An Entropy-Based Adaptive Hybrid Particle Swarm Optimization for Disassembly Line Balancing Problems

Shanli Xiao, Yujia Wang *, Hui Yu and Shankun Nie

School of Electronic and Electrical Engineering, Shanghai University of Engineering Science, 333 Long Teng Road, Shanghai 201620, China; shanli0681@163.com (S.X.); yuhui0113@163.com (H.Y.); nieshankun2012@163.com (S.N.)
* Correspondence: yjwangamber@sues.edu.cn; Tel.: +86-21-6779-1126
Received: 8 August 2017; Accepted: 3 November 2017; Published: 7 November 2017

Abstract: In order to improve the product disassembly efficiency, the disassembly line balancing problem (DLBP) is transformed into a problem of searching for the optimum path in the directed and weighted graph by constructing the disassembly hierarchy information graph (DHIG). Then, combining the characteristic of the disassembly sequence, an entropy-based adaptive hybrid particle swarm optimization algorithm (AHPSO) is presented. In this algorithm, entropy is introduced to measure the changing tendency of population diversity, and the dimension learning, crossover and mutation operator are used to increase the probability of producing feasible disassembly solutions (FDS). Performance of the proposed methodology is tested on the primary problem instances available in the literature, and the results are compared with other evolutionary algorithms. The results show that the proposed algorithm is efficient to solve the complex DLBP.

Keywords: DLBP; DHIG; entropy; population diversity; AHPSO; dimension learning; crossover and mutation operator

1. Introduction

Disassembly line balancing problem (DLBP) is an efficient method for minimizing resources invested in disassembly and maximizing the automation level [1]. However, the DLBP is not only a complex system but also a NP-hard combination optimization problem [2]. How to effectively solve the DLBP is an important problem in the engineering and manufacturing fields. Some researchers obtain the disassembly sequence using the mathematical programming method in which a single object is considered [3,4], but it is easily to fall into the local optimal when the method is applied to solve the complex DLBP. In order to gain the optimal disassembly solutions, many algorithms based on the heuristic rules are proposed in recent years.

Altekin et al. [5] firstly used the mixed integer programming formulation to solve the DLBP. The ant colony optimization (ACO) for DLBP with multiple objectives was proposed by McGovern and Gupta, but the objective functions were in priority order based on the economic interests [6]. Closing to the entire production process, the mathematic model of DLBP was successfully designed [6,7]. A novel multi-objective ant colony optimization (MOACO) algorithm was used to solve DLBP and obtained good benefit in the practice of disassembly process [7]. Kalayci and Gupta adopted simulated annealing (SA) [8], particle swarm optimization (PSO) with local search procedure [9], variable neighborhood search (VNS) [10], and artificial bee colony (ABC) [11] to solve the DLBP, the optimal solutions showed the validity of algorithms. Karadag and Turkbey [12] proposed a new genetic algorithm (GA) for solving the multi-objective stochastic DLBP. Paksoy et al. [13] used the binary fuzzy goal programming (BFGP) to solve a mixed model of DLBP. In the last few years, Kalayci et al. have done a tremendous amount of research in this area and proposed some several
heuristic methods for sequence-dependent DLBP such as ACO [14], PSO [15], ABC [16] and a hybrid algorithm based on GA and VNS [17].

With the increase of the problem scale, the traditional algorithms need much more time to solve the explosive growth of solution space. In this paper, we propose an entropy-based AHPSO algorithm to solve the DLBP. Multi-objective swarm optimization (MOPSO) is a popular multi-objective heuristic method. In contrary to single-objective optimization, there are many solutions when solving multi-objective optimization problem, so it is difficulty to select the best solutions. In this case, the non-dominated solution is that at least one of objective value is better or equal to the others. The external archive is used to store the non-dominated solutions, and the crowding distance (GD) [18] is responsible for deciding if a solution should be added to external archive. In the MOPSO, we need to select the particle’s non-dominated solution as its own historical best position (pbest) and the non-dominated solution of population has got so far as the global optimal position (gbest) when updating the position of the particle. The iteration speed of MOPSO is fast which could make it fall into local optimum easily. The crossover and mutation operation are helpful in this case which not only increase diversity of the particles but also affect the design variables [19].

