad \forall \text{Bus } i \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} - \text{Renew}_t \leq \text{CP} \quad t \in \{t_p\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} - \text{Renew}_t \leq (\text{CP} + \text{CH}) \quad t \in \{t_h\} \\
 & \sum_{i=1}^{\text{BusNo}} \text{BusChg}_{i,t} - \text{Renew}_t \leq (\text{CP} + \text{CH} + \text{CO}) \quad t \in \{t_o\} \\
 & 0 \leq \text{BusChg}_{i,t} \leq \text{MaxChg}_i \quad \forall i, \forall t
 \end{aligned} \tag{9}$$

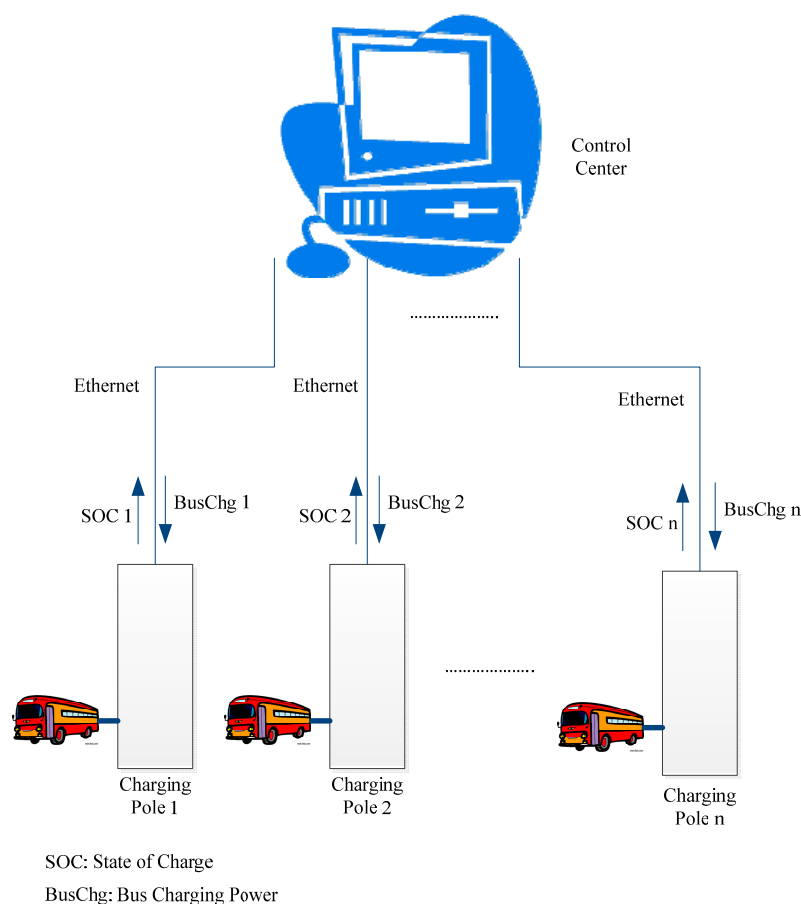


where RenewEng revenue is the revenue obtained by the renewable energy as shown in Equation (10), and  $\text{Renew}_t$  is the output of renewable generation at time  $t$ .

$$\text{RenewEngrevenue} = \left( \text{PP} \times \sum_{t \in \{t_p\}} \text{Renew}_t + \text{HP} \times \sum_{t \in \{t_h\}} \text{Renew}_t + \text{OP} \times \sum_{t \in \{t_h\}} \text{Renew}_t \right) \times 0.25 \times \text{DayNo} \quad (10)$$

### 3.3. Implementation of the Proposed Model in the Field

The proposed model can be implemented in the field as shown in Figure 6. If an EB charging service information platform is established, data of battery SOC and charging demand available in the battery management system can be obtained. Considering the charging pole with the Ethernet communication interface, data of all EBs can be sent to the control center. The control center executes the proposed model, and sends the charging power signals to each EB to minimize the energy cost of the charging station.



**Figure 6.** Implementation of the proposed model in the field.

## 4. Economic Analysis of the Charging Station

An economic analysis of the EB charging station is studied in this paper. In order to help improve air quality, the government in Taiwan offers financial support to the bus companies to encourage them to replace diesel buses with EBs. These subsidies include the purchase of EBs and the construction of the EB charging station. The cost of one EB is NT\$6,500,000, and the government support is NT\$5,200,000. The investment required to build the EB charging station is NT\$36,701,000; the subsidy is NT\$17,249,000.



