Projective Exponential Synchronization for a Class of Complex PDDE Networks with Multiple Time Delays

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Abstract: This paper addresses the problem of projective exponential synchronization for a class of complex spatiotemporal networks with multiple time delays satisfying the homogeneous Neumann boundary conditions, where the network is modeled by coupled partial differential-difference equations (PDDEs). A distributed proportional-spatial derivative (P-sD) controller is designed by employing Lyapunov’s direct method and Kronecker product. The controller ensures the projective exponential synchronization of the PDDE network. The main result of this paper is presented in terms of standard linear matrix inequality (LMI). A numerical example is provided to show the effectiveness of the proposed design method.

Keywords: spatiotemporal behavior; partial differential-difference equation; projective exponential synchronization; linear matrix inequality
1. Introduction

Complex networks have extensive promising applications in many areas, including signal processing, moving image processing, speed detection of moving subjects, logistics networks, EPC system networks, associative memories, etc. This has inspired many researchers to study the problems presented by complex networks (see [1–4] and the references cited therein).

Among them, various synchronizations of complex networks have especially attracted researchers’ attention in the past few decades [5–7]. For example, cluster synchronization, pinning synchronization, projective synchronization, impulsive synchronization, adaptive synchronization, and many other outstanding research works have been presented (e.g., [8–11]). Among all kinds of synchronization schemes, projective synchronization is the best known one because of its wide use in signal processing [12–14].

Time delays are inevitable in the real applications of complex networks. Time delays may cause bifurcation, oscillation, divergence or instability of complex networks [15–17]. Thus, it is extremely important to study the dynamics of complex networks considering time delays, which has become a hotly discussed issue in the area of complex networks studies [18–23]. In addition, a kind of complex networks called complex spatiotemporal networks (e.g., biological systems [24]) have also attracted researchers’ attention in the past few years. The outputs, inputs, and process states and relevant parameters of this kind of complex networks may vary temporally and spatially. Complex spatiotemporal networks can usually be modeled by coupled partial differential equations (PDEs). Recently, many outstanding research works have been carried out on the synchronization of complex spatiotemporal networks recently [22–35].

It is worth mentioning that the model of complex networks with time delays is expressed by coupled partial differential-difference equations (PDDEs). Compared to the complex PDE networks themselves, the dynamics of complex PDDE networks are more difficult to analyze. Up to now, few results are available on the projective exponential synchronization of complex PDDE networks with multiple time delays. This is a very challenging problem, which motivates our study presented in this paper.

The objective of this paper is thus to address the problem of projective exponential synchronization for a class of complex PDDE networks with multiple time delays satisfying the homogeneous Neumann boundary conditions. In order to achieve the projective exponential synchronization of complex PDDE networks, a distributed proportional-spatial derivative (P-sD) controller is designed by using the Lyapunov direct method. The solution of the projective exponential synchronization problem then reduces to the feasibility of a linear matrix inequality (LMI). Moreover, a numerical simulation is provided to illustrate the effectiveness of the proposed synchronization criteria.

The remainder of this paper is organized as follows: the problem formulation and preliminaries are given in the next section. Section 3 studies a distributed P-sD state feedback controller design for projective exponential synchronization of a complex PDDE network with multiple time delays in terms of LMI. Section 4 presents an example to illustrate the effectiveness of the proposed method and Section 5 offers the conclusions.
1.1. Notations

The following notations will be used in what follows. $\mathbb{R}$, $\mathbb{R}^n$ and $\mathbb{R}^{m \times n}$ denote the set of all real numbers, $n$-dimensional Euclidean space and the set of all $m \times n$ matrices, respectively. $\mathcal{N}$ is the set of nodes. $\otimes$ is the Kronecker product for matrices. The identity matrix with appropriate dimensions is denoted by $I$. For a symmetric matrix $M$, $0 > M$ and $0 < M$ respectively stands for $M$ is positive definite and negative definite.

