Measurement Error Estimation for Capacitive Voltage Transformer by Insulation Parameters

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Abstract: Measurement errors of a capacitive voltage transformer (CVT) are relevant to its equivalent parameters for which its capacitive divider contributes the most. In daily operation, dielectric aging, moisture, dielectric breakdown, etc., it will exert mixing effects on a capacitive divider’s insulation characteristics, leading to fluctuation in equivalent parameters which result in the measurement error. This paper proposes an equivalent circuit model to represent a CVT which incorporates insulation characteristics of a capacitive divider. After software simulation and laboratory experiments, the relationship between measurement errors and insulation parameters is obtained. It indicates that variation of insulation parameters in a CVT will cause a reasonable measurement error. From field tests and calculation, equivalent capacitance mainly affects magnitude error, while dielectric loss mainly affects phase error. As capacitance changes 0.2%, magnitude error can reach −0.2%. As dielectric loss factor changes 0.2%, phase error can reach 5′. An increase of equivalent capacitance and dielectric loss factor in the high-voltage capacitor will cause a positive real power measurement error. An increase of equivalent capacitance and dielectric loss factor in the low-voltage capacitor will cause a negative real power measurement error.

Keywords: capacitive voltage transformer (CVT); capacitive divider; insulation parameters; magnitude error; phase error

1. Introduction

A capacitive voltage transformer (CVT) is widely used in high-voltage (HV) and extra high-voltage (EHV) systems instead of a traditional voltage transformer (VT) [1,2]. A CVT’s structure can be mainly divided into a capacitive divider and an electromagnetic unit. A capacitive divider is comprised of an insulating cylinder and a series capacitors inside of it. An electromagnetic unit is comprised of a compensation reactor, a step-down transformer and a damper. A capacitive divider can first lower the system voltage as an input for an electromagnetic unit. By isolation and reduction of the step-down transformer, the low voltage signals can be used for protection and measurement. Compared with a VT, a CVT has the advantages of smaller size, lower cost, and refrain from ferroresonance [3–5]. However, the structure of a CVT is more complicated than a traditional VT which has more measurement accuracy influential parameters, therefore a CVT has more significant measurement error and a higher probability of insulation faults.

Existing research involves CVT measurement errors concerning various factors. Reference [6] uses PSCAD (power systems computer aided design) to simulate the measurement error of CVT under different harmonic conditions. References [7,8] propose a CVT circuit model in harmonic conditions. After simulations and experiments, a relationship between its equivalent parameters and harmonic...
transfer characteristics is obtained. Reference [9] establishes the steady state CVT circuit model with emphasis on the measurement error caused by system frequency and secondary burden change. Reference [10] focuses on the measurement error caused by hysteresis characteristics of the core. It proposes an algorithm that estimates the voltage across the capacitor and the reactor by considering the effect of the hysteresis characteristics of the core and adds it to the measured secondary voltage to obtain the correct voltage. References [11–13] use Maxwell to study the measurement error caused by space field. The conclusions are useful for CVT parameters optimization. Beside measurement errors, plenty of studies are focused on CVT transient response. Reference [14] uses ATP-EMTP (the alternative transients program) to study CVT transient response under both system faults and ferroresonance conditions. The result shows CVT transient response is significantly relevant with CVT component parameters and system conditions. Reference [15] also bases its study on ATP-EMTP simulation and designs an effective electronic ferroresonance circuit which proves to effectively suppress low voltage transients and high voltage ferroresonance oscillations. Reference [16] proposes a new method to reduce the impact of the transient response which is based on a least squares technique. After the case study, it shows this method can minimize the impact of CVT transients.

However, research on measurement errors of a capacitive voltage transformer caused by insulation parameters variation are rarely reported. The insulation parameters of a capacitive divider include equivalent capacitance, dielectric loss factor and surface leakage current. The measurement error of a CVT is directly relevant to a capacitive divider’s insulation parameters. As a capacitive divider is exposed to atmosphere, temperature, moisture, environmental contamination, and humidity it will exert mixing effects on its insulation characteristics, leading to equivalent parameters fluctuation and further resulting in the measurement error. In this paper, a comprehensive circuit model is proposed to characterize a CVT which involves both internal and external insulation characteristics. After simulation and experiments, the relationship between measurement errors and insulation characteristics is obtained.