The bus company rents the EB batteries instead of buying them. The leasing fee for each EB is NT\$43,000 per month. Other costs include personnel expenses, energy costs and maintenance costs for the operation of the EB station. The cash flow for this economic analysis is shown in Figure 7, with a detailed description given below.

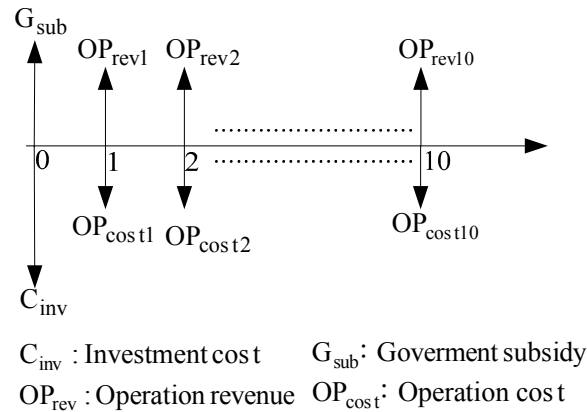


Figure 7. Cash flow for the EB charging station.

1. Investment costs ( $C_{inv}$ ): The investment cost includes the purchase of 10 EBs and construction of the EB charging station.
2. Operational cost ( $OP_{cost}$ ): The operational cost includes the personnel expense, battery leasing fee, energy cost and maintenance cost.
3. Operation revenue ( $OP_{rev}$ ): The operation revenue is the customer traffic service charge.

The present value method shown in Equation (11) is used to perform the economic analysis of the EB station. Sensitivity analyses for some key parameters are discussed in the test results section.

$$NPV = -C_{inv} + G_{sub} + \sum_{i=1}^N \frac{(OP_{rev,i} - OP_{cost,i})}{(1 + d)^i} \quad (11)$$

where  $d$  is the discount rate, and  $N$  is the life cycle.

## 5. Test Results

There are 10 EBs performing transport services in this charging station. According to the guidelines of the bus company, seven EBs perform two transport services and three EBs perform one transport service during the service period, with the transport service of diesel buses completely replaced with electric buses. Charging time intervals of the 10 EBs are shown in Table 2. The charging time interval for an EB is between the end time of one transport service and the start time of the next service. During the charging time intervals, the EB must finish the charging process in order to continue the next transport service. In the controlled charging mode, the problem shown in Equation (3) is used to determine the optimum contracted capacities and charging schedule. In the uncontrolled charging mode, the rated charging power (50 kW) at the beginning of the charging time interval is used. In the tests, CPP, CHP and COP are NT\$223.6/kW, NT\$166.9/kW and NT\$44.7/kW per month, respectively. PP, HP and OP are NT\$4.98/kWh, NT\$3.37/kWh and NT\$1.84 NT\$/kWh, respectively. Charging efficiency is assumed equal to 95%.

**Table 2.** EB charging time intervals.

Vehicle No.	The First Charging-Time Interval	The Second Charging-Time Interval
1	09:00~15:15	22:30~05:45
2	09:30~16:00	22:30~05:45
3	10:00~16:15	22:30~05:45
4	10:15~16:45	22:30~05:45
5	11:00~17:15	22:30~05:45
6	12:30~19:45	23:00~05:45
7	13:45~20:30	23:45~05:45
8~10	22:30~05:45	—

### 5.1. Optimal Power Consumption Planning for Charging Station

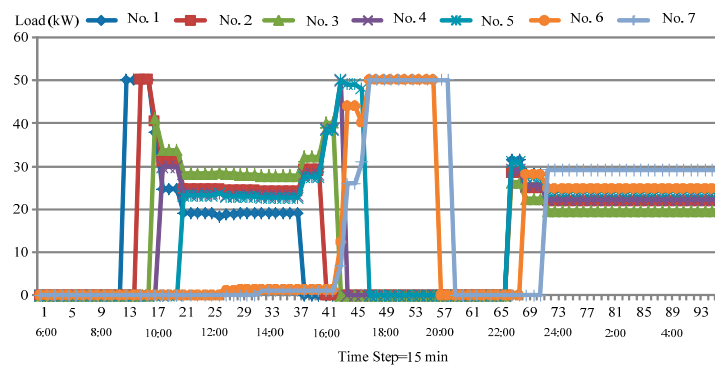
According to recorded battery data, a normal distribution, as shown in (8), is used to model the needed charging energy of an EB completing one transport service. The mean value and standard deviation are 168 kWh and 13 kWh, respectively. Summaries of 1000 iterations' results are described in Table 3. The average values of energy costs in one month for controlled and uncontrolled charging methods are NT\$288,925 and NT\$322,594, respectively. The case of controlled charging would only stipulate 119 kW for average usual contracted capacity, and 117 kW for average off-peak contracted capacity, whereas the uncontrolled charge shall stipulate 250 kW for average usual contracted capacity and 250 kW for average off-peak contracted capacity.