The superscript “$T$” is used for the transpose of a vector or a matrix. The symbol “$*$” is used as an ellipsis in matrix expressions that are induced by symmetry, e.g.,

$$\begin{bmatrix} R + [M + N + \ast] & X \\ Y & \ast \end{bmatrix} \triangleq \begin{bmatrix} R + [M + N + M^T + N^T] & X \\ X^T & Y \end{bmatrix}.$$

2. Preliminaries and Problem Formulation

Consider a class of complex PDDE networks with multiple time delays of the following form:

$$\begin{cases} y_i(t) = \Theta_{i,1} y_i(t) + \Theta_{i,2} y_i(t - \tau_i) + \Theta_{i,3} y_i(t - \tau_2) + Ay_i(t) \\ + A_j y_j(t - \tau_j) + c \sum_{j=1}^{N} g_{ij} y_j(t) + Bu_i(t), (t, x_i) \in [0, L] \times [0, \tau) \end{cases}, \quad (1)$$

where $\mathcal{N} \triangleq \{1, 2, \ldots, N\}$ is the set of nodes. $y_i(t) \in \mathbb{R}^n$ and $u_i(t) \in \mathbb{R}^m$, $i \in \mathcal{N}$, are the state and distributed control input of the $i$-th node, respectively. $\Theta_{i,1} \in \mathbb{R}^{n \times n}$, $\Theta_{i,2} \in \mathbb{R}^{n \times n}$, $A \in \mathbb{R}^{n \times n}$, $B \in \mathbb{R}^{n \times m}$ are known matrices. $\tau_i > 0$, $\tau_2 > 0$, $\tau_2 > 0$ are time delays in the network and $\tau \triangleq \max\{\tau_1, \tau_2, \tau_3\}$ denotes the largest time delay throughout the paper. $x \in [0, L] \subset \mathbb{R}$ and $t \in [0, \tau)$ are the spatial position and time, respectively. $\phi(x, t), \ t \in [-\tau, 0], \ i \in \mathcal{N}$, is the initial value of the $i$-th node. $c$ is a known scalar describing the coupling strength. $G = (g_{ij})_{N \times N}$, $i, j \in \mathcal{N}$, is the coupling configuration matrix representing the topological structure of the network defined to be diffusive, where $g_{ij} > 0 (i \neq j)$, $g_{ii} = -\sum_{j=1, j \neq i}^{N} g_{ij}$. The coupling matrix $G$ is not required to be symmetric or irreducible.

Assume that there is an isolated node $s(x, t)$ satisfying:

$$\begin{cases} s_i(t) = \Theta_{1,1} s_i(t) + \Theta_{1,2} s_i(t - \tau_i) + \Theta_{1,3} s_i(t - \tau_2) + As_i(t) \\ + A_j s_j(t - \tau_j), (t, x_i) \in [0, L] \times [0, \tau) \end{cases}, \quad (2)$$

This paper aims to design a controller to make the complex PDDE network of Equation (1) proportionally synchronize onto the desired state of Equation (2). In order to investigate the projective synchronization of the complex PDDE network, the stability of the zero solution of the error system needs to be studied. Define the synchronization error of the $i$-th node to be:

$$e_i(t) \triangleq y_i(t) + \alpha s_i(t), \quad (3)$$
where $\alpha$ is a desired scaling factor. Thus, it is not difficult to get the synchronization error system of the complex PDDE network as:

$$
e_{i,t}(x,t) = \Theta_{i,t} e_{i,t}(x,t) + \Theta_{i,t} e_{i,t}(x,t) + \Theta_{i,t} e_{i,t}(x,t) + A e_{i,t}(x,t)$$

$$+ A e_{i,t}(x,t) + c \sum_{j=1}^{N} g_{ij} e_{j}(x,t) + B u_{i}(x,t), (x,t) \in [0,L] \times [0, +\infty)$$

$$(4)$$

where $e_{i,0}(x) = y_{i,0}(x) + \alpha x_{i}(x).$

To achieve the synchronization of the complex PDDE network of Equation (1), we consider a distributed P-sD feedback controller:

$$u_{i}(x,t) = K_{1} e_{i,t}(x,t) + K_{2} e_{i,t}(x,t), \quad i \in \mathbb{N},$$