2. Proposed CVT Circuit Model

The structure of a CVT is shown in Figure 1. $C_H$ is the high-voltage capacitor and $C_L$ is the low-voltage capacitor. $L$ is the compensation reactor which can be used to compensate the equivalent capacitance of a capacitive voltage divider. $T$ is the step-down transformer and $D$ is the damper.

The equivalent model of a CVT’s capacitive divider is actually not purely capacitive since it has inner insulation dielectric loss and outer surface leakage current. Taking these aspects into account, the proposed CVT circuit model is shown in Figure 2.

![Figure 1. Structure of capacitive voltage transformer (CVT).](image-url)
It is named as first, second, and third capacitor from bottom to the top in the voltage divider respectively. \(C_{11}, C_{12}, C_2\), and \(C_3\) are the equivalent capacitance of each segment, where \(C_{11}\), \(C_2\), and \(C_3\) belong to the high-voltage capacitor, and \(C_{12}\) belongs to the low-voltage capacitor. The main factors influencing equivalent capacitance are temperature and dielectric breakdown. Since a CVT capacitor has negative temperature coefficient, equivalent capacitance will decrease when temperature increases. Dielectric breakdown will cause a short circuit in series capacitors, which means equivalent capacitance will increase. \(R_{11}, R_{12}, R_{21}\), and \(R_{31}\) are the insulation resistances of each segment. Increase of the dielectric loss factor represents a decrease in insulating resistance. The main factors influencing insulation resistance are temperature and moisture in the insulation. When temperature increases, the dielectric loss of capacitor will first decrease and then increase. Therefore, the corresponding insulation resistance will first increase and then decrease. Moisture in the insulation will result in a larger dielectric loss, which means the insulation resistance will decrease. \(R_{13}, R_{22}\), and \(R_{32}\) are the surface equivalent resistances. Increase of leakage current represents decrease of surface resistance. The main factors influencing the surface resistance is environmental contamination and humidity. When contamination and humidity in the atmosphere increases, the surface leakage current of a capacitive divider will increase, which represents the decrease in surface resistance. The electromagnetic unit, \(L_k\), is the sum of compensation reactor reactance and leakage reactance of the transformer, which can be used to resonate with equivalent capacitance of the voltage divider \(C_0\), \(L_k = 1/(\omega^2 C_0)\). \(R_k\) is the sum of tuning reactor resistance and short circuit resistance of the transformer; \(Z_m\) is the excitation impedance of the transformer; \(Z_d\) and \(Z_L\) are the impedance of the damper and load which are recalculated to the primary side of the step-down transformer.

3. Theoretical Analysis of CVT Measurement Error

To simplify the analysis model, a high-voltage capacitor model and a low-voltage capacitor model are applied. In Figure 3, \(C_{11}\) and \(R_{11}\) are the equivalent capacitance and resistance of the high-voltage capacitor and \(C_k\) and \(R_k\) are the equivalent capacitance and resistance of the low-voltage capacitor. The Thevenin model of the capacitive divider is in Figure 4.
Assuming system voltage is $U_0$, the output voltage of the capacitive divider, $U_0$, can be expressed by Equation (1),

$$
\dot{U}_0 = \dot{U}_s \frac{1}{R_t + j\omega C_L + \frac{1}{R_H + j\omega C_H} + \frac{1}{R_L + j\omega C_L}}.
$$

Equation (1)

Substituting $\tan \delta = 1/(\omega CR)$ into Equation (1), $U_0$ can be expressed by equation (2),

$$
\dot{U}_0 = \dot{U}_s \frac{C_H \tan \delta_H + jC_H}{C_H \tan \delta_H + C_L \tan \delta_L + j(C_H + C_L)}.
$$

Equation (2)

$C_0$ and $R_0$ can be calculated from the capacitive divider equivalent model,

$$
C_0 = C_H + C_L + \frac{(C_H \tan \delta_H + C_L \tan \delta_L)^2}{C_H + C_L}
$$

Equation (3)

$$
R_0 = \frac{C_H \tan \delta_H + C_L \tan \delta_L}{\omega(C_H \tan \delta_H + C_L \tan \delta_L)^2 + \omega(C_H + C_L)^2}.
$$

Equation (4)

The circuit model of the electromagnetic unit is shown in Figure 5, which can be simplified to Figure 6, where $L_e$ and $R_e$ are separately the equivalent reactance and resistance of $Z_m$, $Z_d$, and $Z_L$.

$$
\text{Figure 3. Capacitive divider equivalent model.}
$$

$$
\text{Figure 4. Thevenin model of the capacitive divider.}
$$

$$
\text{Figure 5. Circuit model of the electromagnetic unit.}
$$

$$
\text{Figure 6. Simplified circuit model of the electromagnetic unit.}
$$
Combining Figures 4 and 6, the CVT equivalent model is shown in Figure 7.