In this paper, the improved comprehensive learning strategy [20] and the crossover and mutation operation are embedded in the proposed algorithm to avoid falling into the local optimum. In addition, the entropy is introduced to select the exemplar particles that contribute to the velocity updating and solve the potential degradation caused by the fixed crossover rate and mutation rate. The learning strategies incorporated in the proposed algorithm are as follows:

1. The disassembly hierarchy information graph (DHIG) is introduced into the solution representation to make the real values apply on the permutation of tasks, which makes the DLBP transform into a problem of searching optimum path in the directed and weighted graph.

2. In the proposed algorithm, the selection of the particle with good diversity, crossover rate and mutation rate are depended on the change of the entropy. This can increase the number of the optimal solutions and improve the speed of convergence.

3. The particle with good diversity is added to standard particle swarm velocity update formula, and we propose an improved comprehensive learning strategy, called dimension learning. The particle learns from the gbest of the swarm, its own pbest and the particle with good diversity. In this version, some dimensions are randomly chosen to learn from the gbest. Some of the remaining dimensions are randomly chosen to learn from the particle with good diversity and the remaining dimensions learn from its own pbest, thus making the particles diverse enough for getting the optimal solutions.

The rest of the paper is organized as follows: in Section 2, notations used in this paper are presented. Problem definition and mathematical model of DLBP are given in Section 3. Section 4 introduces the entropy-based AHPSO for the DLBP with multi-objective. The results to evaluate its validity on the benchmark instances and practical example are showed in Section 5. Finally, some conclusions are illustrated in Section 6.

2. Notation

- $CT$ Working cycle of the workstation.
- $ti$ Removal time of $i^{th}$ part.
- $t'i$ Total part removal time requirement in $i^{th}$ workstation.
- $n$ Number of parts for removal.
- $m$ Number of workstations.
- $m^*$ Minimum value of $m$.
- $i, j$ Part identification, part count ($1, \ldots, n$).
- $k$ Workstation count ($1, \ldots, m$).
- $N$ The set of natural numbers.
- $PSi$ $i^{th}$ part in a solution sequence.
- $di$ Demand; quantity of part $i$ requested.
Binary value; (the binary variable is 1 if the part is hazardous, else zero).

\[ h_i = \begin{cases} 1, & \text{if part } i \text{ immediately precedes part } j \\ 0, & \text{otherwise} \end{cases} \]

\[ X_{ij} = \begin{cases} 1, & \text{if part } i \text{ immediately precedes part } j \\ 0, & \text{otherwise} \end{cases} \]

\[ Y_{ik} = \begin{cases} 1, & \text{if } j^k \text{ part is assigned to the } k^k \text{ station} \\ 0, & \text{otherwise} \end{cases} \]

### 3. DLBP Definition and Formulation

The model of DLBP is satisfied with four objectives in this paper and the precedence relationships among the tasks are AND type [2]. The equations of DLBP are given as follows:

\[
\begin{align*}
\min f_1 &= m \\
\min f_2 &= \sum_{i=1}^{m} [CT - t_i]^2 \\
\min f_3 &= \sum_{i=1}^{n} (i \times h_{ps_i}), \quad h_{ps_i} = \begin{cases} 1, & \text{hazardous} \\ 0, & \text{otherwise} \end{cases} \\
\min f_4 &= \sum_{i=1}^{n} (i \times d_{ps_i}), \quad d_{ps_i} \in N, \forall PS_i
\end{align*}
\]

Subject to:

\[
\begin{align*}
\sum_{i=1}^{m} Y_{i} &= 1, \, j = 1, 2, \ldots n \\
\left[ \sum_{i=1}^{n} t_i \right] &\leq m' \leq n \\
Y_{ik} &\leq \sum_{k=1}^{m} Y_{ik}, \forall (i, j) \in IP
\end{align*}
\]

where Equation (1) is used to minimize the number of workstations in one cycle for saving the manpower, material and financial resources. Equation (2) ensures that idle times at each workstation are similar. Equation (3) illustrates that the hazardous parts should be removed as early as possible. Equation (4) is designed to satisfy the need of production. Equation (5) guarantees that each task is only to be assigned at least and at most a workstation and a task cannot be separated to operate on different workstations. Equation (6) assures that the operating time of all workstations do not exceed the permitted working cycle. The constraint in the Equation (7) ensures that the precedence relations among the tasks are not violated.