where $K_{1}$ and $K_{2}$ are real $m \times n$ matrices to be determined. It has been pointed out in [32,34–37] that the controller of Equation (9) can provide more convenient spatial performance. The signal $e_{i,t}(x,t)$ in the controller of Equation (9) can be obtained via the finite difference method. Substituting Equation (9) into Equation (8) yields the closed-loop synchronization error system of the complex PDDE network:

$$e_{i,t}(x,t) = \Theta_{i,t} e_{i,t}(x,t) + \Theta_{i,t} e_{i,t}(x,t) + \Theta_{i,t} e_{i,t}(x,t) + (A + BK_{1}) e_{i,t}(x,t)$$

$$+ A e_{i,t}(x,t) + c \sum_{j=1}^{N} g_{ij} e_{j}(x,t) + B K_{2} e_{i,t}(x,t), (x,t) \in [0,L] \times [0, +\infty)$$

$$(6)$$

Hence, the aim of this paper is to design $K_{1}$ and $K_{2}$ for Equation (6) such that the complex PDDE network of Equation (1) exponentially synchronizes the trajectory of Equation (2). To this end, we firstly introduce the following definition of projective exponential synchronization. The definition is useful for the sequel analysis and design.

**Definition 1.** Given a constant $\rho > 0$, the complex PDDE systems of Equation (1) are said to be projective exponentially synchronized, if there exists a constant $\sigma > 0$ such that the following inequality holds:

$$\|e(\cdot,t)\|_{e}^{2} \leq \sigma \exp(-2\rho t) \|e_{0}\|_{e}^{2}, \quad \forall t \geq 0.$$  

(7)
3. Distributed P-sD State Feedback Control Design for Projective Exponential Synchronization

By using Lyapunov’s direct method, this section will present an LMI-based sufficient condition on the projective exponential synchronization of the complex PDDE network of Equation (1). First, we consider a Lyapunov functional for the closed-loop synchronization error system of Equation (6):

$$V(t) = \sum_{i=1}^{N} \int_{t_i-\tau_i}^{t_i} e_{i,x}^T(x, \rho) R_i e_{i,x}(x, \rho) d \rho dx$$

$$+ \sum_{i=1}^{N} \int_{t_i-\tau_i}^{t_i} e_{i,x}^T(x, \rho) R_i e_{i,x}(x, \rho) d \rho dx$$

$$+ \sum_{i=1}^{N} \int_{t_i-\tau_i}^{t_i} e_{i,x}^T(x, \rho) R_i e_{i,x}(x, \rho) d \rho dx$$

where $P > 0$, $R_k > 0$, $k \in \{1, 2, 3\}$ are real symmetric $n \times n$ matrices to be determined. Based on the property of the Kronecker product for matrices and integrating by parts, a simple calculation gives the time derivative of $V(t)$ that:

$$\dot{V}(t) = -\int_{0}^{\tau} e_{i,x}^T(x, \tau) [I_N \otimes P \Theta_1 + *] e_{i,x}(x, \tau) d\tau - \int_{0}^{\tau} e_{i,x}^T(x, t) [I_N \otimes P \Theta_{1d} + *] e_{i,x}(x, t - \tau) dt$$

$$+ 2 \int_{0}^{\tau} e_{i,x}^T(x, t) (I_N \otimes P \Theta_2) e_{i,x}(x, t) dt + 2 \int_{0}^{\tau} e_{i,x}^T(x, t) (I_N \otimes P \Theta_{2d}) e_{i,x}(x, t - \tau) dt$$

$$+ \int_{0}^{\tau} e_{i,x}^T(x, t) [(I_N \otimes PA + PBK_1) + *] e_{i,x}(x, t) dt + \int_{0}^{\tau} e_{i,x}^T(x, t) (I_N \otimes PA_d) e_{i,x}(x, t - \tau) dt$$

$$+ \int_{0}^{\tau} e_{i,x}^T(x, t) [G \otimes P + *] e_{i,x}(x, t) dt + \int_{0}^{\tau} e_{i,x}^T(x, t) (I_N \otimes R_1) e_{i,x}(x, t) dt$$