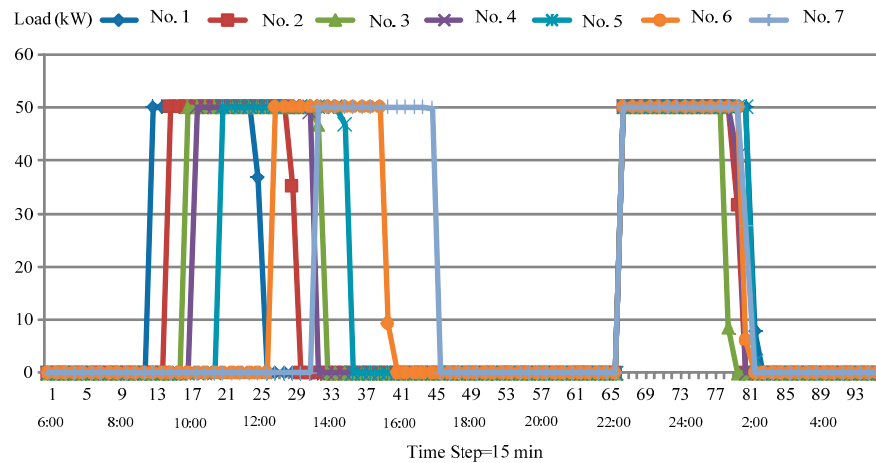
Test results of one of these 1000 iterations are discussed below. Figures 8 and 9 show the controlled and uncontrolled charging schedules of vehicles 1~7, which shall be charged twice. The contracted capacity price and electricity price during a peak time interval are higher than they are at a half-peak time interval. Therefore, a controlled charge avoids charging in the peak time interval as is possible, and flattens the load profile to minimize energy costs. Figure 10 shows the charging station load profiles. The controlled charge reduces and flattens the charging station load peak, as much as possible, thus reducing energy costs. The purpose of the time of use pricing scheme is to shift the charging time to the off-peak period. If too much load is transferred, the pricing rate can be readjusted in each time period to flatten the load profile.

**Table 3.** Controlled charge and uncontrolled charge planning results for 1000 iterations.

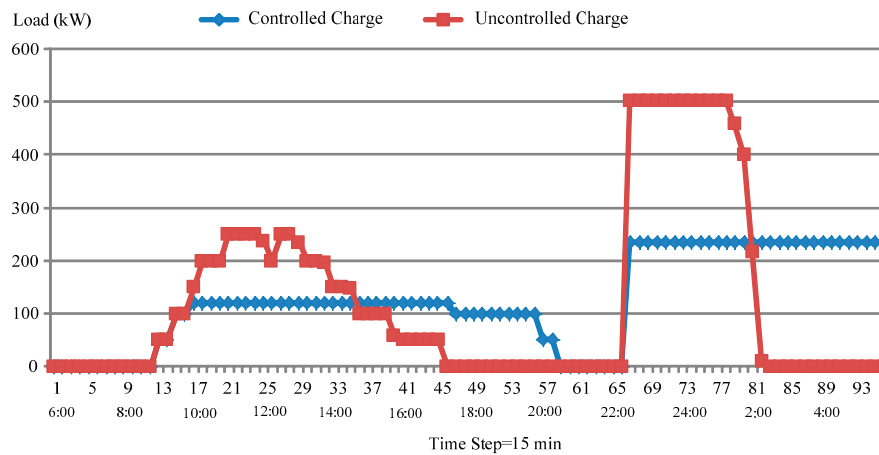
	Controlled Charge	Uncontrolled Charge
The average value of energy cost in one month (NT\$)	288,925	322,594
The average value of usual contracted capacity (kW)	119	250
The average value of half-peak contracted capacity (kW)	0	0
The average value of off-peak contracted capacity (kW)	117	250