### 4. Proposed Algorithm for Solving DLBP

#### 4.1. Solution Representation

In this paper, we use the improved AHPSO to obtain the optimal solutions with the multi-objective function. In order to make the real values apply on the permutation of tasks, each dimension of particle is a random number between (0, 1) to determine the disassembly priority. Based on the priority and zero in-degree [21], the disassembly hierarchy information graph (DHIG) is presented. Take the process of disassembly of five tasks as the example to illustrate above procedure:

Step 1: Generate five (as many as the number of the tasks) random numbers between (0, 1).
Step 2: Select the tasks with zero in-degree in topological sorting as the candidate set based on the precedence graph.
Step 3: If the candidate task set is null, go to step 5.
Step 4: Select the task with the highest disassembly priority from the candidate task set to disassembly and remove the task from the precedence graph; go back to step 2.

Step 5: Output the FDS.

The reverse approach is performed to transform the FDS into the continuous representation for updating the proposed algorithm. We need to generate random numbers between (0, 1) as many as the number of tasks, then these numbers are sorted and placed to the column of task selection priority based on the FDS. Figure 1 shows the conversion process between the continuous representation and permutation-based disassembly sequence.

![Figure 1. The conversion process between the continuous representation and permutation-based disassembly sequence.](image)

### 4.2. Introduction of Entropy

Combining the characteristic of FDSs, two parameters of individual-dimension-entropy and population-distribution-entropy are introduced into the proposed algorithm to balance the trade-off between exploration and exploitation. Suppose that the number of FDSs is NUM, particle dimension (D) is equal to n, R_i represents a set including the j-th elements of all FDSs, b_j is the number of duplicate values in the R_i and P_i = 1/b_j. Relevant definitions are as follows.

**Definition 1.** The individual-dimension-entropy (M) is introduced to assess the diversity of corresponding particle and the larger M is the more diversities the particle has. The particle with good diversity is denoted by pbest. The calculation formula is as follows:

\[
M_i = \sum_{j=1}^{D} \frac{P_i}{b_j} \log \frac{1}{P_i} \quad (i \in \text{NUM}, \ j \in \text{D})
\]  

(8)

**Definition 2.** The population-distribution-entropy (H) can be introduced to reflect the diversity and evolutionary status of the population, which is defined as Equation (9):

\[
H = \frac{1}{D} \sum_{i=1}^{D} \sum_{j=1}^{\text{NUM}} \frac{P_i}{b_j} \log \frac{1}{P_i} 
\]

(9)

### 4.3. Dimension Learning

Each dimension of particle in mostly improved PSO is updated as show in Figure 2 [22]. The updating method of corresponding to the particle dimension maybe make some particles get into the local optimum [23]. In order to improve the spatial search ability of the particle, the dimension learning strategy that different dimensions of the particle have different learning objects is adopted. The process is shown in Figure 3 where the pbest is added to further enhance the diversity of information between particles. p_a and p_c are applied to determine the number of the particle
dimensions that learn from gbest, pbest and pbest_{bin}, respectively. The improved velocity update formula is given in Equation (10):

\[
\begin{align*}
    v_{i,j}(t+1) &= wv_{i,j}(t) + c_{1} \cdot \text{rand}((\text{pbest}_{i,j}(t) - x_{i,j}(t)) + c_{2} \cdot \text{rand}((\text{gbest}_{i,j}(t) - x_{i,j}(t))) \\
    x_{i,j}(t+1) &= x_{i,j}(t) + v_{i,j}(t)
\end{align*}
\]  

(10)

where c1, c2 and c3 are the learning factor of the particle tracking the pbest, gbest and pbest_{bin} respectively. \(r_1\) and \(r_2\) are uniform random number in the interval [0, 1], and \(w\) is an inertia weight.