![Figure 6. Equivalent model of the electromagnetic unit.](image)

![Figure 7. Equivalent model of the capacitor voltage transformer.](image)

The output voltage of CVT \( U' \) which is recalculated to the primary side of the step-down transformer can be expressed by Equation (5),

\[
\dot{U}' = \dot{U}_0 \cdot \frac{R_e + j\omega L_e}{1/j\omega C_0 + R_0 + j\omega L_k + R_k + j\omega L_e + R_e}.
\]

Since the main focus of this paper is on the relationship between measurement error and insulation characteristics, \( R_k + j\omega L_k \) and \( R_e + j\omega L_e \) can be treated as constant. If \( R_k + j\omega L_k \) is marked as \( Z_k \), and \( R_e + j\omega L_e \) is marked as \( Z_e \), Equation (5) can be simplified to Equation (6),

\[
\dot{U}' = \dot{U}_k \cdot \frac{Z_e}{Z_k + Z_e + \frac{[Z_k + Z_e] j\omega C_L \tan \delta_L + j\omega C_H] + 1}.
\]

Assuming the voltage ratio of the step-down transformer is \( N \), the output voltage can be expressed by Equation (7),

\[
\dot{U} = \frac{\dot{U}'}{N}.
\]

It can be concluded from Equations (6)–(7) that measurement error of the CVT is relevant with \( C_H \), \( \tan \delta_H \), \( C_L \), \( \tan \delta_L \). Increase of \( C_H \) and \( \tan \delta_H \) will cause a positive magnitude error while increase of \( C_L \), \( \tan \delta_L \) will cause a negative magnitude error. Increase of \( \tan \delta_H \) will cause a negative phase error while increase of \( \tan \delta_L \) will cause a positive phase error. Increase of \( C_H \) and \( C_L \) will both cause a negative phase error.

### 4. Simulation of Measurement Error with Various Insulation Parameters

Since the parameters of a capacitive divider change more significantly than those of an electromagnetic unit in daily operation, the parameters of an electromagnetic unit and load are assumed unchanged in simulation. Assuming external leakage current is 0, the relationship between measurement error and insulation parameters can be obtained as the dielectric loss factor and equivalent capacitance of each capacitor are changed. Figure 8 shows the simulation model of CVT and Table 1 shows the equivalent parameters of the CVT, where parameters of the ferroresonance damping circuit and the load are recalculated to the primary side of the step-down transformer. And the voltage ratio \( N \) of the step-down transformer is 330.
4.1. CVT Measurement Error with Different Dielectric Loss Factor

To avoid the measurement error caused by change of equivalent capacitance, the equivalent capacitance of the capacitive divider is set as constant according to Table 1. When the individual capacitor’s dielectric loss factor changes, the dielectric loss factor of other capacitors remain 0.05%. CVT phase and magnitude error with different dielectric loss factors are shown in Figures 9 and 10.

It can be concluded, that dielectric loss factor mainly affects the phase error. Measurement error caused by dielectric loss factor change in the second and third capacitor is totally the same. Increase of dielectric loss in the second, third, and upper half of the first capacitor will cause a negative phase error and positive magnitude error. Increase of dielectric loss in the lower half of the first capacitor will cause a positive phase error and negative magnitude error.
It can be concluded that equivalent capacitance mainly affects the magnitude error. Measurement error caused by change of the dielectric loss factor, the dielectric loss factor of each capacitor is fixed to 0.05%. When individual capacitor’s equivalent capacitance varies, the equivalent capacitance of other capacitors remains unchanged. CVT measurement error with different equivalent capacitance is shown in Figures 11 and 12.

To avoid the measurement error caused by change of the dielectric loss factor, the dielectric loss factor of each capacitor is fixed to 0.05%. When individual capacitor’s equivalent capacitance varies, the equivalent capacitance of other capacitors remains unchanged. CVT measurement error with different equivalent capacitance is shown in Figures 11 and 12.

It can be concluded that equivalent capacitance mainly affects the magnitude error. Measurement error caused by equivalent capacitance change in the second and third capacitor is exactly the same. Increase of equivalent capacitance in the second, third, and upper half of first capacitor will cause a negative phase error and positive magnitude error. Increase of equivalent capacitance in the lower half of the first capacitor will cause a negative phase error and negative magnitude error.