1 USD = 31 NT\$.

**Figure 8.** Charging schedule of controlled charge of buses 1~7 for this iteration.



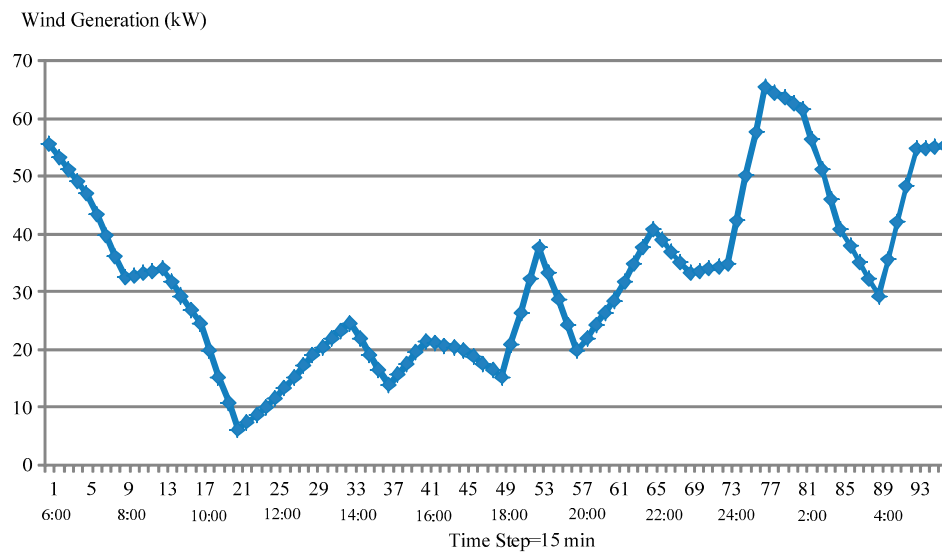
**Figure 9.** Charging schedule of uncontrolled charge of buses 1~7 for this iteration.



**Figure 10.** Charging station load profile for this iteration.

## 5.2. Integration of the Wind Generation

A rated 100 kW wind generation unit is integrated into the charging station. Figure 11 shows the wind generation profile. Table 4 shows the planning results for the controlled and uncontrolled charging methods considering the integration of this wind generation unit. Because the wind generation provides part of the charging load, the contracted capacities and the energy costs for the controlled and uncontrolled charging methods are both reduced. The average values of energy costs in one month for controlled and uncontrolled charging methods are NT\$219,950 and NT\$265,630, respectively. With the integration of the wind generation, all of these contracted capacities are smaller than those without the wind generation, as shown in Table 3. The case of controlled charging would only stipulate 102 kW for average usual contracted capacity, and 88 kW for average off-peak contracted capacity, whereas, the uncontrolled charge shall stipulate 244 kW for average usual contracted capacity and 223 kW for average off-peak contracted capacity.



**Figure 11.** The wind generation profile.

**Table 4.** Controlled charge and uncontrolled charge planning considering the integration of wind generation.

	Controlled Charge	Uncontrolled Charge
The average value of energy cost in one month (NT\$)	219,950	265,630
The average value of usual contracted capacity (kW)	102	244
The average value of half-peak contracted capacity (kW)	0	0
The average value of off-peak contracted capacity (kW)	88	223

### 5.3. Economic Analysis of the Charging Station

This paper considers the investment cost, financial support from the government, operational cost and operation revenue to perform an economic analysis of this charging station. The energy costs for the controlled and uncontrolled charging for one month are described in previous paragraphs. The ticket price charge is NT\$108 per person, and the average number of customers for each trip is 21. This will lead to an operation revenue of NT\$56,291,760 per year. The personnel expenses, leasing fee for batteries, maintenance cost and operation revenue for one year of this charging station are shown in Table 5. The investment cost and financial support from the government are described in Section 4.

The present value method shown in Equation (11) is used to perform this financial analysis. The lifecycle of an EB is 10 years. Table 6 shows the present values for the controlled and uncontrolled charging during 10 years. The difference between these two charging methods is NT\$4,735,000, and this project is feasible for the bus company.