\[p_{c} = \frac{p_{c1} H + p_{c2} (\log_{2} NUM - H)}{\log_{2} NUM} \]  

(11)

\[p_{m} = \frac{p_{m1} H + p_{m2} (\log_{2} NUM - H)}{\log_{2} NUM} \]  

(12)

where, the maximum and minimum probability of crossover and mutation are as follows: \(p_{c1}, p_{c2}, p_{m1}\) and \(p_{m2}\). In this study, the one-point crossover [24] and shift mutation operator [25] are used to produce the new disassembly solutions while satisfying the precedence constraints. For the implement of the one-point crossover, the two FDSs are need. Here, FDS.1 and FDS.2 are randomly selected to illustrate the crossover operation. The procedure is as follows: Firstly select a cut point in the FDSs in order to divide the FDSs into two parts and do not change the positions of the tasks before the cut position. Then, remove the tasks before the cut position in the FDS.1 from the FDS.2 whereas the tasks that are front of the cut point in the FDS.2 are removed from the FDS.1. Lastly, reconstruct two new solutions by recombining the tasks before the cut position in the FDS.1 with the remaining tasks of FDS.2 and placing the remaining tasks of FDS.1 behind the cut point in the FDS.2. The shift mutation operator is defined by randomly selecting a task in the disassembly sequence and inserting it to another randomly selected position based on the precedence matrix. By comparing the domination ability between the new solutions and current solutions, the winner will be converted to
continuous representation (see Section 4.1) and replace the current particle to next generation. Examples for the one-point crossover and shift mutation operator are given in Figures 4 and 5.

![Figure 4. Applying the one-point crossover to assign five-part example.](image1)

![Figure 5. Applying the shift mutation operator to assign five-part example.](image2)

4.5. The Regeneration of the Particles

From a single run, the improved algorithm could obtain a set of non-dominated solutions that are used to be stored by external archive. In this paper, the size of external archive is equal to the population size and controlled by the crowding distance (CD) [18]. The obtained non-dominated solutions are converted to continuous representation as it is mentioned in Section 4.1, then considered as the pbest. If the number of non-dominated solutions is less than the population size, we will randomly select the FDSs from the external archive and take them on order crossover operation [26] for production new solutions.

There are two factors that influence the selection of gbest, that is, CD and grid density (GD) [27]. More specifically, the non-dominated solution with minimal values about the two indexes will be converted to continuous representation and then selected as the gbest.

4.6. Algorithm Procedure for DLBP

The entire optimization procedure of proposed algorithm is repeated until the maximum generation has reached.

Step 1: Set NUM, T_max, CT, D, w, c_1, c_2, c_3, pbest, gbest, pbest_{best}, P_r, P_{n}, P_{a1}, P_{a2}, P_{p1}, P_{p2}.

Step 2: Built the DHIG in order to calculate the individual-dimension-entropy and the population-distribution-entropy by Equations (8) and (9), respectively. Then, select pbest_{best} and calculate the values of P_r and P_{p}.

Step 3: Update the position of particles by Equation (10).

Step 4: Evaluate the objective functions.

Step 5: Adopt self-adaptive crossover and mutation operator to create better solutions.

Step 6: Update the external archive.

Step 7: Convert the non-dominated solution to the continuous representation and replace with pbest for use at the next generation.

Step 8: Make sure the position of the gbest according to the values of CD and GD.

Step 9: If T > T_{max}, go to step 10; else, go back to step 2.

Step 10: Output optimal disassembly solutions.

The above-mentioned procedure of the AHPSO with entropy for DLBP is just like the Figure 6.
5. Numerical Results

5.1. Test for Benchmark Functions

The DTLZ1 and DTLZ2 are used to verify the effectiveness of the multi-objective optimization algorithms. In order to show the motivation of the entropy, we make a comparison between the AHPSO without entropy and AHPSO with entropy in this section. The parameters of algorithms are listed in Table 1 and both algorithms are executed 30 times.

The Pareto optimal fronts obtained by both algorithms for solving the DTLZ1 and DTLZ2 are shown in Figures 7 and 8, respectively. Generational Distance (GD), Spacing (SP) and Maximum Spread (MS) are used to measure the convergence and the coverage, respectively [28]. Table 2 lists the values of GD, SP and MS.