4.2. CVT Measurement Error with Different Equivalent Capacitance

To avoid the measurement error caused by change of the dielectric loss factor, the dielectric loss factor of each capacitor is fixed to 0.05%. When individual capacitor’s equivalent capacitance varies, the equivalent capacitance of other capacitors remains unchanged. CVT measurement error with different equivalent capacitance is shown in Figures 11 and 12.

It can be concluded that equivalent capacitance mainly affects the magnitude error. Measurement error caused by equivalent capacitance change in the second and third capacitor is exactly the same. Increase of equivalent capacitance in the second, third, and upper half of first capacitor will cause a negative phase error and positive magnitude error. Increase of equivalent capacitance in the lower half of the first capacitor will cause a negative phase error and negative magnitude error.
with the power factor of the system. If the power factor \( \cos \) can be calculated. CVT real power measurement error under various insulation parameters can be calculated. CVT real power measurement error of the CVT can be expressed by Equation (9),

\[
W\% = \frac{K_n U I \cos \theta_2 - U_s I \cos \theta_1}{U_s I \cos \theta_1} \times 100\%. \tag{8}
\]

Substituting \( \epsilon\% = \frac{(K_n U - U_s)}{U_s} \times 100\% \) and \( \theta = \theta_2 - \theta_1 \) into Equation (8), the real power measurement error of the CVT can be expressed by Equation (9),

\[
W\% = [(1 + \epsilon) \cos \theta - (1 + \epsilon) \sin \theta \tan \theta_1 - 1] \times 100\%. \tag{9}
\]

It can be seen from Equation (9) that the power measurement error of the CVT is also relevant with the power factor of the system. If the power factor \( \cos \theta_1 \) is set to 0.8 lagging, the real power measurement error under various insulation parameters can be calculated. CVT real power measurement error with different dielectric loss factor and equivalent capacitance are shown in Figures 13 and 14.
measurement error with different dielectric loss factor and equivalent capacitance are shown in Figures 13 and 14.

![Graphical representation of error measurement](image)

**Figure 13.** CVT real power measurement error with different dielectric loss factor.

![Graphical representation of error measurement](image)

**Figure 14.** CVT real power measurement error with different equivalent capacitance.

5. **Experiment**

Since the dielectric loss factor of a real CVT is hard to arbitrarily change, in order to better study the relationship between CVT measurement error and insulation parameters with experiments, a low-voltage CVT model is proposed. The structure of the CVT model is shown in Figure 15. Series connected capacitors are put inside an insulation cylinder to simulate the capacitive divider, and series connected resistors are in parallel with the capacitors to represent the equivalent resistive current by dielectric loss. The electromagnetic unit is equaled by the compensation reactor and the step-down transformer both having equivalent parameters. In experiment, the dielectric loss factor of the capacitive divider can easily be altered by adjusting the resistors. Phase and magnitude error of the CVT can be measured by a Lecory HDO6104 12-bit high precision oscilloscope by comparing the voltage of the CVT model and a 3 kV high accuracy class 0.1 reference VT.

The real picture of low-voltage CVT model is shown in Figure 16. CVT experiment wiring diagram is shown in Figure 17.
5.1. CVT Measurement Error with Various High-Voltage Capacitor Dielectric Loss Factor

In order to eliminate the measurement error caused by dielectric loss factor change in the low-voltage capacitor, the low-voltage capacitor is fixed to 100 nF with no parallel resistance. The dielectric loss factor of low-voltage capacitor is 0.012% which can be measured with a dielectric loss meter. The high-voltage capacitor is fixed to 25 nF. The dielectric loss factor of the high-voltage capacitor with different parallel resistance is shown in Table 2.
The high-voltage capacitor is fixed to 25 nF. The dielectric loss factor of the high-voltage capacitor with different parallel resistance is shown in Table 2.