$$- \int_{0}^{\tau} e_{i,x}^T(x, t - \tau) (I_N \otimes R_1) e_{i,x}(x, t - \tau) dt + \int_{0}^{\tau} e_{i,x}^T(x, t - \tau) (I_N \otimes R_2) e_{i,x}(x, t) dt$$

$$- \int_{0}^{\tau} e_{i,x}^T(x, t - \tau_2) (I_N \otimes R_2) e_{i,x}(x, t) dt + \int_{0}^{\tau} e_{i,x}^T(x, t - \tau_3) (I_N \otimes R_3) e_{i,x}(x, t) dt$$

$$= \int_{0}^{\tau} \bar{e}(x, t) \Psi \bar{e}(x, t) dt$$

where:

$$\bar{e}(x, t) \triangleq [e_{i,x}^T(x, t) e_{i,x}^T(x, t - \tau) e_{i,x}^T(x, t - \tau_2) e_{i,x}^T(x, t - \tau_3)]^T,$$

$$e(x, t) \triangleq [e_{1,x}^T(x, t) e_{2,x}^T(x, t) \cdots e_{N,x}^T(x, t)]^T \in \mathbb{R}^{nN},$$

$$\Psi \triangleq \begin{bmatrix}
P_{11} & I_N \otimes (P \Theta_2 + PBK_2) & 0 & I_N \otimes P \Theta_{1d} & I_N \otimes PA_d \\
* & P_{22} & I_N \otimes P \Theta_{1d} & 0 & 0 \\
* & * & -I_N \otimes R_1 & 0 & 0 \\
* & * & * & -I_N \otimes R_2 & 0 \\
* & * & * & * & -I_N \otimes R_3
\end{bmatrix},$$

in which:

$$P_{11} \triangleq I_N \otimes [PA + PBK_1 + *] + I_N \otimes R_1 + c[G \otimes P + *],$$

$$P_{22} \triangleq -I_N \otimes [P \Theta_1 + *] + I_N \otimes R_1 + I_N \otimes R_2.$$
Theorem 1. Consider the complex PDDE network of Equation (1). For a given scalar $\rho > 0$, there exists a distributed controller with the form of Equation (5) such that the network of Equation (1) achieves projective exponential synchronization, if there exist $n \times n$ symmetric matrices $Q > 0$, $S_1 > 0$, $S_2 > 0$, $S_3 > 0$, and $m \times n$ matrices $Y_1$, $Y_2$ satisfying the following LMI:

$$
\Xi \triangleq \left[ \begin{array}{cccc}
\Xi_{11} & I_N \otimes (\Theta_2 Q + BY_2) & 0 & I_N \otimes A_1 Q \\
* & \Xi_{22} & I_N \otimes \Theta_{2d} Q & 0 \\
* & * & -I_N \otimes S_1 & 0 \\
* & * & * & -I_N \otimes S_2 \\
* & * & * & * & -I_N \otimes S_3 \\
\end{array} \right] > 0,
$$

where:

$$
\Xi_{11} \triangleq I_N \otimes [AQ + BY_1 + *] + I_N \otimes S_1 + c[G \otimes Q + *],
$$

$$
\Xi_{22} \triangleq -I_N \otimes [\Theta_1 Q + *] + I_N \otimes S_1 + I_N \otimes S_2.
$$

In this case, the control gain matrices $K_1$ and $K_2$ of the controller of Equation (5) are:

$$
K_1 = Y_1 Q^{-1} \quad \text{and} \quad K_2 = Y_2 Q^{-1}.
$$

Proof. Assume that LMI of Equation (11) is satisfied for $n \times n$ symmetric matrices $Q > 0$, $S_1 > 0$, $S_2 > 0$, $S_3 > 0$, and $m \times n$ matrices $Y_1$, $Y_2$. With application of Lemma 1, pre- and post-multiplying both sides of the matrix $\Xi$ by the block diagonal matrix $Q \triangleq \text{diag}(I_N \otimes Q^{-1}, I_N \otimes Q^{-1}, I_N \otimes Q^{-1}, I_N \otimes Q^{-1}, I_N \otimes Q^{-1})$, respectively, and letting:

$$
Q = P^{-1}, \quad Y_1 = K_1 Q, \quad Y_2 = K_2 Q, \quad Z = L Q, \quad S_1 = Q R_1 Q, \quad S_2 = Q R_2 Q, \quad S_3 = Q R_3 Q,
$$

we obtain:

$$
\Psi = Q \Xi Q.
$$

Since $Q > 0$, we can get from Equations (11) and (14) that:

$$
\Psi < 0.
$$

By virtue of the matrix theory and Equation (15), we can find an appropriate scalar $\rho \in \mathbb{R}^+$ such that:

$$
\Psi + \rho I \leq 0.
$$

It follows from Equation (16) that the inequality of Equation (9) can be rewritten as:

$$
\dot{V}(t) \leq -\rho \|\hat{e}(t)\|^2 \leq -\rho \|e(t)\|^2, \quad \text{for} \quad e(t) \neq 0.
$$

By using the technique exploited in [36], the inequality of Equation (17) tells us that the closed-loop PDDE system of Equation (1) is exponentially stable if LMI of Equation (11) is fulfilled. From Definition 1, the closed-loop synchronization error system of Equation (6) is exponentially stable, i.e., the PDDE Equation (1) achieves projective exponential synchronization with the isolated node of Equation (2). Moreover, Equation (13) gives the expression of Equation (12). The proof is complete. $\square$
On the basis of Lyapunov’s direct method and integration by parts, Theorem 1 presents an LMI-based sufficient condition on the existence of a distributed state feedback controller of Equation (5) for projective exponential synchronization of the complex PDDE network of Equation (1). The explicit control gain matrices of the desired controller is given as Equation (12) when LMI of Equation (10) is feasible.

Remark 1. The distributed P-sD controller is proposed for exponential stability of PDE systems in [37,38], while projective exponential synchronization of a complex PDDE network with multiple time delays and N identical nodes was studied via the distributed P-sD control.

Remark 2. This paper considers the problem of projective exponential synchronization of a network considering multiple time delays. It is different from those in [34,35], in which the exponential synchronization problem of complex networks without time delays was discussed only.

Remark 3. The complex PDDE network in this paper contains time delays $\tau_1$, $\tau_2$ and $\tau_3$ without coupling time delay. A more complex model with coupling time delay will be further studied in future. Moreover, it should be pointed out that the method in this paper can also be extended to the network with spatially variable parameters. This will also be left for our future work.

4. Simulation Study

In this section, a chemical reactor network with four nodes is used to show the effectiveness of the proposed theoretical results. Every chemical reactor is a network node modeled by the linearized FitzHugh-Nagumo (FHN) equation with coupling terms, where FHN equations have been extensively employed for wavy behavior in chemistry. This reactor network can be given as Equation (1) with the following parameters:

$$y_i(x,t) = [y_{i1}(x,t) \ y_{i2}(x,t)]^T,$$

$$\Theta_1 = \begin{bmatrix} 1 & 0 \\ 0 & 4 \end{bmatrix}, \ \Theta_{1d} = \begin{bmatrix} -0.5 & 0 \\ 0 & 0.5 \end{bmatrix}, \ \Theta_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \ \Theta_{2d} = \begin{bmatrix} -1 & 0 \\ 0 & 0.8 \end{bmatrix}, \ A = \begin{bmatrix} 2 & -0.2 \\ -1 & 3 \end{bmatrix},$$

$$A_y = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \ B = \begin{bmatrix} 0 \end{bmatrix}, \ c = 1, \ L = 20, \ \tau_1 = 1, \ \tau_2 = 1.5, \ \tau_3 = 2, \ \tau = \max\{\tau_1, \tau_2, \tau_3\} = 2, \ \gamma = \begin{bmatrix} -1.3592 & 0.3575 & 0.5155 & 0.4863 \\ -2.155 & 0.5622 & 0.3110 & -0.6576 \\ 0.4121 & -0.9363 & 0.9704 & -0.4462 \\ -0.9077 & -0.8057 & 0.6469 & 1.0665 \end{bmatrix}.$$ (18)