<table>
<thead>
<tr>
<th>Table 1. Parameters setting.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Type</strong></td>
</tr>
<tr>
<td>The particle with</td>
</tr>
<tr>
<td>good diversity</td>
</tr>
<tr>
<td>Crossover rate and</td>
</tr>
<tr>
<td>mutation rate</td>
</tr>
<tr>
<td>Inertia weight</td>
</tr>
<tr>
<td>Learning factor</td>
</tr>
<tr>
<td>The size of external archive</td>
</tr>
<tr>
<td>( NUM )</td>
</tr>
<tr>
<td>( p_c ) ( p_m )</td>
</tr>
<tr>
<td>( D )</td>
</tr>
<tr>
<td>( T_{max} )</td>
</tr>
</tbody>
</table>
As can be seen from the Figure 7, both algorithms can converge to the Pareto optimal solutions, but the AHPSO with entropy is better than AHPSO without entropy in terms of the distribution of the solutions. The statistical results in Table 2 show that AHPSO with entropy has good performance when dealing with the DTLZ1 test problem. In the Figure 8a, we can get that the Pareto optimal solutions obtained by AHPSO without entropy on DTLZ2 can’t converge to the true Pareto optimal front. The AHPSO with entropy, however, shows high convergence. The values of GD, SP and MS (see Table 2) evidence that the proposed algorithm can solve the multi-objective problems well. This is due to updating mechanism of improved algorithm based on the entropy, which can measure the changing tendency of population diversity in real-time.

5.2. Applied Examples

After a set of experiments, the best performing parameter set is determined to be $NUM=100$ (population size), $NP=100$ (the size of external archive), $T_{\text{max}}=300$, $w = 0.729$, $p = 0.1$, $p_s = 0.4$, $c_1 = c_2 = c_3 = 2$, $p_{v_1} = 0.9$, $p_{v_2} = 0.4$, $p_{v_3} = 0.4$, $p_{v_4} = 0.05$ and these are used in benchmark instances and practical example.

Case 1: in this paper, we use a set of benchmark instances to confirm the effectiveness of improved algorithm for DLBP. The size of 19 benchmark instances increases gradually from 8 to 80. 

### Table 2. The values of GD, SP and MS on the DTLZ1 and DTLZ2.

<table>
<thead>
<tr>
<th>Performance Metric</th>
<th>AHPSO without Entropy</th>
<th>AHPSO with Entropy</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>GD $5.1445 \times 10^{-4}$</td>
<td>$1.3342 \times 10^{-4}$</td>
</tr>
<tr>
<td>DTLZ1</td>
<td>SP 0.0055</td>
<td>0.0042</td>
</tr>
<tr>
<td></td>
<td>MS 0.9878</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>GD $3.701 \times 10^{-4}$</td>
<td>$2.403 \times 10^{-4}$</td>
</tr>
<tr>
<td>DTLZ2</td>
<td>SP 0.0063</td>
<td>0.0045</td>
</tr>
<tr>
<td></td>
<td>MS 0.9842</td>
<td>0.9967</td>
</tr>
</tbody>
</table>
in steps of 4 and each workstation has got 26 s at most to fulfill its task. Removal time of each part is to be gained by the Equation (13). In addition, McGovern and Gupta set up that only the last part possessing removal time of 11 is hazardous and only the last part holding removal time of 7 is demanded [6]. Known optimal results are \( f_i = i + 1 \) \((i = 1, 2, \ldots, 19)\), \( f_i = 0 \), \( f_i = 1 \), \( f_i = 2 \) and the immediately preceding matrix \([X_i]_{ee}\) of each benchmark instance is an empty set [6].

\[
t_i = \begin{cases} 
3.0 & \text{if } i \leq \frac{n}{4} \\
5.0 & \text{if } \frac{n}{4} < i \leq \frac{n}{2} \\
7.0 & \text{if } \frac{n}{2} < i \leq \frac{3n}{4} \\
11.0 & \text{if } \frac{3n}{4} < i \leq n 
\end{cases} 
\]

(13)

This paper optimizes multi-objective simultaneously rather than based on the precedence relation between objectives. In order to compare with the DLBP ACO [6], the improved algorithm is run three times to obtain the average results and the results are evaluated in two aspects as follows:

(1) Based on prioritization of multi-objective.
(2) Optimize the objectives simultaneously.