<table>
<thead>
<tr>
<th>Capacitance $C_H$/nF</th>
<th>Resistance $R_H$/MΩ</th>
<th>Dielectric Loss Factor (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>25</td>
<td>150</td>
<td>0.095</td>
</tr>
<tr>
<td>25</td>
<td>120</td>
<td>0.115</td>
</tr>
<tr>
<td>25</td>
<td>90</td>
<td>0.151</td>
</tr>
<tr>
<td>25</td>
<td>60</td>
<td>0.223</td>
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<tr>
<td>25</td>
<td>30</td>
<td>0.434</td>
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<tr>
<td>25</td>
<td>20</td>
<td>0.648</td>
</tr>
<tr>
<td>25</td>
<td>15</td>
<td>0.859</td>
</tr>
</tbody>
</table>

The testing voltage is 0.8, 1, and 1.2 of rated voltage (3 kV). Measurement error under various dielectric loss of the high-voltage capacitor is shown in Figures 18 and 19.

Figure 18. CVT phase error with different high-voltage capacitor dielectric loss factor.

Figure 19. CVT magnitude error with different high-voltage capacitor dielectric loss factor.

Plots in Figures 18 and 19 coordinate with regulations obtained from simulation. When the dielectric loss factor of high-voltage capacitor increases, the phase error is increasing in the negative direction while magnitude error is increasing in the positive direction.
5.2. CVT Measurement Error with Various Low-Voltage Capacitor Dielectric Loss Factor

In order to eliminate the measurement error caused by dielectric loss factor change in the high-voltage capacitor, the high-voltage capacitor is fixed to 25 nF with no parallel resistance. The dielectric loss factor of the high-voltage capacitor is 0.012% which can be measured by a dielectric loss meter. The low-voltage capacitor is fixed to 100 nF. The dielectric loss factor of the low-voltage capacitor with different parallel resistances is shown in Table 3.

<table>
<thead>
<tr>
<th>Capacitance $C_L$/nF</th>
<th>Resistance $R_L$/M$\Omega$</th>
<th>Dielectric Loss Factor (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>60</td>
<td>0.064</td>
</tr>
<tr>
<td>100</td>
<td>30</td>
<td>0.118</td>
</tr>
<tr>
<td>100</td>
<td>20</td>
<td>0.172</td>
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<tr>
<td>100</td>
<td>15</td>
<td>0.224</td>
</tr>
<tr>
<td>100</td>
<td>12</td>
<td>0.276</td>
</tr>
<tr>
<td>100</td>
<td>10</td>
<td>0.330</td>
</tr>
</tbody>
</table>

Plots in Figures 20 and 21 coordinate with regulations obtained from simulation. When the dielectric loss factor of the low-voltage capacitor increases, the phase error is increasing in the positive direction while magnitude error is increasing in the negative direction. However, since the insulation parameters in the simulations and experiments are different, the specific value in experiments is not the same as in the simulations.

Figure 20. CVT phase error with different low-voltage capacitor dielectric loss factor.

Figure 21. CVT magnitude error with different low-voltage capacitor dielectric loss factor.
6. Conclusions

This paper proposes an equivalent circuit model to represent a CVT which incorporates the insulation characteristics of a capacitive divider. This simulation model can reflect the measurement error change caused by insulation parameters fluctuation. In order to verify the simulation results, a low-voltage CVT experimental model is proposed. After software simulations and laboratory experiments, the relationship between measurement error and insulation parameters is obtained.

Conclusions are as following. These conclusions are all straightforward in judging how the measurement error of the CVT will change according to the variation of insulation parameters and whether a certain CVT has the possibility to exceed the measurement error limit.

1. Insulation parameters fluctuation of the CVT’s capacitive divider can contribute a fairly large measurement error. Equivalent capacitance fluctuation mainly affects magnitude error, while dielectric loss factor mainly affects phase error. When equivalent capacitance changes 0.2%, magnitude error can reach $-0.2\%$. When dielectric loss factor changes 0.2%, phase error can reach $5'$.

2. An increase of equivalent capacitance in the high-voltage capacitor will cause a positive magnitude error while that in the low-voltage capacitor will cause a negative magnitude error. An increase of dielectric loss factor in the high-voltage capacitor will cause a negative phase error while that in the low-voltage capacitor will cause a positive phase error.

3. An increase of equivalent capacitance and dielectric loss factor in the high-voltage capacitor will cause positive real power measurement error. An increase of equivalent capacitance and dielectric loss factor in the low-voltage capacitor will cause negative real power measurement error.

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Author Contributions: Lin Du, Bin Chen and Feng Yang developed the theory and performed the simulation. Kun Liu, Xianshun Chen and Fuzhou Zhang carried out the experiments. Bin Chen and Lin Du analyzed the data and wrote the paper.

Conflicts of Interest: The authors declare no conflict of interest.

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