The initial conditions are given as:

$$\varphi(x,t) = \begin{bmatrix} 2\cos(\pi x/L + 2) + 2\sin^2(\pi t) \\ 2\cos(2\pi x/L) \end{bmatrix}, \ \varphi(x,t) = \begin{bmatrix} 3\cos(\pi x/L) \\ 2\cos(3\pi x/L + 2) - 3\sin^2(\pi t) \end{bmatrix},$$

$$\varphi(x,t) = \begin{bmatrix} 5\cos(2\pi x/L) + 4\sin(-3\pi t) \\ \cos^2(\pi x/L) \end{bmatrix}, \ \varphi(x,t) = \begin{bmatrix} 8\sin(0.5\pi x/L + \pi) \\ 2\cos(-5\pi x/L + 3\sin^2(2\pi t)) \end{bmatrix}.$$
s_0(x,t) = [0.2 \ 0.5]^T, \ t \in [-2,0]. \quad (19)

Figure 1 shows the open-loop profiles of evolution of y_i(x,t), i \in \{1,2,3,4\} for the complex PDDE network of Equation (1) with the parameters given in Equation (18) and the initial condition given in Equation (19). It is clear from Figure 1 that the nodes of the complex PDDE network are not synchronized.

![Figure 1. Open-loop profiles of evolution of y_i(x,t), i \in \{1,2,3,4\}.](image)

In this example, the controller of Equation (5) is employed, where \( K_1 \triangleq [k_{11} \ k_{12}] \), \( K_2 \triangleq [k_{21} \ k_{22}] \) are 1x2 matrices to be determined. Divide the spatial domain [0,20] into space instances \( \{x_k, k \in \{0,1,2,\cdots,100\}\}, x_0 = 0, x_{100} = 20 \) of the same distance, where \( x_k - x_{k-1} = 20/100 = 0.2 \). When setting \( \alpha = -1 \) and solving LMI of Equation (11), we get feasible solutions of \( Q > 0 \), \( S_1 > 0 \), \( S_2 > 0 \), \( S_3 > 0 \), and \( Y_1 \), \( Y_2 \). By using of Equation (12), we further get the control gain matrices as follows:

\[
K_1 \triangleq [-13.4733 \ 249.6802] \quad \text{and} \quad K_2 \triangleq [-0.9974 \ -0.2529]. \quad (20)
\]

Applying the controller of Equation (5) with the obtained control parameters \( K_1 \) and \( K_2 \) Equation (20) to the complex PDDE network of Equation (1) with the parameters given in Equation (18) and the initial condition given in Equation (19), the closed-loop error profiles of evolution of \( e_i(x,t), i \in \{1,2,3,4\} \) are shown in Figure 2. Obviously, the proposed control law of Equation (5) can guide the complex PDDE network to projective exponentially synchronize with the isolated node \( s(x,t) \). Moreover, Figure 3 shows the corresponding profiles of evolution of control inputs \( u_i(x,t), i \in \{1,2,3,4\} \).
Figure 2. Close-loop error profiles of evolution of $e_i(x,t), i \in \{1, 2, 3, 4\}$.

Figure 3. Profiles of evolution of control inputs $u_i(x,t), i \in \{1, 2, 3, 4\}$.

5. Conclusions

In this paper, we addressed the projective exponential synchronization problem of a class of complex PDDE networks. By using Lyapunov’s direct method and the technique of integration by parts, a sufficient condition on the existence of distributed P-sD controller achieving the projective exponential synchronization was developed in terms of LMI. The control gain parameters are easily obtained via feasible solutions to the given LMI. Finally, the effectiveness of the proposed theoretical result is illustrated by a numerical example. It should be noted that the method in this paper can be extended to the network with spatially variable parameters as well as coupling time delay. This will be our future research topic.
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Author Contributions

Chengdong Yang contributed the design of the study and manuscript preparation; Jianlong Qiu contributed to the conception of the study; Tongxing Li performed the data analyses; Ancai Zhang and Xiangyong Chen helped perform the discussion and language description of this paper. All authors have read and approved the final manuscript.

Conflicts of Interest

The authors declare that they have no competing interests.

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