The minimum number of workstations on the first four benchmark instances obtained by the proposed algorithm agrees well with the theoretical values. In the wake of increase in the number of tasks, we get the optimal solutions with \( i + 2 \) workstations. The comparisons of the average results based on aspect (1) and aspect (2) are given in Figure 9, where the two curves, Data.1 and Data.2, are the average measure of the solutions based on aspect (1) and aspect (2), respectively.

From Figure 9a we can see that two curves overlap well, almost on the same line, and the computational results relating to the number of workstation are better than ACO algorithm, which got the solutions with \( i + 2 \) workstations. Compared to Data.1 on the range of instance from 1th to 14th, the value of Data.2 is little higher but the performance of proposed algorithm is improved when it is used to solve instances with large size (after 14th instance, the values of Data.2 is declining).

Figure 9b shows the relation between the average balance measure and the number of task. On the whole process of 19 instances, it can be seen from Data.1 that the balance measure increases from 0 to 145.43 and then decreases until it reaches to 38.26. At the same time, the Data.2 shows a downward trend, from 180 to 39.14. After 5th instance, the values of Data.2 are less than or equal to Data.1. The balance measure on the first benchmark instance obtained by McGovern and Gupta was up to 300, the minimum value was about 48. According to the analysis above, we can draw a conclusion that the proposed algorithm can acquire the satisfying results which no matter what in the aspect of basing on prioritization of multi-objective and optimizing the objectives simultaneously.

In Figure 9c, the maximal hazard measure of Data.2 is about 18 and the hazard measure is improved that overall values of Data.2 are lower in comparison with Data.1. Especially after 16th instance, the variation tendency of Data.2 decreases rapidly. We can get that the superiority of improved algorithm is much more obvious for large-size DLBP. In the ACO algorithm, the hazard measure is sub-optimally placed so it will not change if the balance measure is affected. Beyond that, it is a disappointing that hazard measure of ACO is up to around 28.

From Figure 9d, we can learn that the values of demand measure of Data.2 on the first two instances are higher than that of Data.1 but the Data.2 has a significantly lower than Data.1 with the increasing number of task. As for the ACO algorithm, the demand measure is inferior to the Data.1.

Figure 9a,b could not reflect the obvious superiority of the improved algorithm. However, hazard measure and demand measure have remarkable improvement, especially in large-size instance (as seen from Figure 9c,d). In addition, the results of the experiment show that proposed algorithm has good stability on the DLBP.
Figure 9. The comparisons of the average results on different measures (a) Number of workstations; (b) Balance measure; (c) Hazard measure; (d) Demand measure.

Case 2: A cellular telephone instance with 25-part (see Figure 10) defined by Gupta and McGovern [29] is used to verify the performance of the proposed algorithm. The CT is set 18 s and other knowledge databases are as follows:

- The removal times are set to \( t = [3, 2, 3, 10, 10, 15, 15, 15, 15, 2, 2, 2, 2, 2, 2, 2, 3, 18, 5, 1, 5, 15, 2, 2] \);
- The hazard values are quantified to \( h = [1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0] \);
- Demands are set to \( d = [4, 7, 1, 1, 1, 1, 1, 2, 1, 4, 1, 1, 1, 1, 2, 2, 8, 1, 4, 6, 7, 1, 4] \).

Figure 10. Precedence relationships for cellular telephone.
The proposed algorithm is compared with six algorithms which are GA [2], PSO [9], SA [8], VNS [10], ABC [11] and MOACO [7]. Table 1 lists the typical results of above algorithms. Six Pareto optimal solutions obtained by proposed algorithm are given in Figure 11.

According to Pareto dominance relationship, the solution by VNS dominates the results obtained by GA, PSO, SA, ABC and MOACO. From the Figure 11, the Pareto optimal solutions generated by improved algorithm can cover or surpass the current known best solutions and find more feasible solutions that the disassembly line designer can make their own decision.