**Table 5.** Economic analysis parameters for the charging station.

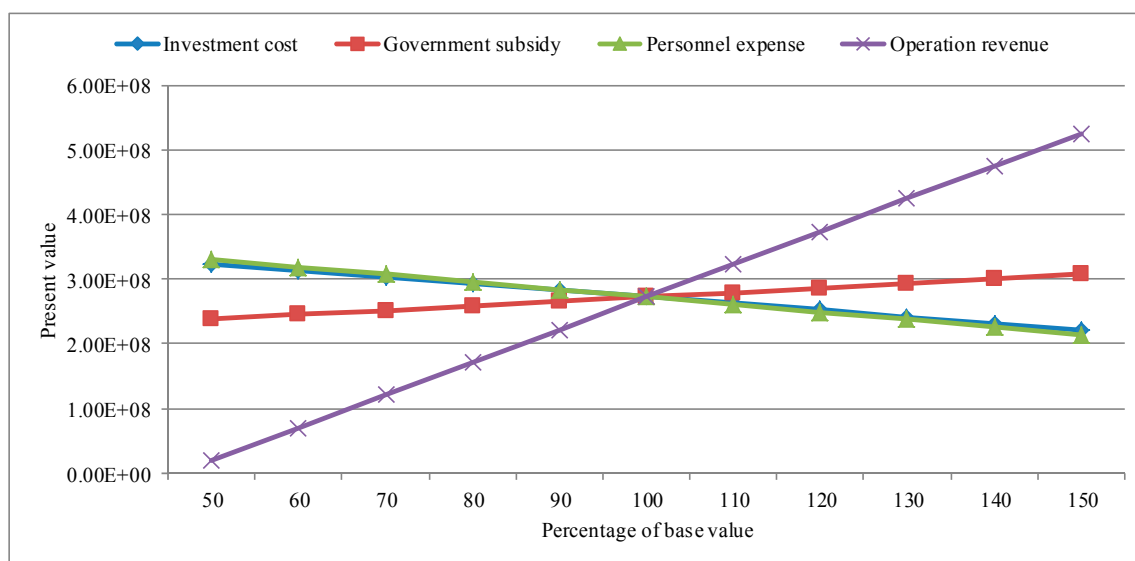
Personnel Expense (NT\$/year)	Leasing Fee (NT\$/year)	Maintenance Cost (NT\$/year)	Operation Revenue (NT\$/year)
12,935,000	5,160,000	500,000	56,291,760

**Table 6.** Economic analysis results for the EB charging station.

	Controlled Charge	Uncontrolled Charge
Present value	272,616,000	267,881,000

#### 5.4. Sensitivity Analyses

In order to handle uncertainties of this project, sensitivity analyses are performed with respect to four key parameters: the investment cost, government subsidy, personnel expense, and operation revenue. All these parameters are changed from 50% to 150% of their current base values respectively. Figures 12 and 13 show the sensitivity analyses results of the controlled charge and uncontrolled charge respectively. These results show that the parameter of operation revenue (traffic service charge) is the most sensitive factor. Equation (12) is the present value deviation rate for the controlled and uncontrolled charge. Table 7 shows the detailed sensitivity analysis results of the operation revenue parameter. When the ticket price is 50% of the current price, the present value for the controlled charge is only NT\$19,792,900. However, the present value will rise to NT\$525,438,000 when the ticket price is 150% of the current price. Table 7 also shows when the ticket price is lower; the present value deviation rate for the controlled and uncontrolled charge incurs a larger value. This means that the controlled charge is more important when the competition forces the bus company to lower the service charge. Detailed sensitivity results of the investment cost, government subsidy, and personnel expense parameters are also demonstrated in Tables 8–10. The controlled charge has a greater impact on the present value deviation rate when the investment cost or personnel expense increases, or the government subsidy decreases. These results are useful for the bus company to face the future competitive challenge.