From Table 3 it is clear that the minimum number of workstations in above methods is 9, the balance measure is also 9, the minimal value for the hazard measure is 76 and the minimal value for the demand measure is 825. From the (a–f) in the Figure 11, the minimal value of workstations and balance measure are 9 respectively, the minimal value of the hazard measure is 72 and the minimal value of the demand measure is 812. The average values of all non-dominated solutions found by improved algorithm are higher than above values except for the \( f_i \), this illustrates the conflict
relationships among the objectives. Based on the above analysis, the improved algorithm has good comprehensive performance with respect to actual engineering application condition of DLBP and solution quality.

Table 3. Comparison of the typical results for 25-part DLBP example.

<table>
<thead>
<tr>
<th>Publication</th>
<th>Method</th>
<th>( f_1 )</th>
<th>( f_2 )</th>
<th>( f_3 )</th>
<th>( f_4 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kalayci et al. 2014 [10]</td>
<td>VNS</td>
<td>9</td>
<td>9</td>
<td>76</td>
<td>825</td>
</tr>
<tr>
<td>Ding et al. 2010 [7]</td>
<td>MOACO</td>
<td>No.1</td>
<td>9</td>
<td>9</td>
<td>87</td>
</tr>
<tr>
<td></td>
<td></td>
<td>No.2</td>
<td>9</td>
<td>11</td>
<td>85</td>
</tr>
</tbody>
</table>

For comparison purposes, seven algorithms are executed 30 times for 25-part DLBP example under the same system configurations. The values of average, standard deviation and confidence interval within 90% for each objective are given in Table 4. The detailed results are demonstrated in Figure 12.

Table 4. Performance comparison of seven algorithms for 25-part disassembly.

<table>
<thead>
<tr>
<th>Objective</th>
<th>Method</th>
<th>Average</th>
<th>Standard Deviation</th>
<th>Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>( f_1 )</td>
<td>GA</td>
<td>15.22</td>
<td>1.34</td>
<td>14.82</td>
</tr>
<tr>
<td></td>
<td>PSO</td>
<td>11.74</td>
<td>1.64</td>
<td>11.25</td>
</tr>
<tr>
<td></td>
<td>SA</td>
<td>12.37</td>
<td>1.01</td>
<td>12.07</td>
</tr>
<tr>
<td></td>
<td>VNS</td>
<td>10.63</td>
<td>1.56</td>
<td>10.16</td>
</tr>
<tr>
<td></td>
<td>ABC</td>
<td>12.9</td>
<td>1.52</td>
<td>12.44</td>
</tr>
<tr>
<td></td>
<td>MOACO</td>
<td>12.26</td>
<td>2.07</td>
<td>11.64</td>
</tr>
<tr>
<td>entropy-based AHPSO</td>
<td>10.32</td>
<td>1.72</td>
<td>9.80</td>
<td>10.84</td>
</tr>
<tr>
<td>( f_2 )</td>
<td>GA</td>
<td>16.51</td>
<td>1.98</td>
<td>15.92</td>
</tr>
<tr>
<td></td>
<td>PSO</td>
<td>14.94</td>
<td>1.43</td>
<td>14.51</td>
</tr>
<tr>
<td></td>
<td>SA</td>
<td>15.37</td>
<td>1.87</td>
<td>14.81</td>
</tr>
<tr>
<td></td>
<td>VNS</td>
<td>13.12</td>
<td>1.64</td>
<td>12.63</td>
</tr>
<tr>
<td></td>
<td>ABC</td>
<td>14.82</td>
<td>1.34</td>
<td>14.42</td>
</tr>
<tr>
<td></td>
<td>MOACO</td>
<td>15.32</td>
<td>1.55</td>
<td>14.85</td>
</tr>
<tr>
<td>entropy-based AHPSO</td>
<td>12.74</td>
<td>1.89</td>
<td>12.17</td>
<td>13.30</td>
</tr>
<tr>
<td>( f_3 )</td>
<td>GA</td>
<td>83.46</td>
<td>2.37</td>
<td>82.75</td>
</tr>
<tr>
<td></td>
<td>PSO</td>
<td>82.27</td>
<td>1.98</td>
<td>81.68</td>
</tr>
<tr>
<td></td>
<td>SA</td>
<td>82.53</td>
<td>3.35</td>
<td>81.52</td>
</tr>
<tr>
<td></td>
<td>VNS</td>
<td>78.55</td>
<td>1.93</td>
<td>77.97</td>
</tr>
<tr>
<td></td>
<td>ABC</td>
<td>82.15</td>
<td>2.30</td>
<td>81.46</td>
</tr>
<tr>
<td></td>
<td>MOACO</td>
<td>89.83</td>
<td>0.93</td>
<td>89.55</td>
</tr>
<tr>
<td>entropy-based AHPSO</td>
<td>74.2</td>
<td>2.31</td>
<td>73.51</td>
<td>74.89</td>
</tr>
<tr>
<td>( f_4 )</td>
<td>GA</td>
<td>934.64</td>
<td>6.72</td>
<td>932.62</td>
</tr>
<tr>
<td></td>
<td>PSO</td>
<td>932.81</td>
<td>5.38</td>
<td>931.19</td>
</tr>
<tr>
<td></td>
<td>SA</td>
<td>970.35</td>
<td>10.54</td>
<td>967.18</td>
</tr>
<tr>
<td></td>
<td>VNS</td>
<td>856.29</td>
<td>4.87</td>
<td>854.83</td>
</tr>
<tr>
<td></td>
<td>ABC</td>
<td>929.43</td>
<td>5.09</td>
<td>927.90</td>
</tr>
<tr>
<td></td>
<td>MOACO</td>
<td>978.67</td>
<td>15.02</td>
<td>974.16</td>
</tr>
<tr>
<td>entropy-based AHPSO</td>
<td>843.82</td>
<td>5.96</td>
<td>842.03</td>
<td>845.61</td>
</tr>
</tbody>
</table>
Although the seven algorithms can get the optimal solutions, the entropy-based AHPSO and VNS are able to reach better results than others algorithms from the overall comprehensive analysis of Figure 12. And in terms of all objectives, the performance of the entropy-based AHPSO is better than the VNS, especially about the objective 3 and objective 4 (see Figure 12c,d). As can be seen in Figure 12a,b, the performance of GA is worst when compare with other algorithms, and the performances of PSO, SA, ABS and MOACO are not significantly different. However, in terms of objective 4 (see Figure 12d), the values of confidence interval within 90% have obvious distinction.

With the above analysis, we can get the entropy-based AHPSO has high stability and accuracy feature.

6. Conclusions

This paper expands the application fields of entropy and an efficient improved algorithm that entropy-based AHPSO is presented for solving DLBP. According to the characteristic of the disassembly sequence, the entropy is introduced into the proposed algorithm to measure the changing tendency of population diversity, particle with good diversity based on the entropy is selected to be added the velocity equation. In addition, the crossover and mutation factor change with the value of entropy. The computational results of the proposed algorithm for a set of benchmark instances and a practical disassembly example are compared with the typical algorithms, which show that the improved algorithm is well suited to the multi-criteria decision making problem and complicated combinatorial optimization problem. As future research directions, the AHPSO with entropy may be improved in terms of effectively constructing the initial solutions and dividing the particle dimensions into several groups by analyzing the relations among disassembly tasks.

Acknowledgments: This project is supported by the National Natural Science Fund of China (Grant No. 61403249) and Shanghai University of Engineering Science (Grand No. E309031601178).
Author Contributions: Shanli Xiao and Yujia Wang conceived and designed the entropy-based AHPSO algorithm; Shanli Xiao and Shankun Nie performed the experiments; Hui Yu and Shankun Nie analyzed the data; Shanli Xiao and Yujia Wang wrote the paper; Finally, Yujia Wang guided to modify and Shanli Xiao revised the paper. All authors have read and approved the final manuscript.

Conflicts of Interest: The authors declare no conflict of interest.

References


© 2017 by the authors. Submitted for possible open access publication under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).