**Figure 12.** Sensitivity analyses of the controlled charge.

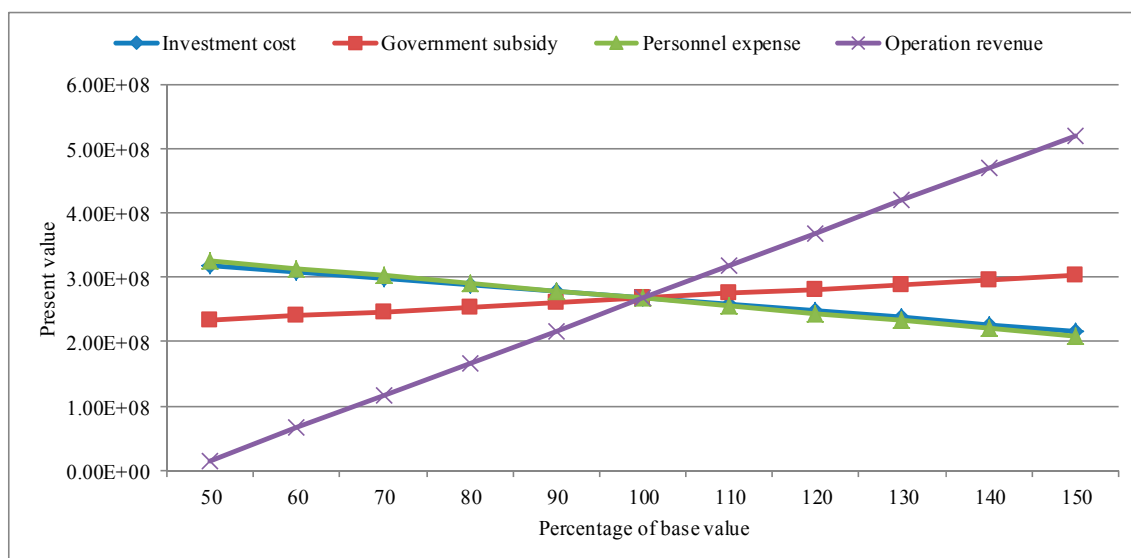


Figure 13. Sensitivity analyses of the uncontrolled charge.

$$\Delta\text{Pres} = \frac{\text{Present value of the controlled charge} - \text{Present value of the uncontrolled charge}}{\text{Present value of the uncontrolled charge}} * 100\% \quad (12)$$

Table 7. Detailed sensitivity results of the operation revenue parameter.

Percentage of the Current Operation Revenue (%)	Present Value of the Controlled Charge (NT\$)	Present Value of the Uncontrolled Charge (NT\$)	$\Delta\text{Pres}$ (%)
50	19,792,900	15,058,300	31.44
60	70,357,400	65,622,800	7.21
70	120,922,000	116,187,000	4.07
80	171,487,000	166,752,000	2.84
90	222,051,000	217,316,000	2.18
100	272,616,000	267,881,000	1.77
110	323,180,000	318,446,000	1.49
120	373,745,000	369,010,000	1.28
130	424,309,000	419,575,000	1.13
140	474,874,000	470,139,000	1.01
150	525,438,000	520,704,000	0.91

Table 8. Detailed sensitivity results of the investment cost parameter.

Percentage of the Current Investment Costs (%)	Present Value of the Controlled Charge (NT\$)	Present Value of the Uncontrolled Charge (NT\$)	$\Delta\text{Pres}$ (%)
50	323,466,000	318,732,000	1.49
60	313,296,000	308,561,000	1.53
70	303,126,000	298,391,000	1.59
80	292,956,000	288,221,000	1.64
90	282,786,000	278,051,000	1.70
100	272,616,000	267,881,000	1.77
110	262,446,000	257,711,000	1.84
120	252,275,000	247,541,000	1.91
130	242,105,000	237,371,000	1.99
140	231,935,000	227,201,000	2.08
150	221,765,000	217,031,000	2.18

**Table 9.** Detailed sensitivity results of the government subsidy parameter.

Percentage of the Current Government Subsidy (%)	Present Value of the Controlled Charge (NT\$)	Present Value of the Uncontrolled Charge (NT\$)	$\Delta$ Pres (%)
50	237,991,000	233,257,000	2.03
60	244,916,000	240,181,000	1.97
70	251,841,000	247,106,000	1.92
80	258,766,000	254,031,000	1.86
90	265,691,000	260,956,000	1.81
100	272,616,000	267,881,000	1.77
110	279,541,000	274,806,000	1.72
120	286,465,000	281,731,000	1.68
130	293,390,000	288,656,000	1.64
140	300,315,000	295,581,000	1.60
150	307,240,000	302,506,000	1.57

**Table 10.** Detailed sensitivity results of the personnel expense parameter.

Percentage of the Current Personnel Expenses (%)	Present Value of the Controlled Charge (NT\$)	Present Value of the Uncontrolled Charge (NT\$)	$\Delta$ Pres (%)
50	330,710,000	325,976,000	1.45
60	319,092,000	314,357,000	1.51
70	307,473,000	302,738,000	1.56
80	295,854,000	291,119,000	1.63
90	284,235,000	279,500,000	1.69
100	272,616,000	267,881,000	1.77
110	260,997,000	256,262,000	1.85
120	249,378,000	244,643,000	1.94
130	237,759,000	233,024,000	2.03
140	226,140,000	221,405,000	2.14
150	214,521,000	209,786,000	2.26

## 6. Conclusions

An EB charging station consumes large amounts of power; hence, it is essential to arrange the charging schedules properly to minimize the energy cost. In the past, the contracted capacities were estimated by experience and the EBs usually began charging immediately after completing the transport service. These behaviors resulted in higher energy costs. A mathematical model used to minimize the energy cost by determining optimal charging schedules and contracted capacities while considering the operational guidelines of a bus company is presented herein. This paper takes a practical charging station as an example to verify the performance of the proposed model. Test results show that the controlled charging model can sharply reduce the EB charging station energy costs. In order to ensure the feasibility of investing in EB charging stations, an economic analysis model is proposed for the EB charging station project. Test results indicate that this project is beneficial for the bus company. Sensitivity analyses suggest that the parameter of operation revenue is the most significant factor. These analytic results are useful for bus companies to operate charging stations.

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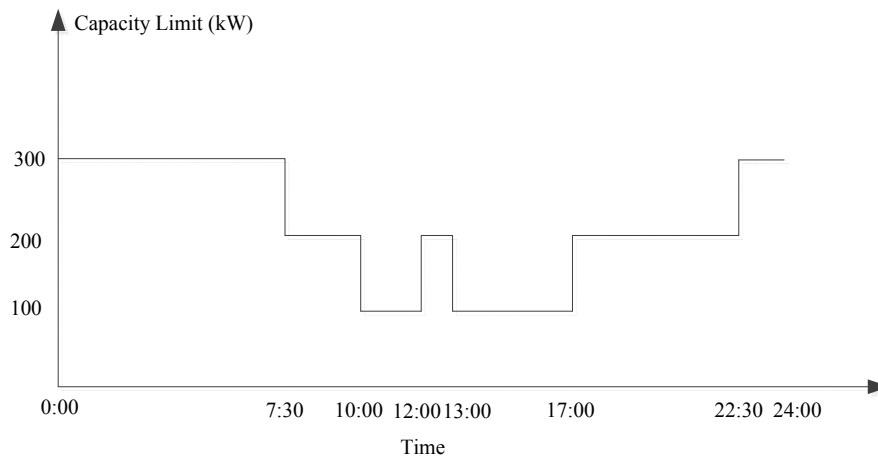
**Conflicts of Interest:** The authors declare no conflict of interest.

## Appendix A

The basic capacity charge is based on the contracted capacities. The large electricity users sign three types of contracted capacities with the Taiwan Power Company, i.e., the usual contracted capacity, half-peak contracted capacity, and off-peak contracted capacity. The usual contracted capacity has the most expense, but it can be used in all the time intervals. The off-peak contracted capacity has



the least expense, while it just can be used in the off-peak time period. The half-peak contracted capacity just can be used in the half-peak time period. The usual, half-peak, and off-peak contracted capacities are charged with NT\$223.6/kW, NT\$166.9/kW and NT\$44.7/kW per month, respectively, in the Taiwan Power Company. The time interval between 12:00 and 13:00 belongs to the half-peak time period, because it is the rest time at noon. If a charging station signs the usual contracted capacity 100 kW, half-peak contracted capacity 100 kW, and off-peak contracted capacity 100 kW with the power company, the capacity limit for this charging station is shown in Figure A1. The capacity limits for the peak, half-peak and off-peak time periods are 100 kW, 200 kW, and 300 kW respectively. According to Equation (1), the basic capacity charge is  $223.6 \times 100 + 166.9 \times 100 + 44.7 \times 0 = \text{NT\$}39,050$  per month.



**Figure A1.** Capacity limit at each time interval for the usual contracted capacity 100 kW, half-peak contracted capacity 100 kW, and off-peak contracted capacity 100 kW.

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